

Errata for the HoTT Book, first edition

May 24, 2023

For the benefit of all readers, the available PDF and printed copies of the book are being updated on a rolling basis with minor corrections and clarifications as we receive them. Every copy has a version marker that can be found on the title page and is of the form “first-edition-XX-gYYYYYYY”, where XX is a natural number and YYYYYYY is the git commit hash that uniquely identifies the exact version. Higher values of XX indicate more recent copies.

Below is a list of corrections and clarifications that have been made so far (except for trivial formatting and spacing changes), along with the version marker in which they were first made. This list is current as of May 24, 2023 and version marker “first-edition-1404-g79e6d60”.

While the page numbering may differ between copies with different version markers (and indeed, already differs between the letter/A4 and printed/ebook copies with the same version marker), we promise that the numbering of chapters, sections, theorems, and equations will remain constant, and no new mathematical content will be added, unless and until there is a second edition.

Location	Fixed in	Change
§1.1	182-gb29ea2f	Change notation $a \equiv_A b$ to $a \equiv b$.
§1.1	154-g42698c2	Appendix A. (Neither are used a
§1.1	154-gac9b226	Clarify that algorithmic decidab
§1.3	42-g4bc5cc2	only meta-theoretic.
§§1.3 and 1.4	42-ga34b313	Mention notation $a = b = c = d$
§1.4	165-g0ad2aba	$c = d$, hence $a = d''$, possibly inc
Remark 1.5.1	80-g8f95fa5	Cumulativity means some eleme
§1.5	51-g67e86db	the index i on \mathcal{U}_i is not an interna
		ambiguity must be justified by r
		Explain that we can’t define Fir
		mention them.
		Add swap as another example of
		discuss the use of subscripts and
		dent functions.
		In the discussion of formation r
		type example should be $\prod_{(x:A)} B$
		Better explanation of recursion o
		tified, and how it relates to the u

Location	Fixed in	Change
§1.6	2-gbe277a8	In the types of g and $\text{ind}_{\sum_{(x:A)} B(x)}$, which x should be a .
§1.6	27-gd0bfa0d	At two places in the definition of R , $R(x, \text{pr}_1(g(x)))$.
§1.6	125-g7fdadbf	When substituting $\lambda x. \text{pr}_1(g(x))$ for a , $\text{pr}_1(g(x))$ is well-typed, the left side of the equation should be $\prod_{(x:A)} R(x, \text{pr}_1(g(x)))$, not $\prod_{(x:A)} R(x, \text{pr}_1(g(a)))$.
§1.7 Theorem 1.8.1	30-g264d934 391-g1ce619a	In two displayed equations, $f(\text{inl}(a))$ should be $f(\text{inl}(a))$. This should not be called a “Theorem”. It should be introduced what that means. Instead of “construct an element of...”, it should be “construct an element of...”.
§1.8	125-g433f87e	In the definition of binary product, the types of $\text{pr}_1(p)$ and $\text{pr}_2(p)$ should be A and B , not A and B of arguments to rec_2 and ind_2 .
§1.11	111-g1e868fa	When translating English to type theory, variables that are unnamed in English but must be named in type theory are unnamed in English but must be named in type theory.
§1.12	154-g4ef49f7	Emphasize that path induction, like function induction, defines a <i>specified</i> function.
§1.12	1373-g142de42	In the second proof that based path induction implies function induction, the observation should be an instance of $\text{ind}_{=A}$, not $\text{ind}'_{=A}$.
§1.12	244-gd58529d	In proof that path induction implies function induction, $D(x, y, p)$ should be written $\prod_{(c:C)} D(x, y, p, c)$ if the type of C matches the premise of D .
Remark 1.12.1	563-g3286941	The facts that any $(x, y, p) : \sum_{(y:B)} (x = y) \rightarrow B$ and that any $(y, p) : \sum_{(y:B)} (a = y) \rightarrow B$ can be proven by path induction respectively.
Exercise 1.4	78-gcce4dc0	The second defining equation of c_s should be $c_s(\text{iter}(C, c_0, c_s, n))$.
Exercise 1.4	293-g4663bfe	The defining equations of the recursive function only hold propositionally, and not definitionally. The principle to prove.
Exercise 1.6	229-ged891f3	This exercise requires function extensionality.
Exercise 1.8	450-g7f38c9a	This exercise requires symmetry of equality. Lemmas 2.1.1 and 2.1.2.
Exercise 1.10	110-gfe4641b	To match the usual Ackermann–Péter function, the displayed equation should be $\text{ack}(s, a, b)$.
Chapter 2	239-gaf3d682	In the chapter introduction, clarify the relationship between topics between paths must be encoded as functions.

