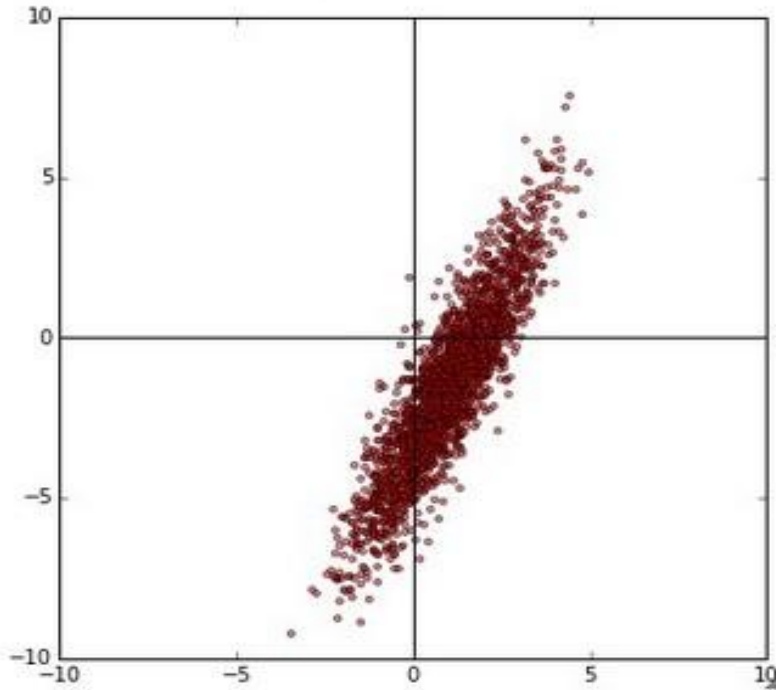
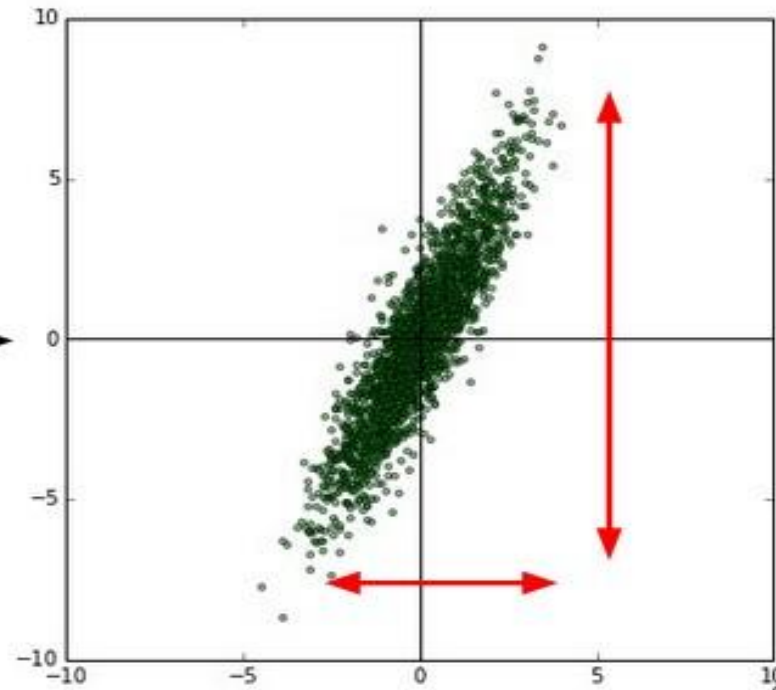


# Training Aspects of Neural Networks

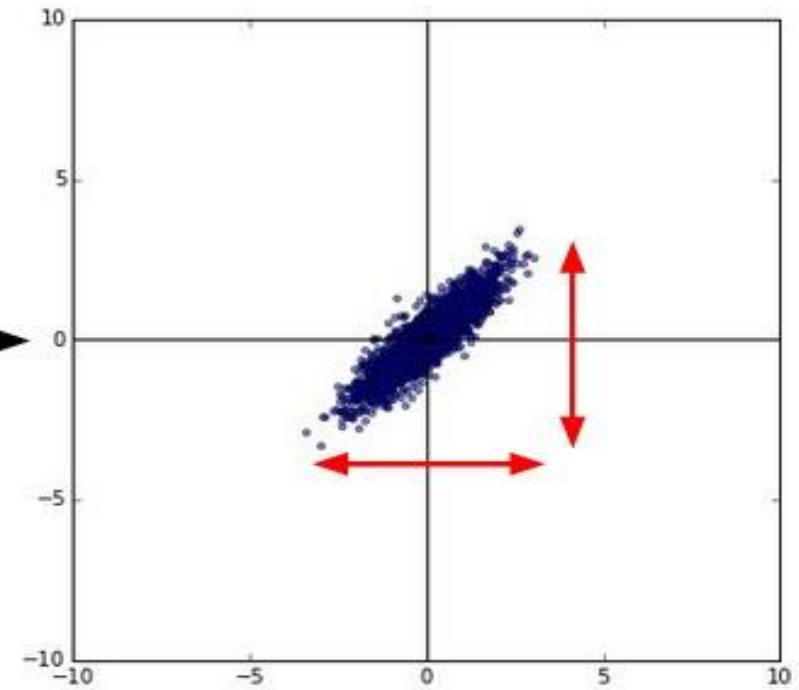
original data



zero-centered data



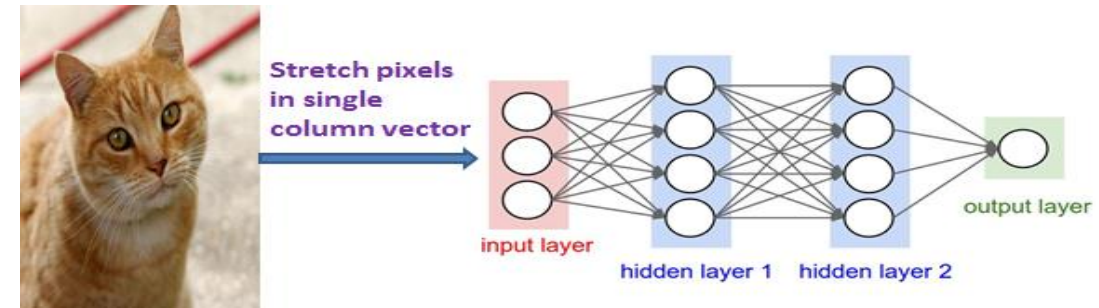
normalized data



# Previous Class

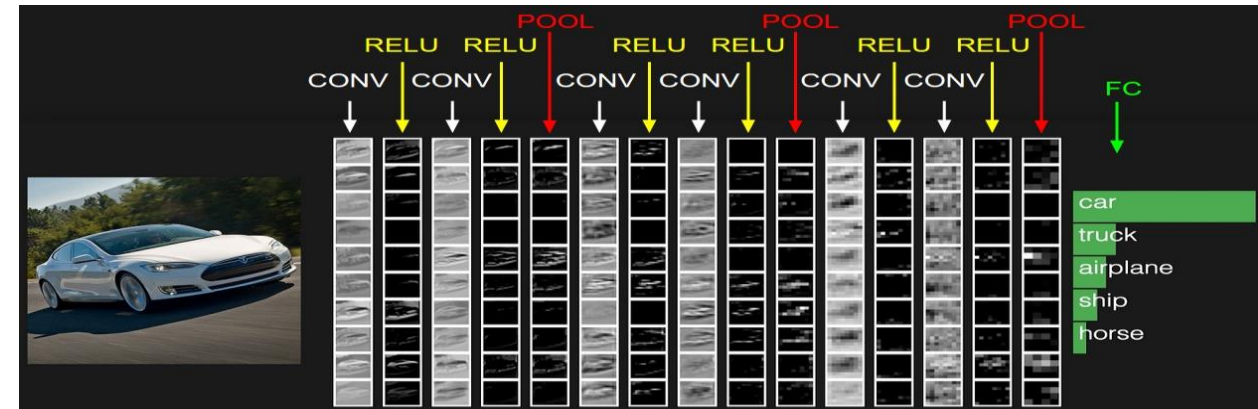
- Neural Network and Image

- Dimensionality
- Local relationship



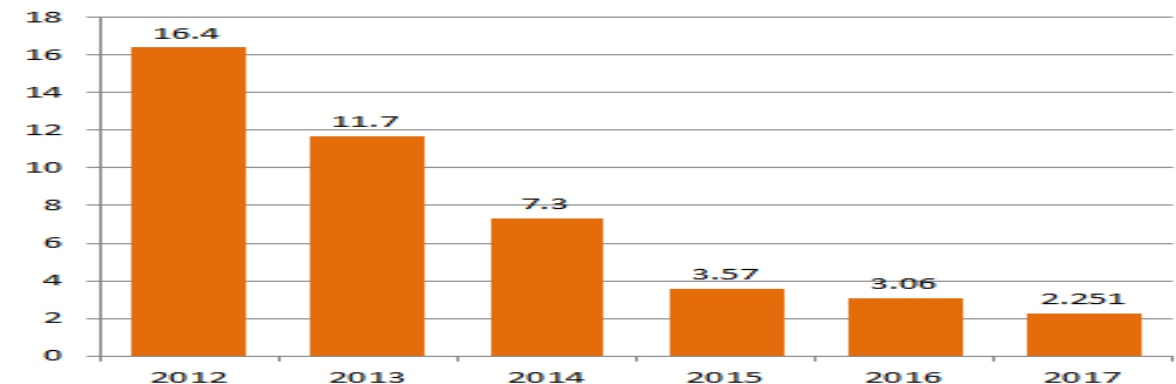
- Convolutional Neural Network (CNN)

- Convolution Layer
- Non-linearity Layer
- Pooling Layer
- Fully Connected Layer
- Classification Layer



- ImageNet Challenge

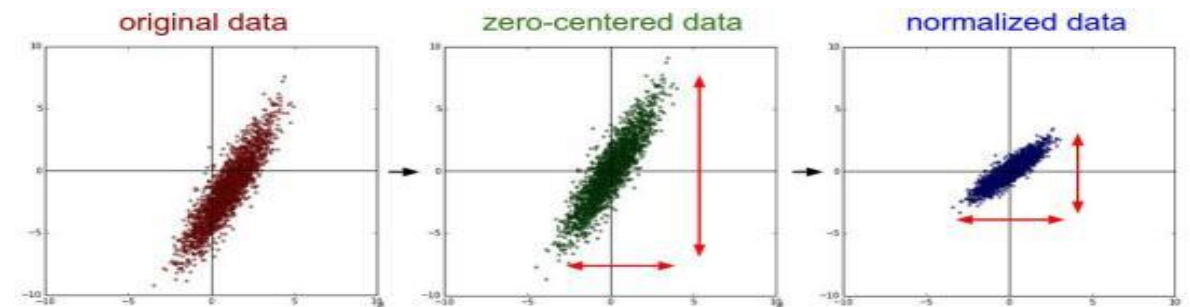
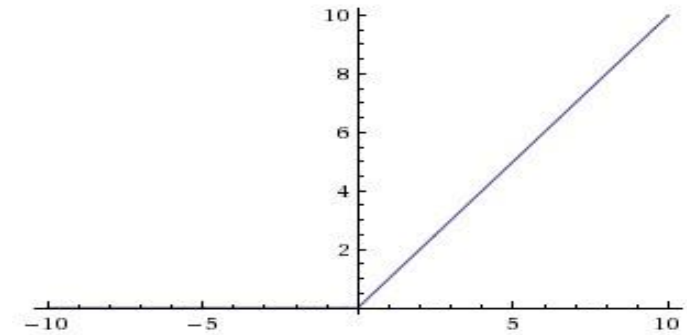
- Progress
- Human Level Performance



# This Class

## Training Aspects of CNN

- Activation Functions
- Dataset Preparation
- Data Preprocessing
- Weight Initialization



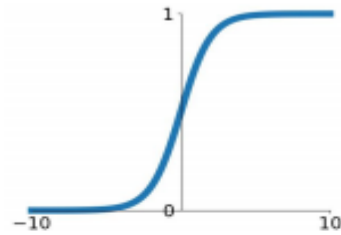
# Activation Functions

# Non-linearity Layer

## Activation Functions

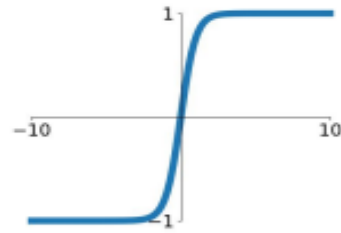
### Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



