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5.1 5.2 5.3 5.4 5.5	metry 8 Convex Hull 8 Geometry Template 8 Half Plane Intersection 9 Segments Intersection 10 Rectangles Union 10	3 1 2 3 4 5 6	<pre>void init() { catalan[0] = catalan[1] = 1; for (int i=2; i<=n; i++) { catalan[i] = 0; for (int j=0; j < i; j++) { catalan[i] += (catalan[j] * catalan[i-j-1]) % MOD;</pre>
Gra 6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8	phs 11 2 SAD 11 Ariculation Point 12 Bridges Tree and Diameter 12 Dinic With Scalling 12 Gomory Hu 13 HopcraftKarp BPM 13 Hungarian 13 Kosaraju 14	8 9 10 11 12 12 13 13 14	<pre>if (catalan[i] >= MOD) {</pre>
6.9 6.10 6.11 6.12 6.13 6.14 6.15 6.16 6.17	Manhattan MST 14 Maximum Clique 14 MCMF 15 Minimum Arbroscene in a Graph 15 Minmimum Vertex Cover (Bipartite) 16 Prufer Code 16 Push Relabel Max Flow 17 Tarjan Algo 17	1 15 1 16 5 17 6 18 6 18	<pre>are not numbered). // 3- The number of ways to completely parenthesize n+1 factors. // 4- The number of triangulations of a convex polygon with n+2 sides // 5- The number of ways to connect the 2n points on a circle to form n disjoint chords. // 6- The number of non-isomorphic full binary trees with n internal nodes (i.e. nodes having at least one son). // 7- The number of monotonic lattice paths from point (0,0) to point (n,n) in a square lattice of size nxn, which do not pass above the main diagonal (i.e. connecting (0,0) to (n,n)).</pre>

2 Algebra

2.1 Gray Code

```
int g (int n) {
    return n ^ (n >> 1);
    int rev_g (int g) {
       int n = 0;
       for (; g; g >>= 1)
        n = q;
       return n;
10
    int calc(int x, int y) { ///2D Gray Code
11
         int a = g(x), b = g(y);
12
         int res = 0;
\frac{13}{14}
         f(i, 0, LG) {
              int k1 = (a \& (1 << i));
\overline{15}
              int k2 = b & (1 << i);
16
              res |= k1 << (i + 1);
17
              res |= k2 \ll i;
18
19
         return res;
20
```

2.2 Primitive Roots

```
int primitive root (int p) {
        vector<int> fact;
        int phi = p - 1, n = phi;
        for (int i = 2; i * i <= n; ++i)
4
             if (n % i == 0) {
5
                 fact.push_back (i);
                 while (n \% i == 0)
                     n /= i:
        if (n > 1)
11
             fact.push_back (n);
        for (int res = 2; res <= p; ++res) {</pre>
             bool ok = true;
             for (size_t i = 0; i < fact.size() && ok; ++i)</pre>
                 ok &= powmod (res, phi / fact[i], p) != 1;
^{17}_{18}
             if (ok) return res;
19
        return -1;
20
```

2.3 Discrete Logarithm minimum x for which $a^x = b\%m$

```
// Returns minimum x for which a ^ x % m = b % m, a and m are coprime.
    int solve(int a, int b, int m) {
         a %= m, b %= m;
         int n = sqrt(m) + 1;
5
         int an = 1;
         for (int i = 0; i < n; ++i)
              an = (an * 111 * a) % m;
         unordered_map<int, int> vals;
         for (int q = 0, cur = b; q \le n; ++q) {
              vals[cur] = q;
11
              cur = (cur * 111 * a) % m;
12
13
14
15
         for (int p = 1, cur = 1; p <= n; ++p) {
    cur = (cur * 111 * an) % m;</pre>
              if (vals.count(cur)) {
16
17
18
19
                  int ans = n * p - vals[cur];
                  return ans;
\frac{20}{21}
         return -1;
    //When a and m are not coprime
```

```
// Returns minimum x for which a ^ x % m = b % m.
24
    int solve(int a, int b, int m) {
        a %= m, b %= m;
int k = 1, add = 0, g;
        while ((g = gcd(a, m)) > 1) {
             if (b == k)
                 return add;
             if (b % q)
31
                 return -1;
             b \neq g, m \neq g, ++add;
             k = (k * 111 * a / g) % m;
33
35
        int n = sqrt(m) + 1;
        int an = \hat{1}:
37
         for (int i = 0; i < n; ++i)
             an = (an * 111 * a) % m;
39
         unordered_map<int, int> vals;
40
         for (int q = 0, cur = b; q \le n; ++q) {
             vals[cur] = q;
41
\overline{42}
             cur = (cur * 111 * a) % m;
43
44
         for (int p = 1, cur = k; p \le n; ++p) {
             cur = (cur * 111 * an) % m;
45
46
             if (vals.count(cur)) {
47
                 int ans = n * p - vals[cur] + add;
48
                 return ans;
49
50
51
         return -1;
52
```

2.4 Discrete Root finds all numbers x such that $x^k = a\%n$

```
This program finds all numbers x such that x^k = a \pmod{n}
    vector<int> discrete_root(int n, int k, int a) {
        if (a == 0)
            return {0};
        int g = primitive_root(n);
        // Baby-step giant-step discrete logarithm algorithm
 8
        int sq = (int) sqrt(n + .0) + 1;
 9
        vector<pair<int, int>> dec(sq);
10
        for (int i = 1; i \le sq; ++i)
11
            dec[i-1] = \{powmod(q, i * sq * k % (n-1), n), i\};
12
        sort(dec.begin(), dec.end());
13
        int any_ans = -1;
14
        for (int i = 0; i < sq; ++i) {
15
            int my = powmod(g, i * k % (n - 1), n) * a % n;
16
            auto it = lower_bound(dec.begin(), dec.end(), make_pair(my, 0)
            if (it != dec.end() && it->first == my) {
18
                 any_ans = it->second * sq - i;
19
                 break;
20
\bar{2}\check{1}
22
        if (any_ans == -1) return {};
\frac{23}{24}
        int delta = (n - 1) / __gcd(k, n - 1);
25
        vector<int> ans;
        for (int cur = any_ans % delta; cur < n - 1; cur += delta)</pre>
            ans.push_back(powmod(q, cur, n));
        sort(ans.begin(), ans.end());
        return ans;
30
```

2.5 Factorial modulo in p*log(n) (Wilson Theroem)

```
int factmod(int n, int p) {
        vector<int> f(p);
        f[0] = 1;
        for (int i = 1; i < p; i++)
5
            f[i] = f[i-1] * i % p;
        int res = 1;
        while (n > 1)
            if ((n/p) % 2)
10
                res = p - res;
            res = res * f[n%p] % p;
11
12
            n /= p;
13
14
        return res;
15
```

2.6 Iteration over submasks

2.7 Totient function

2.8 CRT and EEGCD

```
ll extended(ll a, ll b, ll &x, ll &y) {
          if(b == 0) {
 3
               x = 1;
               y = 0;
 5
               return a;
          11 x0, y0;
          11 q = extended(b, a % b, x0, y0);
          x = y0;
          y = x0 - a / b * y0;
          return q ;
13
     ll de(ll a, ll b, ll c, ll &x, ll &y) {
15
          11 g = extended(abs(a), abs(b), x, y);
16
          if (c % g) return -1;
          x \star = c / g;
17
          y *= c / g;
18
          if(a < 0)\bar{x} = -x;
19
20
          if(b < 0)y = -y;
21
          return g;
     pair<11, 11> CRT(vector<11> r, vector<11> m) {
\begin{array}{c} 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 31 \\ 32 \\ 33 \\ 34 \\ 35 \end{array}
          11 r1 = r[0], m1 = m[0];
          for(int i = 1; i < r.size(); i++) {</pre>
               11 r2 = r[i], m2 = m[i];
               11 x0, y0;
               11 g = de(m1, -m2, r2 - r1, x0, y0);
               if(g == -1) return \{-1, -1\};
               x0 \% = m2;
               11 \text{ nr} = x0 * m1 + r1;
               11 \text{ nm} = \text{m1} / \text{g} * \text{m2};
               r1 = (nr % nm + nm) % nm;
               m1 = nm;
\frac{36}{37}
          return {r1, m1};
```

2.9 FFT

```
typedef complex<double> C;
    typedef vector<double> vd;
    typedef vector<int> vi;
    typedef pair<int, int> pii;
    void fft(vector<C>& a)
         int n = sz(a), L = 31 - \underline{builtin_clz(n)};
         static vector<complex<long double>> R(2, 1);
        static vector<C> rt(2, 1); // (^10% fas te r i f double) for (static int k = 2; k < n; k *= 2) {
             R.resize(n);
             rt.resize(n):
             auto x = polar(1.0L, acos(-1.0L) / k);
13
             rep(i, k, 2 * k) rt[i] = R[i] = i & 1 ? R[i / 2] * x : R[i /
15
        vi rev(n);
16
         rep(i, 0, n) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
17
         rep(i, 0, n) if (i < rev[i]) swap(a[i], a[rev[i]]);
18
         for (int k = 1; k < n; k *= 2)
```

```
for (int i = 0; i < n; i += 2 * k) rep(j, 0, k) {
20
                 Cz = rt[j + k] * a[i + j + k]; //
21
                 a[i + j + k] = a[i + j] - z;
22
                 a[i + j] += z;
23
\overline{24}
\overline{25}
    vd conv(const vd& a, const vd& b) {
26
        if (a.empty() || b.empty()) return {};
27
        vd res(sz(a) + sz(b) - 1);
         int L = 32 - __builtin_clz(sz(res)), n = 1 << L;</pre>
\tilde{2}\tilde{9}
         vector<C> in(n), out(n);
         copy(all(a), begin(in));
31
         rep(i, 0, sz(b)) in[i].imag(b[i]);
32
         fft(in);
33
         for (C\& x : in) x *= x;
34
         rep(i, 0, n) out[i] = in[-i & (n - 1)] - conj(in[i]);
35
         fft (out);
36
         /// \text{rep}(i, 0, sz(\text{res})) \text{ res}[i] = (MOD+(ll) \text{round}(imag(out[i])) / (4 * n)
             ))) % MOD; ///in case of mod
         rep(i, 0, sz(res)) res[i] = imag(out[i]) / (4 * n);
38
         return res;
39
    int main() {
42
        //Applications
43
         //1-All possible sums
44
45
         //2-All possible scalar products
46
         // We are given two arrays a[] and b[] of length n.
47
         //We have to compute the products of a with every cyclic shift of
48
         //We generate two new arrays of size 2n: We reverse a and append n
              zeros to it.
49
         //And we just append b to itself. When we multiply these two
             arrays as polynomials,
50
         //and look at the coefficients c[n-1], c[n], ..., c[2n-2] of the
             product c, we get:
51
         //c[k]=sum\ i+j=k\ a[i]b[j]
\frac{52}{53}
         //3-Two stripes
54
         //We are given two Boolean stripes (cyclic arrays of values 0 and
             1) a and b.
55
         //We want to find all ways to attach the first stripe to the
             second one,
56
         //such that at no position we have a 1 of the first stripe next to
              a 1 of the second stripe.
57 }
```

2.10 Fibonacci

```
2.11 Gauss Determinant
   double det(vector<vector<double>>& a) {
        int n = sz(a); double res = 1;
 3
        rep(i,0,n) {
            int b = i;
 5
            rep(j,i+1,n) if (fabs(a[j][i]) > fabs(a[b][i])) b = j;
            if (i != b) swap(a[i], a[b]), res *= -1;
            res *= a[i][i];
            if (res == 0) return 0;
9
            rep(j,i+1,n) {
10
                double v = a[j][i] / a[i][i];
11
                if (v != 0) \operatorname{rep}(k, i+1, n) a[j][k] -= v * a[i][k];
13
14
        return res;
15
17
   const 11 mod = 12345;
   11 det(vector<vector<ll>>& a) {
        int n = sz(a); ll ans = 1;
        rep(i,0,n) {
21
            rep(j,i+1,n) {
                while (a[j][i] != 0) { // gcd step
                    ll t = a[i][i] / a[j][i];
24
                    if (t) rep(k,i,n)
                    a[i][k] = (a[i][k] - a[j][k] * t) % mod;
```

2.12 GAUSS SLAE

```
const double EPS = 1e-9;
     const int INF = 2; // it doesn't actually have to be infinity or a big
     int gauss (vector < vector <double> > a, vector <double> & ans) {
          int n = (int) a.size();
          int m = (int) a[0].size() - 1;
           vector<int> where (m, -1);
           for (int col = 0, row = 0; col < m && row < n; ++col) {</pre>
10
                int sel = row;
                for (int i = row; i < n; ++i)
   if (abs (a[i][col]) > abs (a[sel][col]))
                          sel = i;
14
                if (abs (a[sel][col]) < EPS)</pre>
                     continue;
16
                for (int i = col; i \le m; ++i)
                     swap (a[sel][i], a[row][i]);
18
19
20
21
22
23
24
25
26
27
28
29
30
31
                where[col] = row;
                for (int i = 0; i < n; ++i)
                     if (i != row) {
                          double c = a[i][col] / a[row][col];
for (int j = col; j <= m; ++j)</pre>
                                a[i][j] -= a[row][j] * c;
                ++row;
          ans.assign (m, 0);
           for (int i = 0; i < m; ++i)</pre>
                if (where[i] != -1)
\begin{array}{c} 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 37 \\ 38 \\ 40 \\ 41 \\ \end{array}
                     ans[i] = a[where[i]][m] / a[where[i]][i];
          for (int i = 0; i < n; ++i) {
                double sum = 0;
                for (int j = 0; j < m; ++j)
    sum += ans[j] * a[i][j];</pre>
                if (abs (sum - a[i][m]) > EPS)
                     return 0;
          for (int i = 0; i < m; ++i)
   if (where[i] == -1)</pre>
43
                     return INF:
```

2.13 Matrix Inverse

return 1;

44

45

```
#define ld long double
    vector < vector<ld> > gauss (vector < vector<ld> > a) {
         int n = (int) a.size();
         vector<vector<ld> > ans(n, vector<ld>(n, 0));
         for (int i = 0; i < n; i++)
              ans[i][i] = 1;
9
         for (int i = 0; i < n; i++) {
              for(int j = i + 1; j < n; j++)
    if(a[j][i] > a[i][i]) {
10
11
12
                        a[j].swap(a[i]);
13
                        ans[j].swap(ans[i]);
14
15
              ld val = a[i][i];
16
              for(int j = 0; j < n; j++) {
    a[i][j] /= val;</pre>
17
18
                   ans[i][j] /= val;
19
\frac{20}{21}
\frac{21}{22}
              for (int j = 0; j < n; j++) {
                   if(j == i)continue;
                   val = a[j][i];
23
                   for (int k = 0; k < n; k++) {
```

