



○○

○○○○○

○○○

○○○

Office Hours!

Instructor:

Trevor Klar, `trevorklar@math.ucsb.edu`

Office Hours:

Mondays 2–3PM

Tuesdays 10:30–11:30AM

Thursdays 1–2PM

or by appointment

Office:

South Hall 6431X (Grad Tower, 6th floor, blue side, first door on the right)

© 2017 Daryl Cooper, Trevor Klar

Finding the log of any number

- (1) Write the number as $10^n \times (\text{number between 1 and 10})$
- (2) Find the log of the **number between 1 and 10** using table or graph
- (3) Log is $n + \log(\text{number between 1 and 10})$

Example: Find $\log(573)$

- (1) $\log(573) = \log(100 \times 5.73) = \log(100) + \log(5.73) = 2 + \log(5.73)$
- (2) $\log(5.73) \approx 0.7582$
- (3) $\log(573) \approx 2 + 0.7582 = 2.7582$

Find $\log(57.3)$

$A \approx 7.582$ $B \approx 10 + 0.7582$ $C \approx 1 + 0.7582$ D Other C

Find $\log(0.573)$

$A \approx -1.7582$ $B \approx -1 + 0.7582$ $C \approx -0.7582$ D Other B

Finding the antilog of any number

Example: 2.306 is not on x -axis of graph $y = 10^x$ or in middle of log table. So how do you use table or graph to find **antilog**(2.306)?

Think about it: **antilog**(2.306) = $10^{2.306}$

$$= \underbrace{10^2}_{\text{duh!}} \times \underbrace{10^{0.306}}_{\text{look it up!}}$$
$$\approx 100 \times 2.02$$
$$= 202$$

This is like the **moving decimal point trick** for logs.

From log table: $10^{0.86} \approx 7.25$.

Use this to find **antilog**(3.86)

≈ 7250

A= I got it right

B= I was close

C= I was wrong

§7.5: Using logs to multiply

First rule of logs: $\log(a \times b) = \log(a) + \log(b)$

Example: Find 2.7×1.6 using logs

Hint: $\log(2.7) \approx 0.43$ and $\log(1.6) \approx 0.20$

Method

- (i) Look up $\log(2.7)$ and $\log(1.6)$
- (ii) Add these
- (iii) Take the **antilog** of result from (ii)
- (iv) Think: Is the answer **reasonable** or did I goof up?

A= done B= confused

§7.5: Using logs to multiply

First rule of logs: $\log(a \times b) = \log(a) + \log(b)$

Example: Find 2.7×1.6 using logs

Hint: $\log(2.7) \approx 0.43$ and $\log(1.6) \approx 0.20$

Look how I write the answer.

- $\log(2.7 \times 1.6) = \log(2.7) + \log(1.6)$
- Look up $\log(2.7) \approx 0.43$ and $\log(1.6) \approx 0.20$, so
 $\log(2.7 \times 1.6) \approx 0.43 + 0.20 = 0.63$
- Is this the answer? Heck No! It is the **log** of the answer
- $2.7 \times 1.6 \approx \text{antilog}(0.63) = 10^{0.63}$
- Look up $10^{0.63} \approx 4.3$
- Is my answer 4.3 reasonable? Yes, about $2 \times 2 = 4$.

A Really Bad Answer

$$\begin{array}{rcl} 2.7 \times 1.6 & \log(2.7 \times 1.6) & \log(2.7) + \log(1.6) \\ & & = 0.43 \quad = 0.20 \end{array}$$

$$0.43 + 0.20 = 0.63 \leftarrow \text{my answer!!}$$

Common mistake: Writing math **so badly** it is **not even wrong***.

Stare at what is written does it make **any sense**?

The answer can't be right: how can 2.7×1.6 be 0.43?

Where is the mistake? It is so badly written that there is no mistake to find because it is **nonsense**.

*“Not even wrong” is due to the physicist Wolfgang Pauli.

Summary of Good Advice

- Write your work properly.
 - Eat your fruit & vegetables
 - Exercise regularly
 - Get enough sleep
- [This advice brought to you by your mother]

Examples:

Example: Find 352×17.7 using logs and tables.

Hint: $\log(3.52) \approx 0.5465$ and $\log(1.77) \approx 0.2480$

A = done B = I'm working! C = confused

My Steps:

(1) $\log(352) = 2 + \log(3.52) \approx 2.5465$ (move the decimal point)

(2) $\log(17.7) = 1 + \log(1.77) \approx 1.2480$ (move the decimal point)

(3) Add:
 $\log(352 \times 17.7) = \log(352) + \log(17.7) \approx 2.5465 + 1.2480 = 3.7945$

(4) So:
 $352 \times 17.7 \approx \text{antilog}(3.7945) = 10^{3.7945} = 10^3 \times 10^{0.7945} \approx 6230$

(5) Check: Is this reasonable? Should be about $300 \times 20 = 6000$

Did you get close?

