## Statistical Data Analysis with Excel for Beginners v2





Trainer: Dr. Alfred Ang





Website: <u>www.tertiarycourses.com.sg</u> Email: enquiry@tertiaryinfotech.com

#### **About the Trainer**

Dr. Alfred Ang is the founder of Tertiary Courses. He is a serial entrepreneur. He founded OSWeb2Design Singapore Pte Ltd in 1997 offering web development, e-commerce store development, graphics design, ebook publishing, mobile apps development, and digital marketing services. He established the first online gardening store in Singapore, Eco City Hydroponics Pte Ltd in 2000, offering a wide range of gardening products such as seeds, plant nutrients, hydroponics kits etc. Eco City Hydroponics has become the most popular and successful gardening store in Singapore. He founded Tertiary Infotech Pte Ltd in 2012 and transformed the business to a training platform, Tertiary Courses in 2014. Tertiary Courses offers a wide range of SkillsFuture courses for PMETs to upgrade their skills and knowledge. He also established Tertiary Courses Malaysia in 2016. He also founded Tertiary Robotics in 2015 offering Arduino, Raspberry Pi, Microbit and Robotics product

Dr. Alfred Ang earned his Ph.D. from National University of Singapore in 2000, majoring in Electrical and Electronics Engineering. He also completed an online MBA course with U21 Global based in Australia. He obtained his B.Sc (Hons) from National University of Singapore in 1992, majoring in Physics. He topped his Physics cohort for 3 consecutive years and funded his degree study with Book prizes, Study awards, bursaries and tuition. He has worked in Defence, Electronics and Semiconductor Industries. His current interests include Machine Learning, Deep Learning, Artificial Intelligence, Internet of Things, Robotics and Programming.

Dr. Alfred Ang is ACTA certified trainer and DACE certified developer. He is an associate adult educator with IAL, IBM Certified AI Practitioner and IBM Certified Design Thinking Practitioner. He was Distinguished Toastmasters (DTM) and Senior Member of IEEE. He has published more than 20 peer reviewed papers and co-inventors for more than 20 inventions.

#### Let's Know Each Other...

Say a bit about yourself

- Name
- What Industry you are from?
- Do you have any prior knowledge in statistics or data analysis?
- Why do you want to learn statistics?

#### **Ground Rules**

- Set your mobile phone to silent mode
- Actively participate in the class. No question is stupid.
- Respect each other view
- Exit the class silently if you need to step out for phone call, toilet break

## Ground Rules for Virtual Training

- Upon entering, mute your mic and turn on the video. Use a headset if you can
- Use the 'raise hand' function to indicate when you want to speak
- Participant actively. Feel free to ask questions on the chat whenever.
- Facilitators can use breakout rooms for private sessions.



## WSQ and SSG TG Application Form

Please fill up the following WSQ and SSG TG Application Form for TRACOM survey, e-cert generation and WSQ funding

https://forms.gle/pJ2WxHZ3fyRbDLVu6



## Digital Attendance

- You need to take digital attendance in the AM and PM.
- Please download the mySkillsFuture apps below to take your digital attendance for WSQ and SFC courses.





#### Guidelines for Facilitators

- 1. Once all the participants are in and introduce themselves
- Goto gallery mode, take a snapshot of the class photo makes sure capture the date and time
- 3. Start the video recording (only for WSQ courses)
- Continue the class
- Before the class end on that day, take another snapshot of the class photo - makes sure capture the date and time
- 6. For NRIC verification, facilitator to create breakout room for individual participant to check (only for WSQ courses)
- Before the assessment start, take another snapshot of the class photo - makes sure capture the date and time (only for WSQ courses)
- For Oral Questioning assessment, facilitator to create breakout room for individual participant to OQ (only for WSQ courses)
- 9. End the video recording and upload to cloud (only for WSQ courses)
- 10. Assessor to send all the assessment records, assessment plan and photo and video to the staff (only for WSQ courses).

## Prerequisite

This is a beginner course. No prerequisite is assumed.

## Learning Outcomes

By end of the course, learners will be able to

- perform data analysis with descriptive statistics, probability theory and probability distributions,
- perform data analysis with sampling theory and hypothesis tastings
- perform data analysis with regression and correlation analysis.

## Agenda

#### Topic 1 Basic Statistics

- Why Statistics Matter
- Types of Data
- Descriptive Statistics
- Probability and Conditional Probability
- Probability Distributions
- Install Excel Statistical Analysis ToolPak

#### Topic 2 Sampling and Hypothesis Testing

- Sampling
- Central Limit Theorem
- Sampling Distribution and Standard Errors of Sample Mean
- Confidence Interval
- Z and T Statistics
- Overview of Hypothesis Testing
- Types of Hypothesis Testing
- Type 1 and Type 2 Errors
- Analysis of Variance (ANOVA)

## Agenda

#### Topic 3 Regression and Correlation Analysis

- Regression Modeling
- Residues and Mean Square Error
- Covariance and Correlation Analysis

#### Final Assessment

- Practical Performance
- Oral Questioning

## Google Classroom

- Goto google classroom https://classroom.google.com
- Enter the class code below to join the class on the top right.
- If you cannot access the google classroom, please inform the trainer or staff.

# C2uew63



Two e-certificates will be awarded to trainees who have demonstrated competency in the WSQ Excel Statistical Analysis assessment and achieved at least 75% attendance.

- WSQ Statement of Attainment (SOA) Data and Statistical Analytics PTP-BIN-4055-1.1 under the Public Transport Skills Framework
- Certification of Achievement by Tertiary Infotech Pte Ltd



## Topic 1 Basic Statistics

#### What is Statistics?

**Statistics** is a discipline which is concerned with:

- designing experiments and other data collection,
- summarizing information to aid understanding,
- drawing conclusions from data, and
- estimating the present or predicting the future.

Statistical statements:

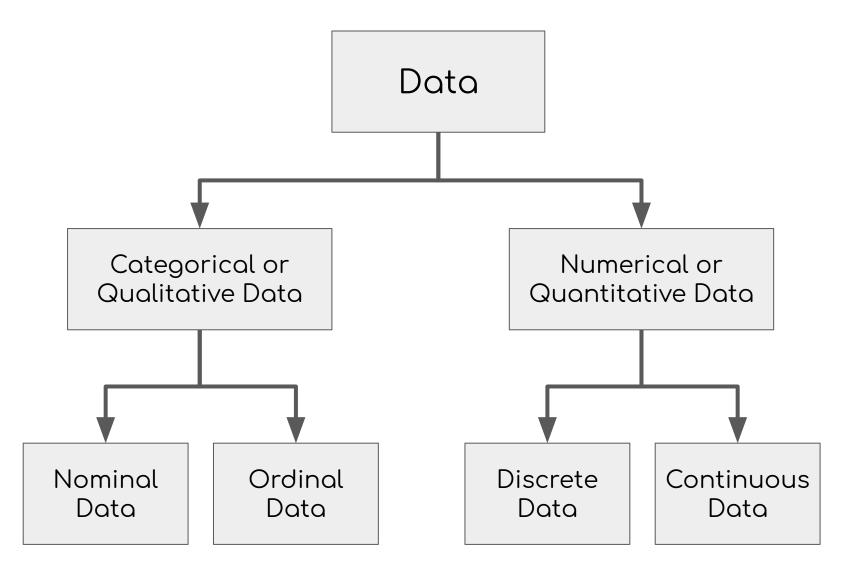
"I sleep for about eight hours per night on average"

"You are more likely to pass the exam if you start preparing earlier"

## Why Statistics Matter?

- Environmental Study
  - Is Singapore getting hotter over last 10 years?
- Policy Study
  - Is more people using green transport such as Bicycles, Buses, Carpool, CNG Cars, Electric Cars, Electric Scooters
- Market Analysis
  - Is more people likely to take green transport if they've seen a recent TV advertisement for green transport?
- Public Transport
  - Is more people likely to commute by MRT if we have more MRT stations in the neighborhood?
- Health Care
  - Does air pollution from vehicles cause any health concern?
- Data Science
  - Statistics is fundamental for understanding Artificial Intelligence and Machine Learning.

## Types of Data



## Categorical and Quantitative Data

- Categorical (Qualitative) Data each observation belongs to one of a set of categories. Examples:
  - Weather (Rainy /Sunny)
  - Air Pollutants (Ozone/Nitrogen Dioxide)
  - Gender (Male or Female)
  - Place of residence (HDB, Condo, ...)
  - Marital status (Married, Single,...)
- Quantitative (Numerical) Data observations take numerical values. Examples:
  - Surface Air temperature
  - Weekly number of dengue cases
  - No. of days with rainfall in a month
  - Age
  - Number of cars
  - Weight

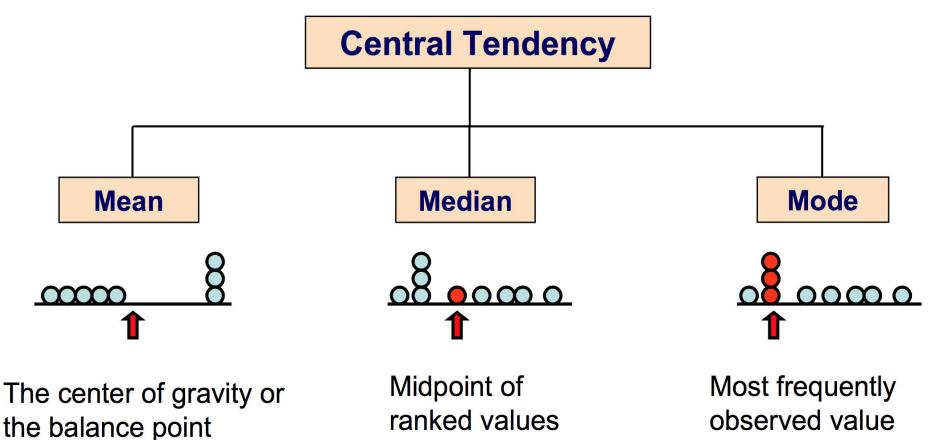
#### Nominal and Ordinal Data

- Nominal Data is defined as data that is used for naming or labelling variables, without any quantitative value. It is sometimes called "labels" data Eg
  - Male/Female
  - Red/Green/Blue
- Ordinal Data is a type of categorical data with an order. The variables in ordinal data are listed in an ordered manner.
  - Disagree/Neutral/Agree/Strongly Agree
  - Very Bad/Bad/Good/Very Good

#### Discrete and Continuous Data

- **Discrete Data is** a set of countable numbers such as 0, 1, 2, 3,.....Examples:
  - No. of days with rainfall in a month
  - Weekly no. of dengue cases
  - Number of children in a family
  - Number of foreign languages spoken
- Continuous Data are continuous numbers from an interval. Examples:
  - Surface Air temperature
  - Amount of rainfall in a month
  - Height
  - Weight

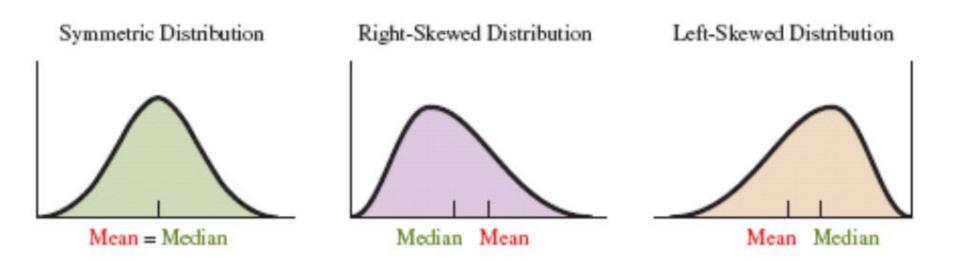
## Measures of Central Tendency



- Mean add up all the values and divide by how many there are
- Median Arrange all the numbers from smallest to largest:
  - o odd number of points: Median = middle value
  - even number of points: Median= mean of the middle two values

#### Mean vs Median

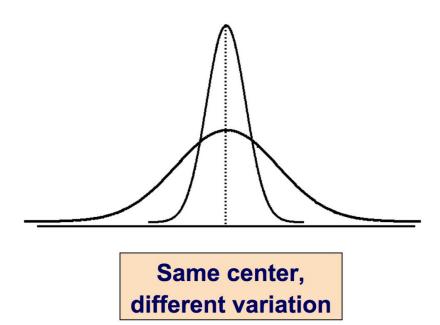
- Mean
  - Useful for roughly symmetric quantitative data
  - Sensitive to outlier data
- Median
  - Splits the data into halves
  - Useful for highly skewed quantitative data
  - Insensitive to outlier data



## Measures of Dispersion

- The measures of dispersion measure the differences between how far "spread out" the data values are.
- Two commonly used measures for dispersion are: range and standard deviation.

