

Variational Methods in Imaging

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Chapter 1

Introduction to Variational Methods and Computer Vision

Variational Methods in Imaging

Feb 2021

Introduction to
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Two Different
Paradigms for
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A Bit of History

Overview of the
Lecture

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- 1 Introduction to Computer Vision**
- 2 Two Different Paradigms for Computer Vision**
- 3 Introduction to Variational Methods**
- 4 A Bit of History**
- 5 Overview of the Lecture**

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Goal of the lecture

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- Give an overview of **computer vision**
- Describe major **inverse problems** in computer vision
- Provide a generic **mathematical approach** for solving them
- Show how to implement such solutions on CPU
- Discuss open problems and limits of the state-of-the-art

Required: basic analysis, linear algebra, statistics

Useful: optimization, PDEs

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Recommended readings

P. Kornprobst, G. Aubert, "Mathematical Problems in Image Processing, Partial Differential Equations and the Calculus of Variations", Springer 2006.

T. Chan, J. Shen, "Image Processing and Analysis: Variational, PDE, Wavelet, and Stochastic Methods", SIAM 2005.

- 2013 video lectures in TU Munich from Daniel CREMERS (11 chapters): [youtube](#) → “Cremers Variational”
- 2017 slides in TU Munich from Yvain QUÉAU (14 chapters) available on request (yvain.queau@gmail.com)

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What is computer vision?

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Computer vision tools: Sensors

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Camera



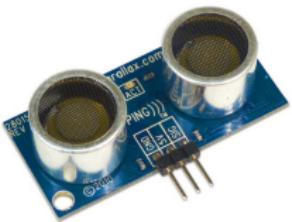
Movie camera



Depth sensor



Infrared sensor



Ultrasound sensor



X-ray scanner

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- Sensors capture **images** (of different types) of the world
- Computer vision aims at high-level analysis (i.e., “understanding”) these visual signals

Computer vision: What for?



Autonomous driving



Augmented reality



Robotics

And also...

- Computer-assisted medical diagnostic
- Videosurveillance
- Surface inspection
- After effects
- Earth monitoring
- ...

Different types of images: Cameras

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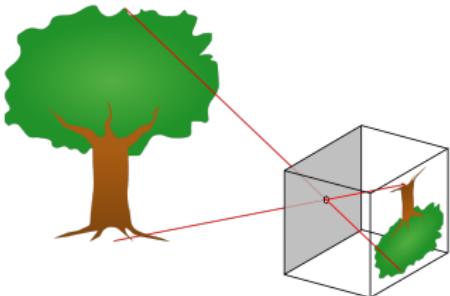
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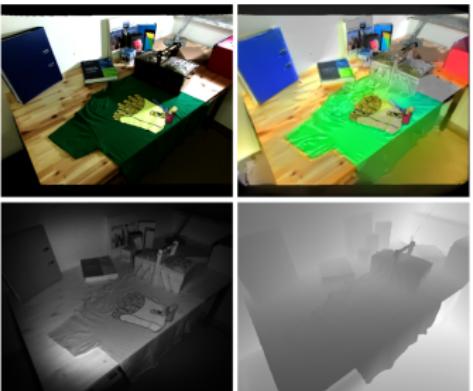
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Measures photons emitted (reflected) by the scene's surface

- Greylevel image = function u associating to each pixel $(x, y) \in \Omega \subset \mathbb{R}^2$ a float value:
 $u : \Omega \rightarrow \mathbb{R}; (x, y) \mapsto u(x, y)$
- RGB cameras associate three float values to each pixel:
 $u : \Omega \rightarrow \mathbb{R}^3; (x, y) \mapsto [u_R(x, y), u_G(x, y), u_B(x, y)]^\top$
- Movie RGB cameras associate three float values to each (pixel, time):
 $u : \Omega \times \mathbb{R} \rightarrow \mathbb{R}^3; (x, y, t) \mapsto [u_R(x, y, t), u_G(x, y, t), u_B(x, y, t)]^\top$

Different types of images: Depth sensors



Measures distances to the scene's surface (based on triangulation or time-of-flight), sometimes also provides IR image

