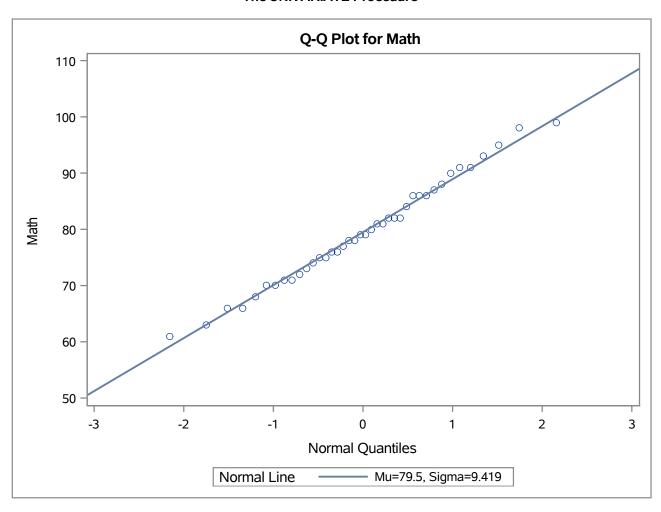


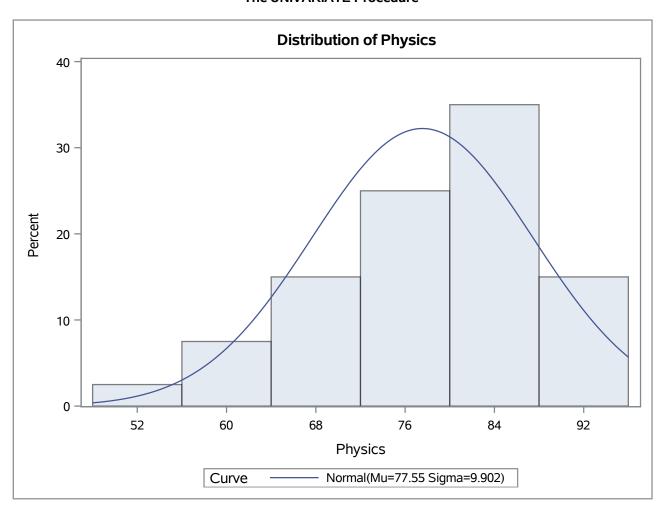
## The UNIVARIATE Procedure **Fitted Normal Distribution for Math**

Parameters for Normal Distribution				
Parameter Symbol Estimate				
Mean	Mu	79.5		
Std Dev	Std Dev Sigma 9.41902			

Goodness-of-Fit Tests for Normal Distribution					
Test	Statistic p Value				
Kolmogorov-Smirnov	D	0.07034282	Pr > D	>0.150	
Cramer-von Mises	W-Sq	0.01815604	Pr > W-Sq	>0.250	
Anderson-Darling	Anderson-Darling				

Quantiles for Normal Distribution			
	Qua	ntile	
Percent	Observed	Estimated	
1.0	61.0000	57.5881	
5.0	64.5000	64.0071	
10.0	67.0000	67.4290	
25.0	72.5000	73.1470	
50.0	79.0000	79.5000	
75.0	86.0000	85.8530	
90.0	92.0000	91.5710	
95.0	96.5000	94.9929	
99.0	99.0000	101.4119	



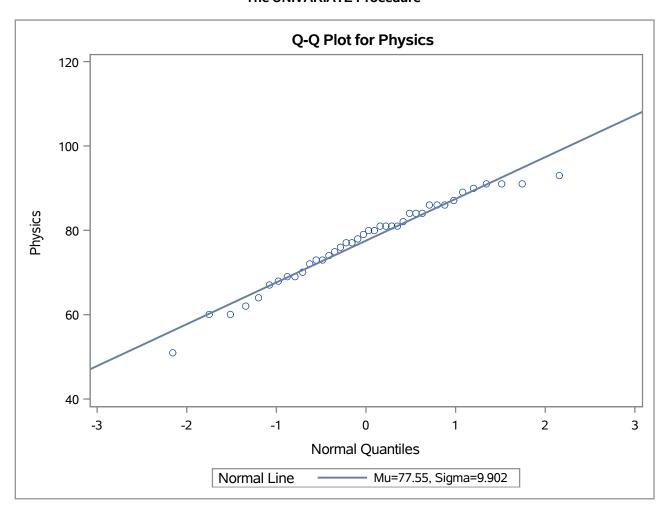


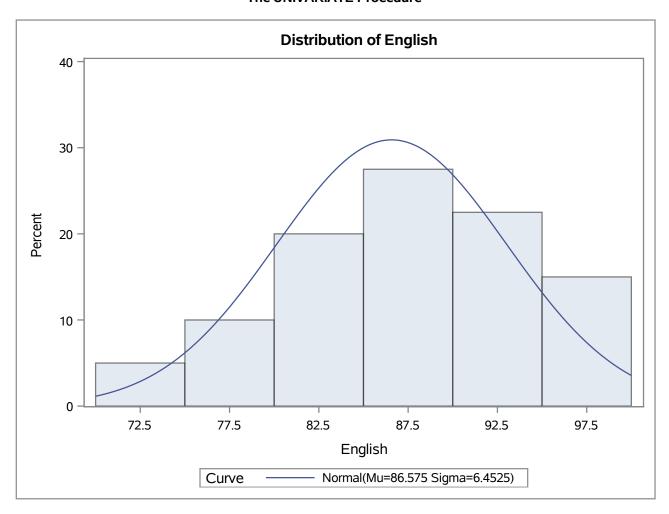
# The UNIVARIATE Procedure **Fitted Normal Distribution for Physics**

Parameters for Normal Distribution				
Parameter Symbol Estimate				
Mean Mu 77.55				
<b>Std Dev</b> Sigma 9.901955				

Goodness-of-Fit Tests for Normal Distribution				
Test	Statistic p Value			
Kolmogorov-Smirnov	D	0.09771068	Pr > D	>0.150
Cramer-von Mises	W-Sq	0.05623708	Pr > W-Sq	>0.250
Anderson-Darling	A-Sq	0.38133060	Pr > A-Sq	>0.250

Quantiles for Normal Distribution			
	Qua	ntile	
Percent	Observed	Estimated	
1.0	51.0000	54.5146	
5.0	60.0000	61.2627	
10.0	63.0000 64.8601		
25.0	71.0000 70.8712		
50.0	79.5000 77.5500		
75.0	85.0000	84.2288	
90.0	90.5000	90.2399	
95.0	91.0000	93.8373	
99.0	93.0000	100.5854	



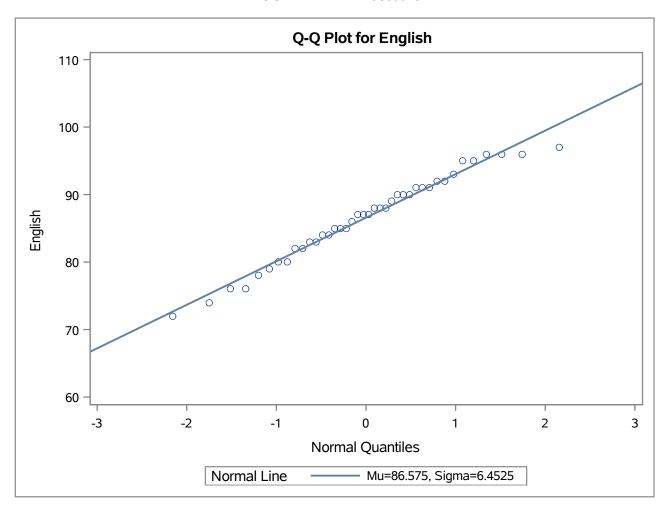


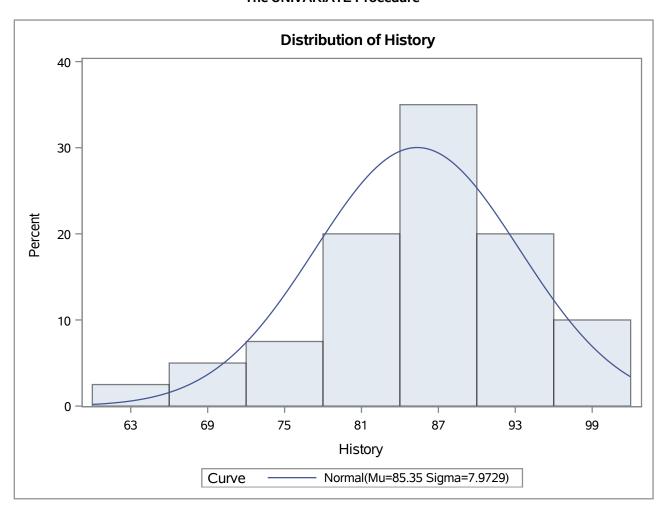
# The UNIVARIATE Procedure **Fitted Normal Distribution for English**

Parameters for Normal Distribution				
Parameter Symbol Estimate				
<b>Mean</b> Mu 86.575				
<b>Std Dev</b> Sigma 6.452539				

