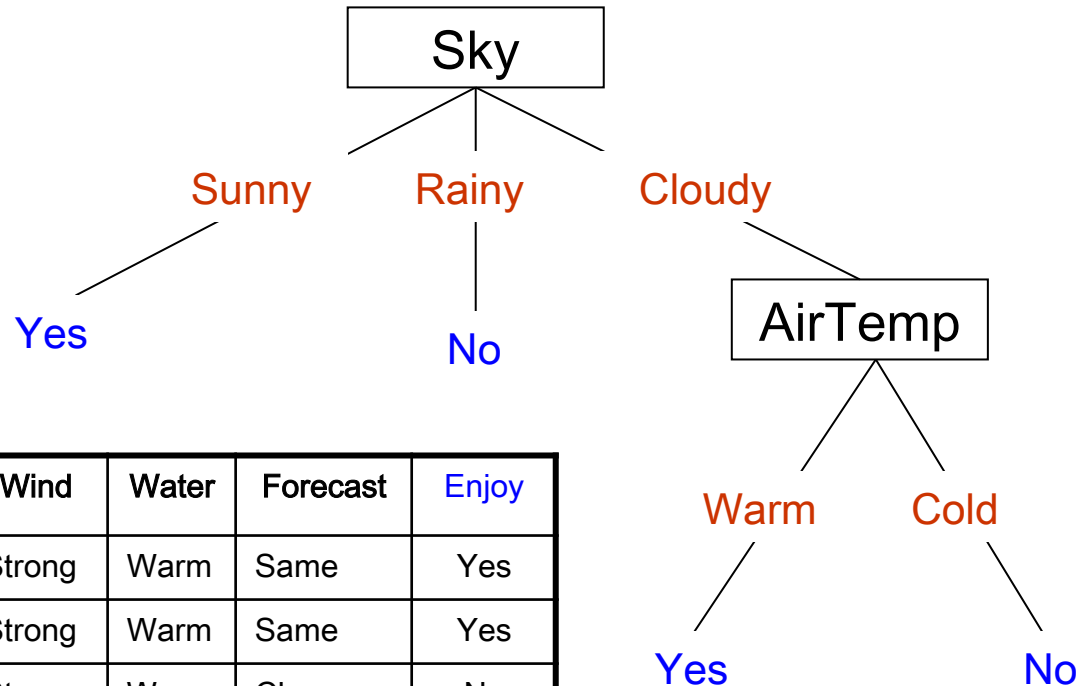


Decision Trees

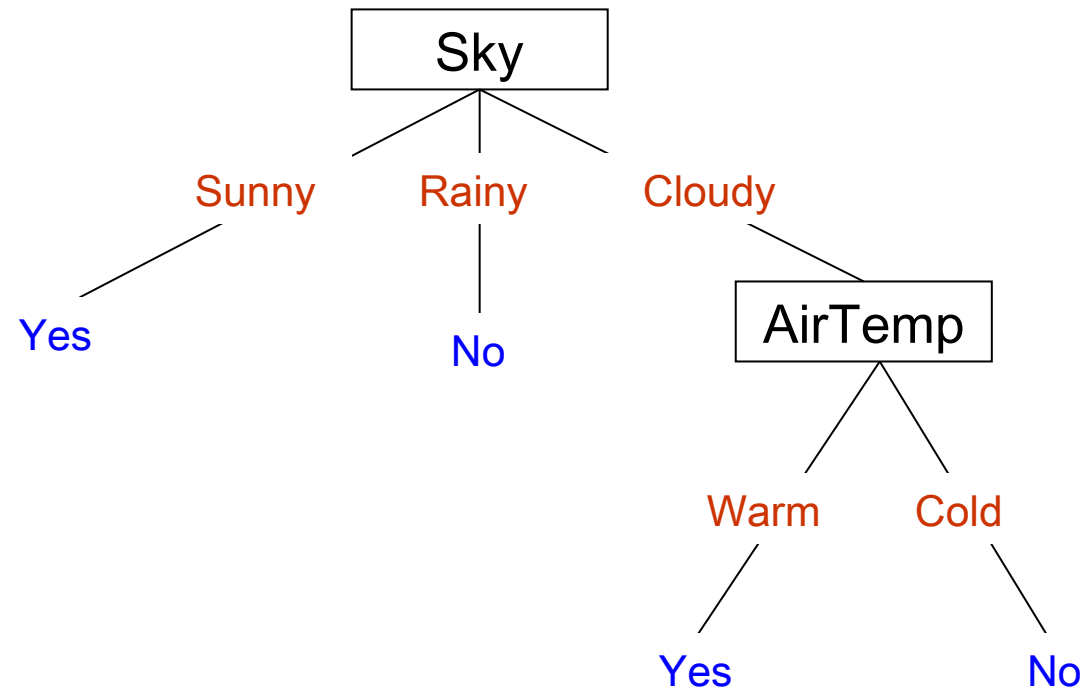
Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes
5	Cloudy	Warm	High	Weak	Cool	Same	Yes
6	Cloudy	Cold	High	Weak	Cool	Same	No

