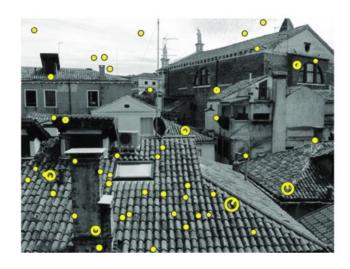
Laboratory of Image Processing

SIFT & MatLab



Pier Luigi Mazzeo pierluigi.mazzeo@cnr.it



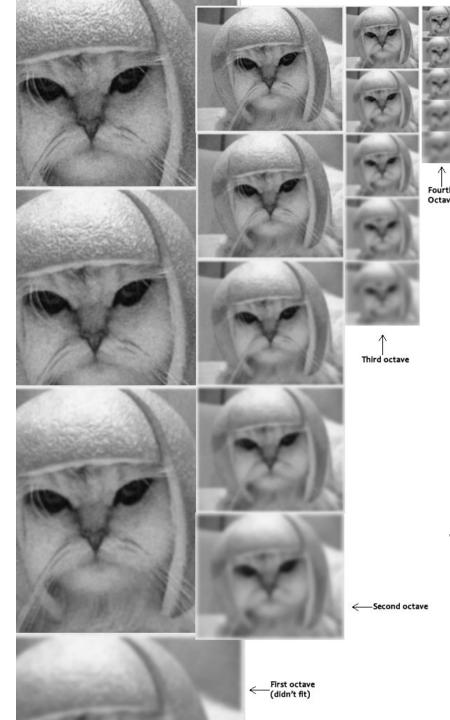


Sift purpose

- Find and describe interest points invariants to:
 - Scale
 - Rotation
 - Illumination
 - Viewpoint

Do it Yourself

- Constructing a scale space
- LoG Approximation
- Finding keypoints
- Get rid of bad key points (A technique similar to the Harris Corner Detector)
- Assigning an orientation to the keypoints
- Generate SIFT features



Construction of a scale space

SIFT takes scale spaces to the next level. You take the original image, and generate progressively blurred out images. Then, you resize the original image to half size. And you generate blurred out images again. And you keep repeating.

The creator of SIFT suggests that 4 octaves and 5 blur levels are ideal for the algorithm

Construction of a scale space (details)

The first octave

• If the original image is doubled in size and antialiased a bit (by blurring it) then the algorithm produces more four times more keypoints. The more the keypoints, the better!

Blurring

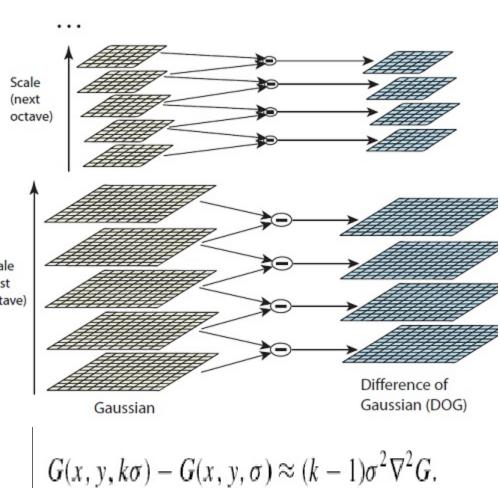
$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

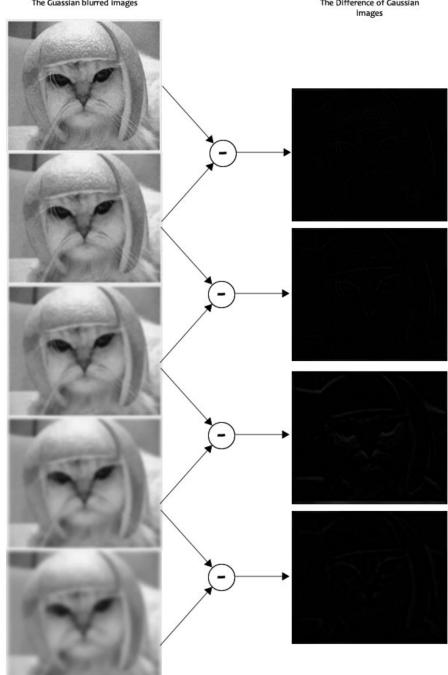
$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2}$$

