

Derive the optimal least squares parameter
Value $\underline{\hat{w}}$ for the total training loss

$$J = \sum_{n=1}^N (t_n - \underline{w}^T \underline{x}_n)^2$$

$$= (\underline{t} - \underline{X} \underline{w})^T (\underline{t} - \underline{X} \underline{w})$$

$$= \underline{t}^T \underline{t} - 2 \underline{w}^T \underline{X}^T \underline{t} + \underline{w}^T \underline{X}^T \underline{X} \underline{w}$$

$$\frac{\partial J}{\partial \underline{w}} = -2 \underline{X}^T \underline{t} + 2 \underline{X}^T \underline{X} \underline{w}$$

Set partial derivative to 0.

$$\therefore \underline{X}^T \underline{t} = \underline{X}^T \underline{X} \underline{w}$$

$$\underline{\underline{\therefore \underline{w} = (\underline{X}^T \underline{X})^{-1} \underline{X}^T \underline{t}}}$$

It's the same as the average loss. Only
differs by a constant.