

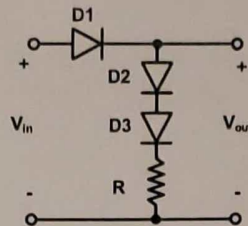
## ECE 310 – Microelectronics I

## Homework #3

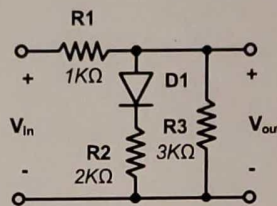
Fall 2021

(Due Date: 10/01/2021, 8.30am)

1. (20pts) For the circuit shown, where  $I_S = 2 \times 10^{-12}$  (A) for the diodes and  $R = 10 \text{ K}\Omega$ . Calculate  $V_{out}$ , and  $I_R$  for a)  $V_{in} = 3.3 \text{ V}$ , and for b)  $V_{in} = 5 \text{ V}$ . Assume room temperature, and  $V_T = 26 \text{ mV}$ .

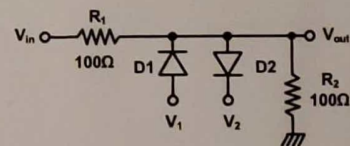


2. (30pts) For the circuit shown below, where  $I_S = 5 \times 10^{-15}$  (A) for the diodes, calculate  $V_{out}$  and  $I_D$  for a)  $V_{in} = 1.5 \text{ V}$  and for b)  $V_{in} = 3 \text{ V}$ . Assume room temperature, and  $V_T = 26 \text{ mV}$ .

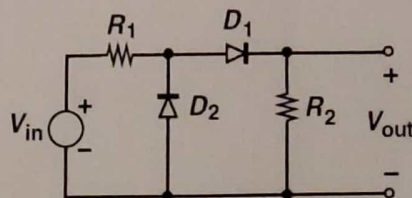


3. (30 pts) For the circuit shown, assume diodes are identical and  $V_{D,ON} = 0.75 \text{ V}$ .

- a. (20pts) Find I/O curve of the circuit for  $V_1 = 0 \text{ V}$ ,  $V_2 = 1 \text{ V}$   
 b. (10pts) Find  $V_1$  and  $V_2$  voltages that allow circuit to pass only input signals between 0 and 3V and draw the new I/O curve.

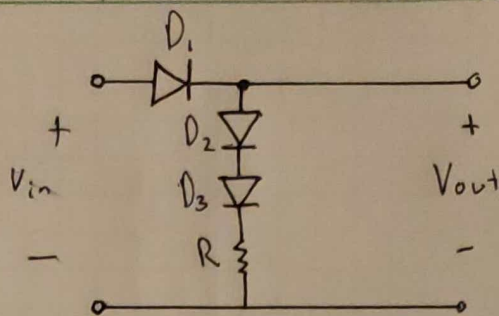


4. (30pts) Use  $R_1 = 500 \Omega$ , and  $R_2 = 1 \text{ k}\Omega$  for the circuit shown below. a) Use SPICE (Cadence) simulator to plot the input/output characteristic of the circuit for  $-5 \text{ V} < V_{in} < +5 \text{ V}$ . b) Also, plot the current flowing through  $R_1$  as a function of  $V_{in}$ . c) Explain the function of the circuit based on your simulations. Use 1N4002 diode model (one you use in ece311 labs) for your simulations.



1

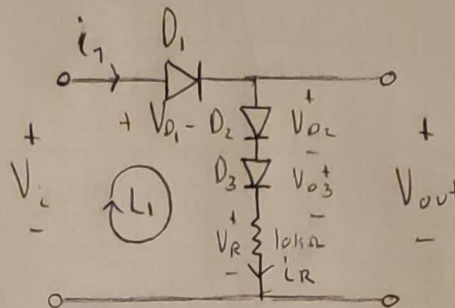
1 Situation: For the given circuit,  $I_s = 2 \times 10^{-12}$  (A) for the diodes, and  $R = 10k\Omega$ . Calculate  $V_{out}$  and  $I_R$  for a.)  $V_{in} = 3.3V$ , and b.)  $V_{in} = 5V$ . Assume room temperature, and  $V_T = 26mV$ .



2 Goal: To calculate the output voltage and Resistor current  $I_R$  given  $V_{in} = 3.3V$  and  $V_{in} = 5V$  at room temperature with a resistor value  $R = 10k$  for the above circuit.

3 Plan: To use KVL along with known equations for diode current and voltage to evaluate the output voltage for the two given input voltages.

