neural_network

October 8, 2020

1 CS498DL Assignment 2

```
[1]: import matplotlib.pyplot as plt
import numpy as np
import math
from sklearn.utils import shuffle

from kaggle_submission import output_submission_csv
from models.neural_net import NeuralNetwork
from models.adam import AdamNeuralNetwork
from utils.data_process import get_CIFAR10_data

//matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots

# For auto-reloading external modules
# See http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2
```

1.1 Loading CIFAR-10

Now that you have implemented a neural network that passes gradient checks and works on toy data, you will test your network on the CIFAR-10 dataset.

```
[2]: # You can change these numbers for experimentation
    # For submission be sure they are set to the default values
    TRAIN_IMAGES = 49000
    VAL_IMAGES = 10000

TEST_IMAGES = 10000

data = get_CIFAR10_data(TRAIN_IMAGES, VAL_IMAGES, TEST_IMAGES)
    X_train, y_train = data['X_train'], data['y_train']
    X_val, y_val = data['X_val'], data['y_val']
    X_test, y_test = data['X_test'], data['y_test']
```

1.2 Train using 2 Layer SGD

To train our network we will use SGD. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
[3]: # Hyperparameters
     input_size = 32 * 32 * 3
     num_layers = 2
     hidden_size = 150
     hidden_sizes = [hidden_size] * (num_layers - 1)
     num_classes = 10
     epochs = 70
     batch_size = 100
     learning_rate = 1e-1
     learning_rate_decay = 0.95
     regularization = 0.001
     # Initialize a new neural network model
     net = NeuralNetwork(input_size, hidden_sizes, num_classes, num_layers)
     # Variables to store performance for each epoch
     train_loss_2sgd = np.zeros(epochs)
     train_accuracy_2sgd = np.zeros(epochs)
     val_accuracy_2sgd = np.zeros(epochs)
     highest_accuracy = -math.inf
     best_network = 0
     # For each epoch...
     for epoch in range(epochs):
         #print('epoch:', epoch)
         # Shuffle the dataset
         #X_train, y_train = shuffle(X_train, y_train)
         # Training
         # For each mini-batch...
         batch_accuracy = []
         f_accuracy = []
         count = 0
         # https://stackoverflow.com/questions/8177079/
      \rightarrow take-the-content-of-a-list-and-append-it-to-another-list
         #https://stackoverflow.com/questions/60133145/
      \rightarrow neural-networks-from-scratch-problem-with-fit-method-when-i-attempt-to-use-mini
         rnd_idx = np.random.permutation(TRAIN_IMAGES)
```

```
n_batches = TRAIN_IMAGES//batch_size
    for batch_idx in np.array_split(rnd_idx, n_batches):
        X_batch = X_train[batch_idx]
        y_batch = y_train[batch_idx]
        f_output = np.argmax(net.forward(X_batch), axis = 1)
        loss = net.backward(X_batch, y_batch, learning_rate, regularization)
        train_loss_2sgd[epoch] += loss
        batch_accuracy.extend(y_batch)
        f_accuracy.extend(f_output)
    #https://stackoverflow.com/questions/25490641/
 →check-how-many-elements-are-equal-in-two-numpy-arrays-python/25490691
    batch_array, f_array = np.array(batch_accuracy), np.array(f_accuracy)
    same_value_count = (batch_array == f_array).sum()
    train_accuracy_2sgd[epoch] = same_value_count / len(batch_accuracy)
    train_loss_2sgd[epoch] /= n_batches
    # Validation
    # No need to run the backward pass here, just run the forward pass to \Box
 → compute accuracy
    batch_accuracy2 = []
    real_accuracy = []
    rnd_idx = np.random.permutation(VAL_IMAGES)
    n_batches = VAL_IMAGES // batch_size
    for batch_idx in np.array_split(rnd_idx, n_batches):
        X_val_batch = X_val[batch_idx]
        y_val_batch = y_val[batch_idx]
        f_output2 = np.argmax(net.forward(X_val_batch), axis = 1)
        batch_accuracy2.extend(y_val_batch)
        real_accuracy.extend(f_output2)
    batch_array2, real_array = np.array(batch_accuracy2), np.array(real_accuracy)
    same_value_count = (batch_array2 == real_array).sum()
    val_accuracy_2sgd[epoch] = same_value_count / len(batch_accuracy2)
    learning_rate = learning_rate * learning_rate_decay
    print("epoch:", epoch, " ", "acc:", val_accuracy_2sgd[epoch], " ", "loss:", "
 →train_loss_2sgd[epoch])
    if val_accuracy_2sgd[epoch] > highest_accuracy:
        highest_accuracy = val_accuracy_2sgd[epoch]
        best_network = net
#print(highest_accuracy = val_accuracy_2sqd[epoch])
sgd_2_best = best_network
#print(train_accuracy, val_accuracy)
```

epoch: 0 acc: 0.413 loss: 1.7563669946069924 epoch: 1 acc: 0.443 loss: 1.5438423856611445

```
epoch: 2
           acc: 0.463
                         loss: 1.4599814710064292
epoch: 3
           acc: 0.494
                         loss: 1.3918972028592211
epoch: 4
           acc: 0.471
                         loss: 1.3392911948766097
epoch: 5
           acc: 0.493
                         loss: 1.2812650037289495
epoch: 6
           acc: 0.522
                         loss: 1.236780642646892
epoch: 7
           acc: 0.522
                         loss: 1.189345546707765
epoch: 8
           acc: 0.519
                         loss: 1.1518541454140006
epoch: 9
           acc: 0.521
                         loss: 1.104030650890289
epoch: 10
                          loss: 1.0581000375200234
            acc: 0.516
epoch: 11
            acc: 0.532
                          loss: 1.0293862920692654
epoch: 12
            acc: 0.52
                         loss: 0.9959116887023791
                         loss: 0.9554296541287884
epoch: 13
            acc: 0.53
epoch: 14
            acc: 0.527
                          loss: 0.9271799393712058
epoch: 15
            acc: 0.546
                          loss: 0.8933549138988446
epoch: 16
            acc: 0.505
                          loss: 0.8642675600931842
epoch: 17
                          loss: 0.8332728092188175
            acc: 0.515
epoch: 18
            acc: 0.534
                          loss: 0.8019122304678645
epoch: 19
            acc: 0.524
                          loss: 0.7765748372229494
epoch: 20
            acc: 0.531
                          loss: 0.7468079941339683
epoch: 21
            acc: 0.532
                          loss: 0.722425651597218
epoch: 22
            acc: 0.527
                          loss: 0.699578797573141
epoch: 23
            acc: 0.529
                          loss: 0.6773617496794496
epoch: 24
            acc: 0.529
                          loss: 0.651246669071911
            acc: 0.514
epoch: 25
                          loss: 0.6283432263374437
epoch: 26
            acc: 0.528
                          loss: 0.6058219020988505
epoch: 27
            acc: 0.521
                          loss: 0.5859774512133323
epoch: 28
                          loss: 0.5681205970182388
            acc: 0.536
epoch: 29
            acc: 0.519
                          loss: 0.5471216694465378
epoch: 30
            acc: 0.527
                          loss: 0.5272340784789056
epoch: 31
            acc: 0.529
                          loss: 0.5100077842787812
            acc: 0.539
epoch: 32
                          loss: 0.4933057201546159
epoch: 33
            acc: 0.525
                          loss: 0.4788375370565466
epoch: 34
            acc: 0.523
                          loss: 0.4623768897108158
epoch: 35
            acc: 0.529
                          loss: 0.45023317161971665
epoch: 36
            acc: 0.519
                          loss: 0.4358153345809717
epoch: 37
            acc: 0.519
                          loss: 0.4212805102898406
epoch: 38
            acc: 0.526
                          loss: 0.40940383584342005
epoch: 39
            acc: 0.532
                          loss: 0.39778599629098677
epoch: 40
            acc: 0.525
                          loss: 0.38771753374881535
epoch: 41
            acc: 0.522
                          loss: 0.37593970193022674
epoch: 42
            acc: 0.526
                          loss: 0.36701591723990157
epoch: 43
            acc: 0.523
                          loss: 0.3583325039232834
epoch: 44
            acc: 0.527
                          loss: 0.34990466669919207
epoch: 45
            acc: 0.519
                          loss: 0.34151229089079127
epoch: 46
            acc: 0.529
                          loss: 0.3335472648297409
epoch: 47
            acc: 0.518
                          loss: 0.3259827829548725
epoch: 48
            acc: 0.519
                          loss: 0.3194882269351194
epoch: 49
            acc: 0.527
                          loss: 0.3132660913254858
```