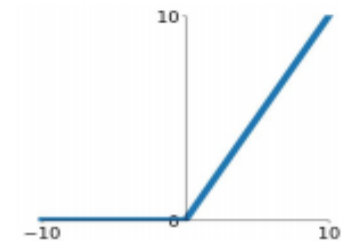
### tanh

$$\tanh(x)$$



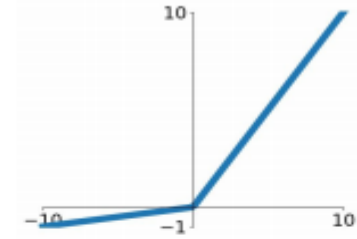
### ReLU

$$\max(0, x)$$



### Leaky ReLU

$$\max(0.1x, x)$$

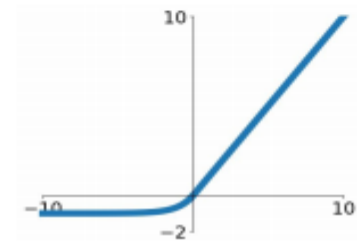


### Maxout

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

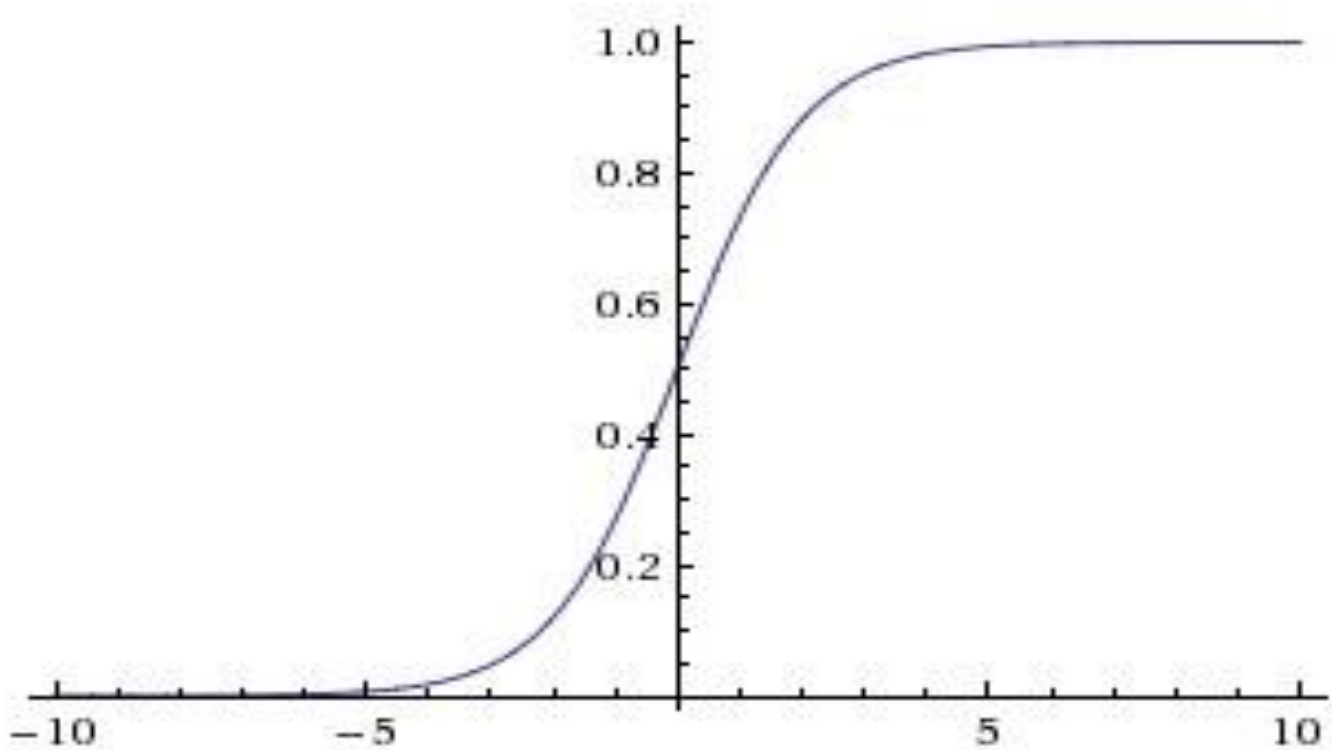
### ELU

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



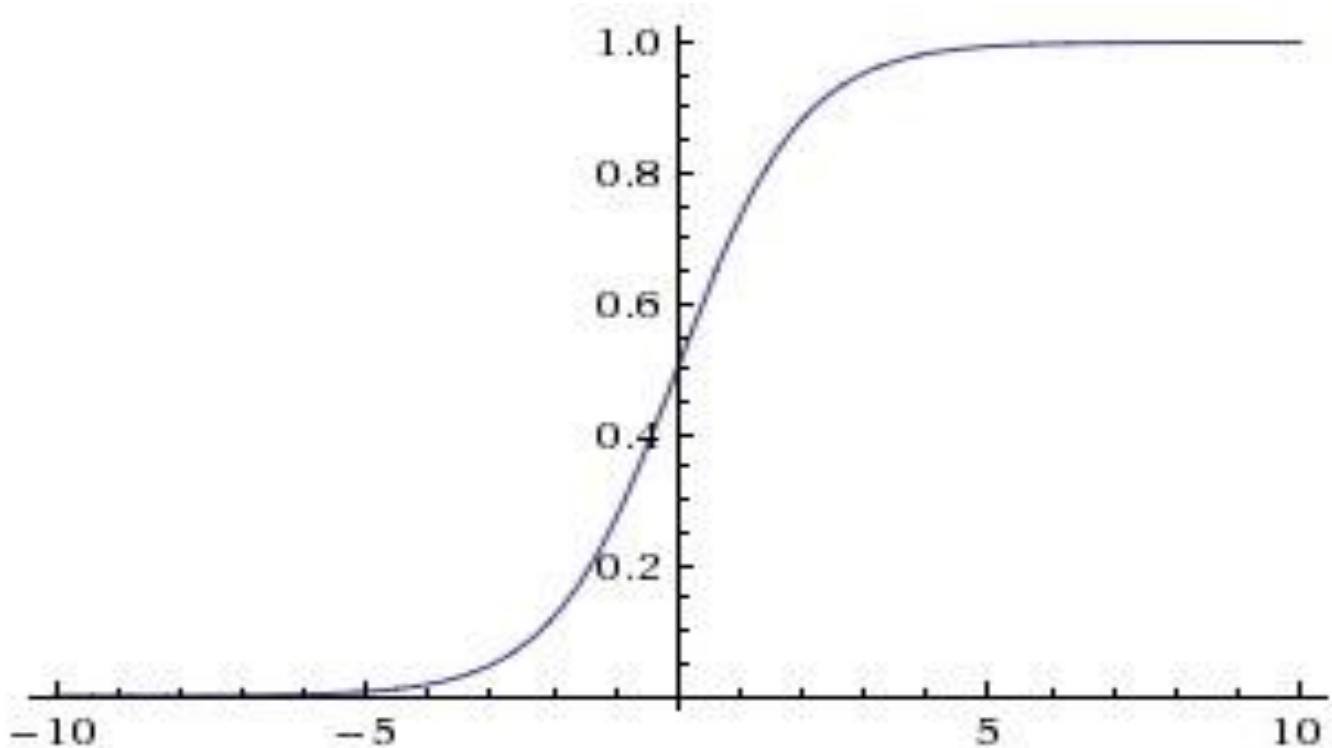
# Activation Functions: Sigmoid

$$\sigma(x) = 1/(1 + e^{-x})$$



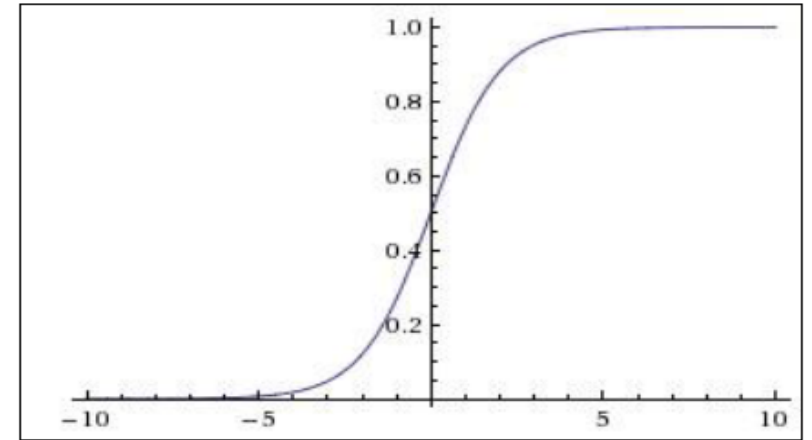
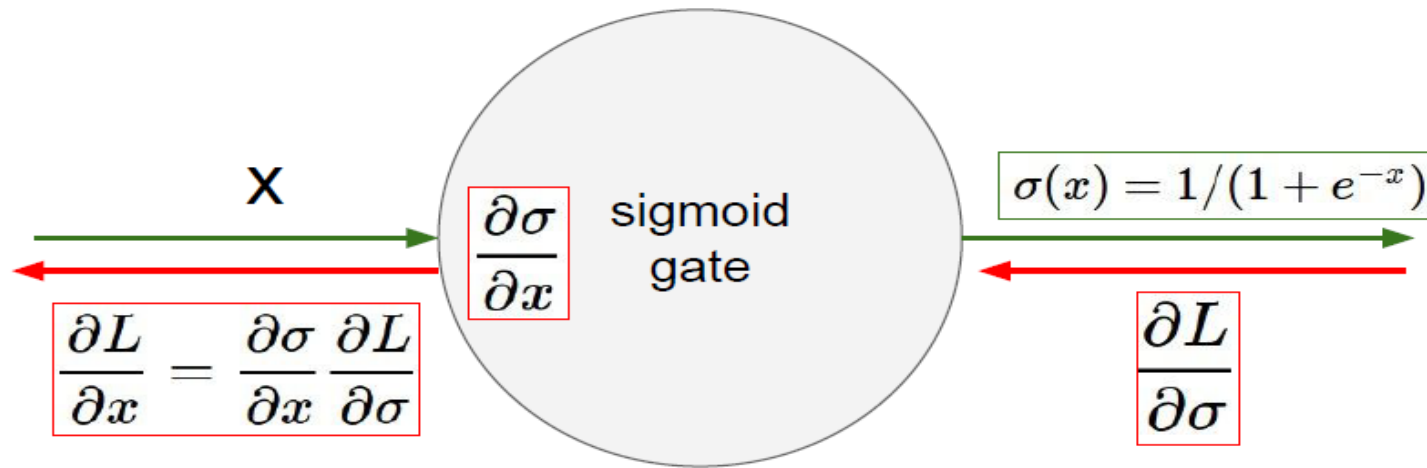
# Activation Functions: Sigmoid

$$\sigma(x) = 1/(1 + e^{-x})$$



- Sigmoids saturate and kill gradients.

# Activation Functions: Sigmoid



What happens when  $x = -10$ ?

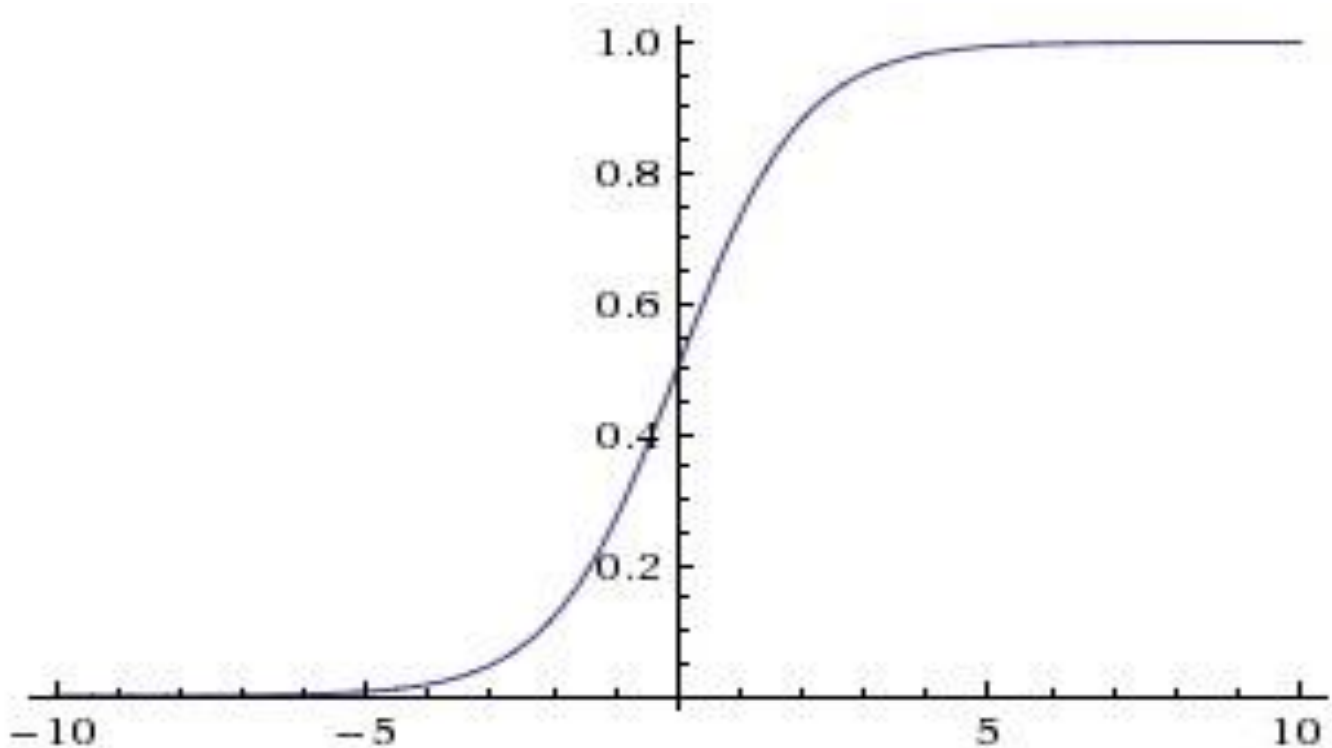
What happens when  $x = 0$ ?

What happens when  $x = 10$ ?



# Activation Functions: Sigmoid

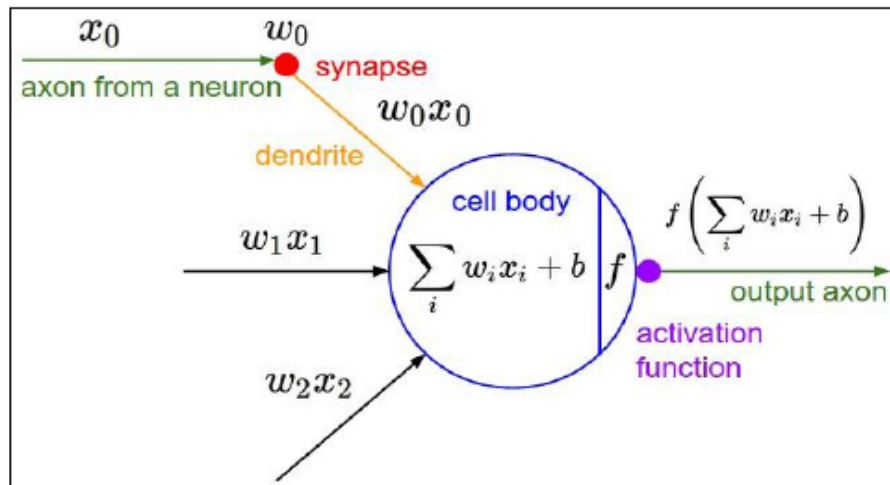
$$\sigma(x) = 1/(1 + e^{-x})$$



- Sigmoids saturate and kill gradients.
- Sigmoid outputs are not zero-centered.

# Activation Functions: Sigmoid

Consider what happens when the input to a neuron ( $x$ ) is always positive:

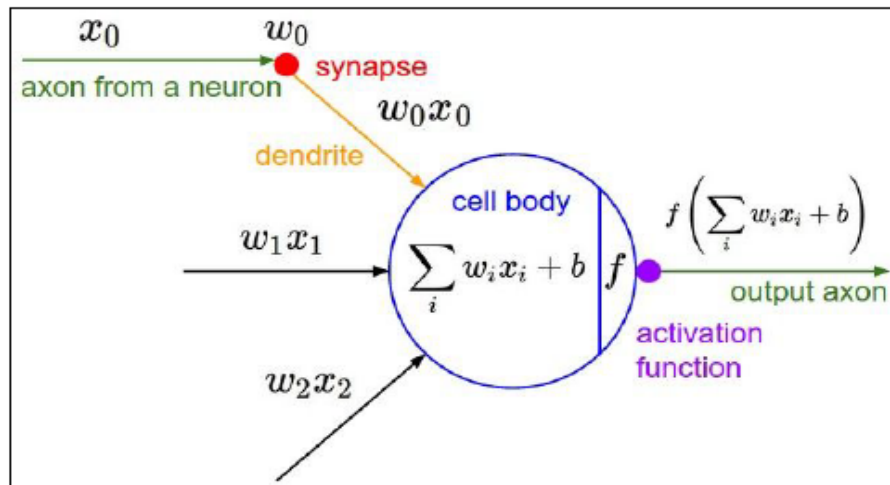


$$f\left(\sum_i w_i x_i + b\right)$$

What can we say about the gradients on  $\mathbf{w}$ ?

