

concordance=TRUE

Spatial integral projection models predict slow
creosotebush encroachment between episodes of rapid
expansion

Trevor Drees^{*a,b}, Brad M. Ochocki^b, Scott L. Collins^c, and Tom E.X. Miller^b

^aDepartment of Biology, Penn State University, State College, PA USA

^bProgram in Ecology and Evolutionary Biology, Department of BioSciences, Rice
University, Houston, TX USA

^cDepartment of Biology, University of New Mexico, Albuquerque, NM USA

April 7, 2020

^{*}thd5066@psu.edu

1 Abstract

2 Encroachment of shrubs into adjacent grasslands has become an increasingly reported
3 phenomenon across the world, and such encroachment is either pulled forward by high
4 population growth at the low-density encroachment front or pushed forward by higher-
5 density areas behind the front. However, at sites such as Sevilleta National Wildlife
6 Refuge in central New Mexico, little is known about whether encroachment is pushed or
7 pulled, and the dynamics of encroachment are not well-understood. Here, long-term en-
8 croachment of creosotebush (*Larrea tridentata*), a native perennial shrub, stands in stark
9 contrast with the stagnation in encroachment observed in recent decades. In order to
10 better understand creosotebush encroachment at this site, we quantify it using a spatially
11 structured population model where a wave of individuals travels at a speed governed by
12 both dispersal and density-dependence. Results indicate that population growth rates
13 generally increase with decreasing density, suggesting that encroachment is pulled by
14 individuals at the low-density wave front, and the spatial population model predicts an
15 encroachment rate of less than 2 cm per year. While the predicted rate of encroach-
16 ment is consistent with observations over recent decades, it does not explain long-term
17 creosotebush encroachment at the study site, suggesting that this process may occur in
18 pulses when recruitment, seedling survival, or dispersal significantly exceed typical rates.
19 Overall, our work demonstrates that individuals at low densities are likely the biggest
20 contributors to creosotebush encroachment at this site, and that this encroachment is
21 likely a process that occurs in large but infrequent bursts rather than at a steady pace.

22 Keywords

23 density-dependence, ecotones, woody encroachment, shrubs, integral projection model,
24 grassland

25 Introduction

26 The encroachment of shrubs and other woody plants into adjacent grasslands has been the
27 focus of an increasing number of studies in recent years, likely in response to increasingly
28 visible vegetation and landscape changes in ecosystems where this process takes place.
29 This process of encroachment generally involves increases in number and/or density of
30 woody shrub-like plants in a given area (?), which can displace other species and alter the
31 local ecosystem. Woody plant encroachment has been observed across many of the arid
32 and semi-arid regions across the world, such as the grasslands of the southwestern United
33 States (Van Auken 2000, 2009; Goslee et al. 2003; Gibbens et al. 2005) and southern
34 South America (Parizek et al. 2002; Cabral et al. 2003), savannas of southern Africa
35 (Trollope et al. 1989; Roques et al. 2001), and Asian steppes (Peng et al. 2013; Chen et
36 al. 2015). These shrub invasions are often regarded as ecological issues in the places where
37 they occur, with the increasing shrub biomass and dispersal being considered as strong
38 drivers of ecosystem degradation and/or desertification (Schlesinger et al. 1990; Ravi et
39 al. 2009) due to how these plants alter the distribution of soil resources (Schlesinger and
40 Pilmanis 1998; Knapp et al. 2008). In other places, ecosystem function and dynamics
41 may be altered in ways that are significantly different and depend on the traits of the
42 invading shrubs (Eldridge et al. 2011). Other adverse effects of encroachment include
43 changes in ecosystem services (Reed et al. 2015; Kelleway et al. 2017), declines in
44 biodiversity (Ratajczak et al. 2012; Sirami and Monadjem, 2012; Brandt et al. 2013),
45 and economic losses in areas where the proliferation of shrubs adversely affects grazing
46 land and pastoral production (Mugasi et al. 2000; Oba et al. 2000).

47 The encroachment of woody plants into adjacent grasslands involves the movement of
48 shrub-grass ecotones, and this kind of expansion can be modelled as a propagating wave
49 that is a gradient of conspecific density varying in both space and time (Kot et al. 1996;
50 Neubert and Caswell 2000; Wang et al. 2002; Pan and Lin 2012). The movement of these

51 waves is dependent upon two major factors: dispersal of propagules and demographic
52 processes within the population. Movement itself is driven by the spatial dispersal of
53 propagules produced by the plants; without such dispersal, expansion does not occur.
54 The speed at which these waves move is highly dependent upon the dispersal kernel
55 shape, especially regarding the frequency of long-distance dispersal events at the tail
56 of the distribution (Skarpaas and Shea 2007). Though dispersal plays a role in where
57 the new recruits that drive the wave's movement are likely to be found, demographic
58 processes are important as well since survival, growth, reproduction, and recruitment
59 rates in the parent plant ultimately affect the number of propagules produced and their
60 fate after release. These demographic processes can strongly affect how waves move,
61 and structured populations in which rates vary between age, size, or life stage can be
62 sensitive to demographic changes that may alter patterns of expansion (Neubert and
63 Caswell 2000).

64 Given that these waves are gradients of conspecific density, the effects of density
65 dependence on demographic rates and population growth are important to consider. Not
66 only does the density of plants influence the strength of resource competition amongst
67 them and thus the extent to which they survive, grow and reproduce, but it also can
68 determine whether a dispersed propagule will germinate and grow or if its competitors
69 will prevent it from becoming established. Since intraspecific competition governs the
70 performance of individuals within the population, the part of the population responsible
71 for wave movement is strongly tied to how demographic rates and population growth vary
72 with changes in conspecific density. If population growth has a negative and monotonic
73 relationship with density such that highest rates of growth tend to be found at the lowest
74 densities, then the invading wave is pulled forward by the plants at the low-density
75 vanguard (Kot et al. 1996). However, if Allee effects result in reduced fitness at low
76 densities, then the wave is instead pushed forward by the plants behind the front edge
77 (Kot et al. 1996; Taylor and Hastings 2005; Sullivan et al. 2017). Such Allee effects can

78 greatly limit population growth at the front of the wave, slowing or halting its movement
79 (Lewis and Kareiva 1993; Veit and Lewis 1996; Keitt et al. 2001).