Amount of Blurring

| | scale — | → | | | |
|--------|----------|----------|-----------|-----------|-----------|
| octave | 0.707107 | 1.000000 | 1.414214 | 2.000000 | 2.828427 |
| | 1.414214 | 2.000000 | 2.828427 | 4.000000 | 5.656854 |
| | 2.828427 | 4.000000 | 5.656854 | 8.000000 | 11.313708 |
| | 5.656854 | 8.000000 | 11.313708 | 16.000000 | 22.627417 |

LoG approximation





Design Gaussian filter

```
% gauss filter: Obtains a smoothed gaussian filter image
용
    - Output:
용
        smooth: image filter by a gaussian filter
용
    - Input:
        image: Matrix containing single band image.
        sigma: Value of the sigma for the Gaussian filter
        kernel size: Size of the gaussian kernel (default: 6*sigma)
function [smooth] = gauss filter(image, sigma, kernel size)
if nargin < 2
    sigma=1;
end
if nargin < 3
    kernel size=6*sigma;
end
gaussian radio=floor(kernel size/2); %radio of the gaussian
x=[-qaussian radio : qaussian radio]; % x values (qaussian kernel size)
gaussiano= \exp(-x.^2/(2*sigma^2))/(sigma*sgrt(2*pi)); %calculate the
unidimensional gaussian
%gaussiano=round(gaussian/min(abs(nonzeros(gaussian)))); %aproximate the
unidimensional kernel to integers
temp=conv2(double(image), double(gaussiano), 'same');
smooth=conv2(double(temp),double(gaussiano'),'same');
end
```

SIFT Matlab Implementation

```
% Obtain the SIFT interest points, and calculate the SIFT descriptor.
% INPUTS
    image: Image to look for interest points. The image is in gray scale.
   num octaves: Number of octaves
   num intervals: Number of intervals s in to achieve the double of the sigma
   value. In the original paper s=2
    sigmavalue: Value of the initial sigma
% OUTPUTS
    sift desc: matrix containing in each row an intersting point
    [x1 y1 octave num imagen in the scale sigma of the scale orientation(bins) ]
function [sift desc]=sift(image,num octaves,num intervals,sigmavalue)
[dimx,dimy]=size(image);
%define constants of the application
antialiassigma=0.5;
k1=2^{(1/num intervals)};
r curvature=5;
contrast threshold=0.03; %Threshold determining a low contrast keypoint to be eliminated
if sigmavalue>1.1
 % contrast threshold=0.07;
end
if sigmavalue==1.4
    contrast threshold=0.06;
End
updown=1;
```

SIFT Matlab Implementation: impyramid

Impyramid: implement Image pyramid reduction and expansion. If A is M-by-N and DIRECTION is 'reduce', then the size of B is ceil(M/2)-by-ceil(N/2). If DIRECTION is 'expand', then the size of B is (2*M-1)-by-(2*N-1).

```
I0 = imread('cameraman.tif');
I1 = impyramid(I0, 'expand');
I2 = impyramid(I1, 'reduce');
I3 = impyramid(I2, 'reduce');
imshow(I0)
figure, imshow(I1)
figure, imshow(I2)
figure, imshow(I3)
```

DOG: Example

```
%Allocate memory
gaussians = cell(4); dogs=cell(4);
%Expansions
init image=impyramid(gauss filter(I0,0.5,42),'expand');
%Gaussians filtering first interval
gaussians(1)={gauss filter(init image,1,4)};
previmage=cell2mat(gaussians(1)) %Obtain the previous image
imagesc(previmage);
%Gaussians filtering second interval
newimage=gauss_filter(previmage, 2, 8); %apply a new smoothing
Dog=newimage-previmage; %calculate the difference of gaussians
Gaussians(2)={newimage}; %Store the results
dogs(1) = {Dog};
imagesc(Dog);
```

