Name:	
Perm:	

Math 34A Practice Midterm 1, Spring 2022

1. (2pts) Solve for x in the following equation.

in the following equation.

$$\frac{4}{5(x-n)} - \frac{5}{4(x+n)} = 0 \quad \text{Clear denominators}$$

$$1(6(x+n)) - 25(x-n) = 0$$

$$1(6x+1) - 25(x-n) = 0 \quad \text{get non-x staff}$$

$$1(6x+1) - 25(x+25n) = 0 \quad \text{on this side}$$

$$1(6x-25x) = -1(6n-25n)$$

$$-9x = -41n$$

$$x = \frac{41}{9}n$$

$$x = \boxed{\frac{41}{9}}$$

2. (2pts) Multiply out and simplify.

6+2×2y-9×-1y-3x

3. (2pts) Substitute x = ab + c into the expression below and simplify

$$2x^2 + 3cx - 1.$$

$$2(ab+c)^{2}+3c(ab+c)-1$$

$$=2(ab+ab+2ab+c+c^{2})+3c\cdot ab+3c\cdot c-1$$

$$=2a^{2}b^{2}+4abc+2c^{2}+3abc+3c^{2}-1$$

$$=2a^{2}b^{2}+7abc+5c^{2}-1$$

4. (2pts) Find the point of intersection of two lines. The first line passes through the points (0,0) and (2,3) while the second line passes through the points (0,0) and (4,0). Finding  $m_1, b_1$  and  $m_2, b_2$  for the equations below may help you find the answer. over 4, down 5

$$y = m_1 x + b_1$$
$$y = m_2 x + b_2$$

$$y = m_2 x + b_2$$

$$y = \frac{3}{2}x + 0$$

$$y = -\frac{5}{4}x + 5$$

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$$y = \frac{3}{2} \times = \frac{3}{2} \cdot \frac{20}{11}$$

$$= \frac{30}{11}$$

$$x = \frac{20}{11}$$

5.	(4pts) Jason started driving from Phoenix towards Isla Vista at noon at a speed of 75
	mph. At 2pm Marie started driving from Isla Vista towards Phoenix at 100 mph. Jason
	and Marie met at 4pm. Meanwhile a bad guy follows Jason. He leaves Phoenix at 1pm
	and drives along the same route at 90 mph.

How many miles from Isla Vista was the bad guy when Jason and Marie met?

230

miles

## 6. (4 points)

(a) A cylinder with radius r and height h has a volume of  $36\pi m^3$ . Express the surface area in terms of the height h.

(The formula for the volume of a cylinder is  $\pi r^2 h$ , and the surface area formula is  $2\pi r^2 + 2\pi r h$ .)



$$A = 2\pi r^{2} + 2\pi rh$$

$$36\pi = \pi r^{2}h, so h = \frac{36\pi}{\pi^{2}} = \frac{36}{r^{2}}.$$

$$A = 2\pi r^{2} + 2\pi r(\frac{36}{r^{2}})$$

$$= 2\pi r^{2}, \frac{72\pi r}{r^{2}}$$

$$= 2\pi r^{2}, \frac{72\pi r}{r^{2}}$$

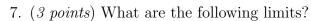
(b) The side of a roof is going to be built. Its shape is an isosceles triangle with base b and height h (figue below). The area of this triangle is  $10m^2$ . Express the perimeter in terms of the height.

Pythongorean Theorem:
$$\frac{b}{2} = h^2 + (\frac{b}{2})^2$$

$$\frac{b}{2} = h^2 + \frac{b^2}{4}$$

$$= (\frac{20}{h}) + 2 \cdot h^2 + (\frac{20}{h})^2$$
(solve for b)
$$= (\frac{20}{h}) + 2 \cdot h^2 + (\frac{10}{h})^2$$

Perimeter = 
$$\frac{20}{h} + 27h^2 + \frac{100}{h^2}$$



- (a)  $\lim_{h\to 0} 10-7h$ This part disappears

when  $x \neq 2$   $\lim_{x \to 2} \frac{x^2 - 4x + 4}{2x - 4}$  both go to zero as  $x = \frac{x^2 - 4x + 4}{2x - 4} = \frac{(x + 2)(x + 2)}{2(x + 2)}$  gots close to 2 .  $= \frac{x + 2 - 1}{2} = \frac{x + 2}{2} =$ 

(c)  $\lim_{n\to\infty} \frac{3n-2}{n+3} = b$  oth get by

n=1,000,000-2 1,000,000+3 is really close to 3.

- 8. (3 points) Compute the logarithms below.
  - (a)  $\log_3(27)$

27=1.3.3.3 or ... 27=3

(b)  $\log_{10}(1,000,000)$ 

1,000,000=1.10.10.10.10.10.10 or...1,000,000 6 1015

(c)  $\log_2(\frac{1}{4})$