

Using Canonical eqⁿs of
Hamiltonian mechanics

$$H = \frac{1}{2} kx^2 + \frac{p^2}{2m}$$

$$\frac{\partial H}{\partial x} = -\frac{dp}{dt}$$

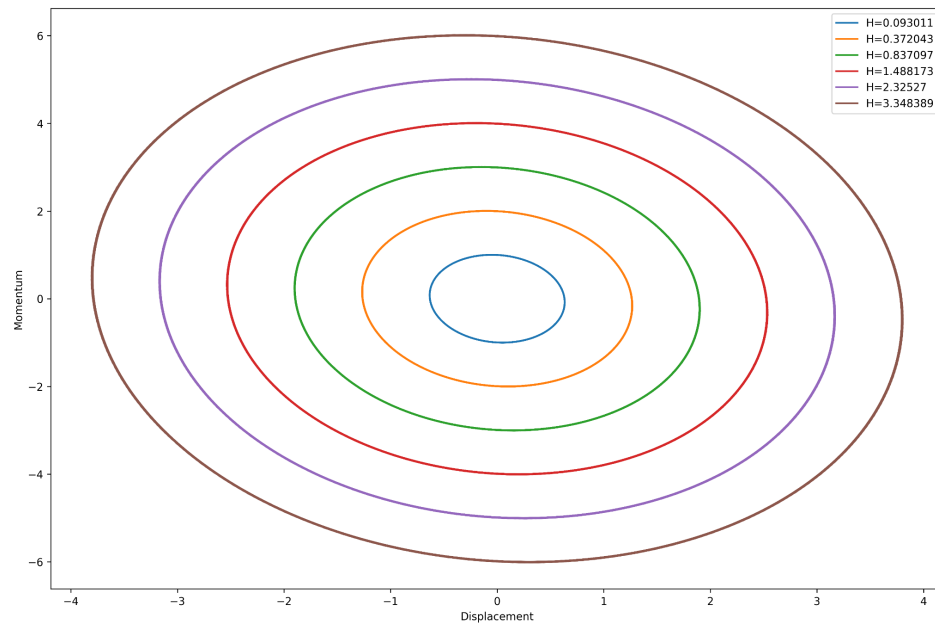
$$\frac{dp}{dt} = -\frac{\partial H}{\partial x} = -kx \quad \text{--- (1)}$$

$$\frac{dx}{dt} = \frac{\partial H}{\partial p} = \frac{p}{m} \quad \text{--- (2)}$$

So

$$\boxed{\begin{aligned} \frac{dp}{dt} &= -kx \\ \frac{dx}{dt} &= \frac{p}{m} \end{aligned}}$$

Time Evolution P and X



Mean Square Displacement with time

