

The Fisher information is defined as the expectation of the negative second derivative. From the expression, we can see that the second derivative of the Gaussian likelihood is

$$\frac{\partial^2 \log(\mathcal{L})}{\partial \mu^2} = -\frac{N}{\sigma^2}$$

Hence the Fisher information is  $\frac{N}{\sigma^2}$