# The Relational Model

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#### Recap

- The relational model is based on the concept of a relation or table.
- Two example relations:

Teams	Name	Home Field	Coach
	Rangers	Runnymede CI	Tarvo Sinervo
	Ducks	Humber Public	Tracy Zheng
	Choppers	High Park	Ammar Jalali

Games	Home team	Away team	Home goals	Away goals
	Rangers	Ducks	3	0
	Ducks	Choppers	1	1
	Rangers	Choppers	4	2
(2) TOO DO	Choppers	Ducks	0	5

#### Relations in Math

- A domain is a set of values.
- Suppose D<sub>1</sub>, D<sub>2</sub>, ... D<sub>n</sub> are domains.
  - -The Cartesian product  $D_1 \times D_2 \times ... \times D_n$  is the set of all tuples  $\langle d_1, d_2, ..., d_n \rangle$  such that  $d_1 \in D_1, d_2 \in D_2, ..., d_n \in D_n$ .
  - I.e., every combination of
     a value from D₁, a value from D₂ etc.
- A (mathematical) relation on D<sub>1</sub>, D<sub>2</sub>, ... D<sub>n</sub> is a subset of the Cartesian product.



### Example

- Example of a mathematical relation:
  - Let  $A = \{p, q, r, s\}, B = \{1, 2, 3\} \text{ and } C = \{100, 200\}.$
  - $-R = \{ \langle q, 2, 100 \rangle, \langle s, 3, 200 \rangle, \langle p, 1, 200 \rangle \}$  is a relation on A, B, C.
- Our database tables are relations too.
- Example:

```
{<Rangers, Ducks, 3, 0>, <Ducks, Choppers, 1, 1>, <Rangers, Choppers, 4, 2>, <Choppers, Ducks, 0, 5>}
```



#### Relation schemas vs instances

Schema: definition of the structure of the relation. Example:

Teams have 3 attributes: name, home field, coach. No two teams can have the same name.

- Notation for expressing a relation's schema Teams(Name, HomeField, Coach)
- Instance: particular data in the relation.
- Instances change constantly; schemas rarely.
- Conventional databases store the current version of the data. Databases that record the history are called *temporal* databases.



## Terminology

#### **Teams**

Name	Home Field	Coach
Rangers	Runnymede CI	Tarvo Sinervo
Ducks	Humber Public	Tracy Zheng
Choppers	High Park	Ammar Jalali
Crullers	WTCS	Anna Liu

- relation (table)
- attribute (column)
- tuple (row)
- arity of a relation: number of attributes
- cardinality of a relation: number of tuples



#### Relations are sets

- A relation is a **set** of tuples, which means:
  - there can be no duplicate tuples
  - order of the tuples doesn't matter
- In another model, relations are bags
  - -aka *multi-sets*
  - -allows duplicates
- Most commercial DBMSs use bag model.
- But for now, we will stick with relations as sets.



#### Database schemas and instances

- Database schema: a set of relation schemas
- Database instance: a set of relation instances



### A schema for our league data

Teams(name, homefield, coach)
Games(hometeam, awayteam, homegoals, awaygoals)

- Can there be >1 team with the same name?
  - Didn't happen in our dataset, but could it?
  - That's up to the league, not us!
- Suppose the league wants to allow
  - multiple teams with same name
  - multiple teams with same home field
- The schema allows it: nothing says otherwise.
- But what if the league wants to disallow
  - multiple teams with the same name *and* home field?

### Constraining the data

- More formally: 

   tuples t₁ and t₂ such that
   (t₁.name = t₂.name)∧
   (t₁.homefield = t₂.homefield)
- Implication: If we know the values for {name, homefield}, we can look up *exactly* one team in the relation.
- I.e., attributes {name, homefield} uniquely identify tuples in this relation.
- We say that {name, homefield} is a "superkey" for relation Teams.



## Superkeys

• Informally:

A **superkey** is a set of one or more attributes whose combined values are unique.