2.14 NTT of KACTL

```
const 11 mod = (119 << 23) + 1, root = 62; // = 998244353 // For p < 2^30 there is a lso e . g . 5 << 25, 7 << 26, 479 << 21
    // and 483 << 21 (same root) . The \hat{1} as t two are > 10^{\circ}9.
    typedef vector<ll> v1;
    void ntt(vl &a) {
        int n = sz(a), L = 31 - __builtin_clz(n);
        static vl rt(2, 1);
        for (static int k = 2, s = 2; k < n; k *= 2, s++) {
             rt.resize(n);
             11 z[] = \{1, modpow(root, mod >> s)\};
11
             rep(i,k,2*k) rt[i] = rt[i / 2] * z[i & 1] % mod;
12
13
        vi rev(n);
14
        rep(i,0,n) \ rev[i] = (rev[i / 2] | (i \& 1) << L) / 2;
15
        rep(i,0,n) if (i < rev[i]) swap(a[i], a[rev[i]]);
16
         for (int k = 1; k < n; k *= 2)
             for (int i = 0; i < n; i += 2 * k) rep(j,0,k)
17
             11 z = rt[j + k] * a[i + j + k] % mod, &ai = a[i + j];
18
             a[i + j + \bar{k}] = ai - z + (z > ai ? mod : 0);
19
20
             ai += (ai + z >= mod ? z - mod : z);
\tilde{2}
22
23
   vl conv(const vl &a, const vl &b) {
24
        if (a.empty() || b.empty()) return {};
25
        int s = sz(a) + sz(b) - 1, B = 32 - _builtin_clz(s), n = 1 << B;
26
        int inv = modpow(n, mod - 2);
        vl L(a), R(b), out(n);
        L.resize(n), R.resize(n);
29
        ntt(L), ntt(R);
        rep(i,0,n) out[-i \& (n-1)] = (l1)L[i] * R[i] % mod * inv % mod;
31
        ntt(out);
        return {out.begin(), out.begin() + s};
33
```

3 Data Structures

3.1 2D BIT

```
1  void upd(int x, int y, int val) {
2    for(int i = x; i <= n; i += i & -i)
3    for(int j = y; j <= m; j += j & -j)
4    bit[i][j] += val;
5  }
6  int get(int x, int y) {
7    int ans = 0;
8    for(int i = x; i; i -= i & -i)
9    for(int j = y; j; j -= j & -j)
10    ans += bit[i][j];
11 }</pre>
```

3.2 2D Sparse table

```
1
        note this isn't the best cache-wise version
        query O(1), Build O(NMlgNlgM)
 4
        be careful when using it and note the he build a dimension above
        i.e he builds a sparse table for each row
        the build sparse table over each row's sparse table
    const int N = 505, LG = 10;
    int st[N][N][LG][LG];
   int a[N][N], lq2[N];
\bar{1}\bar{3}
   int yo(int x1, int y1, int x2, int y2) {
14
     x2++;
15
      v^{2++};
16
      int a = \lg 2[x2 - x1], b = \lg 2[y2 - y1];
```

 $^{\circ}$

```
17
      return max (
18
              \max(st[x1][y1][a][b], st[x2 - (1 << a)][y1][a][b]),
19
              \max(st[x1][y2 - (1 << b)][a][b], st[x2 - (1 << a)][y2 - (1 <<
                    b) ] [a] [b] )
            );
21
22
23
24
25
26
27
28
29
30
31
32
33
34
    void build(int n, int m) { // 0 indexed
      for (int i = 2; i < N; i++) lq2[i] = lq2[i >> 1] + 1;
      for (int i = 0; i < n; i++) {</pre>
         for (int j = 0; j < m; j++) {</pre>
           st[i][j][0][0] = a[i][j];
      for (int a = 0; a < LG; a++) {
  for (int b = 0; b < LG; b++) {</pre>
           if (a + b == 0) continue;
           for (int i = 0; i + (1 << a) <= n; i++) {
             for (int j = 0; j + (1 << b) <= m; <math>j++) {
35
               if (!a)
36
                  st[i][j][a][b] = max(st[i][j][a][b-1], st[i][j+(1 << (
                       b - 1))][a][b - 1]);
               } else {
                  st[i][j][a][b] = max(st[i][j][a - 1][b], st[i + (1 << (a -
38
                        1))][j][a - 1][b]);
41
 3.3
       Mo's
    #include <bits/stdc++.h>
    int n, qq, arr[N], sz = 1000; // sz is the size of the bucket
    int co[N], ans = 0, ansq[N];
    int cul = 1, cur = 1;
    void add(int x) {
         co[arr[x]]++;
```

$4\overline{2}$ 43 44 **if** (co[arr[x]] == 1) 10 ans++; 11 else if (co[arr[x]] == 2)12 13 14 15 ans--; void remove(int x) { 16 co[arr[x]]--; 17 18 **if** (co[arr[x]] == 1) 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 else if (co[arr[x]] == 0)ans--; void solve(int 1, int r, int ind) { r+=1; while (cul < 1) remove(cul++);</pre> while (cul > 1) add(--cul); while (cur < r) add(cur++);</pre> while (cur > r) remove(--cur); ansq[ind] = ans; int main() { FIO cin >> qq; { 1 , ind} $\{1/sz,r\},$ priority_queue<pair<int, int>, pair<int, int>>, vector<pair<</pre> pair<int, int>, pair<int, int>>>, greater<pair<int, int>, pair<int, int>>>> q; for (int i = 0; i < qq; i++) { int 1, r; 39 40 cin >> 1 >> r; 41 q.push($\{\{1 / sz, r\}, \{1, i\}\}\}$); 42 43 while (q.size()) { 44 int ind=q.top().second.second, l=q.top().second.first, r=q.top() .first.second; 45 solve(l, r,ind); 46 q.pop(); 47

3.4 Mo With Updates

```
///O(N^5/3) note that the block size is not a standard size
     #pragma GCC optimize ("03")
     #pragma GCC target ("sse4")
     #include <bits/stdc++.h>
    using namespace std;
    using 11 = long long;
    const int N = 1e5 +5;
    const int M = 2 * N;
    const int blk = 2155;
     const int mod = 1e9 + 7;
17
    struct Query{
18
       int 1, r, t, idx;
19
       Query(int a = 0, int b = 0, int c = 0, int d = 0) {l=a, r=b, t=c, idx = d;}
20
       bool operator < (Query o) {</pre>
21
         if(r'/blk == o.r /blk && 1 / blk == o.1 / blk)return t < o.t;
if(r / blk == o.r / blk)return 1 < o.1;</pre>
22
\overline{23}
          return r < o.r;</pre>
\overline{24}
\overline{25}
    } Q[N];
\frac{26}{27} \\ 28
    int a[N], b[N];
    int cnt1[M], cnt2[N];
int L = 0, R = -1, K = -1;
    void add(int x) { ///add item to range
    // cout << x << '\n';
       cnt2[cnt1[x]]--;
cnt1[x]++;
3\overline{3}
34
       cnt2[cnt1[x]]++;
35
    void del(int x){ ///delete item from range
37
       cnt2[cnt1[x]]--;
       cnt1[x]--;
39
       cnt2[cnt1[x]]++;
40
41
   map<int,int>id;
42 int cnt:
43
    int ans[N];
44
    int p[N], nxt[N];
45
    int prv[N];
46
    void upd(int idx) { //update item value
       if(p[idx] >= L && p[idx] <= R)
48
         del(a[p[idx]]), add(nxt[idx]);
49
       a[p[idx]] = nxt[idx];
50
51
    void err(int idx) {
       if(p[idx] >= L && p[idx] <= R)
53
          del(a[p[idx]]), add(prv[idx]);
54
       a[p[idx]] = prv[idx];
55
56
    int main(){
57
58
       int n, q, 1, r, tp;
59
60
       scanf("%d%d", &n, &q);
       for(int i = 0; i < n; i++) {
  scanf("%d", a + i);
}</pre>
63
64
         if(id.count(a[i]) == 0)
65
          id[a[i]] = cnt++;
a[i] = id[a[i]];
66
67
         b[i] = a[i];
68
       int qIdx = 0;
       int ord = 0;
71
       while (q--) {
72
73
          scanf("%d", &tp);
74
         if(tp == 1){
```

```
/// ADD Query
75
76
77
78
80
81
82
83
84
85
86
87
889
90
              scanf("%d%d", &1, &r); --1, --r;
              Q[qIdx] = Query(1, r, ord-1, qIdx); qIdx++;
            } else{
              /// ADD Update
              scanf("%d%d",p + ord, nxt + ord); --p[ord];
              if(id.count(nxt[ord]) == 0)
                id[nxt[ord]] = cnt++;
              nxt[ord] = id[nxt[ord]];
              prv[ord] = b[p[ord]];
              b[p[ord]] = nxt[ord];
              ++ord;
         sort(Q,Q+qIdx);
 91
         for (int i = 0; i < qIdx; i++) {</pre>
           while (L < Q[i].l) \stackrel{del}{del} (a[L++]);
 93
           while (L > Q[i].l) add (a[--L]);
           while (R < Q[i].r) add (a[++R]);
while (R > Q[i].r) del (a[R--]);
while (K < Q[i].t) upd (++K);</pre>
 94
95
 96
 97
           while (K > Q[i].t) err(K--);
 98
           ///Solve Query I
 99
100
        for(int i = 0; i < qIdx; i++)</pre>
           printf("%d\n", ans[i]);
101
102 \\ 103 \\ 104
        return 0;
105
```

3.5 Ordered Set

3.6 Persistent Seg Tree

```
int val[ N \star 60 ], L[ N \star 60 ], R[ N \star 60 ], ptr, tree[N]; /// N \star 1qN
     int upd(int root, int s, int e, int idx) {
         int ret = ++ptr;
         val[ret] = L[ret] = R[ret] = 0;
         if (s == e) {
              val[ret] = val[root] + 1;
              return ret;
         int md = (s + e) >> 1;
         if (idx <= md) {
              L[ret] = upd(L[root], s, md, idx), R[ret] = R[root];
         } else {
14
              R[ret] = upd(R[root], md + 1, e, idx), L[ret] = L[root];
16
         val[ret] = max(val[L[ret]], val[R[ret]]);
17
         return ret;
18
19
   int gry(int node, int s, int e, int 1, int r){
20
      if(r < s || e < 1 || !node)return 0; //Punishment Value</pre>
\begin{array}{c} 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \end{array}
       if(1 <= s && e <= r){
         return val[node];
       int md = (s+e) >> 1;
       return max(qry(L[node], s, md, l, r), qry(R[node], md+1,e,l,r));
     int merge(int x, int y, int s, int e) {
28
         if(!x||!y)return x | y;
\begin{array}{c} 29 \\ 30 \\ 31 \\ 32 \\ 33 \end{array}
         if(s == e) {
              val[x] += val[y];
              return x;
         int md = (s + e) >> 1;
         L[x] = merge(L[x], L[y], s, md);
```

3.7 Treap

```
mt19937_64 mrand(chrono::steady_clock::now().time_since_epoch().count
    struct Node
        int key, pri = mrand(), sz = 1;
 5
        int lz = 0:
        int idx;
        array<Node*, 2> c = {NULL, NULL};
        Node (int key, int idx) : key(key), idx(idx) {}
 8
 9
10
    int getsz(Node* t) {
        return t ? t->sz : 0;
11
12
13
    Node* calc(Node* t) {
        t - sz = 1 + getsz(t - sc[0]) + getsz(t - sc[1]);
14
        return t;
15
16
17
    void prop(Node* cur) +
        if(!cur || !cur->lz)
19
             return;
20
        cur->key += cur->lz;
21
        if(cur->c[0])
             cur->c[0]->lz += cur->lz;
23
        if(cur->c[1])
    cur->c[1]->lz += cur->lz;
\overline{24}
25
        cur -> 1z = 0;
\overline{26}
    array<Node*, 2> split(Node* t, int k) {
        prop(t);
        if(!t)
\tilde{3}\tilde{0}
        return {t, t};
if(getsz(t->c[0]) >= k) { ///answer is in left node
31
             auto ret = split(t->c[0], k);
             t - c[0] = ret[1];
             return {ret[0], calc(t)};
35
         } else { ///k > t -> c[0]
36
             auto ret = split(t->c[1], k - 1 - getsz(t->c[0]));
             t \to c[1] = ret[0];
37
38
             return {calc(t), ret[1]};
39
    Node* merge(Node* u, Node* v) {
        prop(u);
        prop(v);
44
        if(!u || !v)
45
             return u ? u : v;
46
        if(u->pri>v->pri) {
47
             u \to c[1] = merge(u \to c[1], v);
             return calc(u);
49
50
             v - c[0] = merge(u, v - c[0]);
51
             return calc(v);
    int cnt(Node* cur, int x) {
55
        prop(cur);
\frac{56}{57}
        if(!cur)
             return 0;
        if(cur->key <= x)</pre>
59
             return getsz(cur->c[0]) + 1 + cnt(cur->c[1], x);
60
        return cnt(cur->c[0], x);
61
62
    Node* ins(Node* root, int val, int idx, int pos) {
        auto splitted = split(root, pos);
        root = merge(splitted[0], new Node(val, idx));
64
65
        return merge(root, splitted[1]);
```

3.8 Wavelet Tree

```
// remember your array and values must be 1-based
struct wavelet_tree {
   int lo, hi;
   wavelet_tree *1, *r;
```

```
vector<int> b;
         //nos are in range [x,y]
         //array indices are [from, to)
         wavelet_tree(int *from, int *to, int x, int y) {
              lo = x, hi = y;
              if (lo == hi or from >= to)
                   return;
13
              int mid = (lo + hi) / 2;
              auto f = [mid] (int x) {
\frac{15}{16}
                   return x <= mid;</pre>
\frac{17}{18}
              b.reserve(to - from + 1);
              b.pb(0);
\begin{array}{c} 19 \\ 20 \\ 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 30 \\ 31 \\ 32 \\ 33 \\ 34 \end{array}
              for (auto it = from; it != to; it++)
                  b.pb(b.back() + f(*it));
               //see how lambda function is used here
              auto pivot = stable_partition(from, to, f);
              l = new wavelet_tree(from, pivot, lo, mid);
              r = new wavelet_tree(pivot, to, mid + 1, hi);
          //kth smallest element in [l, r]
         int kth(int 1, int r, int k) {
              if (1 > r)
                   return 0;
              if (lo == hi)
                   return lo;
              int inLeft = b[r] - b[1 - 1];
              int lb = b[1 - 1]; //amt of nos in first (1-1) nos that go in
              int rb = b[r]; //amt of nos in first (r) nos that go in left
36
37
38
39
              if (k <= inLeft)</pre>
                   return this->l->kth(lb + 1, rb, k);
              return this->r->kth(l - lb, r - rb, k - inLeft);
\frac{40}{41}
         //count of nos in [l, r] Less than or equal to k
         int LTE(int 1, int r, int k) {
42
\overline{43}
              if (1 > r \text{ or } k < 10)
44
                   return 0:
\frac{45}{46}
              if (hi <= k)
              return r - 1 + 1;
int lb = b[1 - 1], rb = b[r];
47
48
              return this->l->LTE(lb + 1, rb, k) + this->r->LTE(l - lb, r -
49
50
51
52
53
54
55
56
57
58
60
         //count of nos in [l, r] equal to k
         int count(int 1, int r, int k) {
              if (1 > r \text{ or } k < 10 \text{ or } k > hi)
                   return 0;
              if (lo == hi)
                   return r - 1 + 1;
              int lb = b[1 - 1], rb = b[r], mid = (lo + hi) / 2;
                   return this->1->count(lb + 1, rb, k);
              return this->r->count(1 - 1b, r - rb, k);
61
        SparseTable
```