Decision Trees



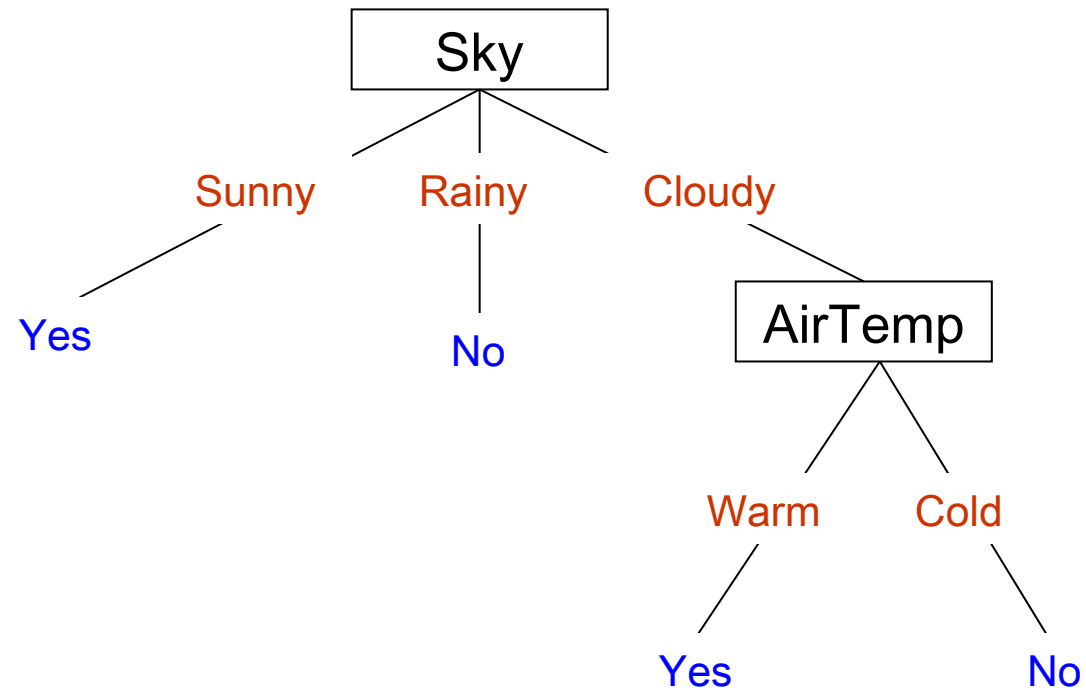
No.	Sky	AirTemp	Humidity	Wind	Water	Forecast	Enjoy
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes
5	Cloudy	Warm	High	Weak	Cool	Same	Yes
6	Cloudy	Cold	High	Weak	Cool	Same	No

