Introduction to Blockchain

Lecture 2: Inside Bitcoin

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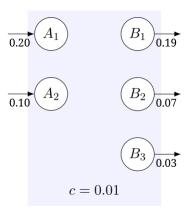
Bitcoin white paper and a bit beyond

Satoshi Nakamoto – Bitcoin: A Peer-to-Peer Electronic Cash System, pp. 1-9, 2008. Online. Available: www.bitcoin.org White paper outline

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Transactions



► double-spend

General format of a Bitcoin transaction (inside a block)

Field	Description	Size		
Version no	currently 1	4 bytes		
Flag	If present, always 0001, and indicates the presence of witness data	optional 2 byte array		
In-counter	positive integer VI = VarInt	1 - 9 bytes		
list of inputs	the first input of the first transaction is also called "coinbase" (its content was ignored in earlier versions)	<in-counter>-many inputs</in-counter>		
Out-counter	positive integer VI = VarInt	1 - 9 bytes		
list of outputs	the outputs of the first transaction spend the mined bitcoins for the block	<out-counter>-many outputs</out-counter>		
Witnesses	A list of witnesses, 1 for each input, omitted if flag above is missing	variable, see Segregated_Witness		
lock_time	if non-zero and sequence numbers are <0xFFFFFFFF: block height or timestamp when transaction is final	4 bytes		

General format (inside a block) of each input of a transaction - Txin

Field	Description	Size	
Previous Transaction hash	doubled SHA256-hashed of a (previous) to-be-used transaction	32 bytes	
Previous Txout-index	non negative integer indexing an output of the to-be-used transaction	4 bytes	
Txin-script length	non negative integer $VI = VarInt$	1 - 9 bytes	
Txin-script / scriptSig	Script	<in-script length=""> -many bytes</in-script>	
sequence_no	normally 0xFFFFFFFF; irrelevant unless transaction's lock_time is >0	4 bytes	

General format (inside a block) of each input of a transaction - Txin

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Txin-script / scriptSig	Script	<in-script length=""> -many bytes</in-script>
sequence_no	normally 0xFFFFFFFF; irrelevant unless transaction's lock_time is >0	4 bytes

General format (inside a block) of each output of a transaction - Txout

Field	Description	Size
value	non negative integer giving the number of Satoshis(BTC/10^8) to be transfered	8 bytes
Txout-script length	non negative integer	1 - 9 bytes VI = VarInt
Txout-script / scriptPubKey	Script	<pre><out-script length=""> -many bytes</out-script></pre>

Script

Bitcoin uses a scripting system for transactions. Forth-like, Script is simple, stack-based, and processed from left to right. It is intentionally not Turing-complete, with no loops.

A script is essentially a list of instructions recorded with each transaction that describe how the next person wanting to spend the Bitcoins being transferred can gain access to them. The script for a typical Bitcoin transfer to destination Bitcoin address D simply encumbers future spending of the bitcoins with two things: the spender must provide

- a public key that, when hashed, yields destination address D embedded in the script, and
- a signature to prove ownership of the private key corresponding to the public key just provided.

A transaction is valid if nothing in the combined script triggers failure and the top stack item is True (non-zero) when the script exits.

Script-2

De facto, Bitcoin script is defined by the code run by the network to check the validity of blocks.

Opcodes (Script words) examples

- Constants: OP_PUSHDATA1. The next byte contains the number of bytes to be pushed onto the stack.
- ► Flow control: OP_NOTIF. If the top stack value is False, the statements are executed. The top stack value is removed.
- Stack: OP_DEPTH. Puts the number of stack items onto the stack.

Types of Transaction-1: Pay-to-PubkeyHash

scriptPubKey: OP_DUP OP_HASH160 <pubKeyHash>
OP_EQUALVERIFY OP_CHECKSIG scriptSig: <sig> <pubKey>