80 Ecological theory for invasion waves as described above provides a tool that can be
81 used to better understand and manage woody encroachment, with many sites of shrub
82 expansion around the world providing opportunities to do so. One particular site of
83 interest is the Chihuahuan Desert of the southwestern United States, where extensive
84 documentation of shrub encroachment already exists. Here, populations of the creosote-
85 bush *Larrea tridentata* have been expanding into nearby grasslands for approximately
86 150 years and have decreased the cover of grasses such as *Bouteloua eriopoda* (Gardner
87 1951; Buffington and Herbel 1965; Gibbens et al. 2005). This encroachment leads to
88 ecotones marking a transition from dense shrubland with numerous dry patches to open
89 grassland, with a transition zone in between where larger shrubs can often be found
90 interspersed among their grassy competitors. Historically, long-term creosotebush en-
91 croachment into grasslands is believed to have been driven by a combination of factors
92 including overgrazing, drought and variability in rainfall, and suppression of fire regimes
93 (Moreno-de las Heras et al. 2016). These shrubs are also thought to further facilitate
94 their own encroachment through positive feedback (Grover and Musick 1990; D’Odorico
95 et al. 2012) by modifying various aspects of their surroundings that could favour con-
96 tinued growth and dispersal, such as local climate (D’Odorico et al. 2010) and rates of
97 soil erosion (Turnbull et al. 2010). Such positive feedback also occurs as herbaceous
98 competitors are eliminated, reducing competition as well as the amount of flammable
99 biomass used to fuel the fires that keep creosotebush growth in check (Van Auken 2000).

100 In addition to these large-scale observations of encroachment, some demographic
101 data on creosotebush are also present and may prove useful in connecting encroachment
102 observations to mathematical models of propagating population wave fronts. Several
103 studies have shown a negative relationship between size and conspecific density in *Larrea*
104 *tridentata* (Yeaton et al. 1977; Phillips and MacMahon 1981; Miller and Huenneke

2000), indicating that density dependence likely regulates resource intake and controls growth in competing shrubs. There is also evidence for a negative relationship between number of fruits and conspecific density (Miller and Huenneke 2000), suggesting that creosotebush fecundity is higher in areas with fewer conspecific neighbours. Overall though, the amount of literature investigating density dependence of demographic rates and population growth in creosotebush is still rather limited. There is also relatively little understanding of how density-dependent demography and population growth facilitate creosotebush expansion, as well as a dearth of data regarding population dynamics at the vanguard of expanding creosotebush populations. Without better knowledge on all of these, it becomes rather difficult to mathematically model creosotebush encroachment, as doing so requires knowledge of the mechanisms occurring at these grass-shrub boundaries. Such gaps in knowledge make it difficult to make estimates of encroachment rates that extend beyond what can be gathered from vegetation surveys.

This research aims to fill these knowledge gaps by not only collecting better data on demographic rates and dispersal in *Larrea tridentata*, but also by connecting it to the mathematical models that portray encroaching populations as propagating waves through space and time. These investigations are novel in the sense that they will be some of the first to apply the aforementioned mathematical model to ecotones of *Larrea tridentata* and its grassy competitors, using density-dependent demographic rates and recruitment to describe the dynamics of ecotone movement in this specific system. First, we quantify how demographic rates such as survival, annual growth, and reproduction vary across both the distribution of shrub sizes as well as a gradient of conspecific density. These demographic data allow us to analyse the pattern of density dependence to see whether this density dependence is strictly monotonic and population growth is maximised at the lowest conspecific density or if Allee effects are present. This will also let us understand if the invasion wave is pulled by the individuals at the front or instead pushed by the individuals behind it. Second, we use a fluid dynamics model to investigate wind dispersal

132 capabilities in this species and construct dispersal kernels to estimate the probability of
133 propagules travelling a given distance. Finally, we combine our data on demographic
134 rates and dispersal, using a spatial integral projection model to obtain estimates for the
135 approximate speed at which the wave advances.

136 **Materials and methods**

137 **Study system**

138 **Encroachment re-surveys**

139 We recorded shrub percent cover along two permanent 1000-m transects that spanned
140 the shrub-grass ecotone, from high to low to near-zero shrub density. These surveys were
141 conducted in summer 2001 and again in summer 2013 to document change in the spatial
142 extent of shrub encroachment. At every 10 meters, shrub cover was recorded in nine
143 cover classes ($<1\%$, $1-4\%$, $5-10\%$, $10-25\%$, $25-33\%$, $33-50\%$, $50-75\%$, $75-95\%$, $>95\%$).
144 For analysis, we visually assessed midpoint values of these cover classes at each meter
145 location for both transects and years.

146 **Demographic data collection**

147 **Observational surveys**

148 **Transplant experiment**

149 **Demographic data analysis**

150 **Observational surveys**

151 **Transplant experiment**

152 Collection of creosotebush demographic data occurred during the early summer of every
153 year from 2013-2017, at the Sevilleta National Wildlife Refuge LTER site in central New

154 Mexico. Four different sampling sites in the eastern part of the reserve were designated,
155 with each of the sites containing 3 different transects. Lengths of these transects varied
156 from 200 to 600 m, and no two sites had identical compositions of transect lengths.
157 Transect length was determined by the strength of vegetation transition, as areas where
158 shrubland more quickly transitions to grassland do not need as long of a transect to
159 capture the gradient of densities as a more gradual transition does. All transects were
160 placed longitudinally along the shrubland-grassland ecotone so a full range of shrub
161 densities could be captured; each transect spanned shrub-dense "core" areas as well as
162 grasslands with few shrubs and the transition zones in between.

