

Question 1:

1)

Given relation $R(L, M, N, O, P, Q)$;

functional dependencies $F = \{LNO \rightarrow M, MN \rightarrow LO, N \rightarrow O, OP \rightarrow LN\}$. Can we infer $NP \rightarrow LM$

We break this down as $NP \rightarrow L$ and $NP \rightarrow M$

From functional dependencies

$N \rightarrow O$ ($NP \rightarrow OP$ FROM augmentation rule)

$OP \rightarrow L$

Therefore $NP \rightarrow L$ is true.

$NP \rightarrow L$ from above

$NP \rightarrow N$ from trivial rule

$NP \rightarrow P$ from trivial rule

$N \rightarrow O$

From above

$NP \rightarrow LNO$

$LNO \rightarrow M$

$NP \rightarrow M$ it is true

Both are true it satisfies $NP \rightarrow LM$.

2) $NQ \rightarrow LO$

Breakdown $NQ \rightarrow L$ AND $NQ \rightarrow O$ Check if $NQ \rightarrow L$:

$N \rightarrow O$

$OP \rightarrow L$

IN THE GIVEN F

L CAN BE DERIVED USING $MN \rightarrow L$

$OP \rightarrow L$

SO, L cannot be derived using NQ Therefore $NQ \rightarrow L$ is not possible $NQ \rightarrow LO$ is not possible

Question2:

A)

As per the edge diagram we don't have incoming edges for B and E.

So it could be possible for candidate key with combination of other attributes. Now add each attribute to find closure:

$(ABE)^+, (CBE)^+, (DBE)^+$

closure of $(ABE)^+$ is $\{A, B, E, D, C\}$

Therefore it is candidate key;

closure of $(CBE)^+$ is $\{C, B, E, A, D\}$

Therefore it is candidate key;

closure of $(DBE)^+$ is $\{D, B, E, A, C\}$

Therefore it is candidate key;

All candidate keys are $(ABE)^+, (CBE)^+, (DBE)^+$

B)

As per the edge diagram we don't have incoming edges for A, B and E.

So it could be possible for candidate key with combination of other attributes. Now add each attribute to find closure:

$(ABCE)^+, (ABDE)^+, (ABEF)^+$

closure of $(ABCE)^+$ is $\{A, B, C, E\}$ Therefore it is not a candidate key;

closure of $(ABDE)^+$ is $\{A,B,E,D\}$ Therefore it is not a candidate key; closure of $(ABEF)^+$ is $\{A,B,E,F,C,D\}$
Therefore it is candidate key;

THEREFORE CANDIDATE KEY IS $(ABEF)^+$;

$(ABEF)^+$ ITSELF IS A SUPERKEY;

Add two attribute C,D to $(ABEF)^+$

$(ABCEF)^+$ is a super key;

$(ABDEF)^+$ is a super key;

$(ABCDEF)^+$ is a super key;

$(ABEF)^+$, $(ABCEF)^+$, $(ABDEF)^+$, $(ABCDEF)^+$ are superkey's

Question3:

Minimal cover of F

Every dependency in F must have a single attribute on the right hand side.

$Z \rightarrow UT \Rightarrow Z \rightarrow U, Z \rightarrow T$

Remove all extraneous attributes such as $P \rightarrow Y$ and $PQ \rightarrow Y$ then Q is extraneous attribute

So, $X \rightarrow Z$ and $XY \rightarrow Z$ then Y is extraneous attribute so remove it $\Rightarrow X \rightarrow Y$

So, In given Functional dependencies: -

1. Convert Right hand side attribute into single
 $Z \rightarrow U, Z \rightarrow T, ZW \rightarrow X, ZW \rightarrow Y$
2. Remove extraneous attribute: $X \rightarrow Z, XY \rightarrow Z$
 $Z \rightarrow T, ZU \rightarrow T \Rightarrow Z \rightarrow T$
3. Remove redundant Functional dependencies :
 $X \rightarrow Z, Z \rightarrow T$

So, minimal cover of given F is :-

$X \rightarrow Z, Z \rightarrow U, Z \rightarrow T, ZW \rightarrow X, ZW \rightarrow Y, WT \rightarrow Z$

Question4:

Equivalent conditions are FD1 covers FD2 and FD2 covers FD1.

Equivalent with FD2: Check if FD2 covers FD1:

Part of relations in FD1: $BC \rightarrow D$, $AB \rightarrow C$, $C \rightarrow A$, $D \rightarrow E$, $BE \rightarrow C$, $D \rightarrow G$, are already in FD2, so we do not need to find them in FD2.

The rest of relations in FD1: $ACD \rightarrow ACDBEG$ so, $ACD \rightarrow B$.

$CG \rightarrow CGADBEG$ so, $CG \rightarrow B$, $CG \rightarrow D$.

$CE \rightarrow CEA$ so, $CE \rightarrow A$, but $CE \rightarrow G$ in FD1 is not covered by FD2.

Finally, FD1 and FD2 are not equivalent.

Equivalent conditions are FD1 covers FD3 and FD3 covers FD1. Equivalent with FD3: Check if FD3 covers FD1:

Part of relations in FD1: $BC \rightarrow D$, $CG \rightarrow D$, $AB \rightarrow C$, $C \rightarrow A$, $D \rightarrow E$, $BE \rightarrow C$, $D \rightarrow G$, $CE \rightarrow G$, are already in FD3, so we do not need to find them in FD3.

The rest of relations in FD1: $ACD \rightarrow ACDGEB$ so, $ACD \rightarrow B$. $CG \rightarrow CGDEAB$ so, $CG \rightarrow B$.

$CE \rightarrow CEGADB$ so, $CE \rightarrow A$.

As a result, FD3 covers FD1.

Check if FD1 covers FD3:

Similarly, $AB \rightarrow C$, $C \rightarrow A$, $D \rightarrow G$, $BE \rightarrow C$, $CG \rightarrow D$, $CE \rightarrow G$, $BC \rightarrow D$, $D \rightarrow E$ are not in FD1. $CD \rightarrow CDAEGB$ so, $CD \rightarrow B$.

As a result, FD1 covers FD3.

Finally, FD1 and FD3 are equivalent.