

Evaluating Bayesian Networks as a Tool for Reasoning with Evidence using Agent-Based Simulations

Ludi van Leeuwen

Abstract

The existing methods for evaluating Bayesian Networks on full court cases are not sufficient, since the subjective probability assigned to the nodes might be overfitted on the world in which all pieces of evidence are true. This would result in incorrect outcomes for BNs where the state of the evidence turns out to be different. A systematic way of evaluating the response of a BN on all possible valuations of cumulative evidence is proposed in this paper, and illustrated by means of a simple agent-based simulation of a robbery. This method works correctly in the simulation, but is implausible to be generalisable to the real world due to combinatorial explosion of possible evidence states, the subjectivity in establishing a ground truth without using simulations, and the imprecision in node definitions in the BN in the first place.

Contents

1	Introduction	5
2	Background	7
2.1	Reasoning with evidence	7
2.2	Bayesian Networks	8
2.2.1	Evaluating Bayesian Networks	11
2.3	Simulation	14
3	Method	15
3.1	Scenarios	15
3.2	Simulation	15
3.2.1	Model	16
3.2.2	Reporters	16
3.3	Construction	17
3.4	Evaluation	18
4	Case Study: Robbery at Grote Markt	20
4.1	Experimental Set-up	20
4.2	Scenarios	20
4.3	Simulation	21
4.3.1	Model	21
4.3.2	Reporters	24
4.4	Construction	28
4.5	Evaluation	28
5	Results	30
6	Discussion	36
6.1	Evaluating BNs over all possible evidence states using simulations . .	36
6.2	Can a modeller do this?	38
6.2.1	Constructing the Manual Network	38
6.2.2	Evaluating the Manual Network	39
6.2.3	Discussing the Manual Network	42
6.3	Evaluating BNs over all possible evidence states in real life	44
6.3.1	de Zoete 2019	44
6.3.2	van Leeuwen 2019	47
6.4	Implications	51

6.5	Using Simulations	52
7	Conclusion	54
7.1	Summary	54
7.2	Future Research	55
8	Appendix	58
8.1	Discussion	59
8.1.1	Network	59
8.1.2	Table	60

1 Introduction

When we find evidence for a hypothesis that we have held in the back of our minds, our belief in that hypothesis increases. This is the essence of reasoning with evidence. Our goal in reasoning with evidence is to find a method that will lead us to believe as many true hypotheses as we can, given the evidence that we have.

However, the relationship between evidence and hypotheses is elusive. How can we be sure that some evidence supports some hypothesis? Even if we know that it does, how can we express how strong the piece of evidence is? Some evidence is very weak, and only after a tedious process of ruling out other factors and careful investigation and collection of other pieces of evidence, we can come to a conclusion about a hypothesis. On the other hand, some evidence is so strong that it leaves no room for doubt.

We can consider three main approaches for reasoning about hypotheses using evidence within the domain of AI and Law ([Di Bello and Verheij, 2018](#)): an argumentative, a scenario-based, and a probabilistic approach. One subfield of the probabilistic approach is the use of Bayesian Networks. Bayesian Networks can make explicit how our beliefs about events should change given that we find certain pieces of evidence for them. This idea of correctly updating on new information make BNs an interesting tool in the courtroom. A Bayesian Network might make transparent how reasoners should update their beliefs based on the evidence, which might increase transparency and fairness. In the ideal case, a Bayesian Network might stop a judge from making a reasoning error.

However, creating and using BNs is far from straightforward for both the builder and the interpreter. From [de Koeijer et al. \(2020\)](#): it is complex, time-consuming, hard to explain, and, the “repeatability [...] leaves much to be desired. Node definitions and model structures are often directed by personal habits, resulting in different models for the same problem, depending on the expert”. This subjectivity is pervasive throughout the Bayesian Network: the events selected, arcs drawn, and numbers elicited are subjective and seem empirically untestable in the data-poor environment of AI and law. These problems might be mitigated in part by evaluation criteria.

These evaluation criteria, however, do not always sufficiently safeguard against an incorrect network, which is a network that predicts the ‘wrong’ outcome based on some set of evidence. A BN for crimes should be accurate across all possible evidence states, since, if we want to use BNs in court and not model court cases afterwards,

we do not know at the start what the state of the evidence will be. However, in general, it is hard for modellers to rationally consider all possible evidence states. A network might respond well to situations where all evidence as presented in the trial is present, but predict the wrong outcome when one evidence node is turned to a different value. This brings up questions about the use of BNs in general: do we really need to consider these states where the evidence is different from the evidence as presented in the trial? Since specifying the joint probability distribution is necessary in BNs, we have to specify all of these numbers. Anyway, if we want to take BNs seriously, they need to be correct over all possible evidence states.

The aim of this project is to define a method for the modeller to evaluate the BN over all possible evidence states, by grounding the BN in an agent-simulation of a crime. We can model crime cases using simulations to a level of realism we desire, measure the frequencies of events that emerge out of this simulation by running the simulation multiple times. In the agent-based system, we have full control over and full knowledge of the world that we are reasoning about, hence we can create a grounding that can be used to evaluate the BN. We can test whether our method of evaluating all possible evidence states works by comparing the predicted output of the BN with the frequency information about the output from the simulation. Then, we will discuss whether it is plausible that this method of evaluation generalises to real life¹. More generally, we want to investigate to what extent simulations can be useful as a tool to investigate Bayesian Networks. We can choose to investigate Bayesian Network methods, such as idiom-structure, the accuracy and use of elicitation, or we can choose to investigate whether simulations are a good modelling primitive for investigating reasoning with evidence in criminal cases. This thesis discusses both of these aspects.

¹The simulation can be interacted with at <https://shielded-journey-34533.herokuapp.com>
Code for this project can be found at <https://github.com/aludi/simulationTest>

2 Background

We want to create grounded Bayesian Networks for reasoning with evidence. This can be done by creating a agent-based simulation, building BNs based on the events in this simulation, and testing the evaluation method on that BN. In this section, the relevant background is laid out on reasoning with evidence, Bayesian Networks, existing evaluation methods for BNs, and agent-based simulations.

2.1 Reasoning with evidence

We consider three main directions in the field of reasoning with evidence within law (Verheij et al., 2015), (Di Bello and Verheij, 2018).

The first direction is via argumentation approaches, where hypotheses and evidence are represented as propositions that attack or support each other, as originating in (Wigmore, 1931) and in part unified by Dung (1995), for a historical overview see (Bench-Capon, 2019). An example of argumentation research in AI and law is ASPIC+ (Prakken et al., 2013).

The second direction is via scenario approaches, where coherent hypotheses are combined into stories (Pennington and Hastie, 1993), (Wagenaar et al., 1993), which are supported with evidence. Different types of stories need different pieces of evidence to be considered ‘valid’ or ‘anchored’ stories, and the extent to which different stories are anchored in the evidence determines how we assess them.

The third direction is via probabilistic approaches, where hypotheses and evidence are assigned probabilities and the relation between hypothesis and evidence is represented with conditional probability, either by applying Bayes’ law directly (Dahlman, 2020), or by using Bayesian Networks. Bayesian Networks can represent aspects of a criminal case or can attempt a scenario-like hybrid and represent the entire case. Examples of this are: modelling actual crime cases (Kadane and Schum, 1996), (Fenton et al., 2019), cases from fiction (Fenton et al., 2012) or fictionalised crime cases (van Leeuwen, 2019). The BN can also represent specific (forensic) aspects of a case, like DNA or blood-spatter evidence, for methods see (Meester and Slooten, 2021). Bayesian Networks can also integrate aspects of argumentation (Wieten et al., 2019), (Timmer, 2016), or of scenario-based construction (Vlek, 2016).

2.2 Bayesian Networks

A Bayesian Network (BN) is a directed acyclic graph that represents the joint probability distribution over a set of events (Pearl, 1988). BNs consists of nodes, arcs and conditional probability tables. A node is a random variable that represents an events. An arc represent a conditional relationships between two events, linking two nodes together. The two nodes are the parent and the child node, the probabilities in the child node are conditioned on the value that the parent node takes. The specification of these conditional probabilities is done in the conditional probability tables (CPT) of each node. As described in (Russell and Norvig, 2010):

The combination of all nodes in the BN results in a full joint probability distribution over all nodes, which is

$$P(x_1, \dots, x_n)$$

We can decompose this using the product rule

$$P(x_1, \dots, x_n) = P(x_n|x_{n-1}, \dots x_1)P(x_{n-1}, \dots x_1)$$

Now, we see that $P(x_{n-1}, \dots x_1)$ is also a joint distribution over all nodes, except node x_n . Hence, we apply the product rule again:

$$P(x_1, \dots, x_n) = P(x_n|x_{n-1}, \dots x_1)P(x_{n-1}|x_{n-2} \dots x_1)P(x_{n-2}, \dots x_1)$$

Keep applying this until we're at

$$P(x_1, \dots, x_n) = P(x_n|x_{n-1}, \dots x_1)P(x_{n-1}|x_{n-2} \dots x_1) \dots P(x_2|x_1)P(x_1)$$

which is equivalent to

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i|x_{i-1}, \dots, x_1)$$

In BNs, we know by definition that

$$P(x_i|x_{i-1}, \dots, x_1) = P(x_i|parents(x_i))$$

Hence,

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(x_i))$$

For every node x , hence, we will fill out the CPT

$$P(x_i | \text{parents}(x_i))$$

We show an example BN in Figure 1. This is the basic form of the evidence idiom (Fenton et al., 2012): we have a cause as a parent node, and a consequence as a child node. In this context, we want to interpret the parent node as a ‘hypothesis’, that we want to prove, but cannot observe directly. The child node is a piece of evidence that we can observe: it is either true, or false. Specifically instantiated, like in Figure 1, we create a basic scenario: ‘suspect shot victim with gun’ as the parent (hypothesis) node, and ‘bullet casings found on ground’ as the child (evidence) node. We can use this network, with the probabilities as defined in the CPTs, to reason about the hypothesis given the evidence that we find.

In Figure 1, the node ‘suspect shot victim with gun’ is a hypothesis. Nodes with one or more incoming arcs are conditionally dependent on their parent node(s). In our example network, the node ‘bullet casings found on the ground’ is conditionally dependent on its parent. The links between the nodes are links of conditional probability, and do not correspond to real-world causality, although they are sometimes interpreted as being causal (Dawid, 2008).

The arcs and the CPTs tell us how we should reason about the hypothesis, given that we find some piece of evidence.

For a simple example, for a node with only one parent, we can just use Bayes law directly.

$$P(H|E) = \frac{P(E|H) \cdot P(H)}{P(E)}$$

To update to our network let us say that we found B , so there are bullet casings on the ground. We want to know what this new evidence will do to our belief in S . This means that we are updating our belief in S , or finding the posterior of S , based on the evidence that we found B .

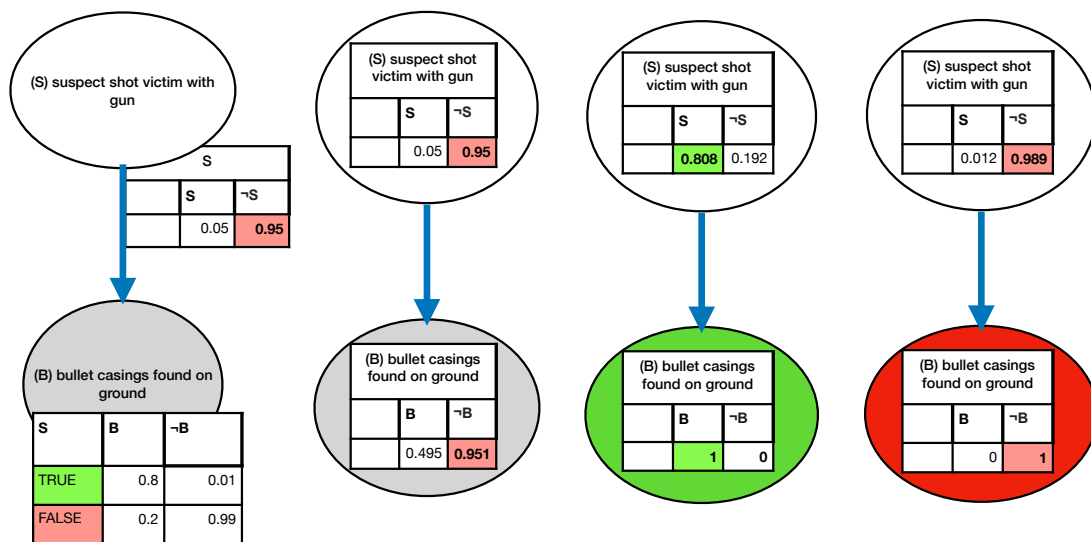


Figure 1: Inference with Bayesian Networks: Defining the network with CPTS, entering no evidence, entering positive evidence, and entering negative evidence

$$P(S|B) = \frac{P(B|S) \cdot P(S)}{P(B)}$$

$$P(B|S) = 0.8, P(S) = 0.05, P(B) = 0.8 \cdot 0.05 + 0.01 \cdot 0.95$$

$$P(S|B) = \frac{0.8 \cdot 0.05}{0.8 \cdot 0.05 + 0.01 \cdot 0.95} = 0.808$$

So now we have found the posterior of S , our belief in S has increased from its prior probability of 0.05, to its posterior probability of 0.808, given evidence B . On the other hand, if we do not find bullet casings on the ground, our belief that the suspect shot the victim decreases from 0.05 to 0.012.

Hence, we can exactly specify how our belief in a hypothetical event changes given all possible values of the evidence. This is the simplest form of Bayesian reasoning, with one piece of evidence, and one hypothesis. The general form of the update is more complicated and has high complexity (see (Russell and Norvig, 2010) for an introduction to updating algorithms). We can use exact inference or approximate inference.

In real-life situations, we are constantly reasoning with many pieces of evidence that might be conditioned on more than one parent node, resulting in tedious and error-prone calculations if we would do them manually. This is where Bayesian Networks are useful.

We can outsource the Bayesian calculation to the BN, however, the network itself has to be constructed in some way. This can be done by hand by modellers, in (proprietary) software with a GUI like AgenaRisk or Hugin. They can also be built, by hand, or automatically constructed from datasets in PyAgrum, (Ducamp et al., 2020), a free Python software package. In this project, PyAgrum was used, using the LazyPropagation algorithm, which uses exact inference.

2.2.1 Evaluating Bayesian Networks

Bayesian Networks have been used to model reasoning with evidence in criminal cases, although these methods have not been used in court. However, even though there are methods for building BNs, it is unclear how we should validate and evaluate them.

In data-rich domains, we can train Bayesian Networks on large amounts of frequency data and estimate the accuracy of the BN by cross-validation. We define a training

set and a test set of the data (usually a 80/20 split). We construct the network based on the training data, 80% of the input. Then, we test if the network learned the correct conditional probability relations on the final 20% of the data, by comparing the expected output in the test data to the predicted output from the BN (Hamilton and Pollino, 2012). The 80/20 split allows us to measure to what extent the network is performing well on the entire dataset, and not just overfitting on the data that it has access to.

However, this approach towards BN validity through accuracy is implausible in BNs for court cases. The court cases involve one-of-a-kind events (Schum and Martin, 1982), which means that it is unlikely that we can find frequency data on most of the nodes present in our BNs. This means that we cannot do an 80/20 type split in our data, as we only have one piece of data, which is the court case that we are modelling. This is why the probabilities in the BNs for court cases not pure frequencies, but instead subjective probabilities based on estimated frequencies, either elicited from experts or estimated by the modeller.

There are other ways of evaluating BNs than accuracy. The evaluation methods used by Fenton et al. (2019) and Vlek (2016), who both model BNs based on real case studies, confine themselves to two approaches:

1. Sensitivity analysis

Sensitivity analysis tests which (parent) nodes have the greatest effect on a given target node. With sensitivity analysis, we can describe how much the target node will change if we make small changes in the conditional probability tables of those parent nodes (Fenton and Neil, 2013). This is useful if the outcome of the network hinges on elicited or subjectively estimated probabilities, since we cannot apply methods like accuracy to a subjectively estimated probability, as we are usually working with extremely limited data. Hence, sensitivity analysis can be used to ‘sanity-check’ elicited probabilities. If the target node is influenced by nodes that are unexpected given the causal relations that we are modelling, something probably has gone wrong. Since Bayesian Networks have many parameters per node, it is not trivial to perform a sensitivity analysis that takes into account all the nodes in the network and interpret the results in a meaningful way - this would be an n -way sensitivity analysis (Van Der Gaag et al., 2007). We can also only define sensitivity analysis only for a given value of evidence: change the state of the evidence, and we might find different sensitivity values (Fenton and Neil, 2013). Various forms of sensitivity analysis are implemented in AgenaRisk and Hugin.