# Activation Functions: Sigmoid

Consider what happens when the input to a neuron ( $x$ ) is always positive:



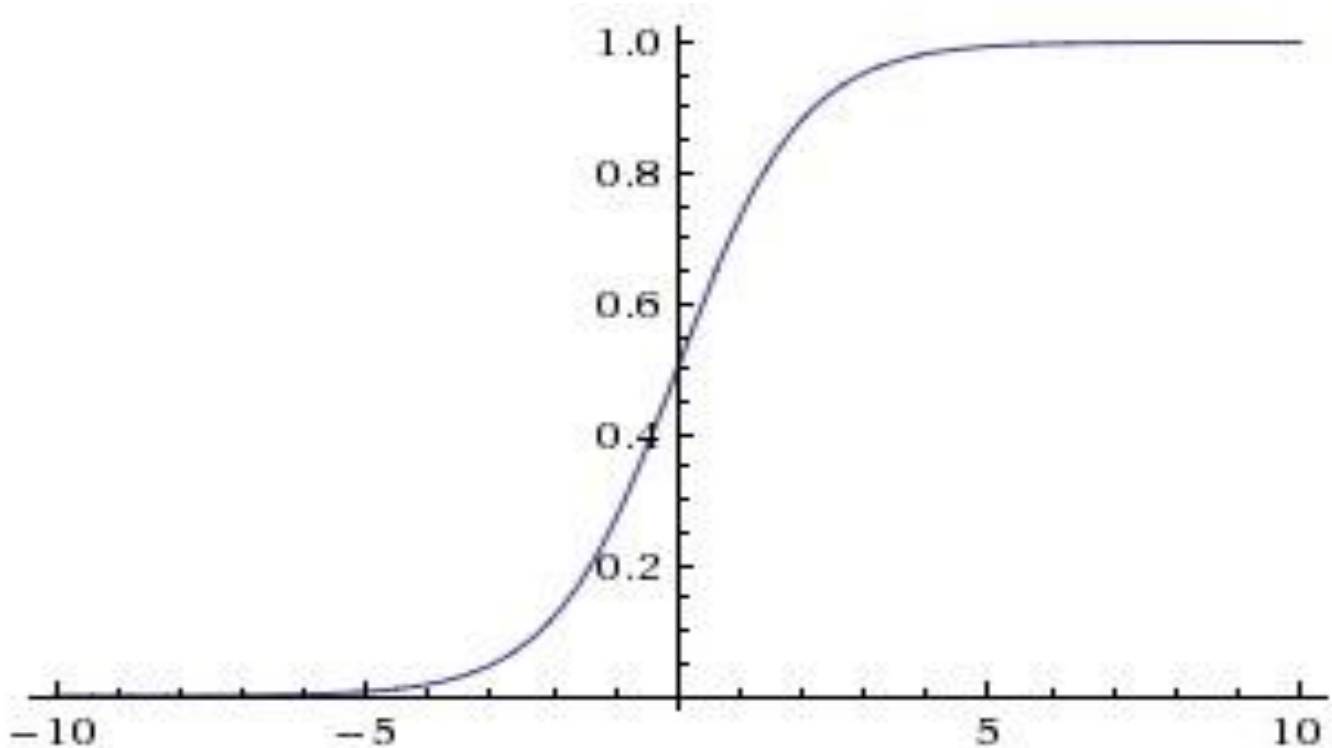
$$f\left(\sum_i w_i x_i + b\right)$$

What can we say about the gradients on  $\mathbf{w}$ ?

Always all positive or all negative  
(this is also why you want zero-mean data!)

# Activation Functions: Sigmoid

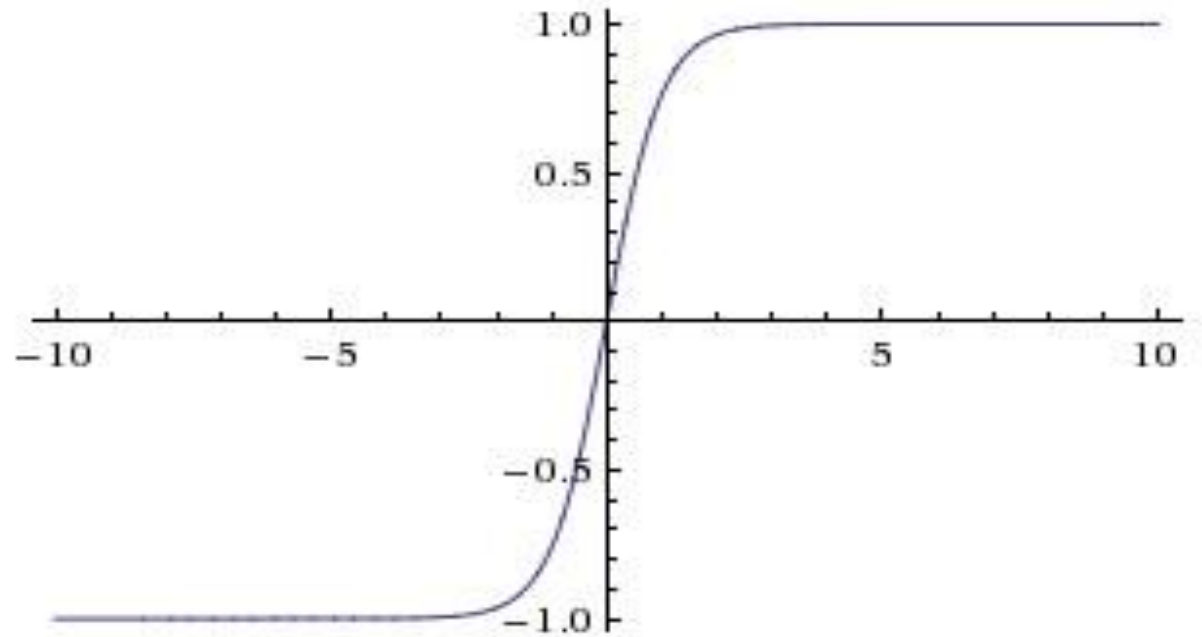
$$\sigma(x) = 1/(1 + e^{-x})$$



- Sigmoids saturate and kill gradients.
- Sigmoid outputs are not zero-centered.
- $\text{Exp}()$  is a bit compute expensive.

# Activation Functions: tanh

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$



[LeCun et al., 1991]

Source: <http://cs231n.github.io>

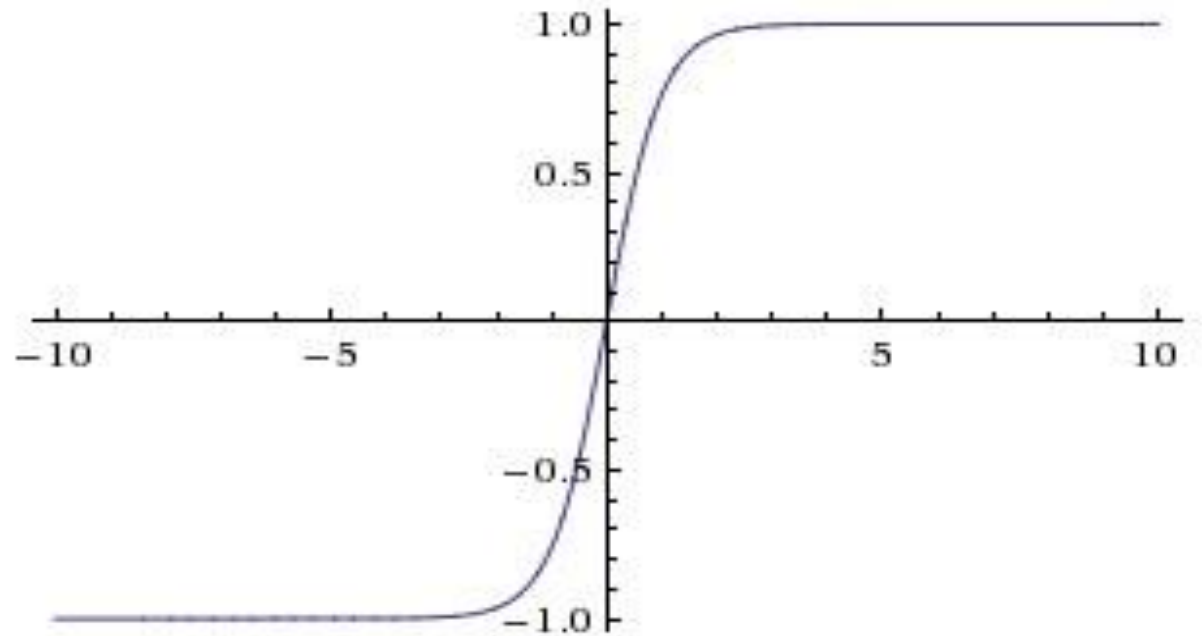
# Activation Functions: tanh

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

tanh neuron is simply a scaled sigmoid neuron

$$\tanh(x) = 2\sigma(2x) - 1.$$

↑  
Sigmoid



[LeCun et al., 1991]

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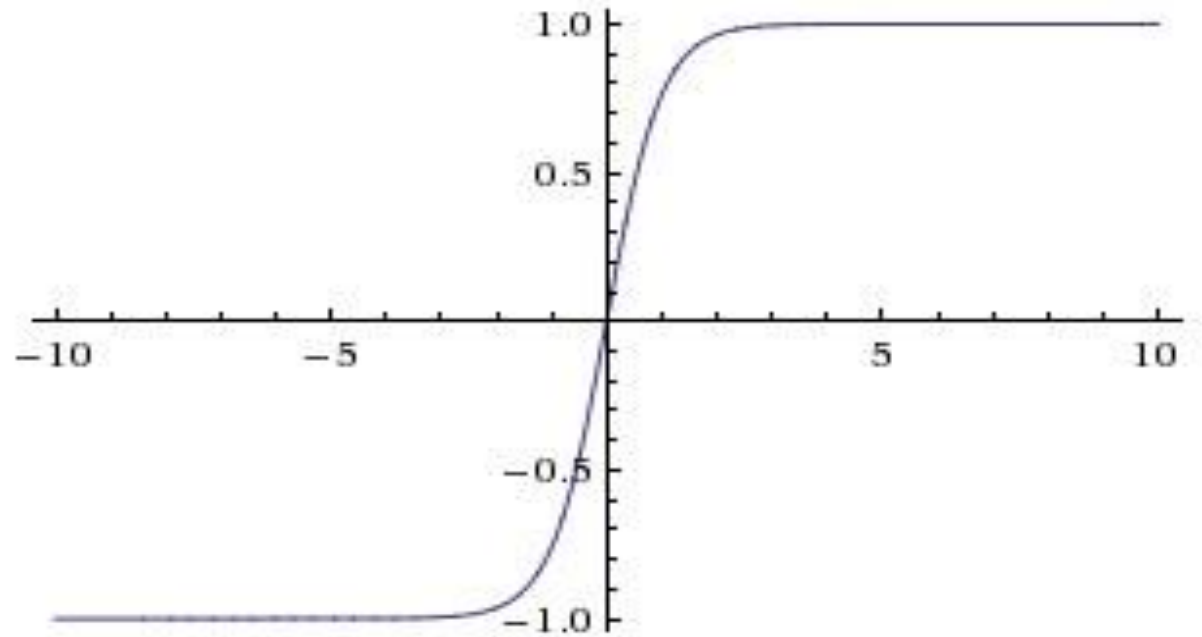
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↑  
Sigmoid



Like the sigmoid neuron, its activations saturate.

Unlike the sigmoid neuron its output is zero-centered.

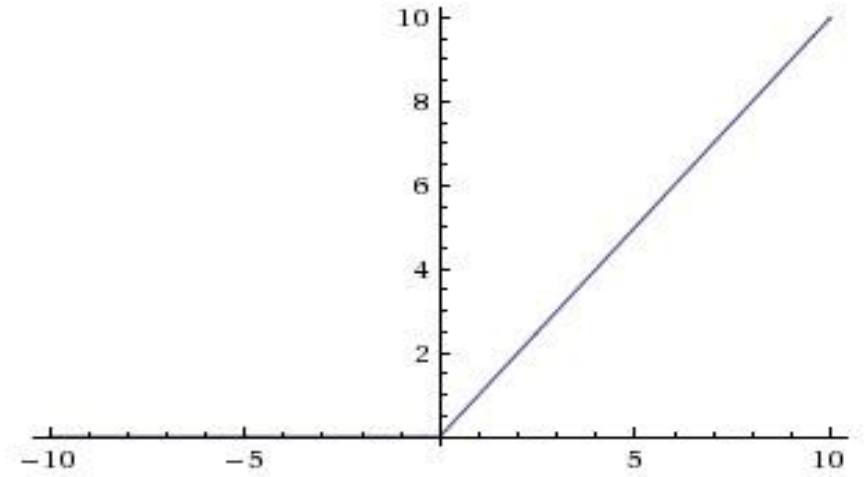
In practice the *tanh non-linearity* is always preferred to the *sigmoid nonlinearity*.

[LeCun et al., 1991]

Source: <http://cs231n.github.io>

# Activation Functions: ReLU

$$f(x) = \max(0, x)$$



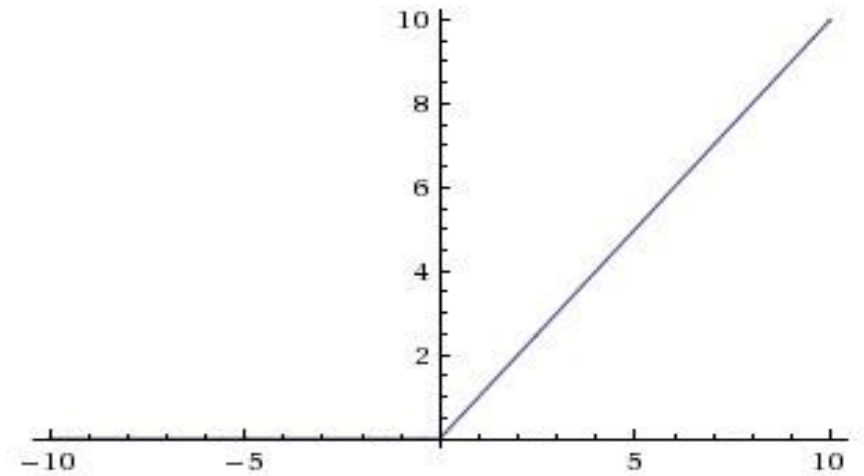
[Krizhevsky et al., 2012]

Source: <http://cs231n.github.io>



# Activation Functions: ReLU

$$f(x) = \max(0, x)$$



ReLU is 6 times faster in the convergence of stochastic gradient descent compared to the sigmoid/tanh ([Krizhevsky et al.](#)).

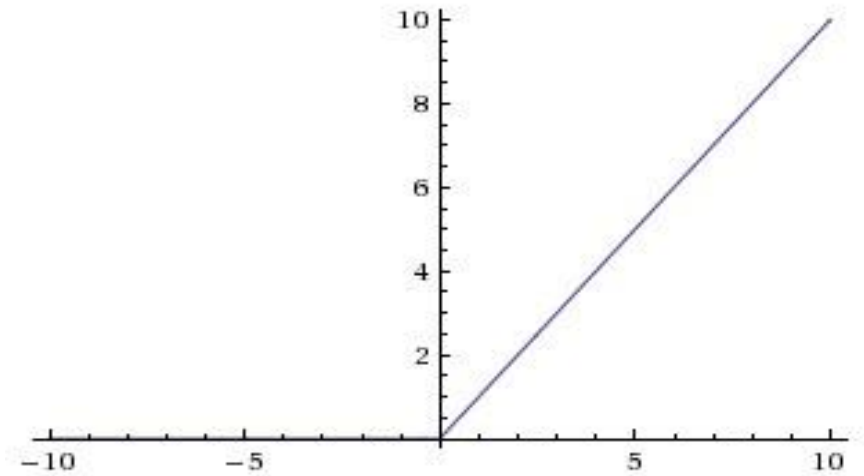
ReLU is simple as compared to tanh/sigmoid that involve expensive operations (exponentials, etc.)