4 DP

4.1 Dynamic Connectivety with SegTree

```
1 #define f(i, a, b) for(int i = a; i < b; i++)</pre>
```

```
#define all(a) a.begin(),a.end()
    #define sz(x) (int)(x).size()
   typedef long long 11;
   const int N = 1e5 + 5;
    struct PT {
        11 x, y;
        PT() {}
10
        PT(11 a, 11 b) : x(a), y(b) {}
11
        PT operator-(const PT &o) { return PT{x - o.x, y - o.y}; }
        bool operator<(const PT &o) const { return make_pair(x, y) <</pre>
            make_pair(o.x, o.y); }
   ll cross(PT x, PT y) {
15
        return x.x * y.y - x.y * y.x;
16
17
18 bool in[300005];
19
   11 qr[300005];
  bool ask[300005];
   vector<PT> t[300005 * 4]; ///segment tree holding points to queries
   void update(int node, int s, int e, int l, int r, PT x) {
        if (r < s || e < 1)return;</pre>
        if (1 <= s && e <= r) { ///add this point to maximize it with</pre>
            queries in this range
            t[node].push_back(x);
            return;
        int md = (s + e) >> 1;
       update(node << 1, s, md, l, r, x);
31
       update(node << 1 | 1, md + 1, e, l, r, x);
   vector<PT> stk;
   inline void addPts(vector<PT> v) {
        stk.clear();
                        ///reset the data structure you are using
        sort(all(v));
        ///build upper envelope
        for (int i = 0; i < v.size(); i++)</pre>
            while (sz(stk) > 1 & cross(v[i] - stk.back(), stk.back() -
                stk[stk.size() - 2]) <= 0)
                stk.pop_back();
41
            stk.push_back(v[i]);
42
   inline ll calc(PT x, ll val) {
45
        return x.x * val + x.y;
47
   il query(ll x) {
        if (stk.empty())
            return LLONG MIN:
        int lo = 0, hi = stk.size() - 1;
        while (lo + 10 < hi) {
            int md = lo + (hi - lo) / 2;
            if (calc(stk[md + 1], x) > calc(stk[md], x))
                1o = md + 1;
                hi = md;
57
        11 ans = LLONG_MIN;
59
        for (int i = lo; i <= hi; i++)</pre>
           ans = max(ans, calc(stk[i], x));
61
        return ans;
62
   void solve(int node, int s, int e) {      ///Solve queries
        addPts(t[node]); //note that there is no need to add/delete
            just build for t[node]
        f(i, s, e + 1) {
67
            if (ask[i]) {
68
                ans[i] = max(ans[i], query(qr[i]));
70
71
        if (s == e)return;
        int md = (s + e) >> 1;
        solve(node << 1, s, md);
74
        solve(node << 1 | 1, md + 1, e);
   void doWork() {
       int n;
        cin >> n;
```

```
stk.reserve(n);
80
          f(i, 1, n + 1) {
81
              int tp;
82
              cin >> tp;
83
              if (tp == 1) { ///Add Query
84
                  int x, y;
85
                  cin >> \bar{x} >> y;
86
87
88
                  val[i] = PT(x, y);
                   in[i] = 1;
              } else if (tp == 2) { ///Delete Query
89
                   int x;
 90
91
                   if (in[x])update(1, 1, n, x, i - 1, val[x]);
92
93
94
95
96
97
                   in[x] = 0;
               } else {
                   cin >> qr[i];
                  ask[i] = true;
98
          f(i, 1, n + 1) ///Finalize Query
99
              if (in[i])
100
                   update(1, 1, n, i, n, val[i]);
\frac{101}{102}
          f(i, 1, n + 1)ans[i] = LLONG_MIN;
103
          solve(1, 1, n);
104
         f(i, 1, n + 1) if (ask[i]) {
105
                   if (ans[i] == LLONG_MIN)
                       cout << "EMPTY SET\n";
106
\frac{107}{108}
                       cout << ans[i] << '\n';
109
```

4.2 CHT Line Container

```
struct Line
        mutable ll m, b, p;
        bool operator<(const Line &o) const { return m < o.m; }</pre>
        bool operator<(ll x) const { return p < x; }</pre>
 5
    };
    struct LineContainer : multiset<Line, less<>>> {
         // (for doubles, use inf = 1/.0, div(a,b) = a/b)
         static const 11 inf = LLONG_MAX;
        ll div(ll db, ll dm) { // floored division
             return db / dm - ((db ^ dm) < 0 && db % dm);
13
14
        bool isect(iterator x, iterator y) {
15
             if (y == end()) {
16
                 x->p = inf;
17
                 return false;
18
19
20
21
22
23
24
25
26
27
28
29
30
             if (x->m == y->m)
                 x->p = x->b > y->b ? inf : -inf;
             else
                 x->p = div(y->b - x->b, x->m - y->m);
             return x->p >= y->p;
        void add(ll m, ll b) {
             auto z = insert(\{m, b, 0\}), y = z++, x = y;
             while (isect(y, z))
                 z = erase(z);
             if (x != begin() && isect(--x, y))
                 isect(x, y = erase(y));
             while ((y = x) != begin() \&\& (--x)->p >= y->p)
31
32
33
34
35
36
37
38
39
                 isect(x, erase(y));
        11 query(ll x) {
             assert(!empty());
             auto 1 = *lower_bound(x);
             return 1.m * x + 1.b;
```

Geometry

5.1 Convex Hull

```
1 struct point {
```

```
point(l\bar{l} x, ll y) : x(x), y(y) {}
 4
        point operator - (point other) {
 5
             return point(x - other.x, y - other.y);
        bool operator <(const point &other) const {</pre>
             return x != other.x ? x < other.x : y < other.y;
10
11
    11 cross(point a, point b) {
12
        return a.x * b.y - a.y * b.x;
13
14
   11 dot(point a, point b) {
15
        return a.x * b.x + a.y * b.y;
16
17
   struct sortCCW {
18
        point center;
20
        sortCCW(point center) : center(center) {}
        bool operator()(point a, point b) {
             11 res = cross(a - center, b - center);
             if(res)
\overline{25}
                 return res > 0;
26
             return dot(a - center, a - center) < dot(b - center, b -</pre>
                 center);
27
28
29
    vector<point> hull(vector<point> v) {
        sort(v.begin(), v.end());
sort(v.begin() + 1, v.end(), sortCCW(v[0]));
30
32
        v.push_back(v[0]);
33
        vector<point> ans ;
34
        for(auto i : v) {
35
             int sz = ans.size();
             while (sz > 1 \&\& cross(i - ans[sz - 1], ans[sz - 2] - ans[sz -
                 11) <= 0)
                 ans.pop_back(), sz--;
38
             ans.push_back(i);
40
        ans.pop_back();
41
        return ans;
42
```

5.2 Geometry Template

```
using ptype = double edit this first ;
   double EPS = 1e-9;
   struct point {
 4
        ptype x, y;
5
        point(ptype x, ptype y) : x(x), y(y) {}
        point operator - (const point & other) const { return point (x -
            other.x, y - other.y);}
        point operator + (const point & other) const { return point (x +
            other.x, y + other.y);}
        point operator *(ptype c) const { return point(x * c, y * c); }
Q
        point operator /(ptype c) const { return point(x / c, y / c); }
10
        point prep() { return point(-y, x); }
11
   };
  ptype cross(point a, point b) { return a.x * b.y - a.y * b.x;}
   ptype dot(point a, point b) {return a.x * b.x + a.y * b.y;}
14
   double abs(point a) {return sqrt(dot(a, a));}
16
   double angle (point a, point b) { // angle between [0 , pi]
17
        return acos(dot(a, b) / abs(a) / abs(b));
18
19
   // a : point in Line, d : Line direction
   point LineLineIntersect(point a1, point d1, point a2, point d2) {
        return a1 + d1 * cross(a2 - a1, d2) / cross(d1, d2);
\overline{23}
    // Line a---b, point C
24
   point ProjectPointLine(point a, point b, point c) {
25
        return a + (b - a) * 1.0 * dot(c - a, b - a) / dot(b - a, b - a);
26
27
    // segment a---b, point C
   point ProjectPointSegment(point a, point b, point c) {
        double r = dot(c - a, b - a) / dot(b - a, b - a);
        if(r < 0)
30
31
           return a;
        if(r > 1)
32
33
           return b;
```

```
\frac{34}{35}
        return a + (b - a) * r;
36
    // Line a---b, point p
    point reflectAroundLine(point a, point b, point p) {
38
        return ProjectPointLine(a, b, p) * 2 - p;// (proj-p) *2 + p
39
40
   // Around origin
41
    point RotateCCW(point p, double t) {
42
        return point(p.x * cos(t) - p.y * sin(t),
43
                     p.x * sin(t) + p.y * cos(t));
44
45
46
   vector<point> CircleLineIntersect(point a, point b, point center,
        double r) {
47
        a = a - center;
48
        b = b - center;
49
        point p = ProjectPointLine(a, b, point(0, 0)); // project point
            from center to the Line
        if(dot(p, p) > r * r)
            return {};
51
52
53
54
55
56
        double len = sqrt(r * r - dot(p, p));
        if(len < EPS)</pre>
            return {center + p};
        point d = (a - b) / abs(a - b);
57
        return {center + p + d * len, center + p - d * len};
58
59
60
    vector<point> CircleCircleIntersect(point c1, ld r1, point c2, ld r2)
61
        if (r1 < r2) {
62
            swap(r1, r2);
63
            swap(c1, c2);
64
65
        1d d = abs(c2 - c1); // distance between c1, c2
66
        if (d > r1 + r2 || d < r1 - r2 || d < EPS) // zero or infinite
67
            return {};
68
        ld angle = a\cos(min((d * d + r1 * r1 - r2 * r2) / (2 * r1 * d)), (
            ld) 1.0));
        point p = (c2 - c1) / d * r1;
\frac{70}{71}
        if (angle < EPS)</pre>
72
73
74
            return {c1 + p};
        return {c1 + RotateCCW(p, angle), c1 + RotateCCW(p, -angle)};
75
76
77
    point circumcircle(point p1, point p2, point p3) {
78
        return LineLineIntersect((p1 + p2) / 2, (p1 - p2).prep(),
79
                                 (p1 + p3) / 2, (p1 - p3).prep());
80
    //I : number points with integer coordinates lying strictly inside the
         polygon.
    //B : number of points lying on polygon sides by B.
    //Area = I + B/2 - 1
       Half Plane Intersection
```

26

27

30

34

35 36

37

38

41

42

43

44

45

 $\frac{46}{47}$

48

 $\tilde{52}$

53 54

56

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61

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80

81

82 83

84

85

88

89

93

94

95

```
const long double eps = 1e-9, inf = 1e9;

// Basic point/vector struct.
struct Point {

long double x, y;
explicit Point(long double x = 0, long double y = 0) : x(x), y(y)

// Addition, substraction, multiply by constant, cross product.

friend Point operator + (const Point& p, const Point& q) {
    return Point(p.x + q.x, p.y + q.y);
}

friend Point operator - (const Point& p, const Point& q) {
    return Point(p.x - q.x, p.y - q.y);
}

friend Point operator * (const Point& p, const long double& k) {
    return Point(p.x * k, p.y * k);
}
```