•



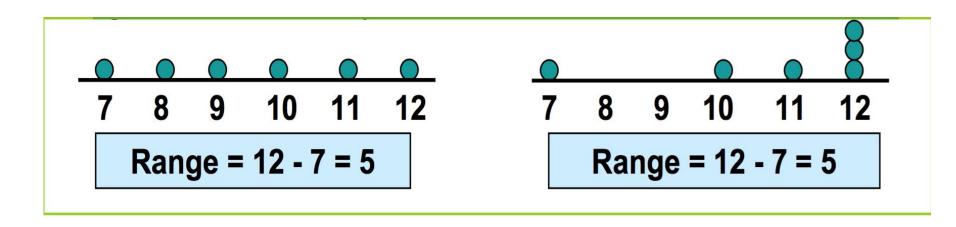
#### Standard Deviation

- The standard deviation measures the dispersion of a dataset relative to its mean and is calculated as the square root of the variance
- Larger standard deviation means greater variability of the data.

$$ext{SD} = \sqrt{rac{\sum |x - ar{x}|^2}{n}}$$

## Range

- Range is the difference between the highest and lowest values.
- Since it uses only the extreme values, it is greatly affected by extreme values.
- Range ignores the way in which data are distributed



## Average Function in Excel

The AVERAGE function measures central tendency, which is the location of the center of a group of numbers in a statistical distribution

AVERAGE(A2:A7)	Averages all of numbers in list
AVERAGE(A2:A4,A7)	Averages the top three and the last number
AVERAGEIF(A2:A7, "<>0")	Averages the numbers in the list except those that contain zero

#### Median Function in Excel

The MEDIAN function measures central tendency, which is the location of the center of a group of numbers in a statistical distribution.

MEDIAN(A2:A6)	Median of the 5 numbers in the range A2:A6. Because there are 5 values, the third is the median.
MEDIAN(A2:A7)	Median of the 6 numbers in the range A2:A7. Because there are six numbers, the median is the midway point between the third and fourth numbers.

#### Mode Function in Excel

The MODE function measures central tendency, which is the location of the center of a group of numbers in a statistical distribution

MODE(A2:A7)	Mode, or most frequently occurring number above
-------------	---

#### STDEVP Function in Excel

 STDEVP assumes that its arguments are the entire population. If your data represents a sample of the population, then compute the standard deviation using STDEV.

STDEVP(A3:A12)	Standard deviation of breaking strength	

## Activity: Descriptive Statistics

Consider the following three sets of observations:

- Set 1: 8,9,10,11,12
- Set 2: 8,9,10,11,100
- Set 3: 8,9,10,11,1000
- (a) Find the median and mean for each data set.
- (b) Find the range and standard deviation for each data set.
- (c) What do these data sets illustrate about the resistance of the median and mean?
- Use the Excel functions to compute the above values.
- Verify the result with the online descriptive statistics tool to compute the answer <a href="https://www.calculatorsoup.com/calculators/statistics/descriptivestatistics.php">https://www.calculatorsoup.com/calculators/statistics.php</a>

## What is Probability?

- Probability is a measure of the likelihood that an event will occur.
- Probability is quantified as a number from 0 to 1

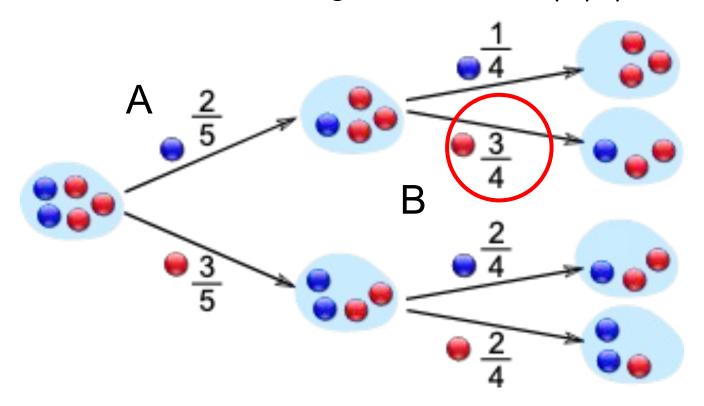
Probabilistics statements:

"The probability of getting a head from tossing a coin is 0.5"

"The probability of tomorrow rainy is high since today is a rainy day"

## Conditional Probability

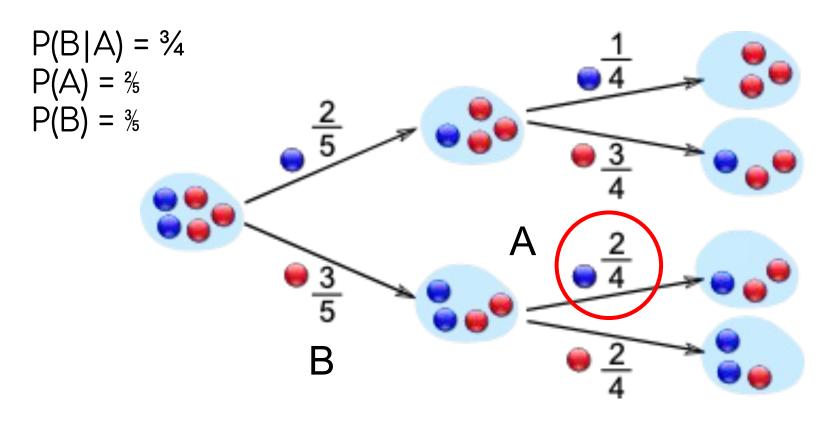
- Conditional probability is the probability of one event (B) given another event (A) is known
- A: get a blue marble first
- B: get a red marble then
- Based on the tree diagram below, P(B|A) = 3/4



## Bayes' Theorem

- Bayes' Theorem is a way of finding a conditional probability when we know other probabilities.
- The formula is P(A|B) = P(A) P(B|A)/P(B)

$$P(A|B) = P(B|A)*P(A)/P(B) = \frac{3}{4}*\frac{3}{5} / \frac{3}{5} = \frac{3}{4}*\frac{2}{3} = \frac{2}{4}$$



## Activity: Conditional Probability

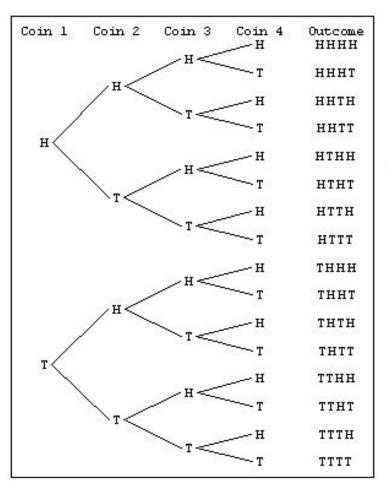
#### **Actual Status**

		Positive	Negative
<b>Test Result</b>	Positive	8 (TP)	2 (FP) Type 1 Error
	Negative	2 (FN) Type 2 Error	88 (TN)
		10	90

- If 100 people took the COVID-19 test, above is the test result
- Compute the conditional probability that a person is positive is tested positive
   P(test positive|actual positive)

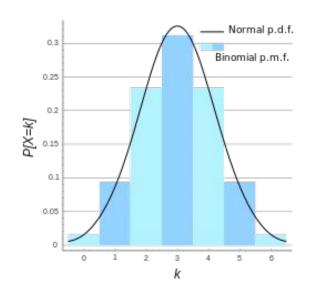
#### Binomial Distribution

- The binomial distribution with parameters n and p is the discrete probability distribution of the number of successes.
- A binomial distribution can be thought of as simply the probability of getting # of head outcome in an experiment of tossing multiple coins.



$$P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$$
n: No of coins/toss
$$\mu_X = np$$
k: No of head
$$\sigma_X^2 = np(1-p)$$

$$\rho = \text{Probability for getting a head in one toss}$$



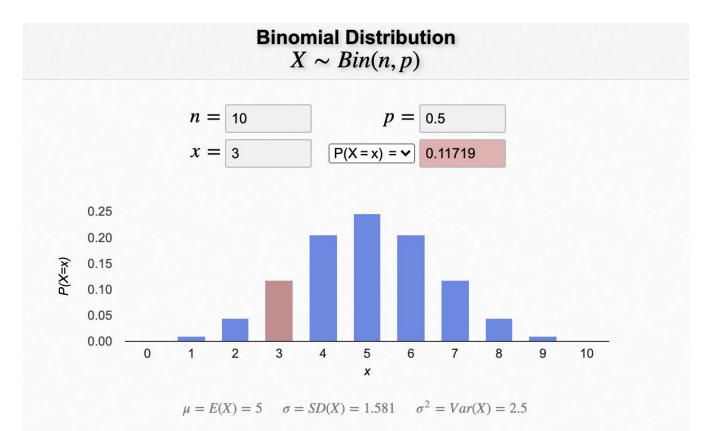
## BINOM.DIST function in Excel

- Use BINOM.DIST in problems with a fixed number of tests or trials, when the outcomes of any trial are only success or failure, when trials are independent, and when the probability of success is constant throughout the experiment.
- For example, BINOM.DIST can calculate the probability that two of the next three babies born are male.

BINOM.DIST(A2,A3,A4,FA	Probability of exactly 6 of 10 trials being
LSE)	successful.

