

# Using Statistical Techniques for Feature Selection

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# Overview

**Methods for selecting and eliminating features**

**Variance thresholds**

**Univariate statistics**

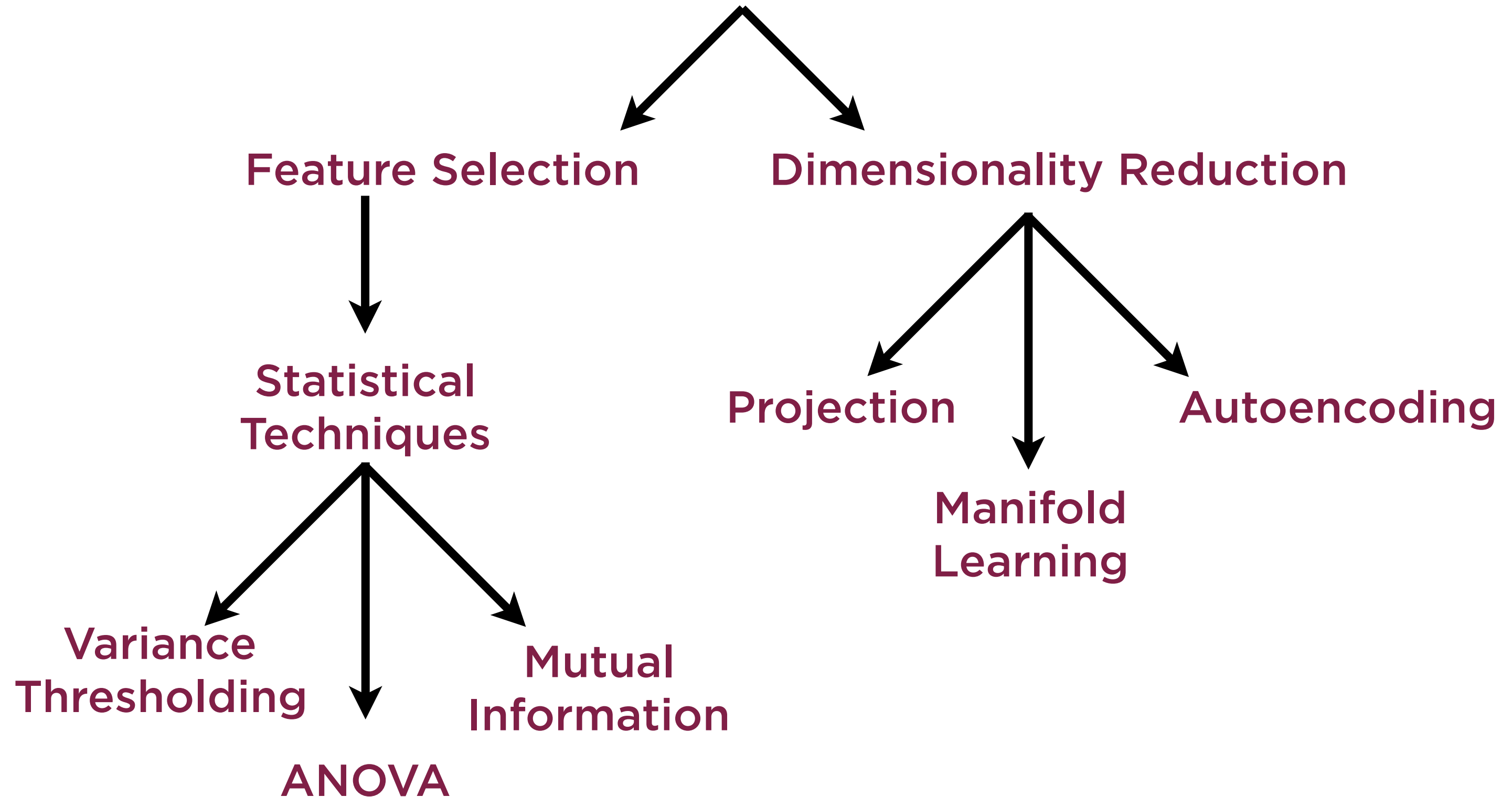
**ANOVA, chi-square, mutual information**

**Dictionary learning and atom extraction**

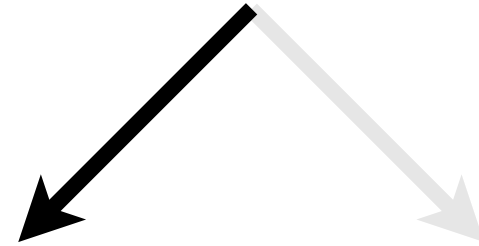
# Statistical Techniques for Feature Selection

