AES Example - Input (128 bit key and message)

Key in English: Thats my Kung Fu (16 ASCII characters, 1 byte each)

Translation into Hex:

T	h	a	t	s		m	y		K	u	n	g		F	u
54	68	61	74	73	20	6D	79	20	4B	75	6E	67	20	46	75

Key in Hex (128 bits): 54 68 61 74 73 20 6D 79 20 4B 75 6E 67 20 46 75

Plaintext in English: Two One Nine Two (16 ASCII characters, 1 byte each)

Translation into Hex:

T	w	o		O	n	e		N	i	n	e		T	w	o
54	77	6F	20	4F	6E	65	20	4E	69	6E	65	20	54	77	6F

Plaintext in Hex (128 bits): 54 77 6F 20 4F 6E 65 20 4E 69 6E 65 20 54 77 6F

AES Example - The first Roundkey

- Key in Hex (128 bits): 54 68 61 74 73 20 6D 79 20 4B 75 6E 67 20 46 75
- $w[0] = (54, 68, 61, 74), w[1] = (73, 20, 6D, 79), w[2] = (20, 4B, 75, 6E), w[3] = (67, 20, 46, 75)$
- $g(w[3])$:
  - circular byte left shift of $w[3]$: $(20, 46, 75, 67)$
  - Byte Substitution (S-Box): $(B7, 5A, 9D, 85)$
  - Adding round constant $(01, 00, 00, 00)$ gives: $g(w[3]) = (B6, 5A, 9D, 85)$
- $w[4] = w[0] \oplus g(w[3]) = (E2, 32, FC, F1)$:

0101 0100	0110 1000	0110 0001	0111 0100
1011 0110	0101 1010	1001 1101	1000 0101
1110 0010	0011 0010	1111 1100	1111 0001
E2	32	FC	F1

- $w[5] = w[4] \oplus w[1] = (91, 12, 91, 88)$, $w[6] = w[5] \oplus w[2] = (B1, 59, E4, E6)$, $w[7] = w[6] \oplus w[3] = (D6, 79, A2, 93)$
- first roundkey: E2 32 FC F1 91 12 91 88 B1 59 E4 E6 D6 79 A2 93