Decision Trees



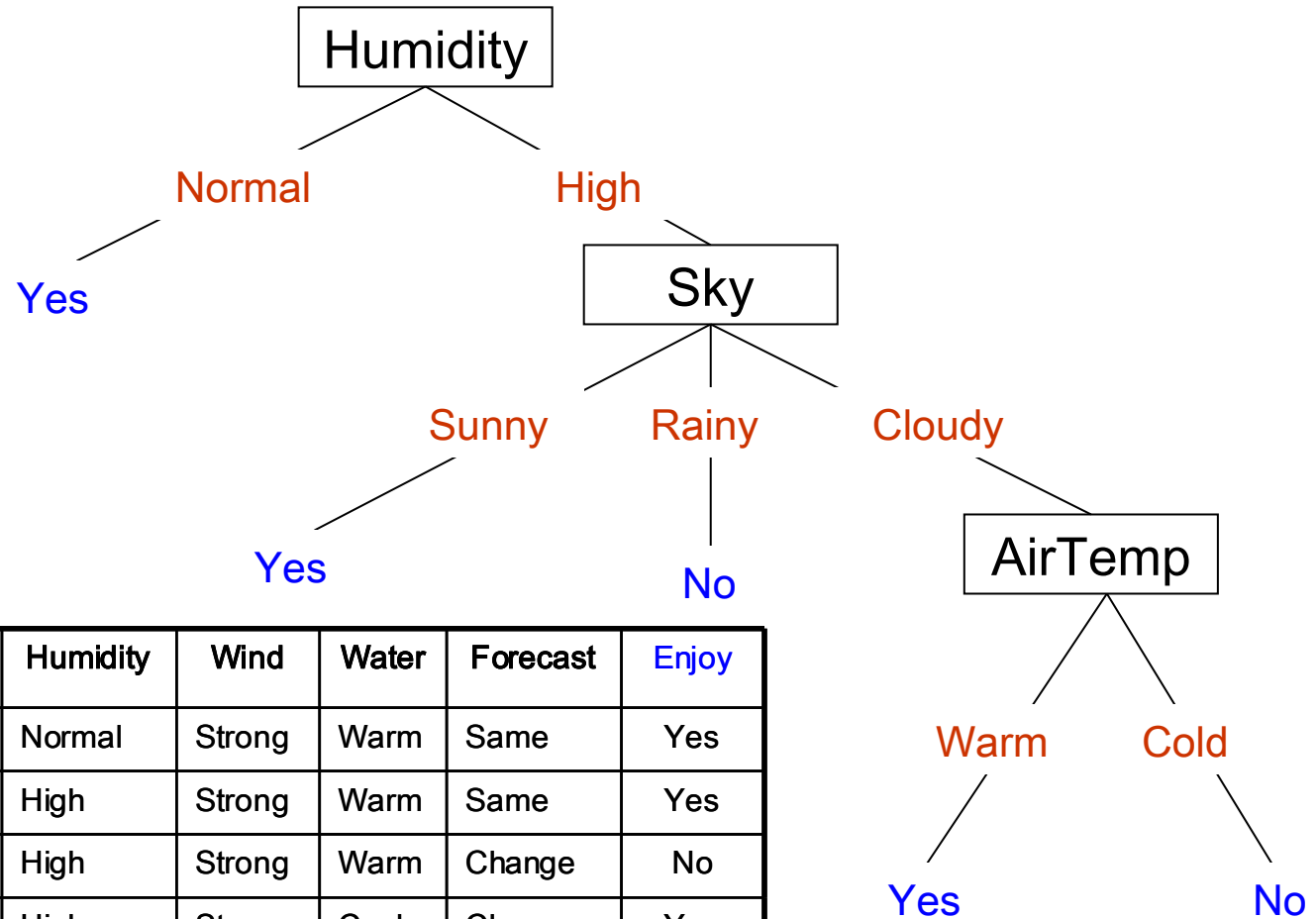
$(\text{Sky} = \text{Sunny}) \vee (\text{Sky} = \text{Cloudy} \wedge \text{AirTemp} = \text{Warm})$