Location	Fixed in	Change
Lemma 2.1.1	166-g37b78ef	Add remarks before and after the statement and proof should be in the element of some type.
Lemma 2.1.2	374-g0bc0908	In the penultimate display in the proof be simply d .
Lemma 2.1.4	750-g91b7348	In the first proofs of (i)–(iii) $\text{ind}_{=A}(D, d, x, y, p)$.
§2.1	435-gee0b28a	In the third paragraph after Lemma 2.1.4 be $p \cdot \text{refl}_y \equiv p$.
§2.1	165-g18642ca	Mention that the notation $a =$ is a variant, indicate concatenation of a and b .
§2.1	253-gdd47c75	Lemma 2.1.4(iv) justifies writing $\alpha \cdot_r r$.
Theorem 2.1.6	253-gdd47c75	The induction defining $\alpha \cdot_r r$ has $\text{ru}_p^{-1} \cdot \alpha \cdot \text{ru}_q$, with ru_p the right p and ru_q the right q . If p is to be well-typed, we assume $p \equiv \text{ru}_{\text{refl}_a} = \text{refl}_{\text{refl}_a}$ and its dual. Proceed by induction not only on α and β but also on 1 -paths. After the proof, remark that we can construct such operations from ru and refl .
Definition 2.1.8	233-gc3fb777	The three displays should be $:=$ instead of \equiv .
§2.2	336-g8ff8a7f	In the type of ap_f towards the proof of Lemma 2.2.1, $g(x)$ should be $f(y)$.
§2.3	154-g4ef49f7	Emphasize that unlike fibrations, type families come with a <i>specific</i> transport .
§2.3	343-g6efd724	The functions Eq. (2.3.6) and Eq. (2.3.7) are concatenating with $\text{transportconst}_p^B$ (instead of transport) respectively.
Corollary 2.4.4	253-gdd47c75	Canceling $H(x)$ may be done by $\text{isequiv}(f) \rightarrow \text{isequiv}(g)$.
§2.4	1171-gab3c0aa	In the proof that $\text{isequiv}(f) \rightarrow \text{isequiv}(g)$ should be $\gamma(x) := \beta(g(x))^{-1} \cdot h(x)$.
§2.6	74-g9896e32	In the type of $\text{pair}^=$ (just after the proof) the second factor in the domain should be $\text{pair}^=$.
§2.6	895-g96db894	In the displayed equation just below (2.6.1) $q, r, p' \cdot q', r$ should be $\text{pair}^=(p \cdot q, r, p', q' \cdot r)$ should be $\text{pair}^=(p, q \cdot r, p', q' \cdot r)$ (the p and q are missing).
Theorem 2.6.4	349-gc7fd9d8	The path is in $A(w) \times B(w)$, not in $A(w)$.
Theorem 2.6.4	76-ga42354c	The third displayed judgmental equation should be $\text{transport}^B(p, \text{pr}_2 x) \equiv \text{pr}_2 x$.
Theorem 2.7.2	507-g8f10eda	In the proof, the equation $f(g(\text{refl}_{w_1}, \text{refl}_{w_2})) = (\text{refl}_{w_1}, \text{refl}_{w_2})$ should be $f(g(\text{refl}_{w_1}, \text{refl}_{w_2})) = (\text{refl}_{w_1}, \text{refl}_{w_2})$.