4 Solution: Redraw



Observe:  $i_1 = i_R$

$$V_{D1} = V_{D2} = V_{D3}$$

\* Same  $I_s$

Given :  $I_s = 2 \times 10^{-12}$   $V_T = 26mV$   
 $R = 10000 \Omega$

KVL on  $L_1$ :  $V_i - V_{D1} - V_{D2} - V_{D3} - V_R = 0$

$$V_i - 3V_D - 10000 i_R = 0 \quad (1) \quad * V_R \text{ Ohm's law}$$

Known Eqn:  $V_{D1} = V_T \ln\left(\frac{i_R}{I_s}\right)$

$$V_{out} = 26 \times 10^{-3} \ln\left(\frac{i_R}{2 \times 10^{-12}}\right) \quad (2)$$

$$(2) \rightarrow (1) \quad V_i - 3\left(26 \times 10^{-3} \ln\left(\frac{i_R}{2 \times 10^{-12}}\right)\right) - 10000 i_R = 0 \quad (3)$$

a.)  $V_{in} = 3.3V \Rightarrow 3.3 - 3\left(26 \times 10^{-3} \ln\left(\frac{i_R}{2 \times 10^{-12}}\right)\right) - 10000 i_R = 0$

\* Solve 1 eqn for 1 unknown with calculator

**1** (continued)

for  $V_{in} = 3.3V$ , Solving eqn (3) for  $i_R$  yields:

$$i_R = 0.000187 A$$

$$i_R = 0.187 \text{ mA}$$

$$V_{out} |_{V_{in}=3.3V}$$

KVL Right Side:

$$V_{out} = V_{O3} + V_{O2} + V_R$$

$$V_{out} = 2V_O + 10000 i_R$$

$$V_{out} = 2V_T \ln\left(\frac{i_R}{i_{S1}}\right) + 10000 i_R \quad (4)$$

Plug in  $i_R = 0.12 \text{ nA}$

$$V_{out} = 2\left(26 \times 10^{-3} \ln\left(\frac{0.187 \times 10^{-3}}{2 \times 10^{-12}}\right)\right) + 10000(0.187 \times 10^{-3})$$

$$V_{out} = 2.824 V$$

b.)  $V_{in} = 5V$

Solve  $i_R |_{V_{in}=5V}$ .

Solve eqn (3) for  $i_R$  with  $V_{in} = 5V$ .

$$\Rightarrow 5 - 3\left(26 \times 10^{-3} \ln\left(\frac{i_R}{2 \times 10^{-12}}\right)\right) - 10000 i_R = 0$$

$$\therefore i_R = 0.352 \text{ mA}$$

Solve  $V_{out} |_{V_{in}=5V}$

Plug  $i_R = 0.352 \text{ mA}$  into eqn (4):

$$V_{out} = 2\left(26 \times 10^{-3} \ln\left(\frac{0.352 \times 10^{-3}}{2 \times 10^{-12}}\right)\right) - 10000(0.352 \times 10^{-3})$$

$$V_{out} = 4.507 V$$



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 (continued)Sanity Check:

Check KVL's with calculated values

a.)  $V_o = V_i - V_{out}$

$V_o = 3.3 - 2.824$

$V_o = 0.46 \text{ V}$

$V_R = 10000 i_R$

$= 10000 (0.187 \times 10^{-3})$

$V_R = 1.87 \text{ V}$

KVL on  $L_1$ :  $V_i - 3V_o - V_R = 0$

$$3.3 - 3(0.46) - 1.87 \approx 0$$

$$0.05 \approx 0$$

 $\therefore$  Reasonable answers for  $i_R$ ,  $V_{out}$  with slight error.

b.)  $V_o = 5 - 4.507$

$V_o = 0.493 \text{ V}$

$V_R = 10000 (0.352 \times 10^{-3})$

$V_R = 3.52 \text{ V}$

KVL on  $L_1$ :  $V_i - 3V_o - V_R = 0$

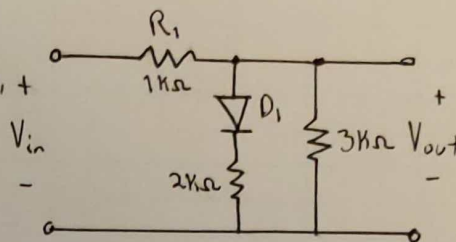
$$5 - 3(0.493) - 3.52 = 0$$

$$0.001 \approx 0$$

 $\therefore$  Reasonable answers for  $i_R$ ,  $V_{out}$  with very small error

2.

1 Situation For the given circuit, +  
 $I_s = 5 \times 10^{-15} \text{ (A)}$ . For the diode,  
 Calculate  $V_{out}$  and  $I_D$  for;  
 a.)  $V_{in} = 1.5 \text{ V}$  and for  
 b.)  $V_{in} = 3 \text{ V}$ . Assume Room  
 temperature and  $V_T = 26 \text{ mV}$



2 Goal: To Calculate the output Voltage,  $V_{out}$ , and Diode current  $I_D$  for  $V_{in} = 1.5 \text{ V}$  and  $V_{in} = 3 \text{ V}$  at room temperature.

3 Plan To Use Fundamental circuit analysis techniques along with known equations for diode current and Voltage to solve for  $V_{out}$  and  $I_D$  for the given parameters for part a.) and b.)