Stack	Script	Description
Empty.	<pre><sig><pubkey>OP DUP OP HASH160 <pubkeyhash>OP EQUALVERIFY OP CHECKSIG</pubkeyhash></pubkey></sig></pre>	scriptSig and scriptPubKey are combined.
<sig><pubkey></pubkey></sig>	OP_DUP OP_HASH160 <pubkeyhash> OP_EQUALVERIFY OP_CHECKSIG</pubkeyhash>	Constants are added to the stack.
<sig><pubkey> <pubkey></pubkey></pubkey></sig>	OP_HASH160 <pubkeyhash> OP_EQUALVERIFY OP_CHECKSIG</pubkeyhash>	Top stack item is duplicated.
<sig><pubkey> <pubhasha></pubhasha></pubkey></sig>	<pre><pubkeyhash>OP_EQUALVERIFY OP_CHECKSIG</pubkeyhash></pre>	Top stack item is hashed.
<sig><pubkey> <pubhasha> <pubkeyhash></pubkeyhash></pubhasha></pubkey></sig>	OP_EQUALVERIFY OP_CHECKSIG	Constant added.
<sig><pubkey></pubkey></sig>	OP_CHECKSIG	Equality is checked between the top two stack items.
true	Empty.	Signature is checked for top two stack items.

A Bitcoin address is only a hash, so the sender can't provide a full public key in scriptPubKey. When redeeming coins that have been sent to a Bitcoin address, the recipient provides both the signature and the public key. The script verifies that the provided public key does hash to the hash in scriptPubKey, and then it also checks the signature against the public key.

Types of Transaction-2: Pay-to-Script-Hash (BIP 0016)

scriptPubKey: OP_HASH160 <scriptHash> OP_EQUAL scriptSig: ..signatures... <serialized script> For example, m-of-n multi-signature transaction: scriptSig: 0 <sig1> ... <script> script: OP_m <pubKey1> ... OP_n OP_CHECKMULTISIG

Stack	Script	Description
Empty.	0 <sig1><sig2>OP_2 <pubkey1><pubkey2> <pubkey3>OP_3 OP_CHECKMULTISIG</pubkey3></pubkey2></pubkey1></sig2></sig1>	Only the scriptSig is used.
0 <sig1><sig2>OP_2 <pubkey1> <pubkey2><pubkey3>OP_3</pubkey3></pubkey2></pubkey1></sig2></sig1>	OP_CHECKMULTISIG	Constants are added to the stack.
true	Empty	Signatures validated in the order of the keys in the script.

P2SH addresses were created with the motivation of moving "the responsibility for supplying the conditions to redeem a transaction from the sender of the funds to the redeemer. They allow the sender to fund an arbitrary transaction, no matter how complicated, using a 20-byte hash"1. Pay-to-Pubkey-hash addresses are similarly a 20-byte hash of the public key.

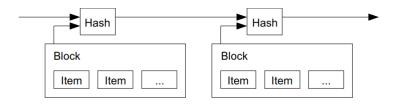
Pay-to-script-hash provides a means for complicated transactions, unlike the Pay-to-pubkey-hash, which has a specific definition for scriptPubKey, and scriptSig. The specification places no limitations on the script, and hence absolutely any contract can be funded using these addresses.

Types of Transaction-3: Generation

The Coinbase transaction, or Generation transaction, is a special transaction in the Bitcoin protocol that differs from a standard transaction as it creates coins from nothing.

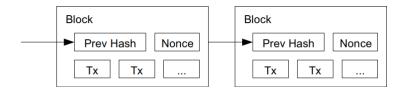
- ▶ It is the reward that miner gets for successfully mining a block.
- reward dependents on the number of blocks from the genesis block and the number of fees included in the transactions of the block.
- ▶ The transaction hash is special alongside the output index where all the bits are set to o and 1 respectively. The coinbase data size is the size of the next field or the coinbase data field.
- ► The coinbase data field can contain information such as the extra nonce, merged mining information and a list of the addresses of the mining pool where the funds are to be sent. The sequence number – all bits are set to 1.
- Once a block has been mined and either sent to one address or the miners who participated in pool the block reward has to be confirmed by 100 blocks – or roughly six hours.

Timestamp Server



The solution we propose begins with a timestamp server. A timestamp server works by taking a hash of a block of items to be timestamped and widely publishing the hash, such as in a newspaper or Usenet post. The timestamp proves that the data must have existed at the time, obviously, in order to get into the hash. Each timestamp includes the previous timestamp in its hash, forming a chain, with each additional timestamp reinforcing the ones before it.

Proof-of-Work



- one-CPU-one-vote
- ▶ longest chain = greatest proof-of-work effort invested

Network

- 1. New transactions are broadcast to all nodes.
- 2. Each node collects new transactions into a block.
- Each node works on finding a difficult proof-of-work for its block.
- 4. When a node finds a proof-of-work, it broadcasts the block to all nodes.
- 5. Nodes accept the block only if all transactions in it are valid and not already spent.
- Nodes express their acceptance of the block by working on creating the next block in the chain, using the hash of the accepted block as the previous hash.