Decision Trees



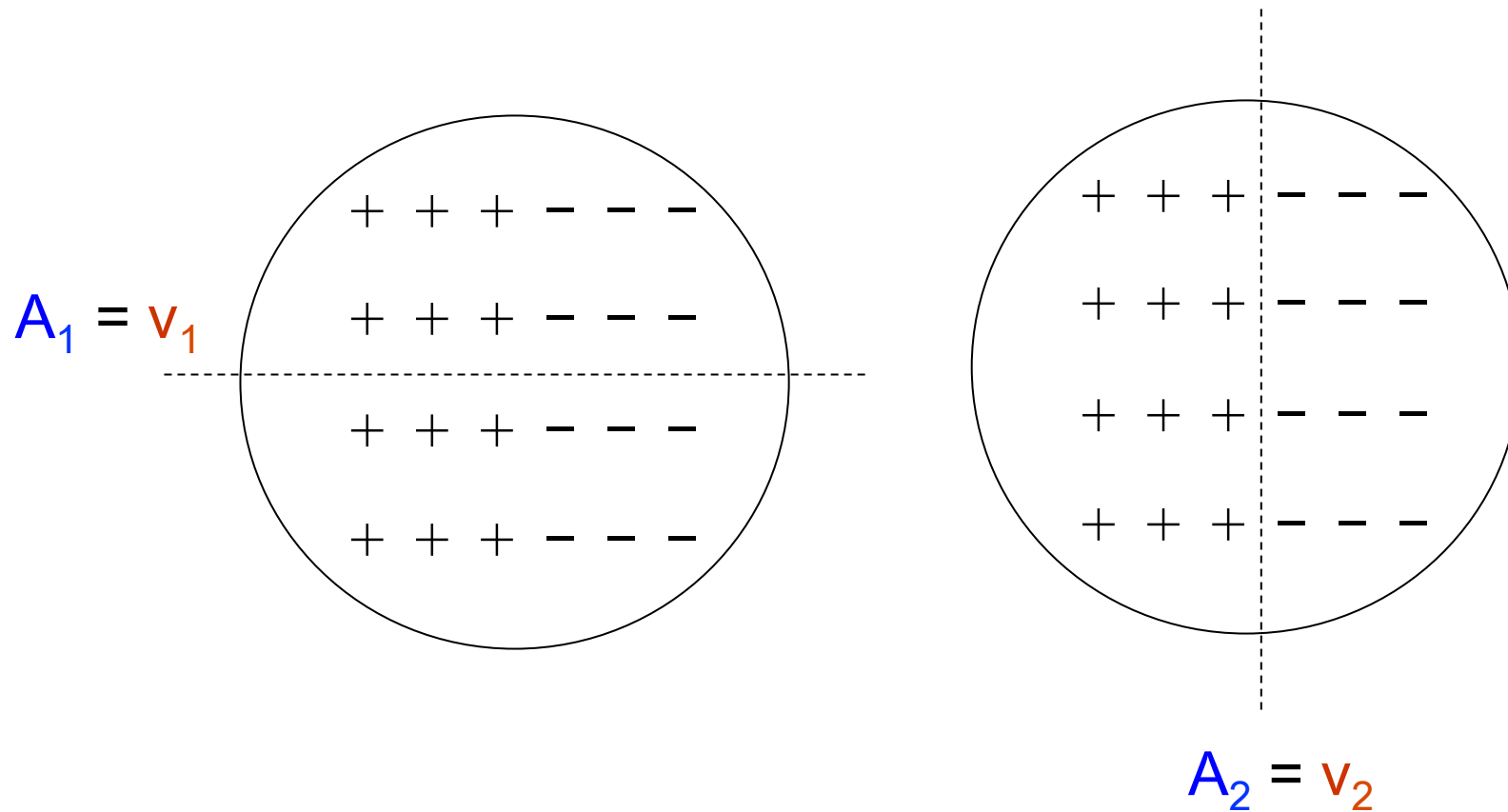
7	Rainy	Warm	Normal	Weak	Cool	Same	?
8	Cloudy	Warm	High	Strong	Cool	Change	?

Decision Trees



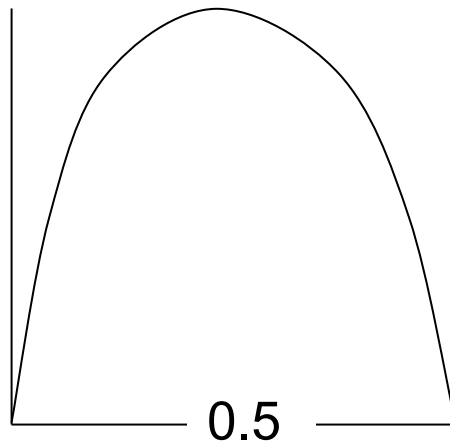
No.	Sky	AirTemp	Humidity	Wind	Water	Forecast	Enjoy
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes
5	Cloudy	Warm	High	Weak	Cool	Same	Yes
6	Cloudy	Cold	High	Weak	Cool	Same	No

Decision Trees



Homogeneity of Examples

- Entropy(S) = $-p_+ \log_2 p_+ - p_- \log_2 p_-$

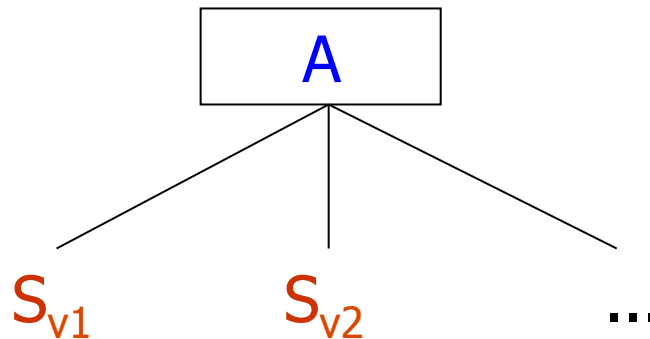


Homogeneity of Examples

- Entropy(S) = $\sum_{i=1,c} -p_i \log_2 p_i$ impurity measure

Information Gain

- $\text{Gain}(S, A) = \text{Entropy}(S) - \sum_{v \in \text{Values}(A)} (|S_v|/|S|) \cdot \text{Entropy}(S_v)$