Location	Fixed in	Change
§2.9	269-g3880fe2	The paragraph preceding the definition (before Eq. (2.9.5)) misstated the condition. The axiom should read “For any A , B is an equivalence. The display $(A \simeq B)$ can be deduced afterwards, outside the proof. The second half of the proof is more concrete, follows abstractly using the 2-out of 3 property, or more concretely by concatenating paths on the left side and then repeatedly using naturality. The second display after the proof should be $\prod_{(x:A)} (\text{happly}(p)(x) =_{f(x)=g(x)} x)$. The sentence preceding the theorem should be deduced from Lemmas 2.3.10 and 2.11.2, but not by rate path induction. The sentence after the theorem should be refl_c , not refl_c .
Axiom 2.10.3	992-gc4a5314	The right-hand side of the display should be $(\text{apd}_f(p))^{-1} \cdot \text{ap}_{(\text{transport}^B p)}(q) \cdot \text{apd}_g(p)$.
Theorem 2.11.1	310-gd5fa240	In Theorem 2.12.5 and the preceding discussion, the equivalence $(\text{inl}(a) = x) \simeq \text{code}(x)$, the proof should be $\text{encode}(\text{inl}(a), -)$ and $\text{decode}(-, \text{inl}(a))$.
§2.11	236-g32be999	In the two displays after the proof, the first should be $\text{encode}(\text{inl}(a), -)$ and the second should be $\text{decode}(-, \text{inl}(a))$.
Theorem 2.11.3	628-g1bd8602	In the first displayed pair of equations, the first should be $\text{transport}^{\text{SemigroupStr}}(p_1, (m, a))$ and the second should be $m'(e(x_1), e(x_2))$.
Theorem 2.11.3	704-g70c069e	The right hand side of the last display should be $m'(e(x_1), e(x_2))$.
Theorem 2.11.4	364-g3c47534	In the discussion of universal properties, the Σ -types surrounding Eq. (2.15.9) should be Σ -types and “right-to-left” should be switched.
§2.12	101-g645f763	It should be mentioned that Hofmann and Streicher proposed an axiom similar to univalence (but not equivalent to univalence) for a universe U .
§2.12	370-g114db82	The domain of $g : \prod_{(x:A)} A(x)$ should be A .
§2.14.2	261-g4ccda0a	The definition of subset should be $\prod_{(x:A)} (P(x) \rightarrow Q(x))$, not $\forall(x:A). P(x) \rightarrow Q(x)$, the latter notation has not been in the book.
§2.14.2	402-g2297ecb	In the proof, p should be r to make the proof of retraction.
§2.15	305-g64685f1	Should be to show that $\neg\neg A$ satisfies the property of $\ A\ $ but with only a proposition A .
Chapter 2 Notes	379-ga57eab2	At the end of the proof, Lemma 3.11.7 should be used as the reason why $\sum_{(g:A \rightarrow A)} (g = \text{id}_A)$ is nonempty.
Eq. (3.2.1)	1193-g54b20e3	
§3.5	86-g39feab1	
Lemma 3.11.7	95-gce0131f	
Exercise 3.14	1162-ga97cb70	
Lemma 4.1.1	87-g693e9b9	