In [Vlek \(2016\)](#), sensitivity analysis is mentioned, but not applied. On the other hand, in [Fenton et al. \(2019\)](#), each individual hypothesis node is subjected to sensitivity analysis, to find out how every parameter in the nodes needs to change in order to result in a 0.95 or a 0.99 posterior for guilt. There are only a few ways that individual nodes can change that would result in a high probability of guilt, from which the authors interpret that the constructed BN is robust to small inaccuracies in subjectively elicited CPTs. However, in the paper, this is only shown for one evidence state. It is not clear how the BN would respond to ‘counterfactual’ pieces of evidence.

2. Cumulative evidence

Another way of evaluating the response of the BN, is by seeing its response to cumulatively setting evidence. This way, we can see how much each piece of evidence (from the defence or the prosecution) changes our belief in the posterior of the output node(s). We could subjectively assess if it makes sense that a certain piece of evidence has a large, or small, effect on the posterior. In both ([Fenton et al., 2019](#)) and ([Vlek, 2016](#)) this cumulative approach shows that, in general, the evidence from the defence decreases our belief that the suspect is guilty, and evidence from the prosecution increases our belief that the suspect is guilty. However, in both cases, the BN is only evaluated on one state of evidence. Both cases only test the cumulative probability of the output node by turning the evidence nodes to values that correspond to the findings of the court.

However, this is a **red**risky move, since this might lead to **red**overfitting the probabilities in the CPTs, so that the network seems to reflect the right ‘evidence strength’ on the court-found state of evidence, but is actually misrepresenting other combinations of evidence, without a way of checking if this is the case.

redOur findings in [Figure 10](#) show that it is necessary to consider all possible combinations of evidence. If we have tunnel vision and only focus on the state of evidence that is found in court, we might create a network that overfits on one state of evidence. This means that if there was a re-trial and the court would decide that some pieces of evidence are not admissible after all, the BNs might show the unreasonable behaviour. Additionally, if we are building the BN before or during the court case, we cannot know yet which state we are in, as none of the evidence has been established yet. Therefore, the network should work correctly over all possible evidence states. If we want to take the premise behind BNs seriously, we have to create a

network that gives sensible results for all possible combinations of evidence, not just the valuation of the evidence that is initially established in court.

2.3 Simulation

We are using agent-based simulations to investigate methods for evaluating Bayesian Networks. Agent-based modelling is a modelling primitive that allows researchers to study models in which agents interact with their environment and with other agents ([Gilbert and Terna, 2000](#)).

Agent-based modelling is useful for simulating criminal behaviour in spatially explicit ways. The actions of a thief and victim are constrained by geography and local knowledge. For instance, a thief cannot move through buildings like a ghost, or steal from someone they have not seen. Due to specific interactions that arise out of the circumstances in each run of the simulation, we can collect frequency information about all the relevant events in our modelled scenario that would be hard to estimate with subjective probabilities or with mathematical (non-spatially explicit) models. Since we have full knowledge of the frequency of events in the simulation, we can use it as a ‘grounding’, or baseline. In a sense, the simulation is a data-generating environment for criminal cases. If we look at the taxonomy of agent-based model levels in ([Gilbert and Troitzsch, 2005](#)), where level 3 is a simulation that really reflects the real world, and level 0 is a ‘caricature of reality, as established with simple graphical devices’, the simulation in this paper is at level 0, to reduce unnecessary modelling and time complexity. In this project, the simulations are programmed in Python using the MESA framework ([Kazil et al., 2020](#)).

3 Method

Our goal is to establish a method for evaluating BNs by preventing overfitting on one evidence state. We can consider an approach in four stages.

1. *Scenarios* We need a set of alternative scenarios that are to be modelled. These scenarios are written description of crime scenarios that contain the hypothetical events and evidence for these events, as postulated by the prosecution and defence.
2. *Simulation* Based on this written description of the scenario(s) to be modelled, an agent-based simulation is created, by first identifying and operationalising all relevant agents, objects and environments, and secondly identifying and operationalising all relevant events. Depending on the goal and complexity of the scenarios to be modelled, the granularity and overall level of the simulation should be considered. The simulation should be repeated until we find the limiting frequency of all events. These frequencies are collected.
3. *Construction* The collected frequencies are used by the K2 algorithm to automatically build a Bayesian Network of the simulation.
4. *Evaluation* The generated Bayesian Network is evaluated on all possible states of the evidence.

3.1 Scenarios

We start our process with one or more written scenarios. These scenarios can be obtained from abridged or simplified court case descriptions of the crime, or they can be wholly fictional (such as in this paper). The scenarios should contain all and only those hypotheses and evidence that are relevant to the case. Both the prosecution and the defence should be able to select relevant events and their evidence.

3.2 Simulation

We can think of the simulation as having two parts: a model of reality, and a way of observing the model by observing variables that the modellers deem interesting. In this paper, the model of reality is an agent-based simulation, and the observation procedure are random variables (or, reporters), which become nodes in the BN. Specifics about the model are explained in the next section.

3.2.1 Model

The agent-based simulation is a simulation that should include the possibilities for all the scenarios as outlined in step 1. It should contain agents, objects and an environment. The agents should traverse the environment, interacting with each other and using objects to be able to do certain interactions (think about stealing an object, or opening a door with a key).

The level of detail or real-world validation at which agents, objects and environments are modelled depend on the purposes of the simulation. We can build a simulation in which agents behave according to a certain criminological theory (such as in (Haojie Zhu, 2021)), in order to investigate how well the outcomes of this simulation line up with data as gathered in reality. However, in this paper, we are focussing on using simulations as a grounding to investigate Bayesian Networks. The detail of the simulation should be kept to the smallest complexity that is possible: it should be complex enough that Bayesian Networks can be usefully applied to it (eg: there should be uncertainty, conditional probabilities, and different states). The focus should be on modelling those nodes, and only those nodes, that are relevant for the Bayesian Network method aspect that is under investigation (for example, creating a simulation to ground a network about the opportunity prior (Fenton et al., 2017) or the scenario-idiom (Vlek, 2016), in this thesis ‘reasoning with evidence’ in general and evaluating BNs over all possible evidence states specifically). The simulation should not be made more complicated than necessary to limit debugging time and complexity.

3.2.2 Reporters

In the simulation, certain events can be brought about. Any one of the above-mentioned events can happen. We need a way to observe these states: this is where reporters come in. A reporter is a random variable that reports the outcome of a relevant event in the simulation and is embedded in the code. If an event happens (or does not happen), the reporter reports that the event is true (or false). In essence, the reporter (R) is a random variable (RV). In short, a random variable is a function that maps an event (e) to a truth value:

$$R : e \rightarrow \{0, 1\}$$

No matter how many reporters we define, we can combine all reporters at the end of one run of the simulation into a global state G .

$$G = (e_0 \rightarrow \{0, 1\} \times e_1 \rightarrow \{0, 1\} \times \dots \times e_n \rightarrow \{0, 1\})$$

or, for n reporters:

$$G = R_1 \times R_2 \times \dots \times R_n$$

We collect these global states over the number of runs that we do for each experiment, which results in the output O of this stage of the method, is a series of global states, one for each run:

$$O = (G_0, G_1, \dots, G_{runs})$$

3.3 Construction

The output of this method is the collection of runs O , where each run is the global state G of the simulation, as measured by the random variables R . These random variables become the nodes in the Bayesian Network.

The Bayesian Network is generated automatically, using the automated BN learner method as implemented in pyAgrum. There are several learners implemented in pyAgrum.² The algorithm used in this experiment to structure the Bayesian Network from the simulation data is the K2 algorithm (Cooper and Herskovits, 1992).

The K2 algorithm is a greedy search algorithm that attempts to maximise the posterior probability of the network by correctly connecting parent nodes to child nodes. It takes an ordering on the nodes as input. The first node in the ordering X_0 does not have any parents. For two nodes X_i and X_j , X_j cannot be the parent node of X_i if $j > i$: a node can only have a parent that is earlier in the ordering. The algorithm processes each node X_i by adding possible parent nodes to X_i (as constrained by the ordering), and maximising the score of the network. The algorithm stops if there are no parents to add, no parents improve the score, or the node has reached the maximal number of parents (Chen et al., 2008).

Due to this ordering constraint, the K2 algorithm is efficient. However, finding the ordering of the nodes as input for the network is not trivial. The ordering should be meaningful, to reflect causal or temporal information present in the domain. By

²An introduction to structure learning using PyAgrum: <http://webia.lip6.fr/~phw/aGrUM/docs/last/notebooks/structuralLearning.ipynb.html>

adding the nodes to the simulation in the relevant order, we can ensure that the order is temporal.

3.4 Evaluation

We can evaluate the response of the Bayesian Network using the effect of cumulative evidence on the posterior probability of the output nodes. This means that we order the evidence nodes chronologically, then instantiate every evidence node to a truth value (either T or F) in order. Then, we measure the posterior probability of all output nodes. This results in a diagram or table where we can see the evidence strength of each piece of true or false evidence reflected. We propose a method for evaluating Bayesian Networks over all possible global evidence states in this paper. This method is described here.

1. **Run** Run the simulation to generate the ‘ground truth’.
2. **BN** Select the BN we want to evaluate.
3. **Selection** From the BN, select all evidence nodes (a total of e) and the relevant outputs O .
4. **Order** Order the evidence nodes. The order can be chronological, or can be the order that the evidence was presented in a court case. Ordering is not necessary for the calculating the posterior on all evidence, but consistency makes comparing figures like ?? and ?? possible.
5. **Collect** Collect all evidence states. This is the set of 2^e combinations of evidence. An evidence state is a valuation of evidence, where for every evidence node, a truth value is specified.
6. **Subset** From the previous step, select only the possible evidence states. We can extract the possible evidence states automatically from a simulation: we run it many times, and select the states that occur at least once in the outcome. The possible evidence states can also be elicited from experts by asking them to manually consider each evidence state.
7. **Frequencies** For every possible evidence state, calculate the frequency distribution of the relevant outputs O by finding the frequency at which every outcome occurs, for every evidence state. Speaking generically about two alternative, non-mutually exclusive outcomes scenario 1 ($scn1$) and scenario 2 ($scn2$), we need to find a probability distribution over $scn1, \neg scn1 \wedge scn2, \neg scn1 \wedge \neg scn2$ that is constrained by $P(scn1) + P(\neg scn1 \wedge scn2) + P(\neg scn1 \wedge \neg scn2) = 1$. Or,

a weaker version, we create a preference ordering on $scn1, \neg scn1 \wedge scn2, \neg scn1 \wedge \neg scn2$, without specifying probabilities. We can automatically create the frequency distribution over outcomes for all states of evidence from the data gathered in the simulation. If we do not have access to frequency data, then subjective frequencies (or a preference ordering over the output) need to be elicited from experts.

8. **Posteriors** For every possible evidence state, turn the relevant nodes in the BN on in order. At each step, record the posterior probability over the outputs. Automatically convert the probability distribution over the outcomes into a preference ordering.
9. **Accuracy Evidence State** Compare the BN prediction of output nodes given evidence to the frequency distribution as established in step 5). Once all evidence is added, we can calculate the divergence of the BN prediction and the actual frequency given the cumulative evidence E in the simulation by

$$|P(output|E) - F(output|E)|$$

10. **Accuracy Total** Calculate the total accuracy per output node by

$$\frac{\sum_{i=0}^e |P(output|E_i) - F(output|E_i)|}{e}$$

For the preference ordering, we do the same, only we calculate a counting score: when the preference ordering extracted from the BN is the same as the one from the simulation, we give a point, otherwise we do not, then average this over all sets of evidence.

4 Case Study: Robbery at Grote Markt

We illustrate the method by means of applying it to a case study of a robbery at the Grote Markt, the central square in Groningen.

4.1 Experimental Set-up

BNs were created and evaluated based on different number of runs, to evaluate how the accuracy of the BN depends on the data available to it.

We want to create both a ground truth, that are the frequencies that we're interested in, and then the probabilities that are going to approximate it so that we can check the accuracy of the network. To find the ground truth, we need to find the limiting frequencies of the events in the simulation, the simulation was run 10,000 times. One thing we want to find out is the necessity of precision on the outcome of the networks. This was done by changing the number of runs that the BN was created on. The different number of runs of the simulation were [1, 50, 100, 300, 500, 750, 1000] for creating the BNs.

Every simulation was run for 100 steps, or until both agents were in their target states.

4.2 Scenarios

We have established three different scenarios. In all scenarios, there are two people walking around the Grote Markt. One person is young, and the other person is old and carries a valuable object.

In scenario 1 (scn1), the young person sees the old person, assesses whether the object is valuable enough to risk stealing, and if the old person is vulnerable enough to steal from, and a motive is established. Then, if the young person has a motive, they will attempt to sneak up on the old person. When they get near, they steal from the old person.

In scenario 2 (scn2), the young person might still be doing all of the above (or they might not), however, before they can steal, or if they decide that they're not stealing at all, the old person drops the object accidentally.

In scenario 3, neither scenario 1 or scenario 2 happens. The people walk around at Grote Markt and then go home. We do not have to represent scenario 3 explicitly, it can be represented as neither scn1 nor scn2.

For our evidence, we have a psychological assessment of the young person, that assesses whether they are psychologically capable of stealing from the old person. We also have cameras at Grote Markt that show whether the young person was seen at all, or was seen stealing. Additionally, we have the fact that the object is gone or not.

4.3 Simulation

Now we need a way to transform the natural language descriptions of the events in the scenarios to observable events in the simulation. First, we identify all relevant actors, objects and environments in the scenario and operationalise them in a simulation. Second, we identify the relevant reporters.

4.3.1 Model

Agents can interact with other agents and with their environment. Every agent has features, functions and roles associated with them. The agents in this simulation are created from the MESA agent class. These are goal-based agents. Based on the scenarios as described in the previous step, we want to create one older, vulnerable agent, and one younger potential thief. In principle, the simulation is flexible enough that any agent can be a thief, as motive is determined by a risk-trade-off and not something inherent to the agents themselves. However, since we wanted to avoid problems with identity and follow the scenarios, we made sure that only one agent would be the thief, by having it have an object that was not valuable and an age that was not vulnerable. The behaviour of the agents is depicted in Figure 2.

All agents have the following **attributes**:

role Every agent has a role of either victim or thief. In a more realistic scenario this role would be assigned based on behaviour, but in this simulation, this was done at the start (because the scenario allows for one thief, and one victim). However, the role ‘thief’ does not mean that the agent will actually steal, and the role ‘victim’ does not mean that the agent will be robbed³: if the victim drops the object, or if the thief and victim never meet, these roles are not fulfilled by the agents. Hence, the role only implies a certain potentiality.

id Every agent has an ID. The thief has ID 1, the victim has ID 0.