[Krizhevsky et al., 2012]

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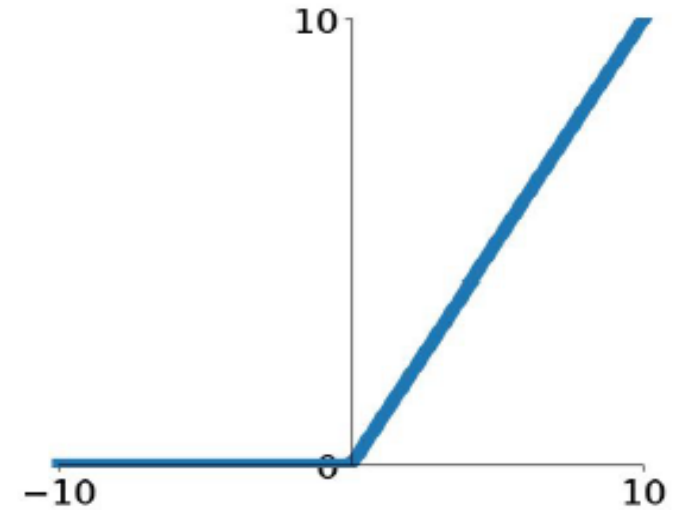
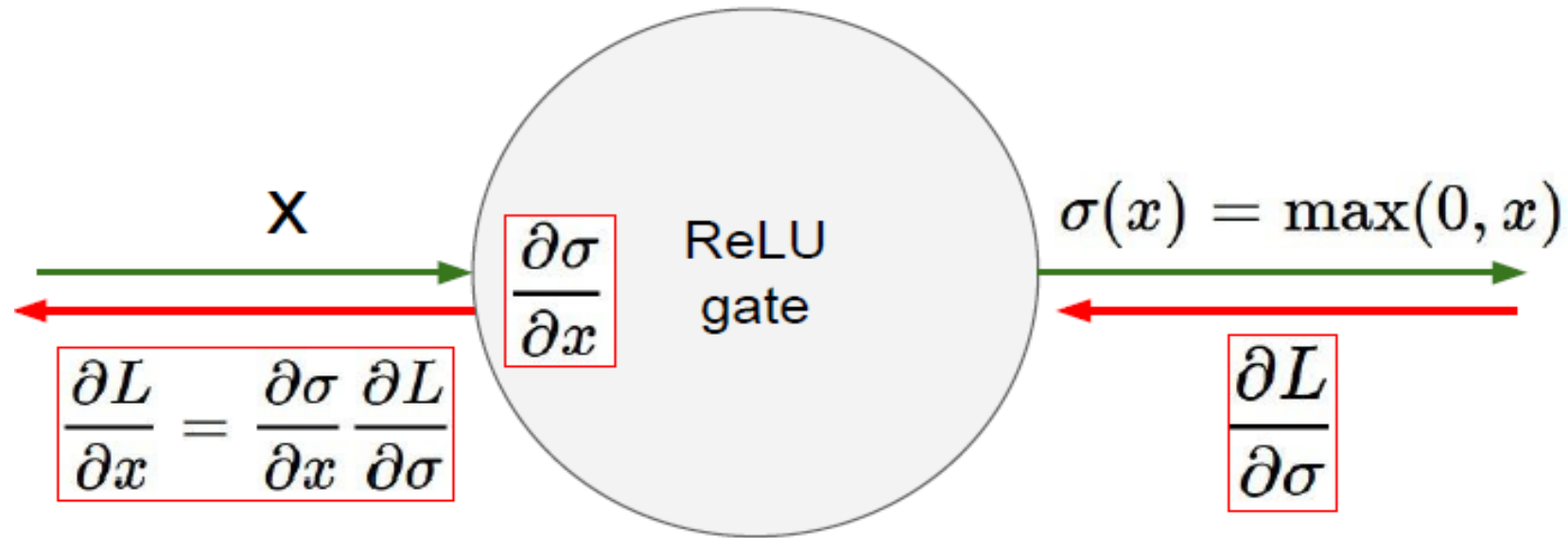
ReLU is simple as compared to tanh/sigmoid that involve expensive operations (exponentials, etc.)

Dying ReLU problem: a large gradient flowing through a ReLU neuron could cause the weights to update in such a way that the neuron will never activate on any datapoint again.

[Krizhevsky et al., 2012]

Source: <http://cs231n.github.io>

# Activation Functions: ReLU



What happens when  $x = -10$ ?

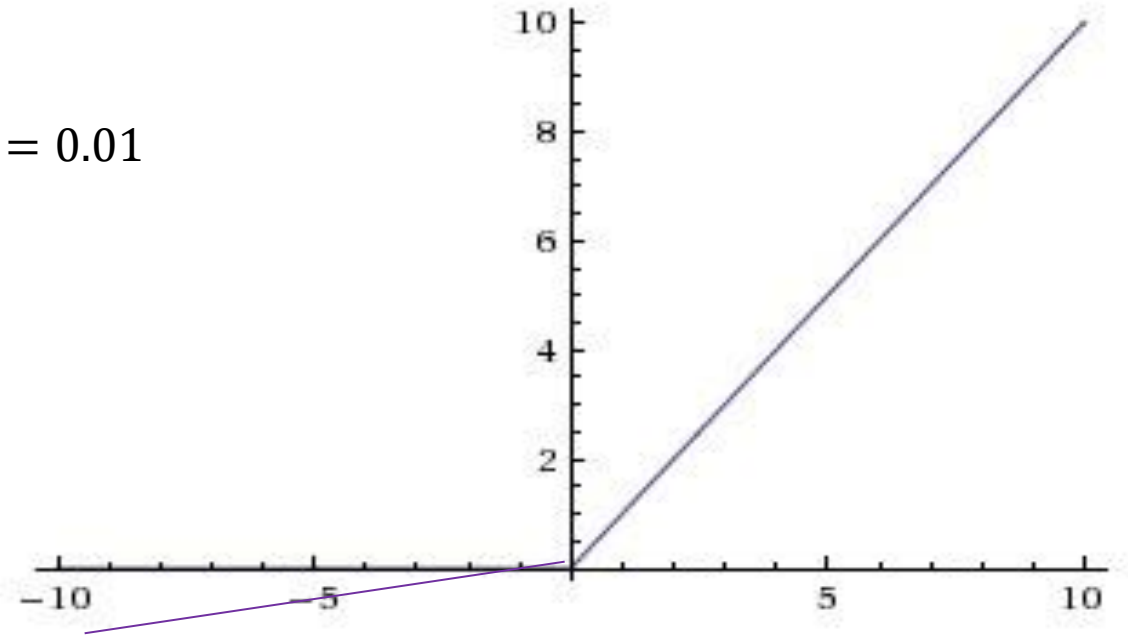
What happens when  $x = 0$ ?

What happens when  $x = 10$ ?

# Activation Functions: Leaky ReLU

$$f(x) = \begin{cases} \alpha x, & x < 0 \\ x, & x \geq 0 \end{cases}$$

$$\alpha = 0.01$$



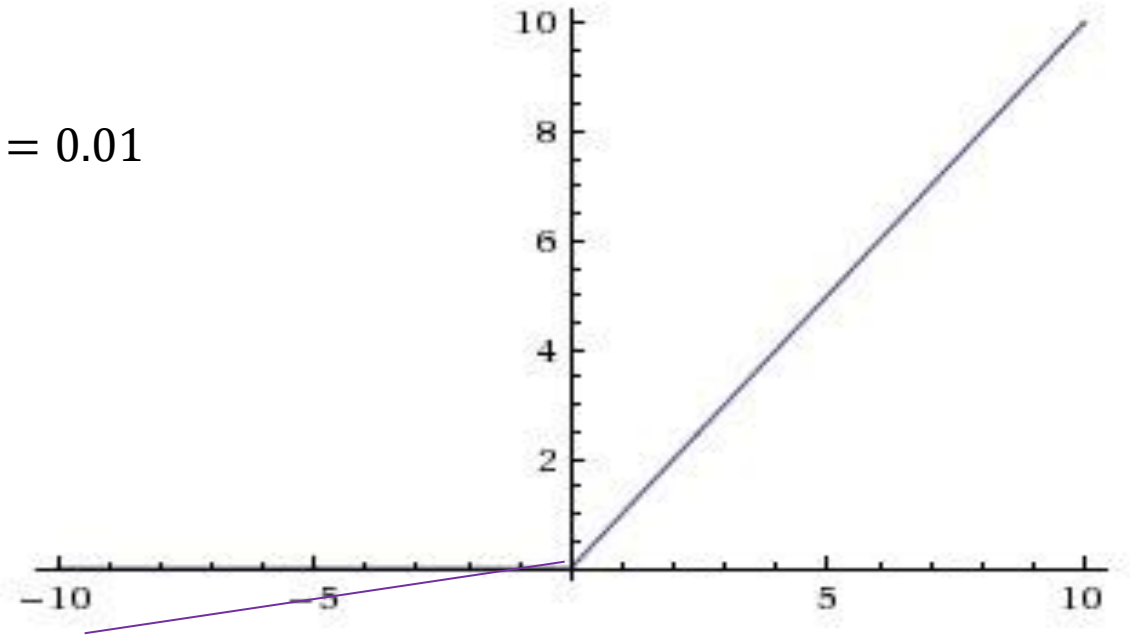
[Mass et al., 2013]

Source: <http://cs231n.github.io>

# Activation Functions: Leaky ReLU

$$f(x) = \begin{cases} \alpha x, & x < 0 \\ x, & x \geq 0 \end{cases}$$

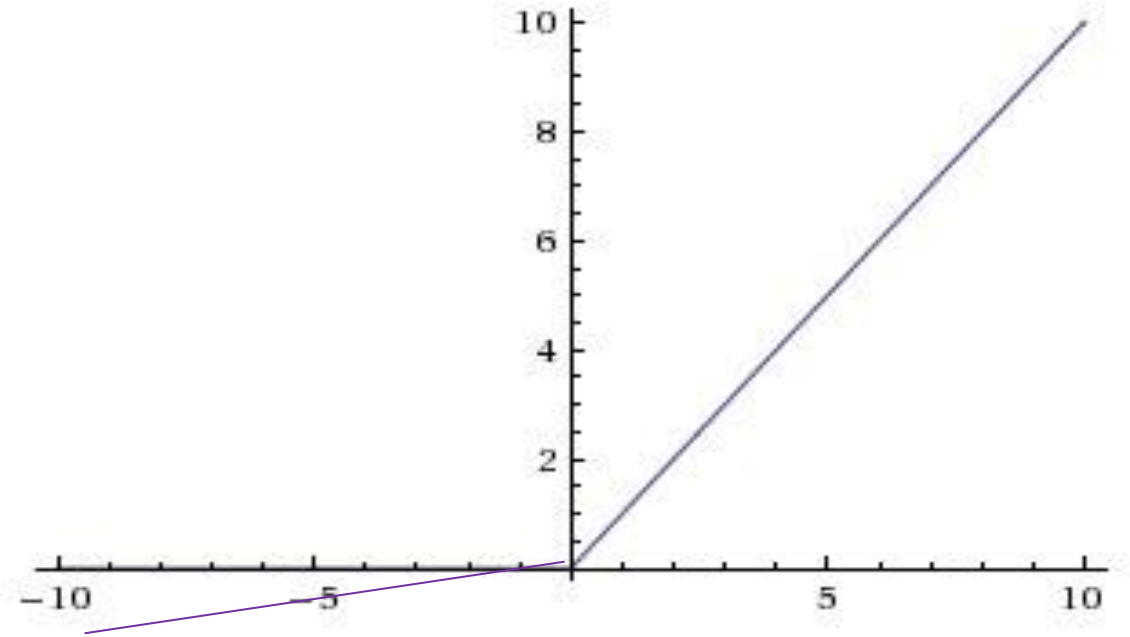
$$\alpha = 0.01$$



Succeeded in some cases, but the results are not always consistent.

# Activation Functions: Parametric ReLU

$$f(x) = \begin{cases} \alpha x, & x < 0 \\ x, & x \geq 0 \end{cases}$$



In PReLU, the slope in the negative region is considered as a parameter of each neuron and learnt from data.

He, K., Zhang, X., Ren, S., & Sun, J. (2015). Delving deep into rectifiers: Surpassing human-level performance on imagenet classification. *IEEE international conference on computer vision (CVPR)*.

Source: <http://cs231n.github.io>

# Activation Functions: Maxout

Maxout neuron (introduced by [Goodfellow et al.](#)) generalizes the ReLU and its leaky version.

The Maxout neuron computes the function:

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

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Both ReLU and Leaky ReLU are a special case of this form (for example, for ReLU, we have  $w_1=0, b_1=0$ ,  $w_2=\text{identity}$ , and  $b_2=0$ ).

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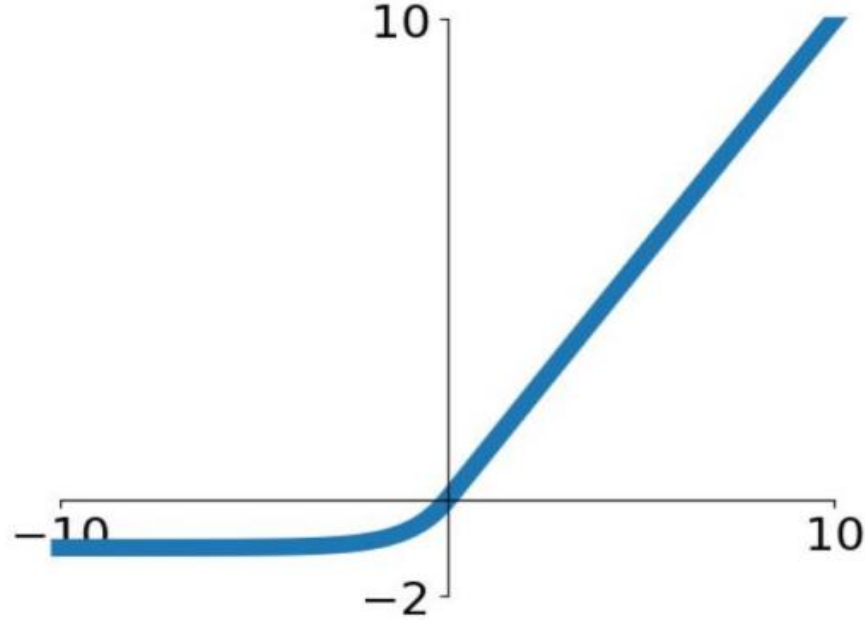
Both ReLU and Leaky ReLU are a special case of this form (for example, for ReLU, we have  $w_1=0, b_1=0$ ,  $w_2=\text{identity}$ , and  $b_2=0$ ).

Unlike the ReLU neurons it doubles the number of parameters.