Location	Fixed in	Change
Theorem 4.2.3	275-g8ea9f71	In the proof, the path concatenations σ and τ were written in reverse order.
Theorem 4.2.3	1043-gcfce4d7	In the proof, the type of τ was $\epsilon(f(g(f(a))))^{-1} \cdot (f(\eta(g(f(a))))$.
Lemma 4.2.12	296-ge3dc076	$\epsilon(f(g(f(a))))^{-1} \cdot (f(\eta(g(f(a))))$.
Corollary 4.3.3	272-gfd47093	In the proof, $(fgx, \epsilon(fx)) = (gfx, \epsilon(fx)) =_{\text{fib}_f(fx)} (x, \text{refl}_{fx})$.
Theorem 4.4.3	299-g85b729b	At the end of the proof, the equation that is $\text{isae}(f)$, not $\text{isContr}(f)$, is a
Lemma 4.7.3	265-g64000fb	In the proof, $\text{lcoh}_f(g, \epsilon)$ should be played equation should have proof of $P(fx)$.
Theorem 4.7.6	275-g84ab032	The path concatenations in the subsequent equations) are reversed.
Theorem 4.7.6	202-g775a3f0	two displayed equations should be
Theorem 4.8.3	205-gf9fe386	The first equivalence in the proof is exercise 2.10.
§4.9	114-gaba76c8	The last equivalence in the proof is
Corollary 4.9.3	484-g2ce1249	mas 3.11.8 and 3.11.9 and Exercise
Theorem 4.9.4	746-g4d540d6	In the proof, $e \cdot \text{pr}_1$ should be (u
Exercise 4.2	358-g9543064	computation better.
§5.2	706-ged2c765	The point of Lemma 4.9.2 is that
§5.3	125-g433f87e	without assuming function extensionality
§5.3	551-g82b74bf	In the statement, “precomposition”
§5.3	218-g42219cb	composition”.
§5.3	525-gb1957b8	In the definition of ψ in the proof, apply (p, x) instead of along p .
		The text should be “Show that f is
		type is equivalent to $A \simeq B$. Can
		definition of a type satisfying the third
		In the proof that $\mathbb{N} \simeq \mathbb{N}'$, the definition
		$\text{rec}_{\mathbb{N}}(\mathbb{N}', 0', \lambda n. \text{succ}') and \text{rec}_{\mathbb{N}}$
		In the definition of \mathbf{N}^w , use 0_2 for
		the ordering of 0_2 and 1_2 in §1.8.
		The definitions of \mathbf{N}^w and List
		$W_{(b:2)} \text{rec}_2(\mathcal{U}, 0, 1, b)$ and $W_{(x:1+A)}$
		In the description of the construction
		is more clearly written as $f : B(a)$
		In the computation rule, the rule
		an argument. It should read
		$e(a, f, (\lambda b. \text{rec}_{W_{(x:A)} B(x)}(E, e, f(b)))$

Location	Fixed in	Change
§5.3	570-g6ec04c3	In the verification that double com
§5.4	554-g9b2a34b	be e_0 and e_f should be e_1 . The definition of the type of W (before Theorem 5.4.7) should read W
§5.5	917-gd6960ad	$\sum_{(f:C \rightarrow D)} \prod_{(a:A)} \prod_{(h:B(a) \rightarrow C)} f(s_C(a, h))$. In the first paragraph, the de
§5.5	608-g6af101f	$W_{(b:2)} \text{rec}_2(\mathcal{U}, 0, 1, b)$. In the computation rule for homo
§5.5	1261-g4cdab82	side should be $\text{rec}_{W_{(x:A)}^h B(x)}(E, e, \text{su})$.
§5.5	1261-g4cdab82	In the commutative diagram p
Eq. (5.6.6)	912-g04d3fb6	$W_s(A, B)$, all occurrences of x sho
§5.7	908-g4b2eb10	In the definition of $W_s(A, B)$, $\alpha(\text{sup}(a, f))$, and $\prod_{(a,f)}$ should be
		In the preceeding sentence, $\delta : d$ s
		The second two constructors of
		$\text{paritynat}(1_2) \rightarrow \text{paritynat}(0_2)$ an
		$\text{paritynat}(1_2)$.
Theorem 5.8.2	139-gd5c5d01	In the proof of (iv) \Rightarrow (i), the
Exercise 5.2	622-ga0bd007	$(\sum_{(b:A)} R(b)) \rightarrow \mathcal{U}$. The two functions should satisfy
Exercise 5.3	622-ga0bd007	mentally.
§5.8	171-gdc4966e	The function should satisfy both n
§6.2	54-gd4a47c2	The subscript of $\text{refl}_A : a =_A a$ sho
		Soon after Remark 6.2.1, the phras
		the fiber over the constructor base
Lemma 6.2.8	423-gf763ae1	Theorems 2.11.3 and 2.11.5 are n
		required by the induction princip
Lemma 6.3.2	417-g4aa6a15	Added Exercise 6.10: the function
		is actually an inverse to happly, so
		sionality axiom follows from an in
Lemma 6.4.2	625-g950efa9	In the second paragraph of the p
§6.4	327-g7cbe31c	extensionality should be omitted.
§6.4	1039-g30da4c6	In the first sentence after the proo
		P " should be " $P : S^2 \rightarrow \mathcal{U}$ ".
		In the sentence after the proof of I
		in which s is a dependent path sho
		P .
§6.6	289-gdefeb8c	In the induction principle for the
		should be $b' =_p^P b'$ and $b =_q^P b$ resp
§6.7	289-gdefeb8c	In the induction principle for the
		should be $b' =_p^P b'$ and $b =_q^P b$ resp