³From now on the ‘ around the roles are dropped

object The thief has an object with a value of 0, the victim's object has a value drawn from a uniform distribution between 500 and 1000.

goal location The goal location of the agent is either it's initial goal location that was assigned at the start, or, when the agent has a motive, it is the current location of the victim agent. The initial goal location for each agent is drawn randomly from any of the accessible locations at the edge of the map.

age The thief's age was 25, the victim's age was drawn from a uniform distribution between 60 and 90.

risk threshold The risk threshold for the victim agent was set to 5000, such that it is never worth for it to steal, the risk threshold for the thief is randomly drawn from a uniform distribution between 800 and 1200.

age threshold The age threshold signifies at what age an agent considers another agent vulnerable: older agents are more vulnerable than younger agents. The victim's age threshold is set to 100, it will only steal from agents that are 100 years or older. The thief's threshold is randomly drawn from a uniform distribution between 50 and 100.

steal state The possible steal states are described as follows:

N Initial state and state that the agent returns to if they fail to perform the task assigned by their state

MOTIVE Agent has selected a target (target is vulnerable and object is valuable)

SNEAK Agent moves towards target's position

STEALING Agent is near target and attempts to steal

SUCCESS Agent has successfully stolen object

DONE Agent has reached their goal location

LOSER Agent has been stolen from

All agents have the following **actions**:

hang around Agents move around randomly.

walk Using standard mesa functionality, at every step of the agent, the agent moves 1 cell in the Moore neighborhood. The agent attempts to walk towards its goal state, whether that is a moving agent or their goal state. They move towards

their goal state by taking the possible step that minimises the distance between their goal and themselves using the Euclidian distance as measure (this does not take buildings into account).

escape Given the use of Euclidian distance instead of a smarter, geographically-informed approach (using waypoints or something similar), agents can get trapped in tight corners of the simulation when they're moving towards their goal. There is an epoch tracker that counts 'stuckness' and then moves the agent into the 'hang around' state, of random movement, for a given time. This means eventually the agent will randomly move away from the 'stuckness'.

see every agent has a visual range of 10 cells. This means that all simulation objects (agents, objects) within that radius are selected. Actual vision is only calculated based on line-of-sight, which means that for each object in range, we use the Bresenham's line algorithm to select the relevant cell that lie on the 'environment grid' in between the agent and the object that it is seeing. For every cell on the straight path between the two objects, we check whether it is 'accessible' or 'non-accessible'. Agents, and light, cannot pass through 'non-accessible' cells. This is an abstraction, in real life there are windows. So if there's one 'inaccessible' cell on the list of cells that are the straight line between seeing agent and object, the agent is not able to see the object.

decide valuable Once the thief has a targeted victim, the thief knows the value of the object of the victim. In this function, the agent decides whether the object is worth stealing. If the value of the object is larger than the risk threshold of the agent, the object is deemed valuable.

decide vulnerable Once the thief has a targeted victim, the thief knows the age of the victim. In this function, the agent decides whether the victim is vulnerable enough to steal from: if the age of the victim is older than the age threshold, the thief considers the victim vulnerable.

sneak Agent moves to the position of the victim, only it can move with a radius of 2 (hence, at higher speed).

steal Whenever the thief is in the same cell as the victim - and they're both still within the simulation (so the victim has not reached its goal yet), the thief steals successfully.

The environment is a discrete grid of size $x = 75$, $y = 50$ that represents the geography of the Grote Markt. The real area of interest is approximately 425m x 280m,

as estimated by the distance tool on Google Maps. This means that one cell in the simulation is equivalent to a square of 5.6m x 5.6m in real life. An agent can move 1 cell per time-step, which means that, given an average human walking speed of 1.4m/s ⁴, one time-step is equivalent to 4 seconds in real life. For the purposes of this simulation, this spatial and time resolution is high enough.

To simulate which parts of the Grote Markt were accessible to the agents, we had to convert a map image of the Grote Markt into an agent-readable world. This was done by writing a method to convert screenshots of maps into an agent-readable environment. The map was screenshotted from <http://maps.stamen.com/terrain/#18/53.21618/6.57225> and converted into greyscale. A grid was overlaid on the image. On the greyscale map, the color of the buildings was in the range of (189, 199): cells within this range were coded as ‘inaccessible’, since agents cannot walk through buildings. All other cells were ‘accessible’. This resulted in a map shared by all agents that constrained their movements. The map constrains both vision and movement of the agent: we used this map to calculate the sight lines of both cameras and agents. An agent or a camera can only see another agent if there are no ‘inaccessible’ grid cell on the sight line between the two, and the other agent is within their visual range. The environment is shown in Figure 4.

There are two types of objects in the simulations, which are the valuable object, and the cameras.

In the scenario, an object is described as being in the possession of agents, or lost accidentally. In this simulation, the object was operationalized as being a feature of the agent, and not as an individual thing by itself.

There are 5 cameras in the simulation. They are placed randomly on the ‘accessible’ cells on the map. Every camera has a visual radius of 5, corresponding to a range of 28m, which is about equivalent to the visual range of real-life security cameras ⁵.

4.3.2 Reporters

We divide all all events into three classes: either an event is ‘evidence’ (E), a ‘hypothesis’ (H), or an ultimate ‘outcome’ (O).

The process of operationalisation is very subjective and depends entirely on the modeller’s assumptions and their time, knowledge or skill constraints. The behaviour of

⁴https://en.wikipedia.org/wiki/Preferred_walking_speed

⁵<https://securitycamcenter.com/how-far-can-security-cameras-see/>

agents, as reflections of actual people, can be modelled in a way that reflect real sociological theories of behaviour (such as in [Gerritsen \(2015\)](#)), or with simple behavioural rules and a random number generator, as in this approach. The environment of the simulation can reflect a real-world geography with different affordances, or can be simplified.

The operationalisation of the random variables is described below.

- (H) **motive_1_0** agent 1's steal state is MOTIVE.
- (H) **sneak_1_0** agent 1's steal state is SNEAK.
- (O) **stealing_1_0** agent 1's steal state is STEALING.
- (O) **object_dropped_accidentally_0** At every epoch, there is a 1/500 probability that the victim agent will drop the object by accident. If the object is dropped, this reporter is turned on.
- (E) **E_psych_report_1_0** indicates a 'psychological profile' for the thief, to establish whether they would be able to steal the object or not. If the thief does not have a motive, there is no chance that it is picked (in-simulation), hence no psych report is established, the reporter remains 0. If the thief has a motive, there is a 0.9 probability that the psych report indicated that the thief is capable of stealing, and 0.1 probability that the thief could not have stolen the object. In this second case, the psych report is incorrect. This reporter is not represented spatially in the simulation.
- (E) **E_camera_1** agent 1 is seen on any one of the cameras.
- (E) **E_camera_seen_stealing_1_0** if any camera sees agent 1 when agent 1's steal state is STEALING.
- (E) **E_object_gone_0** if the object is dropped accidentally, or if the object has been stolen.

A global state where the thief stole the object and all the evidence pointed in this direction, would be represented as (reporters in the same order as in the listing above):

1, 1, 1, 0, 1, 1, 1, 1, 1

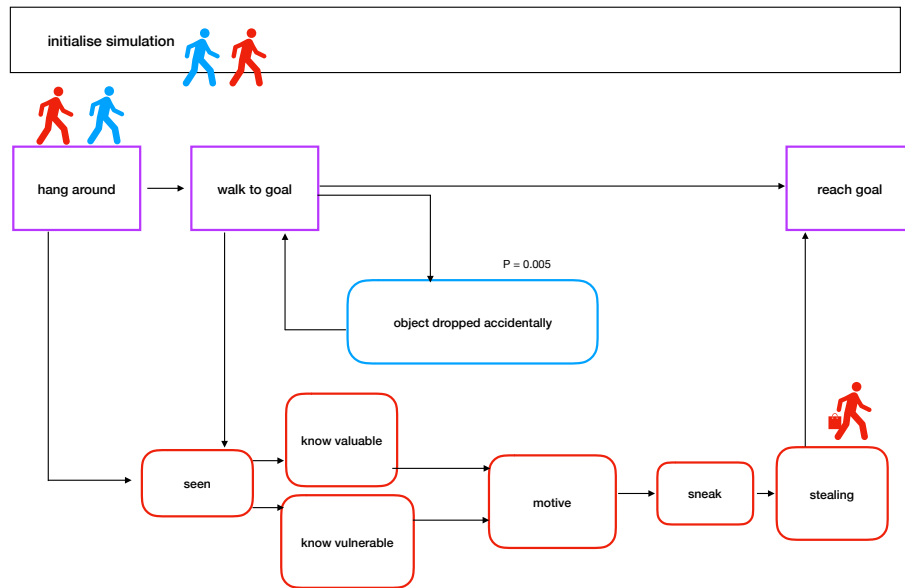


Figure 2: The behaviour of the agents. The nodes with rounded edges correspond to the nodes in the Bayesian Network.

There are two agents, a thief and a victim.



Figure 3: map of environment - 2 agents

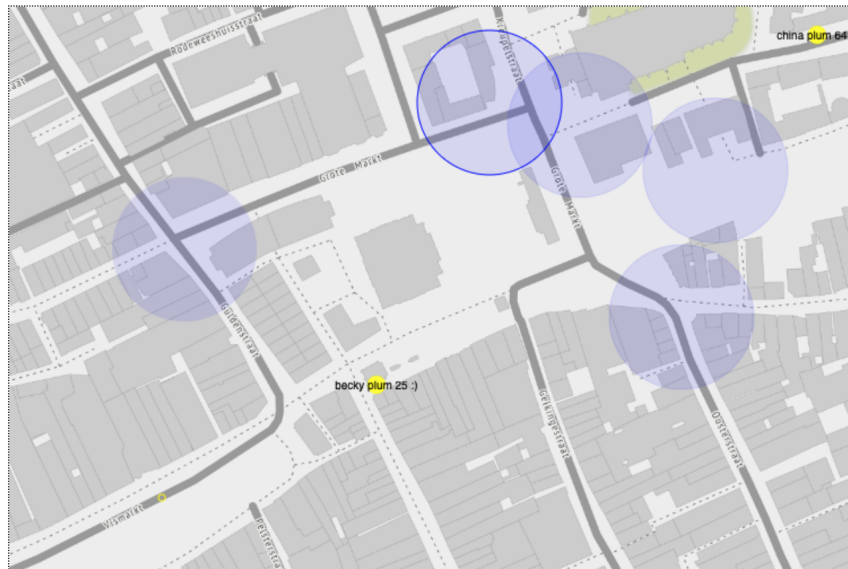


Figure 4: Camera locations are randomly initialized

4.4 Construction

The baseline was created by running the simulation for 10,000 runs. Then, to test to what extent the number of runs (=the amount of data available to the K2 algorithm) influences the accuracy of the network, for each of [1, 50, 100, 300, 500, 750, 1000] runs, the collection of runs O was passed to the K2 algorithm, that generated a network.

The K2 algorithm requires an ordering on the nodes. In all number of runs, this ordering was [object_dropped_accidentally_0, motive_1_0, sneak_1_0, stealing_1_0, E_psych_report_1_0, E_camera_1, E_camera_seen_stealing_1_0, E_object_gone_0]. This ordering was determined by considering the hypothesis-nodes first, and all evidence at the end. We want evidence nodes to be the children of hypotheses nodes, to follow the hypothesis-evidence idiom as established by Fenton. This means that we have to add them the latest in the ordering, so that they will not be parent nodes to hypothesis nodes. The hypothesis nodes belong to two different scenarios: scenario 1 is the motive-sneak-steal scenario, and scenario 2 is the accidental-object-dropped scenario (scn2). Placing scn2 before scn1 in the ordering is not arbitrary. We have to invoke causality in order to establish that this is a sensible ordering: if the agent drops the object, the thief cannot have a motive to steal the object, yet, having a motive does not ‘cause’ or ‘condition’ the object to drop. Hence, the ‘object_dropped_accidentally_0’ should be the parent node, if we’re taking a causal interpretation. We are not required to place scn2 before scn1 in the ordering if we are only using conditional probabilities as constraint.

4.5 Evaluation

1. **Run** We run the simulation 10,000 times to collect the ground truth.
2. **BN** We test all the BNs that we generated. We are generating 7 BNs, every one generated from a dataset with a different size: [1, 50, 100, 300, 500, 750, 1000]. This means we do this evaluation loop 7 times, each time testing a different BN.
3. **Selection** The evidence nodes of the network are the 4 (binary) nodes marked with an ‘E’, which are [E_camera_1, E_camera_seen_stealing_1_0, E_object_gone_0, E_psych_report_1_0]. The output nodes are [‘object_dropped_accidentally_0’, ‘stealing_1_0’].
4. **Order** We order the evidence nodes in the same order as they were presented to the K2 algorithm: [E_psych_report_1_0, E_camera_1, E_camera_seen_stealing_1_0,

E_object_gone_0].

5. **Collect** There are $2^4 = 16$ evidence states in total.
6. **Subset** We can eliminate 7 of the evidence states, because they never occur in simulation. In Table 1, we present an overview of all possible states as generated by the and, if they do not occur at all, why they are impossible.

state	remarks
(0, 0, 0, 0)	ok
(0, 0, 0, 1)	ok
(0, 0, 1, 0)	we cannot have stealing on camera if the agent was not seen on camera
(0, 0, 1, 1)	we cannot have stealing on camera if the agent was not seen on camera
(0, 1, 0, 0)	ok
(0, 1, 0, 1)	ok
(0, 1, 1, 0)	we cannot have stealing on camera without the object being gone
(0, 1, 1, 1)	ok
(1, 0, 0, 0)	ok
(1, 0, 0, 1)	ok
(1, 0, 1, 0)	we cannot have stealing on camera without the object being gone
(1, 0, 1, 1)	we cannot have stealing on camera if the agent was not seen on camera
(1, 1, 0, 0)	we cannot have both psychological report, agent on camera, and not have stealing
(1, 1, 0, 1)	ok
(1, 1, 1, 0)	we cannot have stealing on camera without the object being gone
(1, 1, 1, 1)	ok

Table 1: Possible and impossible states

7. **Frequencies** Using the possible evidence states identified in the previous step, in the ground truth dataset of 10,000 items, calculate the frequency distribution over the possible outcomes. In Table 2 we present the frequencies as generated by the ground truth of the three outcomes, as well as their preference ordering.
8. **Posteriors** For every evidence state, we use the BN as model. In the BN, we turn the evidence nodes to the value specified by their evidence state. We used the LazyPropagation inference engine in PyAgrum to calculate the posteriors of the outcomes in the BN, given the evidence state as input.
9. **Accuracy Evidence State** The posteriors of the outcome nodes in the net-

evidence	H1	H2	H3
(0, 0, 0, 1)	F(dropped) (0.99)	F(steal) (0.01)	F(neither) (0.00)
(0, 0, 0, 0)	F(neither) (1.00)	F(steal) (0.00)	F(dropped) (0.00)
(0, 1, 0, 1)	F(dropped) (0.99)	F(steal) (0.01)	F(neither) (0.00)
(1, 0, 0, 1)	F(steal) (0.93)	F(dropped) (0.07)	F(neither) (0.00)
(0, 1, 0, 0)	F(neither) (1.00)	F(steal) (0.00)	F(dropped) (0.00)
(1, 1, 0, 1)	F(steal) (0.93)	F(dropped) (0.07)	F(neither) (0.00)
(1, 1, 1, 1)	F(steal) (0.95)	F(dropped) (0.05)	F(neither) (0.00)
(1, 0, 0, 0)	F(neither) (1.00)	F(steal) (0.00)	F(dropped) (0.00)
(0, 1, 1, 1)	F(steal) (1.00)	F(dropped) (0.00)	F(neither) (0.00)

Table 2: Frequencies of outcomes for all possible evidence states

work are compared to frequency of those outcomes in the ground truth. The accuracy of the BN per evidence state is presented in the next section.

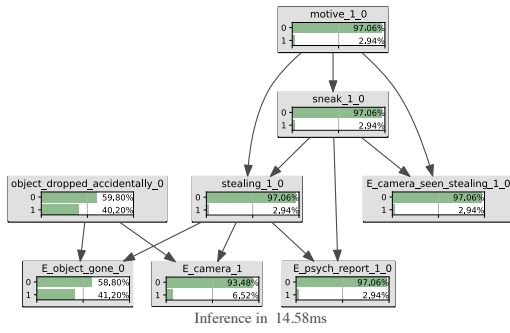
10. **Accuracy Total** The total accuracy per output node is presented in the next section.

5 Results

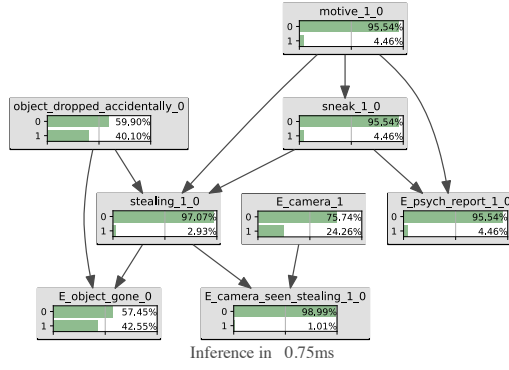
We have the final Bayesian Networks (Figure 5) as created by the K2 algorithm to the runs from the simulation, except when we run the simulation 1 time. If we run the simulation 1 time, the network cannot be produced, as there is not enough data available to the algorithm. In Figure 5, we can see that the structure of the network is not stable: the parents of the nodes depend on the number of runs that were available to the K2 algorithm.