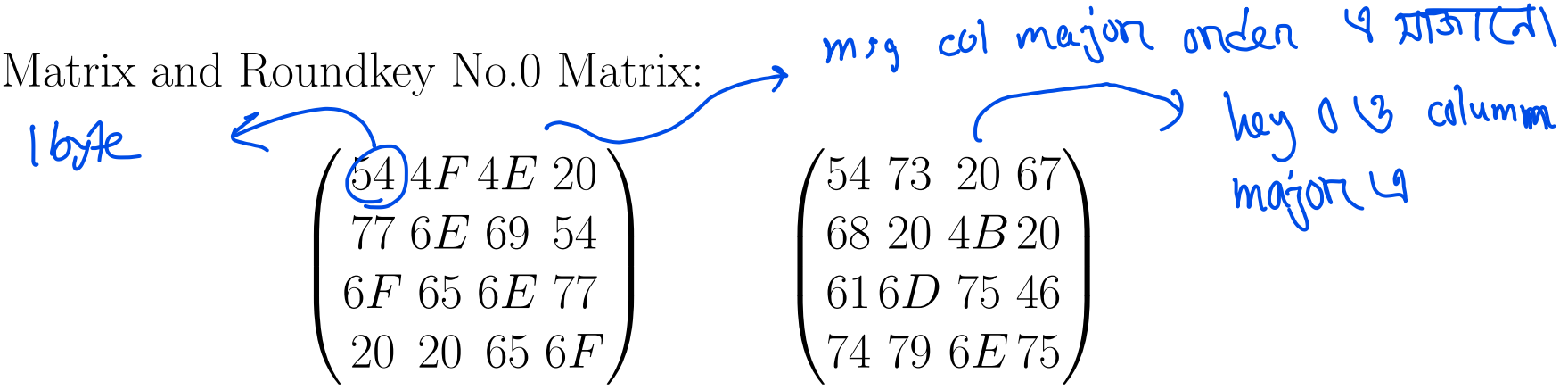
AES Example - All RoundKeys

- Round 0: 54 68 61 74 73 20 6D 79 20 4B 75 6E 67 20 46 75
- Round 1: E2 32 FC F1 91 12 91 88 B1 59 E4 E6 D6 79 A2 93
- Round 2: 56 08 20 07 C7 1A B1 8F 76 43 55 69 A0 3A F7 FA
- Round 3: D2 60 0D E7 15 7A BC 68 63 39 E9 01 C3 03 1E FB
- Round 4: A1 12 02 C9 B4 68 BE A1 D7 51 57 A0 14 52 49 5B
- Round 5: B1 29 3B 33 05 41 85 92 D2 10 D2 32 C6 42 9B 69
- Round 6: BD 3D C2 B7 B8 7C 47 15 6A 6C 95 27 AC 2E 0E 4E
- Round 7: CC 96 ED 16 74 EA AA 03 1E 86 3F 24 B2 A8 31 6A
- Round 8: 8E 51 EF 21 FA BB 45 22 E4 3D 7A 06 56 95 4B 6C
- Round 9: BF E2 BF 90 45 59 FA B2 A1 64 80 B4 F7 F1 CB D8
- Round 10: 28 FD DE F8 6D A4 24 4A CC C0 A4 FE 3B 31 6F 26

eivabe kore total 44 ta word

AES Example - Add Roundkey, Round 0

- State Matrix and Roundkey No.0 Matrix:



$$\begin{pmatrix} 54 & 4F & 4E & 20 \\ 77 & 6E & 69 & 54 \\ 6F & 65 & 6E & 77 \\ 20 & 20 & 65 & 6F \end{pmatrix} \qquad \begin{pmatrix} 54 & 73 & 20 & 67 \\ 68 & 20 & 4B & 20 \\ 61 & 6D & 75 & 46 \\ 74 & 79 & 6E & 75 \end{pmatrix}$$

- XOR the corresponding entries, e.g., $69 \oplus 4B = 22$

$$\begin{array}{r} 0110\ 1001 \\ 0100\ 1011 \\ \hline 0010\ 0010 \end{array}$$

- the new State Matrix is

$$\begin{pmatrix} 00 & 3C & 6E & 47 \\ 1F & 4E & 22 & 74 \\ 0E & 08 & 1B & 31 \\ 54 & 59 & 0B & 1A \end{pmatrix}$$

AES Example - Round 1, Substitution Bytes

- current State Matrix is

$$\begin{pmatrix} 00 & 3C & 6E & 47 \\ 1F & 4E & 22 & 74 \\ 0E & 08 & 1B & 31 \\ 54 & 59 & 0B & 1A \end{pmatrix}$$

- substitute each entry (byte) of current state matrix by corresponding entry in AES S-Box
- for instance: byte 6E is substituted by entry of S-Box in row 6 and column E, i.e., by 9F
- this leads to new State Matrix

$$\begin{pmatrix} 63 & EB & 9F & A0 \\ C0 & 2F & 93 & 92 \\ AB & 30 & AF & C7 \\ 20 & CB & 2B & A2 \end{pmatrix}$$

- this non-linear layer is for resistance to differential and linear cryptanalysis attacks

AES Example - Round 1, Shift Row

- the current State Matrix is

$$\begin{pmatrix} 63 & EB & 9F & A0 \\ C0 & 2F & 93 & 92 \\ AB & 30 & AF & C7 \\ 20 & CB & 2B & A2 \end{pmatrix}$$

- four rows are shifted cyclically to the left by offsets of 0,1,2, and 3
- the new State Matrix is

$$\begin{pmatrix} 63 & EB & 9F & A0 \\ 2F & 93 & 92 & C0 \\ AF & C7 & AB & 30 \\ A2 & 20 & CB & 2B \end{pmatrix}$$

- this linear mixing step causes diffusion of the bits over multiple rounds

AES Example - Round 1, Mix Column

- Mix Column multiplies fixed matrix against current State Matrix:

$$\begin{pmatrix} 02\,03\,01\,01 \\ 01\,02\,03\,01 \\ 01\,01\,02\,03 \\ 03\,01\,01\,02 \end{pmatrix} \begin{pmatrix} 63 & EB & 9F & A0 \\ 2F & 93 & 92 & C0 \\ AF & C7 & AB & 30 \\ A2 & 20 & CB & 2B \end{pmatrix} = \begin{pmatrix} BA & 84 & E8 & 1B \\ 75 & A4 & 8D & 40 \\ F4 & 8D & 06 & 7D \\ 7A & 32 & 0E & 5D \end{pmatrix}$$

- entry BA is result of $(02 \bullet 63) \oplus (03 \bullet 2F) \oplus (01 \bullet AF) \oplus (01 \bullet A2)$:
  - $02 \bullet 63 = 00000010 \bullet 01100011 = 11000110$
  - $03 \bullet 2F = (02 \bullet 2F) \oplus 2F = (00000010 \bullet 00101111) \oplus 00101111 = 01110001$
  - $01 \bullet AF = AF = 10101111$ and $01 \bullet A2 = A2 = 10100010$
  - hence

$$\begin{array}{r} 11000110 \\ 01110001 \\ 10101111 \\ 10100010 \\ \hline 10111010 \end{array}$$