Location	Fixed in	Change
§6.9	468-g5472874	The induction principle for $\ A\ _0$ should be $f(a) \equiv a$. And in the induction principle for $\ A\ _0$ and in the definition of $p =^B_{u(x,y,p,q)} q$ should instead be a .
§6.9	860-gc7d862c	In the penultimate paragraph, the quantifier for $\ A\ _0$ should begin “For every $f : S \rightarrow A$ ”.
Lemma 6.10.3	961-gde36592	The first sentence of the second paragraph should end with $g(x) = \overline{g} \circ \overline{q}(x)$.
Lemma 6.10.8	514-g18ade45	Instead of “is the set-quotient of S by \sim , say “satisfies the universal property modulo \sim ”, and hence is equivalent to \overline{g} . The third and displayed equation should be $(g \circ \text{pr}_1 \circ q, -)$, the fourth displayed equation should be $(g \circ \text{pr}_1 \circ q, -)$, the fifth should be $g(x)$, and the proof should conclude with assumption s ”.
Lemma 6.10.12	535-g0a9abfe	The “computation rules” satisfied by \overline{g} are equalities. Also, the proof requires the previously mentioned equivalences.
Corollary 6.10.13	535-g0a9abfe	The defining clauses should use refl_a rather than $\text{refl}_{\text{base}}$.
Lemma 6.12.1	682-g3af5dbe	Three occurrences of P in the statement should be $(c(g(b)), D(b)(y))$.
Lemma 6.12.3	457-g411ec6d	The right-hand side of the display should be $(c(g(b)), D(b)(y))$.
Lemma 6.12.3	961-gde36592	After the display we should have f denotes a map $B \rightarrow A$ in this context used for functions defined by induction. It may use k instead. Thus f should be Lemma 6.12.4; the first sentence of the third sentences of the paragraph should be the sentence of Lemma 6.12.5; the first, its proof; throughout the statement of the statement of Lemma 6.12.8; and its proof.
§6.12	519-gc99a54c	In the display after the definition of f , the line should be with respect to x . In the second line the subscript of ap should be f .
Lemma 6.12.4	537-gdf3b51d	In the display after the definition of f , the line should be with respect to x . In the second line the subscript of ap should be f .