4 Solution

Part a.)  $V_{in} = 1.5 \text{ V}$

Given:  $I_s = 5 \times 10^{-15} \text{ (A)}$   
 $V_T = 26 \text{ mV}$

Assume:  $n = 1$

Known:  $V_D = V_T \ln \left( \frac{i_D}{I_s} \right)$

$$I_D = I_s \exp \left( \frac{V_D}{n V_T} \right)$$

Nodal Analysis:

$$i_1 = i_D + i_3$$

$$\frac{(1.5 - V_{out})}{1000} = i_D \exp \left( \frac{V_D}{V_T} \right) + \frac{V_{out}}{3000}$$

$$\frac{(1.5 - V_{out})}{10000} = 5 \times 10^{-15} \exp \left( \frac{V_D}{26 \times 10^{-3}} \right) + \frac{V_{out}}{3000} \quad (1)$$

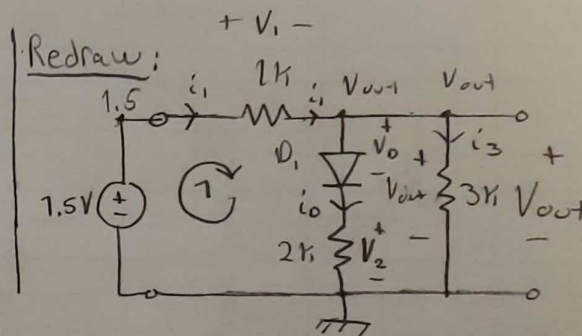
KVL Right Loop:  $V_{out} - V_D - V_2 = 0$

$$V_{out} - V_D - 2000 i_D = 0 \quad \because \text{Ohm's law } R_{2k}$$

$$V_{out} - V_D - 2000 \left( 5 \times 10^{-15} \exp \left( \frac{V_D}{26 \times 10^{-3}} \right) \right) = 0 \quad (2)$$

\* 2 eqn's (1) and (2) with 2 unknowns  $V_{out}$ ,  $V_D$

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2. (continued)

Part a.) (continued)

Solve eqn's ① and ② with calculator yields:

$$V_{out} = 0.991 \text{ V}$$

$$V_0 = 0.6319 \text{ V}$$

Plug  $V_0 \rightarrow I_D$  eqn:

$$I_D = 5 \times 10^{-15} \exp\left(\frac{0.6319}{26 \times 10^{-3}}\right)$$

$$I_D = 0.179 \text{ mA}$$

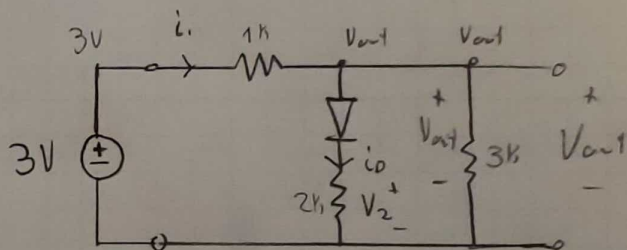
 $V_{out}, I_D \mid V_{in} = 1.5 \text{ V} :$ 

$$V_{out} = 0.991 \text{ V}$$

$$I_D = 0.179 \text{ mA}$$

Part b.)

New Circuit:

Solve eqn's ① and ② for  $V_{out}$ ,  $V_0$ . Exchange  $V_{in}$  in eqn ① from  $1.5 \text{ V} \rightarrow 3 \text{ V}$ 

$$\Rightarrow \frac{(3 - V_{out})}{10000} = 5 \times 10^{-15} \exp\left(\frac{V_0}{26 \times 10^{-3}}\right) + \frac{V_{out}}{3000} \quad (1)$$

$$V_{out} - V_0 - 2000 \left( 5 \times 10^{-15} \exp\left(\frac{V_0}{26 \times 10^{-3}}\right) \right) = 0 \quad (2)$$

$$\text{yields: } V_{out} = 1.817 \text{ V}$$

$$V_0 = 0.6623 \text{ V}$$

$$I_D = 5 \times 10^{-15} \left( \exp\left(\frac{0.6623}{26 \times 10^{-3}}\right) \right)$$

$$I_D = 0.577 \text{ mA}$$

 $V_{out}, I_D \mid V_{in} = 1.5 \text{ V} :$ 

$$V_{out} = 1.817 \text{ V}$$

$$I_D = 0.577 \text{ mA}$$

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**2.** (continued)

Sanity Check:

$$\text{Check } V_D = V_i \ln \left( \frac{I_o}{I_s} \right)$$

For diode in a.) and b.), then KVL Right side.

a.)

$$V_D = 26 \times 10^{-3} \ln \left( \frac{0.179 \times 10^{-3}}{5 \times 10^{-15}} \right)$$

$$V_D = 0.6318 \text{ V}$$

$$V_Z = 2000 (0.179 \times 10^{-3})$$

$$V_Z = 0.358 \text{ V}$$

$$\text{KVL: } V_{out} = V_D + V_Z$$

$$V_{out} = 0.9898$$

$$0.991 \approx 0.9898$$

$\therefore$  Reasonable calculations with low % difference.

b.)

$$V_D = 26 \times 10^{-3} \ln \left( \frac{0.577 \times 10^{-3}}{5 \times 10^{-15}} \right)$$

$$V_D = 0.6623$$

$$V_Z = 2000 (0.577 \times 10^{-3})$$

$$V_Z = 1.154$$

$$V_{out} = V_D + V_Z$$

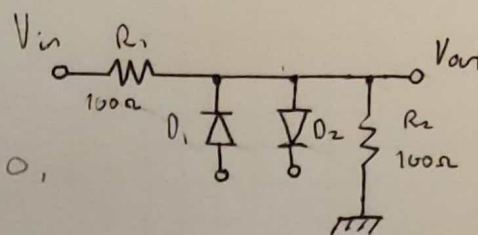
$$V_{out} = 1.8163$$

$$1.817 \approx 1.8163$$

$\therefore$  Reasonable calculations with low % difference.