# Activity: Binomial Distribution

- Use Excel to compute the Binomial probability for n= 10, p=0.5, x=3,4,5,6
- Verify with the following online tool
- https://homepage.divms.uiowa.edu/~mbognar/ap plets/bin.html

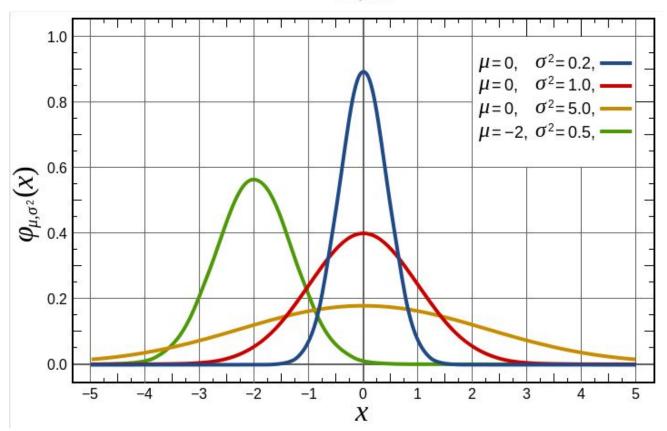


#### Normal Distribution

- Normal distribution, also known as the Gaussian distribution, is a continuous probability distribution that is symmetric about the mean, showing that data near the mean are more frequent in occurrence than data far from the mean
- Normal distribution is approximation of Binomial distribution if n

$$-> \infty$$

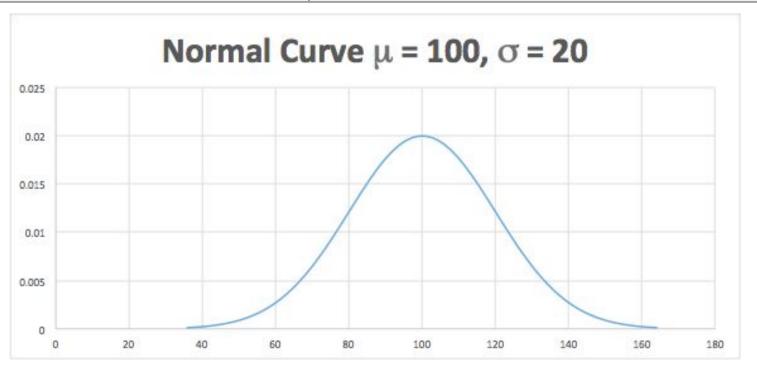
$$f(x \mid \mu, \sigma) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$



#### NORMDIST function in Excel

 The NORMDIST function returns the normal distribution for the specified mean and standard deviation

NORMDIST(A2,A3,A4,TRUE)	Cumulative distribution function
NORMDIST(A2,A3,A4,FALSE)	Probability mass function

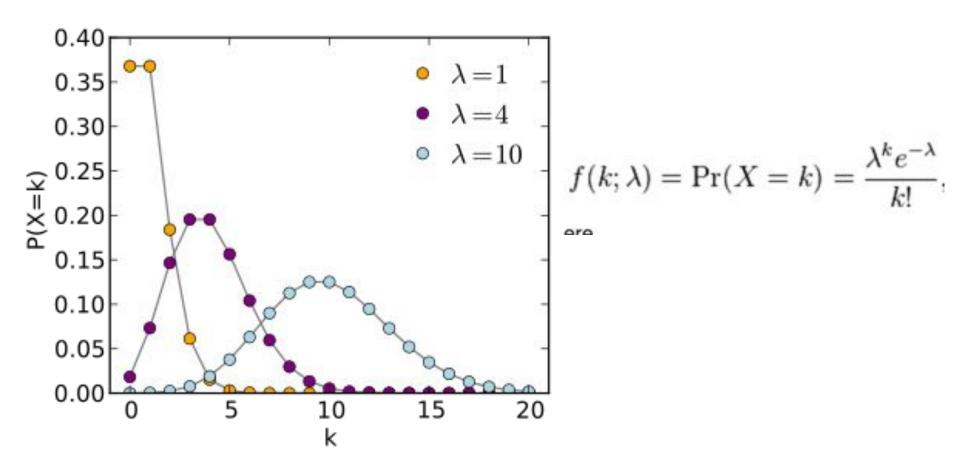


## Activity: Normal Distribution

- The normal distribution for womens height in SIngapore has  $\mu$ = 160cm,  $\sigma$ = 20cm. Most major airlines have height requirements for flight attendants.
- The minimum height requirement is 170cm. What proportion of adult females in Singapore are not tall enough to be a flight attendant?
- Use Excel to compute the value above
- Verify the answer using the following online tool
- https://homepage.divms.uiowa.edu/~mbognar/app lets/normal.html

## Poisson Distribution

 The Poisson distribution lets you estimate the number of customers who will come into a store during a given time period such as an hour or perhaps the number of seconds between times that cars arrive at a toll booth.



## POISSON.DIST Function in Excel

The POISSON.DIST function Returns the Poisson distribution. A common application of the Poisson distribution is predicting the number of events over a specific time, such as the number of cars arriving at a toll plaza in 1 minute.

POISSON.DIST(A2,A3,TRUE)	Cumulative Poisson probability with the arguments specified in A2 and A3.
POISSON.DIST(A2,A3,FALSE)	Poisson probability mass function with the arguments specified in A2 and A3.

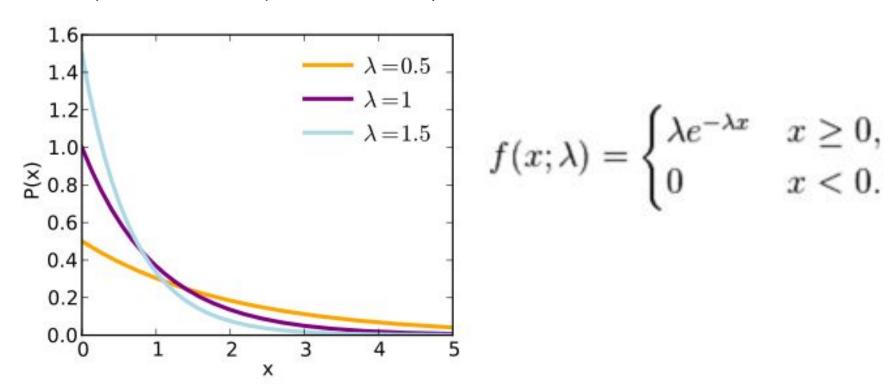
## Activity: Poisson Distribution

- A bank is interested in studying the number of people who use the ATM located outside its office late at night.
- On average, 1.6 customers use the ATM during any
   10 minute interval between 9pm and midnight.
- What is lambda  $\lambda$  for this problem?
- What is the probability of exactly 3 customers using th ATM during any 10 minute interval?
- What is the probability of 3 or fewer people?
- Use Excel to compute the answers and verify using the online tool

https://www.onlinemathlearning.com/poisson-distribution.html

## **Exponential Distribution**

- If you sell products via your company's website, knowing the average time between orders helps you plan the number of employees you'll need to have on duty at any time.
- This type of occurrence is described by the exponential probability distribution.



## EXPON.DIST function in Excel

- EXPON.DIST function returns the exponential distribution. Use EXPON.DIST to model the time between events, such as how long an automated bank teller takes to deliver cash.
- For example, you can use EXPON.DIST to determine the probability that the process takes at most 1 minute.

EXPON.DIST(A2,A3,TRUE)	Cumulative exponential distribution function
EXPON.DIST(0.2,10,FALSE)	Probability exponential distribution function

## Activity: Exponential Distribution

- The number of days ahead travelers purchase their airline tickets can be modeled by an exponential distribution with the average amount of time equal to 15 days.
- Find the probability that a traveler will purchase a ticket fewer than ten days in advance.
- Use Excel to compute the answers and verify using the online tool

https://homepage.divms.uiowa.edu/~mbognar/applets/exp-like.html

#### Software for Statistics

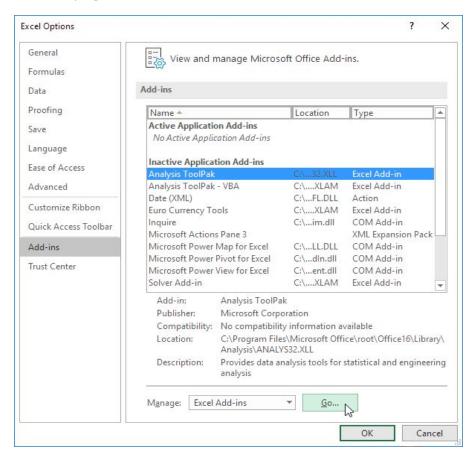
- Minitab <a href="https://www.minitab.com/en-us/">https://www.minitab.com/en-us/</a>
- SPSS Statistics <u>https://www.ibm.com/sg-en/products/spss-statistics</u>
- Jamovi <a href="https://www.jamovi.org/">https://www.jamovi.org/</a>
- R <a href="https://cran.r-project.org/">https://cran.r-project.org/</a>
- Excel Statistical Analysis Tool
- Minitab, SPSS and Excel are commercial software.
- Jamovi and R are free open source software

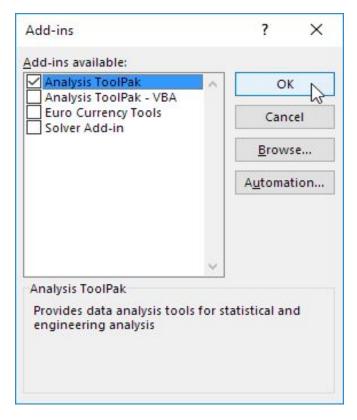
## Excel Data Analysis ToolPak

- If you need to develop complex statistical or engineering analyses, you can save steps and time by using the Analysis ToolPak.
- You provide the data and parameters for each analysis, and the tool uses the appropriate statistical or engineering macro functions to calculate and display the results in an output table. Some tools generate charts in addition to output tables.
- The Toolpak support the following analysis
  - ANOVA
  - Correlation
  - Covariance
  - Descriptive Statistics
  - Exponential Smoothing
  - F-Test
  - Fourier Analysis
  - Histogram
  - Moving Average
  - Rank and Percentile
  - Regression
  - Sampling
  - T-test
  - Z-test

# Install Excel Analysis ToolPak

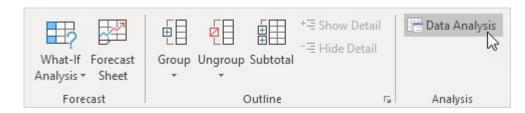
- Click the File tab, click Options, and then click the Add-Ins category.
- In the Manage box, select Excel Add-ins and then click Go.
- If you're using Excel for Mac, in the file menu go to Tools > Excel Add-ins.
- In the Add-Ins box, check the Analysis ToolPak check box, and then click OK



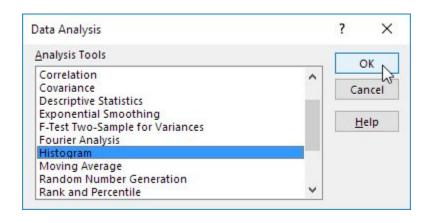


# Install Excel Analysis ToolPak

 On the Data tab, in the Analysis group, you can now click on Data Analysis.



 The following dialog box below appears. For example, select Histogram and click OK to create a Histogram in Excel.