SIFT Matlab Implementation: allocate memory

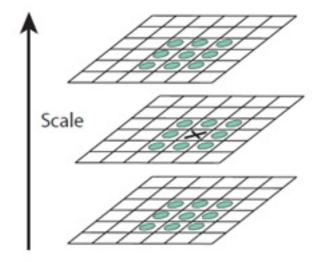
```
%normalize image input
% Assuming 8 bits image
image1=double(image)/255;
% %%%%%% Allocate memory %%%%%%%%%
qaussians = cell(num intervals+3,num octaves);
dogs=cell(num intervals+2, num octaves);
magnitude=cell(num intervals,num octaves);
orientation=cell(num intervals,num octaves);
for i=1:num octaves
   for j=1:num intervals+3
      qaussians(j,i)= {zeros(dimx/(2^(i-2)),dimy/(2^(i-2)))};
   end
   for j=1:num intervals+2
      dogs(j,i) = \{zeros(dimx/(2^{(i-2))},dimy/(2^{(i-2))})\};
   end
   for j=1:num intervals
       magnitude(j,i) = {zeros((dimx/(2^{(i-2)}))-2,(dimy/(2^{(i-2)}))-2)};
       orientation(j,i)={zeros((\dim x/(2^{(i-2)}))-2,(\dim y/(2^{(i-2)}))-2)};
   end
end
```

SIFT Matlab Implementation: DOG

```
% %%% Create first interval of the first octave %%%%%
init image=impyramid(gauss filter(image1,antialiassigma,4*antialiassigma),'expand');
qaussians(1)={qauss filter(init image, sigmavalue, 4*sigmavalue)};
 % %%% Generates all the blurred out images for each octave %%%%
                    and the DoG images
응 응응응
                                                            응응응응
for i=1:num octaves
   sigma=sigmavalue;
                      %reset the sigma value
   for j=1:(num intervals+2)
       sigma=sigma*2^((j-1)/2); %Assign a sigma value acording to the scale
       previmage=cell2mat(gaussians(j,i)); %Obtain the previous image
       newimage=gauss filter(previmage, sigma, 4*sigma); %apply a new smoothing
       dog=previmage-newimage; %calculate the difference of gaussians
       %save the results
       gaussians(j+1,i)={newimage};
       dogs(j,i) = \{dog\};
   end
   %Build the init image in the next level
   if(i<num octaves)</pre>
       lowscale=cell2mat(gaussians(num intervals+1,i));
       upscale=impyramid(lowscale, 'reduce');
       qaussians(1,i+1)={upscale};
   end
end
```

Finding keypoints

• a) Locate maxima/minima in DoG images



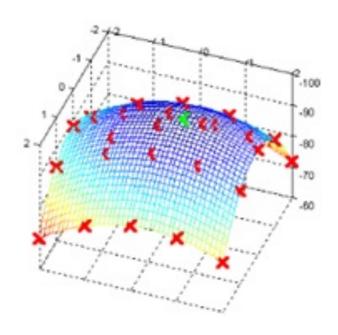
Local extrema detection, the pixel marked \times is compared against its 26 neighbors in a 3 \times 3 \times 3 neighborhood that spans adjacent DoG images.

