

6. Let g be a function from \mathbb{Z}^+ (the set of positive integers) to \mathbb{Q} (the set of rational numbers) defined by

$$(x, y) \in g \text{ iff } y = 4x - 3/7 (g \subseteq \mathbb{Z}^+ \times \mathbb{Q})$$

and let f be a function on \mathbb{Z}^+ defined by

$$(x, y) \in f \text{ iff } y = 5x^2 + 2x - 3 (f \subseteq \mathbb{Z}^+ \times \mathbb{Z}^+)$$

What is the image of x under $g \circ f$ (ie $g \circ f(x)$)?

$$\begin{aligned} g \circ f &= g(f(x)) \\ &= 4(f(x)) - \frac{3}{7} \\ &= 4(5x^2 + 2x - 3) - \frac{3}{7} \\ &= 20x^2 + 8x - 12 - \frac{3}{7} \\ &= 20x^2 + 8x - 12\frac{3}{7} \end{aligned}$$