

## Make graphs

Trevor Burgoyne 13 Nov 2022

```
function [avg_hss, var_hss, avg_kt, var_kt, kphat, kdhat, kp, kd] = make_graphs(ROOT_DIR, PREFIX, DISP_NAME, LABEL_NAME, N_TESTS, N_RUNS, masses)
    COLORS = ["red", "blue", "green", "black"];
    T_START = 20; % s
    T_STEADY = 30; % s, Chosen as start of steady-state response from observation
    T_END = T_START+25; % s
    HREF = 1.25; % m
    g = 9.81; % m/s^2

    % Plotting options
    font_size = 12;
    line_size = 15;
    line_width = 1;
    avg_hss = zeros(1,N_TESTS);
    var_hss = zeros(1,N_TESTS);
    avg_kt = zeros(1,N_TESTS);
    var_kt = zeros(1,N_TESTS);
    kphat = zeros(1,N_TESTS);
    kdhat = zeros(1,N_TESTS);
    kp = zeros(1,N_TESTS);
    kd = zeros(1,N_TESTS);
    for test_n=1:N_TESTS
        ts = zeros(1,N_RUNS);
        kt = zeros(1,N_RUNS);
        hss = zeros(1,N_RUNS);
        zs = zeros(1,N_RUNS);
        figure(test_n)
        hold on
        for run_n=1:N_RUNS
            % Load data
            path = ROOT_DIR + PREFIX + test_n;
            if N_RUNS > 1 % Add runs suffix if more than one run was done
                path = path + "R" + run_n;
            end
            path = path + ".mat";
            load(path);

            if run_n == 1 % Only plot reference once
                plot(time,-z_ref,'Linewidth',line_width,'Color',COLORS(4),'DisplayName','z_{ref}');
            end
            plot(time,-z_est,'Linewidth',line_width,'Color',COLORS(run_n),'DisplayName',LABEL_NAME + " " + run_n);

            % Steady-state error
            idxs = find(time >= T_STEADY & time <=T_END); % Indices of steady state region
            z_arr = -z_est(idxs); % Z values being investigated
            zs(run_n) = double(mean(z_arr)); % m, Experimental settling value
            hss(run_n) = zs(run_n) - HREF; % m, Steady state error

            % Settling time
            idxs = find(time >= T_START & time <=T_END); % Idxs of investigated response
            start_idx = idxs(1);
            z_arr = -z_est(idxs); % Z values being investigated

            % Find last time z dipped below 95% of z_settle
            ts_idx = find(z_arr <= 0.95*zs(run_n));
            if isempty(ts_idx)
                ts1 = 0;
            else
                ts1 = time(ts_idx(end) + start_idx);
            end

            % Find last time z rose above 105% of z_settle
            ts_idx = find(z_arr >= 1.05*zs(run_n));
            if isempty(ts_idx)
                ts2 = 0;
            else
                ts2 = time(ts_idx(end) + start_idx);
            end

            ts(run_n) = max(ts1,ts2); % s, Settling time (use the later time)

            % Kt calculation
```

```

motors = abs([motor1' motor2' motor3' motor4']); % Get all motor values
u = mean(motors);
kt(run_n) = (masses(test_n)*g) / (4*u) * 1000; % N

end

scale = [1.05 0.95]; % scalar values used to position text
for run_n=1:N_RUNS
    % Steady-state error
    if zs(run_n) == max(zs) % Position labels above if the line is higher
        y = scale(1);
    else
        y = scale(2);
    end
    line_name = "h_{ss} = " + hss(run_n);
    text(T_STEADY,y*zs(run_n),line_name,'Color',COLORS(run_n))
    yline(zs(run_n),"--",'Linewidth',line_width,'Color',COLORS(run_n),'HandleVisibility','off')

    % Settling time
    if ts(run_n) == max(ts) % Position labels above if the line is higher
        y = scale(1);
    else
        y = scale(2);
    end
    line_name = "ts = " + (ts(run_n)-T_START);
    text(1.01*max(ts),y*.7,line_name,'Color',COLORS(run_n))
    xline(ts(run_n),"--",'Linewidth',line_width,'Color',COLORS(run_n),'HandleVisibility','off')
end
title(sprintf('%s: $\hat{K}_{p}$ = %s, $\hat{K}_{d}$ = %s',DISP_NAME,num2str(Kp),num2str(Kd)),'Interpreter','latex');
xlabel('Time (s)','fontsize',font_size);
ylabel('Altitude (m)','fontsize',font_size);
legend('show','Location','best');
set(gca,'XMinorGrid','off','GridLineStyle','-','FontSize',line_size)
xlim([T_START-1 T_END+1]);
ylim([0.4 1.5]);
grid on

avg_hss(test_n) = mean(hss);
var_hss(test_n) = var(hss);
avg_kt(test_n) = mean(kt);
var_kt(test_n) = var(kt);
kphat(test_n) = Kp;
kdhat(test_n) = Kd;
kp(test_n) = Kp/(4*avg_kt(test_n));
kd(test_n) = Kd/(4*avg_kt(test_n));

end
end

```

Not enough input arguments.

Error in make\_graphs (line 16)  
 avg\_hss = zeros(1,N\_TESTS);

## Contents

- [PID Control of Quadcopter Altitude Near Hover](#)
- [Vehicle Parameters](#)
- [Step change in altitude reference, m](#)
- [Initial Conditions](#)
- [PD Control With Gravity Feedforward](#)
- [Closed-Loop Transfer Function \(hdes to h\)](#)
- [Convert Gains](#)
- [Simulate Closed-Loop](#)
- [Plot results](#)

## PID Control of Quadcopter Altitude Near Hover

Acknowledgement: Prof. Peter Seiler

```
%-----
function [wn, zeta] = Low_Fidelity_Model(DISP_NAME, m, kT, Kp, Kd)
```

## Vehicle Parameters

close all; clear all; m = 65e-3; % Mass, kg

```
T_START = 19; % s
T_STEADY = 30; % s, Chosen as start of steady-state response from observation
T_END = T_START+25; % s
g = 9.81; % m/s^2
% kT = ; % Thrust coefficient, N
% kT = input('Enter the estimated thrust coefficient, N, kT: ');
umax = 500; % Maximum motor input command, unitless
umin = 0; % Minimum motor input command, unitless
```

## Step change in altitude reference, m

```
Tf = 25; % Final simulation time, sec
hdes0 = 0.7; % Initial altitude, m
hdesf = 1.25; % Final altitude, m
```