# Topic 2 Sampling and Hypothesis Testing

# Sampling Theory

- Sampling theory is the field of statistics that is involved with the collection, analysis and interpretation of data gathered from random samples of a population under study.
- The application of sampling theory is concerned not only with the proper selection of observations from the population that will constitute the random sample
- It also involves the use of probability theory, along with prior knowledge about the population parameters, to analyze the data from the random sample and develop conclusions from the analysis.
- The normal distribution is most heavily utilized in developing the theoretical background for sampling theory.

#### Term Definitions

- A population is the collection of all members of a group
- A sample is a portion of the population selected for analysis
- A parameter is a numerical measure that describes a characteristic of a population
- A **statistic** is a numerical measure that describes a characteristic of a sample

## Sampling Distribution

- Parameters are usually unknown
- Use statistics to estimate parameters.
- The sampling distribution of a statistic is the probability distribution that specifies probabilities for the possible values the statistic can take.

# Sample Mean & Standard Deviation

- The sample mean is a statistics that varies from sample to sample. - statistics, while population mean is a fixed value parameter.
- The estimate of the sample mean and standard deviation is given below.
- Note that the n-1 instead of n in the sample standard deviation is to ensure an unbiased estimate of the popular standard deviation.

$$\overline{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{\sum x_i}{n}$$
  $s = \sqrt{\frac{\sum (x - \overline{x})^2}{n - 1}}$ 

# Example: Pumpkin Weights

 The population is the weight of six pumpkins (in pounds) displayed in a carnival "guess the weight" game booth.

Pumpkin	A	В	C	D	Е	F
Weight (in pounds)	19	14	15	9	10	17

Population Mean =(19+14+15+9+10+17)/6=14 pounds

 You are asked to guess the average weight of the six pumpkins by taking a random sample without replacement from the population.

## Example: Pumpkin Weights (sample size=2)

Sample	Weight	Sample mean
A, B	19, 14	16.5
A, C	19, 15	17.0
A, D	19, 9	14.0
A, E	19, 10	14.5
A, F	19, 17	18.0
B, C	14, 15	14.5
B, D	14, 9	11.5
B, E	14, 10	12
B, F	14, 17	15.5
C, D	15, 9	12
C, E	15, 10	12.5
C, F	15, 17	16
D, E	9, 10	9.5
D, F	9, 17	13
E, F	10, 17	13.5

- When using the sample mean to estimate the population mean, some possible error will be involved since sample mean is random.
- The chance that the sample mean is exactly the population mean is only 1/15.

## Example: Pumpkin Weights (sample size=5)

Sample	Weight	Sample mean
A,B,C,D,E	19,14,15,9,10	13.4
A,B,C,D,F	19,14,15,9,17	14.8
A,B,C,E,F	19,14,15,10,1 7	15.0
A,B,D,E,F	19,14,9,10,17	13.8
A,C,D,E,F	19,15,9,10,17	14.0
B,C,D,E,F	14,15,9,10,17	13.0

- The chance that the sample mean is exactly the population mean is only 1/6.
- The error with a sample of size 5 is on the average smaller than with a sample of size 2.

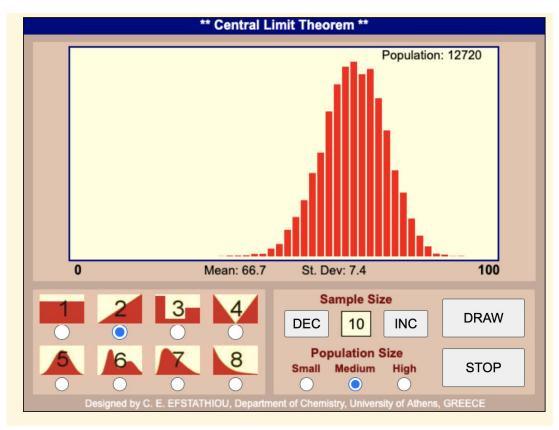
#### Central Limit Theorem

- For random sampling with a sample size n, the sampling distribution of the sample mean is approximately a normal distribution, no matter what the shape of the probability distribution from which the samples are taken.
- A rule of thumb for the sample size is more than 30. However, in most cases, sample size of 5 or more will work.
- The sample distribution standard deviation reduces with sample size.

# Activity: Central Limit Theorem

 Try out eight different distributions, try a sample size of 5, 10,20, and see the sample mean distribution

http://195.134.76.37/applets/AppletCentralLimit/Appl\_CentralLimit2.html

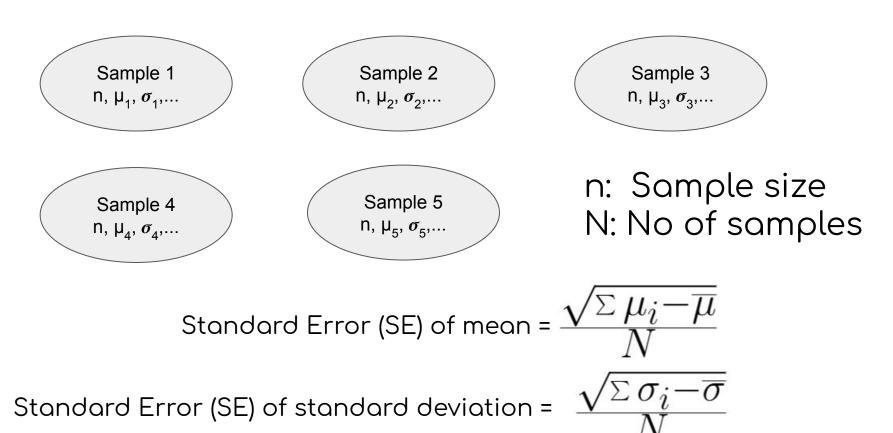


## Applications of CLT

- Central Limit Theorem is used in a number of statistical areas such as:
  - Standard Error
  - Confidence Interval
  - Hypothesis Testing
  - ANOVA

## Standard Error

 The standard error of a statistic is the standard deviation of the sampling distribution of that statistic (mean, standard deviation, mode, median,..)



## Estimate Standard Error

 It is common to estimate the standard error from just one sample. One method is to use bootstrapping method, another method is to compute the standard error based on Central Limit Theorem (CLT) as follows:

Step 1 The formula to find the sample mean

$$\mu_{x} = \frac{\sum_{i=1}^{n} x_{i}}{n}$$

Step 2 Formula to estimate sample standard deviation

$$s = \sqrt{\frac{\sum_{i=1}^{n} (x_i - \mu_x)^2}{n-1}}$$

Step 3 Formula to estimate standard error (SE) of mean

$$SE_{\mu_x} = \frac{s}{\sqrt{n}}$$

#### Standard Error in Excel

 Standard error in Excel can be computed as follows:

STDEV(sampling range)/SQRT(COUNT(sampling range)).

## Activity: Standard Error

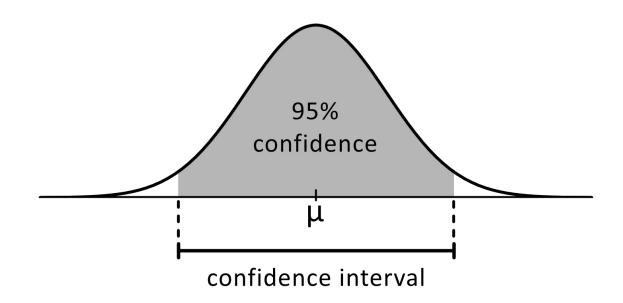
Consider the following three sets of observations:

- Set 1: 8,9,10,11,12
- Set 2: 8,9,10,11,100
- Set 3: 8,9,10,11,1000
- Use Excel to compute the above standard errors.
- Verify the standard errors using the following online tool.

<a href="https://ncalculators.com/statistics/standard-error-calculator.htm">https://ncalculators.com/statistics/standard-error-calculator.htm</a>

#### Confidence Interval

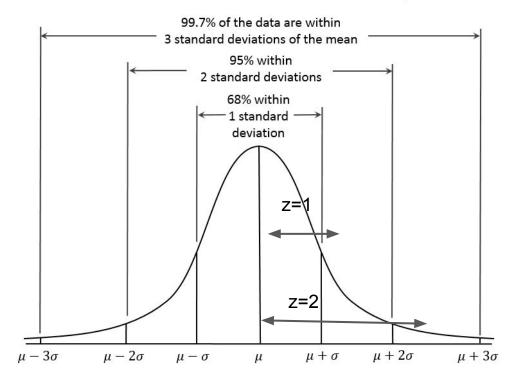
- A confidence Interval is a range of values we are fairly sure our true value lies in
- This is a number chosen to be close to 1, most commonly 0.95
- When the sampling distribution is approximately normal, a 95% confidence interval has margin of error equal to 1.96 standard errors



#### **Z-Score**

- The z-score for an observation is the number of standard deviations that it falls from the mean.
- The z-score is given by

$$z=rac{(x-\mu)}{\sigma}$$
 (population)  $z=rac{(\overline{x}-\mu)}{\sigma/\sqrt{N}}$  (sample)



## Activity: Z-Score

- Compute the z score (population) given
  - $\circ$  x = 154
  - $\circ$   $\mu = 100$
  - $\circ \sigma = 30$
- Compute the Z-score using Excel
- Verify your answer with the online Z-score calculator below

http://www.learningaboutelectronics.com/Articles/Z-score-calculator.php

## Confidence Interval with Z-Score

 The confidence interval for the population mean based on z-score, estimated from a sample for size n is:

$$\overline{x} \pm z \frac{\sigma}{\sqrt{N}}$$

Confidence level	interval calculation
50%	0.67449
75%	1.15035
90%	1.64485
95%	1.95996
97%	2.17009
99%	2.57583
99.9%	3.29053

Critical (7) value to be used in confidence

# Confidence Interval (Z-Score) in Excel

- The CONFIDENCE(alpha, sigma, n) function returns a value that you can use to construct a confidence interval for a population mean.
- The confidence interval is a range of values that are centered at a known sample mean.
- Observations in the sample are assumed to come from a normal distribution with known standard deviation, sigma, and the number of observations in the sample is n.
- The syntax is CONFIDENCE(alpha,sigma,n)

CONFIDENCE(A2,A3,A4)

Confidence interval for a population mean.

# Activity: Confidence Interval (Z-Score)

Suppose we know that the IQ scores of all incoming college freshman are normally distributed with standard deviation of 15. We have a simple random sample of 100 freshmen, and the mean IQ score for this sample is 120. Find a 90% confidence interval for the mean IQ score for the entire population of incoming college freshmen.