**3(a)**

1. Situation: For the circuit shown, assume diodes are identical, and  $V_{D,on} = 0.75V$ . 2.) Find the I/O Curve for the circuit for  $V_1 = 0$ ,  $V_2 = 1V$ .

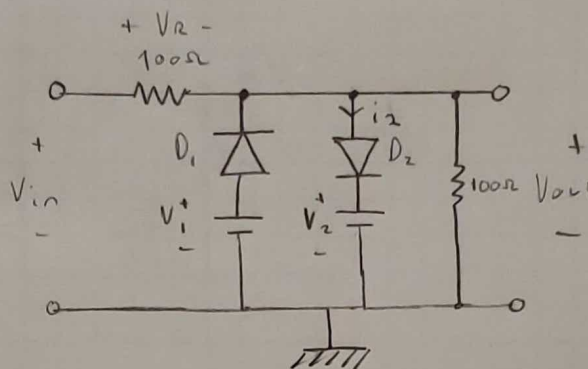


2. Goal: Find the input/output characteristics for the given circuit, then determine the I/O Curve.

3. Plan: Utilize the Constant Voltage Model (CVM) for diodes along with fundamental circuit analysis techniques to determine the input/output behavior.

4. Solution:

Redraw:



State ①  $D_1 = \text{OFF}$ ,  $D_2 = \text{ON}$

The instant  $D_2$  turns on:

$$i_{D2} = 0$$

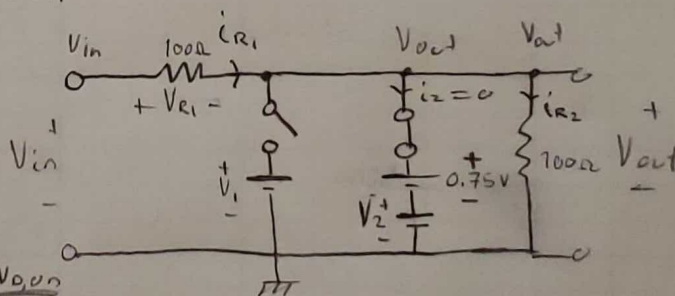
$$V_{D2,on} = 0.75V$$

$$V_2 = 1V$$

$$\therefore i_{R2} = \frac{(1 + 0.75)}{100\Omega} = \frac{1 + V_{D2,on}}{R}$$

$$i_{R2} = \frac{1.75}{100} = i_{R1}$$

$$\therefore i_2 = 0$$



$$\begin{aligned} \therefore V_{in} &= V_{out} + V_{R1} \\ &= i_{R1}(R) + i_{R1}(R) \\ &= 2 \left( \frac{1.75}{100} \right) 100 \end{aligned}$$

$$V_{in} = 3.5 \quad \text{For } D_2 \text{ to turn on}$$

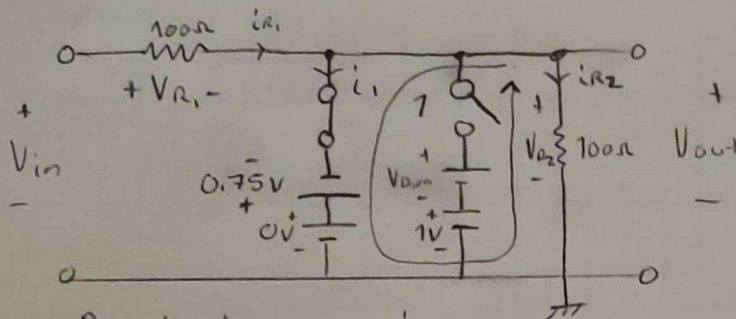


**3(a)** (continued)KVL Outside Loop:  $V_{out} = V_{in} - V_{R_1}$ 

$$V_{out} = 3.5 - 100 \left( \frac{1.75}{100} \right)$$

$$V_{out} = 1.75$$

$\therefore$  For  $V_{in} \geq 3.5V$ :  $D_1 = \text{OFF}$ ,  $D_2 = \text{on}$ ,  
 $V_{out} = 1.75V$  (\*)