AES Example - Add Roundkey, Round 1

- State Matrix and Roundkey No.1 Matrix:

New Round Key

$$\begin{pmatrix} BA & 84 & E8 & 1B \\ 75 & A4 & 8D & 40 \\ F4 & 8D & 06 & 7D \\ 7A & 32 & 0E & 5D \end{pmatrix} \qquad \begin{pmatrix} E2 & 91 & B1 & D6 \\ 32 & 12 & 59 & 79 \\ FC & 91 & E4 & A2 \\ F1 & 88 & E6 & 93 \end{pmatrix}$$

- XOR yields new State Matrix

$$\begin{pmatrix} 58 & 15 & 59 & CD \\ 47 & B6 & D4 & 39 \\ 08 & 1C & E2 & DF \\ 8B & BA & E8 & CE \end{pmatrix}$$

- AES output after Round 1: 58 47 08 8B 15 B6 1C BA 59 D4 E2 E8 CD 39 DF CE

AES Example - Round 2

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} 6A & 59 & CB & BD \\ A0 & 4E & 48 & 12 \\ 30 & 9C & 98 & 9E \\ 3D & F4 & 9B & 8B \end{pmatrix} \qquad \begin{pmatrix} 6A & 59 & CB & BD \\ 4E & 48 & 12 & A0 \\ 98 & 9E & 30 & 9B \\ 8B & 3D & F4 & 9B \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} 15 & C9 & 7F & 9D \\ CE & 4D & 4B & C2 \\ 89 & 71 & BE & 88 \\ 65 & 47 & 97 & CD \end{pmatrix} \qquad \begin{pmatrix} 43 & 0E & 09 & 3D \\ C6 & 57 & 08 & F8 \\ A9 & C0 & EB & 7F \\ 62 & C8 & FE & 37 \end{pmatrix}$$

AES Example - Round 3

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} 1A & AB & 01 & 27 \\ B4 & 5B & 30 & 41 \\ D3 & BA & E9 & D2 \\ AA & E8 & BB & 9A \end{pmatrix} \qquad \begin{pmatrix} 1A & AB & 01 & 27 \\ 5B & 30 & 41 & B4 \\ E9 & D2 & D3 & BA \\ A9 & AA & E8 & BB \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} AA & 65 & FA & 88 \\ 16 & 0C & 05 & 3A \\ 3D & C1 & DE & 2A \\ B3 & 4B & 5A & 0A \end{pmatrix} \qquad \begin{pmatrix} 78 & 70 & 99 & 4B \\ 76 & 76 & 3C & 39 \\ 30 & 7D & 37 & 34 \\ 54 & 23 & 5B & F1 \end{pmatrix}$$

AES Example - Round 4

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} BC & 51 & EE & B3 \\ 38 & 38 & EB & 12 \\ 04 & FF & 9A & 18 \\ 20 & 26 & 39 & A1 \end{pmatrix} \qquad \begin{pmatrix} BC & 51 & EE & B3 \\ 38 & EB & 12 & 38 \\ 9A & 18 & 04 & FF \\ A1 & 20 & 26 & 39 \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} 10 & BC & D3 & F3 \\ D8 & 94 & E0 & E0 \\ 53 & EA & 9E & 25 \\ 24 & 40 & 73 & 7B \end{pmatrix} \qquad \begin{pmatrix} B1 & 08 & 04 & E7 \\ CA & FC & B1 & B2 \\ 51 & 54 & C9 & 6C \\ ED & E1 & D3 & 20 \end{pmatrix}$$

AES Example - Round 5

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} C8 & 30 & F2 & 94 \\ 74 & B0 & C8 & 37 \\ D1 & 20 & DD & 50 \\ 55 & F8 & 66 & B7 \end{pmatrix} \qquad \begin{pmatrix} C8 & 30 & F2 & 94 \\ B0 & C8 & 37 & 74 \\ DD & 50 & D1 & 20 \\ B7 & 55 & F8 & 66 \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} 2A & 26 & 8F & E9 \\ 78 & 1E & 0C & 7A \\ 1B & A7 & 6F & 0A \\ 5B & 62 & 00 & 3F \end{pmatrix} \qquad \begin{pmatrix} 9B & 23 & 5D & 2F \\ 51 & 5F & 1C & 38 \\ 20 & 22 & BD & 91 \\ 68 & F0 & 32 & 56 \end{pmatrix}$$