- Use Excel to compute the confidence interval
- Verify using the following confidence interval tools <u>https://www.mathsisfun.com/data/confidence-interval</u> -calculator.html

https://www.socscistatistics.com/confidenceinterval/default3.aspx

### Confidence Interval with T-Score

- You use the t score for small sample size (N<30), or unknown population standard deviation
- The t score is computed by

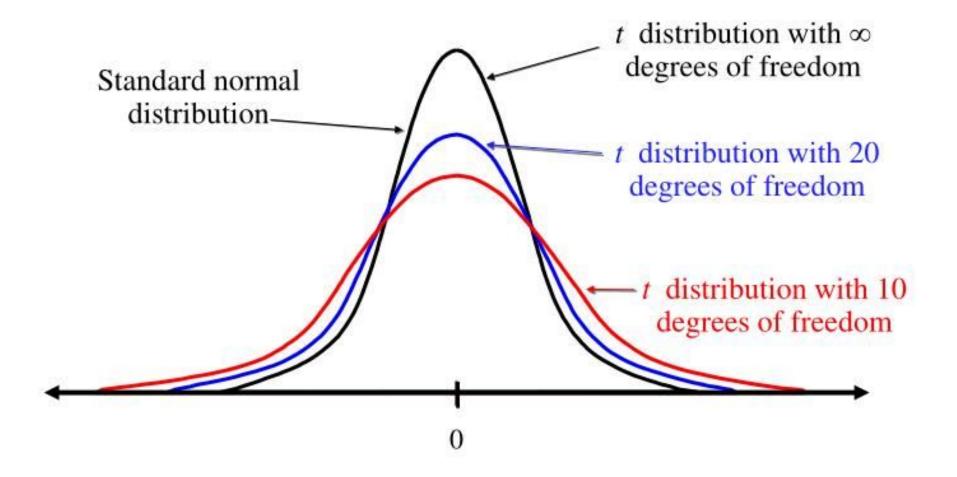
$$t = \frac{(\overline{x} - \mu)}{s/\sqrt{N}}$$

- Traditionally we look up a t values in a t-table. The number of items in your sample, minus one, is your degrees of freedom. For example, if you have 20 items in your sample, then df = 19.
- The confidence interval for the population mean based on t-score is:

$$\overline{x} \pm t \frac{s}{\sqrt{N}}$$

#### Student's t Distribution

The t-distribution is used when n is **small** and  $\sigma$  is **unknown**.



### Confidence Interval using T-score

Because the sample size is small, we need to use the t distribution. For 95% confidence and df = n-1 = 9, t = 2,262.

cum. prob	T_50	£.75	T.00	£.85	T.90	T.56	I.975	1.99	f .995	£ ,999	T.9996
one-tail	0.50	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.001	0.0005
two-tails	1.00	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002	0.001
df	525-23	5 (1957)	577-25520	20002000	Vermier	275/30	111/12/2000	200722	R##208/30	Nemanaka	61355.556
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
2 3	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22,327	31.599
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.000	0.727	0.920	1,156	1.476	2.015	2.571	3,365	4.032	5.893	6.869
6 7	0.000	0.718	0.906	1.134	1.440	1.943	2447	3.143	3.707	5.208	5.959
	0.000	0.711	0.896	1.119	1.415	1.895	2 365	2.998	3.499	4.785	5.408
8	0.000	0.706	0.889	1.108	1.397	1.860	2 208	2.896	3.355	4.501	5.041
9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	0.000	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3,169	4.144	4.587
11	0.000	0.697	0.876	1,088	1.363	1.796	2.201	2.718	3.108	4.025	4.437
12	0.000	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	0.000	0.694	0.870	1.079	1,350	1.771	2.160	2.650	3.012	3.852	4.221
14	0.000	0.692	0.868	1.076	1.345	1.761	2.145	2.824	2.977	3.787	4.140
15	0.000	0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	0.000	0.690	0.865	1.071	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	0.000	0.689	0.863	1.089	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	0.000	0.688	0.862	1.067	1,330	1.734	2.101	2.552	2.878	3.610	3.922
19	0.000	0.688	0.861	1.066	1.328	1.729	2.093	2.539	2.881	3.579	3.883
20	0.000	0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845	3.552	3.850
21	0.000	0.686	0.859	1.083	1.323	1.721	2.080	2.518	2.831	3.527	3.819
22	0.000	0.686	0.858	1.061	1.321	1.717	2.074	2.508	2.819	3.505	3.792

# Confidence Interval (T-Score) in Excel

 The CONFIDENCE.T function returns the confidence interval for a population mean, using a Student's t distribution

CONFIDENCE.T(0.05,1,50)

Confidence interval for the mean of a population based on a sample size of 50, with a 5% significance level and a standard deviation of 1. This is based on a Student's t-distribution.

### Activity: T Value

 Verify the T-value for 95% confidence for a sample size of 10 is consistent with the T-value table using the following online t-value tool

http://www.learningaboutelectronics.com/Articles/T-value-calculator.php

# Activity: Confidence Interval (T-Score)

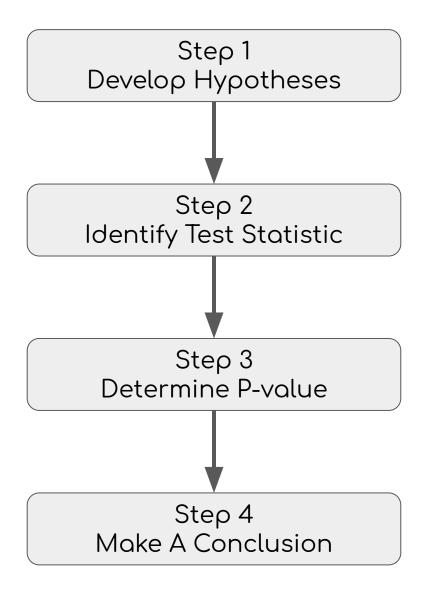
- We have a small random sample of 10 students from the IQ scores of all PSLE students. The mean IQ score for this sample is 120 and sample standard deviation is 15.
- Find a 90% confidence interval for the mean IQ score for the entire population of PSLE students.
- Use Excel to compute the confidence interval using T-Score.
- Verify using the following confidence interval tools based on t-score

https://www.socscistatistics.com/confidenceinterval/default2.aspx

# What is Hypothesis Testing

- A hypothesis is a statement about a population, usually of the form that a certain parameter takes a particular numerical value or falls in a certain range of values
- The main goal in many research studies is to check whether the data support certain hypotheses
- A hypothesis testing (significance test) is a method of using data to summarize the evidence about a hypothesis

# Steps of a Hypothesis Testing



### Step 1: Develop Hypotheses

Each significance test has two hypotheses:

- The null hypothesis states that
  - a parameter takes a particular value
  - a method has null effect (no effect)
- The alternative hypothesis states that
  - a parameter falls in some alternative range of values.
  - a method has better or worst effect
  - We usually set the hypothesis that one wants to conclude as the alternative hypothesis.

# Examples of Hypothesis

Null Hypothesis	Alternative Hypothesis
Age has no effect on mathematical ability.	Mathematical ability depends on age
Taking aspirin daily does not affect heart attack risk.	Taking aspirin daily does affect heart attack risk.
Age has no effect on how cell phones are used for internet access.	Usage of cell phones for internet access depends on age
There is no difference in pain relief after chewing willow bark versus taking a placebo.	There is a difference in pain relief for chewing willow bark versus taking a placebo.

# Step 2: Identify Test Statistic

- A test statistic describes how far that estimate (the sample statistic) falls from the parameter value given in the null hypothesis
- A test statistic is either z-score or t-score.
- In most cases, t-score is used as the sample size is small and the population variance is unknown.

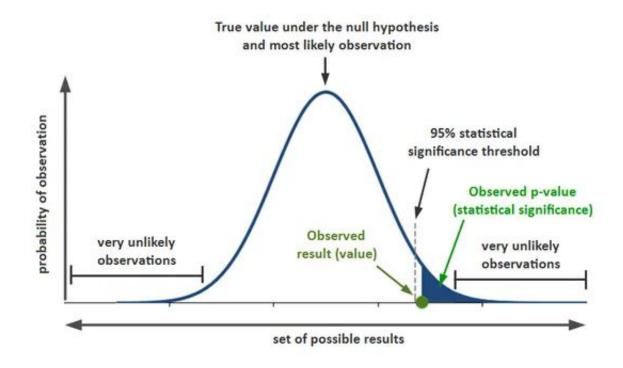
### Step 3: P-value for T Statistic

Sampling Distribution of Test Statistic The P-value is the probability that the test statistic equals the observed value or a value even more extreme P-value H<sub>∩</sub> value More Extreme Values Sample Value of Test Statistic

 The smaller the P-value, the stronger the evidence is against null hypothesis

# Significance Level

- The level of statistical significance is often expressed as a p-value between 0 and 1. The smaller the p-value, the stronger the evidence that you should reject the null hypothesis.
- A p-value less than 0.05 (typically ≤ 0.05) is statistically significant.



# Significance Level

Significant Level	Specification
ρ>0.05	Not Significant
ρ<=0.05 (5%)	Significant
ρ<=0.01 (1%)	Very Significant
ρ<=0.001 (0.1%)	Highly Significant

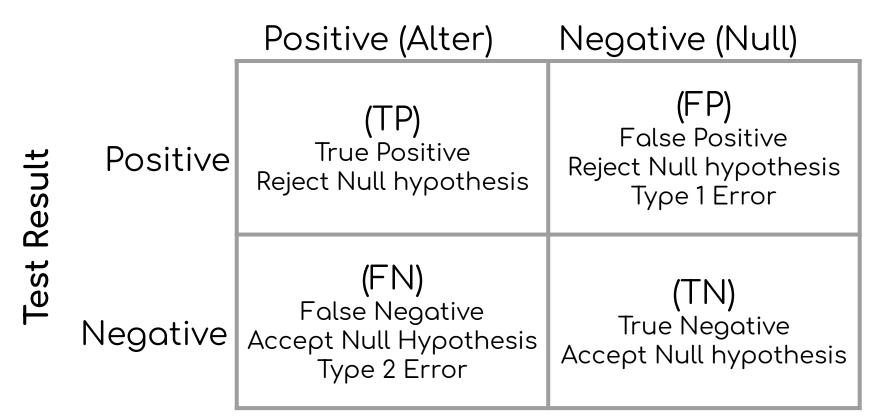
• In practice, the most common significance level is 0.05

### Step 4: Make Conclusion

- Compare P-value with significance Level
- If the P-value < significance level, then reject the null hypothesis and accept the alternative hypothesis.

# Type I and Type II Errors

**Actual Status** 



- Null Hypothesis => Negative
- Alternative Hypothesis => Positive

# Example of Type I and Type II Errors







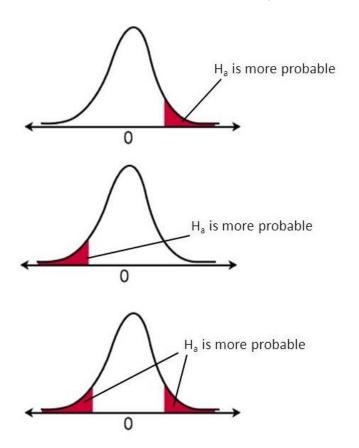


# Types of T-Tests

- One sample t-test: Compare a sample mean to a hypothetical mean
- One sample paired t-test: Compare the difference from the same sample before and after treatment.
- Two sample t-test: Compare two sample means from two population with equal variances.
- Two sample pooled variance t-test: Compare two sample means from two population with unequal variances.
- It is recommended to use a two sample t-test with unequal variance as we don't need to make assumption on the data

#### One Tail vs Two Tail T-Tests

- One tail t-test assumes the mean is higher or lower than a value.
- It is recommended to use a two tail test as we don't need to make assumption on the data



Right-tail test

 $H_a$ :  $\mu$  > value

Left-tail test

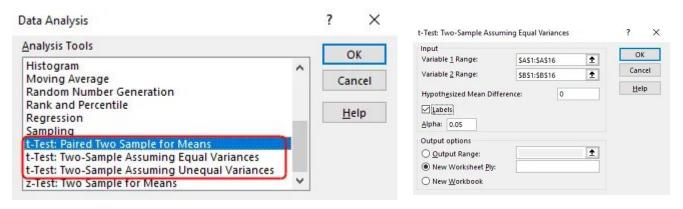
 $H_a$ :  $\mu$  < value

Two-tail test

 $H_a$ :  $\mu \neq value$ 

# Hypothesis Testing in Excel

- In Excel, click Data Analysis on the Data tab.
- From the Data Analysis popup, choose t-Test: Two-Sample Assuming Equal Variances.
- Under Input, select the ranges for both Variable 1 and Variable 2.
- In Hypothesized Mean Difference, you'll typically enter zero. This
  value is the null hypothesis value, which represents no effect. In this
  case, a mean difference of zero represents no difference between the
  two methods, which is no effect.
- Check the Labels checkbox if you have meaningful variables labels in row 1. This option helps make the output easier to interpret. Ensure that you include the label row in step #3.
- Excel uses a default Alpha value of 0.05, which is usually a good value. Alpha is the significance level. Change this value only when you have a specific reason for doing so.
- Click OK.