Goodness-of-Fit Tests for Normal Distribution				
Test	Statistic p Value			
Kolmogorov-Smirnov	D	0.07722090	Pr > D	>0.150
Cramer-von Mises	W-Sq	0.03448985	Pr > W-Sq	>0.250
Anderson-Darling	A-Sq	0.27124408	Pr > A-Sq	>0.250

Quantiles for Normal Distribution			
	Qua	ntile	
Percent	Observed	Estimated	
1.0	72.0000	71.5642	
5.0	75.0000	75.9615	
10.0	77.0000	78.3057	
25.0	82.5000	82.2228	
50.0	87.0000	86.5750	
75.0	91.0000	90.9272	
90.0	95.5000	94.8443	
95.0	96.0000	97.1885	
99.0	97.0000	101.5858	



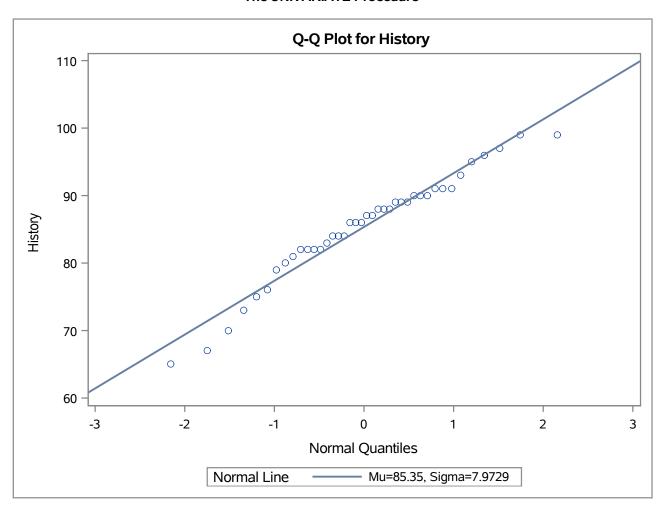


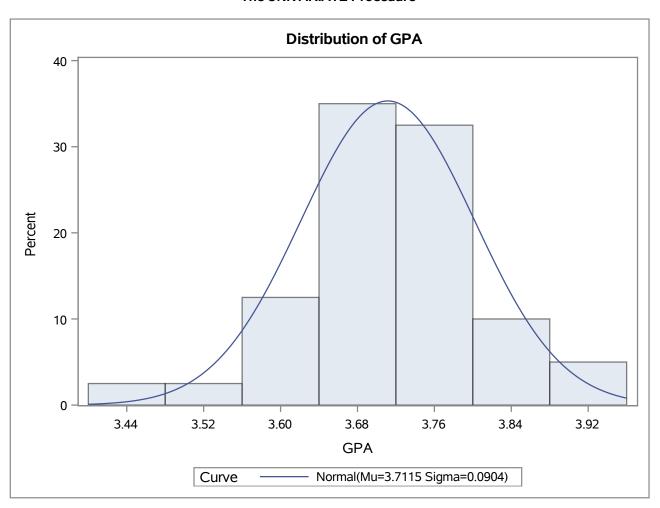
# The UNIVARIATE Procedure **Fitted Normal Distribution for History**

Parameters for Normal Distribution				
Parameter Symbol Estimate				
Mean Mu 85.35				
Std Dev         Sigma         7.972871				

Goodness-of-Fit Tests for Normal Distribution				
Test	Statistic p Value			
Kolmogorov-Smirnov	D	0.11217885	Pr > D	>0.150
Cramer-von Mises	W-Sq	0.09133680	Pr > W-Sq	0.144
Anderson-Darling	<b>A-Sq</b> 0.55936397 <b>Pr &gt; A-Sq</b> 0.14			

Quantiles for Normal Distribution			
	Qua	ntile	
Percent	Observed	Estimated	
1.0	65.0000	66.8023	
5.0	68.5000	72.2358	
10.0	74.0000	75.1324	
25.0	82.0000	79.9724	
50.0	86.5000	85.3500	
75.0	90.0000	90.7276	
90.0	95.5000	95.5676	
95.0	98.0000	98.4642	
99.0	99.0000	103.8977	



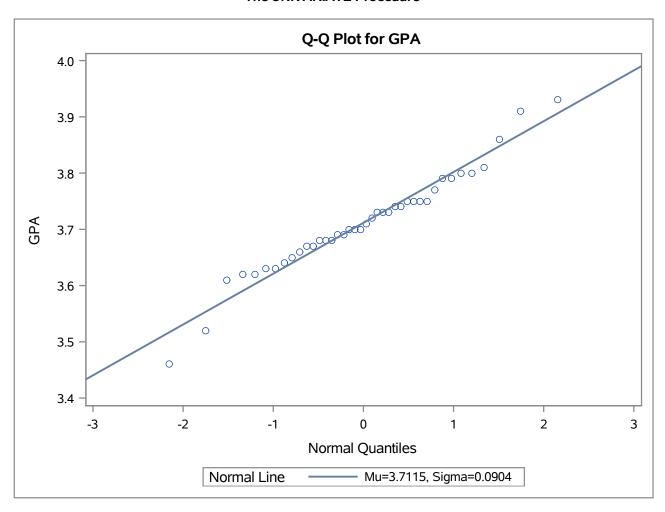


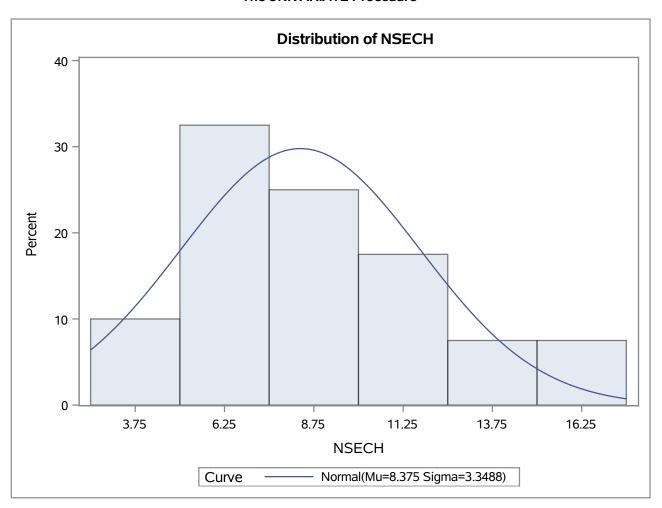
## The UNIVARIATE Procedure **Fitted Normal Distribution for GPA**

Parameters for Normal Distribution					
Parameter Symbol Estimate					
<b>Mean</b> Mu 3.7115					
Std Dev	Sigma	0.090371			

Goodness-of-Fit Tests for Normal Distribution							
Test	Statistic p Value						
Kolmogorov-Smirnov	D	0.11004610	Pr > D	>0.150			
Cramer-von Mises	W-Sq	0.06150884	Pr > W-Sq	>0.250			
Anderson-Darling	A-Sq	0.45370026	Pr > A-Sq	>0.250			

Quantiles for Normal Distribution					
	Qua	ntile			
Percent	Observed	Estimated			
1.0	3.46000	3.50127			
5.0	3.56500	3.56285			
10.0	3.62000	3.59568			
25.0	3.66500 3.650				
50.0	3.70500 3.7115				
75.0	3.75000 3.77245				
90.0	3.80500 3.8273				
95.0	3.88500 3.8601				
99.0	3.93000	3.92173			