```
epoch: 50
            acc: 0.53
                        loss: 0.30714110153183893
epoch: 51
            acc: 0.531
                         loss: 0.301757441382403
epoch: 52
           acc: 0.526
                         loss: 0.29629948386607935
epoch: 53
            acc: 0.523
                         loss: 0.2917078403090416
epoch: 54
            acc: 0.516
                         loss: 0.2864945317770245
epoch: 55
            acc: 0.527
                         loss: 0.2816806259150947
epoch: 56
            acc: 0.524
                         loss: 0.2771672600751209
epoch: 57
            acc: 0.524
                         loss: 0.2738857265616342
epoch: 58
                         loss: 0.26977208521906676
            acc: 0.526
epoch: 59
            acc: 0.514
                         loss: 0.2668132504968874
epoch: 60
            acc: 0.514
                         loss: 0.2635206404631505
epoch: 61
                        loss: 0.26015206312248285
            acc: 0.52
epoch: 62
            acc: 0.518
                         loss: 0.25704643906467894
epoch: 63
                         loss: 0.2546543821996699
            acc: 0.527
epoch: 64
            acc: 0.518
                         loss: 0.2518163584626345
epoch: 65
            acc: 0.519
                         loss: 0.24924726829650862
epoch: 66
            acc: 0.527
                         loss: 0.247200100789656
epoch: 67
            acc: 0.524
                         loss: 0.2445837835702126
epoch: 68
            acc: 0.517
                         loss: 0.24253686323424595
epoch: 69
            acc: 0.523
                         loss: 0.24096948788379302
```

1.3 Train using 3 Layer SGD

To train our network we will use SGD. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
[4]: # Hyperparameters
     input\_size = 32 * 32 * 3
     num_layers = 3
     hidden_size = 150
     hidden_sizes = [hidden_size] * (num_layers - 1)
     num_classes = 10
     epochs = 70
     batch_size = 100
     learning_rate = 1e-1
     learning_rate_decay = 0.95
     regularization = 0.001
     # Initialize a new neural network model
     net = NeuralNetwork(input_size, hidden_sizes, num_classes, num_layers)
     # Variables to store performance for each epoch
     train_loss_3sgd = np.zeros(epochs)
     train_accuracy_3sgd = np.zeros(epochs)
     val_accuracy_3sgd = np.zeros(epochs)
```

```
highest_accuracy = -math.inf
best_network = 0
# For each epoch...
for epoch in range(epochs):
    #print('epoch:', epoch)
    # Shuffle the dataset
    #X_train, y_train = shuffle(X_train, y_train)
    # Training
    # For each mini-batch...
    batch_accuracy = []
    f_accuracy = []
    count = 0
    # https://stackoverflow.com/questions/8177079/
 \rightarrow take-the-content-of-a-list-and-append-it-to-another-list
    #https://stackoverflow.com/questions/60133145/
 \rightarrow neural-networks-from-scratch-problem-with-fit-method-when-i-attempt-to-use-mini
    rnd_idx = np.random.permutation(TRAIN_IMAGES)
    n_batches = TRAIN_IMAGES//batch_size
    for batch_idx in np.array_split(rnd_idx, n_batches):
        X_batch = X_train[batch_idx]
        y_batch = y_train[batch_idx]
        f_output = np.argmax(net.forward(X_batch), axis = 1)
        loss = net.backward(X_batch, y_batch, learning_rate, regularization)
        train_loss_3sgd[epoch] += loss
        batch_accuracy.extend(y_batch)
        f_accuracy.extend(f_output)
    #https://stackoverflow.com/questions/25490641/
 →check-how-many-elements-are-equal-in-two-numpy-arrays-python/25490691
    batch_array, f_array = np.array(batch_accuracy), np.array(f_accuracy)
    same_value_count = (batch_array == f_array).sum()
    train_accuracy_3sgd[epoch] = same_value_count / len(batch_accuracy)
    train_loss_3sgd[epoch] /= n_batches
    # Validation
    # No need to run the backward pass here, just run the forward pass to \Box
 \rightarrow compute accuracy
    batch_accuracy2 = []
    real_accuracy = []
    rnd_idx = np.random.permutation(VAL_IMAGES)
    n_batches = VAL_IMAGES // batch_size
    for batch_idx in np.array_split(rnd_idx, n_batches):
        X_val_batch = X_val[batch_idx]
        y_val_batch = y_val[batch_idx]
```

```
f_output2 = np.argmax(net.forward(X_val_batch), axis = 1)
    batch_accuracy2.extend(y_val_batch)
    real_accuracy.extend(f_output2)

batch_array2, real_array = np.array(batch_accuracy2), np.array(real_accuracy)
    same_value_count = (batch_array2 == real_array).sum()
    val_accuracy_3sgd[epoch] = same_value_count / len(batch_accuracy2)

learning_rate = learning_rate * learning_rate_decay
    print("epoch:", epoch, " ", "acc:", val_accuracy_3sgd[epoch], " ", "loss:", u

train_loss_3sgd[epoch])

if val_accuracy_3sgd[epoch] > highest_accuracy:
    highest_accuracy = val_accuracy_3sgd[epoch]
    best_network = net

sgd_3_best = best_network

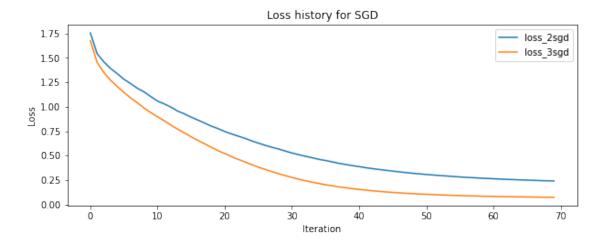
#print(train_accuracy, val_accuracy)
```