Network: node's data structures

Transactions

- transaction pool: an unordered collection of transactions that are not in blocks in the main chain, but for which we have input transactions
- orphan transactions: transactions that can't go into the pool due to one or more missing input transactions.

Blocks

- ▶ blocks in the main branch: the transactions in these blocks are considered at least tentatively confirmed
- blocks on side branches off the main branch: these blocks have at least tentatively lost the race to be in the main branch
- orphan blocks: these are blocks which don't link into the main branch, normally because of a missing predecessor or nth-level predecessor.

Network: process transaction-1

- 1. Check syntactic correctness
- 2. Make sure neither in or out lists are empty
- 3. Size in bytes <= MAX_BLOCK_SIZE
- 4. Each output value, as well as the total, must be in legal money range
- 5. Make sure none of the inputs have hash=0, n=-1 (coinbase transactions)
- 6. Check that nLockTime <= INT_MAX (nLockTime must not exceed 31 bits, as some clients will interpret it incorrectly), size in bytes >= 100 (a valid transaction requires at least 100 bytes. If it's any less, the transaction is not valid), and sig opcount <= 2 (the number of signature operands in the signature for standard transactions will never exceed two)</p>
- 7. Reject "nonstandard" transactions: scriptSig doing anything other than pushing numbers on the stack, or scriptPubkey not matching the two usual forms (this is not a hard requirement on clients)

Network: process transaction-2

- 8. Reject if we already have matching tx in the pool, or in a block in the main branch
- For each input, if the referenced output exists in any other tx in the pool, reject this transaction (not a hard requirement on clients).
- 10. For each input, look in the main branch and the transaction pool to find the referenced output transaction. If the output transaction is missing for any input, this will be an orphan transaction. Add to the orphan transactions, if a matching transaction is not in there already.
- 11. For each input, if the referenced output transaction is coinbase (i.e. only 1 input, with hash=0, n=-1), it must have at least COINBASE_MATURITY (100) confirmations; else reject this transaction
- 12. For each input, if the referenced output does not exist (e.g. never existed or has already been spent), reject this transaction (protection against double-spending).

Network: process transaction-3

- Using the referenced output transactions to get input values, check that each input value, as well as the sum, are in legal money range
- 14. Reject if the sum of input values < sum of output values
- 15. Reject if transaction fee (defined as sum of input values minus sum of output values) would be too low to get into an empty block
- 16. Verify the scriptPubKey accepts for each input; reject if any are bad
- 17. Add to transaction pool (when the transaction is accepted into the memory pool, an additional check is made to ensure that the coinbase value does not exceed the transaction fees plus the expected BTC value)
- 18. "Add to wallet if mine"
- 19. Relay transaction to peers
- 20. For each orphan transaction that uses this one as one of its inputs, run all these steps (including this one) recursively on that orphan

Network: process block

Specific points

- Verify Merkle hash
- Reject if timestamp is the median time of the last 11 blocks or before
- ► For certain old blocks (i.e. on initial block download) check that hash matches known values
- Main brank, side chain and orphan blocks are supported.

Network and Reclaiming Disk Space

Network

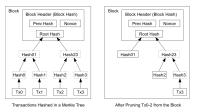
- ▶ the first transaction in a block is a special transaction that starts a new coin owned by the creator of the block
- can also be funded with transaction fees

Network and Reclaiming Disk Space

Network

- the first transaction in a block is a special transaction that starts a new coin owned by the creator of the block
- can also be funded with transaction fees

Reclaiming Disk Space



A block header \sim 80 bytes. If we suppose blocks are generated every 10 minutes, 80 bytes * 6 * 24 * 365 = 4.2MB per year. With computer systems typically selling with 2GB of RAM as of 2008, and Moore's Law predicting current growth of 1.2GB per year, storage should not be a problem even if the block headers must be kept in memory.

