Pre-Calculus

Test 3

Mr. Klar

Use the 3 famous points to write a short table of values for the function. Then sketch a graph of the function. Identify any asymptotes and intercepts. (Hint: Choose values of x so that the entire exponent becomes a famous point.)

1.
$$f(x) = -2^{x+3}$$

2.
$$f(x) = 1 + e^{2x}$$

Evaluate the expression without a calculator.

$$3.\ \log_{1.23}1.23^{456}$$

4.
$$2 \ln e^{3.14}$$

5.
$$5 - \log_{10}(1000)$$

Use the 3 famous points to sketch the parent function. Then use transformations to sketch the given function. (You can erase the parent function once you're done with it if you want.)

6.
$$f(x) = -\ln(x) + 2$$

7.
$$f(x) = 1 + 2\log_3(x+3)$$

Rewrite the log with base 10 by using change-of-base formula.

8.
$$\log_{17} 92$$

Use the properties of logarithms to expand the expression as a sum or difference of logs with no exponents or radicals.

9.
$$\log_3 2b^4$$

10.
$$\ln \frac{x\sqrt{x+1}}{3e^4}$$

Condense the expression to a single logarithm.

11.
$$3\log_3 x + 4\log_3 y^2$$

12.
$$\ln 3x - \ln(x-3) + \ln(x^2-9)$$

Solve for x. Use the fact that $\log_5(2) \approx 0.43$. (Hint: Factor large numbers to simplify logs. You can use my "lame calculator" for the decimal arithmetic.)

13.
$$3^x = 81$$

14.
$$5^{2x} = 250$$

15.
$$\log_6 x = 3$$

16.
$$\log_{10}(x+3) = 4$$

Solve the equation algebraically. Write your answer in terms of logs with no exponents or radicals.

17.
$$\frac{1025}{8 + e^{4x}} = 5$$

18.
$$-xe^{-x} + e^{-x} = 0$$
 (Hint: use the Zero Product Property)

Bonus.
$$\log_{10}(x) - \log_{10}(8 - 5x) = 2$$