- IR image = greylevel image:
 $u : \Omega \rightarrow \mathbb{R}; (x, y) \mapsto u(x, y)$
- Depth image:
 $u : \Omega \rightarrow \mathbb{R}; (x, y) \mapsto u(x, y)$

Different types of images: X-ray Scanners

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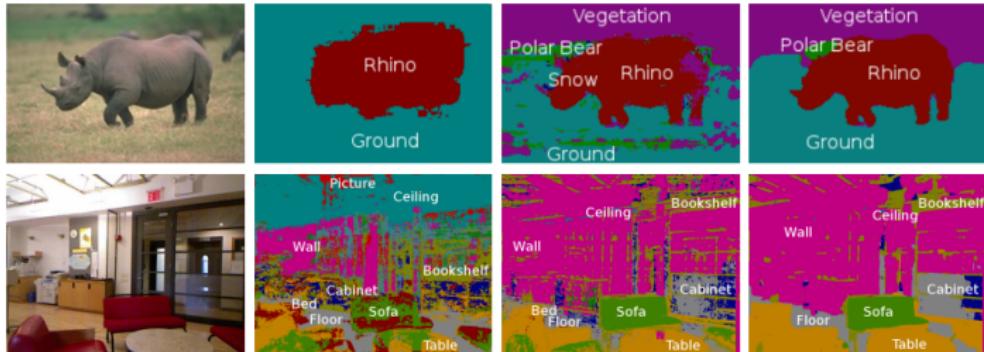
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Measures attenuation of X-ray for a given time and angle

X-ray image = sinogram:

$$u : [0, 2\pi] \times [0, 1] \rightarrow \mathbb{R}; (\theta, \rho) \mapsto u(\theta, \rho)$$

From sensors to visual understanding: What is that?



a) Original image b) Classification of [14]/[7] c) Proposed Classification d) Proposed Segmentation

- Raw measurements from a sensor are easily understood by humans, but not by computers
- Computer vision aims at making computers “understand” what they see

(image source: semantic segmentation by C. HARIZBAS et al., SSVM 2015)



From sensors to visual understanding: Where am I?

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- Various information can be extracted from visual clues: location, map of the environment, etc.

(image source: stereo SLAM by R. WANG et al., ICCV 2017 –
see video)

From sensors to visual understanding: Why do I see such images?



- Understanding the world requires understanding what led to the observed images, e.g. which 3D-shape could have produced a given set of RGB or depth images (**inverse problem**)

(image source: copyme 3D by J. STURM et al., GCPR 2013 – see video)

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How to achieve this task?

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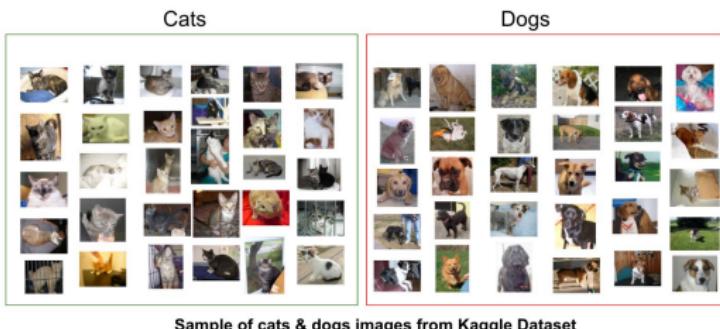
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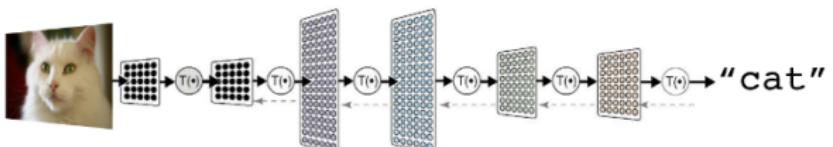
Paradigm 1: machine learning



Case 1: Humans can solve the problem, though they cannot explain why (e.g., recognition tasks): **machine learning**



Provide the machine with annotated data;
Let it “learn” what a cat is



Based on the numerous examples it knows,
machine can tell “this is a cat” when
given a new image

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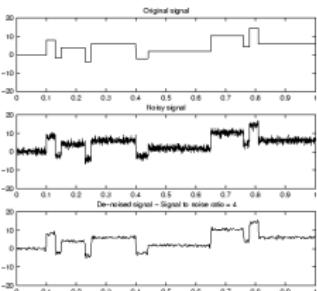
Paradigm 2: variational methods