A = Yes B = No C = Didn't finish

§7.5: Using logs to divide

Remember Log Rule (5): $\log(a \div b) = \log(a) - \log(b)$

Example: Use this rule to find $38.2/1.77$

Hint: $\log(3.82) \approx 0.58$ and $\log(1.77) \approx 0.25$

Method

- (i) Look up $\log(3.82)$ and $\log(1.77)$, find $\log(38.2)$
- (ii) **Subtract!**
- (iii) Take the **antilog** of result from (ii)
- (iv) Think: Is the answer **reasonable** or did I goof up?

A = done B = confused

§7.5: Using logs to divide

Remember Log Rule (5): $\log(a \div b) = \log(a) - \log(b)$

Example: Use this rule to find $38.2/1.77$

Hint: $\log(3.82) \approx 0.58$ and $\log(1.77) \approx 0.25$

Look how I write the answer.

- $\log(38.2 \div 1.77) = \log(38.2) - \log(1.77)$ using $\log(a/b) = \log(a) - \log(b)$
- $\log(38.2) = 1 + \log(3.82) \approx 1.58$ from graph and move decimal point
- $\log(1.77) \approx 0.25$ from graph
- $\log(38.2) - \log(1.77) \approx 1.58 - 0.25 = 1.33$
- Therefore $38.2 \div 1.77 \approx \text{antilog}(1.33) = 10^{1.33}$
- From graph $10^{0.33} \approx 2.1$ so $10^{1.33} \approx 21$.
- Check: Is the answer $\boxed{21}$ reasonable? Yes, about $40 \div 2 = 20$.

Examples:

Example: Find $352/17.7$ using logs and tables.

Hint: $\log(3.52) \approx 0.5465$ and $\log(1.77) \approx 0.2480$

A = done

B = I'm working!

C = confused

My Steps:

(1) $\log(352) = 2 + \log(3.52) \approx 2.5465$ (move the decimal point)

(2) $\log(17.7) = 1 + \log(1.77) \approx 1.2480$ (move the decimal point)

(3) Subtract:

$$\log(352 \div 17.7) = \log(352) - \log(17.7) \approx 2.5465 - 1.2480 = 1.2985$$

(4) So:

$$352 \div 17.7 \approx \text{antilog}(1.2985) = 10^{1.2985} = 10^1 \times 10^{0.2985} \approx 19.9$$

(5) Check: Is this reasonable? Should be about $350 \div 20 \approx 20$

Did you get close?

A = Yes

B = No

C = Didn't finish

Powers Using Logs

Or, exploiting Log Rule (4):

$$\log(a^p) = p \log(a)$$

Use this and the graph of $y = 10^x$ to find $\sqrt{70}$.

One Approach:

- (i) Use graph and move decimal point trick to find $\log(70)$
- (ii) $\log(\sqrt{70}) = \log(70^{1/2}) = (1/2) \log(70)$
- (iii) Take the **antilog** of result from (ii)
- (iv) Think: Is the answer **reasonable** or did I goof up?

Hint: $\log(7) \approx 0.84$

A = done B = working C = confused

Answer: $\sqrt{70} \approx 8.3$. Is that reasonable?

Computer Applications

One kilobyte (1 **KB**) is 2^{10} .

Problem: Calculate 2^{10} using logs. **Hint:** $\log(2) \approx 0.3$

$A \approx 3$ $B \approx 10.3$ $C \approx 30$ $D \approx 1000$ $E \approx 1100$ D

So: $2^{10} \approx 10^3 = 1000$ (really $2^{10} = 1024$).

1KB is really $2^{10} = 1024 \approx 10^3$ (**K** is **Kilo** = thousand)

1MB is really $2^{20} = (2^{10})^2 \approx (10^3)^2 = 10^6$ (**M** is **Mega** = million)

1GB is really $2^{30} = (2^{10})^3 \approx (10^3)^3 = 10^9$ (**G** is **Giga** = billion)

1TB is really $2^{40} = (2^{10})^4 \approx (10^3)^4 = 10^{12}$ (**T** is **Tera** = trillion)

Example: suppose on a certain island the population of rabbits doubles every generation. After 20 generations it multiplies by...
 $2^{20} \approx 1$ million.

Powers of 2 are easy to do, even in your head. To work out 2^n the **log** of the answer is approximately $0.3n$, so 2^n is 1 followed by $0.3n$ zeroes.

Summary of calculations with logs

[Courtesy of Daryl Cooper]

Calculate the **log** of the thing you want then take **antilog** of the result.

Example: To calculate *puppy* = $17^{3.1}$

(i) **doggy** = **log**(*puppy*)

(ii) rules of **logs** to expand **doggy**

(iii) look up **logs** of individual terms in **doggy**. Move decimal point trick.

(iv) Now have numerical value for **doggy**.

(v) so *puppy* = **antilog**(**doggy**) is the answer.

Make sure you never jot down a number on its own. It should always be part of an equation like **log**(945×32) ≈ 4.48 This way one can read and understand what is written. Otherwise you get **gibberish**

Write math the way I do. With **words** and **equations**. One should be able to **read and understand** what is on the paper **without being telepathic**.

Imagine it is a **report** for your employer. In reality you are **explaining it to yourself**.