State (2)  $D_1 = \text{on}$ ,  $D_2 = \text{OFF}$  $D_1$  just on:  $i_1 = 0$ 

$$V_{out} = V_{R_2} = 0V - 0.75V$$

 $\therefore$  KVL 1

$$V_{out} = -0.75V$$

$$i_{R_1} = i_{R_2} = \frac{-0.75}{100}$$

$$\therefore V_{in} = V_{out} + V_{R_1}$$

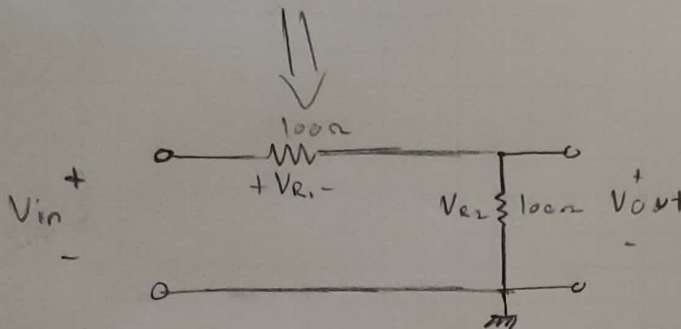
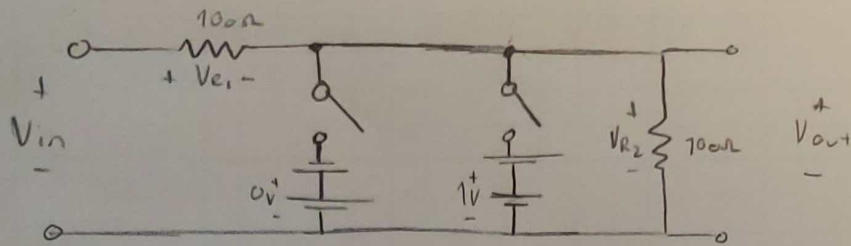
$$= -0.75 + \left( \frac{-0.75}{100} \right) \cdot 100$$

$$V_{in} = -1.50V \text{ for } D_1 \text{ to turn on}$$

$\therefore$  For  $V_{in} \leq -1.50V$ :  $D_1 = \text{on}$ ,  $D_2 = \text{OFF}$  (\*)

$$V_{out} = -0.75V$$

3(w) (continued)

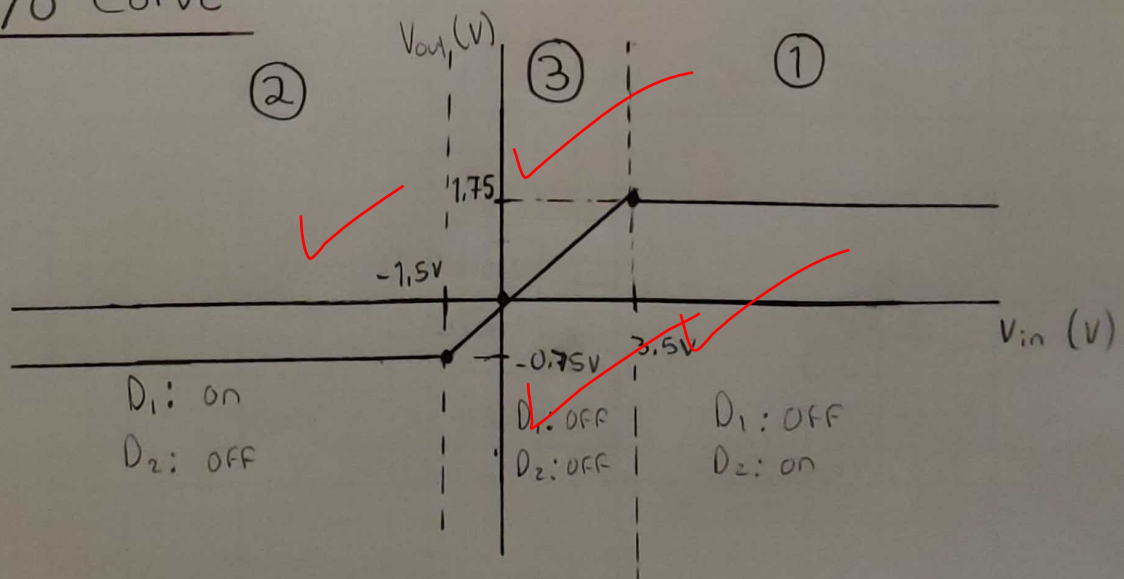
State ③  $D_1 = \text{OFF}$ ,  $D_2 = \text{OFF}$ 

Voltage Division:  $V_{out} = \left( \frac{R_2}{R_1 + R_2} \right) V_{in}$

$$V_{out} = \frac{100}{200} V_{in}$$

$$V_{out} = \frac{1}{2} V_{in}$$

$\therefore$  Slope of  
I/O curve  
from  $[-1.5, 3.5]$

I/O Curve

3(a)

 (continued)5 Sanity Check

The Process was intuitive and the results are reasonable and make sense.



**3(b)**

1 Situation For the same situation outlined in 3(a), Find  $V_1$  and  $V_2$  Voltages that allow the circuit to pass only input signals between 0 and 3V. Then draw the new I/O curve.

2 Goal Find the values for  $V_1$  and  $V_2$  that allow the circuit to pass only input values of 0 to 3V. Then draw the corresponding curve for i/o.

3 Plan:

To use the slope of  $\frac{1}{2}$  from Part 4(a) to calculate which values of  $V_{out}$  shift the input voltage at  $D_1$  and  $D_2$  to 0 and 3V respectively.