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Case 2: Humans know how they would solve the problem (e.g., restoration tasks): **variational methods**



- 1) Model the signal acquisition process:

$$u_0(t) = u(t) + \mathcal{N}(0, \sigma^2), \quad t \in [0, 1]$$

(u_0 : observed signal, u : uncorrupted signal, \mathcal{N} : random Gaussian noise)

- 2) Invoke Bayesian inference to turn the problem into a **continuous optimization problem**:

$$\min_{u: [0,1] \rightarrow \mathbb{R}} \int_{t=0}^1 |u(t) - u_0(t)|^2 + \lambda |u'(t)|^2 dt$$

- 3) Turn the optimization problem into a differential equation (Euler-Lagrange):

$$\lambda u''(t) - u(t) = u_0(t), \quad t \in [0, 1]$$

- 4) Solve the differential equation with the computer

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Machine learning VS Variational methods

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| Machine learning | Variational methods |
|---|---|
| <ul style="list-style-type: none">• AI-oriented• Not clear why it works• Human tells the computer the solution• Requires heavy computational power• Natural framework for classification• Community growing since 2012 | <ul style="list-style-type: none">• Mathematics-oriented• Guarantee of optimality• Human tells the computer how to solve• Usually much more efficient• Natural framework for inverse problems• Community reducing since 2012 |

This lecture: **variational methods**

(in fact, these paradigms are much more complementary than it may seem)

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What are variational methods?

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A few classic inverse problems in computer vision: Denoising



Input image



Piecewise smooth approximation

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Find an image $u : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ “close to” the noisy data
 $u_0 : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$, but “smoother”:

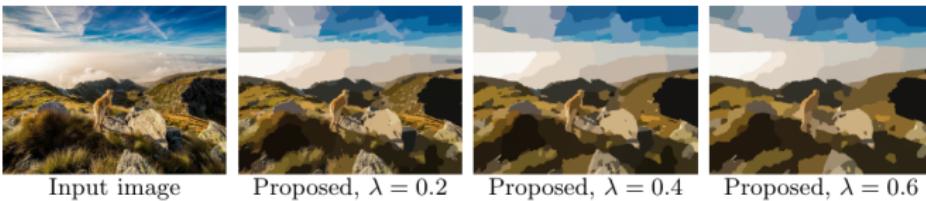
$$\min_{u: \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}} \iint_{(x,y) \in \Omega} \underbrace{|u(x,y) - u_0(x,y)|^2}_{\text{“close to”}} + \lambda \underbrace{\|\nabla u(x,y)\|^2}_{\text{“smoother”}} \, dx dy$$

(image source: fast Mumford-Shah denoising by E. STREKALOVSKIY and D. CREMERS, ECCV 2014)

A few classic inverse problems in computer vision: Segmentation

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Find an image $u : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ “close to” the input image $u_0 : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$, but “piecewise constant”:

$$\min_{u: \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}} \iint_{(x,y) \in \Omega} \underbrace{|u(x,y) - u_0(x,y)|^2}_{\text{“close to”}} + \lambda \underbrace{\delta(\|\nabla u(x,y)\|)}_{\text{“piecewise constant”}} \, dx \, dy$$

(image source: fast Mumford-Shah denoising by E. STREKALOVSKIY and D. CREMERS, ECCV 2014 – see video)



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A few classic inverse problems in computer vision: Inpainting

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(a) Original photograph (b) Inpainted photograph

Fig.1 Removing large objects from images.