## Initial Conditions

```
h0 = hdes0; % Initial altitude, m
hdot0 = 0; % Initial altitude velocity, m/s
hddmax = (4*kT*umax-m*g)/m; % Maximum upward acceleration, m/s^2
```

Not enough input arguments.

```
Error in Low_Fidelity_Model (line 26)
    hddmax = (4*kT*umax-m*g)/m; % Maximum upward acceleration, m/s^2
```

## PD Control With Gravity Feedforward

Consider the following PD control law with gravity feedforward  $u = K_p(h_{des}-h) - K_d\dot{h} + (\hat{m}g)/(4\hat{k}_T)$ . Here  $u$  is the **\*individual motor command\*** input (unitless). Also,  $(\hat{m}, \hat{k}_T)$  indicate that these are estimates used by the controller. The parrot drone Simulink diagram uses:  $\hat{u} = K_{phat}(h_{des}-h) - K_{dhat}\dot{h} + \hat{m}g$  where  $\hat{u}$  is the **\*total thrust\*** command (N). These are related by  $\hat{u} = (4\hat{k}_T)u$ . Thus gains computed using the simplified second-order model must be scaled by  $(4\hat{k}_T)$  before implementing in the parrot Simulink diagram.

NOTE - An integral gain is included below for testing but this can be set to zero to simply to the PD control given above.

```

% Select Gains -- Gains are specified using simplified second order model

GainCase = 2;
switch GainCase
    case 1
        % Select closed-loop natural frequency and damping ratio
        wn = input('Desired natural freq, rad/sec, wn: '); % Desired natural freq, rad/sec
        zeta = input('Desired damping ratio, unitless, zeta: '); % Desired damping ratio, unitless

        % Closed-loop ODE with PD control + perfect gravity cancellation:
        % m hdd = (4*kT)*( Kp*(hdes-h) - Kd*hdot )
        % --> hdd + (4*kT*Kd/m) hdot + (4*kT*Kp/m) h = (4*kT*Kp/m)*hdes
        Kp = wn^2*m/(4*kT);
        Kd = 2*zeta*wn*m/(4*kT);
        Ki = 0;

    case 2
        % Kp = input('Enter the proportional gain, Kp: ');
        % Kd = input('Enter the derivative gain, Kd: ');
        Ki = 0;

        wn = sqrt(Kp*4*kT/m);
        zeta = 4*kT*Kd/(2*wn*m);
end

```

### Closed-Loop Transfer Function (hdes to h)

This constructs the closed-loop model from altitude reference to altitude. It assumes perfect cancellation of the gravitational force by the feedforward term. It also neglects the saturation that limits the motor command.

```

% Plant dynamics (neglecting gravity term)
% m d^2(h)/dt^2 = (4*kT)*u
% The state-space model below has input motor command and outputs [h;hdot]
Ag = [0 1; 0 0];
Bg = [0; 4*kT/m];
Cg = eye(2);
Dg = 0;
G = ss(Ag,Bg,Cg,Dg);
time = [];
h_arr = [];

tstep = 1; % Step time, sec
% Controller: PI and D terms
if Ki==0
    Cpi = ss(Kp);
else
    Cpi = tf([Kp Ki],[1 0]);
end
Cd = ss(Kd);

% Form closed-loop from r to h, T
systemnames = 'G Cpi Cd';
inputvar = '[r]';
outputvar = '[G(1)]';
input_to_G = '[Cpi+Cd]';
input_to_Cpi = '[r-G(1)]';
input_to_Cd = '[-G(2)]';
%T = sysic;

if false
    % Code to debug: Represent controller
    % (*) u = Kp e + Kd edot + Ki integral(e)
    % The actual implementation only uses rate-feedback, i.e. Kd*edot is
    % replaced by -Kd*hdot. However, the form in (*) above is much easier
    % to construct with standard functions and will yield the same poles
    % (only the closed-loop zeros will be different)

```

```

Gb = tf(4*kT/m,[1 0 0]);
if Ki==0
    Cpid = tf([Kd Kp],1);
else
    Cpid = tf([Kd Kp Ki],[1 0]);
end
Tb = feedback(Gb*Cpid,1);
end

```

## Convert Gains

There are two sets of gains: 1) (Kd,Kp,Ki) for simple second order model with motor command input 2) (Kdhat,Kphat,Kihat) for parrot drone simulink model with total thrust command input. These are the gains that should be used in the parrot drone Simulink model.

```

Kdhat = (4*kT)*Kd;
Kphat = (4*kT)*Kp;
Kihat = (4*kT)*Ki;

```

## Simulate Closed-Loop

```

% Parameter estimates
mhat = m;
kThat = kT;

% Disturbance Force, N
Fd = 0;

% Simulate system

% Allow sim to be called as a function
% and have proper variable scope
options = simset('SrcWorkspace','current');
sim('QuadPID',[0 Tf],options);

```

## Plot results

```

font_size = 12;
line_size = 15;
line_width = 1;
color = 'b';

figure();
hold on
text(T_STEADY,1,"w_{n} = " + wn + newline + "zeta = " + zeta);
yline(hdesf,'Linewidth',line_width,'Color','black','DisplayName','z_{ref}')
plot(tsim+T_START,h,'Linewidth',line_width,'Color',color,'DisplayName','Low Sim');
title(sprintf('%s: \hat{K}_p = %s, \hat{K}_d = %s$', DISP_NAME, num2str(Kphat), num2str(Kdhat)), 'Interpreter','latex');
xlabel('Time (s)','fontsize',font_size);
ylabel('Altitude (m)','fontsize',font_size);
legend('show','Location','best');
set(gca,'XMinorGrid','off','GridLineStyle','-','FontSize',line_size)
xlim([T_START T_END+1]);
ylim([0.4 1.5]);
grid on;

time = [time tsim];
h_arr = [h_arr h];

% Steady-state error
idxs = find(time >= T_STEADY-T_START); % Indices of steady state region
z_arr = h_arr(idxs); % Z values being investigated