163 Only plants within a metre of the transect on either side were considered when de-
164 termining baseline shrub densities. These densities were calculated using initial mea-
165 surements from 2013 and were assumed to remain relatively static over the course of
166 the study; each density was recorded as the weighted total amount of shrub volume per
167 5-m transect subsection. The per-shrub volume was calculated as that of an elliptic
168 cone, as this was found to be the figure most closely matching the plant's morphology,
169 using the formula $V_i = \pi lwh/3$ where l , w , and h are the maximum length, maximum
170 width, and height, respectively. Maximum length and width were measured so that they
171 were always perpendicular to each other, and height was measured from the base of
172 the woody stem at the soil surface to the highest part of the shrub. All three of these
173 dimensional measurements were mutually orthogonal and were inclusive only of living
174 parts of the shrub; dead wood and non-foliated outer sections were not included in mea-
175 surements. The total weighted density for the window was then expressed as the sum
176 of log-transformed volumes of each individual shrub contained within. Such a weighted
177 density was chosen because density of individuals alone can often fail to be a useful mea-
178 surement in environments where large size differences between plants of the same species
179 exist. Different-sized plants may vary greatly in their ability to extract resources from
180 the environment around them and may thus differ greatly in their degree of competitive-

ness (Weiner 1990; Hara 1993). By using a weighted density in terms of shrub volume, we were able to account for the extra competitiveness of larger shrubs and thus have a more accurate measurement of conspecific presence that is more suitable for a study population containing significant heterogeneity in size.

A subset of the shrubs used to calculate the baseline densities were tagged, with each plant given a unique identifier that allowed it to be recognised based on sampling site, transect number, and location within 50-m and 5-m subsections. These tagged shrubs then had various demographic measurements recorded on an annual basis. Maximum width, length, and height on each shrub were measured in order to calculate conical volume, using the formula given earlier. Survival status of the shrubs was also recorded, with dead individuals being noted and excluded from measurements in subsequent years. Counts of flowers and fruits on each shrub were recorded as well. In instances where shrubs had large numbers of reproductive structures that would prove difficult to reliably count, estimates were made, with a more accurate count on a fraction of the shrub being extrapolated to the entire individual. The position of each shrub along the transect was noted to a resolution of 5 m so that it could be matched with the baseline density of its corresponding subsection. For shrubs in which a given 5-m subsection was not recorded, their position was estimated to the nearest 50 m; however, compared to the number of finer-resolution 5-m subsections, this occurred relatively infrequently. Establishment of recruits was also accounted for, with new recruits observed within the study area tagged and measured.

Collected demography data were then examined to investigate how weighted density and shrub volume affected four different demographic variables: survival, probability of flowering (i.e. producing at least one flower or fruit), annual growth, and number of reproductive structures. Each of these demographic variables was fit to a different mixed-effects model through maximum likelihood. Both survival and probability of flowering were each fit to generalised linear mixed-effects models using a binomial response and a

208 logit link function. Annual growth was defined as $\ln(V_{t+1}/V_t)$ where V_{t+1} and V_t are the
 209 shrub volumes in the current and previous years, respectively, and was then fit to a linear
 210 mixed-effects model. The number of reproductive structures was defined as the natural
 211 logarithm of the sum of fruits and flowers on the entire shrub and was fit to a linear
 212 mixed-effects model as well. To construct these models, all of the equations listed in
 213 Table 1 were first fit to each of the four demographic variables, with each equation using
 214 volume and standardised density as predictors while also treating the unique transect
 215 in which each shrub was located as a random effect. After these equations were fit to
 216 the data, all eight equations for each demographic variable were ranked based on their
 217 value of the Akaike information criterion (AIC) and weighted based on their quality so
 218 that better-fitting models had a higher weight. Then, coefficients of the same type were
 219 averaged between all eight models for each demographic variable using a weighted mean
 220 corresponding to model quality in order to generate an average model. All four average
 221 models have the general form

$$222 \quad R = \beta_1 v + \beta_2 d + \beta_3 d^2 + \beta_4 vd + \beta_5 vd^2 + \epsilon \quad (1)$$

223 where R is the response variable, v and d are the volume and density, ϵ is a random
 224 transect effect, and β is the coefficient for each type of term.

225 The effect of density dependence on the probability of recruitment from seeds was
 226 also modelled. For every year, the sum of seeds produced the prior year was calculated
 227 for each 5-m subsection, and then probability of recruitment was calculated as the num-
 228 ber of recruits observed in each 5-m subsection divided by that number of seeds. For
 229 any subsection in which seeds were not found, a count of seeds was estimated based on
 230 the number of seeds in a subsection of similar weighted density; this was done to avoid
 231 creating any undefined values of recruitment probability. Both linear and quadratic mod-
 232 els using only weighted density as a predictor were fit to the distribution of recruitment

probabilities, though the linear model was ultimately used because it had a higher AIC value.