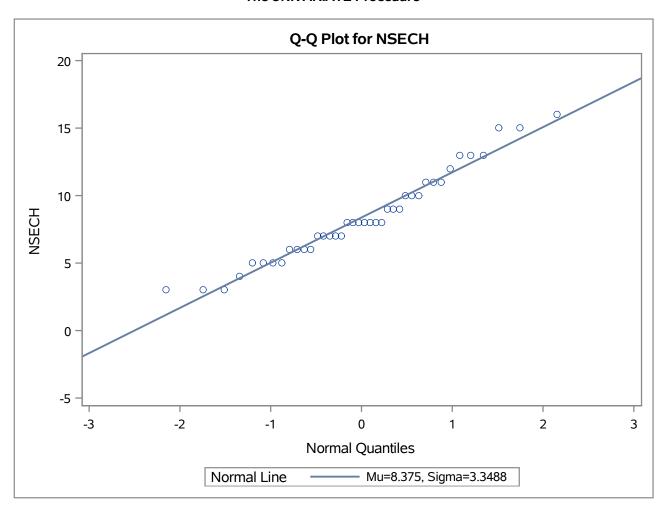


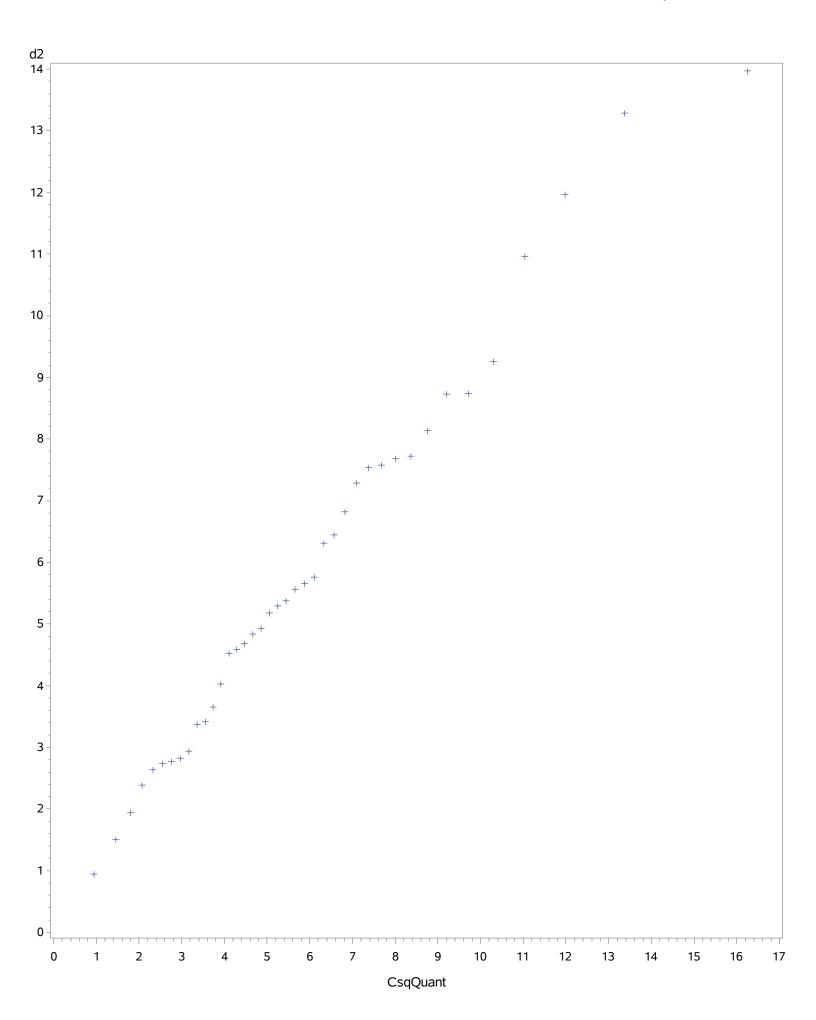
## The UNIVARIATE Procedure **Fitted Normal Distribution for NSECH**

Parameters for Normal Distribution					
Parameter Symbol Estimate					
Mean	Mu	8.375			
Std Dev	Sigma	3.348842			

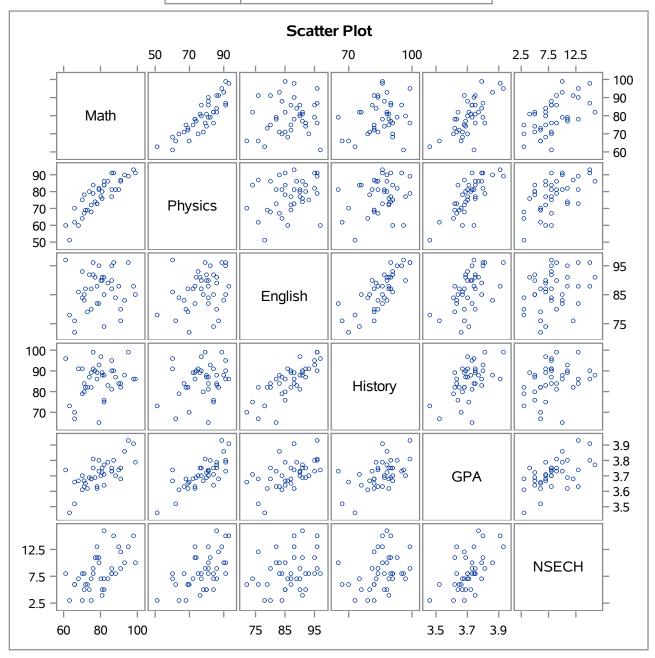
Goodness-of-Fit Tests for Normal Distribution							
Test Statistic p Value							
Kolmogorov-Smirnov	D	0.14457997	Pr > D	0.034			
Cramer-von Mises	W-Sq	0.08399038	Pr > W-Sq	0.185			
Anderson-Darling	A-Sq	0.50346808	Pr > A-Sq	0.202			

Quantiles for Normal Distribution					
	Qua	ntile			
Percent	Observed	Estimated			
1.0	3.00000	0.58443			
5.0	3.00000	2.86664			
10.0	4.50000	4.08329			
25.0	6.00000 6.116				
50.0	8.00000 8.3750				
75.0	10.50000	10.63376			
90.0	13.00000 12.6667				
95.0	15.00000 13.8833				
99.0	16.00000	16.16557			





6 Variables: Math Physics English History GPA **NSECH** 



Covariance Matrix, DF = 39								
	Math Physics English History							
Math	88.71794872	80.64102564	8.34615385	17.87179487				
Physics	80.64102564	98.04871795	18.23974359	20.36666667				
English	8.34615385	18.23974359	41.63525641	40.48589744				
History	17.87179487	20.36666667	40.48589744	63.56666667				

Simple Statistics									
Variable	able N Mean Std Dev Sum Minimum M								
Math	40	79.50000	9.41902	3180	61.00000	99.00000			
Physics	40	77.55000	9.90196	3102	51.00000	93.00000			
English	40	86.57500	6.45254	3463	72.00000	97.00000			
History	40	85.35000	7.97287	3414	65.00000	99.00000			

Pearson Correlation Coefficients, N = 40 Prob >  r  under H0: Rho=0									
	Math Physics English History								
Math	1.00000	0.86463 <.0001	0.13733 0.3981	0.23798 0.1392					
Physics	0.86463 <.0001	1.00000	0.28547 0.0742	0.25798 0.1080					
English	0.13733 0.3981	0.28547 0.0742	1.00000	0.78697 <.0001					
History	0.23798 0.1392	0.25798 0.1080	0.78697 <.0001	1.00000					

	Pearson Correlation Statistics (Fisher's z Transformation)							
Variable	With Variable	N	Sample Correlation	Fisher's z	95% Confid	95% Confidence Limits		
Math	Physics	40	0.86463	1.31140	0.757012	0.926574	<.0001	
Math	English	40	0.13733	0.13820	-0.181968	0.430422	0.4006	
Math	History	40	0.23798	0.24264	-0.079413	0.511569	0.1400	
Physics	English	40	0.28547	0.29363	-0.028576	0.548231	0.0741	
Physics	History	40	0.25798	0.26394	-0.058208	0.527127	0.1084	
English	History	40	0.78697	1.06342	0.629874	0.882208	<.0001	

4 Variables: Math Physics English History

Covariance Matrix, DF = 39									
	Math Physics English History								
Math	88.71794872	80.64102564	8.34615385	17.87179487					
Physics	80.64102564	98.04871795	18.23974359	20.36666667					
English	8.34615385	18.23974359	41.63525641	40.48589744					
History	17.87179487	20.36666667	40.48589744	63.56666667					

Simple Statistics							
Variable	N	Mean	Std Dev	Sum	Minimum	Maximum	
Math	40	79.50000	9.41902	3180	61.00000	99.00000	
Physics	40	77.55000	9.90196	3102	51.00000	93.00000	
English	40	86.57500	6.45254	3463	72.00000	97.00000	
History	40	85.35000	7.97287	3414	65.00000	99.00000	

Pearson Correlation Coefficients, N = 40 Prob >  r  under H0: Rho=0							
Math Physics English Histor							
Math	1.00000	0.86463 <.0001	0.13733 0.3981	0.23798 0.1392			
Physics	0.86463 <.0001	1.00000	0.28547 0.0742	0.25798 0.1080			
English	0.13733 0.3981	0.28547 0.0742	1.00000	0.78697 <.0001			
History	0.23798 0.1392	0.25798 0.1080	0.78697 <.0001	1.00000			

	Pearson Correlation Statistics (Fisher's z Transformation)									
Variable	With Variable	N	Sample Correlation	Fisher's z	99.17% Confidence Limits		p Value for H0:Rho=0			
Math	Physics	40	0.86463	1.31140	0.705249	0.940818	<.0001			
Math	English	40	0.13733	0.13820	-0.287216	0.516772	0.4006			
Math	History	40	0.23798	0.24264	-0.188799	0.589150	0.1400			
Physics	English	40	0.28547	0.29363	-0.139186	0.621447	0.0741			
Physics	History	40	0.25798	0.26394	-0.168172	0.602886	0.1084			
English	History	40	0.78697	1.06342	0.557843	0.904632	<.0001			