23

```
friend long double cross(const Point& p, const Point& q)
        return p.x * q.y - p.y * q.x;
};
// Basic half-plane struct.
struct Halfplane {
    // 'p' is a passing point of the line and 'pq' is the direction
        vector of the line.
    Point p, pq;
    long double angle:
    Halfplane() {}
    Halfplane (const Point & a, const Point & b) : p(a), pq(b - a) {
        angle = atan21(pq.y, pq.x);
    // Check if point 'r' is outside this half-plane.
    // Every half-plane allows the region to the LEFT of its line.
    bool out(const Point& r) {
        return cross(pq, r - p) < -eps;</pre>
    // Comparator for sorting.
    // If the angle of both half-planes is equal, the leftmost one
         should go first.
    bool operator < (const Halfplane& e) const {</pre>
        if (fabsl(angle - e.angle) < eps) return cross(pq, e.p - p) <</pre>
        return angle < e.angle;
    // We use equal comparator for std::unique to easily remove
        parallel half-planes.
    bool operator == (const Halfplane& e) const {
        return fabsl(angle - e.angle) < eps;</pre>
    // Intersection point of the lines of two half-planes. It is
        assumed they're never parallel.
    friend Point inter(const Halfplane& s, const Halfplane& t) {
        long double alpha = cross((t.p - s.p), t.pq) / cross(s.pq, t.
        return s.p + (s.pq * alpha);
};
// Actual algorithm
vector<Point> hp_intersect(vector<Halfplane>& H) {
    Point box[4] = { // Bounding box in CCW order
        Point(inf, inf),
        Point (-inf, inf),
        Point(-inf, -inf),
        Point(inf, -inf)
    };
    for (int i = 0; i < 4; i++) { // Add bounding box half-planes.
        Halfplane aux(box[i], box[(i+1) % 4]);
        H.push_back(aux);
    // Sort and remove duplicates
    sort(H.begin(), H.end());
    H.erase(unique(H.begin(), H.end()), H.end());
    deque<Halfplane> dq;
    int len = \bar{0};
    for(int i = 0; i < int(H.size()); i++) {</pre>
        // Remove from the back of the deque while last half-plane is
        while (len > 1 && H[i].out(inter(dq[len-1], dq[len-2]))) {
             dq.pop_back();
             --len;
        // Remove from the front of the deque while first half-plane
             is redundant
        while (len > 1 && H[i].out(inter(dq[0], dq[1]))) {
```

```
109
         while (len > 2 && dq[0].out(inter(dq[len-1], dq[len-2]))) {
110
              dq.pop_back();
                                                                                     63
111
              --len:
112
                                                                                     64
\frac{113}{114}
         while (len > 2 \&\& dq[len-1].out(inter(dq[0], dq[1]))) {
115
              dq.pop_front();
                                                                                     67
                                                                                              return ++it:
116
              --len;
117
119
                                                                                     71
          // Report empty intersection if necessary
120
         if (len < 3) return vector<Point>();
                                                                                     72
                                                                                              vector<event> e;
          // Reconstruct the convex polygon from the remaining half-planes.
123
         vector<Point> ret(len);
                                                                                     75
124
         for(int i = 0; i+1 < len; i++) {</pre>
125
              ret[i] = inter(dq[i], dq[i+1]);
                                                                                     77
126
127
         ret.back() = inter(dq[len-1], dq[0]);
                                                                                              s.clear();
128
                                                                                     80
         return ret;
129
                                                                                     81
                                                                                     82
                                                                                     83
        Segments Intersection
                                                                                     84
     const double EPS = 1E-9;
                                                                                     85
 \frac{2}{3}
                                                                                     86
     struct pt {
                                                                                     87
         double x, y;
 4
 5
                                                                                     89
     struct seg {
                                                                                     90
                                                                                                  } else {
         pt p, q;
                                                                                     91
         int id;
 10
11
         double get_y (double x) const {
              if (abs(p.x - q.x) < EPS)
                  return p.y;
                                                                                     94
14
              return p.y + (q.y - p.y) * (x - p.x) / (q.x - p.x);
                                                                                     95
 15
                                                                                     96
16
    };
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
33
33
33
33
33
33
33
33
33
     bool intersect1d(double 11, double r1, double 12, double r2) {
                                                                                     99
         if (11 > r1)
              swap(11, r1);
         if (12 > r2)
              swap(12, r2);
         return max(11, 12) <= min(r1, r2) + EPS;
                                                                                         using namespace std;
     int vec(const pt& a, const pt& b, const pt& c) {
                                                                                         class Rectangle {
         double s = (b.x - a.x) * (c.y - a.y) - (b.y - a.y) * (c.x - a.x);
                                                                                         public:
         return abs(s) < EPS ? 0 : s > 0 ? +1 : -1;
                                                                                              Rectangle() {
     bool intersect (const seg& a, const seg& b)
         return intersect1d(a.p.x, a.q.x, b.p.x, b.q.x) &&
                                                                                     11
                 intersect1d(a.p.y, a.q.y, b.p.y, b.q.y) &&
                                                                                                  x1 = X1;
                 vec(a.p, a.q, b.p) * vec(a.p, a.q, b.q) <= 0 &&
                                                                                     13
                                                                                                  y1 = Y1;
                 vec(b.p, b.q, a.p) * vec(b.p, b.q, a.q) <= 0;
                                                                                     14
                                                                                                  x^2 = x^2;
                                                                                     15
                                                                                                  y2 = Y2;
                                                                                     16
    bool operator<(const seg& a, const seg& b)
40
                                                                                     17
                                                                                         struct Event {
\frac{41}{42}
         double x = max(min(a.p.x, a.q.x), min(b.p.x, b.q.x));
                                                                                     19
         return a.get_y(x) < b.get_y(x) - EPS;</pre>
                                                                                     20
                                                                                              Event() {}
43
                                                                                     2\dot{1}
     struct event {
                                                                                                   (type) {}
46
         double x;
 47
         int tp, id;
48
```

dq.pop_front();

// Add new half-plane

// Final cleanup: Check half-planes at the front against the back

dq.push_back(H[i]);

--len;

++len:

100

101

104

105

106

49

event() {}

```
event(double x, int tp, int id) : x(x), tp(tp), id(id) {}
        bool operator<(const event& e) const {</pre>
53
            if^-(abs(x - e.x) > EPS)
54
                return x < e.x;
55
            return tp > e.tp;
56
57
   };
   set<seg> s;
   vector<set<seg>::iterator> where;
   set<seg>::iterator prev(set<seg>::iterator it) {
        return it == s.begin() ? s.end() : --it;
   set<seg>::iterator next(set<seg>::iterator it) {
   pair<int, int> solve(const vector<seg>& a) {
        int n = (int)a.size();
        for (int i = 0; i < n; ++i) {
            e.push_back(event(min(a[i].p.x, a[i].q.x), +1, i));
            e.push_back(event(max(a[i].p.x, a[i].q.x), -1, i));
        sort(e.begin(), e.end());
        where.resize(a.size());
        for (size_t i = 0; i < e.size(); ++i) {</pre>
            int i\overline{d} = e[i].id;
            if (e[i].tp == +1)
                set<seg>::iterator nxt = s.lower_bound(a[id]), prv = prev(
                if (nxt != s.end() && intersect(*nxt, a[id]))
                    return make_pair(nxt->id, id);
                if (prv != s.end() && intersect(*prv, a[id]))
                    return make_pair(prv->id, id);
                where[id] = s.insert(nxt, a[id]);
                set<seq>::iterator nxt = next(where[id]), prv = prev(where
                if (nxt != s.end() && prv != s.end() && intersect(*nxt, *
                    prv))
                    return make_pair(prv->id, nxt->id);
                s.erase(where[id]);
        return make_pair(-1, -1);
```

Rectangles Union

```
#include <bits/stdc++.h>
    #define P(x,y) make_pair(x,y)
        int x1, y1, x2, y2;
        static Rectangle empt;
            x1 = y1 = x2 = y2 = 0;
        Rectangle (int X1, int Y1, int X2, int Y2) {
        int x, y1, y2, type;
        Event (int x, int y1, int y2, int type): x(x), y1(y1), y2(y2), type
   bool operator < (const Event&A, const Event&B) {</pre>
24
   //if(A.x != B.x)
        return A.x < B.x;</pre>
```

```
//if(A.y1 != B.y1) return A.y1 < B.y1;
     //if(A.v2 != B.v2()) A.v2 < B.v2;
28
29
30
31
32
     const int MX = (1 << 17);
     struct Node {
         int prob, sum, ans;
         Node() {}
33
         Node (int prob, int sum, int ans): prob(prob), sum(sum), ans(ans)
\frac{34}{35} \\ 36
     Node tree [MX \star 4];
     int interval[MX];
37
38
39
40
     void build(int x, int a, int b) {
         tree[x] = Node(0, 0, 0);
         if(a == b) {
              tree[x].sum += interval[a];
41
              return;
42
43
         build(x * 2, a, (a + b) / 2);
build(x * 2 + 1, (a + b) / 2 + 1, b);
45
46
47
48
         tree[x].sum = tree[x * 2].sum + tree[x * 2 + 1].sum;
     int ask(int x)
         if(tree[x].prob)
49
             return tree[x].sum;
50
51
52
53
54
55
56
57
58
59
         return tree[x].ans;
     int st, en, V;
     void update(int x, int a, int b) {
         if(st > b || en < a)
              return:
         if(a >= st \&\& b <= en) {
              tree[x].prob += V;
              return;
60
         update(x * 2, a, (a + b) / 2);
update(x * 2 + 1, (a + b) / 2 + 1, b);
61
62
         tree[x].ans = ask(x \star 2) + ask(x \star 2 + 1);
\frac{63}{64}
    Rectangle Rectangle::empt = Rectangle();
65
    vector < Rectangle > Rect;
    vector < int > sorted;
67
    vector < Event > sweep;
    void compressncalc() {
69
         sweep.clear();
          sorted.clear();
70
71
72
73
74
75
76
77
78
80
81
82
83
84
85
86
87
88
          for(auto R : Rect)
              sorted.push_back(R.y1);
              sorted.push_back(R.y2);
         sort(sorted.begin(), sorted.end());
          sorted.erase(unique(sorted.begin(), sorted.end());
         int sz = sorted.size();
          for (int j = 0; j < sorted.size() - 1; <math>j++)
              interval[j + 1] = sorted[j + 1] - sorted[j];
          for(auto R : Rect)
              sweep.push_back(Event(R.x1, R.y1, R.y2, 1));
              sweep.push_back(Event(R.x2, R.y1, R.y2, -1));
         sort(sweep.begin(), sweep.end());
         build(1, 1, sz - 1);
     long long ans;
     void Sweep() {
89
         ans = 0;
90
         if(sorted.empty() || sweep.empty())
91
92
         int last = 0, sz_ = sorted.size();
         for(int j = 0; j < sweep.size(); j++) {
    ans += 111 * (sweep[j].x - last) * ask(1);</pre>
93
94
95
              last = sweep[j].x;
96
              V = sweep[j].type;
97
              st = lower_bound(sorted.begin(), sorted.end(), sweep[j].y1) -
                   sorted.begin() + 1;
98
              en = lower_bound(sorted.begin(), sorted.end(), sweep[j].y2) -
                   sorted.begin();
99
              update(1, 1, \bar{s}z_{-} - 1);
100
101
     int main() {
            freopen("in.in", "r", stdin);
```

```
105
          scanf("%d", &n);
106
          for(int j = 1; j <= n; j++) {</pre>
107
              int a, b, c, d;
scanf("%d %d %d %d", &a, &b, &c, &d);
108
109
               Rect.push_back(Rectangle(a, b, c, d));
110
111
          compressncalc();
112
          Sweep();
113
          cout << ans << endl;
114
```

Graphs

6.1 2 SAD

```
* Description: Calculates a valid assignment to boolean variables a,
         b, c,... to a 2-SAT problem, so that an expression of the type $(
         reports that it is unsatisfiable.
     * Negated variables are represented by bit-inversions (\texttt{\tilde
     * Usage:
     * TwoSat ts(number of boolean variables);
     * ts.either(0, \tilde3); // Var 0 is true or var 3 is false
        ts.setValue(2); // Var 2 is true ts.atMostOne({0, \tilde1, 2}); // <= 1 of vars 0, \tilde1 and 2 are
    * ts.solve(); // Returns true iff it is solvable
    * ts.values[0..N-1] holds the assigned values to the vars
11
     * Time: O(N+E), where N is the number of boolean variables, and E is
         the number of clauses.
13
    struct TwoSat {
14
        int N;
15
        vector<vi> qr;
        vi values; \frac{7}{9} 0 = false, 1 = true
16
17
18
        TwoSat(int n = 0) : N(n), qr(2*n) {}
\frac{19}{20}
        int addVar() { // (optional)
21
            gr.emplace_back();
\overline{22}
            gr.emplace_back();
23
24
25
26
            return N++;
        void either(int f, int j) {
27
            f = \max(2*f, -1-2*f);
            j = \max(2*j, -1-2*j);
29
            gr[f].push_back(j^1);
30
            gr[j].push_back(f^1);
31
32
        void setValue(int x) { either(x, x); }
        void atMostOne(const vi& li) { // (optional)
35
            if (sz(li) <= 1) return;
int cur = ~li[0];</pre>
36
            rep(i,2,sz(li))
                 int next = addVar();
                 either(cur, ~li[i]);
                either(cur, next);
41
                either(~li[i], next);
                cur = "next;
44
            either(cur, ~li[1]);
45
\frac{46}{47}
        vi val, comp, z; int time = 0;
48
        int dfs(int i)
            int low = val[i] = ++time, x; z.push_back(i);
49
            for(int e : gr[i]) if (!comp[e])
50
                low = min(low, val[e] ?: dfs(e));
51
            if (low == val[i]) do {
                x = z.back(); z.pop_back();
54
                 comp[x] = low;
55
                 if (values[x>>1] == -1)
                     values[x>>1] = x&1;
57
            } while (x != i);
58
            return val[i] = low;
59
```

 $\overline{30}$

```
\frac{60}{61} \\ 62
        bool solve() {
             values.assign(N, -1);
63
             val.assign(2*N, 0); comp = val;
             rep(i,0,2*N) if (!comp[i]) dfs(i);
65
             rep(i,0,N) if (comp[2*i] == comp[2*i+1]) return 0;
66
             return 1;
67
68
   };
      Ariculation Point
    vector<int> adj[N];
    int dfsn[N], low[N], instack[N], ar_point[N], timer;
    stack<int> st;
```

void dfs(int node, int par) { dfsn[node] = low[node] = ++timer; int kam = 0;for(auto i: adj[node]) { if(i == par) continue; if(dfsn[i] == 0){ kam++; dfs(i, node); 13 low[node] = min(low[node], low[i]); 14 if(dfsn[node] <= low[i] && par != 0) ar_point[node] = 1;</pre> $15 \\ 16 \\ 17$ else low[node] = min(low[node], dfsn[i]); 18 19 20 21 22 23 24 25 26 27 28 29 **if**(par == 0 && kam > 1) ar_point[node] = 1; int main(){ // Input for (int i = 1; i <= n; i++) {</pre> if(dfsn[i] == 0) dfs(i, 0);for(int i = 1; i <= n; i++) { if(ar_point[i]) c++;

Bridges Tree and Diameter

cout << c << '\n';

```
#include <bits/stdc++.h>
     #define 11 long long
     using namespace std;
     const int N = 3e5 + 5, mod = 1e9 + 7;
     vector<int> adj[N], bridge_tree[N];
    int dfsn[N], low[N], cost[N], timer, cnt, comp_id[N], kam[N], ans;
 8
    stack<int> st;
    void dfs(int node, int par){
         dfsn[node] = low[node] = ++timer;
12
13
         st.push(node);
          for(auto i: adj[node]){
15
               if(i == par) continue;
^{16}_{17}
               if(dfsn[i] == 0){
\begin{array}{c} 18 \\ 19 \\ 20 \\ 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 30 \\ 31 \\ 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 37 \end{array}
                   low[node] = min(low[node], low[i]);
               else low[node] = min(low[node], dfsn[i]);
         if(dfsn[node] == low[node]){
               while(1){
                   int cur = st.top();
                   st.pop();
                   comp_id[cur] = cnt;
                   if(cur == node) break;
    void dfs2(int node, int par) {
         kam[node] = 0;
         int mx = 0, second_mx = 0;
          for(auto i: bridge_tree[node]) {
               if(i == par) continue;
38
               dfs2(i, node);
```

```
kam[node] = max(kam[node], 1 + kam[i]);
40
             if(kam[i] > mx){
41
                  second mx = mx:
                  mx = kam[i];
44
             else second_mx = max(second_mx, kam[i]);
45
46
         ans = max(ans, kam[node]);
47
         if(second_mx) ans = max(ans, 2 + mx + second_mx);
48
\frac{49}{50}
    int main(){
51
         ios_base::sync_with_stdio(0);cin.tie(0);cout.tie(0);
52
53
         cin >> n >> m;
54
         while (m--) {
55
             int u, v;
56
             cin >> u >> v;
57
             adj[u].push_back(v);
58
             adj[v].push_back(u);
59
60
        dfs(1, 0);
for(int i = 1; i <= n; i++) {
61
62
             for(auto j: adj[i]){
63
                 if(comp_id[i] != comp_id[j]){
                      bridge_tree[comp_id[i]].push_back(comp_id[j]);
67
        dfs2(1, 0);
69
        cout << ans;
70
71
72
         return 0;
```