Seed dispersal

Dispersal kernels were calculated using the WALD, or Wald analytical long-distance dispersal, model that uses a mechanistic approach to predict dispersal patterns of plant propagules by wind. The WALD model, which is largely based in fluid dynamics, can serve as a good approximation of empirically-determined dispersal kernels (Katul et al. 2005; Skarpaas and Shea 2007) and may be used when empirical dispersal data is not readily available. Under the assumptions that wind turbulence is low, wind flow is vertically homogenous, and terminal velocity is achieved immediately upon seed release, the WALD model simplifies a Lagrangian stochastic model to create a dispersal kernel that estimates the likelihood a propagule will travel a given distance (Katul et al. 2005). This dispersal kernel takes the form of the inverse Gaussian distribution

$$p(r) = \left(\frac{\lambda'}{2\pi r^3} \right)^{\frac{1}{2}} \exp \left[-\frac{\lambda'(r - \mu')^2}{2\mu'^2 r} \right] \quad (2)$$

that is a slight adaptation from equation 5b in Katul et al. (2005), using r to denote dispersal distance. Here, λ' is the location parameter and μ' is the scale parameter, which depend on environmental and plant-specific properties of the study system. The location and scale parameters are defined as $\lambda' = (H/\sigma)^2$ and $\mu' = HU/F$; these are functions of the height H of seed release, wind speed U at seed release height, seed terminal velocity F , and the turbulent flow parameter σ that depends on both wind speed and local vegetation roughness.

In order to create the dispersal kernel, we first take the wind speeds at measurement height z_m and correct them to find wind speed U for any height H by using the

256 logarithmic wind profile

$$257 \quad U = \frac{1}{H} \int_{d+z_0}^H \frac{u^*}{K} \log \left(\frac{z-d}{z_0} \right) dz \quad (3)$$

258 given in Bullock et al. (2012) equation 6, with the notation slightly modified. Here, z
 259 is the height above the ground, K is the von Karman constant, and u^* is the friction
 260 velocity. The zero-plane displacement d and roughness length z_0 are surface roughness
 261 parameters that, for a grass canopy height h above the ground, are approximated by
 262 $d \approx 0.7h$ and $z_0 \approx 0.1h$. These estimates are from Raupach (1994) for a canopy area
 263 index $\Lambda = 1$ in which the sum of grass canopy elements is equal to the unit area being
 264 measured. A 0.15 m grass height at the study site gives $d = 0.105$ and z_0 , which are
 265 suitable approximations for grassland (Wiernga 1993). Calculations of u^* were done
 266 using equation A2 from Skarpaas and Shea (2007), in which

$$267 \quad u^* = KU_m \left[\log \left(\frac{z_m - d}{z_0} \right) \right]^{-1} \quad (4)$$

268 and U_m is the mean wind velocity at the measurement height z_m . Values for the turbulent
 269 flow parameter σ were then calculated using the estimate made by Skarpaas and Shea
 270 (2007) in their equation A4, where

$$271 \quad \sigma = 2A_w^2 \sqrt{\frac{K(z-d)u^*}{C_0U}} \quad (5)$$

272 and C_0 is the Kolmogorov constant. A_w is a constant that relates vertical turbulence
 273 to friction velocity and is approximately equal to 1.3 under the assumptions of above-
 274 canopy flow made by Skarpaas and Shea (2007), based off calculations from Hsieh and
 275 Katul (2005). In addition, the assumption that $z = H$ was made in order to make the
 276 calculation of σ more feasible.

277 The values from the previous three equations give us the necessary information to

278 calculate μ' and λ' , thus allowing us to create the WALD distribution $p(r)$. However, the
 279 base WALD model does not take into account variation in wind speeds or seed terminal
 280 velocities, which limits its applicability in systems where such variation is present. In
 281 order to account for this variation, we integrate the WALD model over distributions these
 282 two variables using the same method as Skarpaas and Shea (2007). The WALD model
 283 assumes seed release from a single point source, though, which is not realistic for a shrub;
 284 because seeds are released across the entire height of the shrub rather than from a point
 285 source, $p(r)$ was also integrated across the uniform distribution from the grass canopy
 286 height to the shrub height. Thus, under the assumptions that the height at which a
 287 seed is located does not affect its probability of being released and that seeds are evenly
 288 distributed throughout the shrub, this gives the dispersal kernel $K(r)$, where

$$289 \quad K(r) = \iiint p(F)p(U)p(z)p(r) dF dU dz \quad (6)$$

290 and $p(F)$ and $p(U)$ are the PDFs of the terminal velocity F and wind speed U , respec-
 291 tively, and $p(z)$ is the uniform distribution from h to H .

292 The distribution $p(F)$ in the integral above was constructed using experimentally
 293 determined seed terminal velocities. This was done by using a high-speed camera and
 294 motion tracking software to determine position as a function of time, and then using the
 295 Levenberg-Marquardt algorithm to solve a quadratic-drag equation of motion for F . Be-
 296 fore seeds were released, they were dried and then dyed with yellow fluorescent powder,
 297 and then put against a black background to improve visibility and make tracking easier.
 298 While the powder added mass to the seeds, this added mass only yielded an approxi-
 299 mately 2.5% increase and was thus negligible, likely having little effect on their terminal
 300 velocities. Measurements were conducted for 48 seeds that were randomly chosen from a
 301 seed pool derived from different plants, and then an empirical PDF of terminal velocities
 302 was constructed using the data. Constructing $p(U)$ involved creating an empirical PDF

of hourly wind speeds at Five Points, the site closest to the 12 transects being used, that were obtained from meteorological data collected at the Sevilleta National Wildlife Refuge from 1988 to 2010. We did not weight $p(U)$ and assumed that the probability seed release from the shrub is the same regardless of wind speed.

Wave model using spatial integral projection models

Given that the shrub population at this site is approximately homogeneous perpendicular to the direction of encroachment, expansion is modelled as a wave moving in one dimension. A spatial integral projection model (SIPM) is used to estimate the speed at which encroachment occurs; such a model incorporates the effects of variation in traits like plant size that stage-structured models, such as those described in Neubert and Caswell (2000), do not capture. According to Jonjégans et al. (2011), a general SIPM can be formulated as

$$\mathbf{n}(x_2, z_2, t + 1) = \iint \tilde{K}(x_2, x_1, z_2, z_1) \mathbf{n}(x_1, z_1, t) dx_1 dz_1 \quad (7)$$

where x_1 and x_2 are locations of individuals of a particular size before and after one unit of time, and z_1 and z_2 are the respective sizes. The vector \mathbf{n} indicates the population density of each size, and \tilde{K} is a kernel that combines dispersal with demography. Though this SIPM represents a continuous spectrum of shrub sizes and densities, it was implemented by discretising the above integral with a 200 x 200 matrix, as this makes calculations significantly more tractable.