6 Variables: Math Physics English History GPA NSECH

	Covariance Matrix, DF = 39								
Math Physics English		English	History	GPA	NSECH				
Math	88.71794872	80.64102564	8.34615385	17.87179487	0.59358974	18.03846154			
Physics	80.64102564	98.04871795	18.23974359	20.36666667	0.68351282	18.68589744			
English	8.34615385	18.23974359	41.63525641	40.48589744	0.31116667	6.54807692			
History	17.87179487	20.36666667	40.48589744	63.56666667	0.38869231	8.48076923			
GPA	0.59358974	0.68351282	0.31116667	0.38869231	0.00816692	0.17173077			
NSECH	18.03846154	18.68589744	6.54807692	8.48076923	0.17173077	11.21474359			

varnames	xbar Math	mu0
Math	79.5	77.7
Physics	77.55	74.8
English	86.575	86.3
History	85.35	85.1
GPA	3.7115	3.62
NSECH	8.375	6.7

The SAS System

t2	f	fcrit	df1	df2	pval
107.29477	15.589838	2.3803127	6	34	1.6612E-8

varnames	Lol	Upl	LoB	UpB	LoT	UpT
Math	76.487651	82.512349	75.360451	83.639549	73.472167	85.527833
Physics	74.383201	80.716799	73.198206	81.901794	71.213106	83.886894
English	84.511378	88.638622	83.739185	89.410815	82.445608	90.704392
History	82.800152	87.899848	81.846017	88.853983	80.247651	90.452349
GPA	3.6825979	3.7404021	3.671783	3.751217	3.6536658	3.7693342
NSECH	7.3039883	9.4460117	6.903223	9.846777	6.2318619	10.518138

# The MEANS Procedure

The SAS System

# Vars=Engl

Analysis Variable : Ratio					
N	Mean	Std Dev	Minimum	Maximum	
40	1.0031866	0.0747687	0.8342990	1.1239861	

#### Vars=GPA

Analysis Variable : Ratio						
N	Mean	Std Dev	Minimum	Maximum		
40	1.0252762	0.0249644	0.9558011	1.0856354		

### Vars=Hist

	Analysis Variable : Ratio						
N Mean		Std Dev	Minimum	Maximum			
40	1.0029377	0.0936883	0.7638073	1.1633373			

#### Vars=Math

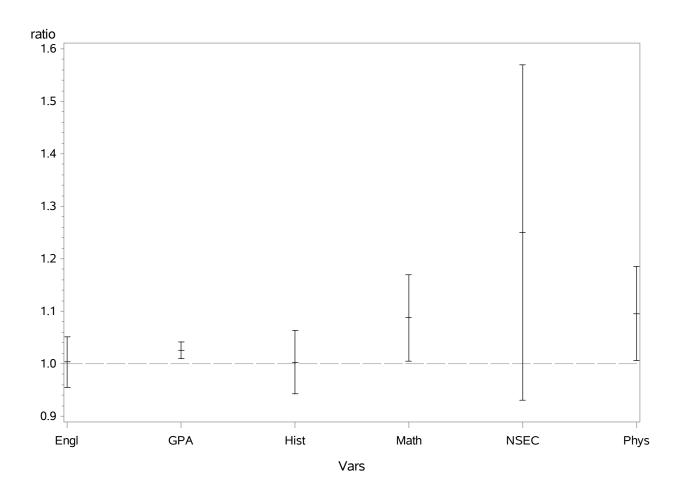
	Analysis Variable : Ratio						
ı	1	Mean	Std Dev	Minimum	Maximum		
40	0	1.0875513	0.1288512	0.8344733	1.3543092		

#### Vars=NSEC

	Analysis Variable : Ratio						
N	Mean	Std Dev	Minimum	Maximum			
40	1.2500000	0.4998272	0.4477612	2.3880597			

### Vars=Phys

	Analysis Variable : Ratio					
N	Mean	Std Dev	Minimum	Maximum		
40	1.0953390	0.1398581	0.7203390	1.3135593		



# AdvM=No

4 Variables: Math Physics English History

Covariance Matrix, DF = 19						
	Math Physics English Histor					
Math	47.71315789	51.69736842	2.15000000	3.38947368		
Physics	51.69736842	86.51315789	12.19736842	6.36842105		
English	2.15000000	12.19736842	50.57631579	57.77894737		
History	3.38947368	6.36842105	57.77894737	91.74736842		

#### AdvM=Yes

4 Variables: Math Physics English History

Covariance Matrix, DF = 19						
	Math Physics English History					
Math	62.34473684	54.71315789	2.35789474	6.81578947		
Physics	54.71315789	66.23947368	14.88421053	13.71052632		
English	2.35789474	14.88421053	32.67368421	20.68421053		
History	6.81578947	13.71052632	20.68421053	29.00000000		

varnames	xbar1 Math	xbar2
Math	73.65	85.35
Physics	72.75	82.35
English	85.55	87.6
History	83.2	87.5

	S1 Col1	Col2	Col3	Col4	S2 Col5	Col6	Col7	Col8
ROW1	47.713158	51.697368	2.15	3.3894737	62.344737	54.713158	2.3578947	6.8157895
ROW2	51.697368	86.513158	12.197368	6.3684211	54.713158	66.239474	14.884211	13.710526
ROW3	2.15	12.197368	50.576316	57.778947	2.3578947	14.884211	32.673684	20.684211
ROW4	3.3894737	6.3684211	57.778947	91.747368	6.8157895	13.710526	20.684211	29

Sp					
55.028947	53.205263	2.2539474	5.1026316		
53.205263	76.376316	13.540789	10.039474		
2.2539474	13.540789	41.625	39.231579		
5.1026316	10.039474	39.231579	60.373684		

t2	fstat	df1	df2	pval
28.224229	6.4990001	4	35	0.0005078

varnames	Lol	Upl	LoB	UpB	LoT	UpT
Math	-16.44887	-6.951126	-17.85122	-5.54878	-19.64522	-3.754782
Physics	-15.19467	-4.005331	-16.84678	-2.353221	-18.9603	-0.239704
English	-6.180211	2.0802106	-7.399865	3.2998648	-8.960148	4.8601479
History	-9.27415	0.6741504	-10.74302	2.1430206	-12.62212	4.0221216

Class Level Information			
Class	Levels	Values	
AdvM	2	No Yes	

Number of Observations Read	40
Number of Observations Used	40

# **Dependent Variable: Math**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	1368.900000	1368.900000	24.88	<.0001
Error	38	2091.100000	55.028947		
Corrected Total	39	3460.000000			

R-Square	Coeff Var	Root MSE	Math Mean
0.395636	9.331006	7.418150	79.50000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
AdvM	1	1368.900000	1368.900000	24.88	<.0001

Source	DF	Type III SS	Mean Square	F Value	Pr > F
AdvM	1	1368.900000	1368.900000	24.88	<.0001

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
Difference	1	1368.900000	1368.900000	24.88	<.0001

Parameter	Estimate	Standard Error	t Value	Pr >  t
Difference	-11.7000000	2.34582496	-4.99	<.0001

# **Dependent Variable: Physics**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	921.600000	921.600000	12.07	0.0013
Error	38	2902.300000	76.376316		
Corrected Total	39	3823.900000			

R-Square	Coeff Var	Root MSE	Physics Mean
0.241010	11.26932	8.739354	77.55000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
AdvM	1	921.6000000	921.6000000	12.07	0.0013

Source	DF	Type III SS	Mean Square	F Value	Pr > F
AdvM	1	921.6000000	921.6000000	12.07	0.0013

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
Difference	1	921.6000000	921.6000000	12.07	0.0013

Parameter	Estimate	Standard Error	t Value	Pr >  t
Difference	-9.60000000	2.76362653	-3.47	0.0013

# Dependent Variable: English

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	42.025000	42.025000	1.01	0.3214
Error	38	1581.750000	41.625000		
Corrected Total	39	1623.775000			

R-Square	Coeff Var	Root MSE	English Mean
0.025881	7.452202	6.451744	86.57500

Source	DF	Type I SS	Mean Square	F Value	Pr > F
AdvM	1	42.02500000	42.02500000	1.01	0.3214

Source	DF	Type III SS	Mean Square	F Value	Pr > F
AdvM	1	42.02500000	42.02500000	1.01	0.3214

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
Difference	1	42.02500000	42.02500000	1.01	0.3214

Parameter	Estimate	Standard Error	t Value	Pr >  t
Difference	-2.05000000	2.04022058	-1.00	0.3214

# **Dependent Variable: History**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	184.900000	184.900000	3.06	0.0882
Error	38	2294.200000	60.373684		
Corrected Total	39	2479.100000			

R-Square	Coeff Var	Root MSE	History Mean
0.074584	9.103750	7.770050	85.35000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
AdvM	1	184.9000000	184.9000000	3.06	0.0882

Source	DF	Type III SS	Mean Square	F Value	Pr > F
AdvM	1	184.9000000	184.9000000	3.06	0.0882

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
Difference	1	184.9000000	184.9000000	3.06	0.0882

Parameter	Estimate	Standard Error	t Value	Pr >  t
Difference	-4.30000000	2.45710570	-1.75	0.0882

# The GLM Procedure **Multivariate Analysis of Variance**

E = Error SSCP Matrix						
	Math Physics English History					
Math	2091.1	2021.8	85.65	193.9		
Physics	2021.8	2902.3	514.55	381.5		
English	85.65	514.55	1581.75	1490.8		
History	193.9	381.5	1490.8	2294.2		