AES Example - Round 6

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} 14 & 26 & 4C & 15 \\ D1 & CF & 9C & 07 \\ B7 & 93 & 7A & 81 \\ 45 & 8C & 23 & B1 \end{pmatrix} \qquad \begin{pmatrix} 14 & 26 & 4C & 15 \\ CF & 9C & 07 & D1 \\ 7A & 81 & B7 & 93 \\ B1 & 45 & 8C & 23 \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} A9 & 37 & AA & F2 \\ AE & D8 & 0C & 21 \\ E7 & 6C & B1 & 9C \\ F0 & FD & 67 & 3B \end{pmatrix} \qquad \begin{pmatrix} 14 & 8F & C0 & 5E \\ 93 & A4 & 60 & 0F \\ 25 & 2B & 24 & 92 \\ 77 & E8 & 40 & 75 \end{pmatrix}$$

AES Example - Round 7

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} FA & 73 & BA & 58 \\ DC & 49 & D0 & 76 \\ 3F & F1 & 36 & 4F \\ F5 & 9B & 09 & 9D \end{pmatrix} \qquad \begin{pmatrix} FA & 73 & BA & 58 \\ 49 & D0 & 76 & DC \\ 36 & 4F & 3F & F1 \\ 9D & F5 & 9B & 09 \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} 9F & 37 & 51 & 37 \\ AF & EC & 8C & FA \\ 63 & 39 & 04 & 66 \\ 4B & FB & B1 & D7 \end{pmatrix} \qquad \begin{pmatrix} 53 & 43 & 4F & 85 \\ 39 & 06 & 0A & 52 \\ 8E & 93 & 3B & 57 \\ 5D & F8 & 95 & BD \end{pmatrix}$$

AES Example - Round 8

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} ED & 1A & 84 & 97 \\ 12 & 6F & 67 & 00 \\ 19 & DC & E2 & 5B \\ 4C & 41 & 2A & 7A \end{pmatrix} \qquad \begin{pmatrix} ED & 1A & 84 & 97 \\ 6F & 67 & 00 & 12 \\ E2 & 5B & 19 & DC \\ 7A & 4C & 41 & 2A \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} E8 & 8A & 4B & F5 \\ 74 & 75 & EE & E6 \\ D3 & 1F & 75 & 58 \\ 55 & 8A & 0C & 38 \end{pmatrix} \qquad \begin{pmatrix} 66 & 70 & AF & A3 \\ 25 & CE & D3 & 73 \\ 3C & 5A & 0F & 13 \\ 74 & A8 & 0A & 54 \end{pmatrix}$$

AES Example - Round 9

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} 33 & 51 & 79 & 0A \\ 3F & 8B & 66 & 8F \\ EB & BE & 76 & 7D \\ 92 & C2 & 67 & 20 \end{pmatrix} \qquad \begin{pmatrix} 33 & 51 & 79 & 0A \\ 8B & 66 & 8F & 3F \\ 76 & 7D & EB & BE \\ 20 & 92 & C2 & 67 \end{pmatrix}$$

- after Mixcolumns and after Roundkey:

$$\begin{pmatrix} B6 & E7 & 51 & 8C \\ 84 & 88 & 98 & CA \\ 34 & 60 & 66 & FB \\ E8 & D7 & 70 & 51 \end{pmatrix} \qquad \begin{pmatrix} 09 & A2 & F0 & 7B \\ 66 & D1 & FC & 3B \\ 8B & 9A & E6 & 30 \\ 78 & 65 & C4 & 89 \end{pmatrix}$$

AES Example - Round 10

- after Substitute Byte and after Shift Rows:

$$\begin{pmatrix} 01 & 3A & 8C & 21 \\ 33 & 3E & B0 & E2 \\ 3D & B8 & 8E & 04 \\ BC & 4D & 1C & A7 \end{pmatrix} \leftarrow \begin{pmatrix} 01 & 3A & 8C & 21 \\ 3E & B0 & E2 & 33 \\ 8E & 04 & 3D & B8 \\ A7 & BC & 4D & 1C \end{pmatrix}$$

- after Roundkey (Attention: no Mix columns in last round):

$$\begin{pmatrix} 29 & 57 & 40 & 1A \\ C3 & 14 & 22 & 02 \\ 50 & 20 & 99 & D7 \\ 5F & F6 & B3 & 3A \end{pmatrix}$$

- ciphertext: 29 C3 50 5F 57 14 20 F6 40 22 99 B3 1A 02 D7 3A

Then Ciphertext Done