Find an image $u : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ “close to” the input image $u_0 : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ on $\bar{\Omega} \subset \Omega$, but “smooth elsewhere”:

$$\min_{u: \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}} \underbrace{\iint_{(x,y) \in \bar{\Omega}} |u(x,y) - u_0(x,y)|^2 \, dx \, dy}_{\text{“close to on } \bar{\Omega}”} + \lambda \underbrace{\iint_{(x,y) \in \Omega \setminus \bar{\Omega}} \|\nabla u(x,y)\|^2 \, dx \, dy}_{\text{“smooth elsewhere”}}$$

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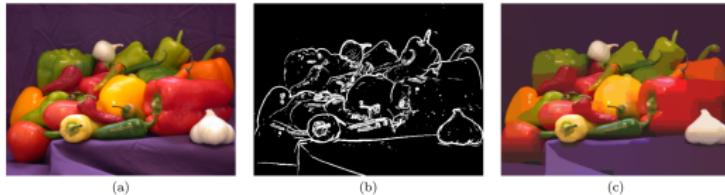
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A few classic inverse problems in computer vision: Data compression



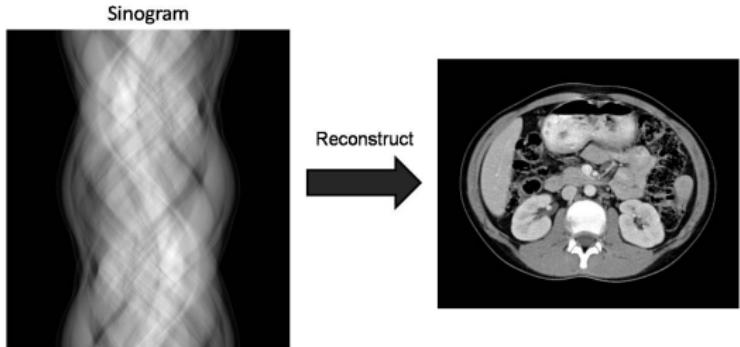
Find an image $u : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ “close to” the compressed image $u_0 : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ on $\bar{\Omega} \subset \Omega$, but “smooth elsewhere”:

$$\min_{u: \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}} \underbrace{\iint_{(x,y) \in \bar{\Omega}} |u(x,y) - u_0(x,y)|^2 + \lambda \|\nabla u(x,y) - \nabla u_0(x,y)\|^2 \, dx dy}_{\text{“close to on } \bar{\Omega}\text{”, at order 1}}$$
$$+ \mu \underbrace{\iint_{(x,y) \in \Omega \setminus \bar{\Omega}} \|\nabla u(x,y)\|^2 \, dx dy}_{\text{“smooth elsewhere”}}$$

(image source: normal integration by Y. QUÉAU et al., JMIV 2018)

A few classic inverse problems in computer vision: 2D-reconstruction (tomography)

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Find a “smooth” image $u : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ “whose Radon transform matches” the noisy sinogram $u_0 : [0, 1] \times [0, 2\pi] \rightarrow \mathbb{R}$

$$\min_{u: \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}} \iint_{(x,y) \in \Omega} \underbrace{|u(x,y) - R^{-1}(u_0)(x,y)|^2}_{\text{"matches sinogram"}} + \lambda \underbrace{\|\nabla u(x,y)\|^2}_{\text{"smooth"}} \, dx \, dy$$

A few classic inverse problems in computer vision: Combining several variational problems

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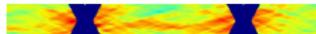
All these tools can be combined in a big variational problem if needed. E.g., joint reconstruction, inpainting and segmentation for Synchrotron X-ray tomography:



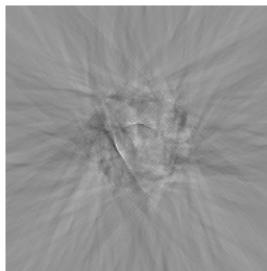
Max IV synchrotron



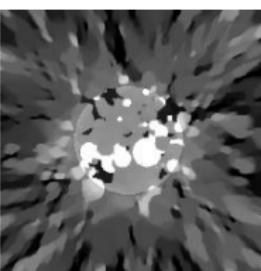
Acquisition device



Sinogram



Reconstruction only



Reconstruction + Segmentation + Inpainting

(image source: CT reconstruction by F. LAUZE et al., SSVM 2017)

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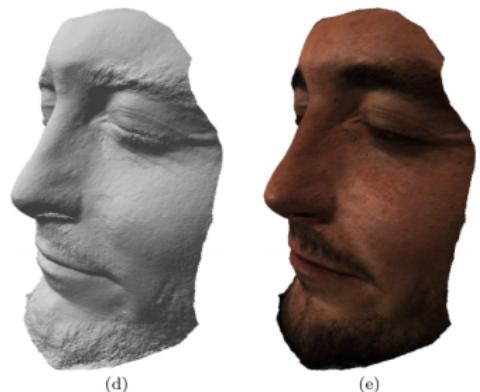
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A few classic inverse problems in computer vision: Single-view 3D-reconstruction