Partial Correlation Coefficients from the Error SSCP Matrix / Prob >  r							
DF = 38	Math	Physics	English	History			
Math	1.000000	0.820691 <.0001	0.047095 0.7759	0.088527 0.5920			
Physics	0.820691 <.0001	1.000000	0.240153 0.1409	0.147845 0.3691			
English	0.047095 0.7759	0.240153 0.1409	1.000000	0.782591 <.0001			
History	0.088527 0.5920	0.147845 0.3691	0.782591 <.0001	1.000000			

## The GLM Procedure **Multivariate Analysis of Variance**

H = Type III SSCP Matrix for AdvM					
	Math	Physics	English	History	
Math	1368.9	1123.2	239.85	503.1	
Physics	1123.2	921.6	196.8	412.8	
English	239.85	196.8	42.025	88.15	
History	503.1	412.8	88.15	184.9	

Characteristic Roots and Vectors of: E Inverse * H, where H = Type III SSCP Matrix for AdvM E = Error SSCP Matrix					
		Characteristic Vector V'EV=1			
Characteristic Root	Percent	Math	Physics	English	History
0.74274286	100.00	0.02786274	-0.00812904	0.00091540	0.00527934
0.00000000	0.00	-0.01475944	0.01021609	-0.03560975	0.03432812
0.00000000	0.00	-0.02591855	0.03141917	0.00079171	0.00000000
0.00000000	0.00	0.00465239	-0.01125210	0.02614008	0.00000000

#### MANOVATest Criteria and Exact F Statistics for the Hypothesis of No Overall AdvM Effect H = Type III SSCP Matrix for AdvM E = Error SSCP Matrix

#### S=1 M=1 N=16.5

Statistic	Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.57380812	6.50	4	35	0.0005
Pillai's Trace	0.42619188	6.50	4	35	0.0005
Hotelling-Lawley Trace	0.74274286	6.50	4	35	0.0005
Roy's Greatest Root	0.74274286	6.50	4	35	0.0005

H = Contrast SSCP Matrix for Difference					
	Math	Physics	English	History	
Math	1368.9	1123.2	239.85	503.1	
Physics	1123.2	921.6	196.8	412.8	
English	239.85	196.8	42.025	88.15	
History	503.1	412.8	88.15	184.9	

#### The GLM Procedure **Multivariate Analysis of Variance**

Characteristic Roots and Vectors of: E Inverse * H, where H = Contrast SSCP Matrix for Difference E = Error SSCP Matrix						
		Characteristic Vector V'EV=1				
Characteristic Root	Percent	Math	Physics	English	History	
0.74274286	100.00	0.02786274	-0.00812904	0.00091540	0.00527934	
0.00000000	0.00	-0.01475944	0.01021609	-0.03560975	0.03432812	
0.00000000	0.00	-0.02591855	0.03141917	0.00079171	0.00000000	
0.00000000	0.00	0.00465239	-0.01125210	0.02614008	0.00000000	

# MANOVATest Criteria and Exact F Statistics for the Hypothesis of No Overall Difference Effect H = Contrast SSCP Matrix for Difference E = Error SSCP Matrix

#### S=1 M=1 N=16.5

Statistic	Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.57380812	6.50	4	35	0.0005
Pillai's Trace	0.42619188	6.50	4	35	0.0005
Hotelling-Lawley Trace	0.74274286	6.50	4	35	0.0005
Roy's Greatest Root	0.74274286	6.50	4	35	0.0005

### The CORR Procedure

### AdvM=No

4 Variables: rMath rPhysics rEnglish rHistory

Covariance Matrix, DF = 19					
	rMath	rPhysics	rEnglish	rHistory	
rMath	47.71315789	51.69736842	2.15000000	3.38947368	
rPhysics	51.69736842	86.51315789	12.19736842	6.36842105	
rEnglish	2.15000000	12.19736842	50.57631579	57.77894737	
rHistory	3.38947368	6.36842105	57.77894737	91.74736842	

### The CORR Procedure

#### AdvM=Yes

4 Variables: rMath rPhysics rEnglish rHistory

Covariance Matrix, DF = 19						
	rMath	rPhysics	rEnglish	rHistory		
rMath	62.34473684	54.71315789	2.35789474	6.81578947		
rPhysics	54.71315789	66.23947368	14.88421053	13.71052632		
rEnglish	2.35789474	14.88421053	32.67368421	20.68421053		
rHistory	6.81578947	13.71052632	20.68421053	29.00000000		

The SAS System

Total Sample Size	40	DF Total	39
Variables	4	DF Within Classes	38
Classes	2	DF Between Classes	1

Number of Observations Read	40
Number of Observations Used	40

Class Level Information						
AdvM	Variable Name	Frequency	Weight	Proportion	Prior Probability	
No	No	20	20.0000	0.500000	0.500000	
Yes	Yes	20	20.0000	0.500000	0.500000	

Within Covariance Matrix Information				
AdvM	Covariance Matrix Rank	Natural Log of the Determinant of the Covariance Matrix		
No	4	14.28119		
Yes	4	12.93266		
Pooled	4	13.90007		

#### The DISCRIM Procedure **Test of Homogeneity of Within Covariance Matrices**

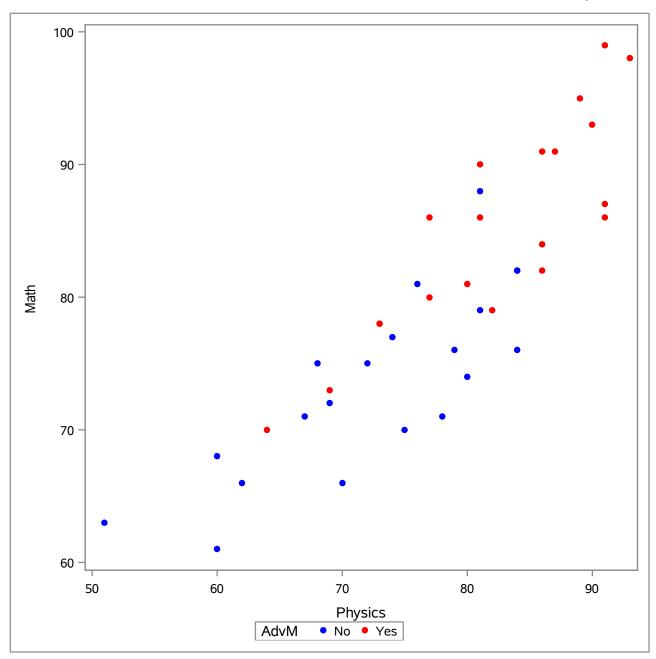
Chi-Square	DF	Pr > ChiSq
9.878987	10	0.4512

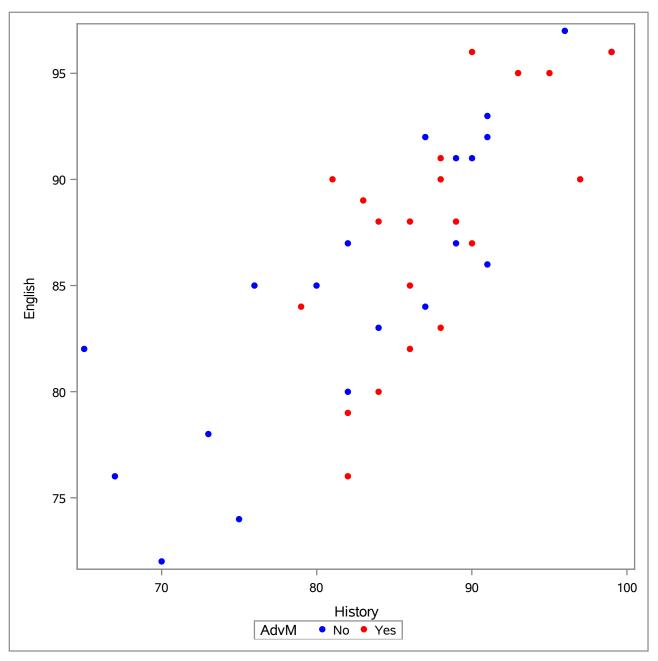
Since the Chi-Square value is not significant at the 0.1 level, a pooled covariance matrix will be used in the discriminant function.