[Goodfellow et al., 2013]

Source: <http://cs231n.github.io>

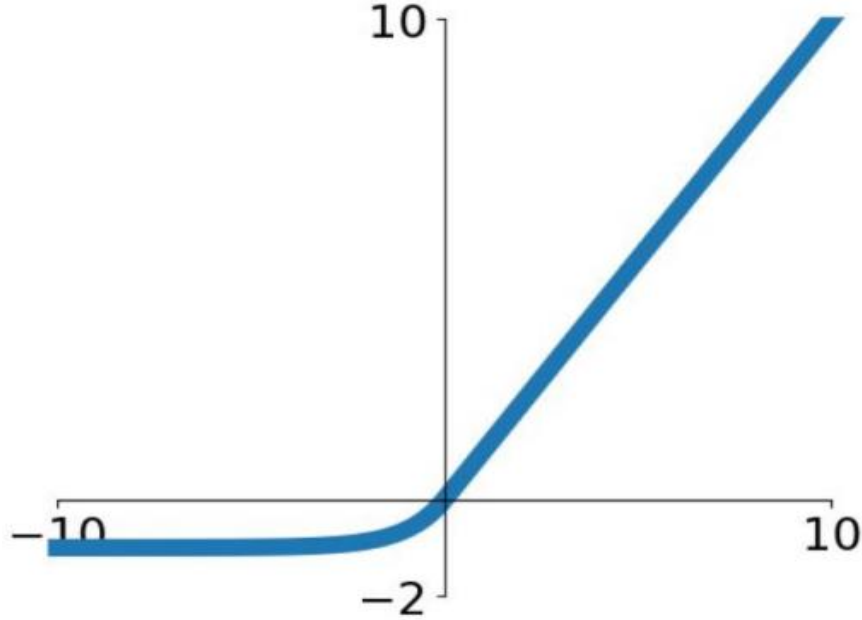
# Activation Functions: ELU



$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha (\exp(x) - 1) & \text{if } x \leq 0 \end{cases}$$

- Exponential Linear Unit

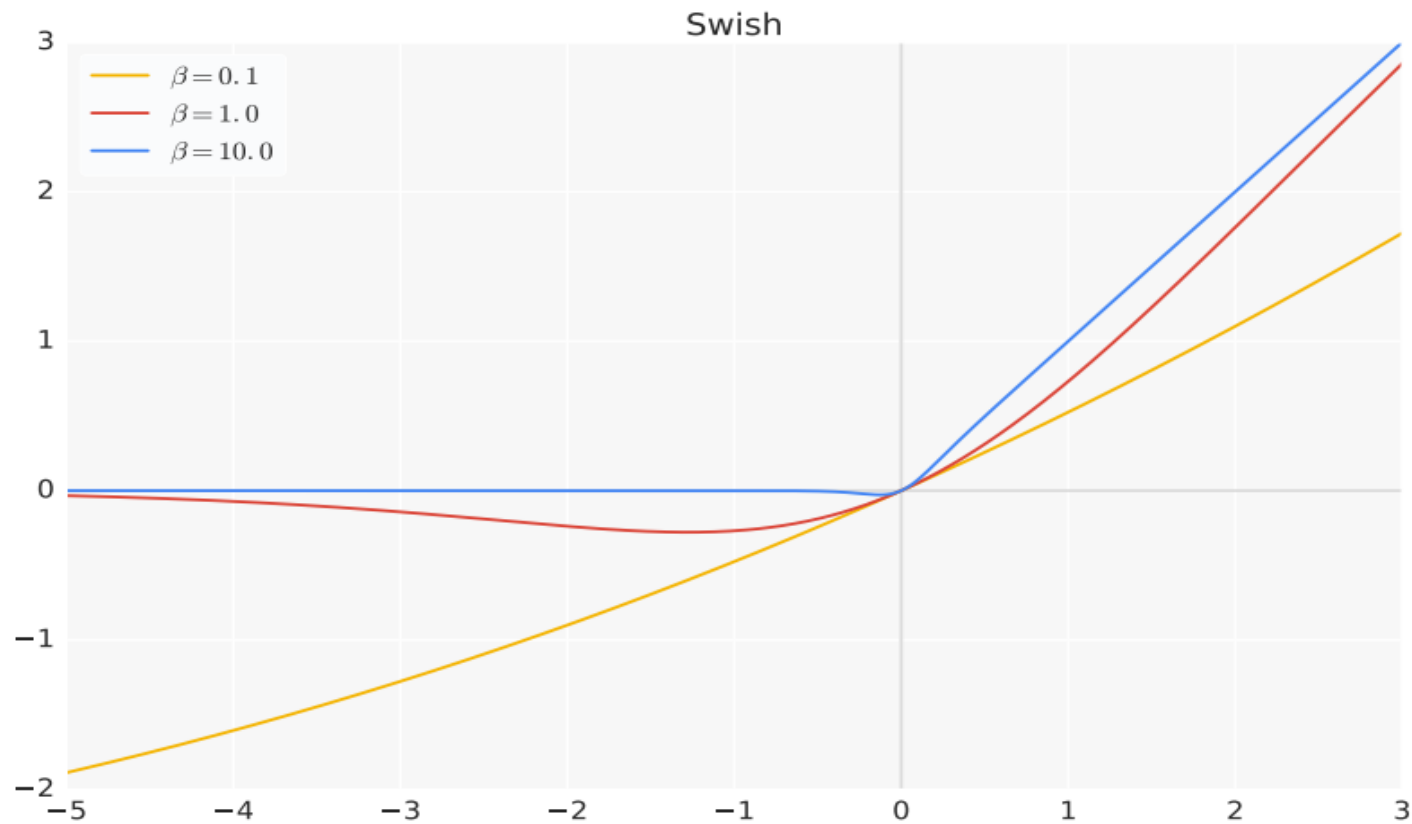
# Activation Functions: ELU



$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha (\exp(x) - 1) & \text{if } x \leq 0 \end{cases}$$

- Exponential Linear Unit
- All benefits of ReLU
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise
- Computation requires `exp()`

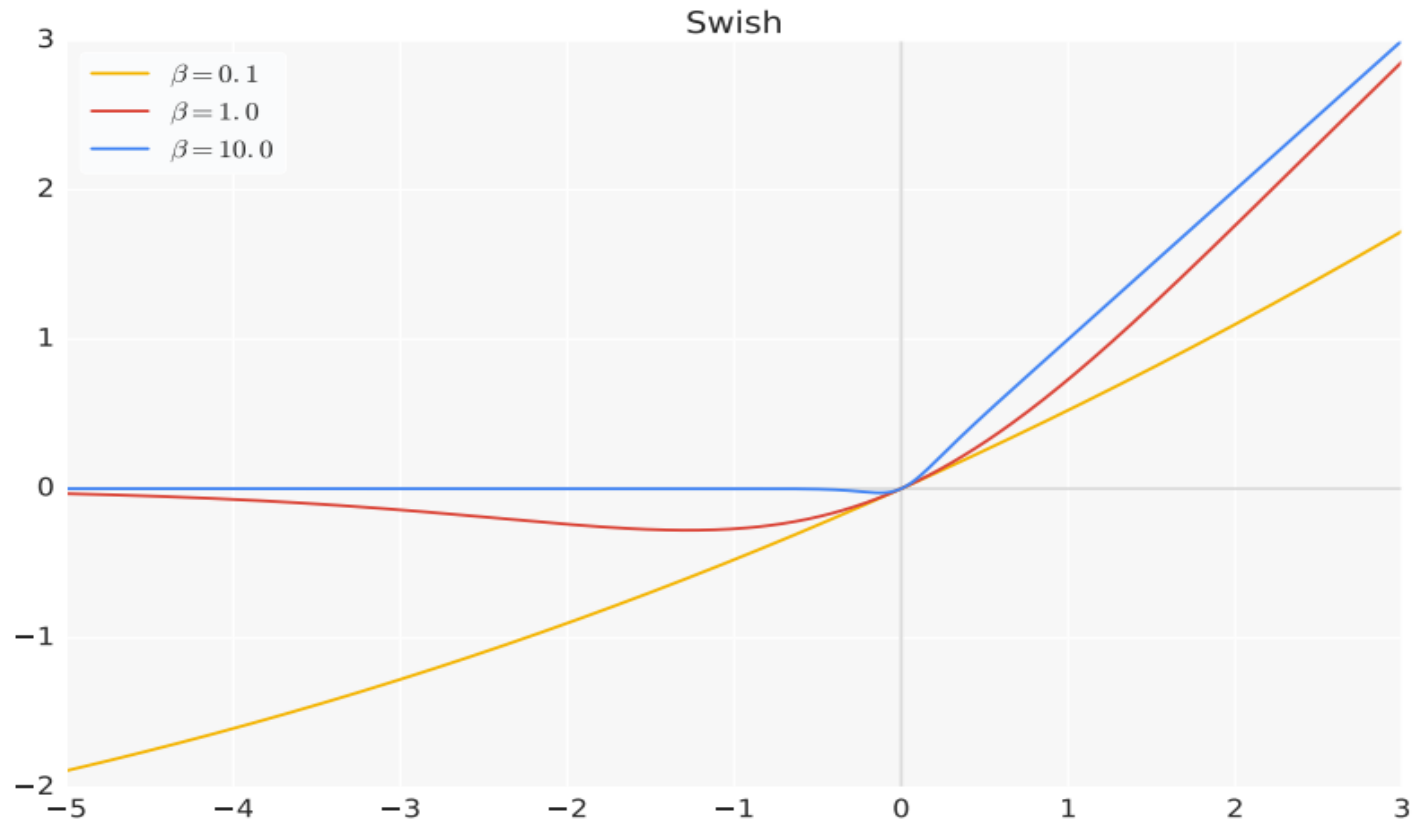
# Activation Functions: Swish



$$f(x) = x \cdot \text{sigmoid}(\beta x)$$

- ReLU is special case of Swish

# Activation Functions: Swish



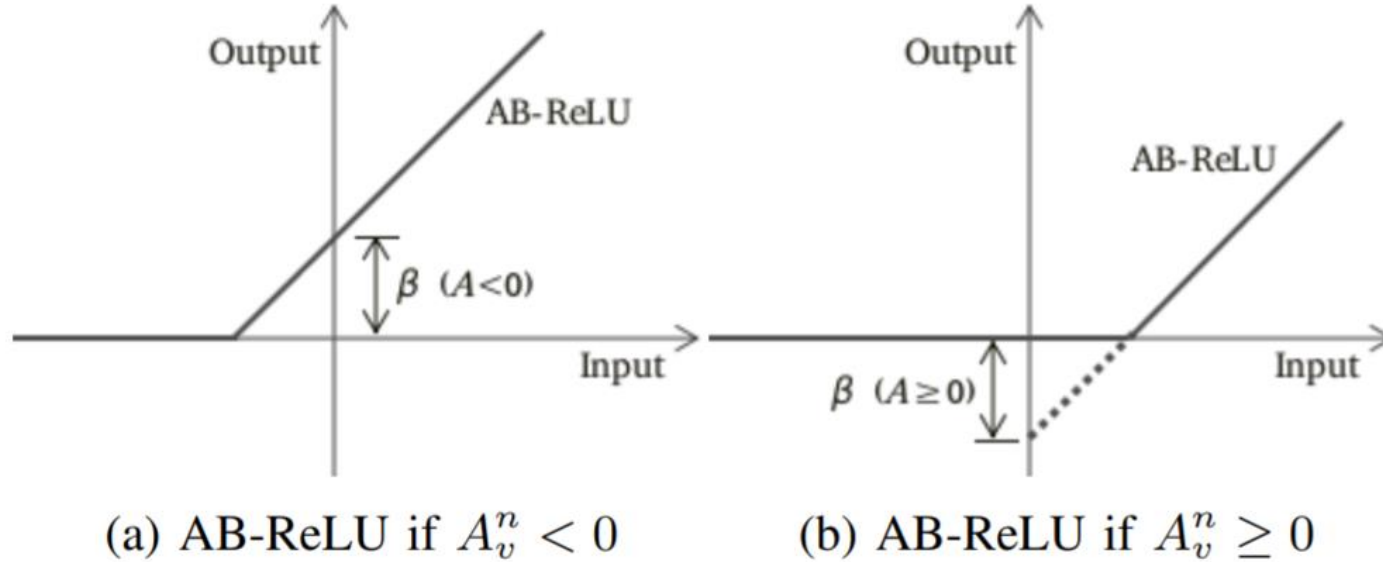
$$f(x) = x \cdot \text{sigmoid}(\beta x)$$

- ReLU is special case of Swish

CIFAR-10 accuracy

Model	ResNet	WRN	DenseNet
LReLU	94.2	95.6	94.7
PReLU	94.1	95.1	94.5
Softplus	94.6	94.9	94.7
ELU	94.1	94.1	94.4
SELU	93.0	93.2	93.9
GELU	94.3	95.5	94.8
ReLU	93.8	95.3	94.8
Swish-1	94.7	95.5	94.8
Swish	94.5	95.5	94.8

# Activation Functions: ABRReLU



$$I_v^{n+1}(\rho) = \begin{cases} I_v^n(\rho) - \beta, & \text{if } I_v^n(\rho) - \beta > 0 \\ 0, & \text{otherwise} \end{cases}$$

$$\beta = \alpha \times A_v^n$$

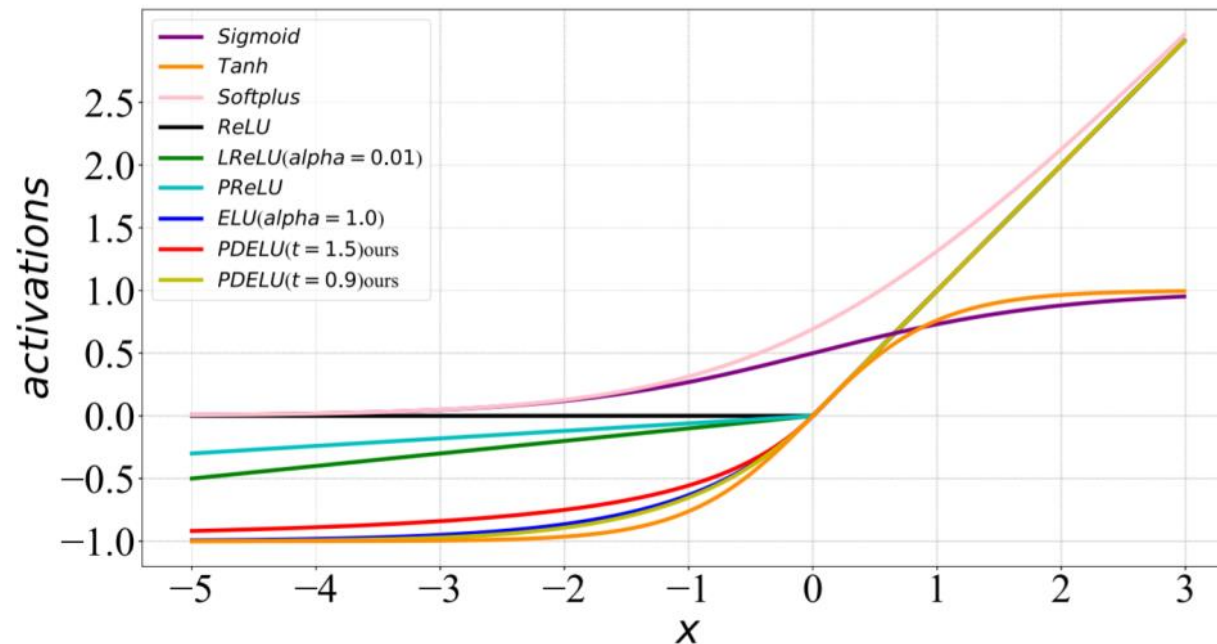
average of input volume

Average Biased ReLU (ABReLU)

# Activation Functions: PDELU

$$f(x_i) = \begin{cases} x_i & \text{if } x_i > 0 \\ \alpha_i \cdot ([1 + (1 - t)x_i]^{\frac{1}{1-t}} - 1) & \text{if } x_i \leq 0 \end{cases}$$

1. When  $x_i \geq 0$ ,  $f(x_i) = x_i$ , so,  $f(x_i) \in [0, +\infty]$ .
2. When  $x_i < 0$  and  $\lim t \rightarrow -\infty$ ,  $f(x_i) = \alpha \cdot ([1 + (1 - t)x_i]^{\frac{1}{1-t}} - 1)$  and  $f(x_i)$  is monotonically increasing exponentially. So,  $f(x_i) \in (-\alpha, 0]$ .