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# Reducing Complexity



# Reducing Complexity

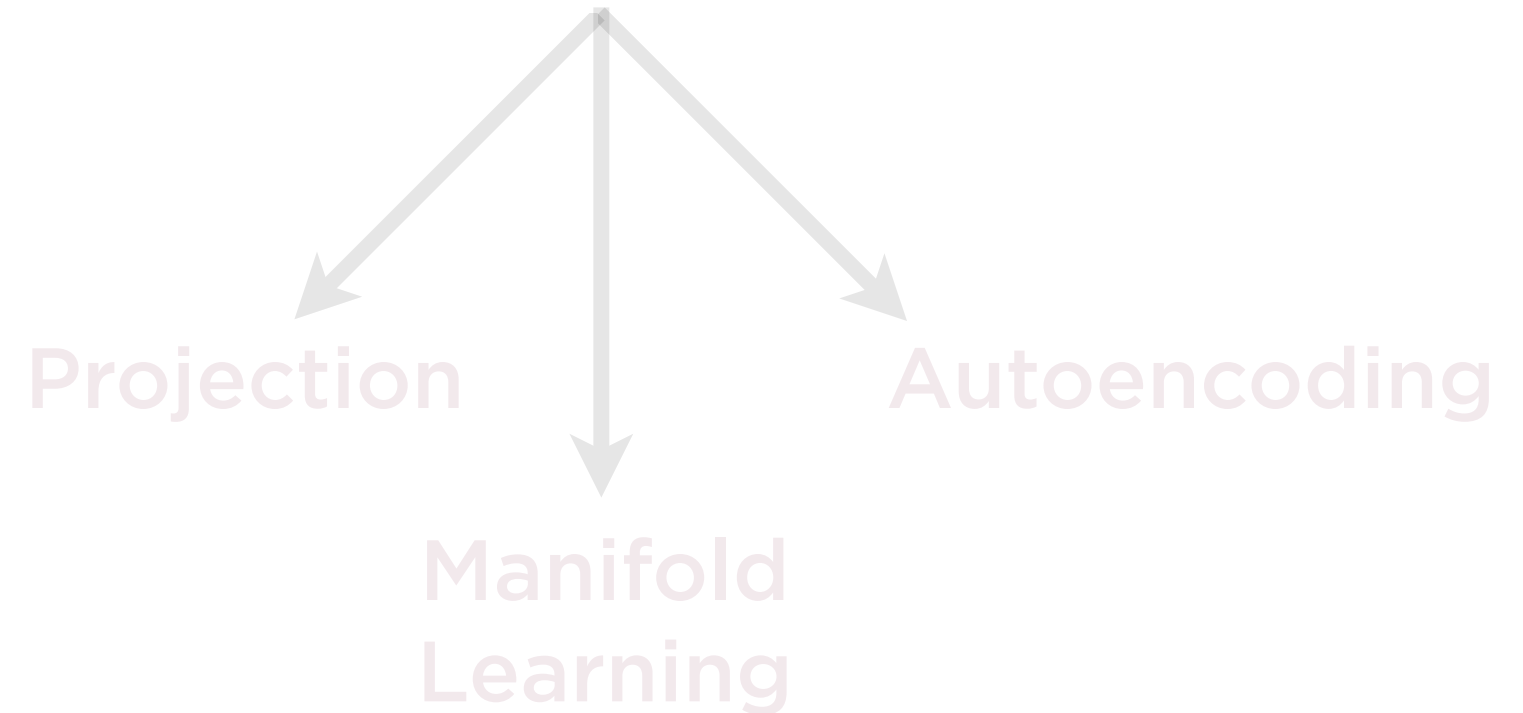


**Feature Selection**

Dimensionality Reduction



Choose a subset of  
original X variables



# Choosing Feature Selection

## Use Case

**Many X-variables**

**Most of which contain little  
information**

**Some of which are very  
meaningful**

**Meaningful variables are  
independent of each other**

## Possible Solution

**Feature selection**

# Hypothesis

Proposed explanation for a phenomenon.



# Lady Tasting Tea

**Lady tasting tea: famous experiment**

**Was tea added before or after milk?**

**Muriel Bristol claimed she could tell**



# Lady Tasting Tea

**Null Hypothesis**  
**( $H_0$ )**

The lady cannot tell if milk was  
poured first

**Alternate Hypothesis**  
**( $H_1$ )**

The lady can tell if milk was  
poured first

# Hypothesis Testing

## Null Hypothesis $H_0$

True until proven false

Usually posits no relationship

## Select Test

Pick from vast library

Know which one to choose

## Significance Level

Usually 1% or 5%

What threshold for luck?