# Activity: One Sample Hypothesis Test

- We know that the national average (population) on the PSLE scoring system is 554 with a standard deviation of 99. Our sample of 90 students from ABC school had an average score of 568.
- Is the 14 point difference in averages enough to say that students in ABC school perform better than the national average at significance level 0.05?
- What is the ABC school average score is 590?
- Use Excel to perform hypothesis testing for one sample
- Verify using the one sample hypothesis testing below

http://www.learningaboutelectronics.com/Articles/Hypothesis-testing-calculator.php

#### One Sample Paired T-test

- If you are studying the same group of students (one sample) before and after taking a special GRE preparation session, you can use one sample paired t-test.
- You can use the following online for paired T-test <u>http://www.learningaboutelectronics.com/Articles/</u> <u>Paired-t-test-calculator.php</u>

### Two Samples T-test using Pooled Variance

 For two samples from two populations with different variances, the null hypothesis is given by:

$$H_o = \mu_1 - \mu_2$$

The test statistics is given by:

$$t = rac{ar{x}_1 - ar{x}_2}{s_p \sqrt{rac{1}{n_1} + rac{1}{n_2}}}$$

with degrees of freedom equal to  $n_1+n_2-2$ 

### Activity: Two Samples Hypothesis Test

 Do women tend to spend more time on housework than men? If so, how much more?

Housework Hours							
Gender	Sample Size	Mean	Standard Deviation				
Women	476	33.0	21.9				
Men	496	19.9	14.6				

- Use Excel to perform hypothesis testing for one sample
- You can use the following online tool for two samples hypothesis testing to analyze the above data

http://www.statskingdom.com/140MeanT2eq.html

### Activity: Two Samples Hypothesis Test

- Independent random samples of 17 students from JC 1 and 13 students from JC 2 yield the following grade points.
- Is there any difference in grade points between JC 1 and JC 2 students?

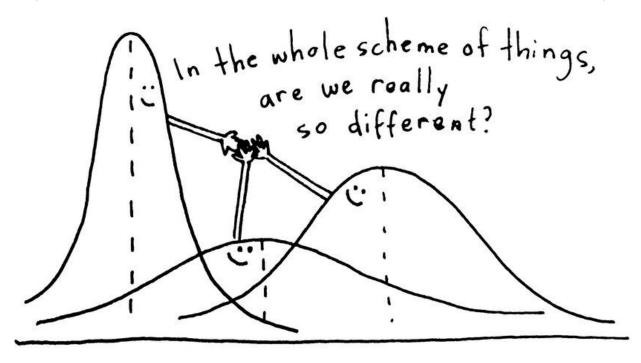
	JC 1		JC 2			
3.04	2.92	2.86	2.56	3.47	2.65	
1.71	3.60	3.49	2.77	3.26	3.00	
3.30	2.28	3.49	2.70	3.20	3.39	
2.88	2.82	2.13	3.00	3.19	2.58	
2.11	3.03	3.27	2.98			
2.60	3.13					

- Use Excel to perform hypothesis testing for one sample
- Verify with two samples hypothesis testing tool below

https://www.socscistatistics.com/tests/studentttest/default2.aspx https://ncalculators.com/statistics/t-test-calculator.htm http://www.learningaboutelectronics.com/Articles/Unpaired-t-test-calculator.php

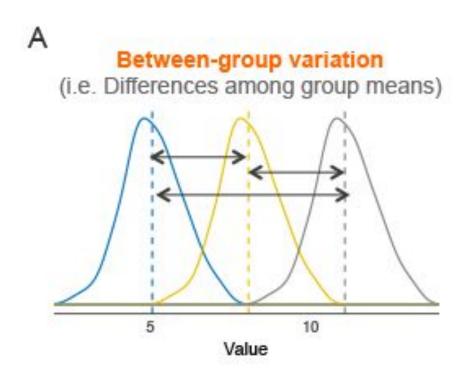
# Analysis of Variance (ANOVA)

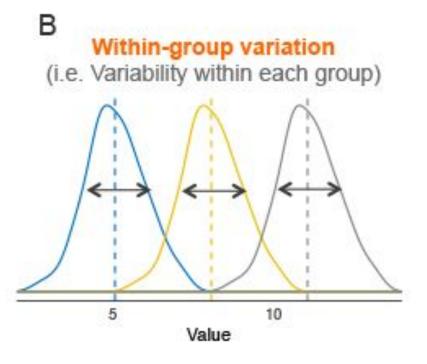
- Analysis of variance (ANOVA) is a statistical technique that is used to check if the means of two or more groups are significantly different from each other.
- ANOVA checks the impact of one or more factors by comparing the means of different samples



### Variability

- ANOVA takes into account between group variation and within group variation.
- Total variation = between-group variation + within-group variation.





# **ANOVA Hypothesis**

- Similar to t-test and chi-square test, ANOVA also uses a Null hypothesis and an Alternate hypothesis.
- The Null hypothesis in ANOVA is valid when all the sample means are equal, or they don't have any significant difference. Thus, they can be considered as a part of a larger set of the population.
- On the other hand, the alternate hypothesis is valid when at least one of the sample means is different from the rest of the sample means. In mathematical form, they can be represented as:

$$H_o: \mu_1 = \mu_2 = \cdots = \mu_L$$

Null hypothesis

 $H_1: \mu_l \neq \mu_m$ 

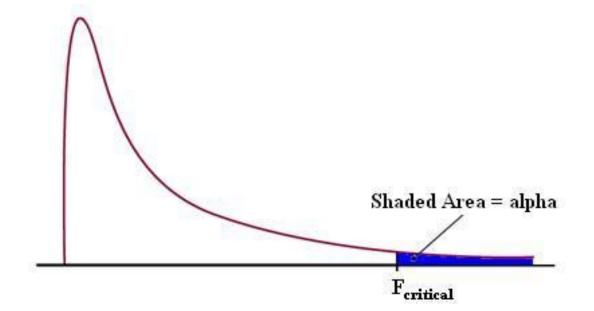
Alternate hypothesis

#### **F** Statistics

- The statistic which measures if the means of different samples are significantly different or not is called the F-Ratio.
- Lower the F-Ratio, more similar are the sample means. In that case, we cannot reject the null hypothesis.
- F = Between group variability / Within group variability
- The numerator term in the F-statistic calculation defines the between-group variability. As we read earlier, as between group variability increases, sample means grow further apart from each other. In other words, the samples are more probable to be belonging to totally different populations.

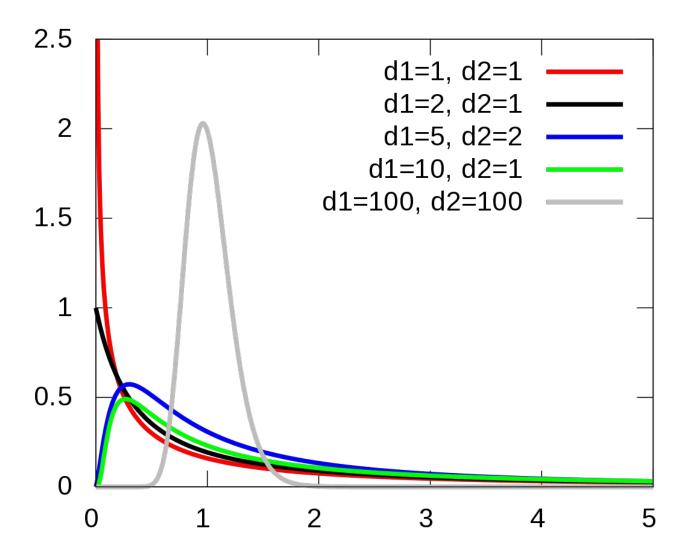
#### P Value for F-Statistic

- This F-statistic calculated here is compared with the F-critical value for making a conclusion.
- If the value of the calculated F-statistic is more than the F-critical value, then we reject the null hypothesis
- Alternatively, one can compute the p-value of F statistics. If the p
  value is less than the significance level, then we reject the null
  hypothesis.
- You can compute the critical F value from this online tool
- https://www.danielsoper.com/statcalc/calculator.aspx?id=4
- https://www.danielsoper.com/statcalc/calculator.aspx?id=7



#### F Distribution

 The F distribution is the probability distribution associated with the f statistic.



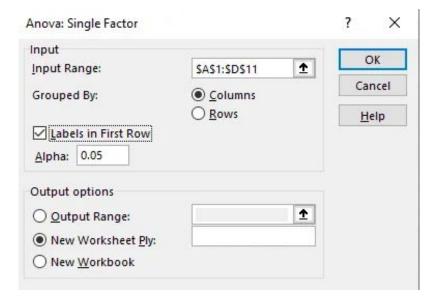
# One Way ANOVA

- The one-way ANOVA is used to determine whether there are any statistically significant differences between the means of three or more independent (unrelated) groups whilst considering only one independent variable or factor.
- Example of data for one-way ANOVA could be:

Detergent A	Detergent B	Detergent C	
15	18	10	
12	14	9	
10	18	7	
6	12	5	

# One Way ANOVA in Excel

- Click Data Analysis on the Data tab.
- From the Data Analysis popup, choose Anova: Single Factor.
- Under Input, select the ranges for all columns of data.
- In Grouped By, choose Columns.
- Check the Labels checkbox if you have meaningful variables labels in row 1. This option helps make the output easier to interpret. Ensure that you include the label row in step #3.
- Excel uses a default Alpha value of 0.05, which is usually a good value. Alpha is the significance level. Change this value only when you have a specific reason for doing so.
- Click OK.



