Student Name:	
PERM:	

Circle the section you ATTEND (if you are enrolled a different section, note which one):

Kyle: Tue:8am Tue:4pm Tue:7pm

David: Tue:5pm Tue:6pm

Yihan: Mon:4pm Mon:5pm Mon:6pm Mon:7pm

Tom: Tue:8am Tue:4pm Wed:8am

Matt: Tue:5pm Tue:6pm Tue:7pm

$\frac{\text{Math 4B, Midterm 2, Spring 2017}}{\text{Version C}}$

<u>Instructions</u>: Read the instructions for each question carefully. No calculators, cell phones, or other electronic devices are permitted. No notes or textbooks. Academic dishonesty will not be tolerated. Show your work, write legibly, and circle your answers.

Question	Points	Score
1	10	
2	10	
3	9	
4	9	
5	3	
Total:	41	

I understand UCSB's policies regarding academic dishonesty, and I certify that this test was taken with academic integrity.

C1.	1	date:	
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\sim 1 \sim 11	and	aacc.	

1. (10 points) Find the general solution to the ODE:

$$y'' + 4y' + 13y = 17e^{3t}$$

 $2.\ (10\ \mathrm{points})$ Solve the initial value problem:

$$x' = 7x + 4y$$
, $y' = 4x + y$, $x(0) = -5$, $y(0) = 5$

3.	(9 points)	A 10 l	kg mass	is attach	ed to	the end	of a s	pring	with	spring	constant	k = 90
	N/m.											

(a) If there is no damping force, at what frequency will the mass naturally oscillate?

(b) If we add a dashpot to the system with a damping constant of b = 100 N/(m/s), will the system be over-damped or under-damped?

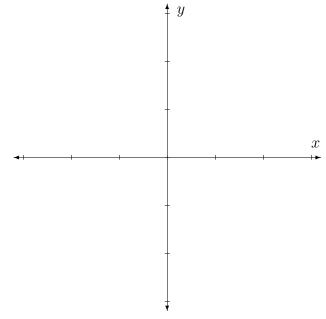
(c) If we keep the damping consant of b = 100 N/(m/s) from part (b) but replace the spring, what new spring constant k will cause the system to be critically damped?

4. (9 points) Consider the non-linear system

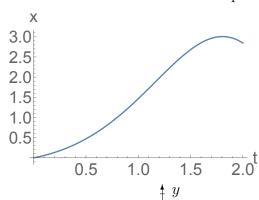
$$\frac{dx}{dt} = x + y$$
$$\frac{dy}{dt} = 1 - x^2$$

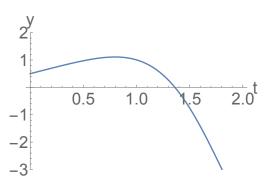
(a) List all equilibrium points for this system.

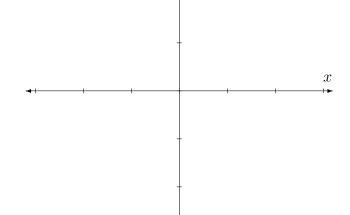
(b) Shade the part of the phase plane in which both x and y are increasing.



(c) The graphs of x(t) and y(t) for a solution $\begin{bmatrix} x \\ y \end{bmatrix}$ to the system are shown below. Sketch the solution curve in the phase plane.







5. (3 points) The real 2×2 matrix A has eigenvector $\vec{v}_1 = \begin{bmatrix} 3 \\ 2-i \end{bmatrix}$ for eigenvalue $\lambda_1 = 2+i$; and A has eigenvector $\vec{v}_2 = \begin{bmatrix} 3 \\ 2+i \end{bmatrix}$ for eigenvalue $\lambda_2 = 2-i$. Given this information, write down the general solution to the system of ODEs

$$\vec{x}' = A\vec{x}$$

If you finish early, you must stay in your seat until the end. You should check your work, but if you are done, you can amuse yourself by coloring in these regular pentagonal tilings.