## Parametric Deformable Exponential Linear Units (PDELU)

# Activation Functions: In Practice

- Use ReLU. Be careful with your learning rates
- Try out PDELU/ABReLU/Swish/
- Try out Leaky ReLU but performance might not be stable
- Try out tanh but don't expect much
- Don't use sigmoid

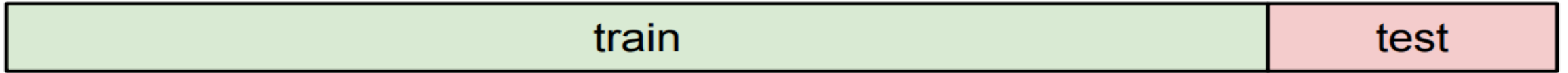


# Dataset Preparation

## Train/Val/Test sets

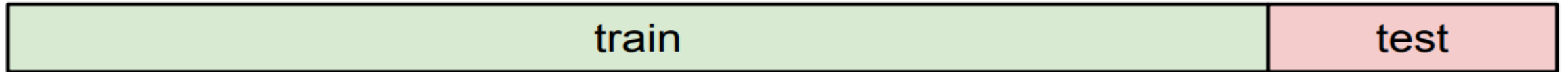
# In General People Do: Train/Test

- Split data into train and test,
- Choose hyperparameters that work best on test data



# In General People Do: Train/Test

- Split data into train and test,
- Choose hyperparameters that work best on test data



**BAD:** No idea how algorithm will perform on new data

# K-Fold Validation

- Split data into folds,
- Try each fold as validation and average the results

fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test

# K-Fold Validation

- Split data into folds,
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fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test

Useful for small datasets, but not used too frequently in deep learning

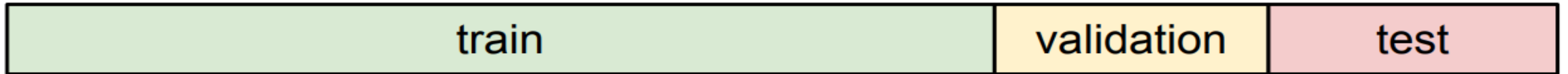
# Better Approach: Train/Val/Test sets

- Split data into **train**, **val**, and **test**;
- Choose hyperparameters on val and evaluate on test



# Better Approach: Train/Val/Test sets

- Split data into **train**, **val**, and **test**;
- Choose hyperparameters on val and evaluate on test



Division can be done based on the size of dataset:

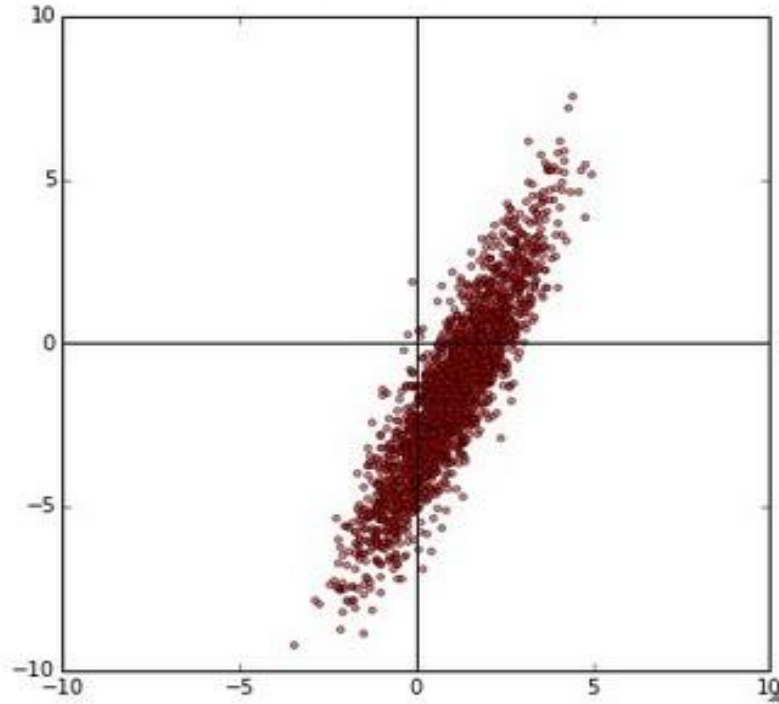
- Roughly 10k or 10% whichever is less for val and test sets.
- Rest in train set.

# Data Preprocessing

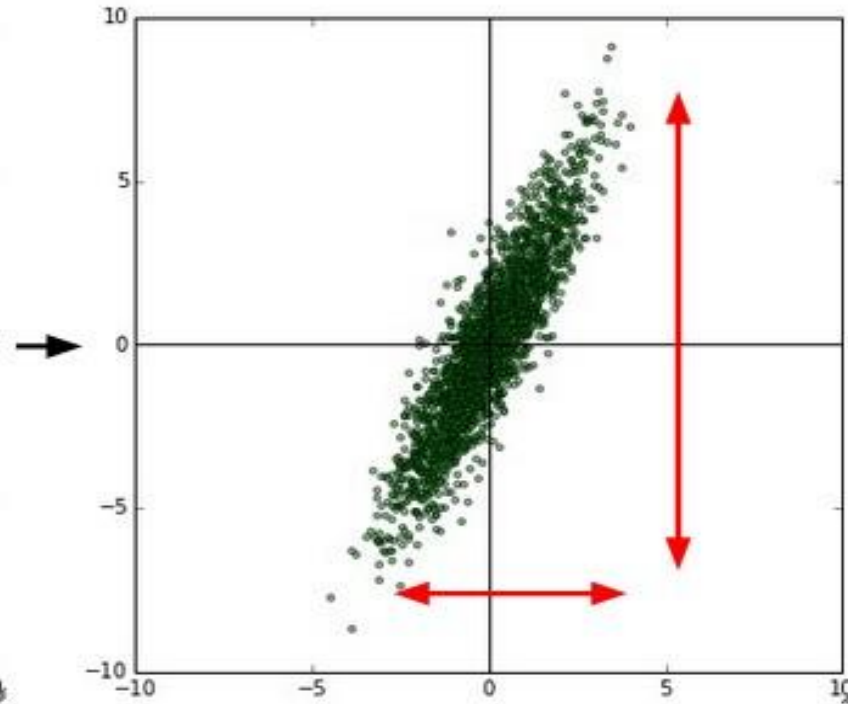


# Data Preprocessing

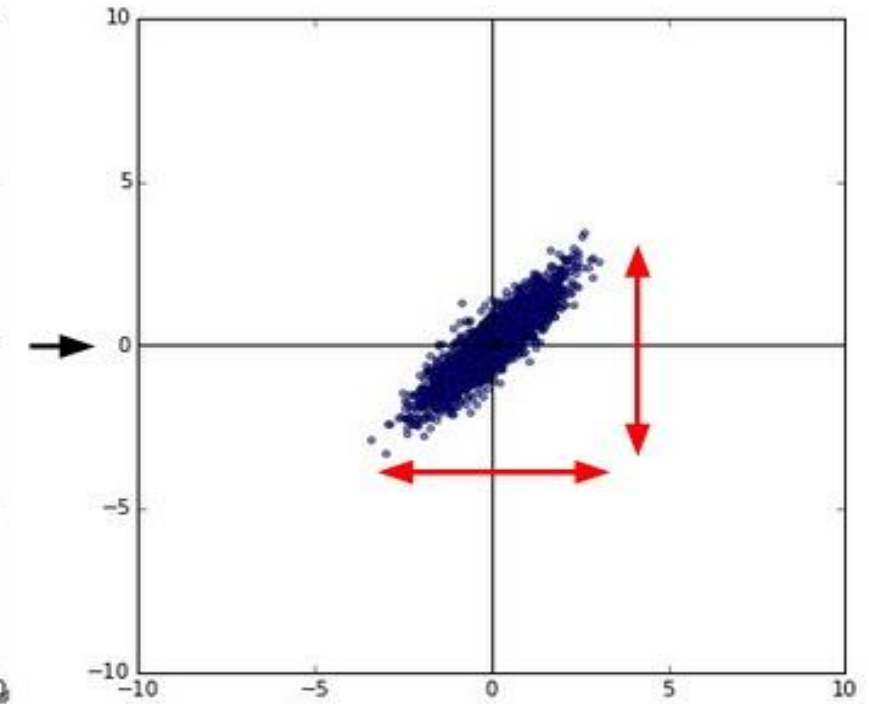
original data



zero-centered data

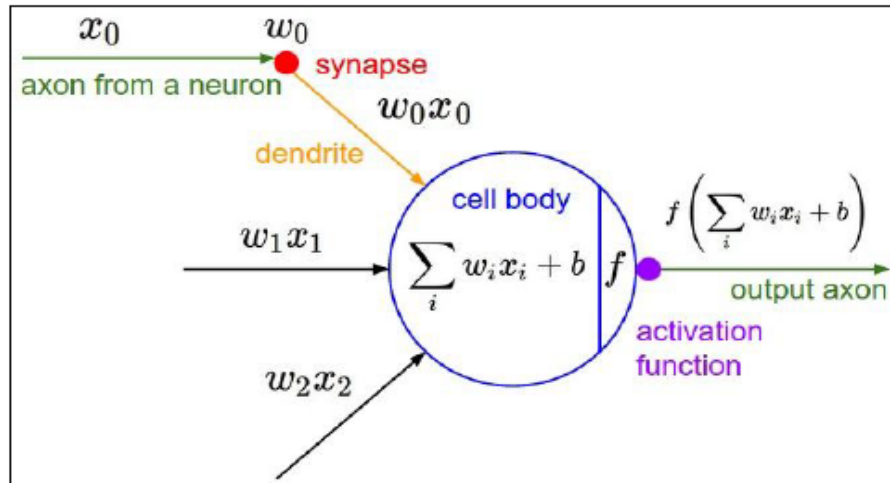


normalized data



# Data Preprocessing

Consider what happens when the input to a neuron ( $x$ ) is always positive:

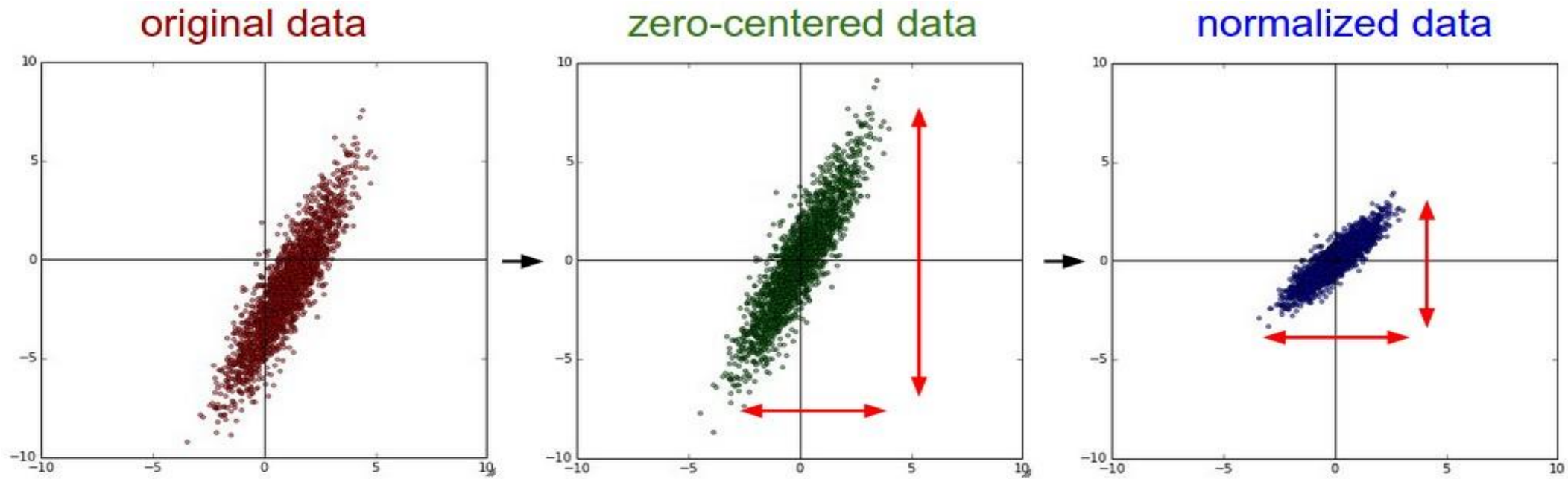


$$f\left(\sum_i w_i x_i + b\right)$$

What can we say about the gradients on  $\mathbf{w}$ ?

Always all positive or all negative  
(this is also why you want zero-mean data!)

# Data Preprocessing



**In practice for Images: only centering is preferred**

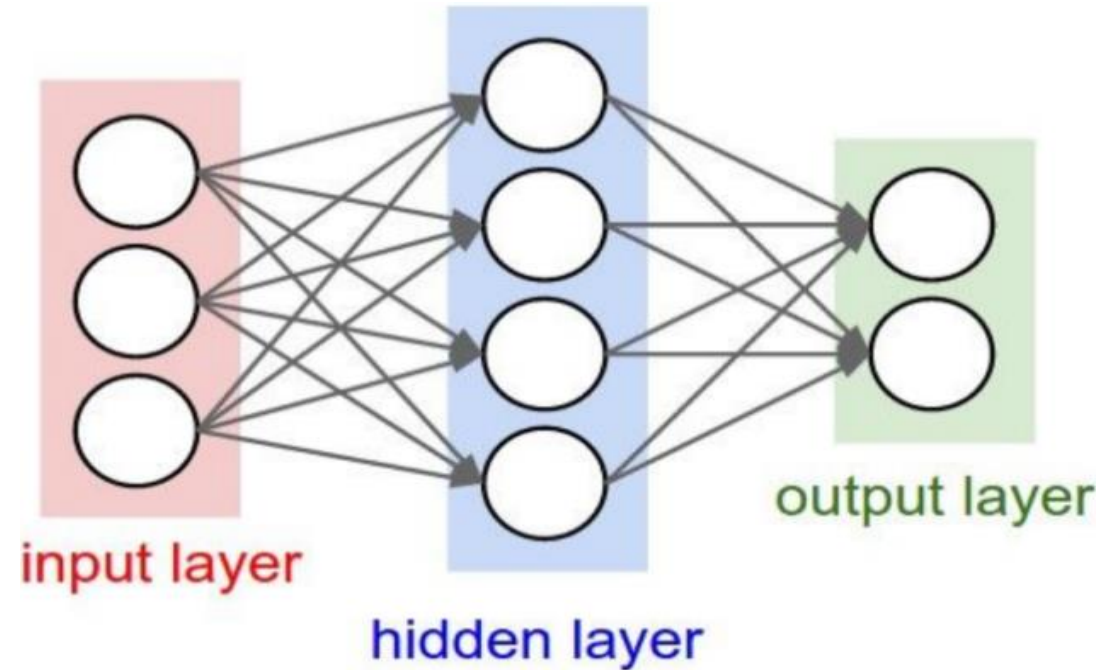
e.g. consider CIFAR-10 example with [32,32,3] images

- Subtract the mean image (e.g. AlexNet)  
(mean image = [32,32,3] array)
- Subtract per-channel mean (e.g. VGGNet, ResNet, etc.)  
(mean along each channel = 3 numbers)

# Weight Initialization

# Weight Initialization: Constant

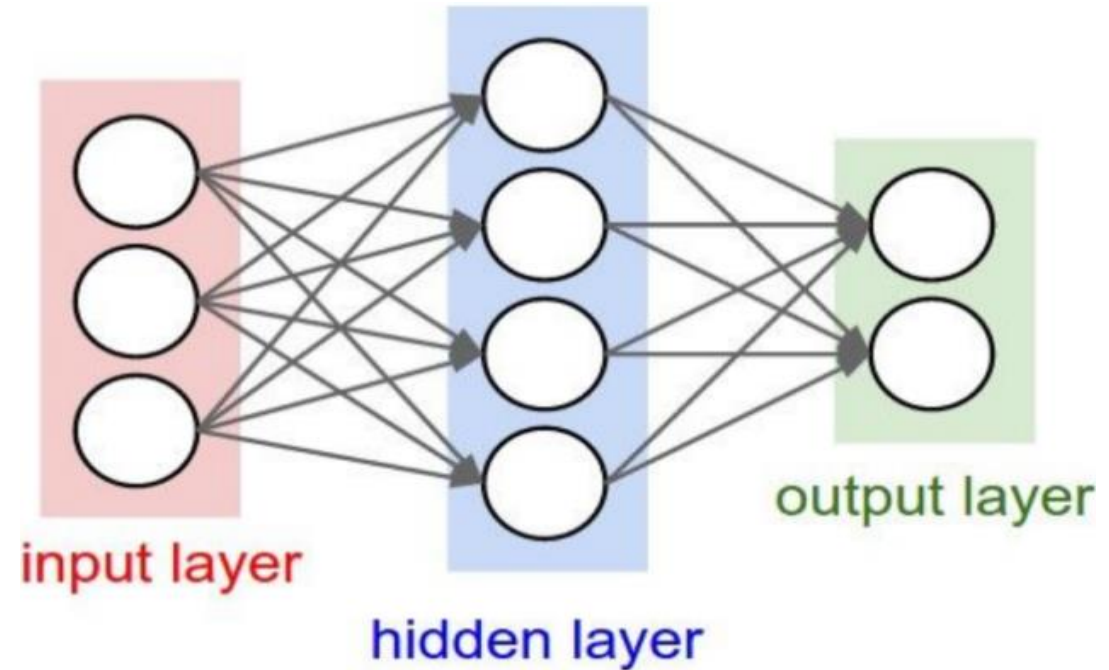
Q: what happens when  $W=\text{Constant}$  init is used?