```

```
zs = double(mean(z_arr)); % m, Experimental settling value
hss = zs - hdesf; % m, Steady state error

line_name = "h_{ss} = " + hss;
text(T_STEADY,1.05*zs,line_name,'Color',color)
yline(zs,"--",'Linewidth',line_width,'Color',color,'HandleVisibility','off')

% Settling Time
if zeta < 0.5 % Underdamped case
    ts = 3/(zeta*wn);
    line_name = "ts = " + (ts-1) + " (theory)";
    text(1.01*(ts+T_START),.6,line_name,'Color','r')
    xline(ts+T_START,"--",'Linewidth',line_width,'Color','r','HandleVisibility','off')
end

% Find last time z dipped below 95% of z_settle
ts_idx = find(h_arr <= 0.95*zs);
if isempty(ts_idx)
    ts1 = 0;
else
    ts1 = time(ts_idx(end));
end

% Find last time z rose above 105% of z_settle
ts_idx = find(h_arr >= 1.05*zs);
if isempty(ts_idx)
    ts2 = 0;
else
    ts2 = time(ts_idx(end));
end

ts = max(ts1,ts2); % s, Settling time (use the later time)

line_name = "ts = " + (ts-1);
text(1.01*(ts+T_START),.6,line_name,'Color',color)
xline(ts+T_START,"--",'Linewidth',line_width,'Color',color,'HandleVisibility','off')
```

```
end
```

## Flight Experiments

Trevor Burgoyne 13 Nov 2022

```
% Paths for data loading
ROOT_DIR = "C:/Users/Trevor/Desktop/AEM 4602W/Controls-Lab/Data/Part 1/";
PREFIX = "pjsdata_T";
DISP_NAME = "No Added Mass";
LABEL_NAME = "Run";
N_TESTS = 3;
N_RUNS = 2;
masses = [68.1, 68, 69.5] / 1000; % kg
[avg_hss, var_hss, avg_kt, var_kt, kphat, kdhat, kp, kd] = make_graphs(ROOT_DIR, PREFIX, DISP_NAME, LABEL_NAME, N_TESTS, N_RUNS, masses)
% Generate Low Fidelity Model Plots
for test_n=1:N_TESTS
    [wn, zeta] = Low_Fidelity_Model(DISP_NAME, masses(test_n), avg_kt(test_n), kp(test_n), kd(test_n));
end
```

avg\_hss =

-0.1181    -0.1434    -0.1828

var\_hss =

1.0e-03 \*  
0.1084    0.0977    0.1194

avg\_kt =

0.5240    0.5358    0.5237

var\_kt =

1.0e-04 \*  
0.6498    0.4380    0.5865

kphat =

1.4300    0.9900    0.8300

kdhat =

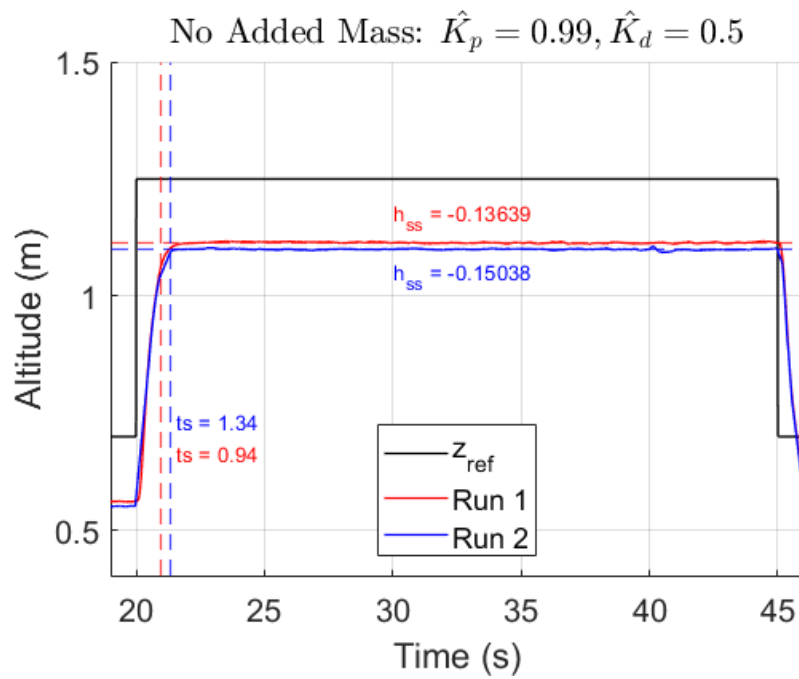
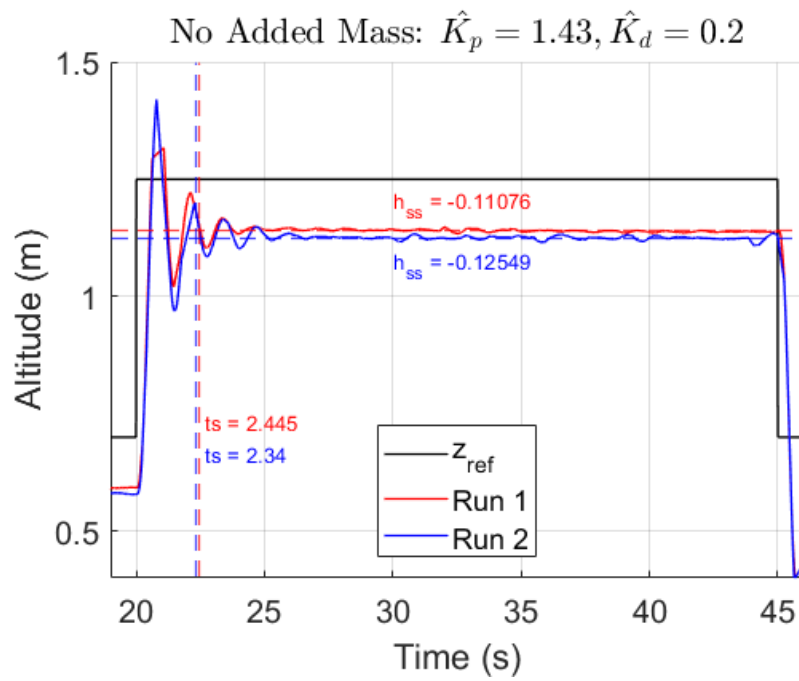
0.2000    0.5000    0.8000