However, despite the variability in network structure, all networks have some important commonalities. In all networks, we see that the evidence ‘E_object_gone_0’ has the parents ‘stealing_1_0’ and ‘object_dropped_accidentally_0’, which correctly reflects the two events under which the object can be done. We also find that generally, ‘motive_1_0’ is a parent node of ‘stealing_1_0’, which reflects the underlying causality that the agent cannot steal without having a motive.

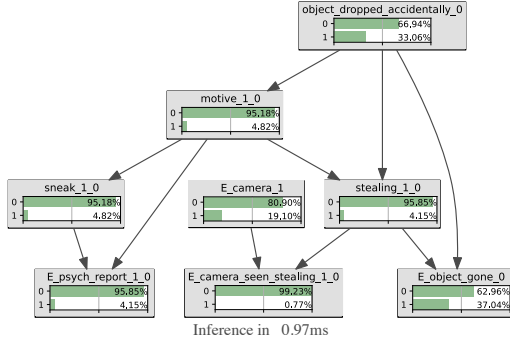
For each of these networks, we set the possible evidence states as outlined in the case study. This means that, for every possible combination of evidence, we find the posterior probability of every output node. This results in a joint probability distribution over all three possible outputs. These are found for all evidence states,



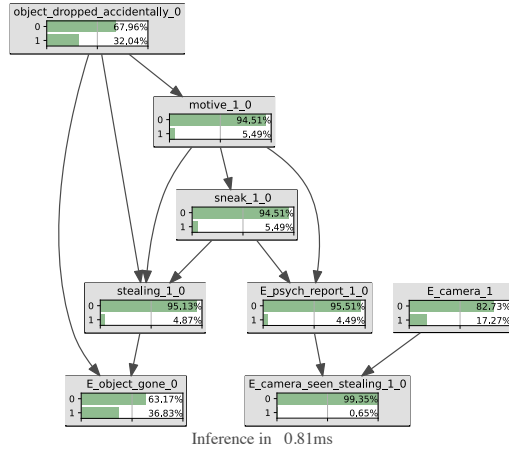
(a) The final network (50 runs)



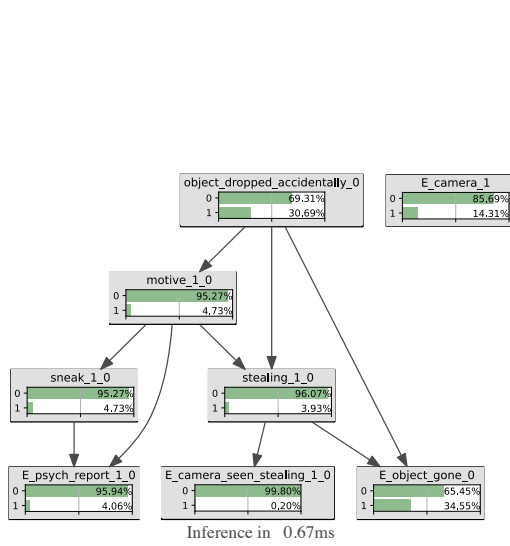
(b) The final network (100 runs)



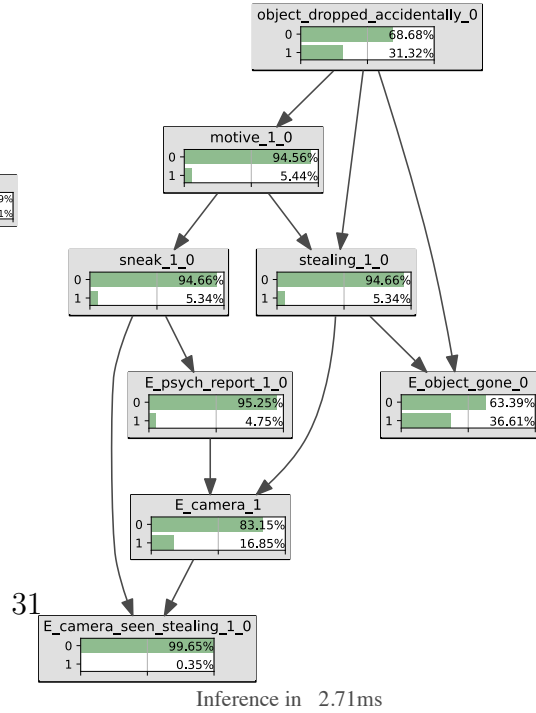
(c) The final network (300 runs)



(d) The final network (500 runs)



(e) The final network (750 runs)



(f) The final network (1000 runs)

Figure 5: All final networks

for every number of runs ⁶, in Tables 3 - 8. We can already see here that there are networks that produce inconsistent results. For example, see the evidence state of (1, 0, 0, 1) in Table 3. In this state, we find that $P(\text{neither}) = -0.26$. This shows that this network cannot represent accurately the mutual exclusive and exhaustive relationship of the three output nodes. As the dataset from which the networks are built increases in size, these inconsistencies decrease.

evidence	H1	H2	H3
(0, 0, 0, 1)	P(dropped) (0.99)	P(neither) (0.01)	P(steal) (0.00)
(0, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 0, 1)	P(dropped) (0.97)	P(steal) (0.03)	P(neither) (0.00)
(1, 0, 0, 1)	P(dropped) (0.86)	P(steal) (0.40)	P(neither) (-0.26)
(0, 1, 0, 0)	P(neither) (0.74)	P(dropped) (0.15)	P(steal) (0.11)
(1, 1, 0, 1)	P(steal) (0.96)	P(dropped) (0.21)	P(neither) (-0.17)
(1, 1, 1, 1)	P(steal) (0.99)	P(dropped) (0.18)	P(neither) (-0.17)
(1, 0, 0, 0)	P(neither) (0.57)	P(steal) (0.22)	P(dropped) (0.21)
(0, 1, 1, 1)	P(steal) (0.88)	P(dropped) (0.27)	P(neither) (-0.15)

Table 3: Posteriors of output nodes for 50 runs

evidence	H1	H2	H3
(0, 0, 0, 1)	P(dropped) (0.99)	P(steal) (0.01)	P(neither) (0.00)
(0, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 0, 1)	P(dropped) (1.00)	P(steal) (0.00)	P(neither) (0.00)
(1, 0, 0, 1)	P(steal) (0.59)	P(dropped) (0.43)	P(neither) (-0.02)
(0, 1, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(1, 1, 0, 1)	P(dropped) (0.87)	P(steal) (0.13)	P(neither) (0.00)
(1, 1, 1, 1)	P(steal) (1.00)	P(dropped) (0.03)	P(neither) (-0.03)
(1, 0, 0, 0)	P(steal) (0.44)	P(neither) (0.36)	P(dropped) (0.20)
(0, 1, 1, 1)	P(dropped) (0.58)	P(steal) (0.53)	P(neither) (-0.11)

Table 4: Posteriors of output nodes for 100 runs

Now that we have the posterior probabilities for all outputs for all evidence states, we present the accuracy of the network, by comparing the posterior output of every BN to the ‘ground truth’ frequency-output of the simulation. The accuracy per output node, for every state of evidence, is presented in Table 9. Overall, the networks have an accuracy of 0.88. Networks that are created from a larger dataset, have higher accuracies than networks generated from smaller accuracies.

⁶Excluding 1, as this did not result in a network

evidence	H1	H2	H3
(0, 0, 0, 1)	P(dropped) (0.98)	P(steal) (0.02)	P(neither) (0.00)
(0, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 0, 1)	P(dropped) (0.99)	P(neither) (0.01)	P(steal) (0.00)
(1, 0, 0, 1)	P(steal) (0.91)	P(dropped) (0.10)	P(neither) (-0.01)
(0, 1, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(1, 1, 0, 1)	P(steal) (0.68)	P(dropped) (0.32)	P(neither) (0.00)
(1, 1, 1, 1)	P(steal) (1.00)	P(dropped) (0.01)	P(neither) (-0.01)
(1, 0, 0, 0)	P(neither) (0.84)	P(steal) (0.12)	P(dropped) (0.04)
(0, 1, 1, 1)	P(steal) (0.87)	P(dropped) (0.16)	P(neither) (-0.03)

Table 5: Posteriors of output nodes for 300 runs

evidence	H1	H2	H3
(0, 0, 0, 1)	P(dropped) (0.97)	P(steal) (0.03)	P(neither) (0.00)
(0, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 0, 1)	P(dropped) (0.97)	P(steal) (0.03)	P(neither) (0.00)
(1, 0, 0, 1)	P(steal) (0.88)	P(dropped) (0.12)	P(neither) (0.00)
(0, 1, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(1, 1, 0, 1)	P(steal) (0.88)	P(dropped) (0.12)	P(neither) (0.00)
(1, 1, 1, 1)	P(steal) (0.88)	P(dropped) (0.12)	P(neither) (0.00)
(1, 0, 0, 0)	P(neither) (0.51)	P(steal) (0.38)	P(dropped) (0.11)
(0, 1, 1, 1)	P(dropped) (0.97)	P(steal) (0.03)	P(neither) (0.00)

Table 6: Posteriors of output nodes for 500 runs

evidence	H1	H2	H3
(0, 0, 0, 1)	P(dropped) (0.98)	P(steal) (0.02)	P(neither) (0.00)
(0, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 0, 1)	P(dropped) (0.98)	P(steal) (0.02)	P(neither) (0.00)
(1, 0, 0, 1)	P(steal) (0.87)	P(dropped) (0.13)	P(neither) (0.00)
(0, 1, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(1, 1, 0, 1)	P(steal) (0.87)	P(dropped) (0.13)	P(neither) (0.00)
(1, 1, 1, 1)	P(steal) (1.00)	P(dropped) (0.00)	P(neither) (0.00)
(1, 0, 0, 0)	P(neither) (0.91)	P(steal) (0.07)	P(dropped) (0.02)
(0, 1, 1, 1)	P(steal) (0.71)	P(dropped) (0.30)	P(neither) (-0.01)

Table 7: Posteriors of output nodes for 750 runs

evidence	H1	H2	H3
(0, 0, 0, 1)	P(dropped) (1.00)	P(steal) (0.00)	P(neither) (0.00)
(0, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 0, 1)	P(dropped) (0.91)	P(steal) (0.09)	P(neither) (0.00)
(1, 0, 0, 1)	P(steal) (0.97)	P(dropped) (0.03)	P(neither) (0.00)
(0, 1, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(1, 1, 0, 1)	P(steal) (0.99)	P(dropped) (0.01)	P(neither) (0.00)
(1, 1, 1, 1)	P(steal) (0.99)	P(dropped) (0.01)	P(neither) (0.00)
(1, 0, 0, 0)	P(neither) (0.67)	P(steal) (0.25)	P(dropped) (0.08)
(0, 1, 1, 1)	P(steal) (0.96)	P(dropped) (0.04)	P(neither) (0.00)

Table 8: Posteriors of output nodes for 1000 runs

runs	50		100		300		500		750		1000		av
evidence	S	D	S	D	S	D	S	D	S	D	S	D	
(0, 0, 0, 1)	0.99	1.00	1.00	1.00	0.99	0.99	0.98	0.98	0.99	0.99	0.99	0.99	0.99
(0, 0, 0, 0)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
(0, 1, 0, 1)	0.98	0.98	0.99	0.99	0.99	1.00	0.98	0.98	0.99	0.99	0.92	0.92	0.98
(1, 0, 0, 1)	0.47	0.21	0.66	0.64	0.98	0.97	0.95	0.95	0.94	0.94	0.96	0.96	0.80
(0, 1, 0, 0)	0.89	0.85	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.98
(1, 1, 0, 1)	0.97	0.86	0.20	0.20	0.75	0.75	0.95	0.95	0.94	0.94	0.94	0.94	0.78
(1, 1, 1, 1)	0.96	0.87	0.95	0.98	0.95	0.96	0.93	0.93	0.95	0.95	0.96	0.96	0.95
(1, 0, 0, 0)	0.78	0.79	0.56	0.80	0.88	0.96	0.62	0.89	0.93	0.98	0.75	0.92	0.82
(0, 1, 1, 1)	0.88	0.73	0.53	0.42	0.87	0.84	0.03	0.03	0.71	0.70	0.96	0.96	0.64
total	0.88	0.81	0.766	0.781	0.934	0.941	0.827	0.857	0.939	0.943	0.942	0.961	0.88

Table 9: Accuracy per state

In Figure 6, we average over all possible evidence states and show the average accuracy of the output nodes ‘stealing_1_0’ and ‘object_dropped_accidentally_0’, per number of runs, as well as the accuracy of the preference ordering.

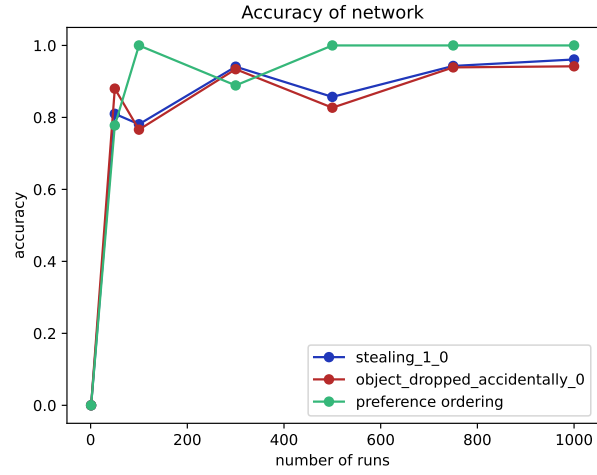


Figure 6: Accuracy of network based on the number of training runs

6 Discussion

The aim of this discussion section is to critically examine both Bayesian Networks and this method for evaluating them. We discuss the results, then, we take two steps that increasingly loosen the assumption of abundant data that we can use to ground our Bayesian Network, to discuss the level of realism and generalisability of using the method of evaluating all evidence states as a way of evaluating Bayesian Networks. Finally, we discuss the use of simulations for investigating Bayesian Networks and for modelling criminal cases.

- First, we consider the limitations that we find when applying the method to our case study, as outlined in the previous two sections.
- Second, we move one step away from this idealised situation, and attempt to construct a Bayesian Network for the situation in the case study manually, hence, not using the automatic BN constructor algorithm, but instead relying on causal knowledge and subjective probability estimates by the modeller. The purpose of this is to evaluate if 1) a modeller can construct a network of similar accuracy to the automatically constructed networks.
- Third, we discuss the use of this method of evaluation for investigating existing Bayesian Networks. We investigate whether we can evaluate modelling primitives or idioms for Bayesian Networks, such as those in (de Zoete et al., 2019). Additionally, we investigate whether this method of evaluation would be suitable for a Bayesian Network of a criminal case, as modelled in (van Leeuwen, 2019). This leads to a discussion of the problem of combinatorial explosion in the number of evidence nodes.
- Fourth, we discuss the implications of the findings in the discussion.
- Finally, we discuss the use of simulations as a modelling primitive with a focus on operationalisation of nodes.

6.1 Evaluating BNs over all possible evidence states using simulations

There is a high variability between runs: if we were to run this experiment twice, we would find a different network structure for all networks, as well as different probabilities predicted. However, the average trend in increasing accuracy with a higher number of states remains.

With this method, we can show that we can create BNs that predict output probabilities that correspond to the limiting frequencies of events in the simulation. We see that both the preference ordering as well as the probabilities in the output nodes in Table ?? are near identical to those in Table 2. This means that the best BN reflects the frequencies in the simulation well, not just on one set of cumulative evidence, but on nearly all sets of cumulative evidence.

The only evidence set where the BN does not reflect the ground truth, is for the evidence set of (0, 1, 1, 0). This is a situation where the agent is seen stealing, but the object is not gone. In the test data of 10,000 entries, there is never an entry where both stealing and dropping are true. Hence, we find that the BN does not predict the output correctly in this case.

When less data is available to the K2 algorithm, such as the case where the simulation was run for 10 times (Table ??), we find that the accuracy of the network decreases. This means that the network is less able to predict the right outcome across all possible evidence states.

This method also allows us to see when the BN is assigning probability values to mutually exclusive nodes that violate probabilistic constraints. The joint probability over all three scenarios can never be greater than 1, which means that none of the probability values of ‘stealing_1_0’, ‘object_dropped_accidentally_0’, and neither, can be smaller than 0. However, in both Table ??, and Table ??, we find that $P(\text{‘neither’})$ can sometimes be smaller than 0. This is also visible in the cumulative probability plots (see Figure ?? where for E_camera_seen_stealing_1_0, the joint probability of outcomes > 1). This shows that the mutually exclusive relation between stealing and dropping is not learned correctly in the network. This improves (but is not gone), when the K2 algorithm has access to more data.