Simplified Payment Verification

Longest Proof-of-Work Chain Block Header **Block Header** Block Header Prev Hash Nonce Prev Hash Nonce Prev Hash Nonce Merkle Root Merkle Root Merkle Root Hash23 Hash01 Merkle Branch for Tx3 Hash2 Hash3 Tx3

Combining and Splitting Value

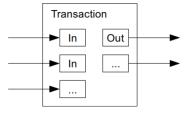


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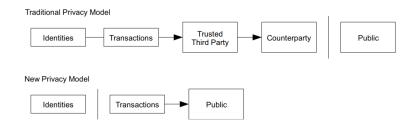
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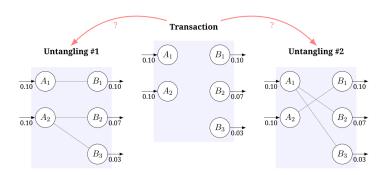
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Bitcoin and mixing

shared send and shared coin mixers

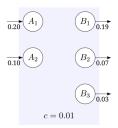
http://bitfury.com/content/5-white-papers-research/bitfury_whitepaper_shared_send_untangling_in_bitcoin_8_24_2016.pdf



Transaction for address clustering

For the purpose of transaction analysis, a (Bitcoin) transaction is viewed as an ordered triplet t = (A, B, c), consisting of:

- ▶ The finite multiset of transaction inputs A, where each input $(a_i, A_i) \in A$ is an ordered pair of the address A_i and the value of the input $a_i > 0$.
- ▶ The finite multiset of transaction outputs \mathcal{B} , where each output $(b_j, B_j) \in \mathcal{B}$ is an ordered pair of the address B_j and the value of the output $b_j \geq 0$.
- ▶ The transaction fee $c = \sum_{(a_i, \cdot) \in \mathcal{A}} a_i \sum_{(b_j, \cdot) \in \mathcal{B}} b_j \ge 0$.



Bitcoin Clustering Problem

Assumptions

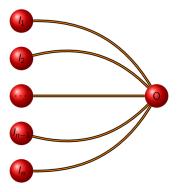
- ► Each Bitcoin address is controlled by a single real-world entity. Thus, we will ignore those sufficiently rare cases in which a multi-signature address is used for joint ownership of bitcoins, and not for multi-factor authentication.
- A single entity may control more than one address.

Goal: Bitcoin clustering algorithm

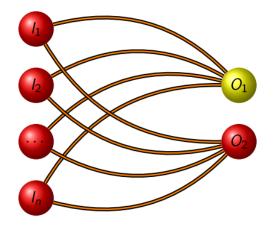
- minimal number of clusters
- ▶ all the addresses in each cluster are controlled by the same user.

Common Spending

If two or more addresses are inputs of the same transaction with one output, then all these addresses are controlled by the same user.



One-time Change



One-time Change (2)

We say that the transaction t = (A, B, c) satisfies the condition of a one-time change if the following conditions hold.

- 1. $\#Addr(\mathcal{B}) = 2$, i.e. the transaction t has exactly two outputs.
- 2. $\#Addr(A) \neq 2$, i.e. the number of t inputs is not equal to two. If #Addr(A) = #Addr(B) = 2 the transaction is most likely shared send mixer.
- 3. Both outputs of transaction t, B_1 and B_2 , are not self-change addresses, i.e. $B_1, B_2 \notin Addr(A)$.
- 4. One output of the transaction B_1 did not exist before transaction t and decimal representation of the value b_1 has more than 4 digits after the dot.
- 5. The other output of the transaction B_2 was previously part of the Bitcoin network and has not been OTC addressed in previous transactions.

The OTC output and all the inputs of the transaction are controlled by the same user.



Off-Chain information

Much public information can be found on the Internet (off-chain information).

If the Bitcoin address is mentioned in the same data frame with the tag (key phrase-entity, for example, company name or username), then it is said say that the address has such a tag.

Tag collection

- passive approach: web crawling of public forums and user profiles (for example, Bitcointalk.com, Twitter and Reddit) and Darknet markets (for example, Silkroad, The Hub Marketplace and Alphabay)
- active approach: manual analysis of Bitcoin companies and data actualization procedures (Satoshi Bones casino uses 1change and 1bones prefixes and BTC-E exchange uses 1eEUR and 1eUSD prefixes, etc.).

Bitcoin Organization Types

We distinguish six categories of Bitcoin organizations

- mining pools (pools)
- exchanges
- Darknet markets (dnm)
- mixers
- gambling
- other services (services).

Unique clean tags per category

services	gambling	mixer	dnm	exchange	pool
57	80	3	16	98	52

Let us call $L = \{\{a_i, a_j\}\}$ the set of negative pairs, where addresses a_i and a_j in each pair have either different tags from the same category or tags from a forbidden pair of categories.