kp =

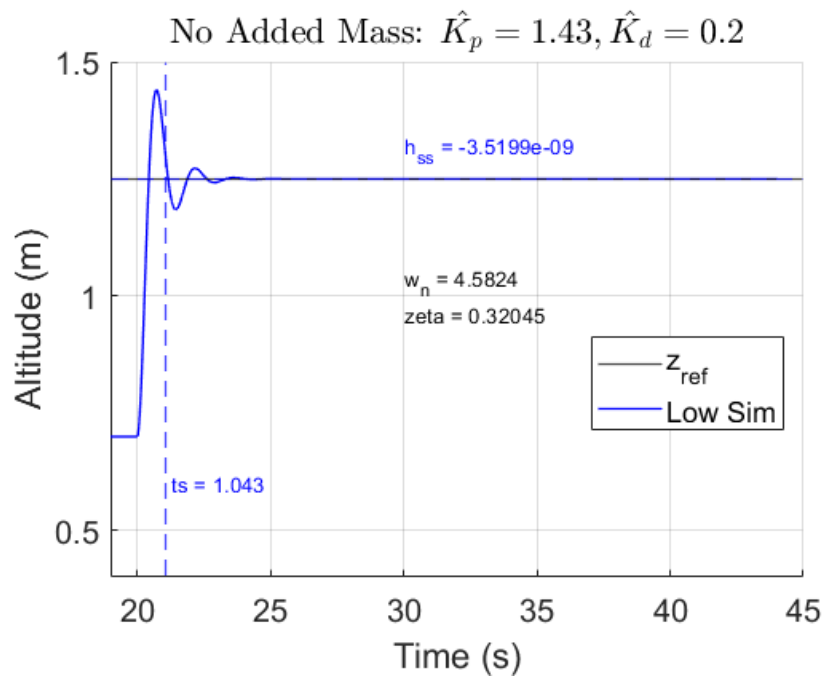
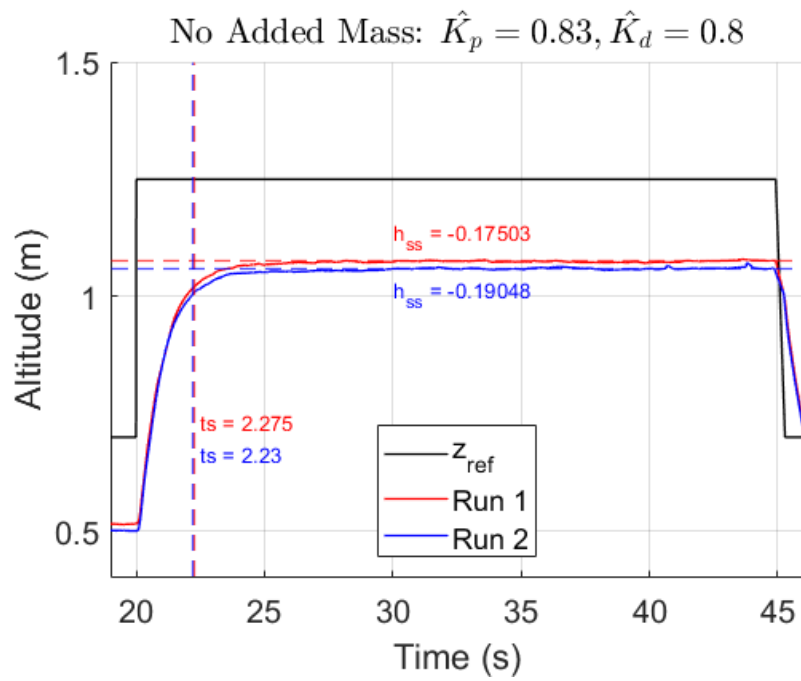
0.6823    0.4619    0.3962

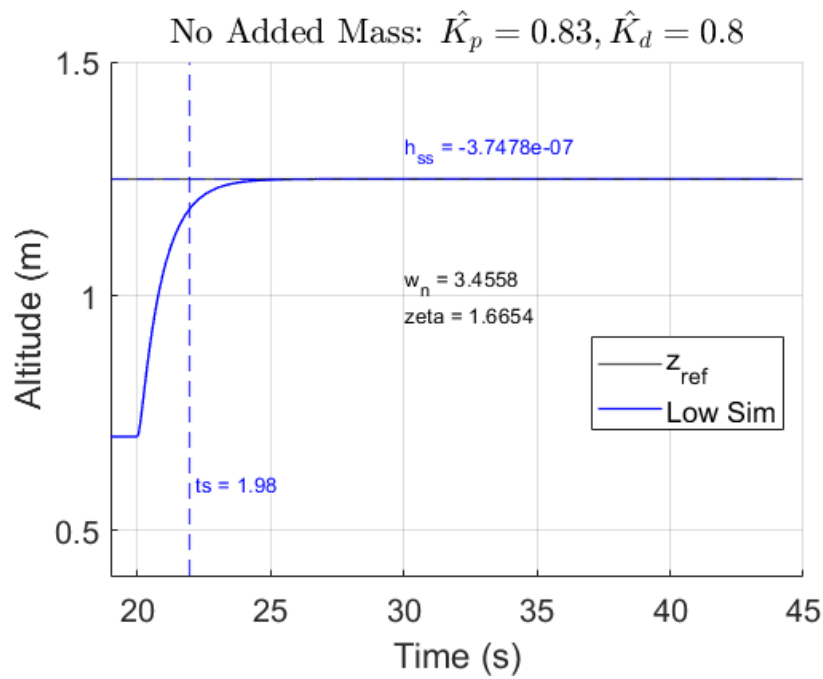
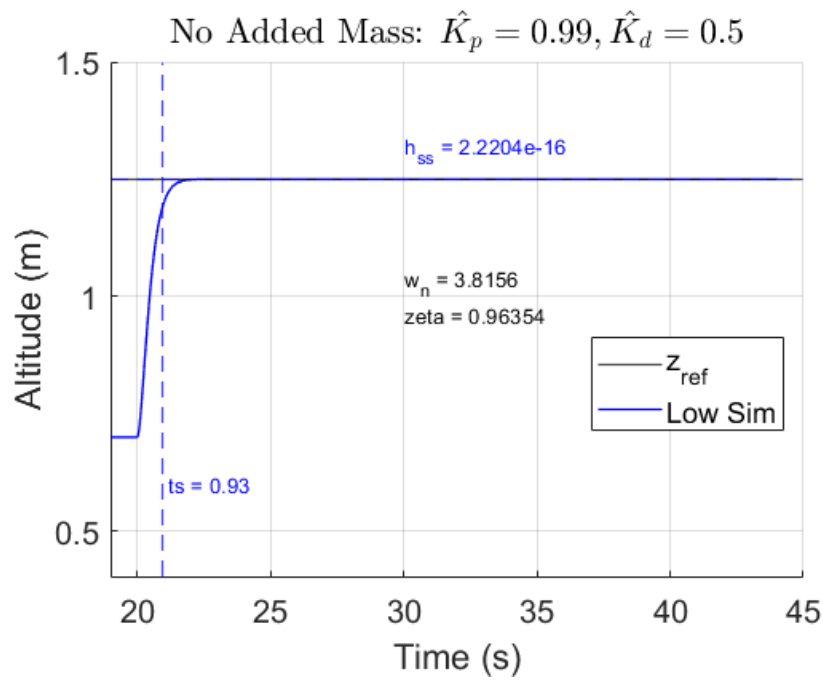
kd =