# Weight Initialization: Constant

Q: what happens when  $W=\text{Constant}$  init is used?

- Every neuron will compute the same output and undergo the exact same parameter updates.
- There is no source of asymmetry between neurons if their weights are initialized to be the same.



# Weight Initialization: Gaussian

First idea: **Small random numbers**

(Gaussian with zero mean and  $1e-2$  standard deviation)

Symmetry breaking: Weights are different for different neurons

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-> gradient diminishing problem.

Increase the standard deviation to 1

Almost all neurons completely saturated, either -1 or 1. Gradients will be all zero.  
-> gradient diminishing problem.

# Weight Initialization: Gaussian

Lets look at  
some  
activation  
statistics

E.g. 10-layer net with  
500 neurons on each  
layer, using tanh  
non-linearities, and  
initializing as  
described in last slide.

```
# assume some unit gaussian 10-D input data
D = np.random.randn(1000, 500)
hidden_layer_sizes = [500]*10
nonlinearities = ['tanh']*len(hidden_layer_sizes)

act = {'relu':lambda x:np.maximum(0,x), 'tanh':lambda x:np.tanh(x)}
Hs = {}
for i in xrange(len(hidden_layer_sizes)):
    X = D if i == 0 else Hs[i-1] # input at this layer
    fan_in = X.shape[1]
    fan_out = hidden_layer_sizes[i]
    W = np.random.randn(fan_in, fan_out) * 0.01 # layer initialization

    H = np.dot(X, W) # matrix multiply
    H = act[nonlinearities[i]](H) # nonlinearity
    Hs[i] = H # cache result on this layer

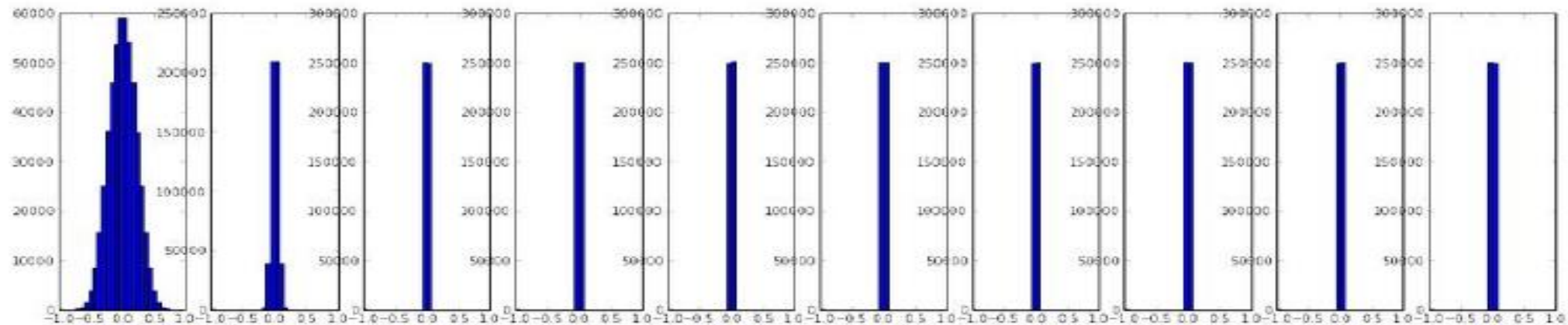
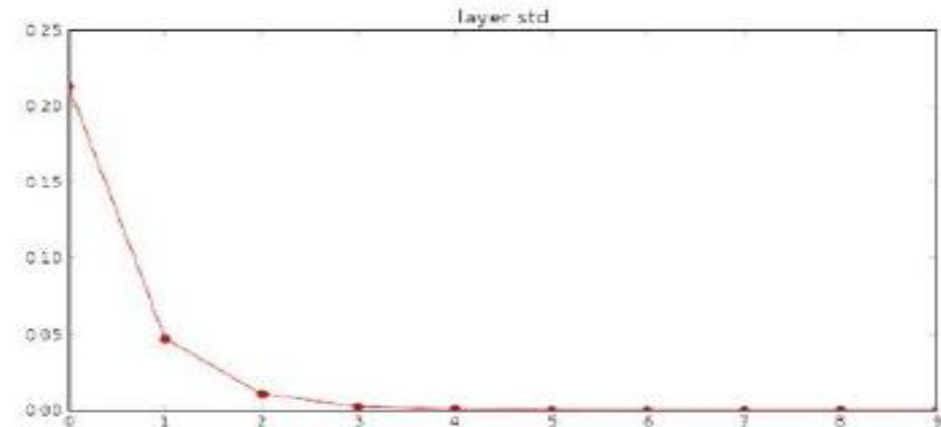
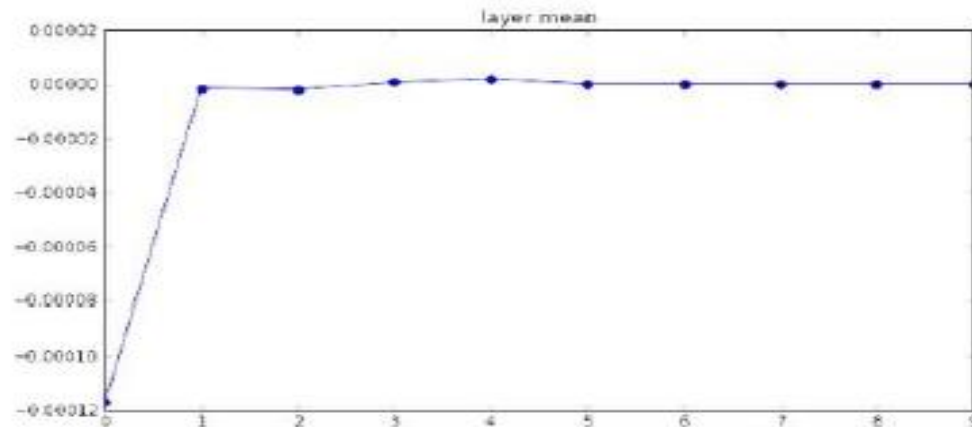
# look at distributions at each layer
print 'input layer had mean %f and std %f' % (np.mean(D), np.std(D))
layer_means = [np.mean(H) for i,H in Hs.iteritems()]
layer_stds = [np.std(H) for i,H in Hs.iteritems()]
for i,H in Hs.iteritems():
    print 'hidden layer %d had mean %f and std %f' % (i+1, layer_means[i], layer_stds[i])

# plot the means and standard deviations
plt.figure()
plt.subplot(121)
plt.plot(Hs.keys(), layer_means, 'ob-')
plt.title('layer mean')
plt.subplot(122)
plt.plot(Hs.keys(), layer_stds, 'or-')
plt.title('layer std')

# plot the raw distributions
plt.figure()
for i,H in Hs.iteritems():
    plt.subplot(1,len(Hs),i+1)
    plt.hist(H.ravel(), 30, range=(-1,1))
```

# Weight Initialization: Gaussian

```
input layer had mean 0.000927 and std 0.998388
hidden layer 1 had mean -0.000117 and std 0.213081
hidden layer 2 had mean -0.000001 and std 0.047551
hidden layer 3 had mean -0.000002 and std 0.010630
hidden layer 4 had mean 0.000001 and std 0.002378
hidden layer 5 had mean 0.000002 and std 0.000532
hidden layer 6 had mean -0.000000 and std 0.000119
hidden layer 7 had mean 0.000000 and std 0.000026
hidden layer 8 had mean -0.000000 and std 0.000006
hidden layer 9 had mean 0.000000 and std 0.000001
hidden layer 10 had mean -0.000000 and std 0.000000
```



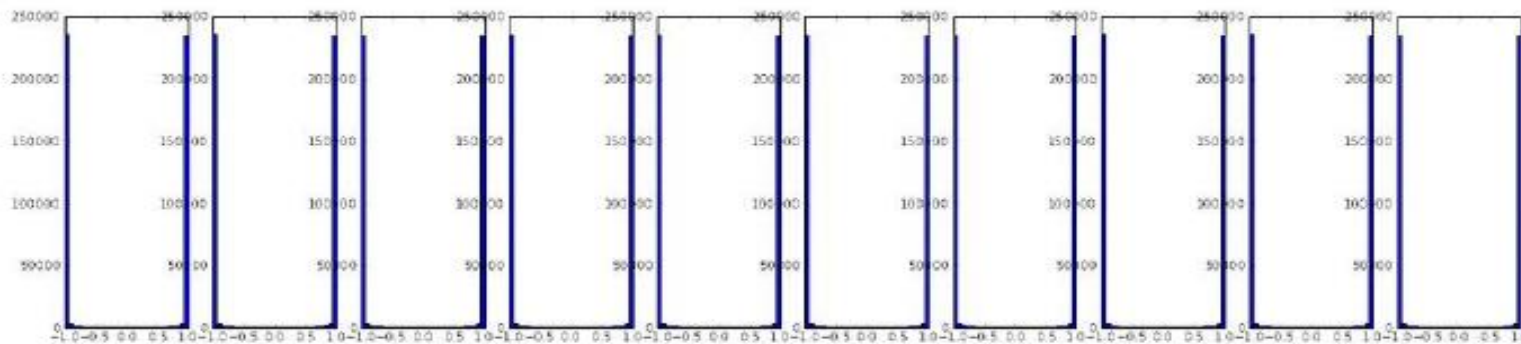
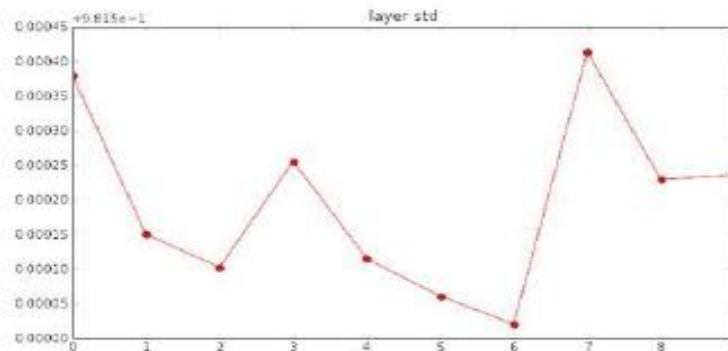
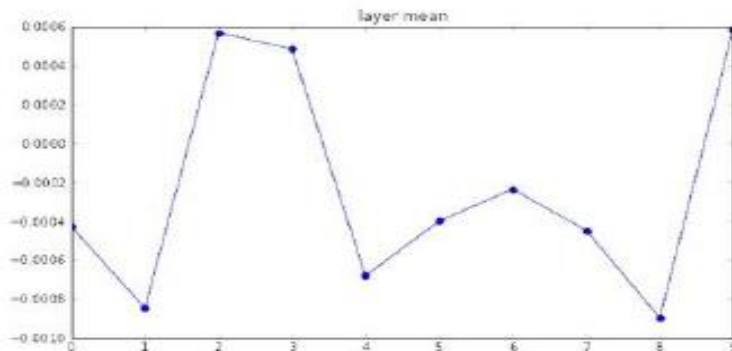


# Weight Initialization: Gaussian

```
W = np.random.randn(fan_in, fan_out) * 1.0 # layer initialization
```

input layer had mean 0.001800 and std 1.001311  
hidden layer 1 had mean -0.000430 and std 0.981879  
hidden layer 2 had mean -0.000849 and std 0.981649  
hidden layer 3 had mean 0.000566 and std 0.981601  
hidden layer 4 had mean 0.000483 and std 0.981755  
hidden layer 5 had mean -0.000682 and std 0.981614  
hidden layer 6 had mean -0.000401 and std 0.981560  
hidden layer 7 had mean -0.000237 and std 0.981520  
hidden layer 8 had mean -0.000448 and std 0.981913  
hidden layer 9 had mean -0.000899 and std 0.981728  
hidden layer 10 had mean 0.000584 and std 0.981736

\*1.0 instead of \*0.01



Almost all neurons completely saturated, either -1 and 1. Gradients will be all zero.

# Weight Initialization: Xavier

**Calibrating the variances with  $1/\sqrt{\text{fan\_in}}$**

```
W = np.random.randn(fan_in, fan_out)/np.sqrt(fan_in)
```

Reasonable initialization.