This method of evaluating a BN over all states of cumulative evidence can distinguish between better and worse BNs, shows when a BN goes wrong and gives us insight in why that happens. Modellers of data-poor BNs are might think about creating an expected preference ordering on all possible evidence states, before starting to build and test the BN, in order to check whether their BN aligns with their common-sense predictions. If the BN is wrong, this is a sign that either the modeller’s estimation is wrong, or that the probabilities as entered in the BN are not correctly representing your actual beliefs.

Creating the simulation and finding the proper limiting frequency is also difficult. We ran the simulation 10,000 times, however, the simulation did not allow a state that should have been possible, which is the state where the thief was seen by cameras,

the psychological report states that he is guilty, but he was not seen stealing, and the object was not gone. In real life, this state is possible. However, the combination of (psychological report = 1, camera = 1), has 118 entries (happens 118 times). Out of all those entries, in the simulation it is always the case that the object is gone. However, in theory, it should be possible that the agent has a psychological report that indicates he will steal, that he's seen on camera, yet does not steal. This is a limitation in the number of runs performed.

6.2 Can a modeller do this?

We have shown that we can generate Bayesian Networks and evaluate them over all possible evidences states automatically, if we use the data as generated in training runs by the simulation. However, the real problem is, if a modeller could actually attempt to create a BN by hand without access to the underlying frequencies from the simulation. If we have a manually-crafted BN, but we also have the underlying true joint probability distribution over all variables in the simulation, we can test if this method of evaluation can show problems with a manually constructed Bayesian Network.

In this section, we manually create a Bayesian Network for the scenarios as given in the case study: a (potential) robbery at the Grote Markt. This was done by imagining how a modeller would manually create a BN if they only had access to the simulation. Instead of looking at the source code of the simulation, the modeller would have access to the visual of the simulation, and would be able to run the simulation multiple times. The reporters that are used, are given, and are the same nodes (reporters) that are outlined in the case study. However, the modeller should construct the structure of the BN, and fill the CPTs of the nodes, using their subjective estimation of causality and frequency of events in simulation. This was done to discuss the influence that the real lack of data, time and control would have on a modeller in a real criminal case.

6.2.1 Constructing the Manual Network

We followed the construction methods as outlined in (?) and (van Leeuwen, 2019). We considered the three different scenarios: 1) the object was stolen, 2) the object was dropped, 3) neither happened. Since we use the same nodes as in the simulation, we do not have a separate node for scenario 3, or a constraint node. Scenario 3 is represented by both other scenarios having low probabilities.

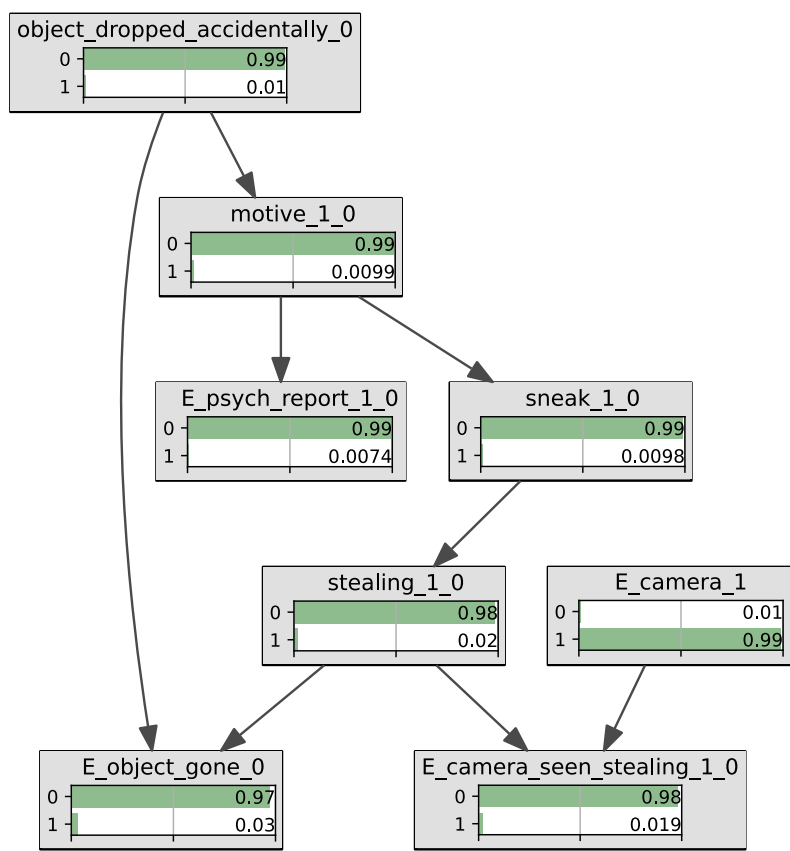
1. Structure within scenarios: The hypothesis nodes of the two scenarios represented explicitly in the networks are: 1: [motive_1_0, sneak_1_0, stealing_1_0], and 2: [object_dropped_accidentally_0]. Within every scenario, we are creating temporal arcs between the hypothesis nodes. For scenario 2, this is easy, since it consists of only 1 node and we do not need to add arcs. For scenario 1, we observe in the simulation that a motive comes before sneaking, which comes before stealing. Hence we identify [motive \rightarrow sneak \rightarrow stealing] as the structure of scenario 1.
2. Structure between scenarios. We need to know which scenario is the parent of the other scenario. Using the causality as described in Section 4.4, we place ‘object_dropped_accidentally_0’ before the first node of scenario 1. This results in the BN

$$object_dropped_accidentally_0 \rightarrow motive_1_0 \rightarrow sneak_1_0 \rightarrow stealing_1_0$$

3. Evidence nodes. For each node, we consider causality. ‘E_psych_report_1_0’ relates to ‘motive_1_0’ only, ‘E_object_gone_0’ to both ‘stealing_1_0’ and ‘object_dropped_accidentally_0’, then ‘E_camera_seen_stealing_1_0’ only directed to ‘stealing_1_0’, with as parent ‘E_camera_1’.
4. For each node, create subjectively estimated conditional probability tables. To simulate the idea that we do not have exact probabilities (from the simulation), we place restrictions on the probabilities that we can add to the CPTs. We can only use [1, 0, 0.99, 0.01, 0.5, 0.25, 0.75] in the CPT. These correspond to: **red**Totally sure, direct causal relation (1, 0), pretty sure but there might be some reason why not (0.99, 0.01), and we are not sure but it’s leaning in a certain direction (0.25, 0.75). The network is presented in Figure 7. The CPTs for the nodes are presented in the Appendix ???.

6.2.2 Evaluating the Manual Network

1. **Run** We run the simulation 10,000 times to collect the ground truth.
2. **BN** We test the manual network (Figure 7).
3. **Selection** The evidence nodes of the network are the 4 (binary) nodes marked with an ‘E’, which are [E_camera_1, E_camera_seen_stealing_1_0, E_object_gone_0, E_psych_report_1_0]. The output nodes are [‘object_dropped_accidentally_0’, ‘stealing_1_0’].



Inference in 1.19ms

Figure 7: Manual network

4. **Order** We order the evidence nodes in the same order in which we test the automated networks [E_psych_report_1_0, E_camera_1, E_camera_seen_stealing_1_0, E_object_gone_0].
5. **Collect** There are $2^4 = 16$ evidence states in total.
6. **Subset** See Table 1
7. **Frequencies** See Table 2.
8. **Posteriors** For every evidence state, we use the BN in Figure 7 as model. In the BN, we turn the evidence nodes to the value specified by their evidence state. We used the LazyPropagation inference engine in PyAgrum to calculate the posteriors of the outcomes in the BN, given the evidence state as input. The posteriors are collected in Table 10.
9. **Accuracy Evidence State** The posteriors of the outcome nodes in the network are compared to frequency of those outcomes in the ground truth. The accuracy of the BN per evidence state is presented in Table 11.
10. **Accuracy Total** We find that, in total, the accuracy for this manual network is 0.71 for the ‘stealing_1_0’ node, and 0.81 for the ‘object_dropped_accidentally_0’ node, with an average accuracy of 0.76.

These accuracy scores mean that the manual network performs slightly worse than the average of the automatically constructed networks (0.88). We see that there are only two cases where the manual network predicts the wrong output: the evidence set (0, 0, 0, 1), and the evidence set (1, 1, 0, 1). We treat these in turn.

- (0, 0, 0, 1): if the object is gone, but there is no other evidence, the manual network predicts that the object is stolen (0.55) rather than dropped (0.45), so about equally likely. The prior probability of the ‘object_dropped_accidentally_0’ node is 0.01, which corresponds to a subjective estimate of ‘not likely, but can happen’. Apparently, we have underestimated the amount of times that an object was dropped, rather than stolen (given that all other evidence is 0): in the simulation, if there is no further evidence, it is much more probable that the object was dropped than stolen.
- (1, 1, 0, 1): if the psychological report is true, the potential thief was seen on camera, but was not seen stealing, and the object is gone, the network should predict that the agent has stolen. However, instead, the manual network breaks (hence, the probability assignments of -1). This combination of evidence is

evidence	H1	H2	H3
(0, 0, 0, 1)	P(steal) (0.55)	P(dropped) (0.45)	P(neither) (0.00)
(0, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 0, 1)	P(dropped) (1.00)	P(steal) (0.00)	P(neither) (0.00)
(1, 0, 0, 1)	P(steal) (1.00)	P(dropped) (0.00)	P(neither) (0.00)
(0, 1, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(1, 1, 0, 1)	P(neither) (3.00)	P(steal) (-1.00)	P(dropped) (-1.00)
(1, 1, 1, 1)	P(steal) (1.00)	P(dropped) (0.00)	P(neither) (0.00)
(1, 0, 0, 0)	P(neither) (1.00)	P(steal) (0.00)	P(dropped) (0.00)
(0, 1, 1, 1)	P(steal) (1.00)	P(dropped) (0.01)	P(neither) (-0.01)

Table 10: Preference ordering with numbers for manual network

impossible in the network, but it should be allowed, as it is a possible state in the simulation.

evidence	steal	dropped
(0, 0, 0, 1)	0.46	0.46
(0, 0, 0, 0)	1.00	1.00
(0, 1, 0, 1)	0.99	0.99
(1, 0, 0, 1)	0.93	0.93
(0, 1, 0, 0)	1.00	1.00
(1, 1, 0, 1)	-0.93	-0.07
(1, 1, 1, 1)	0.95	0.95
(1, 0, 0, 0)	1.00	1.00
(0, 1, 1, 1)	1.00	0.99
total	0.711	0.806

Table 11: Accuracy per evidence state per output node

6.2.3 Discussing the Manual Network

We find that the manual network performs well, with a 0.76 accuracy, which is only slightly worse than the automated networks. It is not the case that the accuracy per evidence state is low, instead, the performance is very accurate over most evidence states, with only two evidence states that cause the lower accuracy. This means that it would be possible to improve the network by focussing on what goes wrong in these two states and adapting it, instead of trying to increase the performance of the network over all possible evidence states. Therefore, it seems possible that we can

manually construct accurate BNs for crime cases, even with subjective probabilities. We can also use the method postulated in Section 3 as a way of evaluating the network to find where we might have over- or under-estimated probabilities in the CPTs, using the grounded frequencies generated from the simulation. Hence, a modeller might be able to construct a BN based on simple scenarios by hand. However, there are some limitations, both in how this network was created, as well as the evaluation method.

To address the main limitation first, ideally, this manual crafting of the BN should be done by someone who was not involved in creating the simulation. Involvement with the crafting of the simulation gives the modeller an unfair advantage compared to an ‘new’ modeller in estimating probabilities and understanding the causal structures, as they know how the simulation works. Additionally, in real life, we do not have access to the source code of the universe either, but we still have to build a network. Hence, the manual network should not be constructed by the modeller who created the simulation. However, due to time constraints, only the modeller of the simulation was available to build the manual BN. This might have improved the accuracy of the manual network.

Additionally, there are three limitations regarding the evaluation method. First of all, we can only use the method to find an evidence state with a low accuracy, but we do not have a way of resolving the low accuracy. The method does not tell you which CPTs need to be changed in what way. Secondly, we can only use the accuracy measure when we have a grounding data, in this case from the simulation. In real life, modellers of criminal cases do not have this grounding data. Finally, we find a problem in the selection of the possible states. In the simulation, some evidence states are not allowed, they have a frequency of 0. For most of these states, the manual network results in an error if these states are entered, as it should. This is where BNs guide the reasoning about evidence of the modeller. However, the manual network allows one state of evidence that is not allowed in the simulation, which is the state of $(1, 1, 0, 0)$. This is the state where the ‘thief’ has a psychological report stating that they could steal, they were seen on camera, but they were not seen stealing, and, most crucially, the object is not gone. This is a case where human intuition and what should happen, clashes with the frequencies of what actually happens in the simulation.

6.3 Evaluating BNs over all possible evidence states in real life

In this section we evaluate two Bayesian Networks with the method outlined before.

6.3.1 de Zoete 2019

The first is a network by de Zoete et al, about child abuse. This is from a paper about probabilistic paradoxes in legal reasoning (de Zoete et al., 2019). The paper considers a case where we want to know if a child is abused. We have a certain behaviour that is associated with abuse, but some study shows that this behaviour occurs about as frequently in children who are not abused. Only when the behaviour *EB* occurs together with an additional characteristic *AC*, there's a strong probability of abuse. It has been proposed that the combination of two evidence pieces is difficult to model - however, de Zoete et al find a way to model it, using the Bayesian Network presented in Figure 8. In this network, they divide the potential children into three groups: 1) a child who is abused, who must exhibit both the behaviour and the additional characteristic, 2) a child who is not abused, who has the behaviour but can never have the additional characteristic, and 3) a child who is not abused, who does not have the behaviour, and also does not have the additional characteristic.

In the paper, a table is presented with the possible outcomes of the network to show that network models the apparent paradox correctly. Turning either one of the nodes *EB* or *AC* on (and leaving the other unspecified) does not affect the probability of the child being abused. This was 0.4, and remains 0.4. However, if we set both *EB* and *AC* to 'true', results in a posterior probability of abuse of 1, as expected.

Now, we apply the method of evaluating the network over all possible evidence states. We did not create a simulation for this, hence we cannot apply the full method.

1. **Run** We cannot run a simulation.
2. **BN** We test the manual network (Figure 8).
3. **Selection** The evidence nodes of the network are the 2 binary nodes *EB* and *AC*. The output node is the ternary node *Group*.
4. **Order** We order the nodes based on the order implied in the text: we care about the exhibited behaviour (*EB*) first, then look at the additional characteristic *AC*.

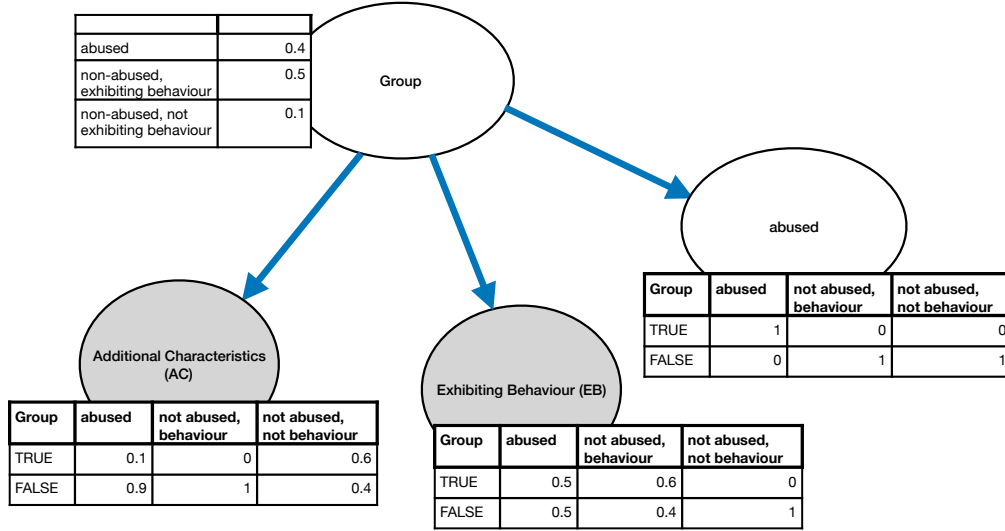


Figure 8: Abuse Network, replicated from (de Zoete et al., 2019)

5. **Collect** There are $2^2 = 4$ evidence states in total.
6. **Subset** All evidence states are possible.
7. **Frequencies** We cannot calculate frequencies.
8. **Posteriors** For every evidence state, we use the BN in Figure 8. In the BN, we turn the evidence nodes to the value specified by their evidence state. We used the LazyPropagation inference engine in PyAgrum to calculate the posteriors of the outcomes in the BN, given the evidence state as input. The posteriors are collected in Table 12.
9. **Accuracy Evidence State, Total** We cannot calculate an accuracy.