Anova: Single Factor						
SUMMARY						
Groups	Count	Sum	Average	Variance		
Strength 1	10	112.0252	11.20252	3.978936		
Strength 2	10	89.37722	8.937722	8.881372		
Strength 3	10	106.8255	10.68255	1.215367		
Strength 4	10	88.37952	8.837952	3.531657		
ANOVA						
Source of Variation	SS	df	MS	F	P-value	F crit
Between Groups	43.61938	3	14.53979	3.303123	0.031054	2.866266
Within Groups	158.466	36	4.401833			
Total	202.0854	39			-	

# Activity: One Way ANOVA

 Test the hypothesis of whether there is any significant differences among the 3 shampoos below using one-way ANOVA test.

Shampoo A	Shampoo B	Shampoo C
36.6	17.5	15.0
39.2	20.6	10.4
30.4	18.7	18.9
37.1	25.7	10.5
34.1	22.0	15.2

 Use Excel to perform the one-way ANOVA and verify using the following online tool https://www.socscistatistics.com/tests/anova/defau lt2.aspx

#### How Variances is Calculated

Solution: 
$$\bar{x}_{1.} = \frac{36.6+39.2+30.4+37.1+34.1}{5} = 35.48, \ \bar{x}_{2.} = \frac{17.5+20.6+18.7+25.7+22.0}{5} = 20.9,$$
 $\bar{x}_{3.} = \frac{15.0+10.4+18.9+10.5+1.2}{5} = 14 \text{ and } \bar{x}_{..} = \frac{35.48+20.9+14}{3} = 23.46.$ 

SS(total) =  $\sum_{i=1}^{3} \sum_{j=1}^{5} (x_{ij} - \bar{x}_{..})^2 = (36.6 - 23.46)^2 + (39.2 - 23.46)^2 + ...$ 
 $+ (10.5 - 23.46)^2 + (15.2 - 23.46)^2 = 1340.456$ 

SS(within) =  $\sum_{i=1}^{3} \sum_{j=1}^{5} (x_{ij} - \bar{x}_{i.})^2 = (36.6 - 35.48)^2 + ... + (34.1 - 35.48)^2$ 
 $+ (17.5 - 20.9)^2 + ... + (22.0 - 20.9)^2 + (15.0 - 14)^2 + ... + (15.2 - 14)^2$ 
 $= 137.828$ 

SS(between) =  $\sum_{i=1}^{3} 5 \times (\bar{x}_{i.} - \bar{x}_{..})^2 = 5 \times ((35.48 - 23.46)^2 + (20.9 - 23.46)^2 + (14 - 23.46)^2$ 
 $= 1202.628$ 

SS: Sum of Squares = Variance SS(total) = SS(within)+SS(between)

#### **ANOVA Table**

#### ANOVA table:

Source	Sum of Squares	Degree of Freedom	Mean Square	F value
Between	1202.628	2	601.314	52.35
Within	137.828	12	11.486	
Total	1340.456	14		

MS: Mean Squares = Sum of Squares/DF F = MS(Between)/MS(Within)

#### Two Way ANOVA

- The two-way ANOVA compares the mean differences between groups that have been split on two independent variables (called factors).
- The primary purpose of a two-way ANOVA is to understand if there
  is an interaction between the two independent variables on the
  dependent variable.
- For example, you could use a two-way ANOVA to understand whether there is an interaction between gender and drug level on anxiety amongst patients, where gender (males/females) and drug level (1,2,3)

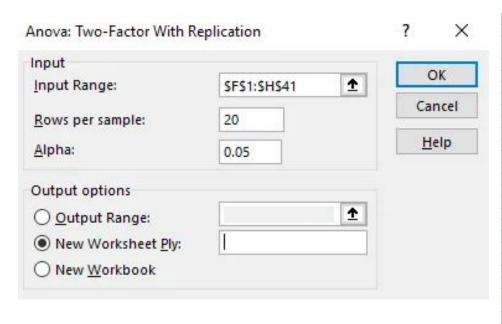
Patents	Drug 1	Drug 2	Drug 3
Male	8	10	8
	4	8	6
	0	6	4
Female	14	4	15
	10	2	12
	6	0	9

#### Hypotheses for Two Way ANOVA

- Because the two-way ANOVA consider the effect of two categorical factors, and the effect of the categorical factors on each other, there are three pairs of null or alternative hypotheses for the two-way ANOVA. For example
- H0: The means of all drug levels are equal
- H1: The mean of at least drug level is different
- H0: The means of the gender groups are equal
- H1: The means of the gender groups are different
- H0: There is no interaction between the drug level and gender
- H1: There is interaction between the drug level and gender

#### Two Way ANOVA in Excel

- Click Data Analysis on the Data tab.
- From the Data Analysis popup, choose Anova: Two-Factor With Replication.
- Under Input, select the ranges for all columns of data.
- In Rows per sample, enter 20. This represents the number of observations per group.
- Excel uses a default Alpha value of 0.05, which is usually a good value. Alpha is the significance level. Change this value only when you have a specific reason for doing so.
- Click OK.



SUMMARY	Mustard	Chocolate Sa	Total			
Hot Dog						
Count	20	20	40			
Sum	1792.113744	1306.332238	3098.445982			
Average	89.6056872	65.3166119	77.46114955			
Variance	35.16069842	28.69639811	182.3814518			
Ice Cream						
Count	20	20	40			
Sum	1226.178267	1860.961921	3087.140187			
Average	61.30891335	93.04809603	77.17850469			
Variance	17.11820778	19.29296334	276.0402416			
Total						
Count	40	40				
Sum	3018.292011	3167.294159				
Average	75.45730027	79.18235396				
Variance	230.7788031	220.5679484				
ANOVA						
Source of Variation	SS	df	MS	F	P-value	F crit
Sample (Food)	1.597762351	1	1.597762351	0.063739502	0.801361808	3.966759784
Columns (Condiment)	277.5205002	1	277.5205002	11.07111978	0.001353292	3.966759784
Interaction	15695.82846	1	15695.82846	626.1533715	1.95348E-38	3.966759784
Within	1905.097085	76	25.06706691			
Total	17880.04381	79				

#### Activity: Two Way ANOVA

- A physiologist was interested in learning whether smoking history and different types of stress tests influence the timing of a subject's maximum oxygen uptake, as measured in minutes.
- The researcher classified a subject's smoking history as either heavy smoking, moderate smoking, or non-smoking. He was interested in seeing the effects of three different types of stress tests a test performed on a bicycle, a test on a treadmill, and a test on steps.
- The physiologist recruited 9 non-smokers, 9 moderate smokers, and 9 heavy smokers to participate in his experiment, for a total of n = 27 subjects.
- He then randomly assigned each of his recruited subjects to undergo one of the three types of stress test

#### Activity: Two Way ANOVA

Here are his resulting data:

Sample History	Bicycle	Treadmill	Step Test
Non Smoker	12.8	16.2	22.6
	13.5	18.1	19.3
	11.2	17.8	18.9
Moderate Smoker	10.9	15.5	20.1
	11.1	13.8	21
	9.8	16.2	15.9
Heavy Smoker	8.7	14.7	16.2
	9.2	13.2	16.1
	7.5	8.1	17.8

 Use Excel to perform the two-way ANOVA and verify using the following online tool http://vassarstats.net/anova2u.html

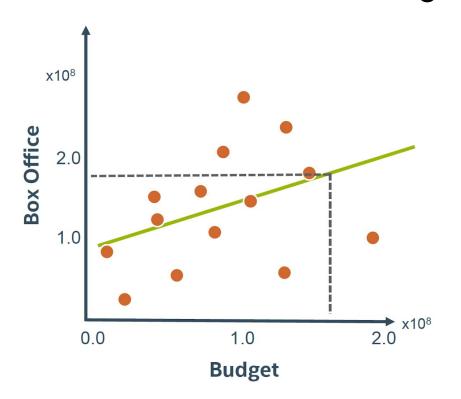
#### One Way vs Two Way ANOVA

- A one-way ANOVA is primarily designed to enable the equality testing between three or more means. A two-way ANOVA is designed to assess the interrelationship of two independent variables on a dependent variable.
- A one-way ANOVA only involves one factor or independent variable, whereas there are two independent variables in a two-way ANOVA.
- In a one-way ANOVA, the one factor or independent variable analyzed has three or more categorical groups. A two-way ANOVA instead compares multiple groups of two factors.
- One-way ANOVA need to satisfy only two principles of design of experiments, i.e. replication and randomization. As opposed to Two-way ANOVA, which meets all three principles of design of experiments which are replication, randomization, and local control.

# Topic 3 Regression and Correlation Analysis

#### Linear Regression

- Linear regression is the most common regression model. Many predictive models use linear regression models
- You can use a linear regression model to predict the box office from the budget.



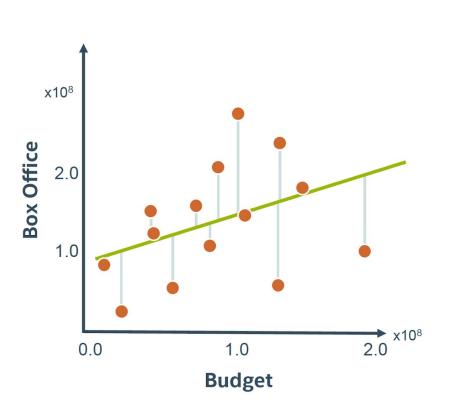
$$y_{\beta}(x) = \beta_0 + \beta_1 x$$

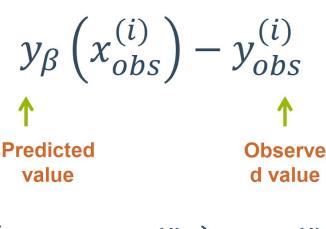
 $\beta_0$  = 80 million,  $\beta_1$  = 0.6

Predict 175 Million Gross for 160 Million Budget

#### Residues

Residue is the difference between the predicted value and actual value

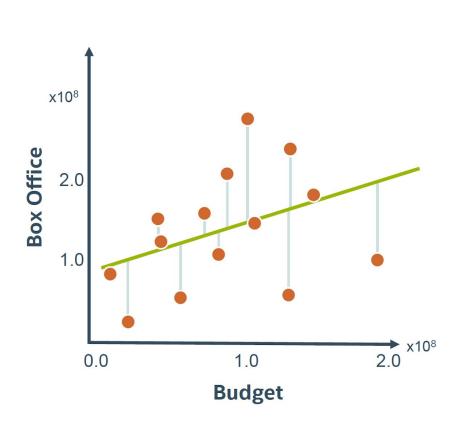




$$\left(\beta_0 + \beta_1 x_{obs}^{(i)}\right) - y_{obs}^{(i)}$$

#### Mean Square Error

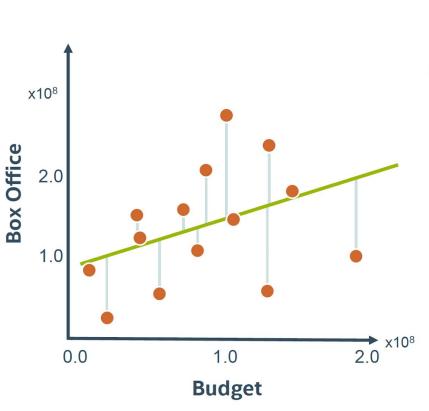
 Mean Square Error (MSE) is the common loss function to measure how good is the linear regression model.



$$\frac{1}{m} \sum_{i=1}^{m} \left( \left( \beta_0 + \beta_1 x_{obs}^{(i)} \right) - y_{obs}^{(i)} \right)^2$$

#### Minimum Mean Square Error

 Regression aims to minimize the MSE to find the best linear regression model.