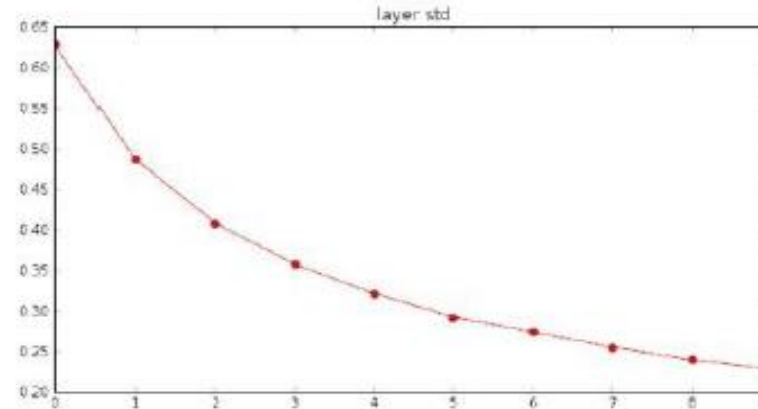
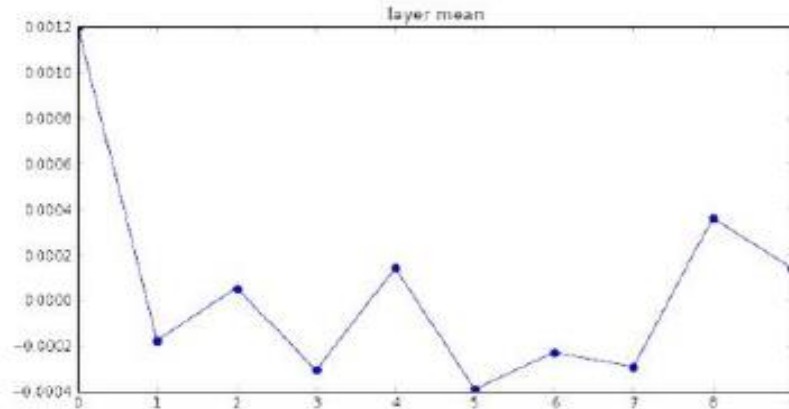
(Mathematical derivation assumes linear activations)

# Weight Initialization: Xavier

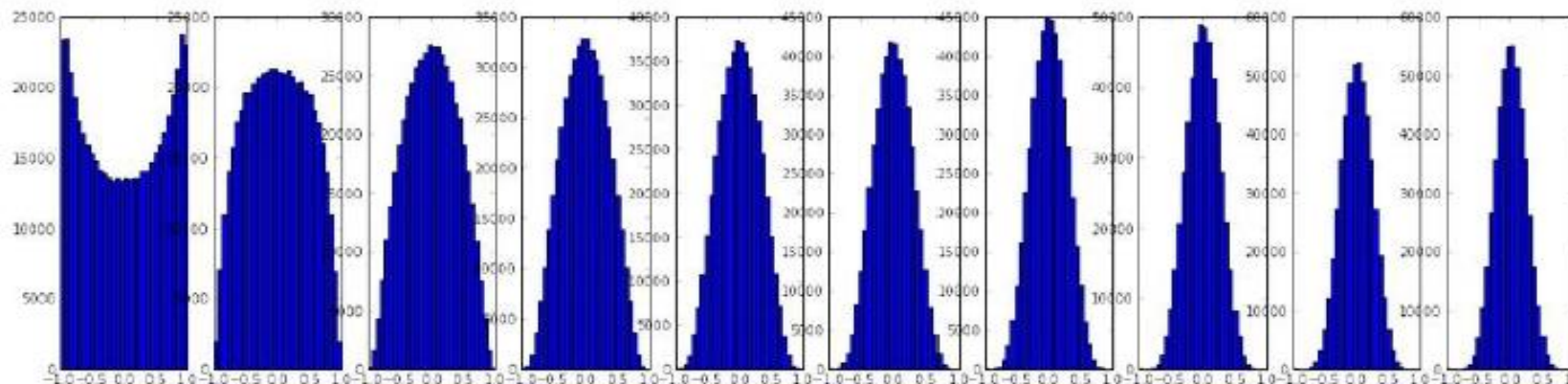
input layer had mean 0.001800 and std 1.001311  
hidden layer 1 had mean 0.001198 and std 0.627953  
hidden layer 2 had mean -0.000175 and std 0.486051  
hidden layer 3 had mean 0.000055 and std 0.407723  
hidden layer 4 had mean -0.000306 and std 0.357108  
hidden layer 5 had mean 0.000142 and std 0.320917  
hidden layer 6 had mean -0.000389 and std 0.292116  
hidden layer 7 had mean -0.000228 and std 0.273387  
hidden layer 8 had mean -0.000291 and std 0.254935  
hidden layer 9 had mean 0.000361 and std 0.239266  
hidden layer 10 had mean 0.000139 and std 0.228008

```
W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in) # layer initialization
```

“Xavier initialization”  
[Glorot et al., 2010]



**Reasonable initialization.**  
(Mathematical derivation  
assumes linear activations)

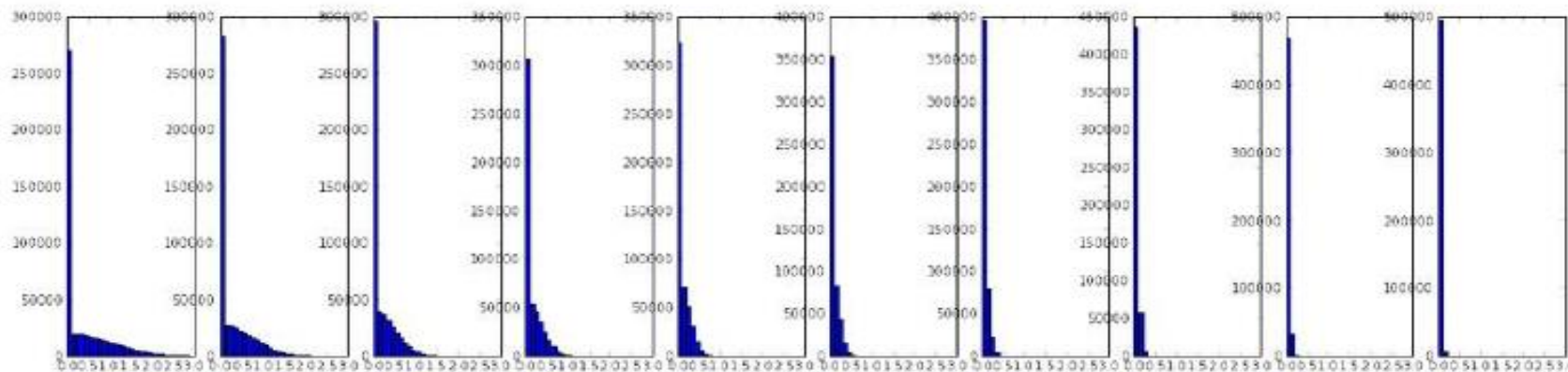
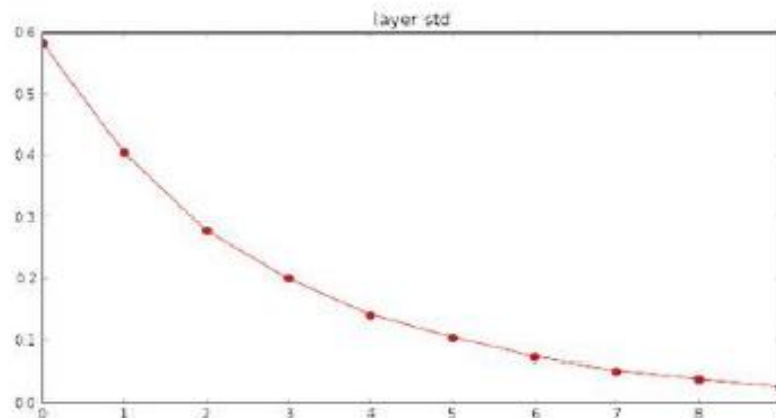
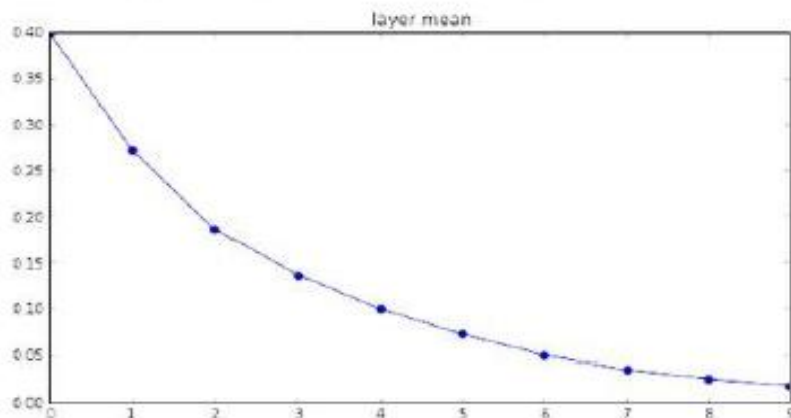


# Weight Initialization: Xavier

input layer had mean 0.000501 and std 0.999444  
hidden layer 1 had mean 0.398623 and std 0.582273  
hidden layer 2 had mean 0.272352 and std 0.403795  
hidden layer 3 had mean 0.186076 and std 0.276912  
hidden layer 4 had mean 0.136442 and std 0.198685  
hidden layer 5 had mean 0.099568 and std 0.140299  
hidden layer 6 had mean 0.072234 and std 0.103280  
hidden layer 7 had mean 0.049775 and std 0.072748  
hidden layer 8 had mean 0.035138 and std 0.051572  
hidden layer 9 had mean 0.025404 and std 0.038583  
hidden layer 10 had mean 0.018408 and std 0.026076

```
W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in) # layer initialization
```

but when using the ReLU  
nonlinearity it breaks.



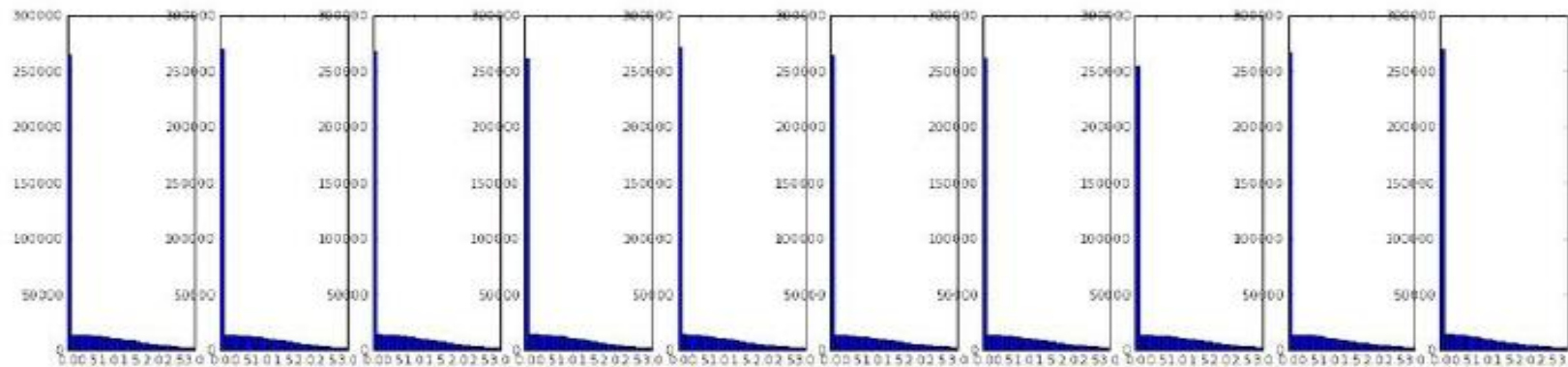
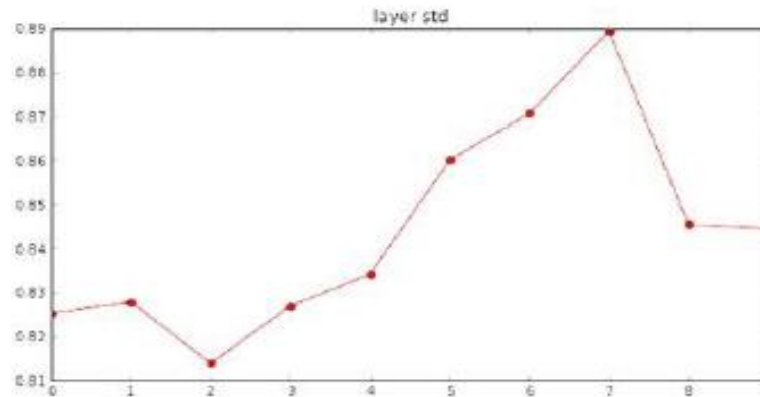
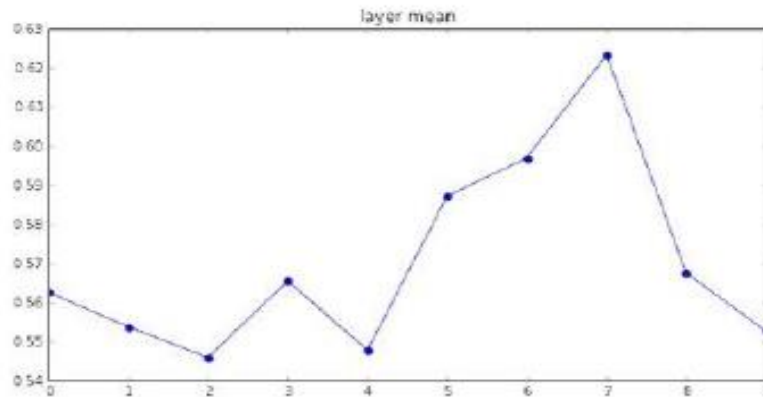


# Weight Initialization: XavierImproved

input layer had mean 0.000501 and std 0.999444  
hidden layer 1 had mean 0.562488 and std 0.825232  
hidden layer 2 had mean 0.553614 and std 0.827835  
hidden layer 3 had mean 0.545867 and std 0.813855  
hidden layer 4 had mean 0.565396 and std 0.826902  
hidden layer 5 had mean 0.547678 and std 0.834092  
hidden layer 6 had mean 0.587103 and std 0.860035  
hidden layer 7 had mean 0.596867 and std 0.870610  
hidden layer 8 had mean 0.623214 and std 0.889348  
hidden layer 9 had mean 0.567498 and std 0.845357  
hidden layer 10 had mean 0.552531 and std 0.844523

```
W = np.random.randn(fan_in, fan_out) / np.sqrt(2/fan_in) # layer initialization
```

He et al., 2015  
(note additional 2/)



Proper initialization is an active area of research...

***Understanding the difficulty of training deep feedforward neural networks*** by Glorot and Bengio, 2010

***Exact solutions to the nonlinear dynamics of learning in deep linear neural networks*** by Saxe et al, 2013

***Random walk initialization for training very deep feedforward networks*** by Sussillo and Abbott, 2014

***Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification*** by He et al., 2015

***Data-dependent Initializations of Convolutional Neural Networks*** by Krähenbühl et al., 2015

***All you need is a good init*** by Mishkin and Matas, 2015

...

# Things to remember

- Training CNN

- Activation Functions: ReLU is common, PDELU/ABReLU/Swish can be tried
- Data Preparation: Train/Val/Test
- Data preprocessing: Centering is common
- Weight initialization: XavierImproved works well with ReLU

# Acknowledgement

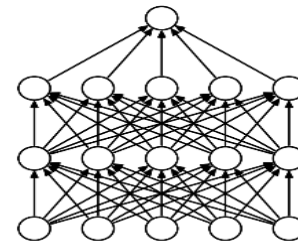
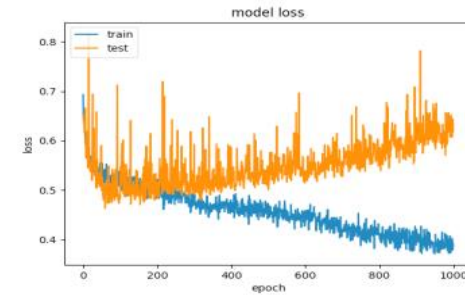
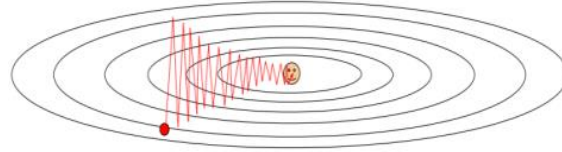
Thanks to the following courses and corresponding researchers for making their teaching/research material online

- Deep Learning, Stanford University
- Introduction to Deep Learning, University of Illinois at Urbana-Champaign
- Introduction to Deep Learning, Carnegie Mellon University
- Convolutional Neural Networks for Visual Recognition, Stanford University
- Natural Language Processing with Deep Learning, Stanford University
- And Many More .....

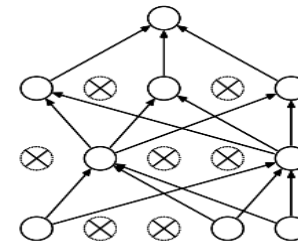
# Next Few Classes

## Training Aspects of CNN

- Optimization
- Learning Rate
- Regularization
- Dropout
- Batch Normalization
- Data Augmentation
- Transfer Learning
- Interpreting Loss Curve



(a) Standard Neural Net



(b) After applying dropout.