0.0954    0.2333    0.3819









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## Added Mass Experiments

Trevor Burgoyne 13 Nov 2022

```
% Paths for data loading
ROOT_DIR = "C:/Users/Trevor/Desktop/AEM 4602W/Controls-Lab/Data/Part 3/";
PREFIX = "pjsdata_P3T";
DISP_NAME = "Added Mass";
LABEL_NAME = "Run";
N_TESTS = 2;
N_RUNS = 2;
masses = [79.3, 80.6] / 1000; % kg
[avg_hss, var_hss, avg_kt, var_kt, kphat, kdhat, kp, kd] = make_graphs(ROOT_DIR, PREFIX, DISP_NAME, LABEL_NAME, N_TESTS, N_RUNS, masses)

for test_n=1:N_TESTS
    [wn, zeta] = Low_Fidelity_Model(DISP_NAME, masses(test_n), avg_kt(test_n), kp(test_n), kd(test_n));
end
```

avg\_hss =

-0.1487    -0.1418

var\_hss =

1.0e-03 \*

0.1446    0.6192

avg\_kt =

0.5450    0.5636

var\_kt =

1.0e-03 \*

0.0114    0.1419

kphat =

0.9900    0.8300

kdhat =

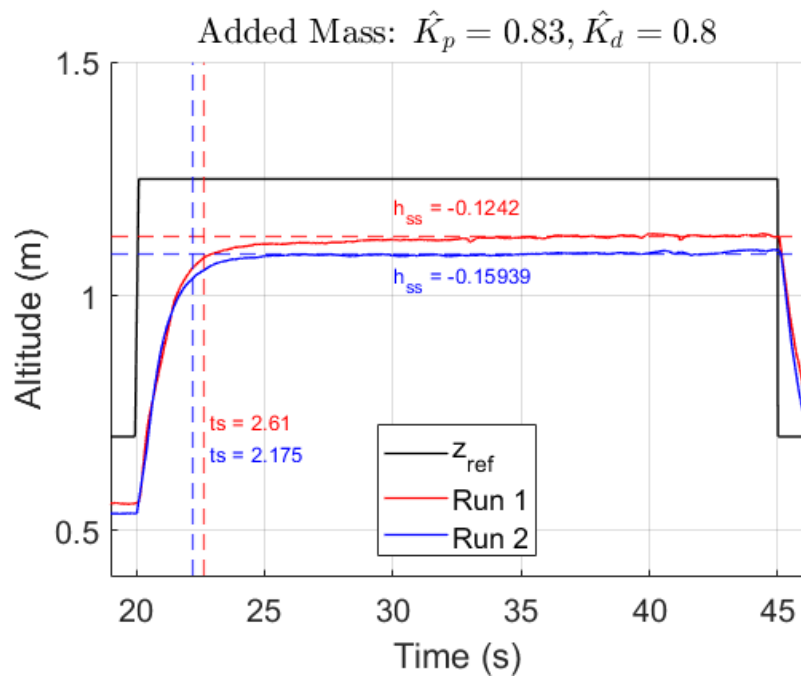
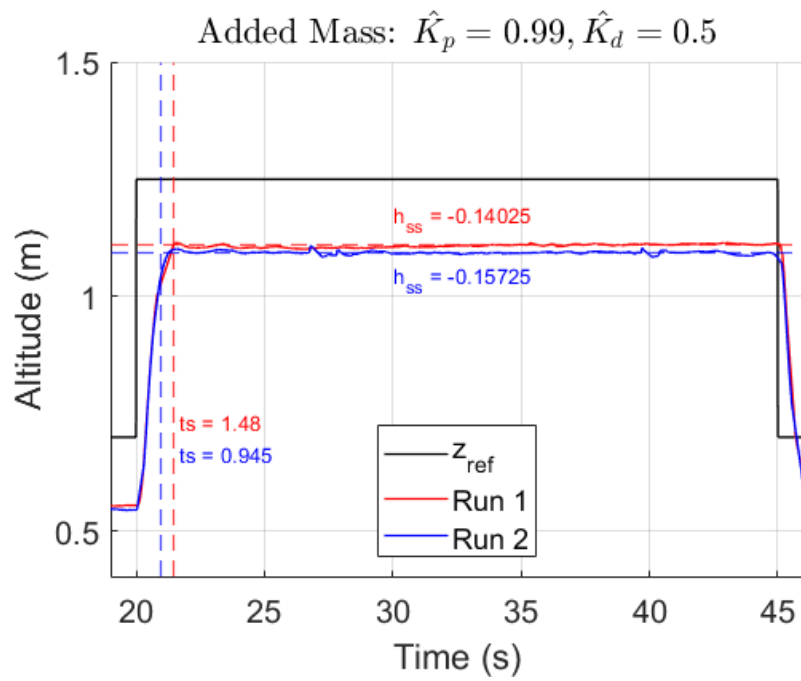
0.5000    0.8000

