

## 5-3 Change

Tuesday, February 8, 2022 1:52 PM

Natural log?

$\ln$  = "logarithm natural"

=  $\log_e$

$e \approx 2.7$

## HW14: Problem 3

Use natural logs to solve the following:

a)  $e^x = 10$

$\log_e(e^x) = x = \log_e(10)$

$x = \ln(10)$

b)  $e^{2x} = e^8$

$\ln(e^{2x}) = \ln(e^8)$

$x = 2x = 8$

c)  $3^x = 7$

$\log_3(3^x) = x = \log_3(7) = \frac{\ln(7)}{\ln(3)}$

$x = \frac{\ln(7)}{\ln(3)}$

d)  $5 \times 2^x = 3^x$

$\ln(5 \cdot 2^x) = \ln(3^x)$

$x = \frac{-\ln(5)}{\ln(2) - \ln(3)}$

$\ln(5) + x \cdot \ln(2) = x \cdot \ln(3)$

$x \cdot \ln(2) - x \cdot \ln(3) = -\ln(5)$

$x(\ln(2) - \ln(3)) = -\ln(5)$

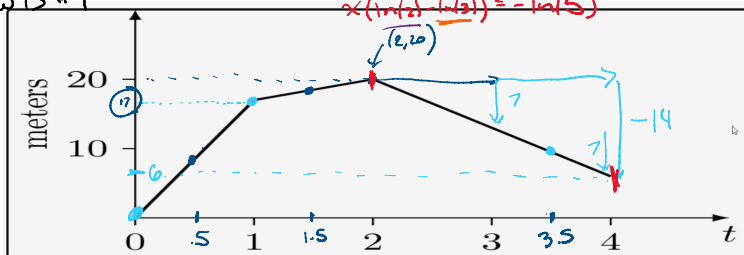
$e^x$  has  $e^x$  as its rate of growth

c)  $3^x = 7$

$\ln(3^x) = \ln(7)$

$x \cdot \ln(3) = \ln(7)$

HW 13 #9



What was the speed of the object at the following times.

(a) At  $t = 0.5$ , the speed was  $\frac{8}{.5}$  m/s

(b) At  $t = 1.5$ , the speed was  $3$  or  $4$  m/s

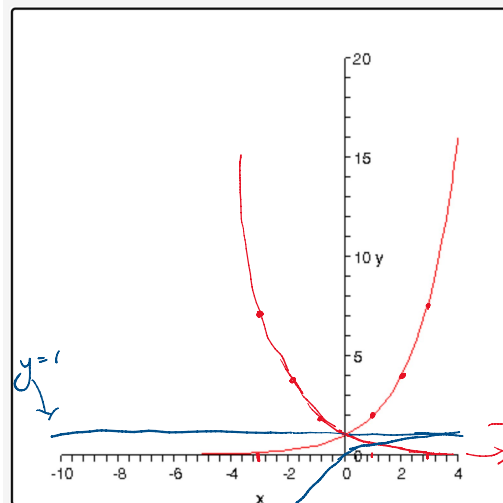
(c) At  $t = 3.5$ , the speed was  $-7$  m/s

(d) What is the significance of the fact that the graph slopes downwards between  $t = 2$  and  $t = 4$ ?

[Hint: speed=distance gone divided by time taken] (You don't have to answer this here)

## HW14: Problem 1

Here is the graph  $y = 2^x$



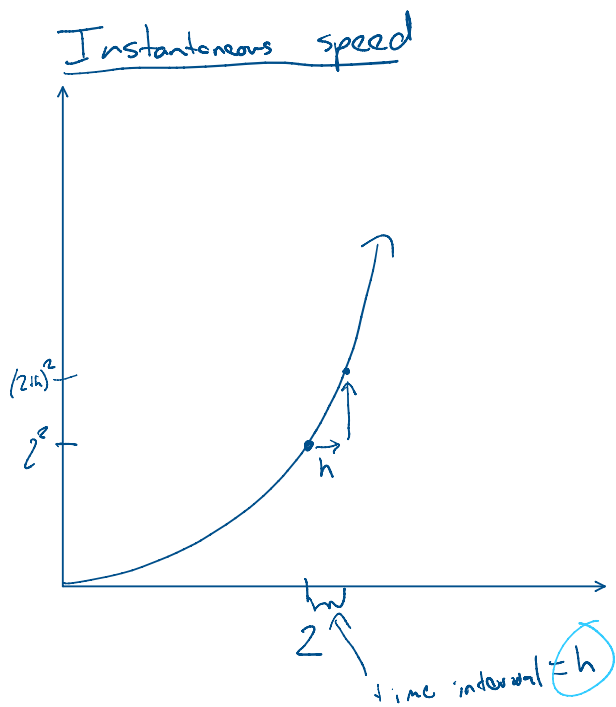
these should be close to 1

On your paper, sketch the graph of  $y = 1 - 2^{-x}$  [HINT: first sketch  $2^{-x}$ ]

Which of these best matches your graph?

Instantaneous speed

$y = x^2$



$$y = x^2$$

final height - initial height

$$= y_2 - y_1$$

$$= (2+h)^2 - 2^2 = \cancel{4} + 4h + h^2 - \cancel{4}$$

$$= 4h + h^2$$

$$h=1: 5 \text{ average speed} = 5$$

$$h=.1: .4 + .01 = .41 \quad \frac{.41}{.1} = 4.1$$

$$h=.01: .04 + .0001 = .0401 \quad \text{average speed} = \frac{.0401}{.01} = 4.01$$

$$\text{Average speed} = \frac{\text{rise}}{\text{run}} = \frac{4h + h^2}{h} = \frac{\cancel{h}(4+h)}{\cancel{h}} = 4+h$$

↑  
error