Movement of the wave is determined by the components of the combined dispersal-demography kernel \tilde{K} , which is of the same form as that used in Jonjégans et al. (2011). Here,

$$\tilde{K}(x_2, x_1, z_2, z_1) = K(x_2 - x_1)Q(z_2 - z_1) + \delta(x_2 - x_1)G(z_2 - z_1) \quad (8)$$

and K is the dispersal kernel, Q a reproduction function, G a growth function, and δ

the Dirac delta function. G is derived from the model for annual growth ratio, and Q is derived from the reproductive structures model as well as other factors including number of seeds per reproductive structure, probability of recruitment from seed, and recruit size. Both G and Q give the probability of transition between sizes; in the case of G , this is the probability of growing from one specific size to another, and in the case of Q the probability that an individual of a specific size produces a recruit of a specific size. The product of K and Q represents the production and dispersal of motile propagules, while the product of G and δ represents the growth of sessile individuals.

Given growth function G and the reproduction function Q , the speed of the moving wave can be calculated as

$$c^* = \min_{s>0} \left[\frac{1}{s} \ln(\rho_s) \right] \quad (9)$$

where s is the wave shape parameter and ρ_s is the dominant eigenvalue of the kernel \mathbf{H}_s (Jonjégans et al. 2011). This estimate for the wavespeed is valid under the assumption that population growth decreases monotonically as conspecific density increases, with the highest rates of growth occurring at the lowest population densities (Lewis et al. 2006). The kernel \mathbf{H}_s is defined as

$$\mathbf{H}_s = M(s)Q(z_2 - z_1) + G(z_2 - z_1) \quad (10)$$

where $M(s)$ is the moment-generating function of the dispersal kernel (Jonjégans et al. 2011). For one-dimensional dispersal, this moment-generating function can be estimated as

$$M(s) = \frac{1}{N} \sum_{i=1}^n I_0(sr_i) \quad (11)$$

where r is the dispersal distance for each observation, and I_0 is the modified Bessel function of the first kind and zeroth order (Skarpaas and Shea 2007). In order to obtain M , numerous dispersal distances were simulated from the dispersal kernel $K(r)$ described

in the previous section, with over 2000 replications for each shrub height increment of 1 cm. This was performed over the range from the lowest possible dispersal height to the maximum shrub height. Once $M(s)$ was obtained for dispersal at each shrub height, \mathbf{H}_s and c^* were calculated for each value of s ; this was done for values of s ranging from 0 to 2, as it is this range in which c^* occurs.

Results

Encroachment re-surveys

Figure ??.

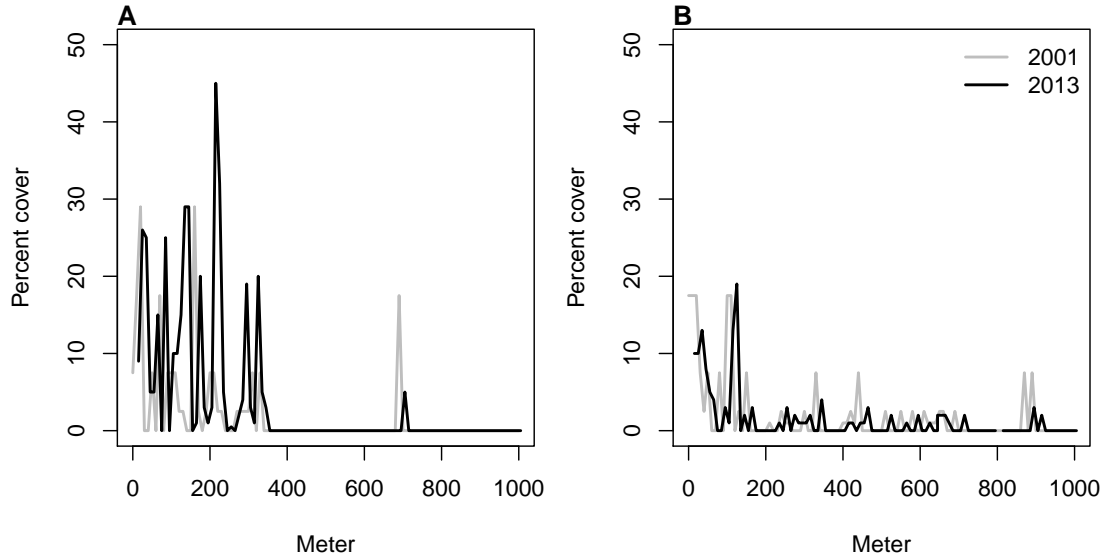


Figure 1: Re-surveys of shrub cover along two permanent transects (A,B) surveyed in 2001 and 2013.

The speed of encroachment at the study site as estimated by the SIPM is rather slow; as can be seen in Figure ??, the low-density wavefront moves at approximately 0.5 cm/yr under normal conditions and at 1 cm/yr under the best seedling survival conditions observed in the dataset. These improved conditions were observed due to above-average rainfall that occurred after greenhouse-grown seedlings were transplanted

364 to the site. Population growth in this low-density region of the moving wave is also low,
 365 with a geometric growth rate of $\lambda \approx 1.006$ and even lower rates of growth the higher-
 366 density regions behind; in the higher-survival scenario the maximum rate increases to
 367 $\lambda \approx 1.013$, with growth still decreasing as density increases. For both scenarios, the
 368 decrease in population growth rate with increasing density was monotonic across the
 369 range of observed standardised densities, as is shown in Figure ???. This suggests that
 370 an Allee effect is likely not present in this population, as the highest rate of population
 371 growth is found at the lowest density vanguard of the encroaching population. Thus, the
 372 conditions necessary for equation 9 to be valid are satisfied, and these wavespeeds are
 373 applicable for a pulled-wave scenario in which no Allee effects are present.