6.4 Dinic With Scalling

```
1 ///O(ElgFlow) on Bipratite Graphs and O(EVlgFlow) on other graphs (I
         think)
    struct Dinic
         #define vi vector<int>
         #define rep(i,a,b) f(i,a,b)
         struct Edge {
              int to, rev;
              11 c, oc;
 9
              11 flow() { return max(oc - c, OLL); } // if you need flows
10
         vi lvl, ptr, q;
11
         vector<vector<Edge>> adj;
12
13
         Dinic(int n) : lvl(n), ptr(n), q(n), adj(n) {}
14
         void addEdge(int a, int b, ll c, int id, ll rcap = 0) {
              adj[a].push_back({b, sz(adj[b]), c, c, id});
15
16
              adj[b].push_back({a, sz(adj[a]) - 1, rcap, rcap,id});
17
18
         11 dfs(int v, int t, 11 f) {
19
              if (v == t || !f) return f;
20
              for (int& i = ptr[v]; i < sz(adj[v]); i++) {</pre>
21
                  Edge& e = adj[v][i];
22
                  if (lvl[e.to] == lvl[v] + 1)
\overline{23}
                       if (ll p = dfs(e.to, t, min(f, e.c))) {
24
                           e.c -= p, adj[e.to][e.rev].c += p;
25
                            return p;
\frac{26}{27}
\overline{28}
              return 0;
\frac{20}{29}
\frac{30}{31}
         11 calc(int s, int t) {
    11 flow = 0; q[0] = s;
    rep(L,0,31) do { // 'int L=30' maybe faster for random data
32
33
                  lvl = ptr = vi(sz(q));
                  int qi = 0, qe = lvl[s] = 1;
34
35
                  while (qi < qe && !lvl[t]) {
                       int^{\dagger}v = q[qi++];
36
                       for (Edge e : adj[v])
   if (!lvl[e.to] && e.c >> (30 - L))
37
                                q[qe++] = e.to, lvl[e.to] = lvl[v] + 1;
                  while (ll p = dfs(s, t, LLONG_MAX)) flow += p;
42
              } while (lvl[t]);
43
              return flow;
```

```
45
       bool leftOfMinCut(int a) { return lvl[a] != 0; }
46
   } ;
      Gomory Hu
```

```
* Author: chilli, Takanori MAEHARA
     * Date: 2020-04-03
     * License: CC0
     * Source: https://github.com/spaghetti-source/algorithm/blob/master/
          graph/gomory_hu_tree.cc#L102
      * Description: Given a list of edges representing an undirected flow
      * returns edges of the Gomory-Hu tree. The max flow between any pair
      * vertices is given by minimum edge weight along the Gomory-Hu tree
          path.
      * Time: $0(V)$ Flow Computations
10
     * Status: Tested on CERC 2015 J, stress-tested
     * Details: The implementation used here is not actually the original
13
     * Gomory-Hu, but Gusfield's simplified version: "Very simple methods
          for all
14
      * pairs network flow analysis". PushRelabel is used here, but any
     * implementation that supports 'leftOfMinCut' also works.
17
    #pragma once
18
19
    #include "PushRelabel.h"
20
21
22
23
24
25
26
27
    typedef array<11, 3> Edge;
    vector<Edge> gomoryHu(int N, vector<Edge> ed) {
  vector<Edge> tree;
        vi par(N);
         rep(i,1,N) {
             PushRelabel D(N); // Dinic also works
for (Edge t : ed) D.addEdge(t[0], t[1], t[2], t[2]);
             tree.push_back({i, par[i], D.calc(i, par[i])});
29
             rep(j,i+1,N)
30
                 if (par[j] == par[i] && D.leftOfMinCut(j)) par[j] = i;
\frac{31}{32}
```

HopcraftKarp BPM

return tree;

```
* Author: Chen Xing
     * Date: 2009-10-13
     * License: CCO
     * Source: N/A
      * Description: Fast bipartite matching algorithm. Graph $9$ should be
      * of neighbors of the left partition, and $btoa$ should be a vector
          full of
 8
      \star -1's of the same size as the right partition. Returns the size of
     * the matching. $btoa[i]$ will be the match for vertex $i$ on the
          right side,
     * or $-1$ if it's not matched.
     * Usage: vi btoa(m, -1); hopcroftKarp(g, btoa);
     * Time: O(\sqrt{V}E)
     * Status: stress-tested by MinimumVertexCover, and tested on
          oldkattis.adkbipmatch and SPOJ:MATCHING
15
    #pragma once
\frac{16}{17}
    bool dfs(int a, int L, vector<vi>& g, vi& btoa, vi& A, vi& B) {
\frac{18}{19}
        if (A[a] != L) return 0;
         A[a] = -1;
\frac{20}{21}
        for (int b : g[a]) if (B[b] == L + 1) {
22
             if (btoa[b] == -1 || dfs(btoa[b], L + 1, g, btoa, A, B))
23
24
25
26
27
28
29
                 return btoa[b] = a, 1;
        return 0;
    int hopcroftKarp(vector<vi>& q, vi& btoa) {
        int res = 0;
\bar{30}
        vi A(g.size()), B(btoa.size()), cur, next;
31
        for (;;) {
```

```
\frac{32}{33}
             fill(all(A), 0);
             fill(all(B), 0);
34
             /// Find the starting nodes for BFS (i.e. layer 0).
35
             cur.clear();
36
             for (int a : btoa) if (a !=-1) A[a] = -1;
37
             rep(a, 0, sz(q)) if(A[a] == 0) cur.push_back(a);
38
             /// Find all layers using bfs.
39
            for (int lay = 1;; lay++) {
40
                 bool islast = 0;
                 next.clear();
41
                 for (int a : cur) for (int b : g[a]) {
                     if (btoa[b] == -1) {
                         B[b] = lay;
45
                         islast = 1;
47
                     else if (btoa[b] != a && !B[b]) {
                         B[b] = lay;
48
49
                         next.push_back(btoa[b]);
50
51
                 if (islast) break;
                 if (next.empty()) return res;
54
                 for (int a : next) A[a] = lay;
                 cur.swap(next);
56
57
             /// Use DFS to scan for augmenting paths.
58
            rep(a, 0, sz(q))
59
                 res += dfs(a, 0, g, btoa, A, B);
61
```

Hungarian 6.7

```
Notes:
             note that n must be <= m
             so in case in your problem n >= m, just swap
         also note this
         void set(int x, int y, ll v) \{a[x+1][y+1]=v;\}
         the algorithim assumes you're using 0-index
 8
         but it's using 1-based
 9
10
    struct Hungarian {
11
         const 11 INF = 1000000000000000000; ///10^18
12
\bar{13}
         vector<vector<ll> > a;
14
         vector<ll> u,v;vector<int> p,way;
15
         Hungarian(int n, int m):
16
         n(n), m(m), a(n+1, vector<11>(m+1, INF-1)), u(n+1), v(m+1), p(m+1), way (m+1)
              +1) {}
17
         void set(int x, int y, ll v) {a[x+1][y+1]=v;}
18
         11 assign(){
             for(int i = 1; i <= n; i++) {
                  int j0=0;p[0]=i;
                  vector<ll> minv(m+1, INF);
21
\bar{2}\bar{2}
                  vector<char> used(m+1, false);
^{24}
                       used[j0]=true;
25
                       int i0=p[j0], j1; ll delta=INF;
                      for(int j = 1; j <= m; j++)if(!used[j]) {
    l1 cur=a[i0][j]-u[i0]-v[j];
    if(cur<minv[j])minv[j]=cur,way[j]=j0;</pre>
26
27
28
                           if (minv[j] < delta) delta=minv[j], j1=j;</pre>
31
                       for(int j = 0; j <= m; j++)
                           if(used[j])u[p[j]]+=delta,v[j]-=delta;
33
                            else minv[j]-=delta;
                       j0=j1;
35
                    while(p[j0]);
37
                      int j1=way[j0];p[j0]=p[j1];j0=j1;
38
                  } while(†0);
39
             return -v[0];
41
         vector<int> restoreAnswer() { ///run it after assign
43
              vector<int> ans (n+1);
              for (int j=1; j<=m; ++j)
44
                  ans[p[j]] = j;
45
             return ans;
47
48
   };
```

```
___
```

51

```
6.8 Kosaraju
       g: Adjacency List of the original graph
       rg : Reversed Adjacency List
       vis : A bitset to mark visited nodes
       adj : Adjacency List of the super graph
       stk : holds dfs ordered elements
cmp[i] : holds the component of node i
       go[i] : holds the nodes inside the strongly connected component i
    #define FOR(i,a,b) for(int i = a; i < b; i++)
12
    #define pb push_back
\frac{13}{14}
    const int N = 1e5+5;
\frac{15}{16}
    vector<vector<int>>g, rg;
17
    vector<vector<int>>go;
    bitset<N>vis;
18
19
    vector<vector<int>>adj;
20
    stack<int>stk;
\overline{21}
    int n, m, cmp[N];
\frac{22}{23}
    void add_edge(int u, int v) {
      g[u].push_back(v);
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
      rg[v].push_back(u);
    void dfs(int u) {
      vis[u]=1;
       for(auto v : g[u])if(!vis[v])dfs(v);
       stk.push(u);
    void rdfs(int u,int c){
      vis[u] = 1;
       cmp[u] = c;
       go[c].push_back(u);
       for(auto v : rq[u])if(!vis[v])rdfs(v,c);
    int scc() {
       vis.reset();
       for(int i = 0; i < n; i++)if(!vis[i])</pre>
40
         dfs(i);
41
       vis.reset();
42
       int c = 0;
\frac{43}{44}
       while(stk.size()){
         auto cur = stk.top();
45
         stk.pop();
         if(!vis[cur])
47
           rdfs(cur,c++);
\frac{48}{49}
```

6.9 Manhattan MST

return c;

```
#include<bits/stdc++.h>
    using namespace std;
    const int N = 2e5 + 9;
    vector<pair<int, int>> q[N];
    struct PT {
      int x, y, id;
      bool operator < (const PT &p) const
        return x == p.x ? y < p.y : x < p.x;
    } p[N];
14
   struct node
15
      int val, id;
16
     t[N];
17
    struct DSU
18
      int p[N];
19
      void init(int n) { for (int i = 1; i \le n; i++) p[i] = i; }
20
      int find(int u) { return p[u] == u ? u : p[u] = find(p[u]); }
21
      void merge(int u, int v) { p[find(u)] = find(v); }
22
23
24
     dsu:
    struct edge
      int u, v, w;
25
      bool operator < (const edge &p) const { return w < p.w; }</pre>
^{26}
```

```
vector<edge> edges;
    int query(int x)
29
      int r = 2e9 + 10, id = -1;
30
      for (; x \le n; x += (x \& -x)) if (t[x].val < r) r = t[x].val, id = t
           [x].id;
      return id;
32
33
    void modify(int x, int w, int id)
34
      for (; x > 0; x -= (x \& -x)) if (t[x].val > w) t[x].val = w, t[x].id
           = id:
    int dist(PT &a, PT &b) {
37
      return abs(a.x - b.x) + abs(a.y - b.y);
38
    void add(int u, int v, int w)
40
      edges.push_back({u, v, w});
   long long Kruskal() {
      dsu.init(n);
44
      sort(edges.begin(), edges.end());
45
      long long ans = 0;
46
      for (edge e : edges)
47
        int u = e.u, v = e.v, w = e.w;
        if (dsu.find(u) != dsu.find(v)) {
49
          ans += w;
50
          g[u].push_back(\{v, w\});
51
          //g[v].push_back({u, w});
52
          dsu.merge(u, v);
53
54
55
      return ans;
57
    void Manhattan()
58
      for (int i = 1; i <= n; ++i) p[i].id = i;
59
      for (int dir = 1; dir <= 4; ++dir) {
60
        if (dir == 2 || dir == 4) {
61
          for (int i = 1; i <= n; ++i) swap(p[i].x, p[i].y);</pre>
62
63
        else if (dir == 3) {
64
          for (int i = 1; i \le n; ++i) p[i].x = -p[i].x;
65
66
        sort(p + 1, p + 1 + n);
67
        vector<int> v;
68
        static int a[N];
        for (int i = 1; i \le n; ++i) a[i] = p[i].y - p[i].x, v.push\_back(a
69
70
        sort(v.begin(), v.end());
71
        v.erase(unique(v.begin(), v.end()), v.end());
72
        for (int i = 1; i \le n; ++i) a[i] = lower_bound(v.begin(), v.end())
              a[i]) - v.begin() + 1;
        for (int i = 1; i <= n; ++i) t[i].val = 2e9 + 10, t[i].id = -1;
for (int i = n; i >= 1; --i) {
74
75
          int pos = query(a[i]);
76
          if (pos != -1) add(p[i].id, p[pos].id, dist(p[i], p[pos]));
77
          modify(a[i], p[i].x + p[i].y, i);
78
79
80
81
    int32_t main() {
      ios_base::sync_with_stdio(0);
      cin.tie(0);
      cin >> n;
85
      for (int i = 1; i <= n; i++) cin >> p[i].x >> p[i].y;
      Manhattan();
      cout << Kruskal() << '\n';</pre>
      for (int u = 1; u <= n; u++) {
        for (auto x: g[u]) cout << u - 1 << ' ' << x.first - 1 << '\n';
90
91
      return 0;
92
```

6.10 Maximum Clique

```
20
21
22
23
24
25
26
    int max_clique (int n) {
      res = 0;
       for (int i = 1; i <= n; i++) {
         edges[i - 1] = 0;
27
         for (int j = 1; j \le n; j++) if (g[i][j]) edges[i-1] = (1LL)
              << (\dot{1} - 1) );
29
       BronKerbosch (n, 0, (1LL \ll n) - 1, 0);
30
       return res;
31
 6.11
         MCMF
         Notes:
 \bar{3}
              make sure you notice the #define int 11
              focus on the data types of the max flow everythign inside is
                   integer
 5
              addEdge(u, v, cap, cost)
              note that for min cost max flow the cost is sum of cost * flow over all edges
    struct Edge {
10
         int to;
11
         int cost;
12
         int cap, flow, backEdge;
13
14
15
    };
    struct MCMF {
\begin{array}{c} 16\\17\\18\\19\\20\\21\\22\\24\\25\\26\\27\\28\\33\\34\\35\\36\\37\\38\\39\\40 \end{array}
         const int inf = 1000000010;
         vector<vector<Edge>> g;
         MCMF (int _n)
              n = _n + 1;
              q.resize(n);
         void addEdge(int u, int v, int cap, int cost) {
              Edge e1 = \{v, cost, cap, 0, (int) g[v].size()\};
              Edge e2 = \{u, -\cos t, 0, 0, (int) g[u].size()\};
              q[u].push back(e1);
              g[v].push_back(e2);
         pair<int, int> minCostMaxFlow(int s, int t) {
              int flow = 0;
              int cost = 0;
              vector<int> state(n), from(n), from_edge(n);
              vector<int> d(n);
              deque<int> q;
              while (true) {
                   for (int i = 0; i < n; i++)
\frac{41}{42}
\frac{43}{44}
                       state[i] = 2, d[i] = inf, from[i] = -1;
                   state[s] = 1;
                   q.clear();
                   q.push_back(s);
\frac{45}{46}
                   d[s] = 0;
                   while (!q.empty())
47
                       int v = q.front();
48
                        q.pop_front();
49
                        state[v] = 0;
50
                        for (int i = 0; i < (int) g[v].size(); i++) {</pre>
```

if (P == 0LL && X == 0LL) { //here we will find all possible maximal 51

cliques (not maximum) i.e. there is no node which can be

BronKerbosch(n, R | (1LL << v), P & edges[v], X & edges[v]);</pre>

if (((1LL << v) & P) && !((1LL << v) & edges[u])) {</pre>

included in this set

for (int v = 0; v < n; v++)

P -= (1LL << v);

 $X \mid = (1LL << v);$

res = max(res, t);

return:

int u = 0;

12

 $\overline{13}$

14

15

16

17

18

19

int t = __builtin_popcountll(R);

while (!((1LL << u) & (P | X))) u ++;</pre>

```
Edge e = g[v][i];
                        if (e.flow \ge e.cap \mid \mid (d[e.to] \le d[v] + e.cost))
                             continue;
                         int to = e.to;
                        d[to] = d[v] + e.cost;
                         from[to] = v;
                         from_edge[to] = i;
                         if (state[to] == 1) continue;
                        if (!state[to] || (!q.empty() && d[q.front()] > d[
                             q.push_front(to);
                         else q.push_back(to);
                        state[to] = 1;
                if (d[t] == inf) break;
                int it = t, addflow = inf;
                while (it != s) {
                    addflow = min(addflow,
                                   g[from[it]][from_edge[it]].cap
                                   - g[from[it]][from_edge[it]].flow);
                    it = from[it]:
                it = t;
                while (it != s)
                    g[from[it]][from_edge[it]].flow += addflow;
                    g[it][q[from[it]][from_edge[it]].backEdge].flow -=
                        addflow;
                    cost += g[from[it]][from_edge[it]].cost * addflow;
                    it = from[it];
                flow += addflow;
            return {cost, flow};
84
   };
```

6.12Minimum Arbroscene in a Graph

53

55

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63 64

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81

82

83

```
const int maxn = 2510, maxm = 7000000;
    const 11 maxint = 0x3f3f3f3f3f3f3f3f3f1LL;
    int n, ec, ID[maxn], pre[maxn], vis[maxn];
   11 in[maxn];
    struct edge_t {
        int u, v;
        11 w;
   } edge[maxm];
    void add(int u, int v, ll w)
12
        edge[++ec].u = u, edge[ec].v = v, edge[ec].w = w;
13
14
15
   11 arborescence(int n, int root) {
16
        11 \text{ res} = 0, \text{ index};
17
        while (true)
18
            for (int i = 1; i \le n; ++i) {
19
                 in[i] = maxint, vis[i] = -1, ID[i] = -1;
20
21
            for (int i = 1; i <= ec; ++i) {
22
                 int u = edge[i].u, v = edge[i].v;
23
                 if (u == v || in[v] <= edge[i].w) continue;</pre>
24
                 in[v] = edge[i].w, pre[v] = u;
25
26
            pre[root] = root, in[root] = 0;
\overline{27}
             for (int i = 1; i <= n; ++i) {
                 res += in[i];
29
                 if (in[i] == maxint) return -1;
31
            for (int i = 1; i <= n; ++i) {
                 if (vis[i] != -1) continue;
                 int u = i, v;
35
                 while (vis[u] == -1) {
                     vis[u] = i;
                     u = pre[u];
38
39
                 if (vis[u] != i || u == root) continue;
                 for (v = u, u = pre[u], ++index; u != v; u = pre[u]) ID[u]
                       = index;
41
                 ID[v] = index;
```

```
struct MinimumVertexCover {
          int n, id;
 5
          vector<vector<int> > g;
          vector<int> color, m, seen;
          vector<int> comp[2];
          MinimumVertexCover() {}
          MinimumVertexCover(int n, vector<vector<int> > g) {
               this->n = n;
               this->g = g;
\frac{13}{14}
               color = m = vector<int>(n, -1);
               seen = vector<int>(n, 0);
15
               makeBipartite();
^{16}_{17}_{18}
          void dfsBipartite(int node, int col) {
19
               if (color[node] != -1) {
20
                    assert(color[node] == col); /* MSH BIPARTITE YA
                          BASHMOHANDES */
\begin{array}{c} 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 30 \\ 31 \\ 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 37 \\ 38 \\ 39 \\ 40 \end{array}
                    return:
               color[node] = col;
               comp[col].push_back(node);
               for (int i = 0; i < int(q[node].size()); i++)</pre>
                    dfsBipartite(g[node][i], 1 - col);
          void makeBipartite() {
               for (int i = 0; i < n; i++)
                    if (color[i] == -1)
                         dfsBipartite(i, 0);
           // match a node
          bool dfs(int node) {
             random_shuffle(g[node].begin(),g[node].end());
               for (int i = 0; i < g[node].size(); i++) {</pre>
                    int child = g[node][i];
                    if (m[child] == -1) {
                         m[node] = child;
m[child] = node;
\begin{array}{c} 41 \\ 42 \\ 43 \\ 44 \\ 45 \\ 46 \\ 47 \\ 48 \end{array}
                         return true;
                    if (seen[child] == id)
                         continue;
                    seen[child] = id;
                    int enemy = m[child];
49
50
51
52
53
54
55
56
57
58
59
60
61
                    m[node] = child;
                    m[child] = node;
                    m[enemy] = -1;
                    if (dfs(enemy))
                         return true;
                    m[node] = -1;
                    m[child] = enemy;
                    m[enemy] = child;
               return false;
          void makeMatching() {
62
          for (int j = 0; j < 5; j++)
63
             random_shuffle(comp[0].begin(),comp[0].end(),myrandom );
64
               for (int i = 0; i < int(comp[0].size()); i++) {</pre>
65
                    id++:
66
                    if(m[comp[0][i]] == -1)
67
                         dfs(comp[0][i]);
```

```
69
         void recurse(int node, int x, vector<int> &minCover, vector<int> &
              if (m[node] != −1)
74
                  return;
75
             if (done[node]) return;
done[node] = 1;
76
              for (int i = 0; i < int(g[node].size()); i++) {</pre>
77
 78
                  int child = g[node][i];
79
                  int newnode = m[child];
80
                  if (done[child]) continue;
81
                  if(newnode == -1) {
82
                      continue;
83
84
                  done[child] = 2;
                  minCover.push_back(child);
                  m[newnode] = -1;
87
                  recurse (newnode, x, minCover, done);
91
         vector<int> getAnswer() {
             vector<int> minCover, maxIndep;
             vector<int> done(n, 0);
94
             makeMatching();
95
             for (int x = 0; x < 2; x++)
96
                  for (int i = 0; i < int(comp[x].size()); i++) {</pre>
97
                      int node = comp[x][i];
                      if (m[node] == -1)
99
                           recurse (node, x, minCover, done);
100
101
102
             for (int i = 0; i < int(comp[0].size()); i++)</pre>
103
                  if (!done[comp[0][i]]) {
104
                      minCover.push_back(comp[0][i]);
105
106
             return minCover;
107
108
    };
```

6.14 Prufer Code

```
1
    const int N = 3e5 + 9;
    prufer code is a sequence of length n-2 to uniquely determine a
        labeled tree with n vertices
    Each time take the leaf with the lowest number and add the node number
         the leaf is connected to
    the sequence and remove the leaf. Then break the algo after n-2
        iterations
    //0-indexed
   int n;
    vector<int> q[N];
   int parent[N], degree[N];
   void dfs (int v) {
      for (size_t i = 0; i < q[v].size(); ++i) {</pre>
13
14
        int to = g[v][i];
15
        if (to != parent[v]) {
16
          parent[to] = v;
17
          dfs (to);
18
19
20
      }
   vector<int> prufer_code() {
      parent[n-1] = -1;
      dfs (n - 1);
      int ptr = -1;
26
27
      for (int i = 0; i < n; ++i) {
        degree[i] = (int) g[i].size();
        if (degree[i] == 1 && ptr == -1) ptr = i;
      vector<int> result;
      int leaf = ptr;
      for (int iter = 0; iter < n - 2; ++iter) {</pre>
        int next = parent[leaf];
34
        result.push_back (next);
```

```
--degree[next];
\frac{36}{37} \\ 38
         if (degree[next] == 1 && next < ptr) leaf = next;</pre>
           ++ptr;
39
           while (ptr < n && degree[ptr] != 1) ++ptr;</pre>
40
           leaf = ptr;
41
4\overline{2}
\overline{43}
      return result;
44
45
    vector < pair<int, int> > prufer_to_tree(const vector<int> &
         prufer_code) {
      int n = (int) prufer_code.size() + 2;
47
      vector<int> degree (n, 1);
48
      for (int i = 0; i < n - 2; ++i) ++degree[prufer_code[i]];</pre>
49
50
51
52
53
54
55
56
57
      int ptr = 0;
      while (ptr < n && degree[ptr] != 1) ++ptr;</pre>
      int leaf = ptr;
      vector < pair<int, int> > result;
      for (int i = 0; i < n - 2; ++i) {
         int v = prufer_code[i];
         result.push_back (make_pair (leaf, v));
         --degree[leaf];
58
59
        if (--degree[v] == 1 && v < ptr) leaf = v;</pre>
60
           ++ptr;
61
           while (ptr < n && degree[ptr] != 1) ++ptr;</pre>
62
63
64
65
      for (int v = 0; v < n - 1; ++v) if (degree[v] == 1) result.push_back
             (make pair (v, n - 1));
66
      return result;
67
 6.15 Push Relabel Max Flow
    struct edge
 2
         int from, to, cap, flow, index;
```

```
edge (int from, int to, int cap, int flow, int index):
 5
               from(from), to(to), cap(cap), flow(flow), index(index) {}
    };
     struct PushRelabel
10
          int n;
11
         vector<vector<edge> > g;
         vector<long long> excess;
         vector<int> height, active, count;
\frac{14}{15}
\frac{16}{16}
         queue<int> Q;
          PushRelabel(int n):
17
               n(n), g(n), excess(n), height(n), active(n), count(2*n) {}
^{18}_{19}
          void addEdge(int from, int to, int cap)
\begin{array}{c} 20 \\ 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 30 \\ 31 \\ 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 37 \\ 38 \\ 39 \\ \end{array}
               g[from].push_back(edge(from, to, cap, 0, g[to].size()));
               if(from==to)
                    g[from].back().index++;
               q[to].push_back(edge(to, from, 0, 0, q[from].size()-1));
         void enqueue(int v)
               if(!active[v] && excess[v] > 0)
                    active[v]=true;
                    Q.push(v);
          void push (edge &e)
               int amt=(int)min(excess[e.from], (long long)e.cap - e.flow);
               if (height[e.from] <= height[e.to] || amt == 0)</pre>
^{40}_{41}_{42}
                    return;
               e.flow += amt;
               g[e.to][e.index].flow -= amt;
43
               excess[e.to] += amt;
44
               excess[e.from] -= amt;
```

```
enqueue (e.to);
    void relabel(int v)
         count[height[v]]--;
         int d=2*n;
         for(auto &it:q[v])
             if(it.cap-it.flow>0)
                 d=min(d, height[it.to]+1);
         height[v]=d;
         count[height[v]]++;
         enqueue (v);
     void gap(int k)
         for (int v=0; v<n; v++)
             if(height[v] < k)</pre>
                 continue;
             count[height[v]]--;
             height[v]=max(height[v], n+1);
             count[height[v]]++;
             enqueue (v);
    void discharge(int v)
         for(int i=0; excess[v]>0 && i<q[v].size(); i++)</pre>
             push(g[v][i]);
         if(excess[v]>0)
             if (count [height[v]] == 1)
                 gap(height[v]);
             else
                 relabel(v);
     long long max flow(int source, int dest)
         count[0] = n-1;
         count[n] = 1;
         height[source] = n;
         active[source] = active[dest] = 1;
         for(auto &it:q[source])
             excess[source]+=it.cap;
             push (it);
         while(!Q.empty())
             int v=0.front();
             Q.pop();
             active[v]=false;
             discharge(v);
         long long max_flow=0;
         for(auto &e:g[source])
             max flow+=e.flow;
         return max_flow;
};
```

6.16 Tarjan Algo

 $\frac{46}{47}$ $\frac{48}{48}$

49

50

51

 $5\overline{2}$

53

 $5\overline{4}$

55

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 $\frac{61}{62}$

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72 73

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 $\frac{83}{84}$

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105

106

 $\frac{107}{108}$

109

110

 $\frac{111}{112}$

 $\frac{113}{114}$

```
vector< vector<int> > scc;
vector<int> adj[N];
int dfsn[N], low[N], cost[N], timer, in_stack[N];
stack<int> st;

// to detect all the components (cycles) in a directed graph
void tarjan(int node) {
    dfsn[node] = low[node] = ++timer;
    in_stack[node] = 1;
```

```
10
          st.push(node);
11
          for(auto i: adj[node]) {
12
               if(dfsn[i] == 0){
13
                   tarjan(i);
                   low[node] = min(low[node], low[i]);
15
16
17
18
               else if(in_stack[i]) low[node] = min(low[node], dfsn[i]);
         if(dfsn[node] == low[node]) {
19
               scc.push_back(vector<int>());
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
               while(1) {
                   int cur = st.top();
                   st.pop();
                   in_stack[cur] = 0;
                   scc.back().push_back(cur);
                   if(cur == node) break;
    int main(){
         int m;
          cin >> m;
         while (m--) {
               int u, v;
               cin >> u >> v;
               adj[u].push_back(v);
          for (int i = 1; i \le n; i++) {
               if(dfsn[i] == 0){
                   tarjan(i);
\frac{40}{41}
\frac{42}{43}
         return 0;
44
```