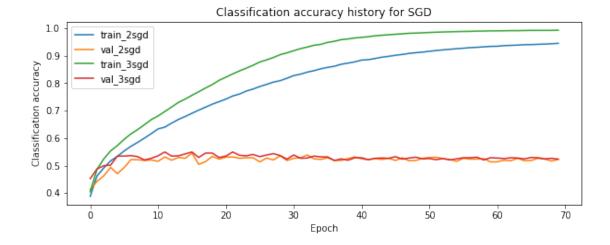
```
epoch: 0
          acc: 0.453
                       loss: 1.677004023009174
epoch: 1
          acc: 0.488
                       loss: 1.45379953649261
epoch: 2
          acc: 0.5
                     loss: 1.3503942934124455
epoch: 3
          acc: 0.502
                       loss: 1.2714836663385856
epoch: 4
          acc: 0.535
                       loss: 1.2072313849984577
epoch: 5
          acc: 0.535
                       loss: 1.1474144874895063
epoch: 6
          acc: 0.537
                       loss: 1.089623937519086
epoch: 7
          acc: 0.533
                       loss: 1.0401858125122139
epoch: 8
          acc: 0.521
                       loss: 0.9858961726096771
epoch: 9
           acc: 0.527
                       loss: 0.9398279342703992
epoch: 10
          acc: 0.536
                        loss: 0.8976653978214381
epoch: 11
           acc: 0.55
                       loss: 0.8561262059031347
epoch: 12
           acc: 0.535
                        loss: 0.8118510697673569
epoch: 13
           acc: 0.536
                        loss: 0.7702320045238036
epoch: 14
           acc: 0.543
                        loss: 0.7320647528822489
epoch: 15
                        loss: 0.6925576170680616
           acc: 0.55
epoch: 16
           acc: 0.53
                        loss: 0.6559131392959091
epoch: 17
           acc: 0.546
                        loss: 0.621298259701281
epoch: 18
           acc: 0.546
                         loss: 0.5858791756710477
epoch: 19
           acc: 0.53
                       loss: 0.5510466674917333
epoch: 20
           acc: 0.535
                        loss: 0.5211836212746989
epoch: 21
                        loss: 0.49002709488133167
           acc: 0.55
epoch: 22
           acc: 0.538
                        loss: 0.46188520469187094
epoch: 23
           acc: 0.536
                         loss: 0.4355002620764879
epoch: 24
           acc: 0.541
                        loss: 0.40856902617885754
epoch: 25
           acc: 0.533
                        loss: 0.3817903786313522
epoch: 26
           acc: 0.539
                        loss: 0.3594901382527652
epoch: 27
           acc: 0.544
                         loss: 0.33670577119408607
epoch: 28
           acc: 0.537
                        loss: 0.31499935217478275
```

```
epoch: 29
            acc: 0.524
                         loss: 0.2957583235544671
epoch: 30
            acc: 0.539
                         loss: 0.2766411366768283
epoch: 31
            acc: 0.527
                         loss: 0.2584630079169545
                         loss: 0.24338492427828637
epoch: 32
            acc: 0.528
epoch: 33
            acc: 0.535
                         loss: 0.22859972183867108
epoch: 34
                         loss: 0.215376542629848
            acc: 0.532
epoch: 35
            acc: 0.532
                         loss: 0.2016927290373801
epoch: 36
            acc: 0.519
                         loss: 0.1914267271535204
epoch: 37
                         loss: 0.17908581934523832
            acc: 0.525
epoch: 38
            acc: 0.52
                         loss: 0.1714844415081876
epoch: 39
            acc: 0.529
                         loss: 0.16169183725701966
epoch: 40
            acc: 0.529
                         loss: 0.15443954754005157
epoch: 41
            acc: 0.522
                         loss: 0.1466140476160938
epoch: 42
            acc: 0.527
                         loss: 0.13991024969530755
epoch: 43
            acc: 0.528
                         loss: 0.13404049682639296
epoch: 44
                         loss: 0.12834543681782018
            acc: 0.527
epoch: 45
            acc: 0.533
                         loss: 0.12323527077588133
epoch: 46
            acc: 0.524
                         loss: 0.1188967831827395
epoch: 47
            acc: 0.528
                         loss: 0.11445545037272246
epoch: 48
            acc: 0.531
                         loss: 0.11053452176646422
epoch: 49
            acc: 0.525
                         loss: 0.10728947916553591
epoch: 50
            acc: 0.526
                         loss: 0.103857689215035
epoch: 51
            acc: 0.522
                         loss: 0.10102401469290313
epoch: 52
            acc: 0.526
                         loss: 0.0981508253297874
epoch: 53
            acc: 0.521
                         loss: 0.09577580009807198
epoch: 54
            acc: 0.525
                         loss: 0.09345375002591083
                         loss: 0.0913514905968868
epoch: 55
            acc: 0.529
epoch: 56
            acc: 0.529
                         loss: 0.0891952829088873
epoch: 57
            acc: 0.531
                         loss: 0.08749426029238787
epoch: 58
            acc: 0.521
                         loss: 0.08573575274236875
epoch: 59
            acc: 0.529
                         loss: 0.08430591368606213
epoch: 60
            acc: 0.528
                         loss: 0.08276065118463065
epoch: 61
            acc: 0.526
                         loss: 0.08143878208804083
epoch: 62
            acc: 0.529
                         loss: 0.08009480476018839
epoch: 63
            acc: 0.528
                         loss: 0.07897881510265979
epoch: 64
            acc: 0.525
                         loss: 0.07789992750329727
epoch: 65
            acc: 0.53
                         loss: 0.07682062807604528
epoch: 66
            acc: 0.529
                         loss: 0.07585787440081536
epoch: 67
                         loss: 0.07488379334436962
            acc: 0.525
epoch: 68
            acc: 0.527
                         loss: 0.0741097806918038
epoch: 69
            acc: 0.524
                         loss: 0.07327738226395974
```

1.4 Graph loss and train/val accuracies for SGD

```
[5]: # Plot the loss function and train / validation accuracies
     plt.subplot(2, 1, 1)
     plt.plot(train_loss_2sgd, label = 'loss_2sgd')
     plt.plot(train_loss_3sgd, label = 'loss_3sgd')
     plt.title('Loss history for SGD')
     plt.xlabel('Iteration')
     plt.ylabel('Loss')
     plt.legend()
     plt.show()
     plt.subplot(2, 1, 2)
     plt.plot(train_accuracy_2sgd, label='train_2sgd')
     plt.plot(val_accuracy_2sgd, label='val_2sgd')
     plt.plot(train_accuracy_3sgd, label='train_3sgd')
     plt.plot(val_accuracy_3sgd, label='val_3sgd')
     plt.title('Classification accuracy history for SGD')
     plt.xlabel('Epoch')
     plt.ylabel('Classification accuracy')
     plt.legend()
     plt.show()
```





