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Homework 5

- ▷ 8 years of operation at 24,000 km per year.
- ▷ average battery output of 204 Wh/km
- ▷ rated cell of 3.6V and capacity of 3.4 Ah, $L=1$, $N(100\%)=1,000$

i) BOL kWh Storage and BOL range $24,000(8) = 192,000 \text{ km}$
 $\frac{192,000 \text{ km}}{1,000} = 192 \text{ km per cycle}$

BOL Range = 192 km per cycle

BOL Storage = $192(204) = 39.16 \text{ kWh}$

ii) Cells Required?

$E_{\text{cell}} = V \times Ah = 3.6 \text{ V} \times 3.4 \text{ Ah} = 12.24 \text{ Wh}$

Number of cells = $\frac{39.16 \text{ kWh}}{12.24 \text{ Wh/cell}} = 3200 \text{ cells}$

iii) Cells Required if BOL Range is 425 km

Storage = $425(204) = 86.7 \text{ kWh}$

Number of cells = $\frac{86.7 \text{ kWh}}{12.24 \text{ Wh/cell}} = 7083 \text{ cells}$

iv) how many Parallel Strings are required if the Pack has 96 cells in Series

$V_{\text{pack}} = 96 \times 3.6 = 345.6 \text{ V}$

Parallel Strings = $\frac{7083}{96} = 74$

v) battery pack mass, assuming pack density of 150

Total energy = 86.7 kWh

Battery mass = $\frac{86.7 \text{ kWh}}{150 \text{ Wh/kg}} = 578 \text{ kg}$

2. PHEV Pack: 10 years at an average of 50 km per day
Average battery output of 5 km/kWh, and a 14.6 Ah cell with
3.65V. $L = 3$ $N(\text{doD}\%) = 1000$

i) B0L battery Pack energy storage

$$\text{Daily energy required} = \frac{50 \text{ km}}{5 \text{ km/kWh}} = 10 \text{ kWh/day}$$

$$10 \text{ years} = 3650 \text{ days}$$

$$3650 = N_{100\%} (100\% / \text{DoD})^L \rightarrow \sqrt[3]{3.65} = \frac{100\%}{\text{DoD}} \rightarrow \text{DoD} = 65\%$$

$$\text{Energy Storage} = \frac{10 \text{ kWh}}{0.65} = \boxed{15.4 \text{ kWh}}$$

ii) Total number of cells

$$E_{\text{cell}} = 14.6 (3.65) = 53.29 \text{ Wh}$$

$$\text{Number of Cell} = \frac{15,400 \text{ Wh}}{53.29 \text{ Wh}} = 288.98 \text{ cells}$$

$$\boxed{288 \rightarrow \text{Nearest multiple of 3}}$$

iii) Pack voltage in 3 Parallel cells

$$n_s = \frac{288}{3} = 96 \quad V_{\text{pack}} = 96 (3.65) = \boxed{350 \text{ V}}$$

iv) battery pack's mass, assuming 150 Wh/Kg

$$\frac{15,400 \text{ Wh}}{150 \text{ Wh/Kg}} = \boxed{102.67 \text{ Kg}}$$

3. NiMH HeV battery Pack: 10,000 cycles Per year for ten years, 60 Wh Per cycle usage, a 6.5 Ah cell with a rated voltage of 1.2 V $L=1.5$ $N(100\%)=1000$

$$N = 10000(10) = 100,000$$

$$DOD = \left(\frac{100,000}{1000} \right)^{1/1.5} (100) = 4.641\%$$

- i) BOL battery Pack storage

$$\text{BOL energy storage} = \frac{60}{0.04641} = 1,292.8 \approx \boxed{1.292 \text{ kWh}}$$

- ii) Total number of cells

$$E_{\text{cell}} = 6.5(1.2) = 7.8$$

$$\text{Total Cell} = \frac{1292}{7.8} = \boxed{165.6 \text{ cells}}$$

- iii) battery Pack's rated voltage if cells are in series

$$V_{\text{pack}} = 165.6(1.2) = \boxed{198.72 \text{ V}}$$