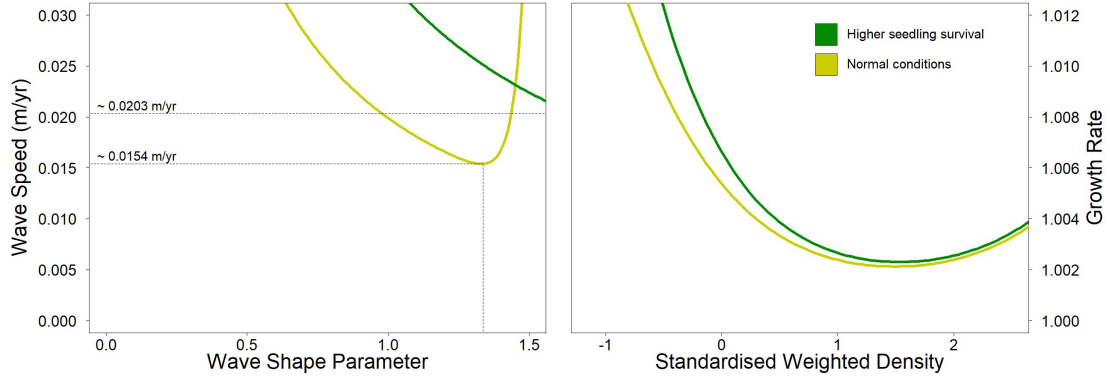


Figure 2: Estimated encroachment wave speeds (left) and geometric rates of population growth (right) for higher post-rainfall seedling survival and normal conditions.

374 As the speed of encroachment is quite limited, so is the extent of wind dispersal.
 375 Long distance dispersal events, while more common for taller shrubs than their shorter
 376 counterparts, are still uncommon overall. For the tallest shrub height of 1.98 m, only
 377 0.32% of propagules exceed a dispersal distance of 5 m, and 0.02% exceed 10 m. At 1
 378 m, or approximately half the tallest shrub height, long distance dispersal is even less
 379 likely, with 0.0046% of propagules exceeding a dispersal distance of 5 m and 0.0009%
 380 exceeding 10 m. Given that the median shrub height is only 0.64 m, the occurrence of

381 long-distance wind dispersal in most of the shrub population is highly improbable, and
382 the few instances in which it occurs will only be limited to the tallest shrubs. Thus,
383 as Figure ?? demonstrates, shorter dispersal distances dominate; even for the tallest
384 shrub, 81% of seeds fall within only a metre of the plant, and this percentage increases
385 as shrub height decreases. Dispersal kernels have their highest probability density at
386 dispersal distances between 2 and 8 cm from the shrub; here, as shrub height increases,
387 the most probable dispersal distance slightly increases while maximum probability density
388 decreases. Regardless of the shrub height, most dispersal will occur very close to the
389 plant, though increases in shrub height dramatically increase the likelihood of dispersal
390 at longer distances. It is clear that the shape of the height-dependent dispersal kernel
391 $K(r)$ varies greatly among the shrub population given the large range of shrub heights
392 observed; shrubs at lower heights have more slender kernels with most of the seeds
393 dispersing closer to the plant, while taller shrubs have kernels with much fatter tails and
394 are more capable of longer-distance dispersal.

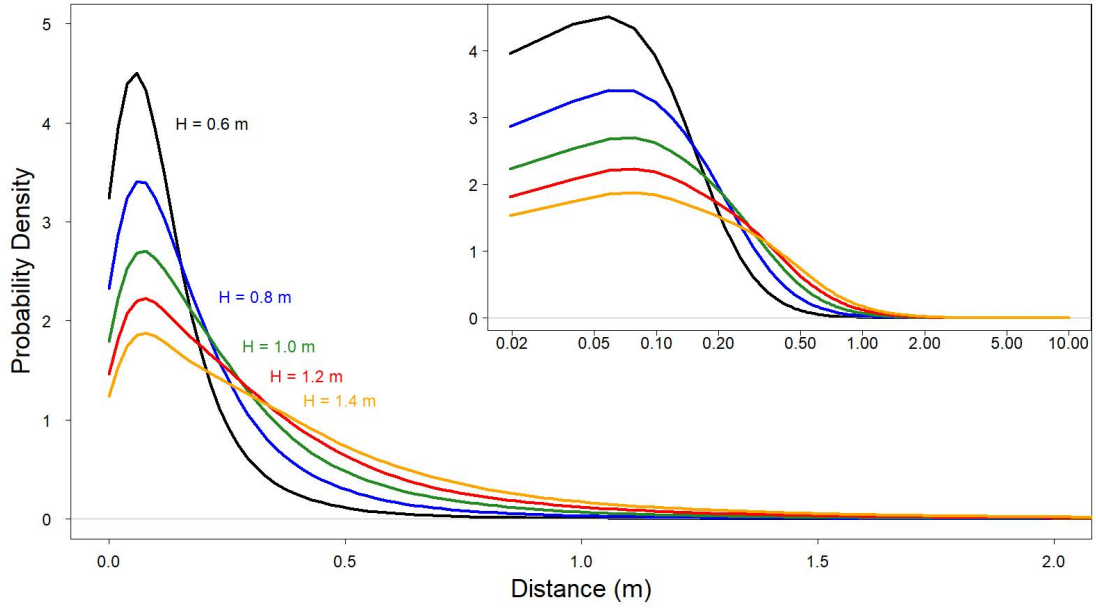


Figure 3: Dispersal kernels, with each colour representing a selected shrub height. The inset plot is the same as the large plot, though with a logarithmic x-axis to more easily show differences in dispersal probability at smaller distances.