- I.e., no two tuples can have the same values on all of these attributes.
- Formally:

If attributes a<sub>1</sub>, a<sub>2</sub>, ..., a<sub>n</sub> form a superkey for relation R, ∄ tuples t<sub>1</sub> and t<sub>2</sub> such that

$$(t_1.a_1 = t_2.a_1) \wedge (t_1.a_2 = t_2.a_2) \wedge \dots \wedge (t_1.a_n = t_2.a_n)$$



#### Example

- Course(dept, number, name, breadth)
  - -One tuple might be <"csc", "343", "Introduction to Databases", True>
- Suppose our knowledge of the domain tells us that no two tuples can have the same value for dept and number.
- This means that {dept, number} is a superkey.
- This is a constraint on what can go in the relation.
- Create an instance of Course that violates it.
- Does every relation have a superkey?



### Keeping it minimal

- If {dept, number} is a superkey, then so is {dept, number, name}.
  - -This follows from the definition.
- But we are more interested in a *minimal* set of attributes with the superkey property.
  - -Minimal in the sense that no attributes can be removed from the superkey without making it no longer a superkey.



#### Keys

- key: a minimal superkey.
- In the schema, by convention we often
  - underline a key.
- Aside: The term "superkey" is related to the term "superset".
  - A superkey is a superset of some key.
     (Not necessarily a proper superset.)
- Can a relation have more than one key?



### Coincidence vs key

- If a set of attributes is a key for a relation:
  - -It does not mean *merely* that there are no duplicates in a particular instance of the relation
  - -It means that in principle there *cannot* be any even if the content of the relation changes.
  - −Only a domain expert can determine what is a key.
- Often we invent an attribute to ensure all tuples will be unique.

This predates databases.

E.g., SIN, ISBN number.



### "Primary key"??

- Some of you have heard the term primary key.
- This is specific to SQL and we'll learn about it later.
  - one of keys that is designated as the one to use for indexing and other functions in the SQL DBMS



### Example: Movies schema handout, Q1-6



#### References between relations

- Relations often refer to each other.
- Example:
   In the Roles relation, the tuple about Han Solo needs to say he is played by Ford.
- Rather than repeat information already in the Artists table, we store Ford's key.
- If aID is a key for Artists, does that mean a particular aID can appear only once in Roles??



### Foreign keys

- The referring attribute is called a foreign key because it refers to an attribute that is a key in another table.
- This gives us a way to refer to a single tuple in that relation.
- A foreign key may need to have several attributes.



### Declaring foreign keys

- A bit of notation: R[A]
  - −R is a relation andA is a list of attributes in R.
  - -R[A] is the set of all tuples from R, but with only the attributes in list A.
- We declare foreign key constraints this way:  $R_1[X] \subseteq R_2[Y]$ 
  - -X and Y may be lists of attributes, of same arity
  - -Y must be a key in R<sub>2</sub>
- Example: Roles[mID]  $\subseteq$  Movies[mID]



## Example: Movies schema handout, Q7-9



### Referential integrity constraints

- These  $R_1[X] \subseteq R_2[Y]$  relationships are a kind of referential integrity constraint or inclusion dependency.
- Not all referential integrity constraints are foreign key constraints.
- For example, we could say
   Artists[aID] ⊆ Roles[aID]
   Here we are not referring to a unique tuple.
- $R_1[X] \subseteq R_2[Y]$  is a foreign key constraint iff Y is a key for relation R2.



#### Designing a schema

- Mapping from the real world to a relational schema is surprisingly challenging and interesting.
- There are always many possible schemas.
- Two important goals:
  - -Represent the data well. For example, avoid constraints that prevent expressing things that occur in the domain.
  - -Avoid redundancy.
- Later, we'll learn some elegant theory that provides sound principles for good design.



#### What's next

- We will learn how to use SQL to
  - -define a database's structure,
  - -put data in it, and
  - -write queries on it.
- First we'll learn how to write queries in relational algebra.
  - -Relational algebra is the foundation for SQL.
  - -Other important concepts, like query optimization, are defined in terms of RA.