6.17 Bipartite Matching

```
// vertex are one based
     struct graph
 3
           int L, R;
 5
           vector<vector<int> > adj;
          graph(int 1, int r) : L(1), R(r), adj(1+1) {}
          void add_edge(int u, int v)
                adj[u].push_back(v+L);
10
\frac{11}{12}
          int maximum_matching()
                 vector<int> mate(L+R+1,-1), level(L+1);
\frac{13}{14}
                 function < bool (void) > levelize = [&]()
15
16
                      queue<int> q;
17
                      for(int i=1; i<=L; i++)</pre>
18
19
                            level[i] = -1;
\begin{array}{c} 20 \\ 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 30 \\ 31 \\ 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 37 \\ 38 \\ 40 \\ 41 \\ \end{array}
                           if (mate[i] < 0)
                                 q.push(i), level[i]=0;
                      while(!q.empty())
                           int node=q.front();
                           q.pop();
                           for(auto i : adj[node])
                                 int v=mate[i];
                                 if(v<0)
                                      return true;
                                 if(level[v]<0)</pre>
                                       level[v] = level[node] +1;
                                      q.push(v);
                      return false;
                 function < bool (int) > augment = [&] (int node)
42
4\bar{3}
                      for(auto i : adj[node])
44
```

```
int v=mate[i];
46
                        if(v<0 || (level[v]>level[node] && augment(v)))
47
48
                             mate[node]=i;
                             mate[i]=node;
50
                             return true;
52
53
                   return false;
54
55
              int match=0;
56
              while(levelize())
57
                   for(int i=1; i<=L; i++)
   if(mate[i] < 0 && augment(i))</pre>
58
59
                             match++;
60
              return match;
61
62
    };
```

7 Math

7.1 Sum Of Floor

```
// \text{ return sum}_{i=0}^{n-1} \text{ floor}((ai + b) / m) \pmod{2^{64}}
    #define ull unsigned long long
    ull floor_sum_unsigned(ull n, ull m, ull a, ull b) {
         ull ans = 0;
         while (true)
             if(a >= m) {
                  ans += n * (n - 1) / 2 * (a / m);
                  a \% = m;
             if (b >= m) {
11
                  ans += n * (b / m);
12
                  b \% = m;
13
14
             ull y_max = a * n + b;
15
             if (y_max < m) break;</pre>
16
             // y_max < m * (n + 1)
// floor(y_max / m) <= n
17
18
             n = (ull)(y_max / m);
19
             b = (ull) (y_max % m);
20
             std::swap(m, a);
21
22
23
         return ans;
```

7.2 Xor With Gauss

```
1
 \tilde{2}
         Some applications
 3
         If you want to find the maximum in xor subset
         just ans = max(ans, ans \hat{p}[i]) for all i
 5
         if you want to count the number of subsets with a certain value
 6
         check all different subsets of p
    */
11 p[66];
 8
 9
    bool add(ll x) {
         for(int i = 60; (~i) && x; --i) {
   if(x >> i & 1) {
10
11
12
                  if(!p[i]) {
13
                       p[i] = x;
14
                       return true;
15
                       else {
16
                         ^{=} p[i];
17
18
19
20
         return false;
2\dot{1}
```

7.3 Josephus

```
1  // n = total person
2  // will kill every kth person, if k = 2, 2,4,6,...
3  // returns the mth killed person
4  ll josephus(ll n, ll k, ll m) {
5   m = n - m;
6  if (k <= 1) return n - m;
7  ll i = m;</pre>
```

```
___
```

7.4 Rabin Miller Primality check

```
// n < 4,759,123,141
// n < 1,122,004,669,633
                                                   3 : 2, 7, 61
4 : 2, 13, 23, 1662803
     // n < 3,474,749,660,383
                                                    6 : pirmes <= 13
    // n < 3,825,123,056,546,413,051
                                                   9 : primes <= 23
     int testPrimes[] = {2,3,5,7,11,13,17,19,23};
     struct MillerRabin{
10
       ///change K according to n
11
       const int K = 9;
       11 mult(ll s, ll m, ll mod){
\frac{13}{14}
          if(!m) return 0;
          11 ret = mult(s, m/2, mod);
          ret = (ret + ret) % mod;
          if (m & 1) ret = (ret + s) % mod;
\begin{array}{c} 17 \\ 18 \\ 19 \\ 20 \\ 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 30 \\ 31 \\ 32 \\ 33 \\ 35 \\ 36 \\ 37 \\ 38 \\ 40 \\ 41 \\ 42 \\ \end{array}
          return ret;
       11 power(11 x, 11 p, 11 mod) {
          11 s = 1, m = x;
          while(p) {
            if(p&1) s = mult(s, m, mod);
            p >>= 1;
            m = mult(m, m, mod);
          return s;
       bool witness(ll a, ll n, ll u, int t) {
          11 x = power(a, u, n), nx;
          for(int i = 0; i < t; i++) {</pre>
            nx = mult(x, x, n);
             if (nx == 1 \text{ and } x != 1 \text{ and } x != n-1) return 1;
             x = nx;
          return x != 1;
       bool isPrime(11 n){    // return 1 if prime, 0 otherwise
          if(n < 2) return 0;
          if(!(n&1)) return n == 2;
43
44
45
46
          for(int i = 0; i < K; i++)if(n == testPrimes[i])return 1;</pre>
          11 u = n-1; int t = 0;
          while (u&1) u >>= 1, t++; // n-1 = u *2^t
\tilde{47}
\frac{1}{48}
          for (int i = 0; i < K; i++) if (witness (testPrimes[i], n, u, t))
49
          return 1;
50
    }tester;
```

8 Strings

8.1 Aho-Corasick Mostafa

```
1     struct AC_FSM {
2     #define ALPHABET_SIZE 26
3
4     struct Node {
5         int child[ALPHABET_SIZE], failure = 0, match_parent = -1;
6         vector<int> match;
7         Node() {
9             for (int i = 0; i < ALPHABET_SIZE; ++i)child[i] = -1;
10             }
11             };
12             vector<Node> a;
14             AC_FSM() {
```

```
a.push_back(Node());
17
18
19
         void construct_automaton(vector<string> &words) {
              for (int w = 0, n = 0; w < words.size(); ++w, n = 0) {
   for (int i = 0; i < words[w].size(); ++i) {</pre>
20
\frac{21}{22}
                       if (a[n].child[words[w][i] - 'a'] == -1) {
   a[n].child[words[w][i] - 'a'] = a.size();
\overline{23}
24
                             a.push back(Node());
25
\frac{26}{27}
                        \dot{n} = a[n].child[words[w][i] - 'a'];
\frac{21}{28}
                   a[n].match.push_back(w);
29
30
              queue<int> q;
              for (int k = 0; k < ALPHABET_SIZE; ++k) {</pre>
31
32
                   if (a[0].child[k] == -1) a[0].child[k] = 0;
                   else if (a[0].child[k] > 0) {
    a[a[0].child[k]].failure = 0;
33
34
35
                        q.push(a[0].child[k]);
36
38
              while (!q.empty())
39
                   int r = q.front();
                   q.pop();
40
41
                   for (int k = 0, arck; k < ALPHABET_SIZE; ++k) {</pre>
42
                        if ((arck = a[r].child[k]) != -1) {
43
                             q.push(arck);
44
                             int v = a[r].failure;
                            while (a[v].child[k] == -1) v = a[v].failure;
a[arck].failure = a[v].child[k];
45
46
47
                             a[arck].match_parent = a[v].child[k];
48
                             while (a[arck].match_parent != -1 &&
49
                                     a[a[arck].match_parent].match.empty())
50
                                  a[arck].match_parent =
51
                                           a[a[arck].match_parent].match_parent;
52
53
54
55
56
57
         void aho_corasick(string &sentence, vector<string> &words,
58
                               vector<vector<int> > &matches) {
59
              matches.assign(words.size(), vector<int>());
60
              int state = 0, ss = 0;
              for (int i = 0; i < sentence.length(); ++i, ss = state) {</pre>
61
62
                   while (a[ss].child[sentence[i] - 'a'] == -1)
63
                        ss = a[ss].failure;
64
                   state = a[state].child[sentence[i] - 'a'] = a[ss].child[
                        sentence[i] - 'a'];
                   for (ss = state; ss != -1; ss = a[ss].match_parent)
66
                        for (int w: a[ss].match)
67
                             matches[w].push_back(i + 1 - words[w].length());
68
69
70
    };
```

8.2 KMP Anany

```
vector<int> fail(string s) {
 23
        int n = s.size();
        vector<int> pi(n);
        for (int i = \bar{1}; i < n; i++) {
 4
            int g = pi[i-1];
             while (g \& \& s[i] != s[g])
                 g = pi[g-1];
 8
            g += s[i] == s[g];
 9
            pi[i] = g;
10
11
        return pi;
12
13
    vector<int> KMP(string s, string t) {
        vector<int> pi = fail(t);
15
        vector<int> ret;
        for(int i = 0, g = 0; i < s.size(); i++) {</pre>
17
            while (q \&\& s[i] != t[q])
18
                 g = pi[g-1];
19
             g += s[i] == t[g];
20
            if(g == t.size()) { ///occurrence found
21
                 ret.push_back(i-t.size()+1);
                 g = pi[g-1];
```

```
ડ
```

 $\overline{28}$

```
\frac{23}{24} \\ 25
          return ret;
\frac{1}{26}
         Manacher Kactl
     // If the size of palindrome centered at i is x, then d1[i] stores (x
    vector<int> d1(n);
    for (int i = 0, l = 0, r = -1; i < n; i++) {
         int k = (i > r) ? 1 : min(d1[1 + r - i], r - i + 1);
while (0 \le i - k \&\& i + k \le n \&\& s[i - k] == s[i + k]) {
 8
          d1[i] = k--;
         if'(i + k > r) {
              1 = i - k;
               r = i + k;
13
14
15
16
     // If the size of palindrome centered at i is x, then d2[i] stores x/2
17
    vector<int> d2(n);
```

int k = (i > r) ? 0 : min(d2[1 + r - i + 1], r - i + 1);

while $(0 \le i - k - 1 \&\& i + k \le n \&\& s[i - k - 1] == s[i + k])$ {

8.4 Suffix Array Kactl

 $if^{(i+k>r)} \{ 1 = i - k - 1;$

r = i + k;

d2[i] = k--;

for (int i = 0, l = 0, r = -1; i < n; i++) {

```
struct SuffixArray {
         using vi = vector<int>;
         #define rep(i,a,b) for(int i = a; i < b; i++)
         \#define all(x) begin(x), end(x)
 5
             Note this code is considers also the empty suffix
             so hear sa[0] = n and sa[1] is the smallest non empty suffix
             and sa[n] is the largest non empty suffix
             also LCP[i] = LCP(sa[i-1], sa[i]), meanining LCP[0] = LCP[1] =
10
             if you want to get LCP(i..j) you need to build a mapping
                  het ween
11
             sa[i] and i, and build a min sparse table to calculate the
                 minimum
             note that this minimum should consider sa[i+1...j] since you
                  don't want
             to consider LCP(sa[i], sa[i-1])
             you should also print the suffix array and lcp at the
                 beginning of the contest
             to clarify this stuff
17
18
        vi sa, lcp;
19
        SuffixArray(string& s, int lim=256) { // or basic_string<int>
^{20}_{21}
             int n = sz(s) + 1, k = 0, a, b;
             vi x(all(s)+1), y(n), ws(max(n, lim)), rank(n);
22
23
24
             sa = lcp = y, iota(all(sa), 0);

for (int j = 0, p = 0; p < n; j = max(1, j * 2), lim = p) {
                 p = j, iota(all(y), n - j);
25
26
27
                 rep(i,0,n) if (sa[i] >= i) y[p++] = sa[i] - i;
                 fill(all(ws), 0);
                 rep(i, 0, n) ws[x[i]] ++;
28
                 rep(i, 1, lim) ws[i] += ws[i - 1];
                 for (int i = n; i--;) sa[--ws[x[y[i]]]] = y[i];
\frac{29}{30}
                 swap(x, y), p = 1, x[sa[0]] = 0;
                 rep(i,1,n) a = sa[i-1], b = sa[i], x[b] =
\begin{array}{c} 31 \\ 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 37 \end{array}
                      (y[a] == y[b] \&\& y[a + j] == y[b + j]) ? p - 1 : p++;
             rep(i,1,n) rank[sa[i]] = i;
             for (int i = 0, j; i < n - 1; lcp[rank[i++]] = k)
                 for (k \& \& k--, j = sa[rank[i] - 1];
                          s[i + k] == s[j + k]; k++);
    };
```

8.5 Suffix Automaton Mostafa

```
struct SA {
        struct node
             int to [26];
            int link, len, co = 0;
                memset(to, 0, sizeof to);
                 co = 0, link = 0, len = 0;
10
        int last, sz;
\overline{13}
        vector<node> v;
14
15
16
             v = vector<node>(1);
17
             last = 0, sz = 1;
        void add_letter(int c) {
            int p = last;
             last = sz++;
             v.push_back({});
            v[last].len = v[p].len + 1;
             v[last].co = 1;
             for (; v[p].to[c] == 0; p = v[p].link)
26
27
                v[p].to[c] = last;
28
             if (v[p].to[c] == last) {
29
                 v[last].link = 0;
30
                 return;
31
32
            int q = v[p].to[c];
33
             if (v[q].len == v[p].len + 1) {
                 v[last].link = q;
35
                 return;
36
37
            int cl = sz++;
38
            v.push back(v[q]);
39
             v.back().co = 0;
40
             v.back().len = v[p].len + 1;
             v[last].link = v[q].link = cl;
4\overline{3}
             for (; v[p].to[c] == q; p = v[p].link)
44
                 v[p].to[c] = cl;
45
\frac{46}{47}
        void build_co() {
             priority_queue<pair<int, int>> q;
48
             for (int i = sz - 1; i > 0; i--)
49
                 q.push({v[i].len, i});
50
51
             while (q.size()) {
                 int i = q.top().second;
52
53
                 q.pop();
54
                 v[v[i].link].co += v[i].co;
55
56
   };
```

8.6 Zalgo Anany

8.7 lexicographically smallest rotation of a string

```
int minRotation(string s) {
    int a=0, N=sz(s); s += s;
    rep(b,0,N) rep(k,0,N) {
        if (a+k == b || s[a+k] < s[b+k]) {b += max(0, k-1); break;}
        if (s[a+k] > s[b+k]) { a = b; break;}
}

return a;
}
```