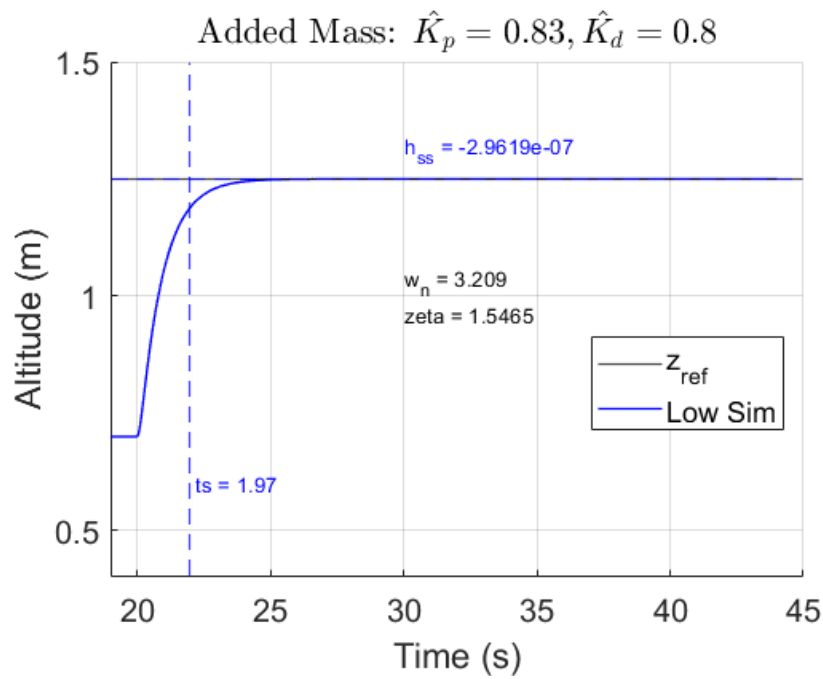
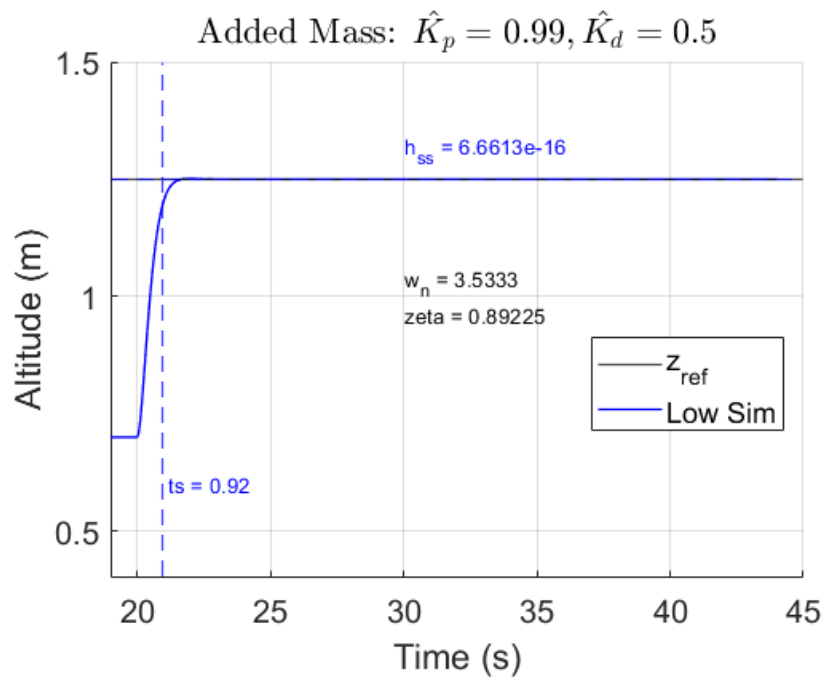
kp =

0.4541    0.3682

kd =

0.2294    0.3549





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## High-Fidelity, Added Mass Sims

Trevor Burgoyne 13 Nov 2022

```
% Paths for data loading
ROOT_DIR = "C:/Users/Trevor/Desktop/AEM 4602W/Controls-Lab/Data/Part 3/";
PREFIX = "part3_t";
DISP_NAME = "Added Mass";
LABEL_NAME = "High Sim";
N_TESTS = 2;
N_RUNS = 1;
masses = [79.3, 80.6] / 1000; % kg
[avg_hss, var_hss, avg_kt, var_kt, kphat, kdhat, kp, kd] = make_graphs(ROOT_DIR, PREFIX, DISP_NAME, LABEL_NAME, N_TESTS, N_RUNS, masses)
```

avg\_hss =

0.0021    0.0038

var\_hss =

0    0

avg\_kt =

0.6585    0.6660

var\_kt =

0    0

kphat =

0.9900    0.8300

kdhat =

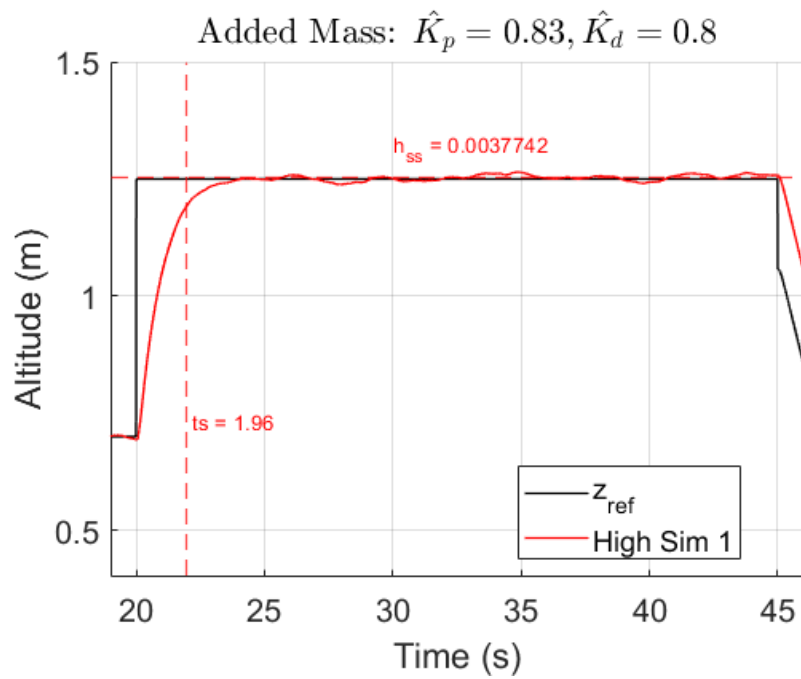
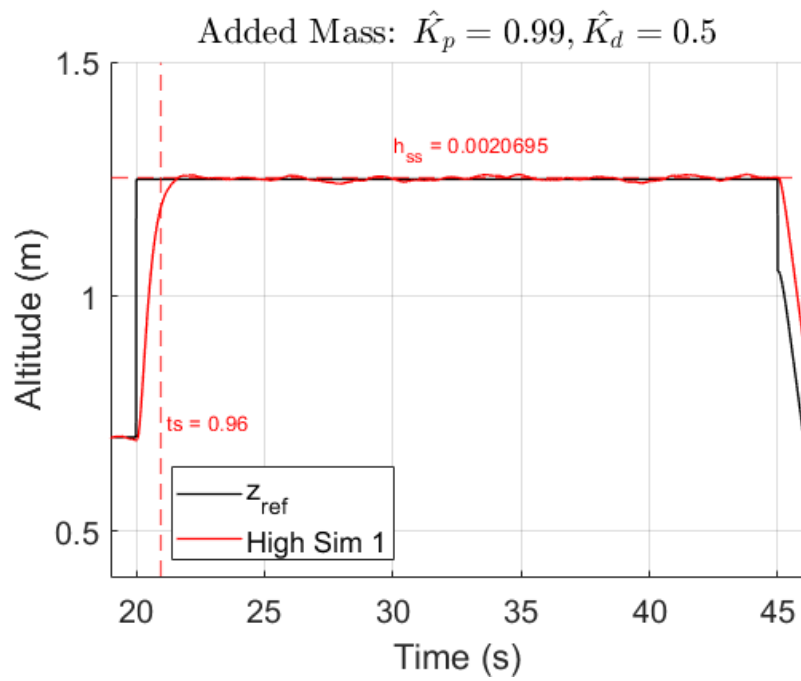
0.5000    0.8000

kp =

0.3758    0.3116

kd =

0.1898    0.3003



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## High-Fidelity, No Mass Sims

