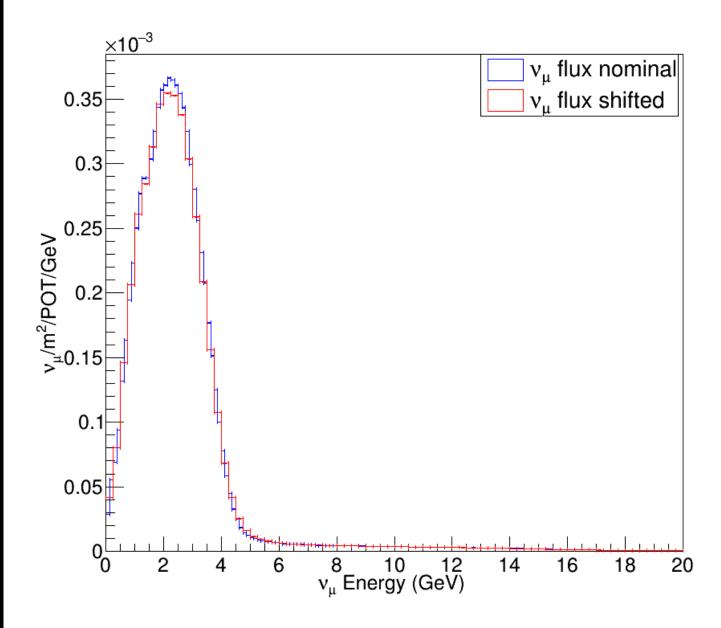
BEAM MONITORING WITH SAND

- My thesis studied the beam monitoring capabilities of the SAND detector, via the comparison of the distribution of an observable sensitive to beam anomalies
- Observable: reconstructed muon momentum
- First systematic: horn-1 0.5 mm Y shift
- Test statistics: χ^2

SIMULATED SAMPLES

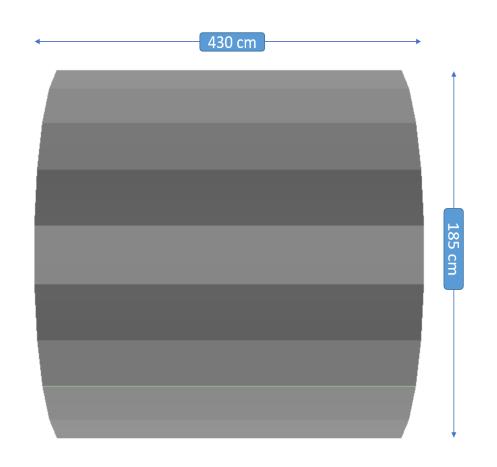


Simulated samples from:

- Nominal neutrino flux
- **Shifted** neutrino flux (Y +0.5mm in the first beam horn)

Note: Histograms retrieved from https://home.fnal.gov/~ljf26/DUNEFluxes

TARGET: FRONT CALORIMETERS



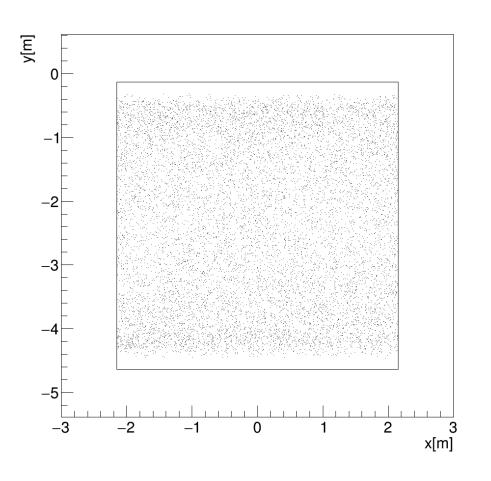


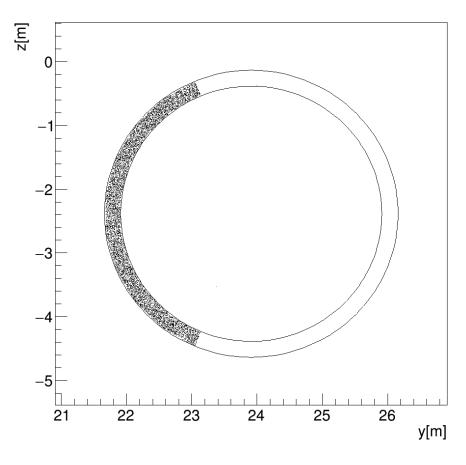
- *Dunendggd* simulated geometry
- Target: 9 front calorimeter barrel modules