1.5 Train using 2 Layer Adam

To train our network we will use Adam. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
[6]: # Hyperparameters
     input_size = 32 * 32 * 3
     num_lavers = 2
     hidden_size = 150
     hidden_sizes = [hidden_size] * (num_layers - 1)
     num_classes = 10
     epochs = 70
     batch_size = 100
     learning_rate = 1e-3
     learning_rate_decay = 0.95
     regularization = 0.001
     beta_one = 0.9
     beta_two = 0.999
     epil = 1e-8
     # Initialize a new neural network model
     net = AdamNeuralNetwork(input_size, hidden_sizes, num_classes, num_layers)
     # Variables to store performance for each epoch
     train_loss_2adam = np.zeros(epochs)
     train_accuracy_2adam = np.zeros(epochs)
     val_accuracy_2adam = np.zeros(epochs)
```

```
highest_accuracy = -math.inf
best_network = 0
# For each epoch...
for epoch in range(epochs):
    #print('epoch:', epoch)
    # Shuffle the dataset
    #X_train, y_train = shuffle(X_train, y_train)
    # Training
    # For each mini-batch...
    batch_accuracy = []
    f_accuracy = []
    count = 0
    # https://stackoverflow.com/questions/8177079/
 \rightarrow take-the-content-of-a-list-and-append-it-to-another-list
    #https://stackoverflow.com/questions/60133145/
 \rightarrow neural-networks-from-scratch-problem-with-fit-method-when-i-attempt-to-use-mini
    rnd_idx = np.random.permutation(TRAIN_IMAGES)
    n_batches = TRAIN_IMAGES//batch_size
    time = 0
    for batch_idx in np.array_split(rnd_idx, n_batches):
        X_batch = X_train[batch_idx]
        y_batch = y_train[batch_idx]
        f_output = np.argmax(net.forward(X_batch), axis = 1)
        loss = net.backward(X_batch, y_batch, learning_rate, time, beta_one,__
 →beta_two, epil, regularization)
        train_loss_2adam[epoch] += loss
        batch_accuracy.extend(y_batch)
        f_accuracy.extend(f_output)
    #https://stackoverflow.com/questions/25490641/
 \rightarrow check-how-many-elements-are-equal-in-two-numpy-arrays-python/25490691
    batch_array, f_array = np.array(batch_accuracy), np.array(f_accuracy)
    same_value_count = (batch_array == f_array).sum()
    train_accuracy_2adam[epoch] = same_value_count / len(batch_accuracy)
    train_loss_2adam[epoch] /= n_batches
    # Validation
    # No need to run the backward pass here, just run the forward pass to_\sqcup
 →compute accuracy
    batch_accuracy2 = []
    real_accuracy = []
    rnd_idx = np.random.permutation(VAL_IMAGES)
    n_batches = VAL_IMAGES // batch_size
    for batch_idx in np.array_split(rnd_idx, n_batches):
```

```
X_val_batch = X_val[batch_idx]
        y_val_batch = y_val[batch_idx]
        f_output2 = np.argmax(net.forward(X_val_batch), axis = 1)
        batch_accuracy2.extend(y_val_batch)
        real_accuracy.extend(f_output2)
    batch_array2, real_array = np.array(batch_accuracy2), np.array(real_accuracy)
    same_value_count = (batch_array2 == real_array).sum()
    val_accuracy_2adam[epoch] = same_value_count / len(batch_accuracy2)
    learning_rate = learning_rate * learning_rate_decay
    print("epoch:", epoch, " ", "acc:", val_accuracy_2adam[epoch], " ", "loss:", u
 →train_loss_2adam[epoch])
    if val_accuracy_2adam[epoch] > highest_accuracy:
        highest_accuracy = val_accuracy_2adam[epoch]
        best network = net
sgd_2_best_adam = best_network
print(highest_accuracy)
#print(train_accuracy, val_accuracy)
```

```
epoch: 0
         acc: 0.455
                       loss: 1.781848481853594
epoch: 1 acc: 0.507 loss: 1.4215156700911995
epoch: 2 acc: 0.502 loss: 1.3271816608662605
epoch: 3 acc: 0.506 loss: 1.2755329343779374
epoch: 4
         acc: 0.485 loss: 1.2290071052401057
epoch: 5
         acc: 0.51
                      loss: 1.19420813474105
epoch: 6
          acc: 0.529
                      loss: 1.154756255361247
epoch: 7
          acc: 0.53
                      loss: 1.1247534765364682
epoch: 8
          acc: 0.529
                       loss: 1.0950878174020258
epoch: 9
          acc: 0.5
                     loss: 1.0688436459006527
epoch: 10
                       loss: 1.0432271910549251
          acc: 0.52
epoch: 11
          acc: 0.519
                        loss: 1.0191682381363585
epoch: 12
                        loss: 0.9936166995061683
          acc: 0.532
epoch: 13
           acc: 0.519
                        loss: 0.9760135965351561
epoch: 14 acc: 0.523
                        loss: 0.9517511006939997
epoch: 15
           acc: 0.529
                        loss: 0.9292873752617823
epoch: 16 acc: 0.535
                        loss: 0.9118295479212173
epoch: 17
           acc: 0.526
                        loss: 0.894332710401648
                        loss: 0.8768767273358347
epoch: 18
           acc: 0.535
epoch: 19
           acc: 0.516
                        loss: 0.8595064917616229
epoch: 20
           acc: 0.538
                        loss: 0.8459411864814331
epoch: 21
           acc: 0.537
                        loss: 0.8292626498421413
epoch: 22
           acc: 0.539
                        loss: 0.8139482023532268
epoch: 23
           acc: 0.539
                        loss: 0.7992217949414239
epoch: 24
           acc: 0.529
                        loss: 0.7882500648581292
           acc: 0.523
epoch: 25
                        loss: 0.7749307679800699
```

