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In [5]:

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r=0.0002981060
t=0.0222834

import math
import numpy as np
import random
import matplotlib.pyplot as plt
import statistics

def norm():
    a=random.random()
    b=random.random()
    A,B=2*a-1, 2*b-1
    x=A*A+B*B
    while x>1:
        a=random.random()
        b=random.random()
        A,B=2*a-1, 2*b-1
        x=A*A+B*B
    z=math.sqrt(-2*math.log(x)/x)
    return(z*A)

def lognormal(k):
    sum=0
    for j in range(k):
        m=norm()
        m=r+t*m
        sum=sum+m
    return sum

Price_1=[]
Price_2=[]
for i in range(10000):
    stock=185.4
    d=0.1
    e=math.sqrt(d)
    normal=[]
    price=[]
    poisson=np.random.poisson(0.01,301)
    for j in range(301):
        k=norm()
        normal.append(k)
    for j in range(301):
        k=poisson[j]
        if k!=0:
            z=lognormal(k)
            z=z+(r-(0.5*t*t))*d+t*normal[j]*e
            stock=stock*math.exp(z)
            price.append(stock)

        if k==0:
            z=(r-(0.5*t*t))*d+t*normal[j]*e
            stock=stock*math.exp(z)
            price.append(stock)

K=1.1*185.4
s=0
for j in range(301):
    s=s+price[j]
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l=K-(s/301)
if l<0:
    l=0
Price_1.append(l)

Put_price=K-price[299]
if Put_price<0:
    Price_2.append(0)
if Put_price>=0:
    Price_2.append(Put_price)
P_1=[]
for j in range(1000):
    P_1.append(Price_1[j])
A=statistics.mean(P_1)
B=statistics.mean(Price_2)
C=statistics.variance(Price_2)
D=statistics.variance(P_1)
sum=0
for j in range(10000):
    sum+=(Price_1[j]-A)*(Price_2[j]-B)

alpha=sum/(10000*C)

actual=[]
for i in range(1000):
    stock=185.4
    d=0.1
    e=math.sqrt(d)
    normal=[]
    price=[]
    poisson=np.random.poisson(0.01,301)
    for j in range(301):
        k=norm()
        normal.append(k)
    for j in range(301):
        k=poisson[j]
        if k!=0:
            z=lognormal(k)
            z=z+(r-(0.5*t*t))*d+t*normal[j]*e
            stock=stock*math.exp(z)
            price.append(stock)

        if k==0:
            z=(r-(0.5*t*t))*d+t*normal[j]*e
            stock=stock*math.exp(z)
            price.append(stock)

K=1.1*185.4
s=0
for j in range(301):
    s=s+price[j]
l=K-(s/301)
if l<0:
    l=0
Put_price=K-price[299]
if Put_price<0:
    Put_price=0
random_variable=l-alpha*(Put_price-B)
actual.append(random_variable)

```

```
print("The mean and variance respectively of average value Asian put option calculated without using control variate are:", A,D)
print("The mean of the same option by using the price of an European put as the control variate :", statistics.mean(actual))
print("The variance of the control variate estimator : " , statistics.variance(actual) )
```

The mean and variance respectively of average value Asian put option calculated without using control variate are: 18.736032528740036 159.66627492487626

The mean of the same option by using the price of an European put as the control variate : 18.573794698674227

The variance of the control variate estimator : 43.82956335858122

In [ ]: