

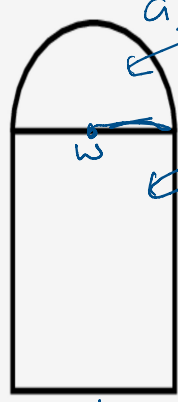
4/28 More Log Stuff

Thursday, April 28, 2022 2:03 PM

HW11 #6

This question was **not** broken. What I missed in lecture was that the area was meant to mean the area of the window and I did not realize this during lecture, but instead right after lecture when a student asked about this.

A window has the shape of a semi-circle placed on top of a rectangle as shown below. (The diagram at the top of page 50 in the text is equivalent.)



a) $A_c = \frac{1}{2} \pi r^2 = \frac{1}{2} \cdot \pi \left(\frac{w}{2}\right)^2 = \frac{1}{8} \pi w^2$

$A_R = w \cdot h$

Window area = $A_c + A_R = \frac{1}{8} \pi w^2 + w \cdot h$

b) Window area = $7 = \frac{1}{8} \pi w^2 + w \cdot h$

solve for h: $h = \frac{7 - \frac{1}{8} \pi w^2}{w} = \frac{7}{w} - \frac{\pi}{8} w$

(a) Express the area A of the window in terms of the width w and height h of the rectangle. (b) If the area is 7, express the height in terms of the width.

(a) $A(h, w) =$

(b) $h(w) =$

$$100 \cdot 3^n = 10^7$$

$$\log(100 \cdot 3^n) = \log(10^7)$$

$$\log(100) + \log(3^n) = 7$$

$$2 + n \cdot \log(3) = 7$$

More Bunnies

We saw that:

- if we start with 100 bunnies, and
 - the bunny population triples every generation,
- then we have 100×3^n bunnies after n generations.

$$100 \cdot 3^n = 10^7$$
$$\log(100 \cdot 3^n) = \log(10^7)$$
$$\log(100) + \log(3^n) = 7$$
$$\log(3^n) = 5$$
$$n \cdot \log(3) = 5$$

1. How many generations until there are $10^7 = 10,000,000$ bunnies?

$$A = \log(5/3) \quad B = 5 - \log(3) \quad C = 5 / \log(3)$$
$$D = 5/3 \quad E = 10^5/3$$

Flu Outbreak

2. At the start of an outbreak of H1N1 flu in a large class of students, there were 5 infected individuals. The numbers doubles every 3 days. How many days until there are 80 infected students?

$$A = \log(16) / \log(2) \quad B = \log(16/2) \quad C = 16 / \log(2)$$

$$D = 3 \log(16) / \log(2) \quad E = \log(48/2)$$

$$\frac{t}{3} = \frac{\log(16)}{\log(2)}$$

$$\log(2^{t/3}) = \log(16)$$
$$t/3 \cdot \log(2) = \log(16)$$

$$5 \cdot 2^{t/3} = 80$$

$$2^{t/3} = 16$$

$$t/3 = 4$$

Limits and Speed

We'll go over this next Tuesday.