```
epoch: 26
            acc: 0.531
                          loss: 0.7615660727751893
epoch: 27
            acc: 0.534
                          loss: 0.7534513010837615
epoch: 28
            acc: 0.529
                          loss: 0.7405757699037835
epoch: 29
            acc: 0.543
                          loss: 0.7291112188397215
epoch: 30
                          loss: 0.7186323274840272
            acc: 0.528
epoch: 31
                         loss: 0.70983000527058
            acc: 0.55
epoch: 32
            acc: 0.54
                         loss: 0.7007016337439341
epoch: 33
            acc: 0.526
                          loss: 0.6928355958573388
epoch: 34
                          loss: 0.6832453685174167
            acc: 0.519
epoch: 35
            acc: 0.542
                          loss: 0.6767654610983624
epoch: 36
            acc: 0.515
                          loss: 0.6680194073307174
epoch: 37
            acc: 0.535
                          loss: 0.6611657172185718
epoch: 38
            acc: 0.536
                          loss: 0.6569975052432504
epoch: 39
            acc: 0.53
                         loss: 0.6478375762047177
epoch: 40
            acc: 0.527
                          loss: 0.6422494132459349
epoch: 41
            acc: 0.525
                          loss: 0.6360803037534456
epoch: 42
            acc: 0.535
                          loss: 0.6309443951003592
epoch: 43
            acc: 0.531
                          loss: 0.6260101047374886
epoch: 44
            acc: 0.535
                          loss: 0.619851770481345
epoch: 45
            acc: 0.526
                          loss: 0.6153586822405722
epoch: 46
            acc: 0.531
                          loss: 0.6104508262444146
epoch: 47
            acc: 0.534
                          loss: 0.6063335428559846
epoch: 48
            acc: 0.526
                          loss: 0.6026869237499377
epoch: 49
                          loss: 0.5991283438611519
            acc: 0.532
epoch: 50
            acc: 0.526
                          loss: 0.5941353287779787
                          loss: 0.5918242225920124
epoch: 51
            acc: 0.527
epoch: 52
                          loss: 0.5873000644489106
            acc: 0.531
epoch: 53
            acc: 0.525
                          loss: 0.5842291593354041
epoch: 54
            acc: 0.532
                          loss: 0.5808482525748033
epoch: 55
            acc: 0.534
                          loss: 0.5786273168354464
epoch: 56
            acc: 0.534
                          loss: 0.5756837558770033
epoch: 57
            acc: 0.533
                          loss: 0.5728897270341072
epoch: 58
            acc: 0.536
                          loss: 0.5703073632336896
epoch: 59
            acc: 0.533
                          loss: 0.5678374946187219
epoch: 60
            acc: 0.54
                         loss: 0.5658667916195199
epoch: 61
            acc: 0.531
                          loss: 0.5631288553140954
epoch: 62
            acc: 0.534
                          loss: 0.5611535719637392
epoch: 63
            acc: 0.528
                          loss: 0.5595607072817882
epoch: 64
            acc: 0.528
                          loss: 0.5575766365714184
epoch: 65
            acc: 0.529
                          loss: 0.5558428471341006
epoch: 66
            acc: 0.534
                          loss: 0.5539401323140312
epoch: 67
            acc: 0.525
                          loss: 0.5525525410563583
epoch: 68
            acc: 0.531
                          loss: 0.55075918248299
epoch: 69
            acc: 0.535
                          loss: 0.5495847779907489
0.55
```

1.6 Train using 3 Layer Adam

To train our network we will use Adam. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
[14]: # Hyperparameters
      input_size = 32 * 32 * 3
      num_layers = 3
      hidden_size = 150
      hidden_sizes = [hidden_size] * (num_layers - 1)
      num_classes = 10
      epochs = 70
      batch_size = 100
      learning_rate = 1e-3
      learning_rate_decay = 0.95
      regularization = 0.001
      beta_one = 0.9
      beta_two = 0.999
      epil = 1e-8
      # Initialize a new neural network model
      net = AdamNeuralNetwork(input_size, hidden_sizes, num_classes, num_layers)
      # Variables to store performance for each epoch
      train_loss_3adam = np.zeros(epochs)
      train_accuracy_3adam = np.zeros(epochs)
      val_accuracy_3adam = np.zeros(epochs)
      highest_accuracy = -math.inf
      best_network = 0
      # For each epoch...
      for epoch in range(epochs):
          #print('epoch:', epoch)
          # Shuffle the dataset
          #X_train, y_train = shuffle(X_train, y_train)
          # Training
          # For each mini-batch...
          batch_accuracy = []
          f_accuracy = []
          count = 0
          # https://stackoverflow.com/questions/8177079/
       \rightarrow take-the-content-of-a-list-and-append-it-to-another-list
```

```
#https://stackoverflow.com/questions/60133145/
\rightarrow neural-networks-from-scratch-problem-with-fit-method-when-i-attempt-to-use-mini
  rnd_idx = np.random.permutation(TRAIN_IMAGES)
  n_batches = TRAIN_IMAGES//batch_size
  time = 0
  for batch_idx in np.array_split(rnd_idx, n_batches):
      X_batch = X_train[batch_idx]
      y_batch = y_train[batch_idx]
      f_output = np.argmax(net.forward(X_batch), axis = 1)
      loss = net.backward(X_batch, y_batch, learning_rate, time, beta_one,__
→beta_two, epil, regularization)
      train_loss_3adam[epoch] += loss
      batch_accuracy.extend(y_batch)
      f_accuracy.extend(f_output)
   #https://stackoverflow.com/questions/25490641/
→check-how-many-elements-are-equal-in-two-numpy-arrays-python/25490691
  batch_array, f_array = np.array(batch_accuracy), np.array(f_accuracy)
  same_value_count = (batch_array == f_array).sum()
  train_accuracy_3adam[epoch] = same_value_count / len(batch_accuracy)
  train_loss_3adam[epoch] /= n_batches
   # Validation
   → compute accuracy
  batch_accuracy2 = []
  real_accuracy = []
  rnd_idx = np.random.permutation(VAL_IMAGES)
  n_batches = VAL_IMAGES // batch_size
  for batch_idx in np.array_split(rnd_idx, n_batches):
      X_val_batch = X_val[batch_idx]
      y_val_batch = y_val[batch_idx]
      f_output2 = np.argmax(net.forward(X_val_batch), axis = 1)
      batch_accuracy2.extend(y_val_batch)
      real_accuracy.extend(f_output2)
  batch_array2, real_array = np.array(batch_accuracy2), np.array(real_accuracy)
  same_value_count = (batch_array2 == real_array).sum()
  val_accuracy_3adam[epoch] = same_value_count / len(batch_accuracy2)
  learning_rate = learning_rate * learning_rate_decay
  print("epoch:", epoch, " ", "acc:", val_accuracy_3adam[epoch], " ", "loss:", u
→train_loss_3adam[epoch])
  if val_accuracy_3adam[epoch] > highest_accuracy:
      highest_accuracy = val_accuracy_3adam[epoch]
      best_network = net
```