Matlab Implementation (find local extrema)

```
list points=[];
for i=1:num octaves
                                       for j=2:(num intervals+1)
                                                                              % Obtain the matrices where to look for the extrema
                                                                             level=cell2mat(dogs(j,i));
                                                                             up=cell2mat(dogs(j+1,i));
                                                                             down=cell2mat(dogs(j-1,i));
                                                                              [sx,sy]=size(level);
                                                                             %look for a local maxima
                                                                             local maxima=(level(2:sx-1,2:sy-1)>level(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) > level(1:sx-2,2:sy-1) ) &
                                                        (level(2:sx-1,2:sy-1)>level(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>level(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(2
                                                      (level(2:sx-1,2:sy-1)>level(2:sx-1,2:sy-1)>level(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:sy-1)>level(3:sx-1,2:
                                                      & (level(2:sx-1,2:sy-1)>level(3:sx,3:sy));
                                                                             local maxima=local maxima & (level(2:sx-1,2:sy-1)>up(1:sx-2,1:sy-2)) & (level(2:sx-1,2:sy-1)>up(1:sx-2,2:sy-1)) & (level(2:sx-1,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1) & (level(2:sx-1,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1) & (level(2:sx-1,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-1)>up(1:sx-2,2:sy-
                                                      (level(2:sx-1,2:sy-1)>up(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,2:sy-1)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,2:sy-1)>up(2:sx-1,2:sy-1) & (level(2:sx-1,2:sy-1)>up(2:sx-1,2:sy-1) & (level(2:sx-1,2:sy-1)>up(2
                                                      (level(2:sx-1,2:sy-1)>up(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>up(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>up(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(3:sx,2:sy-1)>up(
                                                      (level(2:sx-1,2:sy-1)>up(3:sx,3:sy));
                                                                             local maxima=local maxima & (level(2:sx-1,2:sy-1)>down(1:sx-2,1:sy-2)) & (level(2:sx-1,2:sy-1)>down(1:sx-2,2:sy-1)) & (level(2:sx-1,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:sy-1)>down(1:sx-2,2:s
                                                      (level(2:sx-1,2:sy-1)>down(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1) & (level(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)>down(2:sx-1,2:s
                                                      & (level(2:sx-1,2:sy-1)>down(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>down(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>down(3:sx,2:sy-1)) &
                                                      (level(2:sx-1,2:sy-1)>down(3:sx,3:sy));
                                                                             %look for a local minima
                                                                             local minima=(level(2:sx-1,2:sy-1)<level(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) < level(1:sx-2,2:sy-1) ) &
                                                      (level(2:sx-1,2:sy-1) \le (lev
                                                      (level(2:sx-1,2:sy-1) < level(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1) < level(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1) < level(3:sx,2:sy-1)) 
                                                      & (level(2:sx-1,2:sy-1)>level(3:sx,3:sy));
                                                                             local minima=local minima & (level(2:sx-1,2:sy-1) \leq (1:sx-2,1:sy-2)) & (level(2:sx-1,2:sy-1) \leq (1:sx-2,2:sy-1)) & (level(2:sx-1,2:sy-1) \leq (1:sx-2,2:sy-1)) & (level(2:sx-1,2:sy-1) \leq (1:sx-2,2:sy-1)) & (level(2:sx-1,2:sy-1) \leq (1:sx-2,2:sy-1))
                                                      (level(2:sx-1,2:sy-1) \le (lev
                                                      (level(2:sx-1,2:sy-1) \le (lev
                                                      (level(2:sx-1,2:sy-1) < up(3:sx,3:sy));
                                                                              local minima=local minima & (level(2:sx-1,2:sy-1)<down(1:sx-2,1:sy-2)) & (level(2:sx-1,2:sy-1) < down(1:sx-2,2:sy-1)) & (level(2:sx-1,2:sy-1)) & 
                                                      (level(2:sx-1,2:sy-1) < down(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1) < down(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1) < down(2:sx-1,2:sy-1)) & (level(2:sx-1,2:sy-1)) & (level(
                                                      & (level(2:sx-1,2:sy-1) < down(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1) < down(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1) < down(3:sx,2:sy-1)) &
                                                      (level(2:sx-1,2:sy-1)<down(3:sx,3:sy));
                                                                             extrema=local maxima | local minima;
                   %INSERT THE PART OF RID BAD KEY POINT
                   end
```

Finding keypoints

• b) Find subpixel maxima/minima



$$D(\mathbf{x}) = D + \frac{\partial D}{\partial \mathbf{x}}^T \mathbf{x} + \frac{1}{2} \mathbf{x}^T \frac{\partial^2 D}{\partial \mathbf{x}^2} \mathbf{x}$$

Get rid of bad key points

Removing low contrast features

Tr(H) = Dxx + Dyy

If the magnitude of the intensity (i.e., without sign) at the current pixel in the DoG image (that is being checked for minima/maxima) is less than a certain value, it is rejected

Removing edges

Det(H) = DxxDyy - (Dxy)2

R = Tr(H)²/Det(H)

• If the value of R is greater for a candidate keypoint, then that keypoint is poorly localized and hence rejected.

$$H = \begin{bmatrix} D_{xx} D_{xy} \\ D_{xy} D_{yy} \end{bmatrix}$$

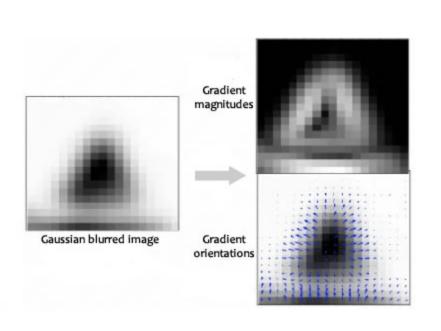
Matlab Implementation (remove poorly contrasted keypoints)