$$N_{week} = r_{CC} \times f_{CC}^{-1} \times m_{mod} \times n_{mod}$$
= $(4.865 \times 10^5 ev[\nu_{\mu}(CC)]/ton/week) \times (2/3)^{-1} \times (2.75 ton) \times (9)$
 $\approx 1.75 \times 10^6$

One week's worth of statistics

TARGET: FRONT CALORIMETERS





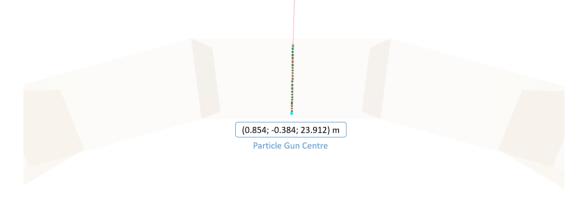
• Interaction vertex distributions on the *xy* and *yz* planes

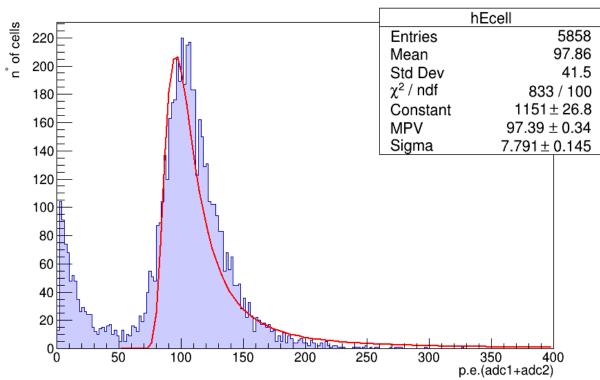
$$N_{week} = r_{CC} \times f_{CC}^{-1} \times m_{mod} \times n_{mod}$$

= $(4.865 \times 10^5 ev[\nu_{\mu}(CC)]/ton/week) \times (2/3)^{-1} \times (2.75 ton) \times (9)$
\(\times 1.75 \times 10^6\)

One week's worth of statistics

PRELIMINARY MEASUREMENT: LIGHT YIELD





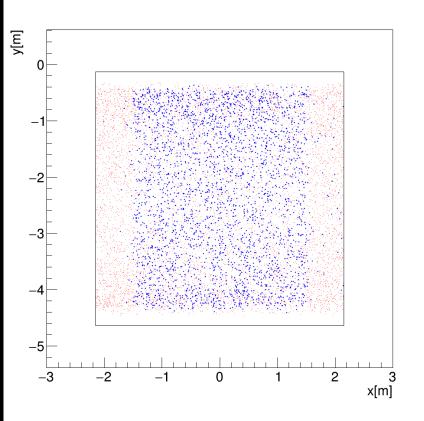
 Simulated 1000 muons at 10 GeV passing through an ECAL barrel module

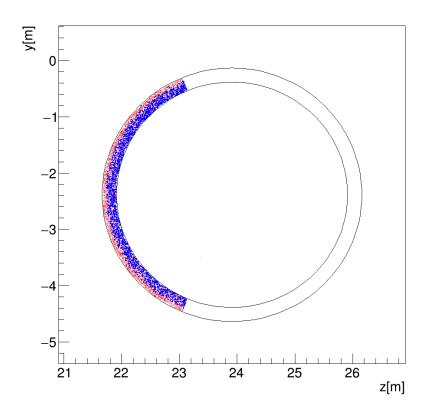
$$\Delta E_{cell} \simeq \left(\frac{dE}{dx}\right)^{MIP} \rho_{Pb} \Delta x_{Pb} + \left(\frac{dE}{dx}\right)^{MIP} \rho_{Sc} \Delta x_{Sc} \simeq 42.22 \text{ MeV}$$

$$N_{p.e.}^{cell} = (97.4 \pm 0.3) \text{ p.e.}$$

$$c = \frac{N_{p.e.}^{cell}}{\Delta E_{cell}} \simeq 2.31 \text{ [p.e./MeV]}$$

FIDUCIAL CUT





Spatial distribution in ND hall global coordinates of the true neutrino interaction vertexes of the events that survive the fiducial cut (blue) and those that don't (red).