Even though we have not simulated this scenario and hence have no baseline, we can still evaluate the posterior of the network based on our subjective expectations of how evidence should influence our reasoning. We see that the network performs as expected in 3 out of 4 cases. If we do not set any evidence, we just have the prior probability. Setting either one of the pieces of evidence to ‘false’ reduces our belief in the posterior that the child has been abused (from 0.40 to 0.375 and from 0.40 to

Evidence	P(abused)	p(nonAbusedBehaviour)	p(nonAbusednotBehaviour)
no evidence set	0.40	0.50	0.10
EB and AC	1.00	0	0
EB and $\neg AC$	0.375	0.625	0
$\neg EB$ and AC	0.25	0	0.75
$\neg EB$ and $\neg AC$	0.4286	0.4762	0.0952

Table 12: Posterior belief in either of the three hypotheses given evidence states

0.25). This lines up with common sense: the evidence is negative, hence we reduce our belief in the posterior.

However, there we identify one strange case, presented in Figure 9, which is the case of both pieces of evidence being negative. So the child does not perform the behaviour and also does not have the additional characteristic. We would expect the probability that the child is abused to drop from 0.4 to something lower (perhaps not 0, but something lower). However, instead we find that the posterior of ‘abused’ increases to 0.42. This does not seem like a conclusion that we want to draw. Unfortunately, it is unclear what is wrong with this network so we do not know why it produces a higher posterior belief in abuse if there is a total absence of evidence. We do not know how the CPTs should be changed in order to produce a network that conforms to our intuitions about the evidence. Hence, our method can only tell us that our network results in an unexpected outcome on some evidence state, yet does not tell us how to resolve this.

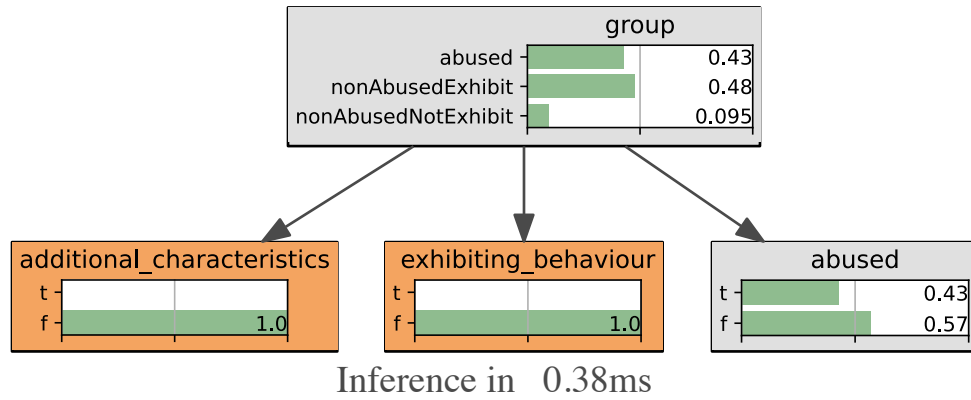


Figure 9: Posterior probability for abuse is higher than prior given that evidence is false

6.3.2 van Leeuwen 2019

We applied the method for evaluating evidence on all evidence states to the network presented in [van Leeuwen \(2019\)](#), shown in Figure 10. This network models a crime case where a suspect P murdered a tenant, then fled by car, and later called his parents to confess the crime, which is modelled as scenario 1 (scn1). In his own testimony, P states that he has amnesia and does not remember the day of the murder, and also that he was kidnapped, which is modelled as scenario 2 (scn2). The two scenarios are mutually exclusive and exhaustive.

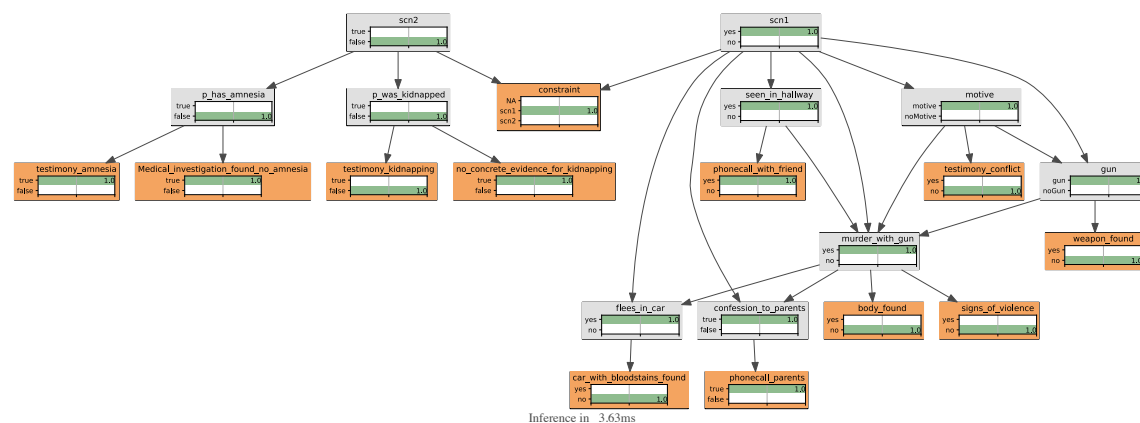


Figure 10: Example of subjective probability estimation resulting in a guilty verdict for insufficient evidence

We did not create a simulation for modelling this scenario. It is not plausible for a network of this size to manually create the baseline by stating the expected posterior per outcome for every evidence state. Hence we have an ungrounded Bayesian Network. We cannot create a manual distribution over posteriors for a network of this size. The evaluation is as follows.

1. **Run** We cannot run a simulation.
2. **BN** We test a manually constructed network of the two alternative scenarios (Figure 10).
3. **Selection** The evidence nodes of the network are the 11 binary nodes: ‘testimony_amnesia’ (TA), ‘Medical_investigation_found_no_amnesia’ (MA), ‘testimony_kidnapping’ (TK), ‘no_concrete_evidence_for_kidnapping’ (NK), ‘phonecall_parents’ (PP), ‘car_with_bloodstains_found’ (CB), ‘body_found’ (BF), ‘signs_of_violence’ (SV), ‘phonecall_with_friend’(PF), ‘testimony_conflict’ (TC), ‘weapon_found’

(WF). The output nodes are the nodes *scn1*, representing that suspect P is guilty, and *scn2*, representing that P is not guilty.

4. **Order** We order the nodes as we read them from left-to-right in the network, which is the order as presented in the **Selection** step.
5. **Collect** There are $2^{11} = 2048$ evidence states in total.
6. **Subset** Some evidence states are not possible. However, we do not know which evidence states are not possible. Since we neither have a simulation to generate only possible states, nor enough time to consider all possible combinations of evidence states manually, it is not possible to know which evidence states are impossible.
7. **Frequencies** We cannot calculate frequencies.
8. **Posteriors** For every evidence state, we use the BN in Figure 10. In the BN, we turn the evidence nodes to the value specified by their evidence state. We used the LazyPropagation inference engine in PyAgrum to calculate the posteriors of the outcomes in the BN, given the evidence state as input. Instead, A selection of interesting cases is presented in Table 13. Posteriors over all evidence states can be found in Table 14.
9. **Accuracy Evidence State, Total** We cannot calculate an accuracy.

We find that we do not have to handle all 2048 evidence states. The network constrained some combinations of evidence states, in 56.25% of evidence states, the combination of evidence was not allowed by virtue of the BN. In the remaining 896 evidence states, the evidence state was applied to the network and the posterior probability for scenario 1 and scenario 2 were calculated. In general, scenario 1 and scenario 2 are about equally preferred under the states of evidence, in 428 states, scenario 1 has a higher posterior probability. In 468 states, scenario 2 has a higher posterior. In 768 states of evidence, it is the case that either scenario 1 or scenario 2 is equal to 1, which means that we are fully convinced that that scenario is correct, which means that in half the cases, we fully believe scenario 1, and in the other half, we fully believe scenario 2.

1. In case 1, we find that, if all evidence nodes are true, which is the situation as found in the court case, the network shows that scenario 1 is the case, and that the suspect is guilty, with a probability of 1. This is the expected output, and corresponds to the outcome of [van Leeuwen \(2019\)](#).

C	evidence	H1	H2
1	TA, MA, TK, NK, CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
2	TA, ¬MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
3	TA, MA, TK, NK, CB, PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
4	TA, MA, TK, NK, CB, PP, BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.40)	scn2 (0.60)
5	TA, ¬MA, TK, ¬NK, ¬CB, PP, BF, ¬SV, PF, TC, WF	scn1 (0.07)	scn2 (0.93)
6	¬TA, ¬MA, ¬TK, ¬NK, ¬CB, ¬PP, ¬BF, ¬SV, ¬PF, ¬TC, ¬WF	None	None

Table 13: Interesting rows extracted from complete table

2. In case 2, we find that there is no body, no signs of violence, no car with bloodstains, no evidence of existing conflict. The only evidence that the prosecution has, are two phone calls. The outcome of the network is that the suspect is guilty ($P(\text{scn1} = \text{'yes'}) = 100\%$). But the evidence that is entered into this network, would not reasonably support this conclusion. No reasonable arguer would argue that this state of evidence is sufficient for a guilty verdict.
3. In case 3, we fully believe scenario 2, so that the suspect is not guilty. However, all evidence that we have learned about scenario 2 shows that scenario 2 is not true: we have testimony for amnesia, but no medical record of it. We have testimony for kidnapping, but no concrete evidence for kidnapping. This should mean that our posterior belief in scenario 2 should decrease. We also have a little evidence on the side of scenario 1: two phone calls, and a car with bloodstains. This would not be enough for a conviction, but it should be enough that our belief in scenario 1 is not 0.
4. In case 4, we believe the same case as evidence state in case 3, but now we change our evidence. From not having a body found, we add that we find the body, and we see that our belief in scenario 1 increases, from 0 to 0.40. This is a change of our belief in a reasonable direction given new evidence. The size of the belief-change, from 0 to 0.40, is difficult to assess without a realistic baseline.
5. In case 5, we find that the suspect says that he has amnesia and also that he was kidnapped, and this is supported by the other evidence. This adds support for scenario 2. However, we also find a lot of support for scenario 1: a body, a testimony of conflict, the phone calls, weapon found. Just not the car, and no signs of violence on the scene. Here, my subjective probability estimation machine thinks that, even though scenario 2 has some good evidence going for

it, I believe that scenario 1 is more likely than 0.07. Hence, the output does not line up with my expectation.

6. In case 6, we present a special case: if all evidence nodes are false, the inference engine shows the result that the evidence is altogether incompatible. Since both scenarios are mutually exclusive and exhaustive, this result is sensible and shows that the BN can indeed structure our reasoning.

Even without using a simulation, this method can be used to gain insight in whether the BN conforms to our expectations. We can identify cases where it seems to work correctly, such as case 1) and case 3). In case 1), the output conforms to the one datapoint that we have (given all evidence, the suspect is guilty), the BN makes the same decision as the court. In case 4), we find that the network, in this circumstance, responds sensibly to a change in evidence. However, in case 2), 3) and 5), we find the performance of the network not convincing. In case 2), there is insufficient evidence for scenario 1, yet the network chooses scenario 1. In case 3), there is insufficient evidence for scenario 2, yet the network chooses scenario 2. In case 5), there is support for both scenarios, but the posterior probability for scenario 1 seems (subjectively) too low. Furthermore, we now also know which states are deemed impossible (example: case 6). However, since we do not have a simulation or real-life test-cases, we do not have a way of ‘objectively’ checking whether the network performs correctly or not, and to objectively identify combinations of evidence for which the network is performing badly. We can only do spot-checks and manually search through the output to see if we found anything interesting. Also, if we found a case for which the network performs incorrectly, it is also not clear what we should do with that: how should we change the probabilities in the CPT in order to increase ‘accuracy’?

It is possible to apply this method of evaluation to other networks based on criminal cases (given that they are produced in an open-access format), to non-systematically check the performance of these networks over all possible evidence valuations. In the networks as considered in the Anjum case study in [Vlek \(2016\)](#), or the Simonshaven case in [Fenton et al. \(2019\)](#), the evidence nodes are distinguished from the hypothesis nodes. Even without considering the temporality of evidence, we can set the cumulative evidence all at once. However, since we do not have simulations for grounding, or data for grounding, we cannot actually evaluate the networks based on ‘objective’ measures. Manually considering all evidence sets will be even more problematic than before. Instead of 11 nodes, the Simonshaven network has 13 evidence nodes, and the Anjum network has 20 evidence nodes. If we assume that calculating 1 case will take around 0.0037 seconds (as calculated from 7.66 seconds for 2048 entries, this

does not hold entirely because it also depends on the number of hypothesis nodes), producing all possible Simonshaven states and posteriors should take $2^{13} = 30$ seconds, which is still reasonable. The Anjum network would take 64 minutes. That is only considering the automatic calculation of the posteriors, and does not consider the time-complexity of creating a manual or automatic baseline. Additionally, some of the nodes in the Simonshaven are not binary nodes ('number of people in woods' has three possible states), resulting in a higher complexity as well.

6.4 Implications

The discussion about the networks presented in this section suggest that there is a limited use for both ungrounded Bayesian Networks as well as for the evaluation method as outlined in the Method section.

In case of (de Zoete et al., 2019), Figure 8, we are essentially investigating a method for creating a BN. This network is an implementation of a Bayesian Network idiom that is supposed to model the situation where either piece of evidence by itself is not enough to increase the posterior, yet both pieces of evidence together are convincing. This is an example of a BN idiom, like the other BN idioms that are presented in that same paper, as well as in Fenton et al. (2019). Idioms generally have few nodes and the evidence states that are possible are clear, so we do not need a simulation to consider the possible states. In this case, we can use the method of evaluation, even without a grounding simulation, to discover the evidence states for which these idioms might behave unexpectedly.

However, this method of evaluating Bayesian Networks on all possible evidence states is not plausible for BNs that move away from abstracted, small idioms and attempt to model actual or fictional criminal cases. In the worst case, if we have e evidence states, this means that we have 2^e possible evidence states. We would have to define a preference ordering or probability distribution on the output nodes in 2^e cases. This is plausible in a network with 4 evidence nodes, like the idiom-networks. However, networks that model criminal cases have more than 4 evidence nodes. This necessarily puts an upper bound on the level of granularity one can model in their network. If a network becomes more detailed in how evidence is represented, the higher the chance that considering all possible evidence states becomes impossible. A rough estimation shows that a 20-evidence-node network will take about an hour, but 20 pieces of evidence are not much in a complex case. Due to exponentiality, a network with 25 evidence nodes would result in 2.3 months of calculations.

If we take a different approach and attempt to create the BN from elicited, statistical

information as found in the real world, we run into a different problem. Even though we might be able to find statistics about criminal behaviour, it is unclear to what extent those statistics would generalise towards probabilities in the network. For example, we might be able to estimate the proportion of Dutch people who own a gun. However, this information by itself hardly seems relevant when we look at the facts of the case as described in the case ⁷: the suspect was ex-military and might have killed someone with the same weapon before. Using a general statistic about gun-ownership in the Netherlands does not fit the case, hence, low generalisation: the statistics that we might use to ‘ground’ the network might be irrelevant. Furthermore, we might not always be able to define which statistic is the most relevant. This is the fundamental ‘problem of the reference class’ (Colyvan et al., 2001).

Both these problems mean that we cannot know for which evidence states the network is accurate. Even if the manual, subjectively estimated networks have an accuracy of 0.76, as we have shown for the network in Figure 11, we cannot be sure that this relatively high accuracy holds for a network that is as complex as the network in Figure 10, or the networks in Vlek (2016) or Fenton et al. (2019). We need to define many more cases of evidence than we are actually reasoning with. In the court cases, we are only considering evidence that we believe is true: we do not have to reason about what we would conclude if we had found the evidence in a different state. In BNs, we are implicitly defining the joint probability distribution over all possible evidence states: in the (van Leeuwen, 2019) network, all 2048 evidence states are defined implicitly, and for all these evidence states, the network must be correct. This is a very high bar to clear.