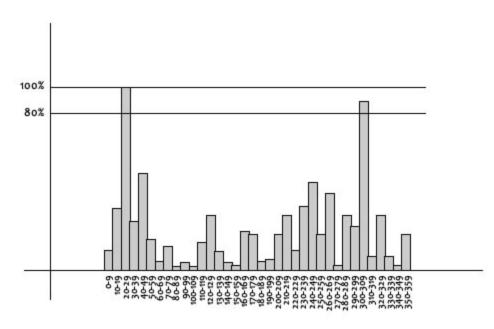
```
%indices of the extrema points
        [x,y]=find(extrema);
        numtimes=size(find(extrema));
        for k=1:numtimes
            x1=x(k);
           y1=y(k);
            if(abs(level(x1+1,y1+1))<contrast threshold)</pre>
                                                            %low contrast point are discarded
               extrema(x1,y1)=0;
                   %keep being extrema, check for edge
               rx=x1+1;
               ry=y1+1;
               fxx= level(rx-1,ry)+level(rx+1,ry)-2*level(rx,ry); % double derivate in x direction
               fyy= level(rx,ry-1)+level(rx,ry+1)-2*level(rx,ry); % double derivate in y direction
               fxy= level(rx-1,ry-1)+level(rx+1,ry+1)-level(rx-1,ry+1)-level(rx+1,ry-1); %derivate inx
    and y direction
               trace=fxx+fyy;
               deter=fxx*fyy-fxy*fxy;
               curvature=trace*trace/deter;
               curv threshold= ((r curvature+1)^2)/r curvature;
               if(deter<0 || curvature>curv threshold) %Reject edge points
                   extrema(x1,y1)=0;
               end
            end
        end
%check
list points=[list points; [x y repmat(i,numtimes,1) repmat(j-1,numtimes,1) zeros(numtimes,1)
zeros(numtimes,1)] ];
```

Plot KP-Position

```
list points= sift desc;
  figure; imshow(image,[]);hold on;
 x3=[];
 y3=[];
      for j=1:size(list points,1),
          x4=list points(j,2)*2^(list_points(j,3)-2);
          y4=list points(j,1)*2^(list points(j,3)-2);
          plot(x4 ,y4 , 'ro', 'color', [1 0 0], 'markerfacecolor', [1
0 0], 'markersize', 2.5 );
          x3=[x3;x4];
          y3=[y3;y4];
      end
      hold off
```

Assigning an orientation to the keypoints

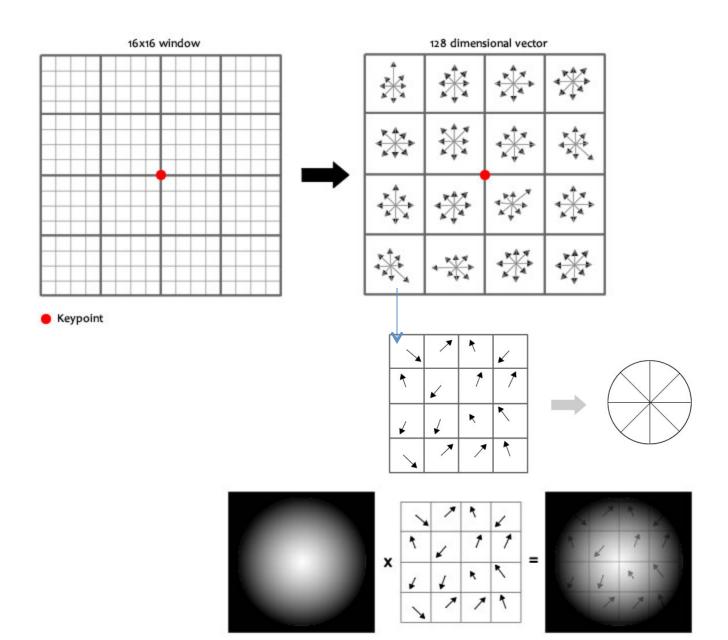




$$m(x,y) = \sqrt{(L(x+1,y) - L(x-1,y))^2 + (L(x,y+1) - L(x,y-1))^2}$$

$$\theta(x,y) = \tan^{-1}((L(x,y+1) - L(x,y-1))/(L(x+1,y) - L(x-1,y)))$$

Generate SIFT features



Generate SIFT features

- You take a 16×16 window of "in-between" pixels around the keypoint. You split that window into sixteen 4×4 windows. From each 4×4 window you generate a histogram of 8 bins. Each bin corresponding to 0-44 degrees, 45-89 degrees, etc. Gradient orientations from the 4×4 are put into these bins. This is done for all 4×4 blocks. Finally, you normalize the 128 values you get.
- To solve a few problems, you subtract the keypoint's orientation and also threshold the value of each element of the feature vector to 0.2 (and normalize again).