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(image source: photometric stereo by Y. QUÉAU et al., JMIV 2017 – see video)



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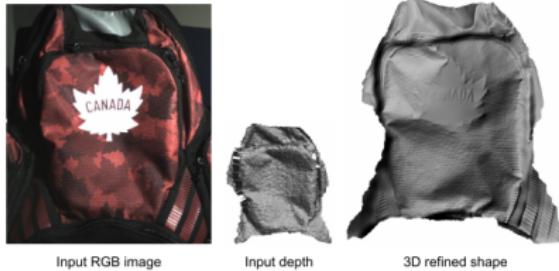
Find a depth map $u : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ “explaining” the image
 $I : \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}$:

$$\min_{u: \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}} \iint_{(x,y) \in \Omega} \|\mathbf{a}(x, y) \cdot \nabla u(x, y) - I(x, y)\|^2 \, dx \, dy$$

A few classic inverse problems in computer vision: shading-aware depth refinement

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(image source: depth super-resolution by S. PENG et al., ICCVW 2017)



Find a high-res depth map $u : \Omega_{HR} \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ “close to” a low-res one $u_0 : \Omega_{LR} \subset \mathbb{R}^2 \rightarrow \mathbb{R}$ which “matches” a high-res image $I : \Omega_{HR} \subset \mathbb{R}^2 \rightarrow \mathbb{R}$:

$$\min_{u: \Omega \subset \mathbb{R}^2 \rightarrow \mathbb{R}} \underbrace{\iint_{(x,y) \in \Omega_{LR}} |Ku(x,y) - u_0(x,y)|^2 dx dy}_{\text{“close to”}} + \lambda \underbrace{\iint_{(x,y) \in \Omega_{HR}} \|\mathbf{a}(x,y) \cdot \nabla u(x,y) - I(x,y)\|^2}_{\text{“matches”}}$$

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Variational Methods = a generic tool for inverse problems

Whatever the sensor:

- Camera
- Depth sensor
- X-ray sensor
- ...

Whatever the task:

- Restoration
- Reconstruction
- Segmentation
- ...

Recast the problem as an optimization problem:

$$\min_{u: \Omega \subset \mathbb{R}^n \rightarrow \mathbb{R}^d} \int_{\Omega} \mathcal{L}(x, u(x), \nabla u(x), \dots) dx$$

Key issues

- What are Ω , n and d ?
- How to choose \mathcal{L} ?
- Is there a solution? Unique?
- How to discretize and solve the optimization problem?





Where do such ideas come from?

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Historical motivation I

- 1657: Fermat's principle ("The path taken between two points by a ray of light is the path that can be traversed in the least time")
- 1744 (Euler) : first necessary condition to solve

$$\begin{cases} \min_{u: [x_A, x_B] \rightarrow \mathbb{R}} \int_{x_A}^{x_B} \mathcal{L}(x, u(x), u'(x)) dx \\ u(x_A) = u_A \\ u(x_B) = u_B \end{cases}$$

- 1746: principle of least actions (Maupertuis): "Nature is thrifty in all its actions"
- 1755: reformulation by Lagrange of Euler's necessary condition (\Rightarrow Euler-Lagrange equation in 1766) :

$$\frac{\partial \mathcal{L}}{\partial u} - \frac{d}{dx} \left(\frac{\partial \mathcal{L}}{\partial u'} \right) = 0$$

- 1786: extension to $\min_u \int_{x_A}^{x_B} \mathcal{L}(x, u(x), u'(x), u''(x)) dx$
(Legendre)

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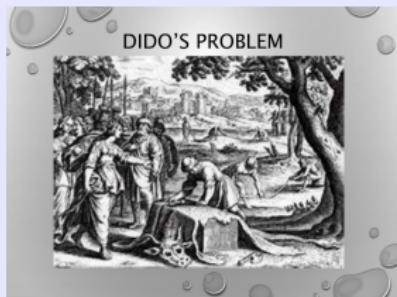
Historical Motivation II: Before that...