Trevor Burgoyne 13 Nov 2022

```
% Paths for data loading
ROOT_DIR = "C:/Users/Trevor/Desktop/AEM 4602W/Controls-Lab/Data/Part 2/";
PREFIX = "sim_t";
DISP_NAME = "No Added Mass";
LABEL_NAME = "High Sim";
N_TESTS = 6;
N_RUNS = 1;
masses = 69*ones(1,N_TESTS)/1000; % kg
[avg_hss, var_hss, avg_kt, var_kt, kphat, kdhat, kp, kd] = make_graphs(ROOT_DIR, PREFIX, DISP_NAME, LABEL_NAME, N_TESTS, N_RUNS, masses)
```

avg\_hss =

0.0005	0.0021	0.0038	0.0017	0.0062	0.0042
--------	--------	--------	--------	--------	--------

var\_hss =

0	0	0	0	0	0
---	---	---	---	---	---

avg\_kt =

0.6815	0.6669	0.6489	0.6615	0.6534	0.6536
--------	--------	--------	--------	--------	--------

var\_kt =

0	0	0	0	0	0
---	---	---	---	---	---

kphat =

1.4300	0.9900	0.8300	1.6900	0.5000	0.1000
--------	--------	--------	--------	--------	--------

kdhat =

0.2000	0.5000	0.8000	0.6900	0.9900	0.1000
--------	--------	--------	--------	--------	--------

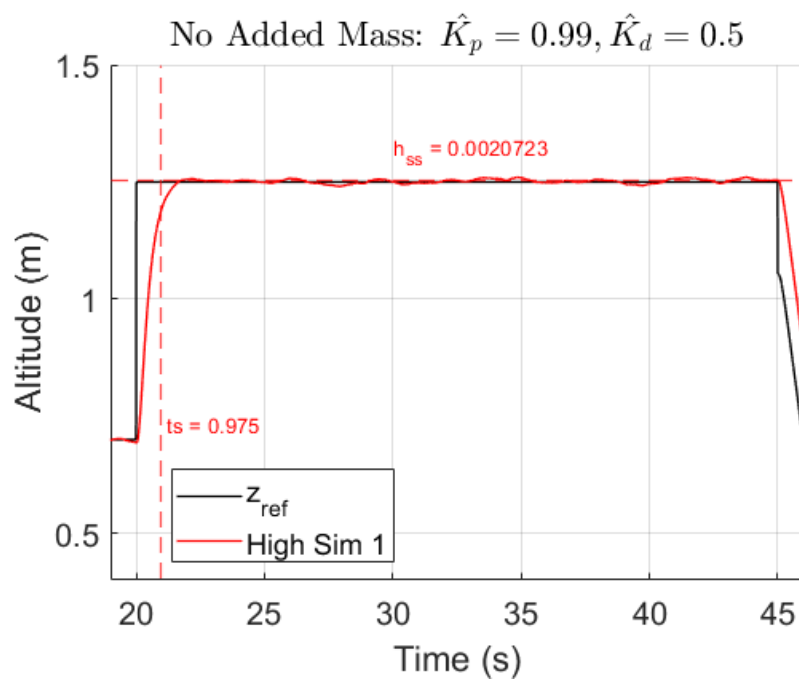
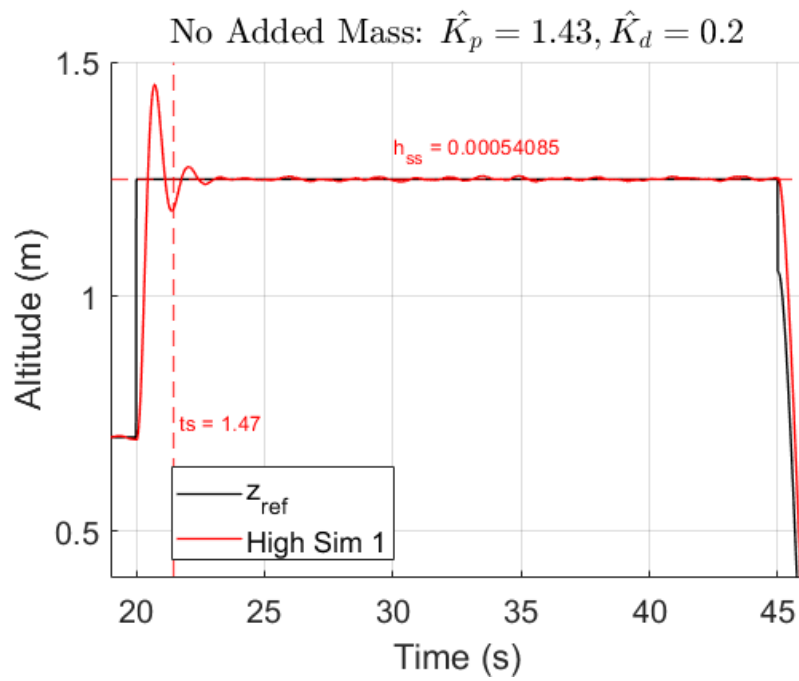
kp =