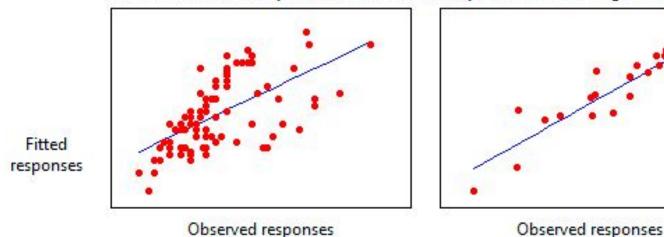


$$\min_{\beta_0,\beta_1} \frac{1}{m} \sum_{i=1}^{m} \left( \left( \beta_0 + \beta_1 x_{obs}^{(i)} \right) - y_{obs}^{(i)} \right)^2$$

#### R Square (Goodness Of Fit)

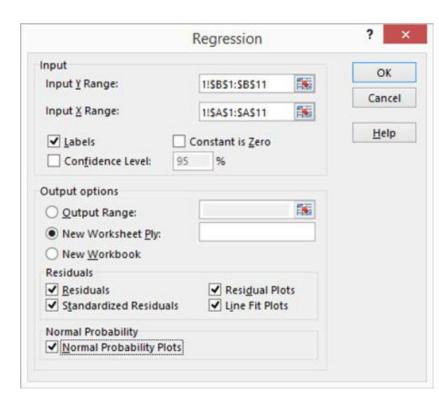
- R-squared is a statistical measure of how close the data are to the fitted regression line.
- R-squared = Explained variation / Total variation
- R-squared is always between 0 and 1
  - 0 indicates that the model explains none of the variability of the response data around its mean.
  - 1 indicates that the model explains all the variability of the response data around its mean.

#### Plots of Observed Responses Versus Fitted Responses for Two Regression Models



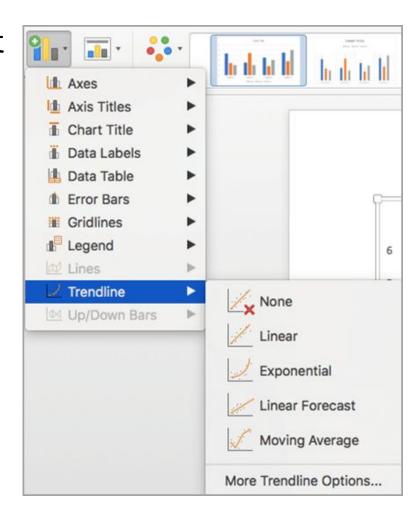
#### Regression in Excel

- When Excel displays the Data Analysis dialog box, select the Regression tool from the Analysis Tools list and then click OK.
- Identify your Y and X values.
- Select a location for the regression analysis results.
- Identify what data you want returned.
- Click OK.



#### Add Trend Line in Excel

- On the View menu, click Print Layout.
- In the chart, select the data series that you want to add a trendline to, and then click the Chart Design tab.
- On the Chart Design tab, click Add Chart Element, and then click Trendline.
- Choose a trendline option or click More Trendline Options.



#### Activity: Regression

- The data are collected at the end of an introductory statistics course. The table shows the data for the eight males in the class on these variables and on the number of class lectures for the course that the student reported skipping during the term.
- Investigate the relationship between x=study time and y=GPA. Find the prediction equation and interpret the slope.
- Use Excel to do a regression and verify using the the following one tool <a href="https://www.graphpad.com/quickcalcs/linear1/">https://www.graphpad.com/quickcalcs/linear1/</a>

Student	Study Time	Grade Point
1	14	2.8
2	25	3.6
3	15	3.4
4	5	3.0
5	10	3.1
6	12	3.3
7	5	2.7
8	21	3.8

#### What is Covariance

- Variance is a measure of the variability or spread in a set of data
- We use the following formula to compute variance for population and sample respectively.

$$Var(x) = \frac{\sum (x - \overline{x})^2}{N}$$
  $Var(x) = \frac{\sum (x - \overline{x})^2}{N - 1}$ 

- Covariance is a measure of the extent to which corresponding elements from two sets of ordered data move in the same direction.
- We use the following formula to compute covariance for population and sample respectively

$$Cov(x,y) = \frac{\sum (x-\overline{x})(y-\overline{y})}{N}$$
  $Cov(x,y) = \frac{\sum (x-\overline{x})(y-\overline{y})}{N-1}$ 

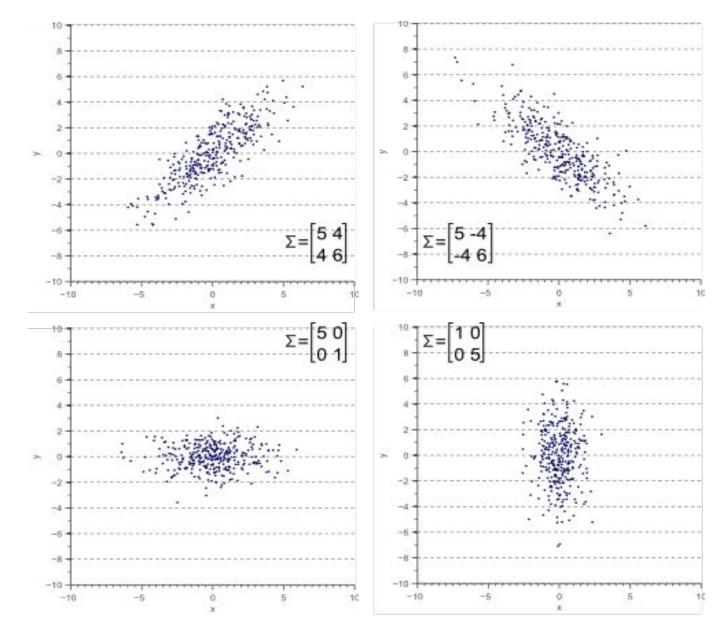
#### Covariance Matrix

 Variance and covariance are often displayed together in a covariance matrix given as follows:

$$Cov(A) = \begin{bmatrix} \frac{\sum (x_i - \overline{X})(x_i - \overline{X})}{N} & \frac{\sum (x_i - \overline{X})(y_i - \overline{Y})}{N} \\ \frac{\sum (x_i - \overline{X})(y_i - \overline{Y})}{N} & \frac{\sum (y_i - \overline{Y})(y_i - \overline{Y})}{N} \end{bmatrix}$$

$$= \begin{bmatrix} Cov(X, X) & Cov(Y, X) \\ Cov(X, Y) & Cov(Y, Y) \end{bmatrix}$$

#### Covariance Matrix Visualization



#### COVARIANCE.P function in Excel

- The COVARIANCE.P function returns population covariance, the average of the products of deviations for each data point pair in two data sets. Use covariance to determine the relationship between two data sets.
- For example, you can examine whether greater income accompanies greater levels of education.

COVARIANCE.P(A2:A6,
B2:B6)

Covariance, the average of the products of deviations for each data point pair above

#### Activity: Covariance

Compute the covariance for the following data

X: 90,90,60,60,30

Y: 60,90,60,60,30

- Use Excel to compute the covariance
- Verify the answer using the online covariance calculator

https://www.calculatored.com/math/algebra/covariance-calculator

#### What is Correlation

- The correlation coefficient is also known as the Pearson product-moment correlation coefficient, or Pearson's correlation coefficient.
- It is obtained by dividing the covariance of the two variables by the product of their standard deviations.

$$Corr(x,y) = \frac{Cov(x,y)}{\sigma_x \sigma_y}$$

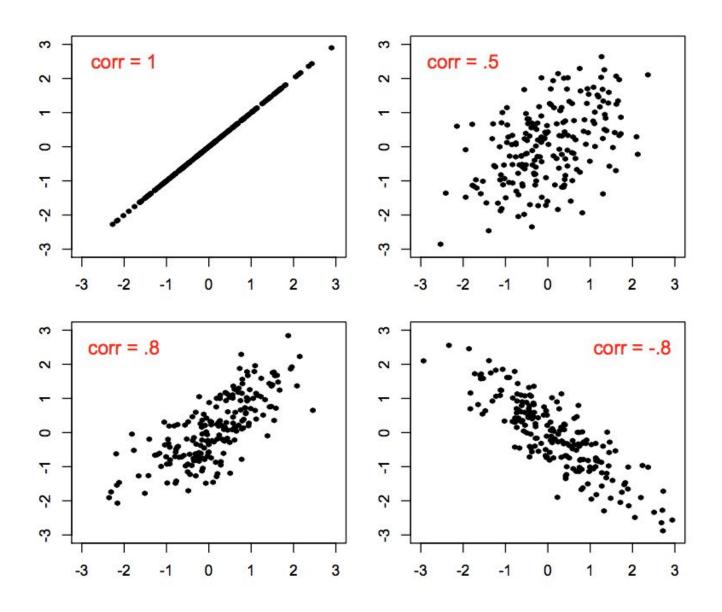
- The values of the correlation coefficient can range from -1 to +1. The closer it is to +1 or -1, the more closely are the two variables are related.
- The positive sign signifies the direction of the correlation i.e. if one
  of the variables increases, the other variable is also supposed to
  increase.

#### **Correlation Matrix**

 For multiple variables, we can display all the correlation coefficients in the matrix form as below:

```
\begin{bmatrix} 1 & Corr(X,Y) & Corr(X,Z) \\ Corr(X,Y) & 1 & Corr(Y,Z) \\ Corr(X,Z) & Corr(Y,Z) & 1 \end{bmatrix}
```

#### Correlation Coefficient



#### CORREL function in Excel

- The CORREL function returns the correlation coefficient of two cell ranges. Use the correlation coefficient to determine the relationship between two properties.
- For example, you can examine the relationship between a location's average temperature and the use of air conditioners.

Correlation coefficient of the two data sets in columns A and B.

#### **Activity: Correlation**

Compute the Pearson correlation coefficient for the following data

X: 90,90,60,60,30

Y: 60,90,60,60,30

Use Excel to compute the correlation and verify using the online covariance calculator

https://www.socscistatistics.com/tests/pearson/def ault2.aspx

# Summary Q&A

Practice Makes Perfect

### Final Assessment

#### Written Assessment (PP)

This is a Written Assessment (PP)

Duration: 60 mins

- 1. The assessor will pass the practical problems in hardcopy to you.
- 2. This is an open book exam that must be completed individually.

#### Submission Procedure:

1. After completion, please pass the hardcopy to the assessor

## Course Feedback https://goo.gl/R2eumq



#### TRAQOM Survey

- You will receive a TRAQOM link after the class.
- Please submit TRAQOM feedback and survey after the class.



### Thank You!

Dr. Alfred Ang

Tel: 96983731

Email: <a href="mailto:angch@tertiaryinfotech.com">angch@tertiaryinfotech.com</a>

Facebook: <a href="https://www.facebook.com/angchewhoe">https://www.facebook.com/angchewhoe</a>

Linkedin: https://www.linkedin.com/in/angchewhoe/