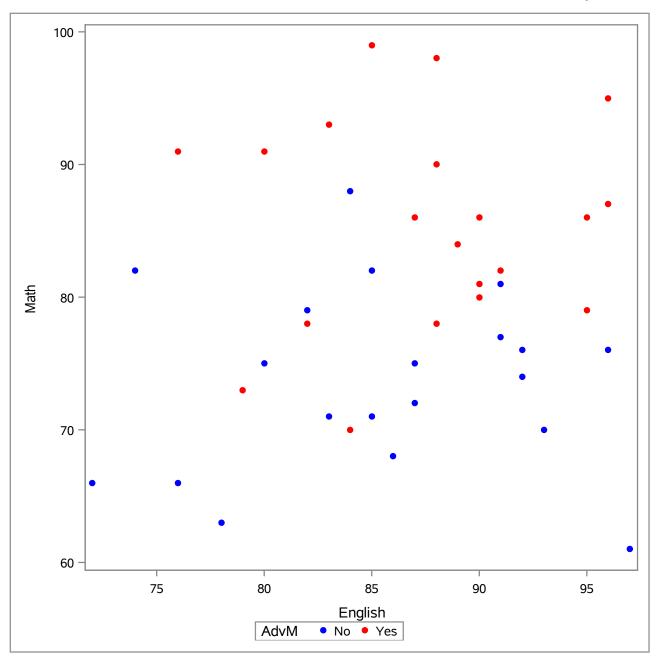
Reference: Morrison, D.F. (1976) Multivariate Statistical Methods p252.

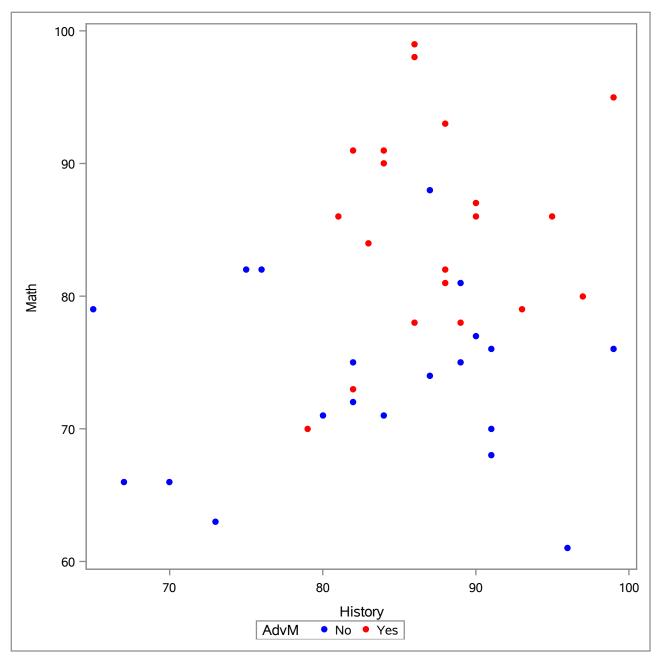
Generalized Squared Distance to AdvM					
From AdvM	No	Yes			
No	0	2.82242			
Yes	2.82242	0			

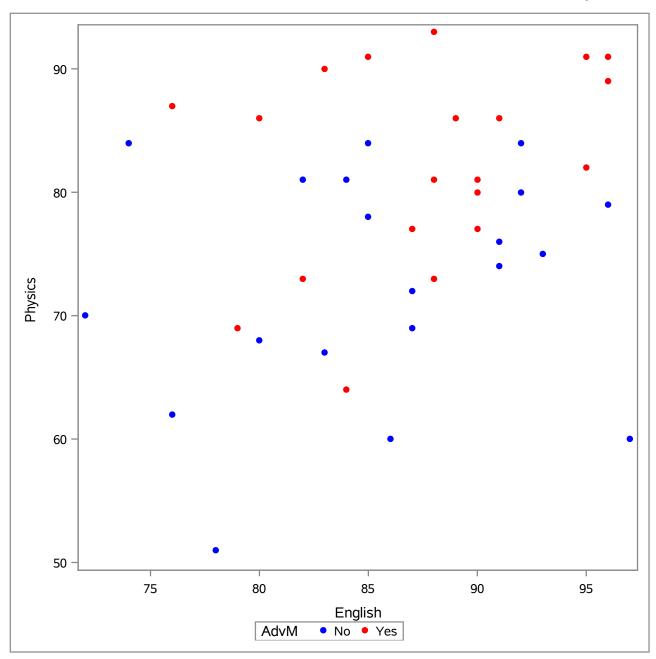
Linear Discriminant Function for AdvM					
Variable	No	Yes			
Constant	-142.40965	-164.30820			
Math	2.26747	2.55602			
Physics	-1.04034	-1.12453			
English	2.55354	2.56302			
History	-0.29988	-0.24521			

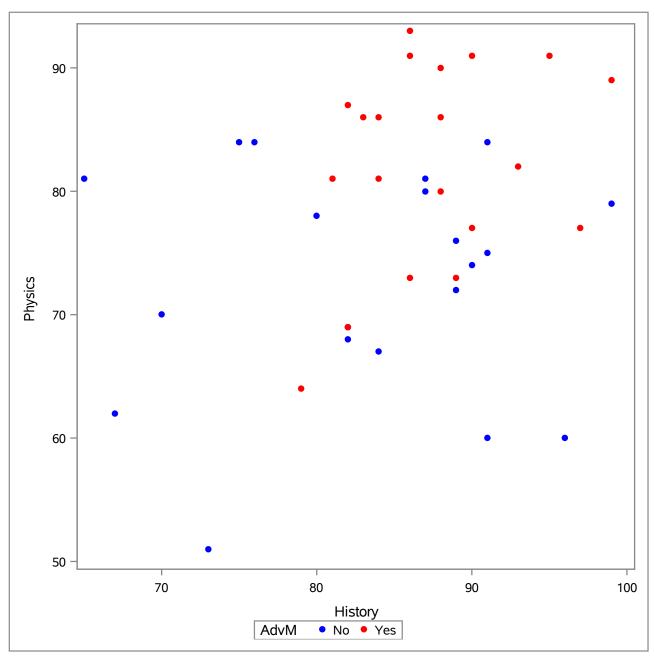


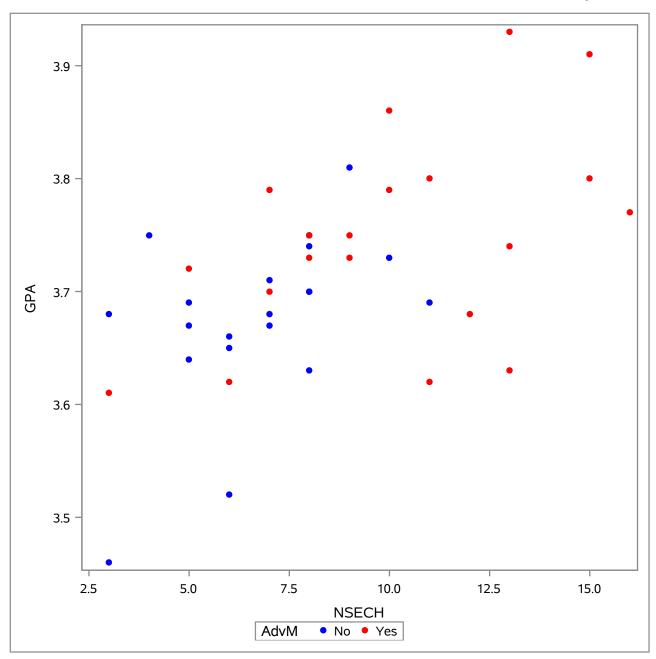












Total Sample Size	40	DF Total	39
Variables	6	DF Within Classes	38
Classes	2	DF Between Classes	1

Number of Observations Read	40
Number of Observations Used	40

	Class Level Information				
AdvM	Variable Name	Frequency	Weight	Proportion	Prior Probability
No	No	20	20.0000	0.500000	0.500000
Yes	Yes	20	20.0000	0.500000	0.500000

Within Covariance Matrix Information			
AdvM	Covariance Determinant of the Matrix Rank Covariance Matrix		
No	6	9.19622	
Yes	6	8.83806	
Pooled	6	9.66555	

#### The DISCRIM Procedure **Test of Homogeneity of Within Covariance Matrices**

Chi-Square	DF	Pr > ChiSq
20.517475	21	0.4887

Since the Chi-Square value is not significant at the 0.1 level, a pooled covariance matrix will be used in the discriminant function.

Reference: Morrison, D.F. (1976) Multivariate Statistical Methods p252.