Bitcoin Organization Types

	services	gambling	mixer	dnm	exchange	pool
services	165,970	66,387	0	0	441	186
gambling	66,387	11,9857	0	0	0	9
mixer	0	0	0	0	1,703	1
dnm	0	0	0	0	13	18
exchange	441	0	1,703	13	606,357	198,551
pool	186	9	1	18	198,551	1,561

Table: The number of addresses with distinct clean tags in respective pairs of categories.

	services	gambling	mixer	dnm	exchange	pool
services	F	Α	F	F	F	Α
gambling	Α	F	F	F	F	Α
mixer	F	F	F	F	F	F
dnm	F	F	F	F	F	F
exchange	F	F	F	F	F	Α
pool	Α	Α	F	F	Α	F

Table: Table shows if the appearance of addresses having two distinct clean tags in the same cluster should be forbidden. "F" stays for forbidden and "A" is for allowed.

Probabilistic model

We note that both CS and OTC heuristics and the set of negative pairs L may contain erroneous information.

Different types of observations (which we *treat as an independent* to make it computationally solvable):

- ▶ In the event that all the addresses $Addr_H(t)$ for some $t \in T_H$ indeed belong to the same user is true with probability p.
- ▶ In the event that two addresses $\{a_i, a_j\} \in L$ are controlled by the same user is true with probability q. In other words, the information about the negative association between any pair of addresses in L is validated by the probability 1 q.

Probabilistic model (2)

Let the likelihood $\mathbb{P}(A, T_H, L \mid p, q)$ be a function of the clustering A, transactions T_H and negative pairs L:

$$\begin{split} & \mathbb{P}\left(A, T_{H}, L \mid p, q\right) = \\ & = \prod_{t \in T_{H}} p^{\mathbb{I}\left(Addr_{H}(t) \subset CI(A)\right)} \times (1-p)^{\mathbb{I}\left(Addr_{H}(t) \not\subset CI(A)\right)} \\ & \times \prod_{\{a, a'\} \in L} (1-q)^{\mathbb{I}\left(\{a, a'\} \not\subset CI(A)\right)} \times q^{\mathbb{I}\left(\{a, a'\} \subset CI(A)\right)}, \end{split}$$

where for some set of Bitcoin addresses S the notation $S \subset CI(A)$ means, that there exists a cluster A_I such that $S \subseteq A_I$.

Probabilistic model (3)

Finally, the log-likelihood reads as

$$\begin{split} & \ln \mathbb{P}\left(A, T_H, L \mid p, q\right) = \\ & = \sum_{t \in T_H} \mathbb{I}\big(Addr_H(t) \subset \mathit{Cl}(A)\big) \ln(1-p) + \sum_{t \in T_H} \mathbb{I}\big(Addr_H(t) \not\subset \mathit{Cl}(A)\big) \ln(p) \\ & + \sum_{\{a,a'\} \in L} \mathbb{I}\big(\{a,a'\} \not\subset \mathit{Cl}(A)\big) \ln(1-q) + \sum_{\{a,a'\} \in L} \mathbb{I}\big(\{a,a'\} \subset \mathit{Cl}(A)\big) \ln(q). \end{split}$$

Let Δ_{A_m} be the number of negative pairs in cluster A_m . Then, if we merge all the clusters corresponding to $Addr_H(t_j)$, the change of the log-likelihood is equal to

$$\Delta_{\mathbb{P}}(t_j,A,L\mid p,q) = \ln\left(rac{p}{1-p}
ight) + \left(\Delta_{\hat{A_j}} - \sum_{i=1}^{m_j} \Delta_{A_{k_i}}
ight) \ln\left(rac{q}{1-q}
ight).$$

Experimental Setup

- ▶ Bitcoin blockchain data from 3^d January of 2009 to 9th March of 2017: 211, 789, 876 transactions which cover 244, 030, 115 unique addresses.
- ▶ CS heuristic condition is satisfied for 8, 161, 086 transactions with 28, 416, 034 unique addresses.
- ▶ OTC heuristic condition holds for 35,844,487 OTC transactions with 69, 520, 194 unique addresses.
- ▶ Both conditions give a total of 44,005,573 covered transactions with 95.250.167 unique addresses (the overlap is 2,686,061 addresses).