## Alternative Hypothesis

Negation of null hypothesis

Usually asserts specific relationship

## Test Statistic

Convert to p-value

How likely it was just luck?

## Accept or Reject

Small p-value? Reject

Small: Below significance level

# Statistical Techniques

**Variance Thresholding**

**Chi-square Test**

**ANOVA**

**Mutual Information**

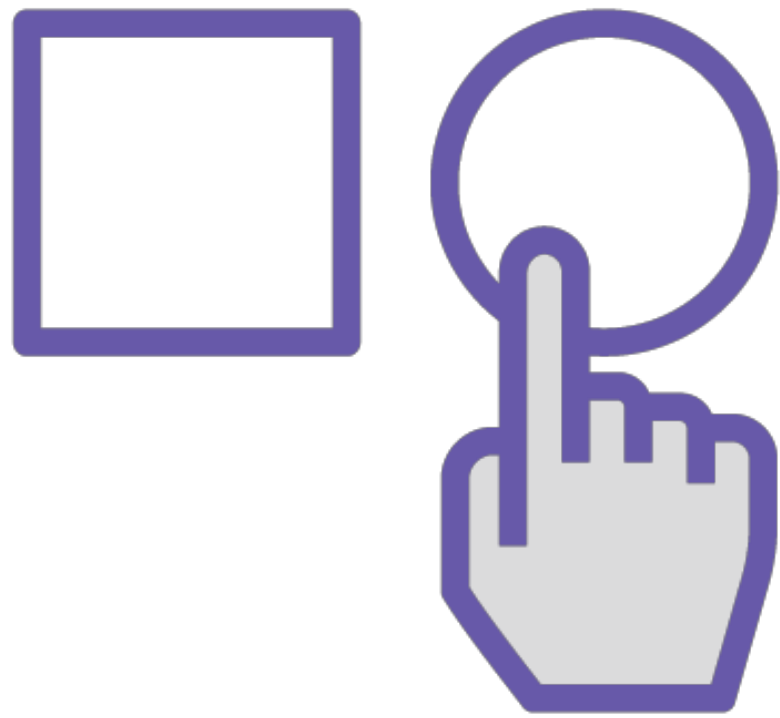
# Variance Thresholding

If all points have the same value for an X-variable, that variable adds no information. Extend this idea and drop columns with variance below a minimum threshold.

# Chi-square ( $\chi^2$ ) Feature Selection

For each X-variable, use the Chi-square test to evaluate whether that variable and Y are independent. If yes, drop that feature. Used for categorical X and Y.

# Chi-square Feature Selection



**Does observed data deviate from those expected in a particular analysis?**

**Tests the effect of one variable on the outcome, univariate analysis**

**Sum of the squared difference between observed and expected data in all categories**

ANOVA

**A**nalysis **O**f **V**ariance

# ANOVA

Looks across multiple groups of populations, compares their means to produce one score and one significance value



# ANOVA

Looks across **multiple** groups of populations, compares their means to produce one score and one significance value

# ANOVA Feature Selection

For each X-variable, use the ANOVA F-test to check whether mean of Y category varies for each distinct value of X. If not, drop that X-variable.

# Diabetes Risk



Underweight  
patients

Normal weight  
patients

Overweight  
patients

Perform an ANOVA test to know whether the risk of diabetes is significantly different between these groups

# ANOVA Hypotheses

**Null Hypothesis**  
**( $H_0$ )**

$H_0$ : All groups of patients are at an equal risk of diabetes

**Alternate Hypothesis**  
**( $H_1$ )**

$H_1$ : All groups of patients are NOT at an equal risk of diabetes



F-statistic

$$F = \frac{\text{Variance between groups}}{\text{Variance within a group}}$$



## F-statistic

**If the groups are similar,  $F \sim 1$**

**If the groups are different,  $F$  will be large**



## P-value

### Significance of the F-statistic

Smaller p-values indicate that the results are not due to chance

Large F-statistic and small p-value - means the null hypothesis can be rejected

# Mutual Information

Measures the amount of information obtained on random variable by observing another.



# Mutual Information

Conceptually similar to using ANOVA F-test for feature selection; superior as it also captures non-linear dependencies (unlike ANOVA-based feature selection).

# Dictionary Learning

Representation learning method to find a sparse representation of input data.

# Demo

**Use variance threshold to select features for regression**

# Demo

**Use univariate statistics to select features for classification**

# Demo

**Using dictionary learning to find sparse representations of complex data**

# Summary

**Methods for selecting and eliminating features**

**Variance thresholds**

**Univariate statistics**

**ANOVA, chi-square, mutual information**

**Dictionary learning and atom extraction**