Location	Fixed in	Change
Lemma 6.12.4	961-gde36592	The subscript of ap should also be b in the fourth, and fifth displays. In the fifth display, $\text{refl}_{g(b)}$ should be $\text{refl}_{g(b)}$.
Lemma 6.12.8	961-gde36592	Both occurrence of the function f in the final two steps of the calculation should be f .
Lemma 6.12.7	501-ge895f81	Both occurrences of P in the state P should be P . The occurrences of Q in the proof should be Q .
Theorem 7.1.4	180-gb672a4d	In the last displayed equation of the proof, the base case in the proof is just L .
Theorem 7.1.10	101-g713f48c	The third paragraph is wrong: in the proof, $\ A\ $ would actually work to define $\ A\ $.
§7.3	480-gdc84050	In the second paragraph of the first section, the function $f(x, x)$ should be $x =_X x$.
Theorem 7.2.2	1131-gc1748fa	In the proof of the lemma, “If x is in $\text{inr}(t)$ ”.
Lemma 7.2.4	644-g627c0a8	In the proof, encode and decode should be encode and decode .
Theorem 7.3.12	412-gb9582fc	The converse direction is false unless U is inhabited. Also, the occurrences of p in the proof should be just p and $\text{pr}_2 w$, not $\text{pr}_2 w$.
Lemma 7.5.12	801-g01922a8	In the proof that the first composition is $f(x)$.
Lemma 7.5.14	367-g1c8c07e	In the second paragraph of the proof, the occurrences of y should be $f(x)$.
Theorem 7.7.4	658-g016f3a4	In the second paragraph of the proof, the occurrences of pr_2 (but not the third) should be pr_2 .
Exercise 7.2	101-ga366be2	“entires” should be “entirely”.
Exercise 7.2	683-g8941e50	This exercise needs more precise definition of “colimit”.
Exercise 7.8	1074-gcd42187	$\text{AC}_{\infty, \infty}$ is not Theorem 2.15.7, but Theorem 2.15.8.
Exercise 7.8	603-ge113e08	The penultimate sentence should be “univalence for any $m \geq 0$ and any $n \geq 0$ ”.
Lemma 8.1.8	535-g0a9abfe	The proof by induction on $n : \mathbb{Z}$ is not Corollary 6.10.13.
Lemma 8.1.12	535-g0a9abfe	The clauses defining q_z should use the erratum for Lemma 6.10.12).
Theorem 8.2.1	1062-gf3bfeae	In the proof, E is not $(n + 1)$ -connected.
Lemma 8.4.4	1181-g3e51973	In the proof, $(x : A)$ should be $(x : A)$.
Corollary 8.4.8	1023-gf188aeb	The proof requires a separate argument for the basepoint.
Theorem 8.5.1	256-g9e6fcb8	The phrase “whose fibers are S^1 ” should be “the basepoint is S^1 ”. The same change applies to exercises 8.8 and 8.9.
Lemma 8.5.3	1062-gf3bfeae	In the definition of $E^{\text{tot}'}$ in the proof, the occurrences of $E^{\text{tot}'}$ should be $E^{\text{tot}'}$.

Location	Fixed in	Change
Lemma 8.6.1	396-g868335b	In the proof, the function k should be named ℓ , to avoid confusion. It should also be named ℓ , to avoid confusion.
Definition 8.6.5	87-g3f977b2	In the second displayed equation, the right-hand side should be $\text{merid}(x_1)^{-1}$.
Lemma 8.6.2	1203-g7464bf1	The type family P defined in the text should be Q , to avoid clashes with the type P in the statement.
Lemma 8.6.2	399-g8897c94	In the last sentence of the proof, the phrase “ $(n - 1)$ -truncated” should be “ $(n - 1)$ -truncated”.
Lemma 8.6.10	88-g0c0be67	The type of m should be $a_1 = a_2$. The proof should begin with $C(a_1, \text{transport}^B(m^{-1}, a_2))$, “we may assume a_2 is a_1 and m is the identity”.
§8.6	165-gd5584c6	In (8.6.11), r'' should be r' , the type of r should be $\text{transport}^B(\text{merid}(x_0)^{-1}, q)$, and the proof of identifying this with $q \cdot \text{merid}(x_0)^{-1}$ should be $\text{transport}^B(n, \text{merid}(x_0)^{-1})$.
§8.6	474-g5289470	The point of r should be $\text{transport}^B(n, \text{merid}(x_0)^{-1})$. The statement $\pi_3(\mathbb{S}^2) = \mathbb{Z}$ should be stated as a consequence of from Corollary 8.5.2 and Theorem 8.5.1.
Theorem 8.8.3	1092-ge3b8b71	After applying the induction hypothesis, the proof to be checked that for every path p from x to y , $\pi_k(x = x, p) \rightarrow \pi_k(f(x) = f(x), p)$.
§8.9	1154-g301662b	In the strengthening of condition (iv), the right side should read just “ c ” instead of “ c in $\text{hom}_B(b, c)$ ”.
Example 9.1.15	1307-gfe63517	Stating that every isomorphism is an equivalence is inaccurate (consider the discrete category). A more accurate statement is that every isomorphism is the identity arrow. Notice that for the proof, this must be combined with skeletal property.
Definition 9.2.1	807-gebec78b	In Item (iv), it should read “ $\text{hom}_B(b, c)$ ”.
§9.4	1218-gcb6ba30	Just before Definition 9.4.6, it should say “a category” instead of “However, \mathcal{C} is not a category”.
Theorem 9.5.4	971-g6096085	The sequence of equations at the end of the proof, with $\alpha_{a'}(f) = \alpha_{a'}(\mathbf{y}a_{a,a'}(f)(1_a))$, should remain a, a' rather than a, a .
Definition 9.8.1	897-g94fb722	In (iv), “if $f : \text{hom}_X(x, y)$ ” should be “if $g : \text{hom}_X(y, z)$ ”.
§9.8	1111-g3332a31	The type of objects A_0 of the weak 2-category structures should be defined as $\text{hom}_X(x, y)$.
Chapter 9	966-g04374f5	The first sentence after Theorem 9.8.1 should be “if a precategory A admits a weak 2-category structure, then A is a category...”.