sgd_3_best_adam = best_network print(highest_accuracy) #print(train_accuracy, val_accuracy)

```
loss: 1.695785622456197
epoch: 0
           acc: 0.443
epoch: 1
                         loss: 1.4349419417617093
           acc: 0.482
epoch: 2
           acc: 0.498
                         loss: 1.337647648172673
epoch: 3
           acc: 0.509
                         loss: 1.2636183772759182
epoch: 4
           acc: 0.51
                        loss: 1.208515871832974
epoch: 5
           acc: 0.519
                         loss: 1.1555652605012536
epoch: 6
           acc: 0.524
                         loss: 1.1099358302035622
epoch: 7
                         loss: 1.0691541169977619
           acc: 0.526
epoch: 8
           acc: 0.525
                         loss: 1.0302290742688571
epoch: 9
           acc: 0.539
                         loss: 0.9955487992393077
epoch: 10
            acc: 0.519
                          loss: 0.9589991222603809
epoch: 11
            acc: 0.529
                          loss: 0.9246341263139255
epoch: 12
            acc: 0.537
                          loss: 0.8977564416436331
epoch: 13
            acc: 0.524
                          loss: 0.8676460375672775
epoch: 14
            acc: 0.542
                          loss: 0.838806086528868
epoch: 15
            acc: 0.521
                          loss: 0.8138471652958539
epoch: 16
            acc: 0.523
                          loss: 0.787427493895793
epoch: 17
            acc: 0.553
                          loss: 0.7637115132717165
epoch: 18
            acc: 0.526
                          loss: 0.7421986144563922
epoch: 19
                          loss: 0.7197181957468192
            acc: 0.535
epoch: 20
            acc: 0.536
                          loss: 0.6972338024747221
epoch: 21
                          loss: 0.6791092822887249
            acc: 0.534
epoch: 22
            acc: 0.52
                         loss: 0.6607535171627347
epoch: 23
            acc: 0.538
                          loss: 0.6420326299914598
epoch: 24
                          loss: 0.6227775324514834
            acc: 0.535
epoch: 25
            acc: 0.523
                          loss: 0.607008924831012
epoch: 26
            acc: 0.525
                          loss: 0.5928696041234346
epoch: 27
            acc: 0.52
                         loss: 0.5774938586144541
epoch: 28
            acc: 0.535
                          loss: 0.5634221850152258
epoch: 29
            acc: 0.536
                          loss: 0.5505526434679565
epoch: 30
            acc: 0.533
                          loss: 0.5388774524582731
epoch: 31
                          loss: 0.5260930796628566
            acc: 0.532
epoch: 32
            acc: 0.529
                          loss: 0.5153074824454947
epoch: 33
            acc: 0.54
                         loss: 0.5046332809115942
epoch: 34
            acc: 0.523
                          loss: 0.4944624123586097
epoch: 35
            acc: 0.521
                          loss: 0.4849217970528342
epoch: 36
            acc: 0.516
                          loss: 0.4749705861681502
epoch: 37
            acc: 0.527
                          loss: 0.46735566480727947
epoch: 38
            acc: 0.532
                          loss: 0.45670911866997477
epoch: 39
                          loss: 0.44936412533368064
            acc: 0.517
epoch: 40
            acc: 0.522
                          loss: 0.44212804147397816
epoch: 41
            acc: 0.526
                          loss: 0.4348712669618535
epoch: 42
            acc: 0.53
                         loss: 0.4280145822256825
```

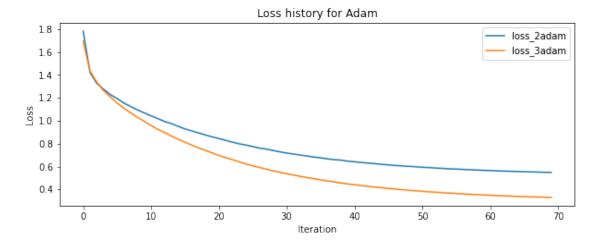
```
epoch: 43
            acc: 0.518
                         loss: 0.42176413913112726
epoch: 44
            acc: 0.524
                         loss: 0.41585553552184956
epoch: 45
           acc: 0.52
                        loss: 0.4096427615124636
epoch: 46
            acc: 0.519
                         loss: 0.40406487696911075
epoch: 47
            acc: 0.527
                         loss: 0.39899573873757155
epoch: 48
                         loss: 0.39341209966365626
            acc: 0.514
epoch: 49
           acc: 0.535
                         loss: 0.38927909343304684
epoch: 50
            acc: 0.526
                         loss: 0.3844557162836823
epoch: 51
           acc: 0.525
                         loss: 0.3801241809623601
epoch: 52
            acc: 0.533
                         loss: 0.3764500853599727
epoch: 53
            acc: 0.525
                         loss: 0.3724487310741941
epoch: 54
                         loss: 0.36889221466797584
            acc: 0.528
epoch: 55
            acc: 0.523
                         loss: 0.36557442128421136
epoch: 56
                         loss: 0.361997894084862
            acc: 0.525
epoch: 57
            acc: 0.531
                         loss: 0.35836412516543265
epoch: 58
            acc: 0.535
                         loss: 0.3559525103520796
epoch: 59
            acc: 0.518
                         loss: 0.35328963406948205
epoch: 60
           acc: 0.523
                         loss: 0.350248227089357
epoch: 61
            acc: 0.522
                         loss: 0.3477245600699434
epoch: 62
            acc: 0.526
                         loss: 0.34542030967086956
epoch: 63
           acc: 0.53
                        loss: 0.3428098360003228
epoch: 64
           acc: 0.526
                         loss: 0.34071922942417454
epoch: 65
           acc: 0.528
                         loss: 0.33866178830843063
           acc: 0.519
epoch: 66
                         loss: 0.3370056623940969
epoch: 67
           acc: 0.52
                        loss: 0.33486720605681053
epoch: 68
            acc: 0.531
                         loss: 0.33307852575230334
epoch: 69
            acc: 0.518
                         loss: 0.33191046827364284
0.553
```

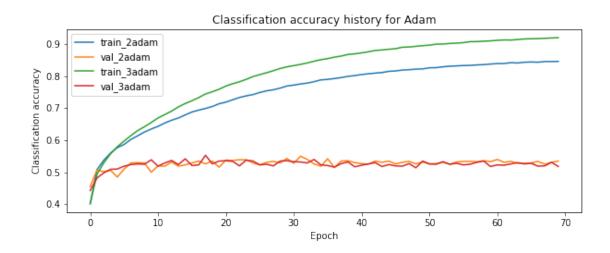
1.7 Graph loss and train/val accuracies for Adam

```
[15]: # Plot the loss function and train / validation accuracies
    plt.subplot(2, 1, 1)
    plt.plot(train_loss_2adam, label='loss_2adam')
    plt.plot(train_loss_3adam, label='loss_3adam')
    plt.title('Loss history for Adam')
    plt.xlabel('Iteration')
    plt.ylabel('Loss')
    plt.legend()
    plt.show()

plt.subplot(2, 1, 2)
    plt.plot(train_accuracy_2adam, label='train_2adam')
```

```
plt.plot(val_accuracy_2adam, label='val_2adam')
plt.plot(train_accuracy_3adam, label='train_3adam')
plt.plot(val_accuracy_3adam, label='val_3adam')
plt.title('Classification accuracy history for Adam')
plt.xlabel('Epoch')
plt.ylabel('Classification accuracy')
plt.legend()
plt.show()
```





1.8 Hyperparameter tuning

Once you have successfully trained a network you can tune your hyparameters to increase your accuracy.

Based on the graphs of the loss function above you should be able to develop some intuition about

what hyperparameter adjustments may be necessary. A very noisy loss implies that the learning rate might be too high, while a linearly decreasing loss would suggest that the learning rate may be too low. A large gap between training and validation accuracy would suggest overfitting due to large model without much regularization. No gap between training and validation accuracy would indicate low model capacity.

You will compare networks of two and three layers using the different optimization methods you implemented.

The different hyperparameters you can experiment with are: - Batch size: We recommend you leave this at 200 initially which is the batch size we used. - Number of iterations: You can gain an intuition for how many iterations to run by checking when the validation accuracy plateaus in your train/val accuracy graph. - Initialization Weight initialization is very important for neural networks. We used the initialization W = np.random.randn(n) / sqrt(n) where n is the input dimension for layer corresponding to W. We recommend you stick with the given initializations, but you may explore modifying these. Typical initialization practices: http://cs231n.github.io/neural-networks-2/#init - Learning rate: Generally from around 1e-4 to 1e-1 is a good range to explore according to our implementation. - Learning rate decay: We recommend a 0.95 decay to start. - Hidden layer size: You should explore up to around 120 units per layer. For three-layer network, we fixed the two hidden layers to be the same size when obtaining the target numbers. However, you may experiment with having different size hidden layers. - Regularization coefficient: We recommend trying values in the range 0 to 0.1.