Matlab Implementation (KP-calculate magnitude and orientation)

```
% calculate magnitude, orientation
for i=1:num octaves
   for j=1:num intervals
      previmage=cell2mat(gaussians(j+updown,i)); %add 2 to
associate to the sigma of the upper image, or add 1 to associate to
the sigma of the lower one.
      [rx,ry]=size(previmage);
      dx=previmage(3:rx,2:ry-1)-previmage(1:rx-2,2:ry-1);
      dy=previmage(2:rx-1,1:ry-2)-previmage(2:rx-1,3:ry);
      mag=sqrt(dx.*dx + dy.*dy);
      ori=atan2(dy,dx);
      magnitude(j,i)={mag};
      orientation(j,i)={ori};
   end
end
```

GaussWindow Function

```
function [f,n] = gausswindow( s,n )
%gausswindow: Create a gaussian window
with kernel size given by n, and
%sigma given by s
   Detailed explanation goes here
if nargin<2
n=ceil(2*s); % force creation of options
end
x=-n:n;
[Y,X] = meshgrid(x,x);
f = \exp(-(X.^2+Y.^2)/(2*s^2));
end
```

Matlab Implementation (Calculate the KP-dominant orientation)

```
new ones=[];
% Calculate the orientation of the keypoints
points size=size(list points,1);
for i=1:points size %Look in the keypoints
   octave=list points(i,3); %octave of the interest point
   level=(list points(i,4))+updown; %level of the interest point
   x1=list points(i,1); % x position of the interest point
   y1=list points(i,2); % y position of the interest point
   sigma=sigmavalue*k1^(level-1); %calculate the sigma in the corresponding
scale
   list points(i,5)=sigma;
   mag=cell2mat(magnitude(level-updown,octave)); %magnitude of the gradient
   ori=cell2mat(orientation(level-updown,octave)); %direction of the gradient
    [weights,n]=gausswindow(1.5*sigma); %create weights around the interest point
   hist=zeros(36,1); %create an empty histogram
    [xmax,ymax]=size(mag);
```

Matlab Implementation (Calculate the KP-dominant orientation)

```
all=x1-n; % Positioning in the KP neighbors
a12=x1+n;
a21=y1-n;
a22=y1+n;
a31=1;
a32=2*n+1;
a41=1;
a42=2*n+1;
if((x1-n)<1) % Left of the minimum size
   a11=1;
   a31=n-x1+2;
end
if((y1-n)<1)
    a21=1;
    a41=n-y1+2;
end
if((x1+n)>xmax) % Right of the maximum size
    a12=xmax;
    a32=(2*n+1)-(x1+n-xmax);
end
if((y1+n)>ymax)
    a22=ymax;
    a42=(2*n+1)-(y1+n-ymax);
end
```

Matlab Implementation (Calculate the KP-dominant orientation)

```
w=mag(al1:al2,a21:a22).*weights(a31:a32,a41:a42); %weight of each pixel in the bin, after gaussian
                                                    weighting and magnitude assignation.
    ori=ori(a11:a12,a21:a22);
                                 % obtain the direction separated in bins of each one of the points near to
    ori=ceil((ori+pi)*18/pi);
                                   the keypoint
    [orix,oriy]=size(ori);
    %calculate histogram
    for i1=1:orix
        for j1=1:oriy
            hist(ori(i1, j1))=hist(ori(i1, j1))+w(i1, j1);
        end
    end
    [maxval,bin]=max(hist);
    list points(i,6)=bin;
    lista=find(hist>(0.8*maxval));
   more=size(lista,1);
    if(more>1)
        for i3=1:more
            if(lista(i3) ~= bin)
                new ones=[new ones; [x1 y1 octave list points(i,4) list points(i,5) lista(i3)]];
            end
        end
    end
end
sift desc=[list points];
```

ShowKeys Function

```
% showkeys(image, locs)
% This function displays an image with SIFT keypoints overlayed.
    Input parameters:
      image: the file name for the image (grayscale)
      locs: matrix in which each row gives a keypoint location (row,
            column, scale, orientation)
function showkeys(image, locs)
disp('Drawing SIFT keypoints ...');
% Draw image with keypoints
figure('Position', [50 50 size(image,2) size(image,1)]);
colormap('gray');
imagesc(image);
hold on;
imsize = size(image);
for i = 1: size(locs, 1)
    % Draw an arrow, each line transformed according to keypoint parameters.
    TransformLine(imsize, locs(i,:), 0.0, 0.0, 1.0, 0.0);
    TransformLine(imsize, locs(i,:), 0.85, 0.1, 1.0, 0.0);
    TransformLine(imsize, locs(i,:), 0.85, -0.1, 1.0, 0.0);
end
hold off;
```