Location	Fixed in	Change
Theorem 9.9.5	313-g8ee79db	In the second proof, the third constructor follows from the fourth constructor. In the fifth constructor, $j(g) \cdot j(f)$ should be $j(g \cdot f)$ throughout the proof. Finally, for the third constructor should be included and $j(g) \cdot j(f)$ to be implied by "higher inductive type". It should be mentioned that Hofmann considered this definition of categorical products. The equation $ B _0 \times A _0 \equiv B \times A _0$ should be $ B _0 \cdot A _0 \equiv B \times A _0$. In the proof, the second sentence should have " $s(a') : \text{acc}(a')$ " rather than " $s(a) : \text{acc}(a)$ ". The second sentence of the proof should be "by induction on A , suppose A/b is a V -set". The statement should say $X : \mathcal{U}$ rather than $X : \mathcal{V}$. The penultimate sentence of the proof should be " $b < c$ " rather than "if $a < b$ and $a < c$ ". The statement of (i) should end with "whenever $h(f(a)) =_p h(g(b))$ ". The second clause in the induction should be "Verify that if $f : A \rightarrow V$ and $g : B \rightarrow V$ are V -sets, then $h(\text{set}(A, f)) =_q^p h(\text{set}(B, g))$, where h is the second constructor of V and (1) that $h(f(a)) =_p^q h(g(b))$ whenever $f(a) =_p g(b)$ ". The proof that membership is well-founded should be "hence $x = g(b)$ and $x \in \text{set}(B, g)$ ". In the definition of V -set, the notation $\text{set}(A, f)$ should be $\text{set}(A, f)$. In the pairing axiom, the pair class should be $\text{pair}(u, v)$ rather than $\text{not } u \cup v$. The replacement axiom should be $\text{replace}(f, g)$ rather than $\text{replace}(f, g)$. The displayed class should be $\{ y \in V \mid \dots \}$ rather than $\{ y \mid \dots \}$. Its proof should begin "let C denote the class of V -sets". In the proof of the function set axiom, the statement $[u] \rightarrow V$ and $[u] \rightarrow V$ should be $[u] \rightarrow V$ and $[v] \rightarrow V$. Extra parentheses around $\forall(x \in v)$ should be added to make the formula unambiguous. Extra parentheses around $\forall(y \in x)$ should be added to make the formula unambiguous. The notation $\in V$ should be $: V$. The statement should say "For all $x \in V$, $(q < x)$ and $U_x(q) \Leftrightarrow (x < q)$ ".
Chapter 9 Notes	379-ga57eab2	
Lemma 10.2.4	1303-ga530d97	
Lemma 10.3.8	1290-g4101ad3	
Theorem 10.3.20	140-g55de417	
Lemma 10.3.22	140-gd7f8960	
Theorem 10.4.3	140-gcca0bcf	
Theorem 10.4.4	871-g85bcd11	
§10.5	753-gc87ce23	
§10.5	706-ged2c765	
§10.5	1056-g4060c2b	
Theorem 10.5.8	708-g6f53189	
Theorem 10.5.8	723-g9cf5b44	
Theorem 10.5.8	706-ged2c765	
Exercise 10.12	1053-ge13dd65	
Exercise 10.13	1053-ge13dd65	
Exercise 10.13	1056-g4060c2b	
Lemma 11.2.2	165-gb002a64	