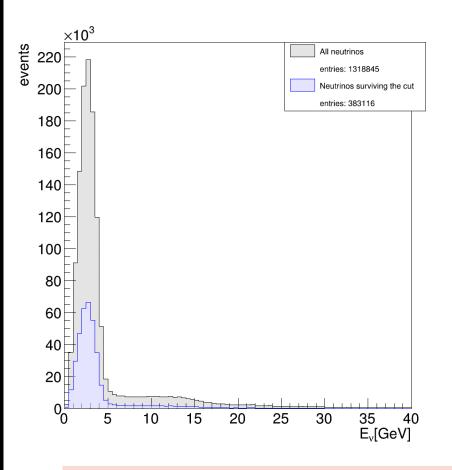
• Threshold on the energy deposition on the outer layer (E < 15MeV):

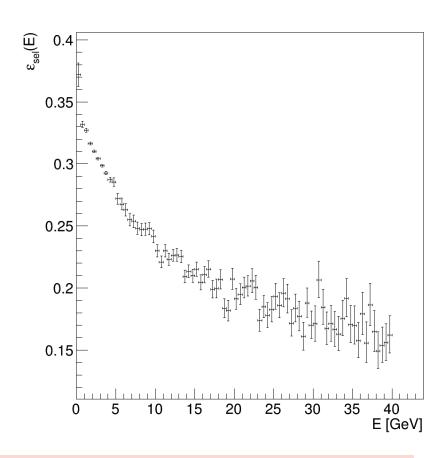
$$N_{p.e.}^{th} = c \times \Delta E_{th} \simeq 35$$
 p.e.

• X vertex, estimated as a weighted average on the energy deposition on the cells, is selected as:

$$|x_V| \le 1.5 \text{ m}$$

FIDUCIAL CUT





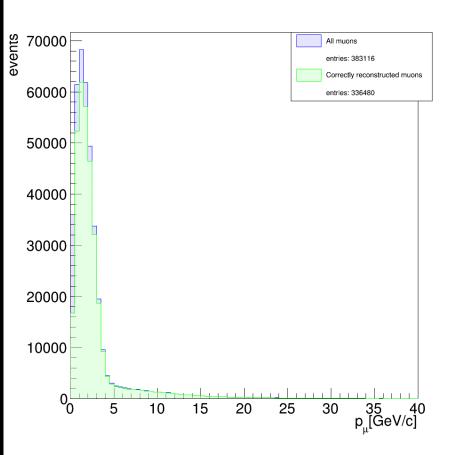
(*Left*) Energy (Monte Carlo truth) distribution of neutrinos from the CC nominal sample (grey); distribution surviving the fiducial cut (blue). (*Right*) Selection efficiency as a function of neutrino energy from the Monte Carlo truth.

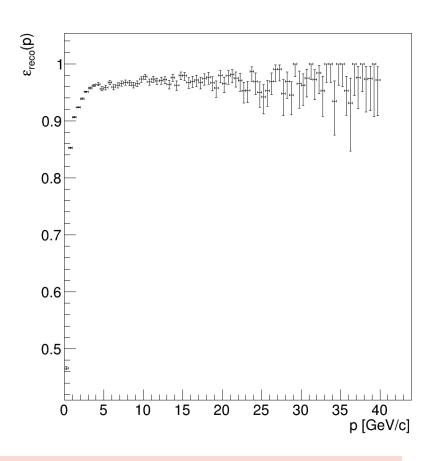
• Selection efficiency:

$$\varepsilon_{cut} = \frac{N_{fid}}{N_{CC}} = 0.2905 \pm 0.0004$$

Note: efficiency decreases at higher energy; might be due to nuclei fragmentation in DIS