Generalized Squared Distance to AdvM			
From AdvM	No Yes		
No	1.38629	4.85433	
Yes	4.85433	1.38629	

Linear Discriminant Function for AdvM			
Variable	No	Yes	
Constant	-1899	-1887	
Math	-1.19676	-0.89340	
Physics	-5.55718	-5.61701	
English	-0.92258	-0.89944	
History	-3.26909	-3.19034	
GPA	1273	1261	
NSECH	-5.73978	-5.47044	

# The DISCRIM Procedure Classification Summary for Calibration Data: WORK.STUDENTDATA Resubstitution Summary using Linear Discriminant Function

Number of Observations and Percent Classified into AdvM			
From AdvM	No	Yes	Total
No	18	2	20
	90.00	10.00	100.00
Yes	4	16	20
	20.00	80.00	100.00
Total	22	18	40
	55.00	45.00	100.00
Priors	0.5	0.5	

Error Count Estimates for AdvM				
	No Yes Total			
Rate	0.1000	0.2000	0.1500	
Priors	0.5000	0.5000		

# The DISCRIM Procedure Classification Summary for Calibration Data: WORK.STUDENTDATA Cross-validation Summary using Linear Discriminant Function

Number of Observations and Percent Classified into AdvM			
From AdvM	No	Yes	Total
No	17	3	20
	85.00	15.00	100.00
Yes	5	15	20
	25.00	75.00	100.00
Total	22	18	40
	55.00	45.00	100.00
Priors	0.5	0.5	

Error Count Estimates for AdvM			
	No Yes Total		
Rate	0.1500	0.2500	0.2000
Priors	0.5000	0.5000	

# The DISCRIM Procedure Classification Summary for Test Data: WORK.SDTEST Classification Summary using Linear Discriminant Function

Observation Profile for Test Data	
Number of Observations Read	5
Number of Observations Used	5

Number of Observations and Percent Classified into AdvM				
	No Yes Total			
Total	1 20.00	4 80.00	5 100.00	
Priors	0.5	0.5		

Obs	Math	Physics	English	History	GPA	NSECH	No	Yes	_INTO_
1	96	94	90	91	3.83	12	0.01513	0.98487	Yes
2	82	77	89	88	3.69	6	0.34058	0.65942	Yes
3	74	73	93	87	3.65	5	0.79050	0.20950	No
4	94	90	80	75	3.70	7	0.07965	0.92035	Yes
5	85	77	97	90	3.68	8	0.07138	0.92862	Yes

Total Sample Size	40	DF Total	39
Variables	4	DF Within Classes	38
Classes	2	DF Between Classes	1

Number of Observations Read	40
Number of Observations Used	40

Class Level Information						
AdvM Name Frequency Weight Proportion Probability						
No	No	20	20.0000	0.500000	0.500000	
Yes	Yes	20	20.0000	0.500000	0.500000	

Within Covariance Matrix Information						
Covariance AdvM Matrix Rank Covariance Matrix Rank						
No	4	14.28119				
Yes	4	12.93266				
Pooled	4	13.90007				

#### The DISCRIM Procedure **Test of Homogeneity of Within Covariance Matrices**

Chi-Square	DF	Pr > ChiSq
9.878987	10	0.4512

Since the Chi-Square value is not significant at the 0.1 level, a pooled covariance matrix will be used in the discriminant function.

Reference: Morrison, D.F. (1976) Multivariate Statistical Methods p252.

Generalized Squared Distance to AdvM					
From AdvM	No	Yes			
No	1.38629	4.20872			
Yes	4.20872	1.38629			

Linear Discriminant Function for AdvM						
Variable No						
Constant	-143.10279	-165.00135				
Math	2.26747	2.55602				
Physics	-1.04034	-1.12453				
English	2.55354	2.56302				
History	-0.29988	-0.24521				

# The DISCRIM Procedure Classification Summary for Calibration Data: WORK.STUDENTDATA Resubstitution Summary using Linear Discriminant Function

Number of Observations and Percent Classified into AdvM						
From AdvM	No	Yes	Total			
No	18	2	20			
	90.00	10.00	100.00			
Yes	4	16	20			
	20.00	80.00	100.00			
Total	22	18	40			
	55.00	45.00	100.00			
Priors	0.5	0.5				

Error Count Estimates for AdvM						
	No Yes Total					
Rate	0.1000	0.2000	0.1500			
Priors	<b>Priors</b> 0.5000 0.5000					

# The DISCRIM Procedure Classification Summary for Calibration Data: WORK.STUDENTDATA Cross-validation Summary using Linear Discriminant Function

Number of Observations and Percent Classified into AdvM						
From AdvM No Yes Tota						
No	16	4	20			
	80.00	20.00	100.00			
Yes	4	16	20			
	20.00	80.00	100.00			
Total	20	20	40			
	50.00	50.00	100.00			
Priors	0.5	0.5				

Error Count Estimates for AdvM						
	No Yes Total					
Rate	0.2000	0.2000	0.2000			
<b>Priors</b> 0.5000 0.5000						

# The DISCRIM Procedure Classification Summary for Test Data: WORK.SDTEST Classification Summary using Linear Discriminant Function

Observation Profile for Test Data			
Number of Observations Read	5		
Number of Observations Used	5		

Number of Observations and Percent Classified into AdvM				
	No	Yes	Total	
Total	1 20.00	4 80.00	5 100.00	
Priors	0.5	0.5		

Obs	Math	Physics	English	History	GPA	NSECH	No	Yes	_INTO_
1	96	94	90	91	3.83	12	0.02371	0.97629	Yes
2	82	77	89	88	3.69	6	0.28180	0.71820	Yes
3	74	73	93	87	3.65	5	0.74133	0.25867	No
4	94	90	80	75	3.70	7	0.07532	0.92468	Yes
5	85	77	97	90	3.68	8	0.12064	0.87936	Yes

Total Sample Size	40	DF Total	39
Variables	2	DF Within Classes	38
Classes	2	DF Between Classes	1

Number of Observations Read	40
Number of Observations Used	40

Class Level Information					
					Prior Probability
No	No	20	20.0000	0.500000	0.500000
Yes	Yes	20	20.0000	0.500000	0.500000

Within Covariance Matrix Information				
AdvM	Covariance Matrix Rank  Natural Log of the Determinant of the Covariance Matrix			
No	2	7.28290		
Yes	2	7.03540		
Pooled	2	7.22410		

#### The DISCRIM Procedure **Test of Homogeneity of Within Covariance Matrices**

Chi-Square	DF	Pr > ChiSq
2.327499	3	0.5073

Since the Chi-Square value is not significant at the 0.1 level, a pooled covariance matrix will be used in the discriminant function.

Reference: Morrison, D.F. (1976) Multivariate Statistical Methods p252.

Generalized Squared Distance to AdvM				
From AdvM				
No	1.38629	3.99148		
Yes	3.99148	1.38629		

Linear Discriminant Function for AdvM				
Variable	No	Yes		
Constant	-50.02684	-66.88274		
Math	1.27864	1.55765		
Physics	0.06179	-0.00688		

# The DISCRIM Procedure Classification Summary for Calibration Data: WORK.STUDENTDATA Resubstitution Summary using Linear Discriminant Function

Number of Observations and Percent Classified into AdvM				
From AdvM	No	Yes	Total	
No	16	4	20	
	80.00	20.00	100.00	
Yes	5	15	20	
	25.00	75.00	100.00	
Total	21	19	40	
	52.50	47.50	100.00	
Priors	0.5	0.5		

Error Count Estimates for AdvM					
	No Yes Total				
Rate	0.2000	0.2500	0.2250		
Priors	0.5000	0.5000			

# The DISCRIM Procedure Classification Summary for Calibration Data: WORK.STUDENTDATA Cross-validation Summary using Linear Discriminant Function

Number of Observations and Percent Classified into AdvM					
From AdvM					
No	16	4	20		
	80.00	20.00	100.00		
Yes	6	14	20		
	30.00	70.00	100.00		
Total	22	18	40		
	55.00	45.00	100.00		
Priors	0.5	0.5			

Error Count Estimates for AdvM					
	No Yes Total				
Rate	0.2000	0.3000	0.2500		
Priors	0.5000	0.5000			

# The DISCRIM Procedure Classification Summary for Test Data: WORK.SDTEST Classification Summary using Linear Discriminant Function

Observation Profile for Test I	Data
Number of Observations Read	5
Number of Observations Used	5

Number of Observations and Percent Classified into AdvM					
	Total				
Total	1 20.00	4 80.00	5 100.00		
Priors	0.5	0.5			

Obs	Math	Physics	English	History	GPA	NSECH	No	Yes	_INTO_
1	96	94	90	91	3.83	12	0.03006	0.96994	Yes
2	82	77	89	88	3.69	6	0.32403	0.67597	Yes
3	74	73	93	87	3.65	5	0.77243	0.22757	No
4	94	90	80	75	3.70	7	0.03952	0.96048	Yes
5	85	77	97	90	3.68	8	0.17189	0.82811	Yes

#### The CLUSTER Procedure **Ward's Minimum Variance Cluster Analysis**

	Eigenvalues of the Covariance Matrix							
	Eigenvalue	Difference	Proportion	Cumulative				
1	190.510610	107.590254	0.6284	0.6284				
2	82.920357	66.855713	0.2735	0.9018				
3	16.064644	8.644075	0.0530	0.9548				
4	7.420568	1.147431	0.0245	0.9793				
5	6.273137	6.270953	0.0207	1.0000				
6	0.002184		0.0000	1.0000				

