

DISTRIBUZIONI NOTEVOLI DISCRETE

Funz. di probabilità	Aspettazione	Varianza	Funz. Gen. Momenti
$p_X(k)$	$\mathbb{E}[X]$	$\text{Var}(X)$	$G_X(t)$

Bernoulli

$\text{Ber}(p)$ $p \in [0, 1]$	$\begin{cases} p & \text{se } k = 1 \\ 1 - p & \text{se } k = 0 \\ & k \in \{0, 1\} \end{cases}$	p	$p(1 - p)$	$pe^t + (1 - p)$
-----------------------------------	--	-----	------------	------------------

Binomiale

$\text{Bin}(n, p)$ $n \in \{1, 2, \dots\}$ $p \in [0, 1]$	${n \choose k} p^k (1 - p)^{n-k}$ $k \in \{0, 1, \dots, n\}$	np	$np(1 - p)$	$(pe^t + (1 - p))^n$
---	---	------	-------------	----------------------

Geometrica

$\text{Geo}(p)$ $p \in [0, 1]$	$p(1 - p)^{k-1}$ $k \in \{1, 2, \dots\}$	$\frac{1}{p}$	$\frac{1-p}{p^2}$	$\begin{cases} \frac{p}{e^{-t} - (1-p)} & \text{se } t < \log \frac{1}{1-p} \\ +\infty & \text{se } t \geq \log \frac{1}{1-p} \end{cases}$
-----------------------------------	---	---------------	-------------------	--

Poisson

$\text{Pois}(\mu)$ $\mu \in (0, +\infty)$	$e^{-\mu} \frac{\mu^k}{k!}$ $k \in \{0, 1, \dots, n\}$	μ	μ	$e^{\mu(e^t - 1)}$
--	---	-------	-------	--------------------

**Binomiale
Negativa**

$\text{NBin}(r, p)$ $r \in \{1, 2, \dots\}$ $p \in [0, 1]$	${k-1 \choose r-1} p^r (1 - p)^{k-r}$ $k \in \{r, r+1, \dots\}$	$\frac{r}{p}$	$r \frac{1-p}{p^2}$	$\begin{cases} \left(\frac{p}{e^{-t} - (1-p)} \right)^r & \text{se } t < \log \frac{1}{1-p} \\ +\infty & \text{se } t \geq \log \frac{1}{1-p} \end{cases}$
--	--	---------------	---------------------	---

Ipergeometrica

$\text{Hyper}(r, b, n)$ $r, b, n \in \{1, 2, \dots\}$ $n \leq r + b$	$\frac{{r \choose k} {b \choose n-k}}{{r+b \choose n}}$ $k \in \{\max\{0, n-b\}, \dots, \min\{r, n\}\}$	$\frac{nr}{r+b}$	$\frac{nrb(r+b-n)}{(r+b)^2(r+b-1)}$	
--	--	------------------	-------------------------------------	--

DISTRIBUZIONI NOTEVOLI CONTINUE

	Dens. di probabilità $f_X(x)$	Aspettazione $\mathbb{E}[X]$	Varianza $\text{Var}(X)$	Funz. Gen. Momenti $G_X(t)$
Uniforme $\text{U}(\alpha, \beta)$ $\alpha, \beta \in \mathbb{R}$ $\alpha \leq \beta$	$\begin{cases} \frac{1}{\beta-\alpha} & \text{se } x \in (\alpha, \beta) \\ 0 & \text{altrimenti} \end{cases}$	$\frac{\alpha+\beta}{2}$	$\frac{(\beta-\alpha)^2}{12}$	$\frac{e^{\beta t} - e^{\alpha t}}{t(\beta-\alpha)}$
Esponenziale $\text{Exp}(\lambda)$ $\lambda \in (0, \infty)$	$\begin{cases} \lambda e^{-\lambda x} & \text{se } x \geq 0 \\ 0 & \text{altrimenti} \end{cases}$	$\frac{1}{\lambda}$	$\frac{1}{\lambda^2}$	$\begin{cases} \frac{\lambda}{\lambda-t} & \text{se } t < \lambda \\ +\infty & \text{se } t \geq \lambda \end{cases}$
Gamma $\Gamma(\lambda, n)$ $\lambda \in (0, \infty)$ $n \in \{1, 2, \dots\}$	$\begin{cases} \frac{\lambda^n}{(n-1)!} x^{n-1} e^{-\lambda x} & \text{se } x \geq 0 \\ 0 & \text{altrimenti} \end{cases}$	$\frac{n}{\lambda}$	$\frac{n}{\lambda^2}$	$\begin{cases} \left(\frac{\lambda}{\lambda-t}\right)^n & \text{se } t < \lambda \\ +\infty & \text{se } t \geq \lambda \end{cases}$
Pareto $\text{Par}(\alpha)$ $\alpha > 0$	$\begin{cases} \frac{\alpha}{x^{\alpha+1}} & \text{se } x \geq 1 \\ 0 & \text{altrimenti} \end{cases}$	$\frac{\alpha}{\alpha-1}$ se $\alpha > 1$	$\frac{\alpha}{(\alpha-1)^2(\alpha-2)}$	$\#$ se $\alpha > 2$
Gaussiana $\text{N}(\mu, \sigma^2)$ $\sigma > 0$ $\mu \in \mathbb{R}$	$\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$	μ	σ^2	$e^{\mu t + \frac{\sigma^2}{2}t^2}$