6.5 Using Simulations

This is no problem in the simulation, we know what the methods for determining the probabilities in the nodes are valid (which means that they always correctly reflect the underlying process that is generating them), because it’s literally programmed in this way - directly reflecting the states, we literally just count the frequencies. However, in real life, we might not even know the validity of different possible mappings for the same node. In short, how do we determine in real life that ‘sneak_1_0’? How can we determine if anyone is actually ‘sneaking’, and how will we know if this method of determination is valid? This is also why BNs for forensic-statistical processes are more legitimate: in these forensic-statistic fields, we have defined clear methods and we know the method through which we are mapping: these variables

⁷Case number: ECLI:NL:RBUTR:2004:AO3150

are operationalised. This is not the case for more ‘vague’ nodes like ‘motive’.

Due to the simulation approach in this paper, we can establish a statistical ground truth in step 4) of our method. We can create both a joint probability distribution and a preference ordering automatically from the simulation. In real life, this would have to be elicited in some way. Even if we assume that we are not in a combinatorial explosion, we would still need to define either a subjective probability distribution over all possible outcomes, or a preference ordering, and use this as a baseline to test the predictions of our BN against. This involves subjectivity twice: first in defining the preference ordering or probability distribution over outcomes, and second the probabilities that are inputted in the CPTs. Future research might establish how successful people are in estimating preference orderings or probability distributions over output nodes, so that we can use these subjective orderings as a baseline, instead of an ordering generated by frequency data from the simulation.

As we saw when we applied the method to the network without a simulation, it is not plausible to create a manual baseline, as this would be mind-numbingly boring and consume too much time. Creating a simulation would mean that the simulation should go beyond one room, and instead model an entire city, all places that the suspect can be all the time. This requires a lot more data and attention than is possible now, and it is also unclear how we would test the validity of the simulation, which would result in all our problems just being shifted up a step (to the simulation level, instead of in the BN). This means that simulations might be a good tool to investigate the methods of BNs, but are not suitable for actually investigating real-life crimes (although they might be usable as a tool for predicting situations - stuff where we have frequency data about).

Yes, simulations are a nicer modelling primitive than straight BNs. Could use a true simulation to generate data and cases and train a BN on that, and use decision making based on BN data. A simulation like programmed now is nice as a data-generator, but not so much as a reasoning thing. However, it is unclear unknown difficult to know in what detail one should model for a real case, instead of just a test-case.

Simulations are nice because you do not have to deal with calculating the probabilities yourself. For instance, calculating the probability of motive, means that we need to calculate vulnerable and valuable. This can be done, given that the guy has a target: $\text{valuable} = (2/5) * (1/2) * (1/2) = 0.1$, while $\text{vulnerable} = (1/5) + (3/5)(1/2) = 0.5$. Hence, $\text{motive} = 0.05$, or 5%, just by bare probability calculations, which matches the probability as found in the network and the training dataset. However, this

was relatively easy because these were straightforward uniform distributions. This calculation is going to be more complex if we're dealing with either more complex distributions (normals, etc.), or if we do not have a good idea about the underlying distributions. However, doing this using simulations makes it a lot easier, the numbers 'just' emerge without any calculation. We even encounter this in the simulation right now: the probability that the camera sees the stealing is very difficult to calculate analytically. Simulations are a more natural way to think about this. The simulation can also easily become more relevant (more like a level 1 or 2 simulation in the taxonomy), by creating more realistic agent motivation models and behaviour. On the other hand, debugging simulation results is really annoying.

7 Conclusion

7.1 Summary

We have shown that simulations can be used to ground Bayesian Networks and we created an evaluation method for them. Bayesian Networks can be created from the simulation automatically, and these Bayesian Networks can be evaluated for accuracy over all evidence states systematically. We know that these networks are accurate because 1) the predicted prior probabilities of events in the network correspond exactly to the frequency of events in the simulation and 2) adding all possible states of evidence to the Bayesian Network results in the same output prediction as given by the simulation. Accuracy increases the more data is available to automatically construct the network, hence we find that some networks are better than others, and we can make a real evaluation.

However, this method of evaluation is not suitable for 1) real-life criminal cases and 2) networks with > 25 evidence nodes. In real-life criminal cases, we do not have the grounding necessary to check whether the network is accurate automatically. Creating this checking-dataset by hand means that we have to specify for all possible evidence states what our prediction of the output nodes is, which takes too long and we do not have a good grounding to prefer one set of evidence states over the other. Additionally, in real life we do not have to reason over all sets of possible evidence, we just need to reason with the set of evidence that we found. There need to be fewer than 25 evidence nodes in the network (given personal-computer constraints), as runtime increases exponentially with the number of nodes.

7.2 Future Research

The simulation in this paper is not complex, and does not model reality in any realistic way. The purpose of this simulation was just to generate data, and did not need to reflect any specific facts about the world. However, agent-based modelling can be useful for investigating different aspects of Bayesian Networks, or reasoning with evidence more generally. Increasing the level of the simulation from level 0 to something that reflects reality is useful to investigate problems such as the Opportunity Prior as presented in [Fenton et al. \(2017\)](#).

Letting people estimate probabilities on simulations to investigate elicitation accuracy.

Bibliography

- Bench-Capon, T. (2019). Before and after dung: Argumentation in ai and law. *Argument and Computation*, 11:1–18.
- Chen, X.-W., Anantha, G., and Lin, X. (2008). Improving bayesian network structure learning with mutual information-based node ordering in the k2 algorithm. *IEEE Transactions on Knowledge and Data Engineering*, 20(5):628–640.
- Colyvan, M., Regan, H. M., and Ferson, S. (2001). Is it a crime to belong to a reference class. *Journal of Political Philosophy*, 9(2):168–181.
- Cooper, G. and Herskovits, E. (1992). A bayesian method for the induction of probabilistic networks from data. *Machine Learning*, 9:309–347.
- Dahlman, C. (2020). De-biasing legal fact-finders with bayesian thinking. *Topics in Cognitive Science*, 12(4):1115–1131.
- Dawid, A. P. (2008). Beware of the dag! In *JMLR: Workshop and Conference Proceedings 6*: 59–86.
- de Koeijer, J. A., Sjerps, M. J., Vergeer, P., and Berger, C. E. (2020). Combining evidence in complex cases-a practical approach to interdisciplinary casework. *Science & Justice*, 60(1):20–29.
- de Zoete, J., Fenton, N., Noguchi, T., and Lagnado, D. (2019). Resolving the so-called “probabilistic paradoxes in legal reasoning” with bayesian networks. *Science & Justice*, 59(4):367–379.

- Di Bello, M. and Verheij, B. (2018). Evidential reasoning. In Bongiovanni, G., Postema, G., Rotolo, A., Sartor, G., Valentini, C., and Walton, D. N., editors, *Handbook of Legal Reasoning and Argumentation*, pages 447–493. Springer, Dordrecht.
- Ducamp, G., Gonzales, C., and Willemin, P.-H. (2020). aGrUM/pyAgrum : a Toolbox to Build Models and Algorithms for Probabilistic Graphical Models in Python. In *10th International Conference on Probabilistic Graphical Models*, volume 138 of *Proceedings of Machine Learning Research*, pages 609–612, Skørping, Denmark.
- Dung, P. M. (1995). On the acceptability of arguments and its fundamental role in nonmonotonic reasoning, logic programming and n-person games. *Artificial Intelligence*, 77:321–357.
- Fenton, N., Lagnado, D., Dahlman, C., and Neil, M. (2017). The opportunity prior: A simple and practical solution to the prior probability problem for legal cases. In *ICAIL '17*. ICAIL.
- Fenton, N., Neil, M., and Lagnado, D. A. (2012). A general structure for legal arguments about evidence using bayesian networks. *Cognitive Science*, 37(1):61–102.
- Fenton, N., Neil, M., Yet, B., and Lagnado, D. (2019). Analyzing the simonshaven case using bayesian networks. *Topics in Cognitive Science*, 12(4):1092–1114.
- Fenton, N. E. and Neil, M. D. (2013). *Risk Assessment and Decision Analysis With Bayesian Networks*. CRC Press, Boca Raton.
- Gerritsen, C. (2015). Agent-based modelling as a research tool for criminological research. *Crime Science*, 4(1).
- Gilbert, N. and Terna, P. (2000). How to build and use agent-based models in social science. *Mind & Society*, 1(1):57–72.
- Gilbert, N. and Troitzsch, K. (2005). *Simulation for the social scientist*. McGraw-Hill Education (UK).
- Hamilton, C. S. and Pollino, C. (2012). Good practice in bayesian network modelling. *Environmental Modelling and Software*, 37:134–145.
- Haojie Zhu, F. W. (2021). An agent-based model for simulating urban crime with improved daily routines. *Computers, Environment and Urban Systems*.

- Kadane, J. B. and Schum, D. A. (1996). *A Probabilistic Analysis of the Sacco and Vanzetti Evidence*. Wiley, Chichester.
- Kazil, J., Masad, D., and Crooks, A. (2020). Utilizing python for agent-based modeling: The mesa framework. In Thomson, R., Bisgin, H., Dancy, C., Hyder, A., and Hussain, M., editors, *Social, Cultural, and Behavioral Modeling*, pages 308–317, Cham. Springer International Publishing.
- Meester, R. and Slooten, K. (2021). *Probability and Forensic Evidence*. Cambridge University Press.
- Pearl, J. (1988). *Probabilistic Reasoning in Intelligent Systems: Networks of Plausible Inference*. Morgan Kaufmann Publishers Inc., San Francisco, CA, USA.
- Pennington, N. and Hastie, R. (1993). Reasoning in explanation-based decision making. *Cognition*, 49(1–2):123–163.
- Prakken, H., Wyner, A., Bench-Capon, T. J. M., and Atkinson, K. (2013). A formalization of argumentation schemes for legal case-based reasoning in ASPIC+. *Journal of Logic and Computation*, 25(5):1141–1166.
- Russell, S. and Norvig, P. (2010). *Artificial Intelligence: A Modern Approach. Third Edition*. Pearson, Boston (Massachusetts).
- Schum, D. A. and Martin, A. W. (1982). Formal and empirical research on cascaded inference in jurisprudence. *Law & Soc’y Rev.*, 17:105.
- Timmer, S. (2016). *Designing and Understanding Forensic Bayesian Networks using Argumentation*. PhD thesis, University of Utrecht.
- Van Der Gaag, L. C., Renooij, S., and Coupé, V. M. (2007). Sensitivity analysis of probabilistic networks. In *Advances in probabilistic graphical models*, pages 103–124. Springer.
- van Leeuwen, L. (2019). A comparison of two hybrid methods for analysing evidential reasoning. In *JURIX*.
- Verheij, B., Bex, F., Timmer, S. T., Vlek, C. S., Meyer, J.-J. C., Renooij, S., and Prakken, H. (2015). Arguments, scenarios and probabilities: connections between three normative frameworks for evidential reasoning. *Law, Probability and Risk*, 15(1):35–70.

- Vlek, C. (2016). *When stories and numbers meet in court*. PhD thesis, University of Groningen.
- Wagenaar, W. A., Van Koppen, P. J., and Crombag, H. F. (1993). *Anchored narratives: The psychology of criminal evidence*. St Martin’s Press.
- Wieten, R., Bex, F., Renooij, S., and Prakken, H. (2019). Constructing bayesian network graphs from labeled arguments.
- Wigmore, J. H. (1931). *The Principles of Judicial Proof or the Process of Proof as Given by Logic, Psychology, and General Experience, and Illustrated in Judicial Trials, 2nd ed.* Little, Brown and Company, Boston (Massachusetts).

8 Appendix

This appendix contains:

The probability distribution and preference ordering over outcomes for all possible evidence for the automated networks on the simulation.

The probability distribution and preference ordering over outcomes for all possible evidence for the Jurix 2019 network.

8.1 Discussion

8.1.1 Network

%%%% SCENARIO 2 %%%%

potential (object_dropped_accidentally_0)

0 1
(0.99 0.01)

%%%% SCENARIO 1 %%%%

potential (motive_1_0 | object_dropped_accidentally_0)

0 1
(0.99 0.01) % object_dropped_accidentally_0=0
(1 0) % object_dropped_accidentally_0=1

potential (sneak_1_0 | motive_1_0)

0 1
(1 0) % motive_1_0=0
(0.01 0.99) % motive_1_0=1

potential (stealing_1_0 | sneak_1_0)

0 1
(0.99 0.01) % sneak_1_0=0
(0.01 0.99) % sneak_1_0=1

%%%% EVIDENCE NODES %%%%

```
potential (E_camera_1)
0          1
( 0.01 0.99 )
```

```
potential (E_psych_report_1_0 | motive_1_0)
0          1
( 1 0 ) % motive_1_0=0
( 0.25 0.75 ) % motive_1_0=1
```

```
potential (E_camera_seen_stealing_1_0 | E_camera_1 stealing_1_0)
0          1
( 1 0 ) % E_camera_1=0 stealing_1_0=0
( 1 0 ) % E_camera_1=0 stealing_1_0=1
( 1 0 ) % E_camera_1=1 stealing_1_0=0
( 0 1 ) % E_camera_1=1 stealing_1_0=1
```

```
potential (E_object_gone_0 | object_dropped_accidentally_0 stealing_1_0)
0          1
( 1 0 ) % object_dropped_accidentally_0=0 stealing_1_0=0
( 0 1 ) % object_dropped_accidentally_0=0 stealing_1_0=1
( 0 1 ) % object_dropped_accidentally_0=1 stealing_1_0=0
( 0 1 ) % object_dropped_accidentally_0=1 stealing_1_0=1
```

8.1.2 Table

This table shows the output of the Jurix network on the states that are possible for it. For 56% of input, the network says that the evidence entered together is not possible, which would represent impossible states. However, this leaves us with too many possible states.