4 Solution.

Known from 4(a): Between regions (2) and (1),

$$V_{out} = \frac{1}{2} V_{in}$$

For left bound  $V_1$  on  $D_1$ :

$$V_{out} = -0.75 V = -V_{0, on} \quad \therefore \text{From (2)}$$

We want  $V_{in} = 0$  on left bound:

$$\therefore V_{out}' = \frac{1}{2}(0)$$

$$V_{out}' = 0$$

$$V_{out}' - V_{out} = V_1 \quad * \text{ to correct left bound}$$

$$0 - (-0.75) = V_1$$

$$\therefore \boxed{V_1 = 0.75 V}$$

For Right bound  $V_2$  on  $D_2$ :

$$\therefore V_{out}' = \frac{1}{2}(3)$$

$$V_{out}' = 1.5 V$$

$$V_{out} = 1.75 \quad \therefore \text{From (1)}$$

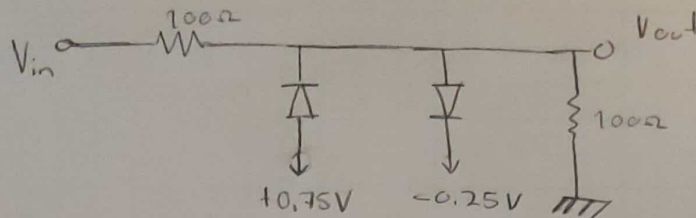
$$V_2 = V_{out}' - V_{out}$$

$$V_2 = 1.5 - 1.75$$

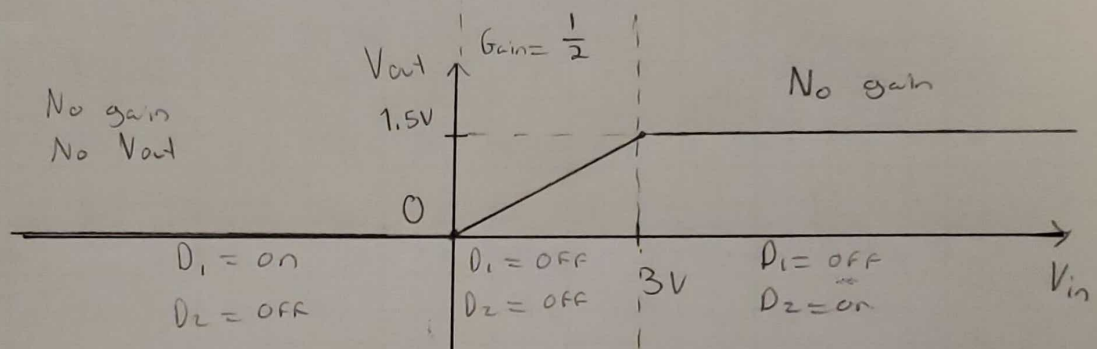
$$\boxed{V_2 = -0.25 V}$$

**3(b)** (continued)

New Circuit

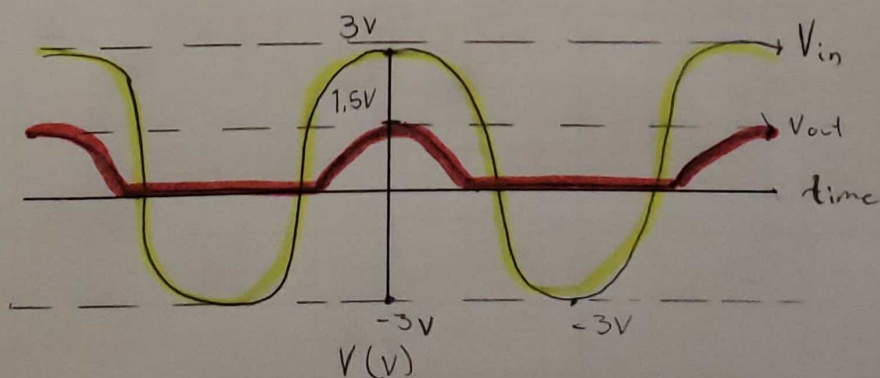


I/O Curve



Sanity Check

Example Input / output vs t



$V_{in}$   
 $V_{out}$

$V_{out}$  only "senses"  $V_{in}$  between  $0 < V_{in} < 3V$   
then  $V_{out}$  can only reach a peak of  
1.5 Volts.