Hints: - After getting a sense of the parameters by trying a few values yourself, you will likely want to write a few for-loops to traverse over a set of hyperparameters. - If you find that your train loss is decreasing, but your train and val accuracy start to decrease rather than increase, your model likely started minimizing the regularization term. To prevent this you will need to decrease the regularization coefficient.

```
[20]: # Hyperparameters Tuning
      input\_size = 32 * 32 * 3
      num_layers = 2
      hidden_size = 25
      hidden_sizes = [hidden_size] * (num_layers - 1)
      num_classes = 10
      epochs = 50
      batch_size = 100
      learning_rate = 1e-1
      learning_rate_decay = 0.95
      regularization = 0.1
      # Initialize a new neural network model
      net = NeuralNetwork(input_size, hidden_sizes, num_classes, num_layers)
      # Variables to store performance for each epoch
      train_loss_2sgd_tune = np.zeros(epochs)
      train_accuracy_2sgd_tune = np.zeros(epochs)
      val_accuracy_2sgd_tune = np.zeros(epochs)
```

```
highest_accuracy = -math.inf
best_network = 0
# For each epoch...
for epoch in range(epochs):
    #print('epoch:', epoch)
    # Shuffle the dataset
    #X_train, y_train = shuffle(X_train, y_train)
    # Training
    # For each mini-batch...
   batch_accuracy = []
    f_accuracy = []
    count = 0
    # https://stackoverflow.com/questions/8177079/
 \rightarrow take-the-content-of-a-list-and-append-it-to-another-list
    #https://stackoverflow.com/questions/60133145/
 \rightarrow neural-networks-from-scratch-problem-with-fit-method-when-i-attempt-to-use-mini
    rnd_idx = np.random.permutation(TRAIN_IMAGES)
    n_batches = TRAIN_IMAGES//batch_size
    for batch_idx in np.array_split(rnd_idx, n_batches):
        X_batch = X_train[batch_idx]
        y_batch = y_train[batch_idx]
        f_output = np.argmax(net.forward(X_batch), axis = 1)
        loss = net.backward(X_batch, y_batch, learning_rate, regularization)
        train_loss_2sgd_tune[epoch] += loss
        batch_accuracy.extend(y_batch)
        f_accuracy.extend(f_output)
    #https://stackoverflow.com/questions/25490641/
 →check-how-many-elements-are-equal-in-two-numpy-arrays-python/25490691
    batch_array, f_array = np.array(batch_accuracy), np.array(f_accuracy)
    same_value_count = (batch_array == f_array).sum()
    train_accuracy_2sgd_tune[epoch] = same_value_count / len(batch_accuracy)
    train_loss_2sgd_tune[epoch] /= n_batches
    # Validation
    # No need to run the backward pass here, just run the forward pass to,
 \rightarrow compute accuracy
    batch_accuracy2 = []
    real_accuracy = []
    rnd_idx = np.random.permutation(VAL_IMAGES)
    n_batches = VAL_IMAGES // batch_size
    for batch_idx in np.array_split(rnd_idx, n_batches):
        X_val_batch = X_val[batch_idx]
        y_val_batch = y_val[batch_idx]
        f_output2 = np.argmax(net.forward(X_val_batch), axis = 1)
```

```
batch_accuracy2.extend(y_val_batch)
    real_accuracy.extend(f_output2)

batch_array2, real_array = np.array(batch_accuracy2), np.array(real_accuracy)
    same_value_count = (batch_array2 == real_array).sum()
    val_accuracy_2sgd_tune[epoch] = same_value_count / len(batch_accuracy2)

learning_rate = learning_rate * learning_rate_decay
    print("epoch:", epoch, " ", "acc:", val_accuracy_2sgd_tune[epoch], " ",

"loss:", train_loss_2sgd_tune[epoch])

if val_accuracy_2sgd_tune[epoch] > highest_accuracy:
    highest_accuracy = val_accuracy_2sgd_tune[epoch]
    best_network = net

#print(highest_accuracy = val_accuracy_2sgd[epoch])
sgd_2_best_tune = best_network

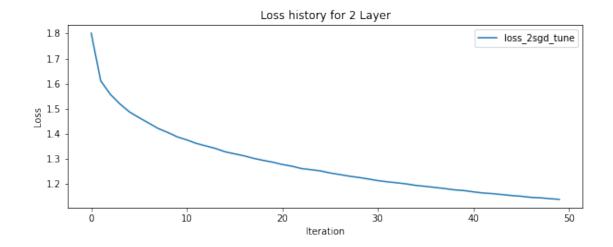
#print(train_accuracy, val_accuracy)
```

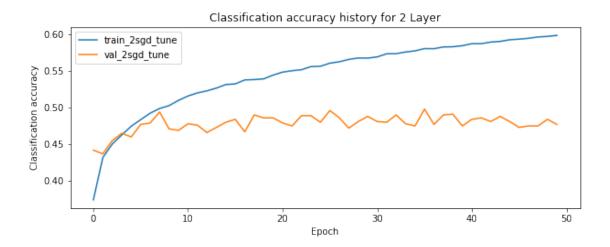
```
epoch: 0
          acc: 0.442
                       loss: 1.8008444256987126
epoch: 1
          acc: 0.437
                       loss: 1.611029937709001
          acc: 0.455
epoch: 2
                       loss: 1.557684436982191
epoch: 3
         acc: 0.465 loss: 1.5194882445381626
epoch: 4
         acc: 0.46
                      loss: 1.487650026603168
epoch: 5
          acc: 0.477
                       loss: 1.464897963941532
epoch: 6
          acc: 0.479
                       loss: 1.4435274695184899
epoch: 7
          acc: 0.494
                       loss: 1.421720912199226
epoch: 8
          acc: 0.471
                       loss: 1.405974528093507
epoch: 9
          acc: 0.469
                       loss: 1.3883570471806888
epoch: 10
          acc: 0.478
                        loss: 1.3760785631736878
epoch: 11
          acc: 0.476
                        loss: 1.362307455376832
epoch: 12
           acc: 0.466
                        loss: 1.3520588663381863
epoch: 13
                        loss: 1.3422022081620555
           acc: 0.473
epoch: 14
           acc: 0.48
                       loss: 1.3288786230150236
epoch: 15
           acc: 0.484
                        loss: 1.3206803529549533
epoch: 16
           acc: 0.467
                        loss: 1.3128390576432816
epoch: 17
           acc: 0.49
                       loss: 1.302610722987751
epoch: 18
           acc: 0.486
                        loss: 1.2946451837291582
epoch: 19
           acc: 0.486
                        loss: 1.2874666959732848
epoch: 20
           acc: 0.479
                        loss: 1.2781390320584836
epoch: 21
                        loss: 1.2715903308143137
           acc: 0.475
epoch: 22
           acc: 0.489
                        loss: 1.2621895831402514
epoch: 23
           acc: 0.489
                        loss: 1.2574908820048958
epoch: 24
           acc: 0.48
                       loss: 1.2526596733617423
epoch: 25
           acc: 0.496
                        loss: 1.2445091814835614
epoch: 26
           acc: 0.486
                        loss: 1.2383504420328693
epoch: 27
           acc: 0.472
                        loss: 1.231774455634069
epoch: 28
           acc: 0.481
                        loss: 1.2265772303853162
```

```
epoch: 29
            acc: 0.488
                         loss: 1.2206010136872816
epoch: 30
            acc: 0.481
                         loss: 1.214059339534931
epoch: 31
           acc: 0.48
                        loss: 1.20922372582806
epoch: 32
            acc: 0.49
                        loss: 1.2052462793108731
epoch: 33
            acc: 0.478
                         loss: 1.2008297663977063
epoch: 34
            acc: 0.475
                         loss: 1.1949063440052996
epoch: 35
           acc: 0.498
                         loss: 1.1911228617620973
epoch: 36
            acc: 0.477
                         loss: 1.1867454599291403
epoch: 37
            acc: 0.49
                        loss: 1.1824755758406962
epoch: 38
            acc: 0.491
                         loss: 1.177316755723951
                         loss: 1.1744851048010752
epoch: 39
            acc: 0.475
epoch: 40
                         loss: 1.1693162729161617
            acc: 0.484
                         loss: 1.1648293416665758
epoch: 41
            acc: 0.486
epoch: 42
            acc: 0.481
                         loss: 1.1622548887285458
epoch: 43
            acc: 0.488
                         loss: 1.1584692725388686
epoch: 44
            acc: 0.481
                         loss: 1.154465576847213
epoch: 45
            acc: 0.473
                         loss: 1.1516646826346773
epoch: 46
            acc: 0.475
                         loss: 1.147423874490345
epoch: 47
            acc: 0.475
                         loss: 1.1455399725879165
epoch: 48
            acc: 0.484
                         loss: 1.1422660960441715
epoch: 49
            acc: 0.477
                         loss: 1.1393723519596815
```