	Number	Number of	
Category	of	common tags	Examples of common tags
	tags	(size)	
services	33	5 (> 100K)	Bitpay.com, Xapo.com
gambling	34	6 (> 50K)	999Dice.com, primedice.com
mixer	3	1 (> 100K)	BitcoinFog
dnm	14	5 (> 100K)	SilkRoad Marketplace
exchange	64	12 (> 100K)	BTC-e.com, Bittrex.com
pool	15	2 (> 50K)	BTCChina, Hashnest.com

Table: Tags of the biggest cluster in case of clustering without constraints (26, 694, 671 addresses).

Algorithms

- greedy (historical) approach: go retrospectively through all the transactions in the Bitcoin network, which satisfy one of the heuristics
- ▶ greedy additive clustering (add): first step, to perform clustering with $q \rightarrow 0$, where the clusters are not allowed to contain any negative pairs. In the second step, we once again go through Bitcoin transactions historically and optimize likelihood.

Maximum Cluster Size

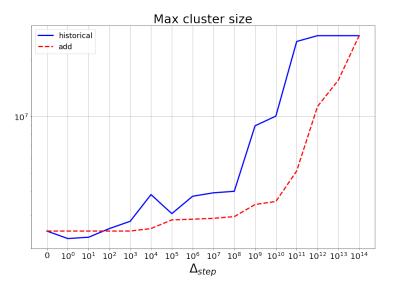


Figure: The size of the biggest cluster, where Δ_{step} is allowed to increase the number of negative pairs per transaction.

Negative Links

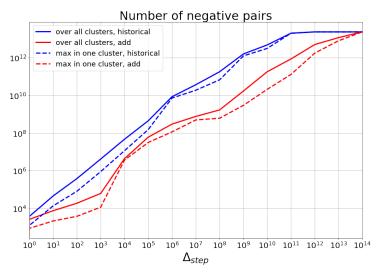


Figure: Number of negative pairs in whole clustering and the maximum in one cluster, where Δ_{step} is allowed to increase the number of negative pairs per transaction.

Calculations

- p = probability an honest node finds the next block
- q = probability the attacker finds the next block
- z blocks.

$$\begin{split} q_z &= \begin{cases} 1 & \text{if } p \leq q \\ (q/p)^z & \text{if } p > q \end{cases} \\ \lambda &= z \frac{q}{p} \\ \sum_{k=0}^{\infty} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 & \text{if } k > z \end{bmatrix} \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} (1 - (q/p)^{(z-k)}) & \text{if } k \leq z \\ 1 & \text{if } k > z \end{bmatrix} \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} (1 - (q/p)^{(z-k)}) & \text{if } k \leq z \\ 1 & \text{if } k > z \end{bmatrix} \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{z} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} 1 - (q/p)^{(z-k)} & \text{if } k \leq z \\ 1 - \sum_{k=0}^{$$

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Bitcoin Improvements

Bitcoin improvements: forks

- soft fork: backward capability
 - ► SegWit: August 2017.
- hard fork: change to a protocol that renders older versions invalid
 - ▶ November 2017: Segwit2x didn't happen in Bitcoin network
 - -> Bitcoin Cash
 - June 2016: Ethereum Classic and The DAO.
- source code fork
 - October 2011: Litecoin
 - decreased block generation time (2.5 minutes)
 - increased maximum number of coins
 - different hashing algorithm (scrypt, instead of SHA-256).

