The hypothesis spaces learned by our test PMSI for all domains at once. Useful primitives for the Language Queries, Equation Solving, and Robot Planning domains are orange, blue, and green, respectively. Notice how it's learned action chunks are naturally from separate domains. We did not explicitly tell it of do this.

```
DQN #6 (lowest level)
1. (after to before)
2. (in-back-of_to_in-front-of)
3. (because_to_before)
4. (chain before relations)
5. (in-front-of to before)
6. (years_to_after)
7. (check if solution is explicit)
8. (simplify_products)
9. (simplify_fractions)
10. (add_like_terms)
11. (divide by relevant multiple)
12. (apply_quadratic_formula)
13. (update_innerese_world_representation)
14. (attempt_to_place_x_on_y)
15. (unstack_item_above_x_to_reach_x)
16. (unstack item above y to make room for x)
DQN #5
1. (in-back-of to in-front-of)
2. (because_to_before)
3. (simplify fractions)
4. (unstack item above y to make room for x \Rightarrow update innerese world representation)
5. (add_like_terms => divide_by_relevant_multiple => check_if_solution_is_explicit)
6. (in-front-of to before => chain before relations)
```

```
7. (unstack_item_above_y_to_make_room_for_x => attempt_to_place_x_on_y)
8. (unstack item above x to reach x \Rightarrow attempt to place x on y)
9. (apply quadratic formula => check if solution is explicit)
10. (simplify products => add like terms)
11. (after to before => chain before relations)
12. (years_to_after => after_to_before)
DQN #4
1. (in-front-of to before => chain before relations)
2. (after to before => chain before relations)
3. (years_to_after => after_to_before)
4. (simplify products => add like terms => apply quadratic formula => check if solution is explicit)
5. (unstack item above y to make room for x \Rightarrow attempt to place x on y \Rightarrow
unstack item above y to make room for x => update innerese world representation =>
because_to_before)
6. (unstack item above y to make room for x \Rightarrow attempt to place x on y \Rightarrow
unstack item above x to reach x \Rightarrow attempt to place x on y)
7. (simplify fractions => simplify products => add like terms)
8. (attempt to place x on y => in-back-of to in-front-of => because to before)
9. (simplify fractions => add like terms => divide by relevant multiple => check if solution is explicit)
DQN #3
1. (years to after => after to before)
2. (simplify products => add like terms => apply quadratic formula => check if solution is explicit)
3. (unstack item above y to make room for x \Rightarrow attempt to place x on y \Rightarrow
unstack item above y to make room for x => update innerese world representation =>
because to before)
4. (attempt to place x on y => in-back-of to in-front-of => because to before => in-front-of to before =>
chain before relations)
5. (simplify fractions => simplify products => add like terms => simplify fractions => add like terms =>
divide by relevant multiple => check if solution is explicit)
6. (unstack_item_above_y_to_make_room_for_x => attempt_to_place_x_on_y =>
unstack_item_above_x_to_reach_x => attempt_to_place_x_on_y =>
unstack_item_above_y_to_make_room_for_x => attempt_to_place_x_on_y)
```

7. (attempt\_to\_place\_x\_on\_y => in-back-of\_to\_in-front-of => because\_to\_before => after\_to\_before => chain before relations)

## **DQN. #2**

- 1. (simplify products => add like terms => apply quadratic formula => check if solution is explicit)
- 2. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => update\_innerese\_world\_representation => because\_to\_before)
- 3. (simplify\_fractions => simplify\_products => add\_like\_terms => simplify\_fractions => add\_like\_terms => divide by relevant multiple => check if solution is explicit)
- 4. (attempt\_to\_place\_x\_on\_y => in-back-of\_to\_in-front-of => because\_to\_before => after\_to\_before => chain\_before\_relations)
- 5. (years\_to\_after => after\_to\_before => attempt\_to\_place\_x\_on\_y => in-back-of\_to\_in-front-of => because to before => in-front-of to before => chain before relations)
- 6. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y)

## DQN #1 (top level)

- 1. (simplify products => add like terms => apply quadratic formula => check if solution is explicit)
- 2. (simplify\_fractions => simplify\_products => add\_like\_terms => simplify\_fractions => add\_like\_terms => divide by relevant multiple => check if solution is explicit)
- 3. (attempt\_to\_place\_x\_on\_y => in-back-of\_to\_in-front-of => because\_to\_before => after\_to\_before => chain before relations)
- 4. (years\_to\_after => after\_to\_before => attempt\_to\_place\_x\_on\_y => in-back-of\_to\_in-front-of => because\_to\_before => in-front-of\_to\_before => chain\_before\_relations)
- 5. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => update\_innerese\_world\_representation => because\_to\_before => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_y => attempt\_to\_place\_y\_to\_make\_room\_for\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_y => unstack\_item\_above\_y\_to\_ma

The hypothesis spaces learned by our test PMSI for the Language Queries domain.

```
DQN #4 (lowest level)
1. (years_to_after)
2. (after_to_before)
3. (because to before)
4. (in-back-of_to_in-front-of)
5. (in-front-of to before)
6. (chain before relations)
DQN #3
1. (in-front-of to before => chain before relations)
2. (because_to_before => chain_before_relations)
3. (after_to_before => chain_before_relations)
4. (years to after)
5. (in-back-of_to_in-front-of)
DQN#2
1. (in-back-of_to_in-front-of => in-front-of_to_before => chain_before_relations)
2. (chain_before_relations => because_to_before => chain_before_relations)
3. (after_to_before => chain_before_relations)
4. (years_to_after)
DQN #1 (top level)
1. (in-back-of to in-front-of => in-front-of to before => chain before relations)
2. (chain_before_relations => because_to_before => chain_before_relations)
3. (years to after => after to before => chain before relations)
```

The hypothesis spaces learned by PMSI for the Equation Solving domain.

DQN #2 (lowest level)

```
1. (add_like_terms)
2. (simplify fractions)
3. (simplify_products)
4. (apply_quadratic_formula)
5. (divide_by_relevant_multiple)
6. (check_if_solution_is_explicit)
DQN #1 (top level)
1. (divide_by_relevant_multiple => check_if_solution_is_explicit)
2. (apply_quadratic_formula => check_if_solution_is_explicit)
3. (simplify_fractions => simplify_products)
4. (add_like_terms)
The hypothesis spaces learned by PMSI for the Robot Planning domain.
DQN #4 (lowest level)
1. (attempt_to_place_x_on_y)
2. (unstack_item_above_x_to_reach_x)
```

3. (unstack item above y to make room for x)

4. (update innerese world representation)

- 1. (unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y)
- 2. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y)
- 3. (unstack item above y to make room for  $x \Rightarrow$  unstack item above x to reach x)
- 4. (update\_innerese\_world\_representation)

## **DQN #2**

- 1. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => unstack\_item\_above\_x\_to\_reach\_x => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y)
- 2. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => unstack\_item\_above\_x\_to\_reach\_x => unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y)
- 3. (update\_innerese\_world\_representation)

## DQN #1 (top level)

- 1. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => unstack\_item\_above\_x\_to\_reach\_x => unstack\_item\_above\_y\_to\_make\_room\_for\_x => attempt\_to\_place\_x\_on\_y => unstack\_item\_above\_y\_to\_make\_room\_for\_x => unstack\_item\_above\_x\_to\_reach\_x)
- 2. (unstack\_item\_above\_y\_to\_make\_room\_for\_x => unstack\_item\_above\_x\_to\_reach\_x => unstack\_item\_above\_x\_to\_reach\_x => attempt\_to\_place\_x\_on\_y)
- 3. (update innerese world representation)