
MATH 260: ORDINARY
DIFFERENTIAL EQUATIONS

PUBLIC NOTES FOR ANY ORDINARY
DIFFERENTIAL EQUATION'S CLASS

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