Model Comparison

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Task 1: Conceptual Questions

- **What is the purpose of using cross-validation when fitting a random forest model?**

  Cross-validation is used to estimate how well the random forest will perform on unseen data by repeatedly splitting the data into "folds," training on some folds and validating on the others. This helps guard against overfitting and provides a more reliable measure of out-of-sample predictive accuracy.

- **Describe the bagged tree algorithm.**

  Bagged trees (bootstrap aggregating) build many decision trees on different bootstrap samples of the training data and then average (for regression) or majority-vote (for classification) their predictions. By aggregating across models trained on varied subsets, bagging reduces variance and improves stability compared to a single decision tree.

- **What is meant by a general linear model?**

  A general linear model (GLM) expresses a continuous response variable (Y) as a linear combination of predictors where epsilon is assumed to be normally distributed with constant variance. It encompasses methods like ANOVA, ANCOVA, and multiple linear regression.

- **When fitting a multiple linear regression model, what does adding an interaction term do? That is, what does it allow the model to do differently as compared to when it is not included in the model?**

  An interaction term allows the effect of one predictor on the response to change depending on the level of the other predictor. Without interactions the model assumes additive effects; with interactions it can capture non-additive relationships, where the slope for (X_1) varies by the value of (X_2).

- **Why do we split our data into a training and test set?**

  Splitting data ensures that we can train the model on one subset (training set) and then evaluate its performance on completely unseen data (test set). This provides an unbiased assessment of how well the model generalizes to new observations and helps detect overfitting.

Task 2: Data Prep

Packages and Data

```
library(tidyverse)
library(tidymodels)
library(caret)
library(yardstick)
library(glmnet)

Heart_data <- read_csv(
  "heart.csv")
summary(Heart_data)
```

```
      Age            Sex            ChestPainType        RestingBP
 Min.   :28.00   Length:918         Length:918         Min.   :  0.0
 1st Qu.:47.00   Class :character   Class :character   1st Qu.:120.0
 Median :54.00   Mode  :character   Mode  :character   Median :130.0
 Mean   :53.51                                         Mean   :132.4
 3rd Qu.:60.00                                         3rd Qu.:140.0
 Max.   :77.00                                         Max.   :200.0
  Cholesterol      FastingBS       RestingECG            MaxHR
 Min.   :  0.0   Min.   :0.0000   Length:918         Min.   : 60.0
 1st Qu.:173.2   1st Qu.:0.0000   Class :character   1st Qu.:120.0
 Median :223.0   Median :0.0000   Mode  :character   Median :138.0
 Mean   :198.8   Mean   :0.2331                      Mean   :136.8
 3rd Qu.:267.0   3rd Qu.:0.0000                      3rd Qu.:156.0
 Max.   :603.0   Max.   :1.0000                      Max.   :202.0
 ExerciseAngina       Oldpeak          ST_Slope          HeartDisease
 Length:918         Min.   :-2.6000   Length:918         Min.   :0.0000
 Class :character   1st Qu.: 0.0000   Class :character   1st Qu.:0.0000
 Mode  :character   Median : 0.6000   Mode  :character   Median :1.0000
                    Mean   : 0.8874                      Mean   :0.5534
                    3rd Qu.: 1.5000                      3rd Qu.:1.0000
```

```
Max.   : 6.2000                       Max.   :1.0000
```

Question 1:

Heart Disease is treated as a quantitative variable which does not make sense. Conceptually, Heart Disease is a categorical variable since 0 means no heart disease and 1 means presence of heart disease. A decimal like 0.5 wouldn't fall into either category. A person either has or does not have heart disease (1 or 0).

Question 2:

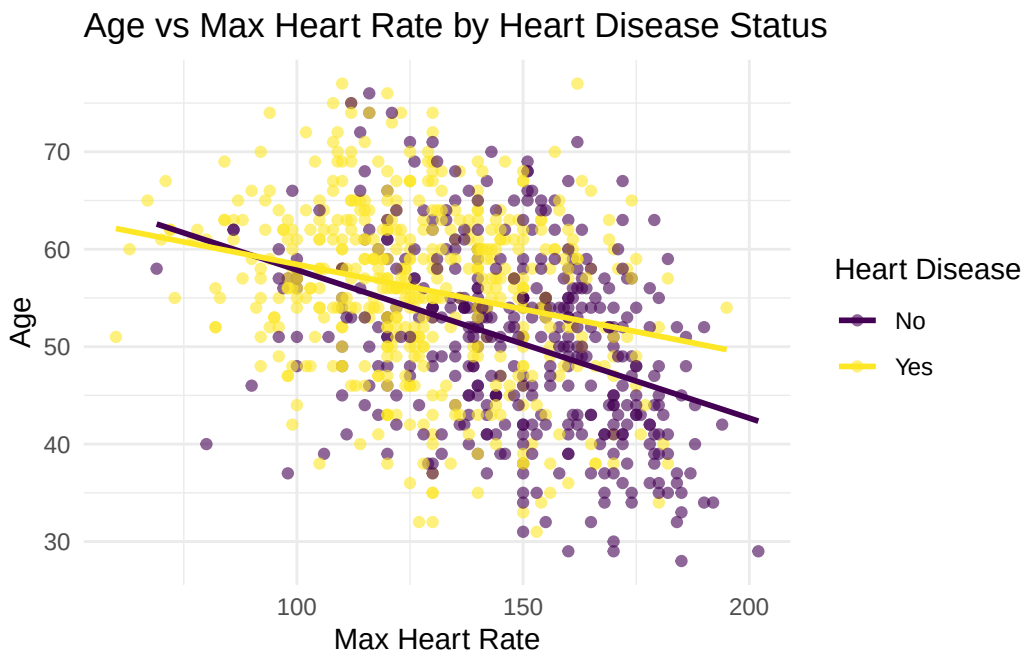
```
new_heart <- Heart_data %>%
  mutate(Heart_Disease = factor(HeartDisease, levels = c(0, 1), labels = c("No", "Yes"))) %>%
  select(-ST_Slope, -HeartDisease)
```

