Name:	
Perm:	

Math 34A Midterm 3, Summer 2022

(*100 pts total*)

1. Use the log table provided with this exam to answer the following questions:

   (a) (*4 pts*) Find $\log(10) + \log(0.316)$.

   (b) (*4 pts*) If $\log(y) = 6.3$, then find y.

   $y =$

   (c) (*4 pts*) Find the average rate of change of 10^x between $x = 0.7$ and $x = 0.9$.

   $\frac{\Delta y}{\Delta x} =$

2. Compute the following derivatives.

(a) (*4 pts*) $\dfrac{d}{dx}\left(3x^5 - 2x^2 - 14\sqrt{x}\right) =$

(b) (*4 pts*) $\dfrac{d}{dx}\left(4x^2 + 5e^{2x} - 5e^{3x}\right) =$

(c) (*4 pts*) Consider the function

$$f(x) = \frac{a}{\sqrt[3]{x}} - \frac{b}{(e^x)^2}$$

where a and b are constants. Find $f'(1)$.

$f'(1) =$

3. This question is about the graph of the function

$$f(x) = 2x^3 + 3x^2 - 12x + 172.$$

(a) (*5 pts*) What is the slope of the graph at $x = 0$?

slope = $\boxed{}$

(b) (*5 pts*) What is the equation of the tangent line to the graph at $x = 2$? Use the form $y = mx + b$.

$y =$ $\boxed{}$

(c) (*5 pts*) For which x value(s) does the graph have 0 slope?

$x =$ $\boxed{}$

(d) (*5 pts*) For which x values is the graph $y = f(x)$ concave down?

$\boxed{}$

4. A large Nerf ball is launched upward from the top of a cliff. Its height (in meters) t seconds after launch is modeled by the equation

$$h(t) = -5t^2 + 30t + 50.$$

(In this problem we are ignoring horizontal movement.)

(a) (*7 pts*) Find the function which gives the velocity of the ball after t seconds.

(b) (*7 pts*) What is the initial height of the ball?

h = m

(c) (*7 pts*) What is the acceleration of the ball after 5 seconds?

acceleration = m/s^2

(d) (*7 pts*) When does the ball stop rising and begin to fall? (Hint: What would the ball's speed be at that moment?)

at t = s

(e) (*7 pts*) What was the ball's maximum height?

h = m

5. A bacteria colony on a petri dish is growing in the shape of a circle. After t days, the radius of the circle is $t^2 + 2t$ mm.

   (a) (*6 pts*) What is the area of the circle after t days?

$$A(t) = \boxed{} \text{ mm}^2$$

   (b) (*7 pts*) How quickly is the area of the circle growing after t days?

$$A'(t) = \boxed{} \text{ mm}^2/\text{day}$$

   (c) (*8 pts*) As time goes by will the area of the circle grow faster, slower, or does the area grow at a constant rate? Why? (Use calculus to justify your answer).