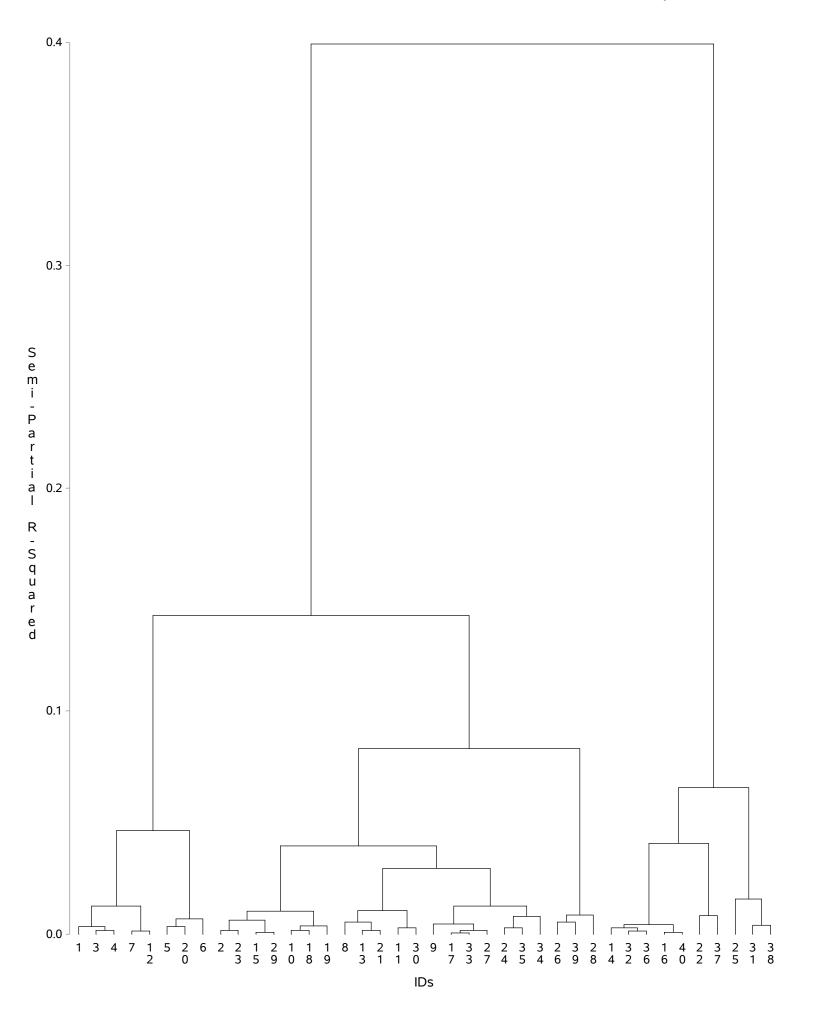
7.10858 **Root-Mean-Square Total-Sample Standard Deviation** 

**Root-Mean-Square Distance Between Observations** 24.62485

Cluster History							
Number of Clusters	Clusters Joined		Freq	Semipartial R-Square	R-Square	Tie	
39	17	33	2	0.0005	.999		
38	16	40	2	0.0006	.999		
37	15	29	2	0.0008	.998		
36	32	36	2	0.0012	.997		
35	7	12	2	0.0013	.996		
34	13	21	2	0.0015	.994		
33	2	23	2	0.0016	.992		
32	10	18	2	0.0016	.991		
31	3	4	2	0.0016	.989		
30	CL39	27	3	0.0017	.987		
29	11	30	2	0.0027	.985		
28	24	35	2	0.0028	.982		
27	14	CL36	3	0.0029	.979		
26	1	CL31	3	0.0032	.976		
25	5	20	2	0.0032	.973		
24	CL32	19	3	0.0035	.969		
23	31	38	2	0.0038	.965		
22	CL27	CL38	5	0.0041	.961		
21	9	CL30	4	0.0043	.957		
20	8	CL34	3	0.0053	.952		
19	26	39	2	0.0053	.946		
18	CL33	CL37	4	0.0063	.940		

### The CLUSTER Procedure Ward's Minimum Variance Cluster Analysis

	Cluster History							
Number of Clusters	Clusters Joined		Freq	Semipartial R-Square	R-Square	Tie		
17	CL25	6	3	0.0068	.933			
16	CL28	34	3	0.0079	.925			
15	22	37	2	0.0083	.917			
14	CL19	28	3	0.0085	.908			
13	CL18	CL24	7	0.0103	.898			
12	CL20	CL29	5	0.0106	.888			
11	CL21	CL16	7	0.0124	.875			
10	CL26	CL35	5	0.0126	.863			
9	25	CL23	3	0.0157	.847			
8	CL12	CL11	12	0.0295	.817			
7	CL13	CL8	19	0.0394	.778			
6	CL22	CL15	7	0.0405	.737			
5	CL10	CL17	8	0.0464	.691			
4	CL6	CL9	10	0.0656	.625			
3	CL7	CL14	22	0.0833	.542			
2	CL5	CL3	30	0.1427	.399			
1	CL2	CL4	40	0.3992	.000			



Class Le	vel Inform	nation
Class	Levels	Values
CLUSTER	2	12

Number of Observations Read	40
Number of Observations Used	40

### **Dependent Variable: Math**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	1613.333333	1613.333333	33.20	<.0001
Error	38	1846.666667	48.596491		
Corrected Total	39	3460.000000			

R-Square	Coeff Var	Root MSE	Math Mean
0.466281	8.768702	6.971118	79.50000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
CLUSTER	1	1613.333333	1613.333333	33.20	<.0001

Source	DF	Type III SS	Mean Square	F Value	Pr > F
CLUSTER	1	1613.333333	1613.333333	33.20	<.0001

### **Dependent Variable: Physics**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	2448.033333	2448.033333	67.61	<.0001
Error	38	1375.866667	36.207018		
Corrected Total	39	3823.900000			

R-Square	Coeff Var	Root MSE	Physics Mean
0.640193	7.759158	6.017227	77.55000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
CLUSTER	1	2448.033333	2448.033333	67.61	<.0001

Source	DF	Type III SS	Mean Square	F Value	Pr > F
CLUSTER	1	2448.033333	2448.033333	67.61	<.0001

### Dependent Variable: English

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	255.208333	255.208333	7.09	0.0113
Error	38	1368.566667	36.014912		
Corrected Total	39	1623.775000			

R-Square	Coeff Var	Root MSE	English Mean
0.157170	6.931842	6.001243	86.57500

Source	DF	Type I SS	Mean Square	F Value	Pr > F
CLUSTER	1	255.2083333	255.2083333	7.09	0.0113

Source	DF	Type III SS	Mean Square	F Value	Pr > F
CLUSTER	1	255.2083333	255.2083333	7.09	0.0113

### **Dependent Variable: History**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	300.833333	300.833333	5.25	0.0276
Error	38	2178.266667	57.322807		
Corrected Total	39	2479.100000			

R-Square	Coeff Var	Root MSE	History Mean
0.121348	8.870747	7.571183	85.35000

Source DF		Type I SS	Type I SS Mean Square		Pr > F
CLUSTER	1	300.8333333	300.8333333	5.25	0.0276

Source	DF	Type III SS	Mean Square	F Value	Pr > F
CLUSTER	1	300.8333333	300.8333333	5.25	0.0276

### **Dependent Variable: GPA**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	0.10208333	0.10208333	17.92	0.0001
Error	38	0.21642667	0.00569544		
Corrected Total	39	0.31851000			

R-Square	Coeff Var	Root MSE	GPA Mean
0.320503	2.033359	0.075468	3.711500

Source	DF Type I SS		Mean Square	F Value	Pr > F
CLUSTER	1	0.10208333	0.10208333	17.92	0.0001

Source	urce DF Type III SS M		Mean Square	F Value	Pr > F
CLUSTER	1	0.10208333	0.10208333	17.92	0.0001

### **Dependent Variable: NSECH**

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	102.6750000	102.6750000	11.66	0.0015
Error	38	334.7000000	8.8078947		
Corrected Total	39	437.3750000			

R-Square	R-Square Coeff Var		NSECH Mean
0.234753	35.43653	2.967810	8.375000

Source	Source DF		ype I SS Mean Square		Pr > F
CLUSTER	1	102.6750000	102.6750000	11.66	0.0015

Source	DF	Type III SS	Mean Square	F Value	Pr > F
CLUSTER	1	102.6750000	102.6750000	11.66	0.0015

The SAS System

		Math		Math Physics		English		History	
Level of CLUSTER	N	Mean	Std Dev	Mean	Std Dev	Mean	Std Dev	Mean	Std Dev
1	30	83.1666667	7.57529257	82.0666667	6.04542194	88.0333333	5.67197182	86.9333333	7.09022315
2	10	68.5000000	4.50308536	64.0000000	5.92546294	82.2000000	6.95701085	80.6000000	8.94675608

		GI	PA	NSE	СН
Level of CLUSTER	N	Mean	Std Dev	Mean	Std Dev
1	30	3.74066667	0.07376259	9.30000000	3.21794537
2	10	3.62400000	0.08071899	5.60000000	1.95505044

### The SAS System

### The FREQ Procedure

Frequency Percent Row Pct Col Pct

Table of AdvM by CLUSTER			
	CLUSTER		
AdvM	1	2	Total
No	12 30.00 60.00 40.00	8 20.00 40.00 80.00	20 50.00
Yes	18 45.00 90.00 60.00	5.00 10.00 20.00	20 50.00
Total	30 75.00	10 25.00	40 100.00