395 Density and size dependence are evident in all 4 of the demographic rates, with
 396 coefficients for each model displayed in Table 2. For growth, reproduction, and survival,
 397 density dependence is mostly negative and monotonic; this is not the case for probability
 398 of flowering, where shrub size seems to be more important than the effects of density alone
 399 and suggests that larger shrubs have a higher probability of flowering than their smaller
 400 counterparts. This, along with size and density dependence in growth and reproduction,
 401 is shown in Figure ?? . Size dependence is positive for reproduction, as would be expected
 402 since larger plants typically produce more flowers and fruits. However, annual growth
 403 decreases as size increases; this could be in part due to the annual growth in this study
 404 being quantified as a proportion relative to the shrub's initial size. While larger shrubs
 405 may produce more plant material over a year in terms of absolute volume, smaller shrubs
 406 produce less but can still have higher annual growth in terms of the percentage of volume

407 added relative to their initial volume. When compared to density, shrub size is a much
408 stronger predictor of survival, with significant differences in mortality rates depending on
409 shrub size. For small shrubs, mortality is exceptionally high, and increases in volume for
410 these shrubs only slightly increase the likelihood of survival. However, after shrubs reach
411 a logarithmic volume of approximately 7.3, they are almost guaranteed to survive, with
412 survival rates near 100% persisting regardless of any further size increases. Interestingly,
413 though most recruits were found at lower densities, the probability of recruitment from
414 seed displays positive density dependence; the probability of recruitment was still very
415 low, though, with a baseline rate of approximately 2 recruits per 10,000 seeds.

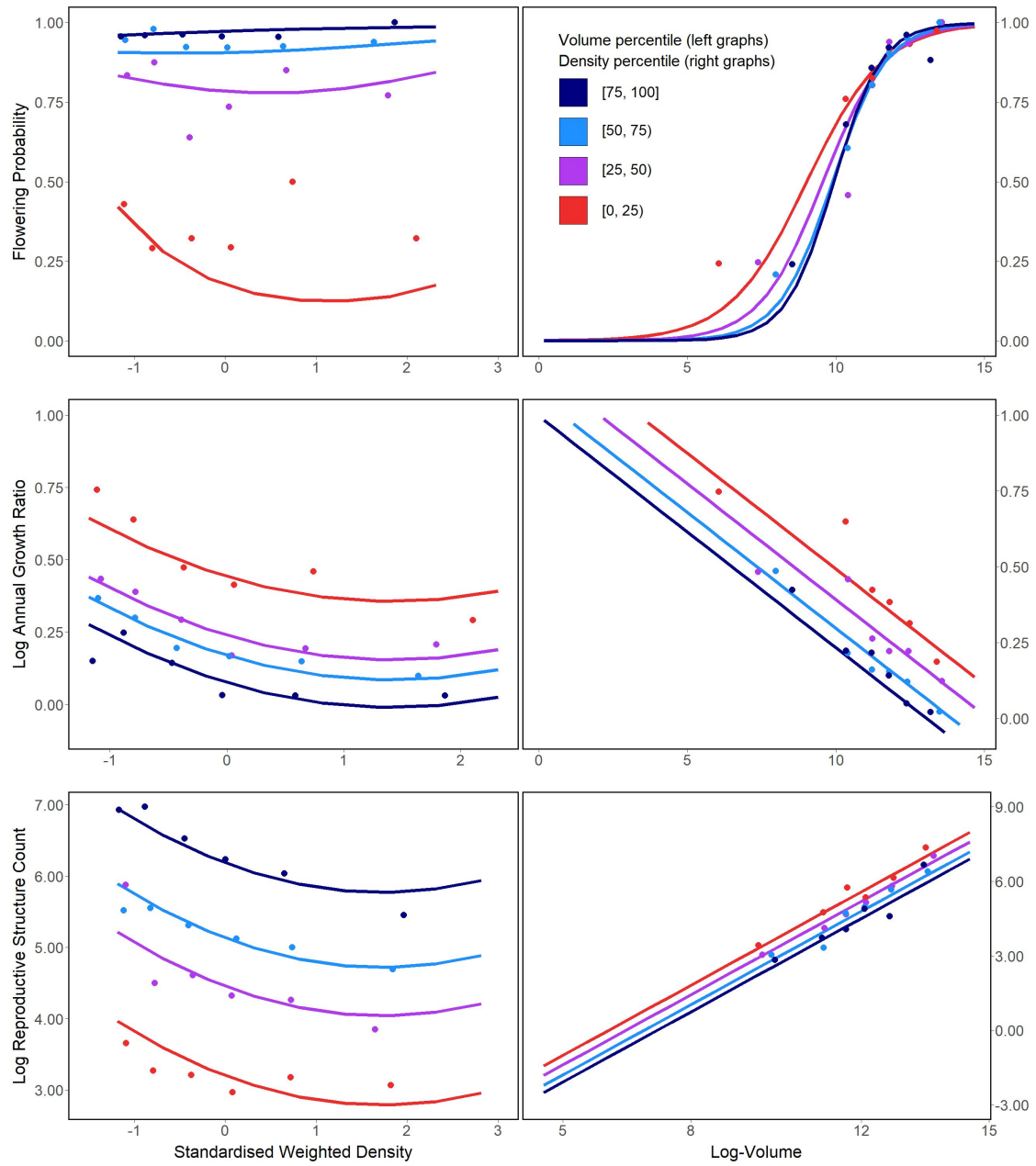


Figure 4: Flowering probability (top row), log annual growth ratio (centre row), and log reproductive structure count (bottom row) at all four sampling sites. In the left column of graphs, the three response variables are shown as a function of density for each of four volume quartiles, with each quartile containing six density bins; in the right column, the opposite occurs, with response variables shown as functions of four volume quartiles that each contain six density bins. Graphs quantifying the number of reproductive structures include data only on plants that flowered.