MOMENTUM RECONSTRUCTION SELECTION



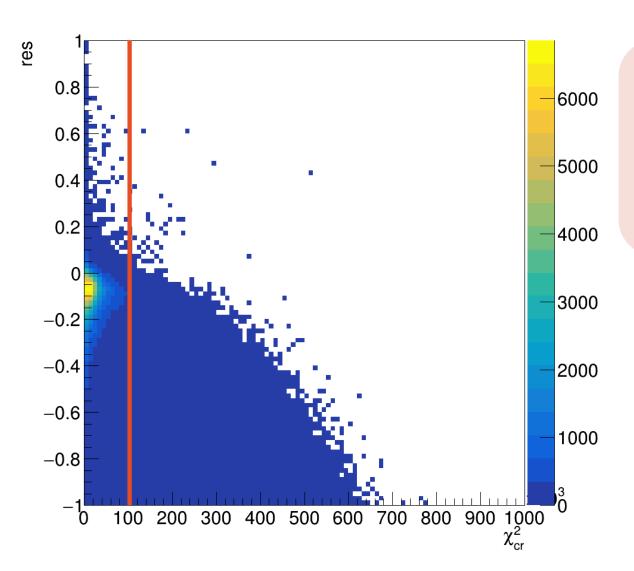


• Momentum reconstruction efficiency:

$$\varepsilon_{reco} = \frac{N_{reco}}{N_{fid}} = 0.9168 \pm 0.0004$$

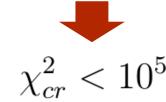
(*Left*) Distributions of the true Monte Carlo momenta of the muons from the fiducial sample (blue) and only the ones correctly reconstructed (green). (*Right*) Reconstruction algorithm efficiency as a function of the true Monte Carlo muon momentum

MOMENTUM RECONSTRUCTION QUALITY SELECTION



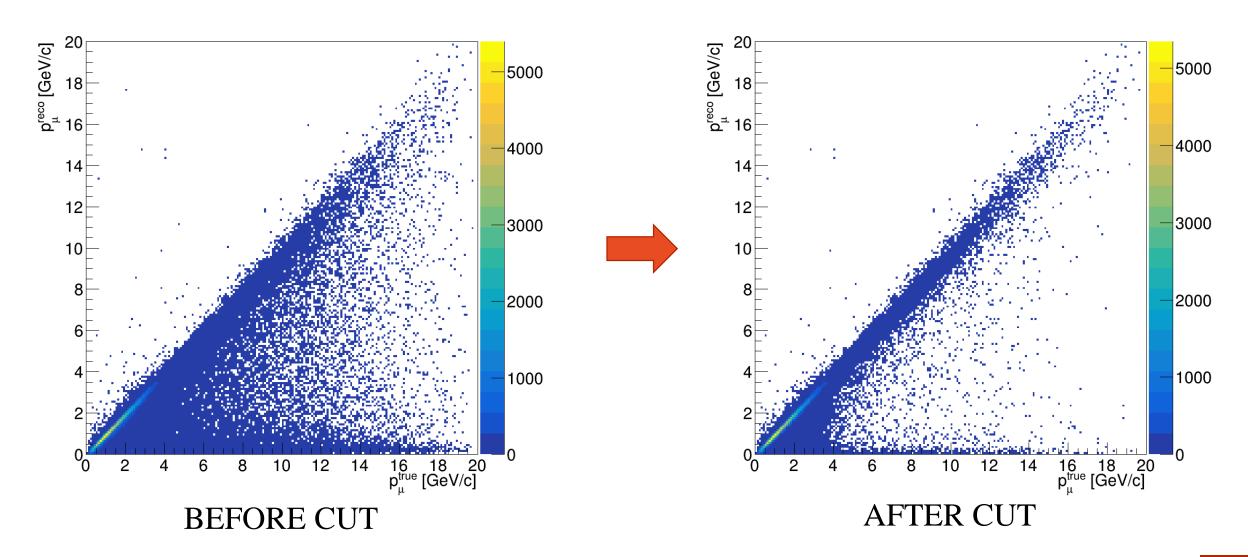
$$\chi_{cr}^2 = \frac{1}{N_{hits}} \sum_{i=1}^{N_{hits}} |(y_i - y_C)^2 + (z_i - z_C)^2 - R^2|$$