Bitcoin hard forks

- ► Segwit2x Bitcoin Cash
- ▶ Bitcoin Gold



Bitcoin improvements protocols-1: Hierarchical Deterministic Wallets

▶ BIP32, BIP39 and BIP44

```
64536 luggage
                 65133 mixed
                                 65346 nurse
                                                  65543 path
                                                                   16156 prevent
                                                                                    16353 recipe
                                                                                                     11666 rua
64531 lumber
                 65134 mixture
                                                  65544 patient
                                                                                    16354 record
                                                                                                     11661 rule
                                 65341 nut
                                                                   16151 price
64532 lunar
                65135 mobile
                                 65342 oak
                                                                                    16355 recycle
                                                                                                     11662 run
                                                  65545 patrol
                                                                   16152 pride
64533 lunch
                65146 model
                                                                                    16466 reduce
                                 65343 obey
                                                  65556 pattern
                                                                   16153 primary
                                                                                                     11663 runway
                                 65344 object
                                                                                   16461 reflect
64534 luxury
                65141 modify
                                                  65551 pause
                                                                   16154 print
                                                                                                     11664 rural
64535 lyrics
                65142 mom
                                 65345 oblige
                                                  65552 pave
                                                                   16155 priority
                                                                                    16462 reform
                                                                                                     11665 sad
                                                  65553 payment
                                                                                    16463 refuse
64546 machine 65143 moment
                                 65356 obscure
                                                                  16266 prison
                                                                                                    11616 saddle
64541 mad
                65144 monitor
                                 65351 observe
                                                  65554 peace
                                                                   16261 private
                                                                                    16464 region
                                                                                                     11611 sadness
                65145 monkey
                                 65352 obtain
                                                  65555 peanut
                                                                                   16465 regret
                                                                                                    11612 safe
64542 magic
                                                                   16262 prize
64543 magnet
                65156 monster
                                 65353 obvious
                                                  16666 pear
                                                                   16263 problem
                                                                                   16416 regular
                                                                                                     11613 sail
64544 maid
                65151 month
                                 65354 occur
                                                  16661 peasant
                                                                   16264 process
                                                                                    16411 reject
                                                                                                    11614 salad
                                                                   16265 produce
64545 mail
                65152 moon
                                 65355 ocean
                                                  16662 pelican
                                                                                   16412 relax
                                                                                                     11615 salmon
                                                                   16216 profit
64556 main
                65153 moral
                                 65466 october
                                                  16663 pen
                                                                                    16413 release
                                                                                                    11626 salon
64551 major
                65154 more
                                 65461 odor
                                                  16664 penalty
                                                                  16211 program
                                                                                   16414 relief
                                                                                                    11621 salt
64552 make
                 65155 morning
                                 65462 off
                                                  16665 pencil
                                                                   16212 project
                                                                                    16415 relv
                                                                                                    11622 salute
64553 mammal
               65266 mosquito
                                 65463 offer
                                                  16616 people
                                                                   16213 promote
                                                                                   16426 remain
                                                                                                    11623 same
                                                                   16214 proof
                                                                                   16421 remember 11624 sample
64554 man
                 65261 mother
                                 65464 office
                                                  16611 pepper
                                                  16612 perfect
                                                                   16215 property
                                                                                   16422 remind
                                                                                                    11625 sand
64555 manage
                65262 motion
                                 65465 often
65666 mandate 65263 motor
                                 65416 oil
                                                  16613 permit
                                                                   16226 prosper
                                                                                    16423 remove
                                                                                                    11636 satisfy
                                                  16614 person
                                                                   16221 protect
                                                                                    16424 render
                                                                                                    11631 satoshi
65661 mango
                 65264 mountain 65411 okay
                                                                   16222 proud
                                                                                   16425 renew
65662 mansion
               65265 mouse
                                 65412 old
                                                  16615 pet
                                                                                                     11632 sauce
```

Bitcoin improvements protocols-2: SegWit

Segregated Witness

- ▶ Transaction malleability: While transactions are signed, the signature does not currently cover all the data in a transaction that is hashed to create the transaction hash. Thus, while uncommon, it is possible for a node on the network to change a transaction you send in such a way that the hash is invalidated. Note that this just changes the hash; the output of the transaction remains the same and the bitcoins will go to their intended recipient. However this does mean that, for instance, it is not safe to accept a chain of unconfirmed transactions under any circumstance because the later transactions will depend on the hashes of the previous transactions, and those hashes can be changed until they are confirmed in a block (and potentially even after a confirmation if the block chain is reorganized). In addition, clients must always actively scan for transactions to them; assuming a txout exists because the client created it previously is unsafe.
- SegWit defines a new structure called a witness that is committed to blocks separately from the transaction merkle tree. This structure contains data required to check transaction validity but is not required to determine transaction effects. In particular, signatures and redeem scripts are moved into this new structure, which does not count towards the traditional 1 MB block size limit. Instead, a new weight parameter is defined, and blocks are allowed to have at most 4 million weight units (WU). A byte in the original 1 MB zone of the block weighs 4 WU, but a byte in a witness structure only weighs 1 WU, allowing blocks that are technically larger than 1 MB without a hardforking change.

Bitcoin improvements protocols-2: SegWit (2)

Segregated Witness profit

- protection from transaction malleability
- increase block capacity
- useful for anchoring and lightning
- ▶ optimizes CHECKSIG, CHECKMULTISIG (O(n)) instead of $O(n^2)$ to check n signatures per transaction).

Thank you for your attention!