Discussion

The slow movement of the encroaching creosotebush wave at the Sevilleta LTER site can likely be contributed to a combination of three factors: short dispersal distances with extremely limited long-distance dispersal events, very low probability of recruitment from seed, and high seedling mortality. These three barriers, when combined, form a formidable challenge to the establishment of new shrubs at the low-density front of the wave. First, a seed must travel far enough to avoid competition with the parent shrub, which is unlikely given the dispersal kernels shown in Figure 2. Even if the seed manages to be dispersed this far, its chances of becoming a seedling are low. Caching and consumption by seed-eaters such as a variety of seed-harvesting ants (Whitford et al. 1978, 1980; Lei 1999) and the kangaroo rat *Dipodomys merriami* (Chew and Chew 1970) decreases the amount of seeds available for germination. However, reduction in germination caused by destruction of seeds may be partly mitigated by the more favourable germination conditions that these seeds can experience when cached underground (Chew and Chew 1970). Many of the remaining seeds will still fail to germinate, and in the unlikely event that germination does occur, seedlings will likely die given the high rates of mortality observed in smaller shrubs. Such high rates of creosotebush seedling mortality have been observed in other studies as well (Boyd and Brum 1983; Bowers et al. 2004), probably due to a combination of herbivory, competition, and abiotic stresses.

However, as low as they are, the wavespeed estimates given in this paper are still conservative estimates for reasons mostly related to dispersal. First, it is important to note that the dispersal kernels used here, while they account for variation in factors such as wind speed and terminal velocity, may underestimate the distances that shrub propagules travel. Because the WALD model assumes that terminal velocity is reached immediately upon seed release, seeds in the estimate thus take a shorter time to fall and have less time to be transported by wind, and the true frequency of long-distance

442 dispersal events may thus be greater than what is estimated here. Second, dispersal at the
443 study site could occur through additional mechanisms other than wind. For example,
444 secondary dispersal through runoff from significant rainfall events can transport seeds
445 (Thompson et al. 2014), and given that long-distance dispersal by bird and subsequent
446 species divergence is thought to be responsible for creosotebush being in North America
447 in the first place (Wells and Hunziker 1976), short-distance dispersal by other animals
448 at the study site likely occurs. As mentioned above, seeds are transported by seed-
449 harvesting ants and granivorous mammals, where they are often stored in caches that
450 can be appreciable distances from the parent shrubs. Whether transportation occurs via
451 ant or rodent, creosotebush seeds can be moved significantly further than wind alone
452 can, though many of these seeds are eventually consumed.

453 Despite the more conservative estimates our model yields, the estimated rate of dis-
454 persal in creosotebush populations at the Sevilleta National Wildlife Refuge is consistent
455 with observations from the past 50-60 years, as creosotebush expansion during this time
456 has been minimal (Moreno-de las Heras et al. 2016). However, it cannot explain the
457 long-term increases in creosotebush cover at the study site, as total encroachment over
458 the past 150 years is much greater than what would be expected given the encroachment
459 rates derived by our models. Such a discrepancy is likely due to much of the expansion
460 occurring in an episodic fashion, with short times during which rapid encroachment oc-
461 curs due to favourable environmental conditions. This could be due in part to seedling
462 recruitment, which is a factor that strongly limits creosotebush expansion, being rare
463 and episodic. For example, Allen et al. (2008) estimate that a major recruitment event
464 occurred at this site in the 1950s, which is supported by photographic evidence from
465 Milne et al. (2003) of a drought-driven expansion during this time. Moreno-de las Heras
466 et al. (2016) estimate that after this expansion, several smaller creosotebush recruitment
467 events occurred in decadal episodes. However, such events can be highly localised and
468 may not necessarily occur at the low-density front of encroachment, which could explain

469 how these recruitment events can still coexist with lack of encroachment in the recent
470 past.

471 Overall, our observations and model highlight three aspects of creosotebush encroach-
472 ment that should be the focus of future studies seeking to obtain better estimates of
473 encroachment rates. First, negative density dependence in survival, growth, and repro-
474 duction is demonstrated, along with size dependence. The clear dependence on size and
475 conspecific density suggests that they both should be considered when estimating cre-
476 osotebush expansion and quantifying the demographic variation that contributes to it.
477 Second, wind dispersal in these shrubs is quite limited; though the dispersal kernels seen
478 here are typical in the sense that they are characterised by high near-plant dispersal and
479 exceptionally low long-distance dispersal, the scale across which such dispersal occurs
480 is small, with most seeds landing within only 1 m of the shrub. Wind dispersal alone
481 may be an underestimate of the true amount of dispersal occurring, and future work
482 should seek to incorporate the effects of dispersal by runoff and animals so that a more
483 representative model of total dispersal can be obtained. Finally, encroachment is slow or
484 even stagnates, but only most of the time. Though our encroachment speed estimates
485 are representative of creosotebush populations for most years, the significant expansion
486 seen over larger time scales suggests that there is episodic expansion in other years; while
487 our model is consistent with the recent stagnation in creosotebush encroachment at the
488 Sevilleta LTER site, a model that also includes interannual variability in factors such
489 as survival and recruitment would be able to better account for instances of episodic
490 population expansion that are characteristic of this location.

491 **Acknowledgements**

492 **Author contributions**

493 **Data accessibility**