'testimony_amnesia' (TA), 'Medical_investigation_found_no_amnesia' (MA), 'testimony_kidnapping'

(TK), 'no_concrete_evidence_for_kidnapping' (NK), 'car_with_bloodstains_found' (CB),
 'phonecall_parents' (PP), 'body_found' (BF), 'signs_of_violence' (SV), 'phonecall_with_friend'(PF),
 'testimony_conflict' (TC), 'weapon_found' (WF).

case	evidence	scn1	scn2
1	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
2	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
3	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
4	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
5	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
6	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
7	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
8	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
9	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
10	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
11	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
12	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
13	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
14	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
15	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
16	\neg TA, \neg MA, \neg TK, \neg NK, \neg CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
17	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
18	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
19	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
20	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
21	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
22	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
23	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
24	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, \neg BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
25	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
26	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
27	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
28	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
29	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
30	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
31	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
32	\neg TA, \neg MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
33	\neg TA, \neg MA, \neg TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
34	\neg TA, \neg MA, \neg TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)

415	TA, ¬MA, TK, ¬NK, CB, ¬PP, BF, SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
416	TA, ¬MA, TK, ¬NK, CB, ¬PP, BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
417	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
418	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
419	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
420	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
421	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
422	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, ¬TC, WF	scn1 (0.01)	scn2 (0.99)
423	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
424	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, TC, WF	scn1 (0.01)	scn2 (0.99)
425	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
426	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
427	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
428	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
429	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
430	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, PF, ¬TC, WF	scn1 (0.26)	scn2 (0.74)
431	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
432	TA, ¬MA, TK, ¬NK, CB, PP, ¬BF, SV, PF, TC, WF	scn1 (0.35)	scn2 (0.65)
433	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
434	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
435	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
436	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
437	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
438	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, PF, ¬TC, WF	scn1 (0.48)	scn2 (0.52)
439	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
440	TA, ¬MA, TK, ¬NK, CB, PP, BF, ¬SV, PF, TC, WF	scn1 (0.50)	scn2 (0.50)
441	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
442	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
443	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
444	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
445	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, PF, ¬TC, ¬WF	scn1 (0.06)	scn2 (0.94)
446	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, PF, ¬TC, WF	scn1 (0.53)	scn2 (0.47)
447	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, PF, TC, ¬WF	scn1 (0.22)	scn2 (0.78)
448	TA, ¬MA, TK, ¬NK, CB, PP, BF, SV, PF, TC, WF	scn1 (0.53)	scn2 (0.47)
449	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
450	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
451	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
452	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)

453	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
454	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
455	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
456	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, ¬SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
457	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
458	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
459	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
460	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
461	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
462	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
463	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
464	TA, ¬MA, TK, NK, ¬CB, ¬PP, ¬BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
465	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
466	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
467	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
468	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
469	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
470	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
471	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
472	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, ¬SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
473	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
474	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
475	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
476	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
477	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
478	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
479	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
480	TA, ¬MA, TK, NK, ¬CB, ¬PP, BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
481	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
482	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
483	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
484	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
485	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
486	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
487	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
488	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, ¬SV, PF, TC, WF	scn1 (0.01)	scn2 (0.99)
489	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
490	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)

491	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
492	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
493	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
494	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, PF, ¬TC, WF	scn1 (0.18)	scn2 (0.82)
495	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
496	TA, ¬MA, TK, NK, ¬CB, PP, ¬BF, SV, PF, TC, WF	scn1 (0.30)	scn2 (0.70)
497	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
498	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
499	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
500	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
501	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
502	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, PF, ¬TC, WF	scn1 (0.63)	scn2 (0.37)
503	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
504	TA, ¬MA, TK, NK, ¬CB, PP, BF, ¬SV, PF, TC, WF	scn1 (0.72)	scn2 (0.28)
505	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
506	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
507	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
508	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
509	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, PF, ¬TC, ¬WF	scn1 (0.03)	scn2 (0.97)
510	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, PF, ¬TC, WF	scn1 (0.84)	scn2 (0.16)
511	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, PF, TC, ¬WF	scn1 (0.14)	scn2 (0.86)
512	TA, ¬MA, TK, NK, ¬CB, PP, BF, SV, PF, TC, WF	scn1 (0.84)	scn2 (0.16)
513	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
514	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
515	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
516	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
517	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
518	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
519	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
520	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, ¬SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
521	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
522	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
523	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
524	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
525	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
526	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
527	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
528	TA, ¬MA, TK, NK, CB, ¬PP, ¬BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)

529	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
530	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
531	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
532	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
533	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
534	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
535	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
536	TA, \neg MA, TK, NK, CB, \neg PP, BF, \neg SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
537	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
538	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
539	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
540	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
541	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
542	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
543	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
544	TA, \neg MA, TK, NK, CB, \neg PP, BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
545	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
546	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
547	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
548	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
549	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
550	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (0.18)	scn2 (0.82)
551	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
552	TA, \neg MA, TK, NK, CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (0.31)	scn2 (0.69)
553	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
554	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
555	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
556	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
557	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
558	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (0.93)	scn2 (0.07)
559	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (0.02)	scn2 (0.98)
560	TA, \neg MA, TK, NK, CB, PP, \neg BF, SV, PF, TC, WF	scn1 (0.95)	scn2 (0.05)
561	TA, \neg MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
562	TA, \neg MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
563	TA, \neg MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
564	TA, \neg MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
565	TA, \neg MA, TK, NK, CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.03)	scn2 (0.97)
566	TA, \neg MA, TK, NK, CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (0.97)	scn2 (0.03)

567	TA, ¬MA, TK, NK, CB, PP, BF, ¬SV, PF, TC, ¬WF	scn1 (0.14)	scn2 (0.86)
568	TA, ¬MA, TK, NK, CB, PP, BF, ¬SV, PF, TC, WF	scn1 (0.97)	scn2 (0.03)
569	TA, ¬MA, TK, NK, CB, PP, BF, SV, ¬PF, ¬TC, ¬WF	scn1 (0.00)	scn2 (1.00)
570	TA, ¬MA, TK, NK, CB, PP, BF, SV, ¬PF, ¬TC, WF	scn1 (0.00)	scn2 (1.00)
571	TA, ¬MA, TK, NK, CB, PP, BF, SV, ¬PF, TC, ¬WF	scn1 (0.00)	scn2 (1.00)
572	TA, ¬MA, TK, NK, CB, PP, BF, SV, ¬PF, TC, WF	scn1 (0.00)	scn2 (1.00)
573	TA, ¬MA, TK, NK, CB, PP, BF, SV, PF, ¬TC, ¬WF	scn1 (0.71)	scn2 (0.29)
574	TA, ¬MA, TK, NK, CB, PP, BF, SV, PF, ¬TC, WF	scn1 (0.98)	scn2 (0.02)
575	TA, ¬MA, TK, NK, CB, PP, BF, SV, PF, TC, ¬WF	scn1 (0.91)	scn2 (0.09)
576	TA, ¬MA, TK, NK, CB, PP, BF, SV, PF, TC, WF	scn1 (0.98)	scn2 (0.02)
577	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
578	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, ¬SV, PF, ¬TC, WF	scn1 (1.00)	scn2 (0.00)
579	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, ¬SV, PF, TC, ¬WF	scn1 (1.00)	scn2 (0.00)
580	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, ¬SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
581	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
582	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, SV, PF, ¬TC, WF	scn1 (1.00)	scn2 (0.00)
583	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, SV, PF, TC, ¬WF	scn1 (1.00)	scn2 (0.00)
584	TA, MA, ¬TK, ¬NK, ¬CB, PP, ¬BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
585	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, ¬SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
586	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, ¬SV, PF, ¬TC, WF	scn1 (1.00)	scn2 (0.00)
587	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, ¬SV, PF, TC, ¬WF	scn1 (1.00)	scn2 (0.00)
588	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, ¬SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
589	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
590	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, SV, PF, ¬TC, WF	scn1 (1.00)	scn2 (0.00)
591	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, SV, PF, TC, ¬WF	scn1 (1.00)	scn2 (0.00)
592	TA, MA, ¬TK, ¬NK, ¬CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
593	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
594	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, ¬TC, WF	scn1 (1.00)	scn2 (0.00)
595	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, TC, ¬WF	scn1 (1.00)	scn2 (0.00)
596	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, ¬SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
597	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
598	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, SV, PF, ¬TC, WF	scn1 (1.00)	scn2 (0.00)
599	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, SV, PF, TC, ¬WF	scn1 (1.00)	scn2 (0.00)
600	TA, MA, ¬TK, ¬NK, CB, PP, ¬BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
601	TA, MA, ¬TK, ¬NK, CB, PP, BF, ¬SV, PF, ¬TC, ¬WF	scn1 (1.00)	scn2 (0.00)
602	TA, MA, ¬TK, ¬NK, CB, PP, BF, ¬SV, PF, ¬TC, WF	scn1 (1.00)	scn2 (0.00)
603	TA, MA, ¬TK, ¬NK, CB, PP, BF, ¬SV, PF, TC, ¬WF	scn1 (1.00)	scn2 (0.00)
604	TA, MA, ¬TK, ¬NK, CB, PP, BF, ¬SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)

605	TA, MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
606	TA, MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
607	TA, MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
608	TA, MA, \neg TK, \neg NK, CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
609	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
610	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
611	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
612	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
613	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
614	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
615	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
616	TA, MA, \neg TK, NK, \neg CB, PP, \neg BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
617	TA, MA, \neg TK, NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
618	TA, MA, \neg TK, NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
619	TA, MA, \neg TK, NK, \neg CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
620	TA, MA, \neg TK, NK, \neg CB, PP, BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
621	TA, MA, \neg TK, NK, \neg CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
622	TA, MA, \neg TK, NK, \neg CB, PP, BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
623	TA, MA, \neg TK, NK, \neg CB, PP, BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
624	TA, MA, \neg TK, NK, \neg CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
625	TA, MA, \neg TK, NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
626	TA, MA, \neg TK, NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
627	TA, MA, \neg TK, NK, CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
628	TA, MA, \neg TK, NK, CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
629	TA, MA, \neg TK, NK, CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
630	TA, MA, \neg TK, NK, CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
631	TA, MA, \neg TK, NK, CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
632	TA, MA, \neg TK, NK, CB, PP, \neg BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
633	TA, MA, \neg TK, NK, CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
634	TA, MA, \neg TK, NK, CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
635	TA, MA, \neg TK, NK, CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
636	TA, MA, \neg TK, NK, CB, PP, BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
637	TA, MA, \neg TK, NK, CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (1.00)	scn2 (0.00)
638	TA, MA, \neg TK, NK, CB, PP, BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
639	TA, MA, \neg TK, NK, CB, PP, BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
640	TA, MA, \neg TK, NK, CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
641	TA, MA, TK, \neg NK, \neg CB, \neg PP, \neg BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
642	TA, MA, TK, \neg NK, \neg CB, \neg PP, \neg BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)

681	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
682	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
683	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
684	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
685	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
686	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (0.11)	scn2 (0.89)
687	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
688	TA, MA, TK, \neg NK, \neg CB, PP, \neg BF, SV, PF, TC, WF	scn1 (0.20)	scn2 (0.80)
689	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
690	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
691	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
692	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
693	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
694	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (0.49)	scn2 (0.51)
695	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
696	TA, MA, TK, \neg NK, \neg CB, PP, BF, \neg SV, PF, TC, WF	scn1 (0.60)	scn2 (0.40)
697	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
698	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
699	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
700	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
701	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (0.02)	scn2 (0.98)
702	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, PF, \neg TC, WF	scn1 (0.75)	scn2 (0.25)
703	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, PF, TC, \neg WF	scn1 (0.09)	scn2 (0.91)
704	TA, MA, TK, \neg NK, \neg CB, PP, BF, SV, PF, TC, WF	scn1 (0.75)	scn2 (0.25)
705	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
706	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
707	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
708	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
709	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
710	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
711	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
712	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, \neg SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
713	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
714	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
715	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
716	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
717	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
718	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)

719	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
720	TA, MA, TK, \neg NK, CB, \neg PP, \neg BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
721	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
722	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
723	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
724	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
725	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
726	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
727	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
728	TA, MA, TK, \neg NK, CB, \neg PP, BF, \neg SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
729	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
730	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
731	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
732	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
733	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
734	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
735	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
736	TA, MA, TK, \neg NK, CB, \neg PP, BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
737	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
738	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
739	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
740	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
741	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
742	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (0.12)	scn2 (0.88)
743	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
744	TA, MA, TK, \neg NK, CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (0.21)	scn2 (0.79)
745	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
746	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
747	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
748	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
749	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
750	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (0.88)	scn2 (0.12)
751	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (0.01)	scn2 (0.99)
752	TA, MA, TK, \neg NK, CB, PP, \neg BF, SV, PF, TC, WF	scn1 (0.92)	scn2 (0.08)
753	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
754	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
755	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
756	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)

757	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.02)	scn2 (0.98)
758	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (0.95)	scn2 (0.05)
759	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (0.09)	scn2 (0.91)
760	TA, MA, TK, \neg NK, CB, PP, BF, \neg SV, PF, TC, WF	scn1 (0.96)	scn2 (0.04)
761	TA, MA, TK, \neg NK, CB, PP, BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
762	TA, MA, TK, \neg NK, CB, PP, BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
763	TA, MA, TK, \neg NK, CB, PP, BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
764	TA, MA, TK, \neg NK, CB, PP, BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
765	TA, MA, TK, \neg NK, CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (0.59)	scn2 (0.41)
766	TA, MA, TK, \neg NK, CB, PP, BF, SV, PF, \neg TC, WF	scn1 (0.96)	scn2 (0.04)
767	TA, MA, TK, \neg NK, CB, PP, BF, SV, PF, TC, \neg WF	scn1 (0.86)	scn2 (0.14)
768	TA, MA, TK, \neg NK, CB, PP, BF, SV, PF, TC, WF	scn1 (0.96)	scn2 (0.04)
769	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
770	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
771	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
772	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
773	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
774	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
775	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
776	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, \neg SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
777	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
778	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
779	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
780	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
781	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
782	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
783	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
784	TA, MA, TK, NK, \neg CB, \neg PP, \neg BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
785	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
786	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
787	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
788	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
789	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
790	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
791	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
792	TA, MA, TK, NK, \neg CB, \neg PP, BF, \neg SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
793	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
794	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)

795	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
796	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
797	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
798	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
799	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
800	TA, MA, TK, NK, \neg CB, \neg PP, BF, SV, PF, TC, WF	scn1 (0.00)	scn2 (1.00)
801	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
802	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
803	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
804	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
805	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
806	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, \neg TC, WF	scn1 (0.05)	scn2 (0.95)
807	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
808	TA, MA, TK, NK, \neg CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (0.11)	scn2 (0.89)
809	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
810	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
811	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
812	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
813	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
814	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (0.82)	scn2 (0.18)
815	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
816	TA, MA, TK, NK, \neg CB, PP, \neg BF, SV, PF, TC, WF	scn1 (0.90)	scn2 (0.10)
817	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
818	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
819	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
820	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
821	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.01)	scn2 (0.99)
822	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (0.97)	scn2 (0.03)
823	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (0.04)	scn2 (0.96)
824	TA, MA, TK, NK, \neg CB, PP, BF, \neg SV, PF, TC, WF	scn1 (0.98)	scn2 (0.02)
825	TA, MA, TK, NK, \neg CB, PP, BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
826	TA, MA, TK, NK, \neg CB, PP, BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
827	TA, MA, TK, NK, \neg CB, PP, BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
828	TA, MA, TK, NK, \neg CB, PP, BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
829	TA, MA, TK, NK, \neg CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (0.40)	scn2 (0.60)
830	TA, MA, TK, NK, \neg CB, PP, BF, SV, PF, \neg TC, WF	scn1 (0.99)	scn2 (0.01)
831	TA, MA, TK, NK, \neg CB, PP, BF, SV, PF, TC, \neg WF	scn1 (0.77)	scn2 (0.23)
832	TA, MA, TK, NK, \neg CB, PP, BF, SV, PF, TC, WF	scn1 (0.99)	scn2 (0.01)

871	TA, MA, TK, NK, CB, PP, \neg BF, \neg SV, PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
872	TA, MA, TK, NK, CB, PP, \neg BF, \neg SV, PF, TC, WF	scn1 (0.91)	scn2 (0.09)
873	TA, MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
874	TA, MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
875	TA, MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
876	TA, MA, TK, NK, CB, PP, \neg BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
877	TA, MA, TK, NK, CB, PP, \neg BF, SV, PF, \neg TC, \neg WF	scn1 (0.06)	scn2 (0.94)
878	TA, MA, TK, NK, CB, PP, \neg BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
879	TA, MA, TK, NK, CB, PP, \neg BF, SV, PF, TC, \neg WF	scn1 (0.24)	scn2 (0.76)
880	TA, MA, TK, NK, CB, PP, \neg BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
881	TA, MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
882	TA, MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
883	TA, MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
884	TA, MA, TK, NK, CB, PP, BF, \neg SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
885	TA, MA, TK, NK, CB, PP, BF, \neg SV, PF, \neg TC, \neg WF	scn1 (0.40)	scn2 (0.60)
886	TA, MA, TK, NK, CB, PP, BF, \neg SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
887	TA, MA, TK, NK, CB, PP, BF, \neg SV, PF, TC, \neg WF	scn1 (0.78)	scn2 (0.22)
888	TA, MA, TK, NK, CB, PP, BF, \neg SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)
889	TA, MA, TK, NK, CB, PP, BF, SV, \neg PF, \neg TC, \neg WF	scn1 (0.00)	scn2 (1.00)
890	TA, MA, TK, NK, CB, PP, BF, SV, \neg PF, \neg TC, WF	scn1 (0.00)	scn2 (1.00)
891	TA, MA, TK, NK, CB, PP, BF, SV, \neg PF, TC, \neg WF	scn1 (0.00)	scn2 (1.00)
892	TA, MA, TK, NK, CB, PP, BF, SV, \neg PF, TC, WF	scn1 (0.00)	scn2 (1.00)
893	TA, MA, TK, NK, CB, PP, BF, SV, PF, \neg TC, \neg WF	scn1 (0.98)	scn2 (0.02)
894	TA, MA, TK, NK, CB, PP, BF, SV, PF, \neg TC, WF	scn1 (1.00)	scn2 (0.00)
895	TA, MA, TK, NK, CB, PP, BF, SV, PF, TC, \neg WF	scn1 (1.00)	scn2 (0.00)
896	TA, MA, TK, NK, CB, PP, BF, SV, PF, TC, WF	scn1 (1.00)	scn2 (0.00)

Table 14: All posteriors for the network in ([van Leeuwen, 2019](#))