$$res = 1 - p_{\mu}^{true} / p_{\mu}^{reco}$$



$$\varepsilon_{qual} = \frac{N_{qual}}{N_{reco}} = 0.9290 \pm 0.0004$$

MOMENTUM RECONSTRUCTION QUALITY SELECTION

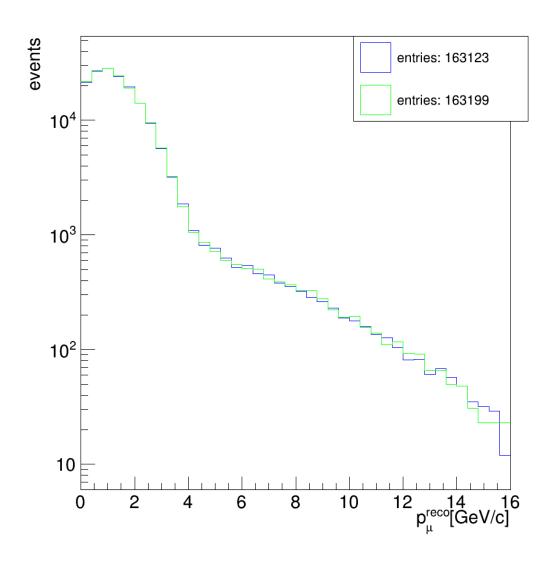


CHI-SQUARED TWO-SAMPLE TEST STATISTICS

$$T = \sum_{i=1}^{k} \frac{(u_i - v_i)^2}{u_i + v_i}$$

- Where k is the number of bins in the histograms and u_i and v_i are their contents
- T approximately follows a chi-squared distribution

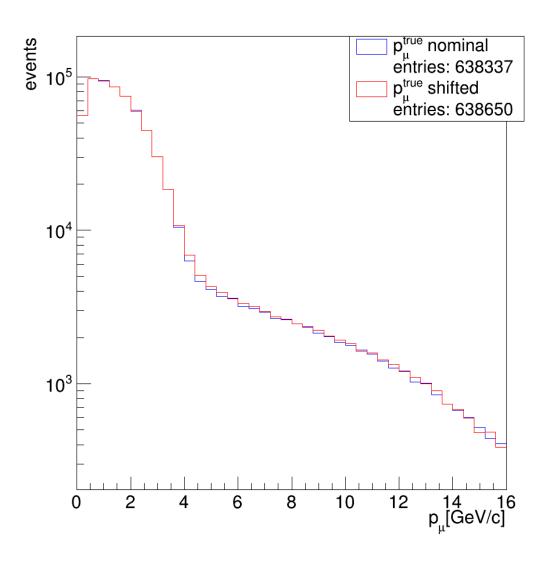
CONTROL ANALYSIS: TWO NOMINAL SAMPES



• We apply the T two equally large nominal samples ($\sim 0.8 \times 10^6$ events):

$$p_{control} = 0.527; \quad \sigma_{control} = 0.633 \ (\chi^2)$$

CONTROL ANALYSIS: IDEAL SELECTION

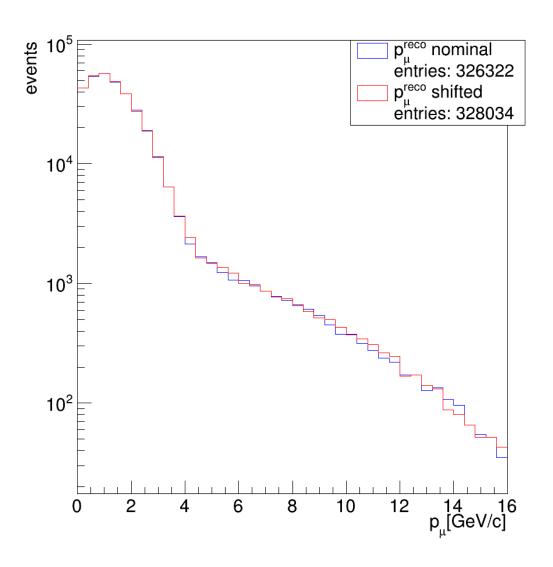


- We applied *T* the test to the true Monte Carlo momenta from the nominal and shifted samples.
- A fiducial cut was applied by selecting events whose true interaction position was in the fiducial volume
- This was done in order to gauge what the best possible p-value (i.e. the smallest and most decisive) might be:

$$p_{truth} = 5.15 \times 10^{-7}; \quad \sigma_{truth} = 5.02 \ (\chi^2)$$

Note: in principle no p-value should be smaller than p_{truth}

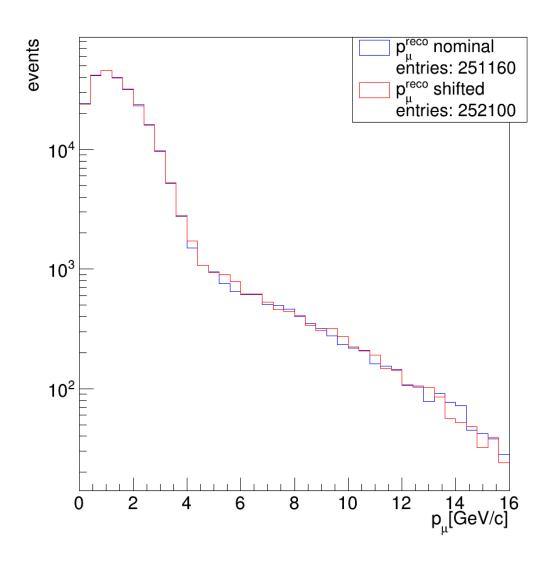
RESULTS: FIDUCIAL + RECONSTRUCTION



$$p_{reco} = 1.55 \times 10^{-3};$$

$$\sigma_{reco} = 3.17$$

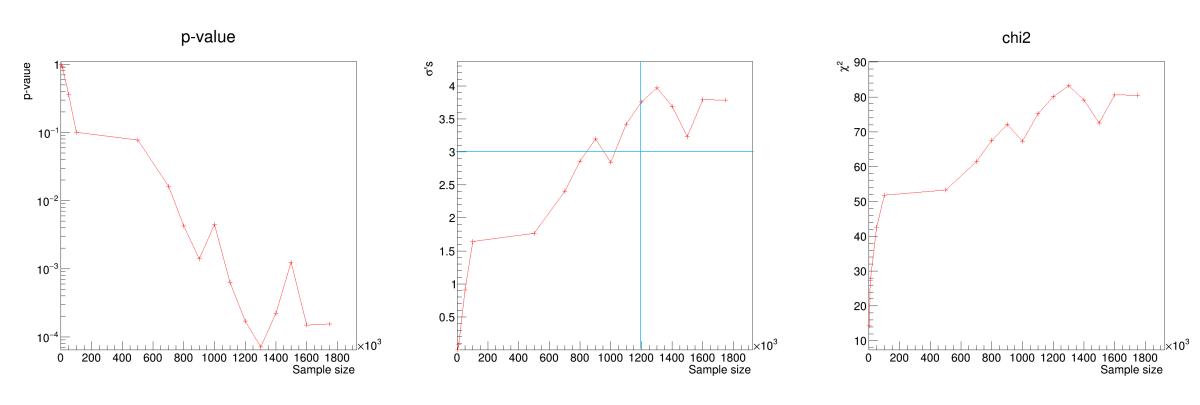
RESULTS: FIDUCIAL + RECONSTUCTION + QUALITY



We repeat the procedure by applying the quality cut to both samples:

$$p_{reco} = 1.55 \times 10^{-4};$$
$$\sigma_{reco} = 3.78$$

P-VALUE EVOLUTION WITH THE SAMPLE



- As we should expect, as the samples become larger the χ^2 and number of σ 's increase, while the p-value decreases.
- With a sample grater than 1.2 million events, comparable to (even if smaller) that the one expected during a week of data taking, is possible to identify the beam anomaly with a confidence level corresponding to more than 3σ

CONCLUSIONS

- We observed that in the case of a perfect detector with a perfect reconstruction, (i.e. using the Monte Carlo "truth"), the significance of the difference among the nominal and shifted samples does not exceed 5σ
- Using reconstructed quantities, fiducial volume and quality selection we reach $\sim 3.8\sigma$ confidence level
- The result can be improved: for example include neutrinos with interactions in the STT, or consider the reconstructed position on the *xy* plane of the interaction vertexes, both in the front calorimeters and the STT.