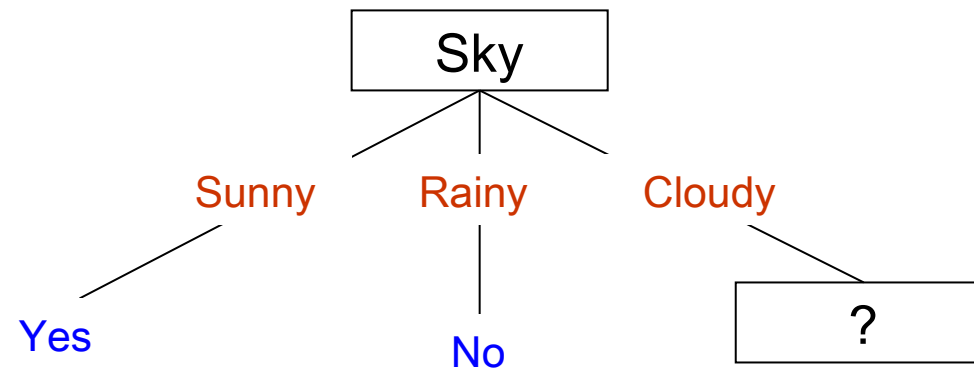
Example

- $\text{Entropy}(S) = -p_+ \log_2 p_+ - p_- \log_2 p_- = - (4/6) \log_2 (4/6) - (2/6) \log_2 (2/6)$
 $= 0.389 + 0.528 = 0.917$
- $\text{Gain}(S, \text{Sky})$
 $= \text{Entropy}(S) - \sum_{v \in \{\text{Sunny, Rainy, Cloudy}\}} (|S_v|/|S|) \text{Entropy}(S_v)$
 $= \text{Entropy}(S) - [(3/6) \cdot \text{Entropy}(S_{\text{Sunny}}) + (1/6) \cdot \text{Entropy}(S_{\text{Rainy}}) +$
 $\quad (2/6) \cdot \text{Entropy}(S_{\text{Cloudy}})]$
 $= \text{Entropy}(S) - (2/6) \cdot \text{Entropy}(S_{\text{Cloudy}})$
 $= \text{Entropy}(S) - (2/6) [- (1/2) \log_2 (1/2) - (1/2) \log_2 (1/2)]$
 $= 0.917 - 0.333 = 0.584$

Example

- $\text{Entropy}(S) = -p_+ \log_2 p_+ - p_- \log_2 p_- = - (4/6) \log_2 (4/6) - (2/6) \log_2 (2/6)$
 $= 0.389 + 0.528 = 0.917$
- $\text{Gain}(S, \text{Water})$
 $= \text{Entropy}(S) - \sum_{v \in \{\text{Warm}, \text{Cool}\}} (|S_v|/|S|) \text{Entropy}(S_v)$
 $= \text{Entropy}(S) - [(3/6) \cdot \text{Entropy}(S_{\text{Warm}}) + (3/6) \cdot \text{Entropy}(S_{\text{Cool}})]$
 $= \text{Entropy}(S) - (3/6) \cdot 2 \cdot [-(2/3) \log_2 (2/3) - (1/3) \log_2 (1/3)]$
 $= \text{Entropy}(S) - 0.389 - 0.528$
 $= 0$

Example



- $\text{Gain}(S_{\text{Cloudy}}, \text{AirTemp})$
 $= \text{Entropy}(S_{\text{Cloudy}}) - \sum_{v \in \{\text{Warm, Cold}\}} (|S_v|/|S|) \text{Entropy}(S_v)$
 $= 1$
- $\text{Gain}(S_{\text{Cloudy}}, \text{Humidity})$
 $= \text{Entropy}(S_{\text{Cloudy}}) - \sum_{v \in \{\text{Normal, High}\}} (|S_v|/|S|) \text{Entropy}(S_v)$
 $= 0$

Inductive Bias

- Hypothesis space: complete!

Inductive Bias

- Hypothesis space: complete!
- Shorter trees are preferred over larger trees
- Prefer the simplest hypothesis that fits the data

Inductive Bias

- Decision Tree algorithm: searches **incompletely** thru a **complete** hypothesis space.

⇒ **Preference** bias

- Candidate-Elimination searches **completely** thru an **incomplete** hypothesis space.

⇒ **Restriction** bias