ShowKeys Function

```
% ----- Subroutine: TransformLine -----
% Draw the given line in the image, but first translate, rotate, and
% scale according to the keypoint parameters.
% Parameters:
    Arrays:
    imsize = [rows columns] of image
    keypoint = [subpixel row subpixel column scale orientation]
    Scalars:
    x1, y1; begining of vector
    x2, y2; ending of vector
function TransformLine(imsize, keypoint, x1, y1, x2, y2)
% The scaling of the unit length arrow is set to approximately the radius
   of the region used to compute the keypoint descriptor.
len = 6 * keypoint(3);
% Rotate the keypoints by 'ori' = keypoint(4)
s = sin(keypoint(4));
c = cos(keypoint(4));
% Apply transform
r1 = keypoint(1) - len * (c * y1 + s * x1);
c1 = keypoint(2) + len * (- s * y1 + c * x1);
r2 = keypoint(1) - len * (c * y2 + s * x2);
c2 = keypoint(2) + len * (- s * y2 + c * x2);
line([c1 c2], [r1 r2], 'Color', 'c');
```

Matlab Implementation: Plot KP-Features

```
%%%PLOT FEATURES
dire=((list_points(:,6)/18))*pi + pi/2;
mag=(list_points(:,3))+list_points(:,4);
locs=[y3 x3 mag dire];
showkeys(image, locs);
end
```

Testing the detector

- i=imread('groceries_gray.jpg');
- Sift_Descriptor=sift(i,3,5,1.1);

VI_feat

 The VLFeat open source library implements popular computer vision algorithms including SIFT, MSER, k-means, hierarchical k-means, agglomerative information bottleneck, and quick shift. It is written in C for efficiency and compatibility, with interfaces in MATLAB for ease of use, and detailed documentation throughout. It supports Windows, Mac OS X, and Linux

VI_feat

- Download vl_feat from http://www.vlfeat.org/
- run('VLFEATROOT/toolbox/vl_setup')

- Permanent setup
 - To permanently add VLFeat to your MATLAB environment, add this line to your startup.m file:
 - run('VLFEATROOT/toolbox/vl_setup')

Extracting frames and descriptors

```
pfx = fullfile(vl root, 'data', 'roofs1.jpg');
I = imread(pfx);
image(I) ;
I = single(rgb2gray(I)) ;
[f,d] = vl sift(I) ;
perm = randperm(size(f,2));
sel = perm(1:50);
h1 = v1 plotframe(f(:,sel));
h2 = v1 plotframe(f(:,sel));
set(h1, 'color', 'k', 'linewidth', 3);
set(h2,'color','y','linewidth',2);
h3 = v1 plotsiftdescriptor(d(:,sel),f(:,sel)) ;
set(h3,'color','g')
```

Basic Matching

```
pfx1 = fullfile(vl_root, 'data', 'roofs1.jpg');
Ia = imread(pfx1);
pfx2 = fullfile(vl_root, 'data', 'roofs2.jpg');
Ib = imread(pfx2);
[fa, da] = vl_sift(Ia);
[fb, db] = vl_sift(Ib);
[matches, scores] = vl_ubcmatch(da, db);
```

Visualization

```
m1= fa (1:2, matches(1,:));
m2=fb(1:2, matches(2,:));
m2(1,:) =
m2(1,:)+640*ones(1,size(m2,2));
X = [m1(1,:); m2(1,:)];
Y = [m1(2,:); m2(2,:)];
imshow(c);
hold on;
line(X,Y)
vl plotframe(aframe(:,matches(1,:)));
vl plotframe(m2);
```

Custom frames

- The MATLAB command vl_sift (and the command line utility) can bypass the detector and compute the descriptor on custom frames using the Frames option.
- For instance, we can compute the descriptor of a SIFT frame centered at position (100,100), of scale 10 and orientation -pi/8 by

```
fc = [100;100;10;-pi/8];
[f,d] = vl_sift(I,'frames',fc);
fc = [100;100;10;0];
[f,d] = vl_sift(I,'frames',fc,'orientations');
```