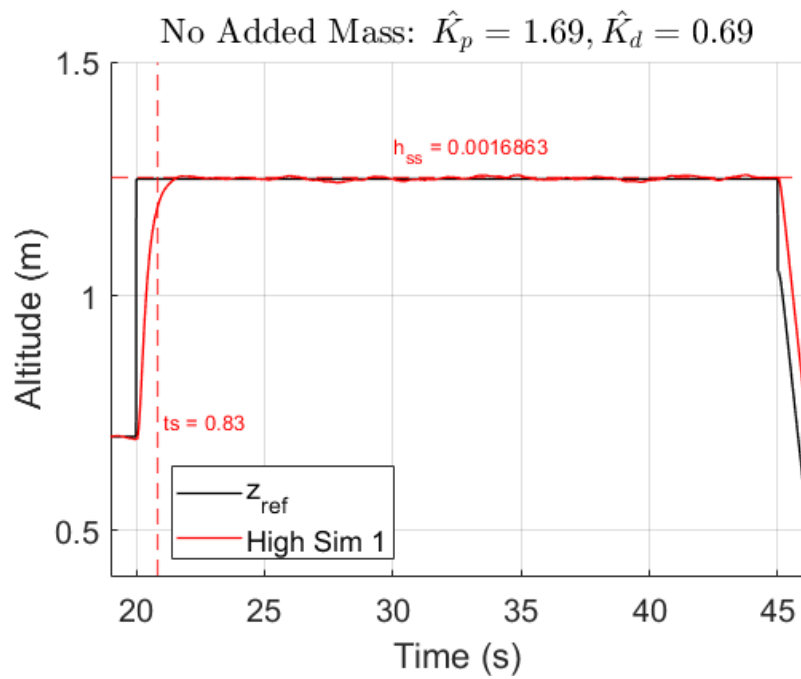
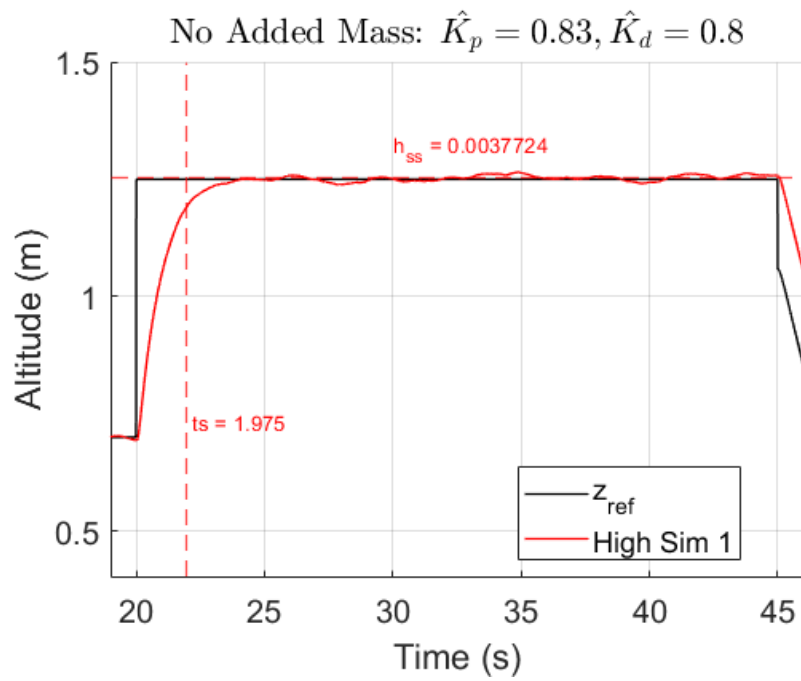
0.5245	0.3711	0.3198	0.6387	0.1913	0.0383
--------	--------	--------	--------	--------	--------

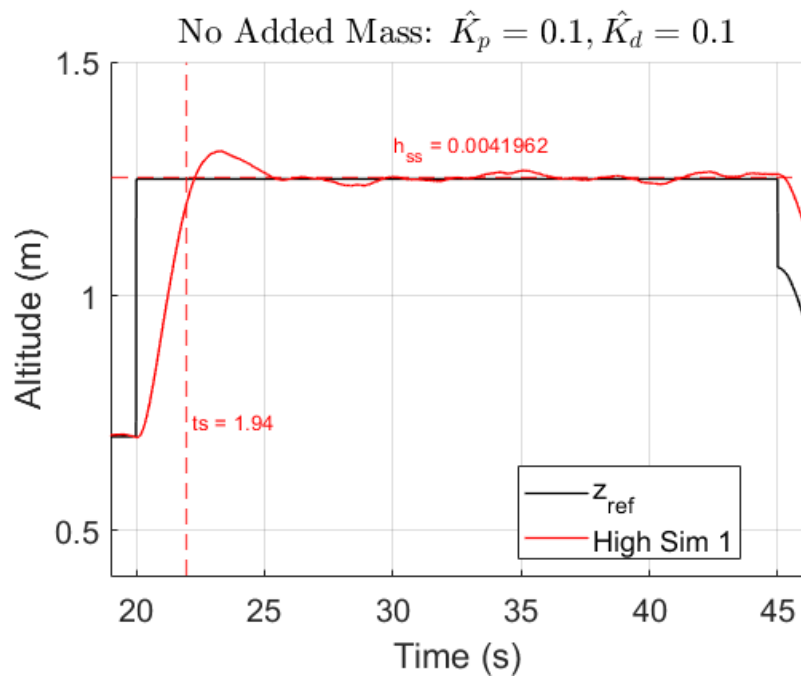
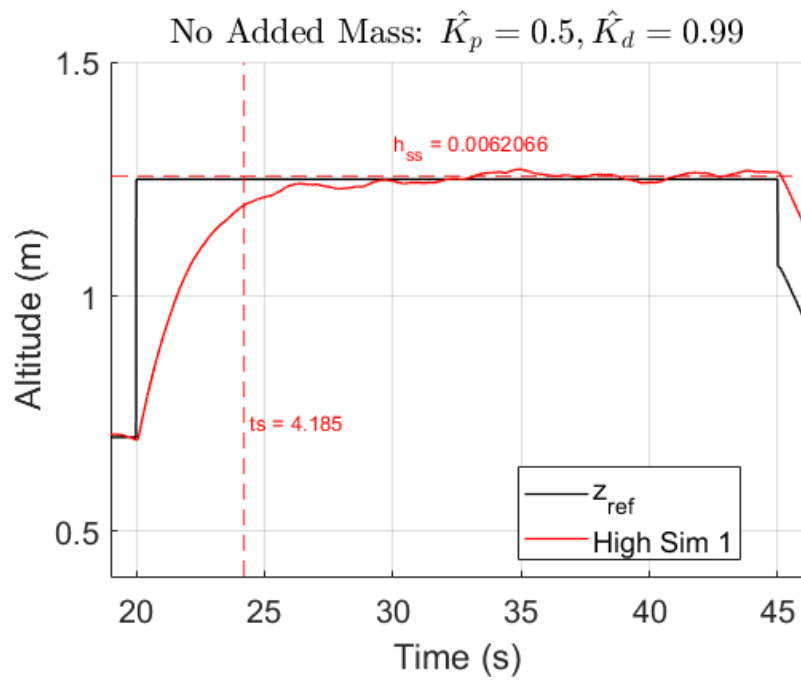
kd =

0.0734	0.1874	0.3082	0.2608	0.3788	0.0383
--------	--------	--------	--------	--------	--------









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