Location	Fixed in	Change
Theorem 11.2.4	165-g179b359	In the proof, the sentence beginning “From $0 < a < x$ or $x < b < 0$, so that $x < a$ or $x < b$ ” should be replaced by “From $0 < a < x$ or $x < b < 0$, so that $x < a$ or $x < b$, and a, b , and c are either all positive or all negative”.
Theorem 11.2.4	merge of 38792ed8fb9b08275d14ed1c92830d42a806e2b5	In the proof of the theorem, the definition of $L_{x^{-1}}(q)$ should be changed as follows: $L_{x^{-1}}(q) := (q < 0 \wedge (qr < 1))$ and $U_{x^{-1}}(q) := (q > 0 \wedge (qr < 1))$ for positive x , and $L_{x^{-1}}(q) := (q < 0 \wedge (qr > 1))$ and $U_{x^{-1}}(q) := (q > 0 \wedge (qr > 1))$ for negative x .
§11.2.2	832-g0cb658e	In the second paragraph, at “From $\delta > 0$ ”, the quantification should be over $\delta \in \mathbb{Q}_+$.
§11.3.2	1209-g3e5ad94	In the statement of (\mathbb{R}_c, \sim) -recursion, the statement “ $f(\lim(x)) : A$ ” should be “ $f(\lim(x)) : A$ ”.
Theorem 11.3.16	1069-g3b333d5	In the description of openness of c , the statement “ $\exists(\delta : \mathbb{Q}_+)$ ” should be “ $\exists(\delta : \mathbb{Q}_+)$ ”.
Lemma 11.4.1	87-g82b27c3	(11.4.2) should be $c : \prod_{(q,r:\mathbb{Q})} (q < r \Rightarrow c(x, s, t) < c(x, r, t))$ therefore the use of c in the proof of 11.4.1 should be $c(x, s, t)$.
Theorem 11.5.6	1270-g3f17b85	In the proof, $n : \mathbb{N}$ should be $k : \mathbb{N}$. Also in the last equation, n should be $0 \leq i \leq k$. Also in the last equation, n should be ℓ .
§11.6	1189-ga9c35f0	The inductive case of $\iota_{\mathbb{Q}_D}$ should be $\{ \iota_{\mathbb{Q}_D}(a/2^n - 1/2^n) \mid \iota_{\mathbb{Q}_D}(a/2^n + 1/2^n) \}$.
Example 11.6.18	636-g827e7ea	In the first bullet point, to prove $x^L + z$ is a left option of $x^L + y$, induction on z , since only when z is a left option of y can we say that $x^L + z$ is a left option of $x^L + y$.
Exercise 11.13	222-g3453cf1	This is the intermediate value theorem.
Example 11.6.18	980-ge9d0398	For the codomain of the outer recursion, the statement “ $(x < y) \rightarrow (g(x) < g(y))$ ” should be “ $(x < y) \rightarrow (g(x) < g(y))$ ”.
Example 11.6.18	980-ge9d0398	In the first bullet of the verification, the outer inductive hypothesis should be “ $x^L + y \leq x^L + z$ and $x^R + y \leq x^R + z$ ”. No-induction on z is required (the induction is defined by a cut).
Example 11.6.18	980-ge9d0398	The verification that Conway’s number is a number (i.e. all its left options are less than all its right options) is omitted. This requires turning the outer induction with codomain a verification of the theorem 11.6.7.

Location	Fixed in	Change
Appendix A	165-g76db618	After the introduction of the judgements, the sentence beginning “In particular, should say instead “In particular, Clarify the distinction between type well-formedness judgments, and the condition for the latter.
Appendix A.2.1	64-g7c2312e	In Σ -COMP and the following paragraph and “we bind $\dots y$ in C ” should list. The c argument in the eliminator (the COMP rules) should not bind a variable. The unbiased eliminator for the identity is $\text{ind}_{=A}$, not $\text{ind}'_{=A}$.
Appendix A.2.5	26-gcd691e8	
Appendix A.2.8	338-g4e1c688	
Appendix A.2.10	578-ga4b94a5	