

# Appendix

**Definition 1** (Buyers/Sellers). *Each buyer,  $B_i$ , has a true cost for the item they are buying,  $c_i$ , and a bid  $b_i$  such that  $b_i \geq c_i$ . Each seller,  $S_j$ , has a true price for the item they are selling,  $p_j$ , and an ask  $a_j$  such that  $a_j \leq p_j$ . Buyers and sellers also have a UUID unique with respect to their type. For example, if there are 5 buyers and 5 sellers, the buyers will have UUIDs 0, 1, 2, 3, 4 and the sellers will have UUIDs 0, 1, 2, 3, 4. In the program we represent the buyer  $B_i$  as a list  $[u_i, c_i, b_i]$  such that  $B_i[0] = u_i$  is the UUID of the buyer,  $B_i[1] = c_i$  is the true cost of the buyer, and  $B_i[2] = b_i$  is the bid of the buyer. We represent the seller  $S_j$  as a list  $[v_j, p_j, a_j]$  such that  $S_j[0] = v_j$  is the UUID of the seller,  $S_j[1] = p_j$  is the true price of the seller, and  $S_j[2] = a_j$  is the ask of the seller.*

**Definition 2** (Clearing Price). *Consider some bid  $b$  and ask  $a$ . The clearing price,  $cp(b, a)$ , a function of the bid and ask that maps to the price at which the transaction clears. We require that  $cp(b, a) \in [a, b]$ .*

**Definition 3** (Surplus). *Let  $B_i$  denote a buyer with cost  $c_i$  and bid  $b_i$ . Let  $S_j$  denote a seller with price  $p_j$  and ask  $a_j$ . Consider some clearing price  $cp(b_i, a_j)$ . The surplus for the buyer is defined as  $s_{B_i} = c_i - cp(b_i, a_j)$  and the surplus for the seller is defined as  $s_{S_j} = p_j - cp(b_i, a_j)$ . The total surplus of the transaction, defined  $s_{B_i, S_j} = s_{B_i} + s_{S_j}$ , is the sum of the surplus for the buyer and the seller. The surplus of any buyer or seller not involved in a transaction is 0.*

**Theorem 1** (Surplus Calculation). *The calculation of surplus in the market does not depend on the clearing price.*

*Proof.* We define the surplus of the market as the summation of the surplus for each transaction. Note that for each transaction with buyer and seller  $B_i, S_j$ , the surplus is defined as  $s_{B_i, S_j} = c_i - p_j$  and thus does not depend on the clearing price.  $\square$