\* For any  $V_{in} > 3V$ ,  $V_{out}$  will flatline  
on the  $V$  vs  $t$  graph

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## 4(a)

**Situation:** Use Cadence simulator to plot the i/o characteristic for the circuit below for  $-5 < V_{in} < 5$ .

Schematic

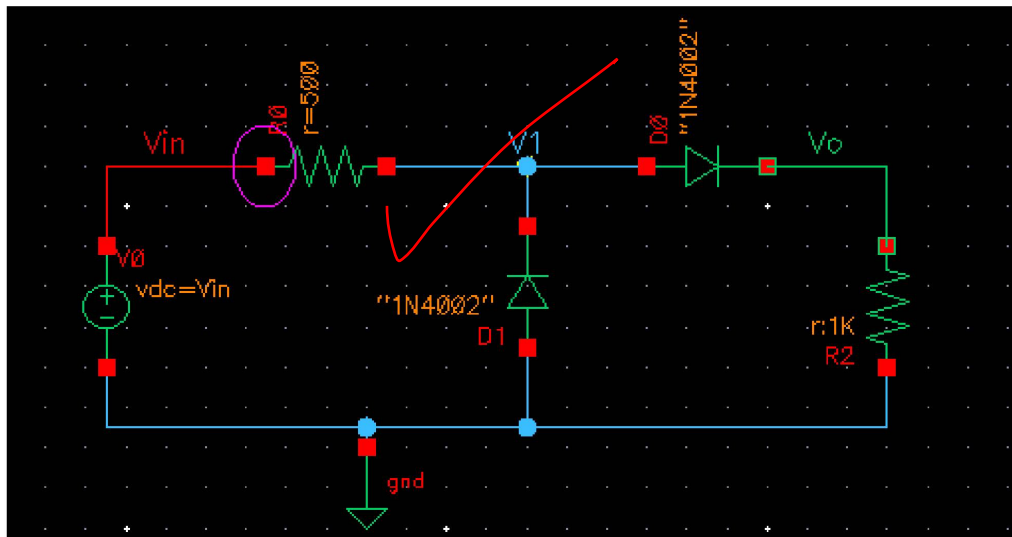


Figure 1: Schematic

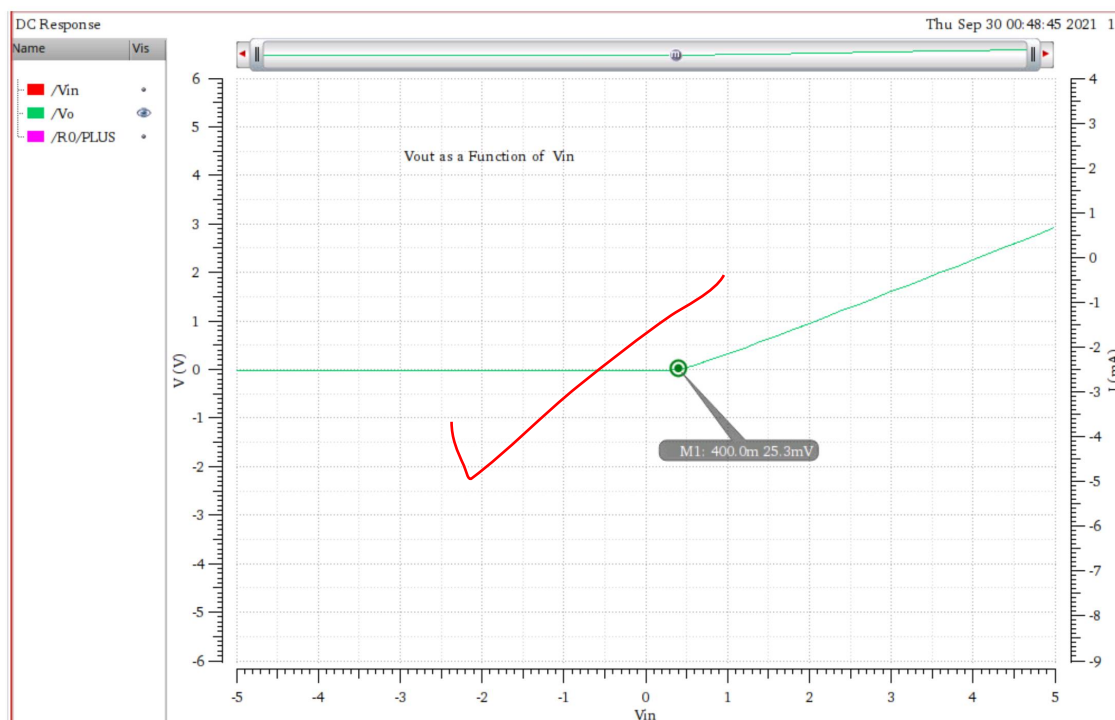
DC Response Simulation Results –  $V_{out}$  vs  $V_{in}$ 

Figure 2



**4(b)**

Situation: Plot the current flowing through  $R_1$  as a function of  $V_{in}$ .