Task 3: EDA

1. Plot to check for interaction

```
ggplot(new_heart, aes(x = MaxHR, y = Age, color = Heart_Disease)) +
  geom_point(alpha = 0.6) +
  geom_smooth(method = "lm", se = FALSE) +
  scale_color_viridis_d(option = "D") +
  labs(
    title = "Age vs Max Heart Rate by Heart Disease Status",
    x = "Max Heart Rate",
    y = "Age",
    color = "Heart Disease"
  ) +
  theme_minimal()
```

```
`geom_smooth()` using formula = 'y ~ x'
```



2. Conclusion based on visual evidence

We can see that the slopes are different. An additive model would assume their slopes to be the same. Therefore, to account for different slopes, we need to use an interaction model.

Task 4: Testing and Training

```
set.seed(101)
split <- initial_split(new_heart, prop = 0.8)
train <- training(split)
test <- testing(split)
```

Task 5: OLS and LASSO

1. Interaction model

```
ols_mlr <- lm(Age ~ MaxHR * Heart_Disease, data = train)
summary(ols_mlr)
```

```
Call:
lm(formula = Age ~ MaxHR * Heart_Disease, data = train)

Residuals:
     Min       1Q   Median       3Q      Max
-22.7703  -5.7966   0.4516   5.7772  20.6378

Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
(Intercept)            75.58896    3.07510  24.581  < 2e-16 ***
MaxHR                  -0.16992    0.02064  -8.233 8.43e-16 ***
Heart_DiseaseYes       -8.58502    3.83433  -2.239  0.02546 *
MaxHR:Heart_DiseaseYes  0.08343    0.02716   3.072  0.00221 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 8.478 on 730 degrees of freedom
Multiple R-squared:  0.1839,    Adjusted R-squared:  0.1806
F-statistic: 54.84 on 3 and 730 DF,  p-value: < 2.2e-16
```

2. RMSE

```
predictions <- predict(ols_mlr, newdata = test)
residuals <- test$Age - predictions
OLS_rmse <- sqrt(mean(residuals^2))
OLS_rmse
```

```
[1] 9.100206
```

3. Performance

```
LASSO_recipe <- recipe(Age ~ MaxHR + Heart_Disease, data = train) %>%
  step_dummy(Heart_Disease) %>%
  step_normalize(all_predictors()) %>%       # Standardize all predictors
  step_interact( ~ MaxHR:starts_with("Heart_Disease_") )  # Add interaction terms
LASSO_recipe
```

```
-- Recipe ----------------------------------------------------------------------



-- Inputs

Number of variables by role

outcome:   1
predictor: 2



-- Operations

* Dummy variables from: Heart_Disease

* Centering and scaling for: all_predictors()

* Interactions with: MaxHR:starts_with("Heart_Disease_")
```

4. Spec, Grid, Results

```r
LASSO_spec <- linear_reg(penalty = tune(), mixture = 1) %>%
  set_engine("glmnet")
cv_folds <- vfold_cv(train, v = 10)

LASSO_wf <- workflow() %>%
  add_model(LASSO_spec) %>%
  add_recipe(LASSO_recipe)

lasso_grid <- grid_regular(penalty(), levels = 200)

LASSO_results <- tune_grid(
  LASSO_wf,
  resamples = cv_folds,
  grid = lasso_grid,
  metrics = metric_set(rmse)
```

```
)

best_LASSO <- select_best(LASSO_results, metric = "rmse")
best_LASSO
```

```
# A tibble: 1 x 2
       penalty .config
         <dbl> <chr>
1 0.0000000001 Preprocessor1_Model001
```

```
final_lasso_wf <- finalize_workflow(LASSO_wf, best_LASSO)
final_lasso_fit <- fit(final_lasso_wf, data = train)
tidy(final_lasso_fit)
```

```
# A tibble: 4 x 3
  term                      estimate      penalty
  <chr>                        <dbl>        <dbl>
1 (Intercept)                  54.0  0.0000000001
2 MaxHR                        -3.08 0.0000000001
3 Heart_Disease_Yes             1.36 0.0000000001
4 MaxHR_x_Heart_Disease_Yes     1.03 0.0000000001
```

5. RMSE

I would expect the RMSE to be very similar since the LASSO applied very little penalty (1e-10) and the same variables were used. The scale is different (ie our intercept is only 54) since we normalized the variables, but that won't change the RMSE.

```
# Get LASSO predictions
lasso_preds <- predict(final_lasso_fit, new_data = test) %>%
  bind_cols(test)

# Compute RMSE
rmse_lasso <- rmse(lasso_preds, truth = Age, estimate = .pred)
rmse_lasso
```

```
# A tibble: 1 x 3
  .metric .estimator .estimate
  <chr>   <chr>          <dbl>
1 rmse    standard        9.10
```

6. Compare RMSE

We can see that both models have similar RMSE.

```
rmse_lasso
```

```
# A tibble: 1 x 3
  .metric .estimator .estimate
  <chr>   <chr>          <dbl>
1 rmse    standard        9.10
```

```
OLS_rmse
```

```
[1] 9.100206
```

7. Why are they same even though we have different coefficient?

As stated, we standardized our variables in the LASSO model, which makes the coefficients look different. However, we use the same variables and interactions, so they are making very similar predictions. Thus, our RMSE is nearly the same.

Task 6: Logistic Regression