

Suppose $U = \{b, \{c, 3\}, 3, 4, \{4, 5\}, 5\}$ is a universal set with the following subsets:

$$A = \{\{c, 3\}, 3, \{4, 5\}\}, B = \{b, \{c, 3\}, 4, 5\} \text{ and } C = \{b, 3, 4, 5\}.$$

Which one of the following statements regarding $\mathcal{P}(A)$ is **false**?

- a. The cardinality of $\mathcal{P}(A)$ is 8.
- b. $\{\{\}\} \subset \mathcal{P}(A)$
- c. $\{3\} \in \mathcal{P}(A)$
- d. $\mathcal{P}(A) = \{\{\}, \{\{c, 3\}\}, \{3\}, \{\{4, 5\}\}, \{\{c, 3\}, 3\}, \{\{c, 3\}, \{4, 5\}\}, \{3, \{4, 5\}\}\}$

Question 2 of 10

Suppose $U = \{\{a, b\}, a, c, d, \{a, d\}, e\}$ is a universal set with the following subsets:

$$A = \{\{a, b\}, a, \{a, d\}\}, B = \{a, d, e\} \text{ and } C = \{\{a, b\}, a, d, \{a, d\}, e\}.$$

Which one of the following sets is **not** a subset of $\mathcal{P}(B)$?

- a. $\{\{\}, \{a, d, e\}\}$
- b. $\{a, d\}$
- c. $\{\{a, d\}, \{a, e\}\}$
- d. $\{\{\}\}$

Question 3 of 10

Let $S = \{\{a\}, b, \{a, \{b\}\}, c\}$.

Which one of the following relations on S is a strict partial order?

- a. $\{(\{a\}, b), (b, \{a, \{b\}\}), (c, b)\}$
- b. $\{(\{a\}, b), (c, \{a, \{b\}\}), (b, c)\}$
- c. $\{(c, \{a\}), (b, \{a\}), (\{a, \{b\}\}, \{a\})\}$
- d. $\{(\{a\}, \{a\}), (b, b), (c, c)\}$

Question 4 of 10

Suppose $U = \{b, \{c, 3\}, 3, 4, \{4, 5\}, 5\}$ is a universal set with the following subsets:

$A = \{\{c, 3\}, 3, \{4, 5\}\}$, $B = \{b, \{c, 3\}, 4, 5\}$ and $C = \{b, 3, 4, 5\}$.

Which one of the following sets represents $U - B$?

- a. U
- b. $\{3, \{4, 5\}\}$
- c. $\{b, \{c, 3\}, 4, 5\}$
- d. $(U - A) - C$

Question 5 of 10

Suppose $U = \{b, \{c, 3\}, 3, 4, \{4, 5\}, 5\}$ is a universal set with the following subsets:

$A = \{\{c, 3\}, 3, \{4, 5\}\}$, $B = \{b, \{c, 3\}, 4, 5\}$ and $C = \{b, 3, 4, 5\}$.

Which one of the following sets represents $B \cap C$?

- a. $\{b, 3, 4, 5\}$
- b. $\{b, 4, 5\}$
- c. $\{4, 5\}$
- d. $\{3, \{c, 3\}\}$

Question 6 of 10

Let $C = \{a, b, 1, 2\}$.

Which one of the following alternatives contains a relation on C that satisfies trichotomy?

- a. $\{(a, 2), (1, a), (b, b), (b, 1), (2, b), (2, 1)\}$
- b. $\{(a, b), (a, 2), (2, b), (1, b), (a, 1), (b, a)\}$
- c. $\{(a, a), (a, b), (a, 1), (a, 2), (2, 1), (2, b)\}$
- d. $\{(2, 1), (1, b), (b, a), (b, 2), (a, 2), (1, a)\}$

Question 7 of 10

Let $A = \{1, 2, c, d\}$. Which one of the following relations is NOT a functional relation on A ?

- a. $\{(1, c), (d, d), (2, 1)\}$
- b. $\{(1, 1), (2, 1), (c, 1), (d, 1)\}$
- c. $\{(1, 2), (c, d), (d, c), (1, d)\}$
- d. $\{(d, 1)\}$

Question 8 of 10

Which one of the statements in the following alternatives is equivalent to $(\neg p \rightarrow q) \vee q$?
(*Hint:* simplify the given statement using logical equivalences.)

- a. $\neg p \vee q$
- b. $p \vee q$
- c. $p \vee \neg q$
- d. $\neg p \vee \neg q$

Question 9 of 10

Consider the two statements below:

Statement 1: $\forall x \in \mathbb{Z}, [(3 - 2x \leq 3) \vee (x^2 - 3 \geq 1)]$

Statement 2: $\exists x \in \mathbb{Z}^+, [(4 - x^2 > 1) \wedge (1 - 3x \geq -2)]$

Which one of the following alternatives is true regarding statements 1 and 2?

- a. Statement 1 is false and statement 2 is true.
- b. Statement 1 is true and statement 2 is false.
- c. Both statements 1 and 2 are false.
- d. Both statements 1 and 2 are true.

Question 10 of 10

Consider the statement

If n is even, then $4n^2 + 7n - 1$ is odd.

Which one of the following statements provides the **converse** of the given statement?

- a. If n is odd, then $4n^2 + 7n - 1$ is even.
- b. If $4n^2 + 7n - 1$ is even, then n is odd.
- c. If $4n^2 + 7n - 1$ is odd, then n is even.
- d. If n is even, then $4n^2 + 7n - 1$ is even.