Multiplying signed numbers

As a reminder, signed numbers are positive and negative numbers. When we multiply signed numbers, therefore, there are three possible combinations. We could be multiplying

- 1. Two positive numbers
- 2. Two negative numbers
- 3. One positive number and one negative number

For each of these combinations, let's talk about what happens when we multiply.

When we multiply two positive numbers, the result will always be positive.

$$3 \times 4 = 12$$

$$10 \times 1 = 10$$

When we multiply two negative numbers, the result will always be positive.

$$(-3) \times (-4) = 12$$

$$(-10) \times (-1) = 10$$

When we multiply a positive number by a negative number, the result will always be negative.

$$3 \times (-4) = -12$$

$$(-10) \times 1 = -10$$

Here's a summary of our findings:

	Positive × Positive	Positive
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In other words, if the signs are the same, the product will be positive. But if the signs are different, the product will be negative.

Even though 0 isn't a signed number, it's important to know that the result of multiplying any number by 0 is 0.

$$5 \times 0 = 0$$

$$0 \times -3 = 0$$

The result of a multiplication doesn't depend on the order of the numbers.

$$4 \times 5 = 20 = 5 \times 4$$

$$3 \times -2 = -6 = -2 \times 3$$

$$-5 \times 6 = -30 = 6 \times -5$$

$$-3 \times -7 = 21 = -7 \times -3$$

Up to now, we've usually used the times symbol \times to indicate multiplication. But as we go forward in math, we'll start to use the dot symbol \cdot more and more for multiplication. So 6×2 and $6 \cdot 2$ mean the same thing.

The dot is a little bit raised, so we won't confuse it with a decimal point. The reason we use this dot symbol is because it's easy to confuse \times with the variable x.

When you're multiplying negative numbers, it's good to get into the habit of enclosing negative numbers in parentheses, especially when the negative number is the second number, but all of these are acceptable:

$$6 \times -2 = -12$$

$$(-5) \cdot 3 = -15$$

$$(-7) \cdot (-4) = 28$$

$$(-8) \times (6) = -48$$

It's also acceptable to indicate multiplication using only parentheses, instead of the \times or \cdot symbols. You can put both numbers in parentheses. If you only put one number in parentheses, it should be the second one. All of these are good ways to express multiplication:

$$3(4) = 12$$

$$-2(5) = -10$$

$$(-7)(3) = -21$$

(-	-6)	(-7)	= 42