9 Trees

9.1 Centroid Decomposition

```
Properties:
             1. consider path(a,b) can be decomposed to path(a,lca(a,b))
                  and path(b, lca(a,b))
             where lca(a,b) is the lca on the centroid tree
             2. Each one of the n^2 paths is the concatenation of two paths
                   in a set of O(n lg(n))
             paths from a node to all its ancestors in the centroid
                  decomposition.
              3. Ancestor of a node in the original tree is either an
                  ancestor in the CD tree or
             a descendadnt
    vector<int> adj[N]; //adjacency list of original graph
    int n;
    int sz[N];
    bool used[N]:
    int centPar[N]; //parent in centroid
15
    void init(int node, int par) { ///initialize size
16
         sz[node] = 1;
\tilde{17}
         for(auto p : adj[node])
18
             if(p != par && !used[p]) {
19
                  init(p, node);
20
21
22
23
24
25
26
27
28
29
30
31
                  sz[node] += sz[p];
    int centroid(int node, int par, int limit) { ///get centroid
         for(int p : adj[node])
             if(!used[p] && p != par && sz[p] * 2 > limit)
             return centroid(p, node, limit);
         return node;
    int decompose(int node)
         init (node, node);
                               ///calculate size
         int c = centroid(node, node, sz[node]); //get centroid
\frac{32}{33}
         used[c] = true;
         for(auto p : adj[c])if(!used[p.F]) {
                                                      ///initialize parent for
             others and decompose
34
35
36
37
38
39
             centPar[decompose(p.F)] = c;
        return c;
    void update(int node, int distance, int col) {
         int centroid = node;
\frac{40}{41}
         while(centroid) {
             centroid = centPar[centroid];
45
    int query(int node) {
\begin{array}{c} 46 \\ 47 \\ 48 \\ 49 \\ 51 \\ 52 \\ 53 \\ 55 \\ \end{array}
        int ans = 0;
        int centroid = node;
        while(centroid) {
             ///solve
             centroid = centPar[centroid];
         return ans;
56
```

9.2 Dsu On Trees

```
1 const int N = 1e5 + 9;
2 vector<int> adj[N];
3 int bigChild[N], sz[N];
```

```
void dfs(int node, int par)
        for(auto v : adj[node]) if(v != par){
            dfs(v, node);
            sz[node] += sz[v];
            if(!bigChild[node] || sz[v] > sz[bigChild[node]]) {
                bigChild[node] = v;
10
11
12
   void add(int node, int par, int bigChild, int delta) {
15
        ///modify node to data structure
16
17
        for(auto v : adj[node])
18
        if(v != par && v != bigChild)
19
            add(v, node, bigChild, delta);
   void dfs2(int node, int par, bool keep) {
23
        for(auto v : adj[node])if(v != par && v != bigChild[node]) {
            dfs2(v, node, 0);
        if(bigChild[node]) {
\overline{27}
            dfs2(bigChild[node], node, true);
29
        add(node, par, bigChild[node], 1);
        ///process queries
31
        if(!keep) {
            add(node, par, -1, -1);
33
34
```

9.3 Heavy Light Decomposition (Along with Euler Tour)

```
Notes:
             1. 0-based
             2. solve function iterates over segments and handles them
             if you're gonna use it make sure you know what you're doing
             3. to update/query segment in[node], out[node]
             4. to update/query chain in[nxt[node]], in[node]
            nxt[node]: is the head of the chain so to go to the next chain
                  node = par[nxt[node]]
   int sz[mxN], nxt[mxN];
    int in[N], out[N], rin[N];
    vector<int> g[mxN];
13
   int par[mxN];
15
    void dfs_sz(int v = 0, int p = -1) {
        sz[v] = 1;
par[v] = p;
17
        for (auto &u : g[v]) {
19
             if (u == p) {
20
                 swap(u, g[v].back());
             if(u == p) continue;
            dfs_sz(u,v);
\frac{24}{25}
             sz[v] += sz[u];
             if (sz[u] > sz[g[v][0]])
26
                 swap(u, q[v][0]);
27
28
        if(v != 0)
\overline{29}
            g[v].pop_back();
\bar{30}
    void dfs_hld(int v = 0) {
        in[v] = t++;
         rin[in[v]] = v;
        for (auto u : q[v])
            nxt[u] = (u == g[v][0] ? nxt[v] : u);
37
            dfs_hld(u);
38
        out[v] = t;
40
43
   bool isChild(int p, int u) {
      return in[p] <= in[u] && out[u] <= out[p];</pre>
45
    int solve(int u,int v) {
```

```
J
```

```
47
         vector<pair<int,int> > sequ;
48
         vector<pair<int,int> > seqv;
49
         if(isChild(u,v)){
50
51
52
53
54
55
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57
58
59
           while(nxt[u] != nxt[v]){
              seqv.push_back(make_pair(in[nxt[v]], in[v]));
              v = par[nxt[v]];
           segv.push_back({in[u], in[v]});
           else if(isChild(v,u)){
           while(nxt[u] != nxt[v]){
           segu.push_back(make_pair(in[nxt[u]], in[u]));
           u = par[nxt[u]];
           segu.push_back({in[v], in[u]});
61
62
63
       } else
           while (u != v) {
              if(nxt[u] == nxt[v]) {
64
                if(in[u] < in[v]) segv.push_back({in[u],in[v]}), R.push_back</pre>
                    (\{u+1,v+1\});
                else sequ.push_back({in[v],in[u]}), L.push_back({v+1,u+1});
                break;
68
               else if(in[u] > in[v]) {
                segu.push_back({in[nxt[u]],in[u]}), L.push_back({nxt[u]+1, u
                u = par[nxt[u]];
71
               else {
                segv.push_back({in[nxt[v]],in[v]}), R.push_back({nxt[v]+1, v
73
74
75
76
77
78
79
80
81
82
83
84
85
86
                v = par[nxt[v]];
         reverse (seqv.begin(), seqv.end());
         int res = 0, state = 0;
         for(auto p : sequ) {
              qry(1,1,0,n-1,p.first,p.second,state,res);
         for(auto p : seqv) {
              qry(0,1,0,n-1,p.first,p.second,state,res);
         return res;
```

9.4 Mo on Trees

10 Numerical

10.1 Lagrange Polynomial

```
class LagrangePoly {
    public:
        LagrangePoly(std::vector<long long> _a) {
             //f(i) = \_a[i]
             //interpola o vetor em um polinomio de grau y.size() - 1
             v = a:
             den.resize(y.size());
             int n = (int) y.size();
             for (int i = 0; i < n; i++) {
                 y[i] = (y[i] % MOD + MOD) % MOD;
                 den[i] = ifat[n - i - 1] * ifat[i] % MOD;
12
13
14
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16
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22
23
24
                 if((n - i - 1) % 2 == 1)
                      den[i] = (MOD - den[i]) % MOD;
        long long getVal(long long x) {
             int n = (int) y.size();
             x = (x % MOD + MOD) % MOD;
                 //return y[(int) x];
             std::vector<long long> 1, r;
```

```
\frac{25}{26}
              1.resize(n);
             1[0] = 1;
              for (int i = 1; i < n; i++) {
                  l[i] = l[i - 1] * (x - (i - 1) + MOD) % MOD;
30
              r.resize(n);
              r[n - 1] = 1;
32
              for (int i = n - 2; i >= 0; i--) {
33
                  r[i] = r[i + 1] * (x - (i + 1) + MOD) % MOD;
34
             long long ans = 0;
for(int i = 0; i < n; i++) {</pre>
35
36
37
                  long long coef = l[i] * r[i] % MOD;
38
                  ans = (ans + coef * y[i] % MOD * den[i]) % MOD;
39
40
              return ans;
    private:
         std::vector<long long> y, den;
```

11 Guide

11.1 Notes

- Don't forget to solve the problem in reverse (i.e deleting-¿adding or adding-¿deleting, ...etc)
- Max flow is just choosing the maximum number of paths between source and sink
- If you have a problem that tells you choose a[i] or b[i] (or a range) choose one of them initially and play a take or leave on the other
- If the problem tells you to do something cyclic solving it for x + x
- Problems that are close to NP problems sometimes have greedy solutions for large input i.e n ξ =20-30
- Check datatypes (if you are getting WA or TLE or RTE)
- in case of merging between sets try bitsets (i.e i + j or sth)
- If you have a TLE soln using bitset might help
- If everything else fails think Brute force or randomization
- If you have a solution and you think it's wrong write it instead of doing nothing

11.2 Assignment Problems

- If you see a problem that tells you out of N choose K that has some property (think flows or aliens trick)
- If you see a problem that tells for some X choose a Y (think flows)
- If the problem tells you to choose a Y from L-¿R (think range flow i.e putting edges between the same layer)

11.3 XOR problems

- If the problem tells your something about choosing an XOR of a subset (think FWHT or XOR-basis)
- If the problem tells you about getting XOR of a tree path let a[i] = XOR tree from root to i and solve this as an array
- If the problem tells you range XOR sth it's better to have prefix XOR and make it pairs XOR.

11.4 Subset Problems

• Problems that tells you what is the number of ways to choose X out of N that has some property (think convolution)

11.5 Decompositions

- If a problem is a asking you to calculate the answer after K steps you can calculate the answer for K
- If the nubmer of queries is significintly larger than updates or vice versa you can use square root Decompositions to give advantage to one over the other

11.6 Strings

- Longest Common Substring is easier with suffix automaton
- Problems that tell you cound stuff that appears X times or count appearnces (Use suffixr links)
- Problems that tell you find the largest substring with some property (Use Suffix links)
- Remember suffix links are the same as a ho corasic failure links (you can memoize them with dp)
- Problems that ask you to get the k-th string (can be either suffix automaton or array)
- Longest Common Prefix is mostly a (suffix automaton-array) thing
- try thinking bitsets

11.7 Trees

- For problems that ask you to count stuff in a substree think (Euler Tour with RQ Small to Large DSU on Trees PersistentSegTree)
- For Path Problems think (Centroid Decomposition HLD)
- For a path think (HLD + Euler Tour)
- Note that the farthest node to any node in the tree is one of the two diameter heads
- In case of asking F(node, x) for each node it's probably DP on Trees

11.8 Flows

- If you want to make a K-covering instead of consdiring lit edges consider non-lit edges
- To get mincost while mainting a flow network (note that flows are batched together according to cost)
- If the problem asks you to choose some stuff the minimizes use Min Cut (If maximizes sum up stuff and subtract min cut)

11.9 Geometry

- In case of a set of points try scaling and translation
- \bullet Lattice points on line: $\gcd(dx,dy)\,+\,1$
- Pick's theorem: $A = I + \frac{B}{2} 1$
- sine rule: $\frac{A}{sin(a)} = \frac{B}{sin(b)} = \frac{C}{sin(c)}$
- cosine rule: $C^2 = A^2 + B^2 2AB \times cos(c)$
- Dot product = $|A||B| \times cos(a)$
- Cross product = $|A||B| \times sin(a)$
- • Rotation around axis: $R = (cos(a) \times Id + sin(a) \times crossU + (1 - cos(a)) \times outerU)$
- Angle of regular polygon = $\frac{180 \times (n-2)}{n}$
- # Diagonals of regular polygon = $\frac{n(n-3)}{n}$
- Triangulation of n-gon = Catalan (n-2)

11.10 Area

- triangle = $\frac{B \times H}{2}$
- triangle = $\sqrt{(S \times (S A) \times (S B) \times (S C))}$, S = PERIMETER/2
- triangle = $r \times S$, r = radius of inscribed circle
- circle = $R^2 \times \pi$
- ellipse = $\pi \times r_1 \times r_2$
- sector = $\frac{(r^2 \times a)}{2}$
- circular cap = $\frac{R^2 \times (a sin(a))}{2}$
- trapzoid = $\frac{(B1+B2)}{2} \times H$
- prsim = perimeter(B)L + 2area(B)
- sphere = $4\pi r^2$

11.11 Volume

- Right circular cylinder = $\pi r^2 h$
- Pyramid = $\frac{Bh}{3}$
- Right circular cone = $\frac{\pi r^2 h}{3}$
- Sphere = $\frac{4}{3}\pi r^2 h$
- Sphere sector= $\frac{2}{3}\pi r^2 h = \frac{2}{3}\pi r^3 (1 \cos(a))$
- Sphere cap = $\frac{\pi h^2(3r-h)}{3}$

11.12 Combinatorics

- Cayley formula: number of forest with k trees where first k nodes belongs to different trees = kn^{n-k-1} . Multinomial theorem for trees of given degree sequence $\binom{n}{d_t}$
- Prufer sequence (M5da calls it parent array)
- K-Cyclic permutation = $\binom{n}{k} \times (k-1)!$
- Stirling numbers $S(n,k) = k \times S(n-1,k) + S(n,k-1)$ number of way to partition n in k sets.

- Bell number $B_n = \sum_{1}^{n} (n-1, k) B_k$
- # ways to make a graph with k components connected $n^{k-2} \times \prod_{i=1}^k s_i$
- Arithmetic-geometric-progression $S_n = \frac{A_1 \times G_1 A_{n+1} \times G_{n+1}}{1-r} + \frac{dr}{(1-r)^2} \times (G_1 G_{n+1})$

11.13 Graph Theory

- Graph realization problem: sorted decreasing degrees: $\sum_{1}^{k} d_i = k(k-1) + sum_(k+1)^n \min(d_i, k)$ (first k form clique and all other nodes are connected to them).
- Euler formula: v + f = e + c + 1
- # perfect matching in bipartite graph, DP[S][j] = DP[S][j-1] + DP[S/v][j-1] for all v connected to the j node.

11.14 Max flow with lower bound

- feasible flow in a network with both upper and lower capacity constraints, no source or sink: capacities are changed to upper bound lower bound. Add a new source and a sink. let M[v] = (sum of lower bounds of ingoing edges to v) (sum of lower bounds of outgoing edges from v). For all v, if M[v];0 then add edge (S,v) with capacity M, otherwise add (v,T) with capacity -M. If all outgoing edges from S are full, then a feasible flow exists, it is the flow plus the original lower bounds.
- maximum flow in a network with both upper and lower capacity constraints, with source s and sink t: add edge (t,s) with capacity infinity. Binary search for the lower bound, check whether a feasible exists for a network WITH-OUT source or sink (B).

11.15 Joseph problem

$$g(n,k) = \begin{cases} 0 & \text{if } n = 1\\ (g(n-1,k)+k) \bmod n & \text{if } 1 < n < k\\ \left\lfloor \frac{k((g(n',k)-n \bmod k) \bmod n')}{k-1} \right\rfloor \text{ where } n' = n - \left\lfloor \frac{n}{k} \right\rfloor & \text{if } k \le n \end{cases}$$