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Dido's problem

≈ 800 BC: Queen Dido lands in Carthago...



What is the closed curve which has the maximum area for a given perimeter?



The brachistochrone

- 1638: first mention by Galileo
- 1696: challenge by Johann Bernoulli to his fellows
- 1697: solutions by Johann Bernoulli, Leibniz, Newton and... Jacob Bernoulli

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- 19th century: Dirichlet, Riemann, Weierstrass and Neumann study **Dirichlet's problem** :

$$\min_{u: \Omega \rightarrow \mathbb{R}} \int_{\Omega} \|\nabla u(x)\|^2 dx \quad (1)$$

depending on boundary conditions, with $\Omega \subset \mathbb{R}$, \mathbb{R}^2 or \mathbb{R}^3

- 1900: Hilbert problems number 20 and 23
 - Number 20: Do all variational problems with certain boundary conditions have solutions?
 - Number 23: Further development of the calculus of variations
- 1900-... : Hilbert space theory, optimization,...

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Conclusion on those historical landmarks

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It is **natural** to formulate computer vision tasks as variational problems

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Short version at INP-ENSEEIHT:

- | | |
|------------------------|---------------------------------|
| Chapter 1 (Today): | Introduction |
| Chapter 2 (Today): | Diffusion-based Image Filtering |
| Chapter 3 (Feb 23th): | Variational Image Restoration |
| Chapter 4 (March 3rd): | High-level Applications |

Full version in TU Munich (2017 slides available upon request,
also lectures by Prof. Cremers on youtube):

- | | |
|-------------|---|
| Chapter 0: | Introduction |
| Chapter 1: | Images and Image Filtering |
| Chapter 2: | Diffusion Filtering |
| Chapter 3: | Variational Calculus |
| Chapter 4: | Variational Image Restoration |
| Chapter 5: | Image Segmentation I – Basics |
| Chapter 6: | Image Segmentation II – Variational Approaches |
| Chapter 7: | Image Segmentation III – Bayesian Inference |
| Chapter 8: | Level Set Methods |
| Chapter 9: | Convex Relaxation Methods I – Segmentation |
| Chapter 10: | Motion Estimation & Optical Flow |
| Chapter 11: | Convex Relaxation Methods II – Multiview Reconstruction |
| Chapter 12: | Photometric Techniques |

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Practical 1: Variational Image Restoration

stractory for images since it is overly sensitive to noise. An alternative approach is to solve for level lines with minimal curvature, using an anisotropic diffusion PDE model. The first work on this problem was Nitzberg and Mumford's 2.1-D model [7]. Sapiro, Caselles, and Ballester [8] introduced inpainting through the inpainting domain, but only used an anisotropic diffusion PDE model. The first work on inpainting a obscuring foreground object was Mumford and Shah's [2], based on a variant of the Mumford-Shah model for image denoising by Rudin, Osher, and Fatemi [9]. TV regularization was originally developed for image denoising by Rudin, Osher, and Fatemi [9]. Inpainting is an interpolation problem, but only if the length of the boundary to be restored is small. TV, but this is less successful for restoring. Inpainting is also used to solve discoloration problems.

Input image



Restored image

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Paradigms for
Computer Vision

Introduction to
Variational Methods

A Bit of History

Overview of the
Lecture

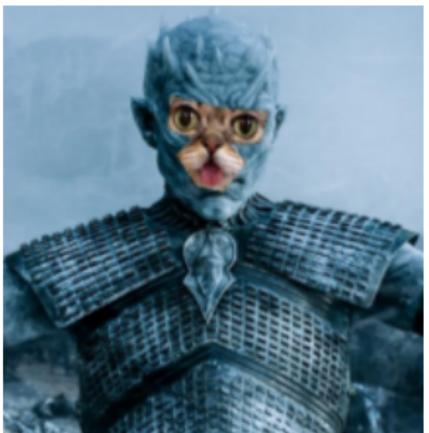


Overview of the practicals

Introduction to
Variational Methods
and Computer Vision

Yvain QUÉAU

Practical 2: Poisson Image Editing



Naive editing



Poisson editing

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Practical 3: Variational Image Segmentation



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