1.9 Graph loss and train/val accuracies for 2 Layer after tuning

```
[21]: # Plot the loss function and train / validation accuracies
      plt.subplot(2, 1, 1)
      plt.plot(train_loss_2sgd_tune, label='loss_2sgd_tune')
      plt.title('Loss history for 2 Layer')
      plt.xlabel('Iteration')
      plt.ylabel('Loss')
      plt.legend()
      plt.show()
      plt.subplot(2, 1, 2)
      plt.plot(train_accuracy_2sgd_tune, label='train_2sgd_tune')
      plt.plot(val_accuracy_2sgd_tune, label='val_2sgd_tune')
      plt.title('Classification accuracy history for 2 Layer')
      plt.xlabel('Epoch')
      plt.ylabel('Classification accuracy')
      plt.legend()
      plt.show()
```





1.10 Run on the test set

When you are done experimenting, you should evaluate your final trained networks on the test set.

```
[22]: best_2layer_sgd_prediction = np.argmax(sgd_2_best.forward(X_test), axis = 1)
   best_3layer_sgd_prediction = np.argmax(sgd_3_best.forward(X_test), axis = 1)
   best_2layer_adam_prediction = np.argmax(sgd_2_best_adam.forward(X_test), axis = 1)
   best_3layer_adam_prediction = np.argmax(sgd_3_best_adam.forward(X_test), axis = 1)
   best_3layer_adam_prediction = np.argmax(sgd_3_best_adam.forward(X_test), axis = 1)
```

1.11 Kaggle output

Once you are satisfied with your solution and test accuracy, output a file to submit your test set predictions to the Kaggle for Assignment 2 Neural Network. Use the following code to do so:

```
[23]: output_submission_csv('kaggle/nn_2layer_sgd_submission.csv', □

→best_2layer_sgd_prediction)

output_submission_csv('kaggle/nn_3layer_sgd_submission.csv', □

→best_3layer_sgd_prediction)

output_submission_csv('kaggle/nn_2layer_adam_submission.csv', □

→best_2layer_adam_prediction)

output_submission_csv('kaggle/nn_3layer_adam_submission.csv', □

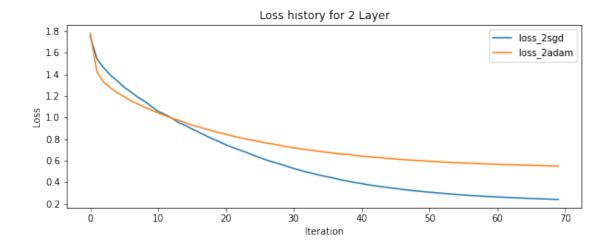
→best_3layer_adam_prediction)
```

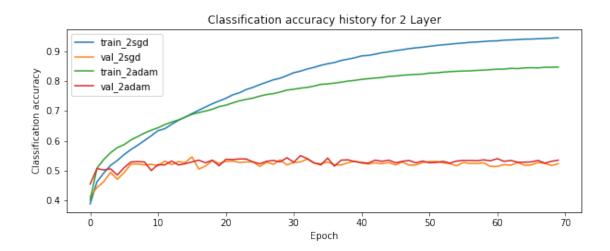
1.12 Compare SGD and Adam

Create graphs to compare training loss and validation accuracy between SGD and Adam. The code is similar to the above code, but instead of comparing train and validation, we are comparing SGD and Adam.

1.13 Graph loss and train/val accuracies for 2 Layer

```
[24]: # Plot the loss function and train / validation accuracies
      plt.subplot(2, 1, 1)
      plt.plot(train_loss_2sgd, label='loss_2sgd')
      plt.plot(train_loss_2adam, label='loss_2adam')
      plt.title('Loss history for 2 Layer')
      plt.xlabel('Iteration')
      plt.ylabel('Loss')
      plt.legend()
      plt.show()
      plt.subplot(2, 1, 2)
      plt.plot(train_accuracy_2sgd, label='train_2sgd')
      plt.plot(val_accuracy_2sgd, label='val_2sgd')
      plt.plot(train_accuracy_2adam, label='train_2adam')
      plt.plot(val_accuracy_2adam, label='val_2adam')
      plt.title('Classification accuracy history for 2 Layer')
      plt.xlabel('Epoch')
      plt.ylabel('Classification accuracy')
      plt.legend()
      plt.show()
```





1.14 Graph loss and train/val accuracies for 3 Layer

```
[25]: # Plot the loss function and train / validation accuracies
plt.subplot(2, 1, 1)
plt.plot(train_loss_3sgd, label='loss_3sgd')
plt.plot(train_loss_3adam, label='loss_3adam')
plt.title('Loss history for 3 Layer')
plt.xlabel('Iteration')
plt.ylabel('Loss')
plt.legend()
```

```
plt.show()

plt.subplot(2, 1, 2)

plt.plot(train_accuracy_3sgd, label='train_3sgd')

plt.plot(val_accuracy_3sgd, label='val_3sgd')

plt.plot(train_accuracy_3adam, label='train_3adam')

plt.plot(val_accuracy_3adam, label='val_3adam')

plt.title('Classification accuracy history for 3 Layer')

plt.xlabel('Epoch')

plt.ylabel('Classification accuracy')

plt.legend()

plt.show()
```