DC Response Simulation Results –  $I_{R1}$  vs  $V_{in}$

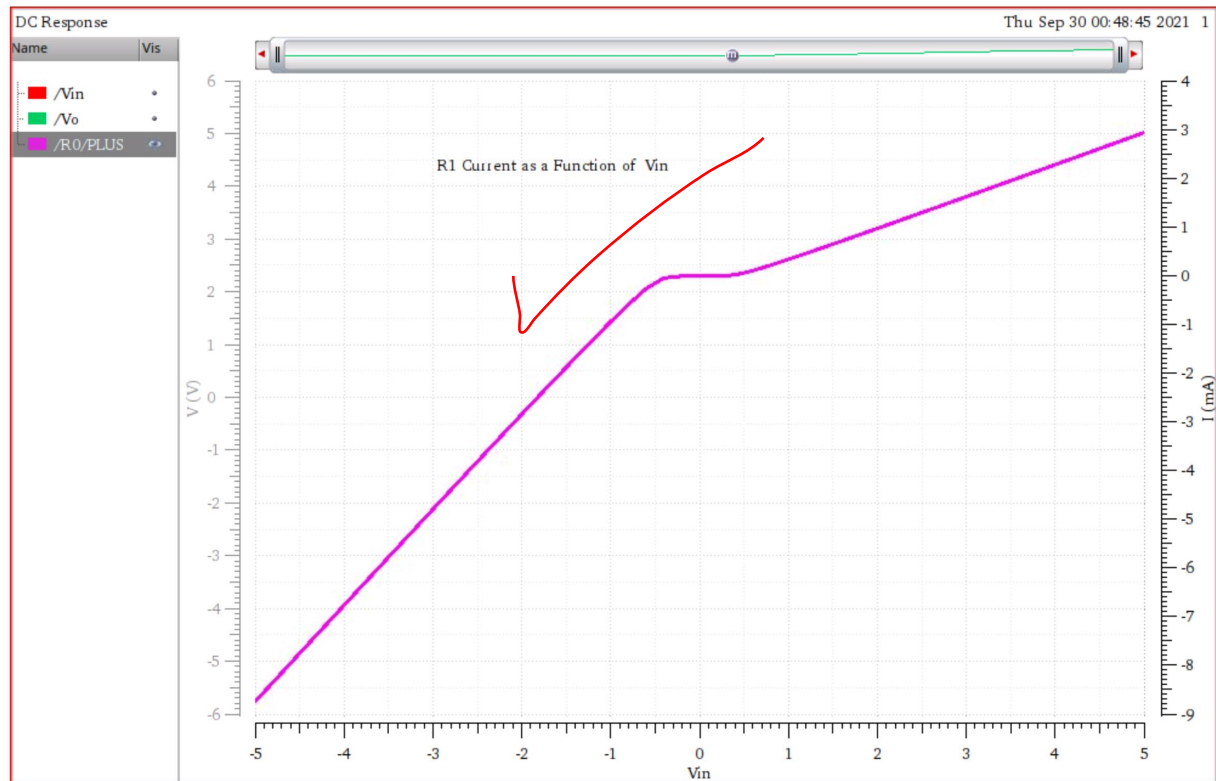


Figure 3

**4(c)**

1 Situation For the circuit illustrated in 4(a) Figure 1, Use the results from the I/O and  $I_R$  vs  $V_{in}$  Simulations to Explain the function of the circuit.

2 Goal: Understand and explain the function of the given circuit.

3 Plan: "

4 Solution:

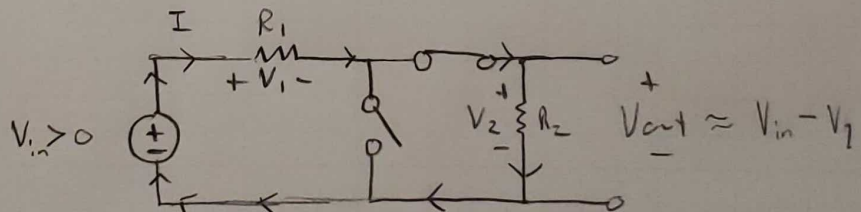
When  $V_{in}$  reaches a value of about 0.4V,  $D_1$  turns on and allows current to flow through to  $V_{out}$  node. This is shown in Figure 1 of 4(a) with a marker where  $V_{out}$  just barely begins to gain voltage. After this value,  $V_{out}$  approaches a linear relationship with  $V_{in}$  including voltage drops across  $R_1$ ,  $R_2$ , and  $D_1$ . This voltage drop results in a slope of less than 1 for  $V_{in} > 0.4$ .

For  $V_{in}$  slightly less than 0 and beyond,  $D_2$  turns on,  $D_1$  is off. Then no voltage is transferred to  $V_{out}$ .

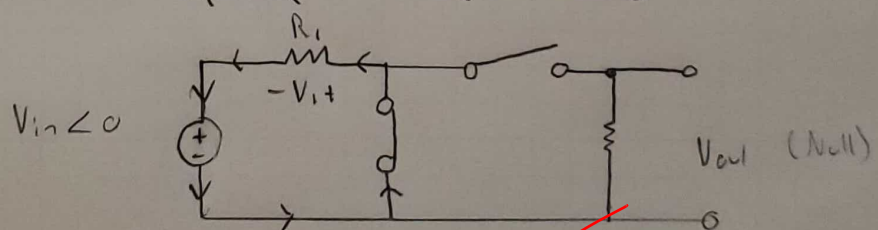
To the left of  $V_{in} = 0$ , the I/O curve has a slope closer to 1, because less voltage drops across resistance. Here, the current through  $R_1$  is negative.

5 Sanity Check. Quasi-Ideal Model to illustrate operation:

$$V_{in} \gtrsim 0.4V$$



$$V_{in} \lesssim 0$$



The circuit works as a half-wave rectifier with voltage drops across  $R_1$  and  $R_2$ .