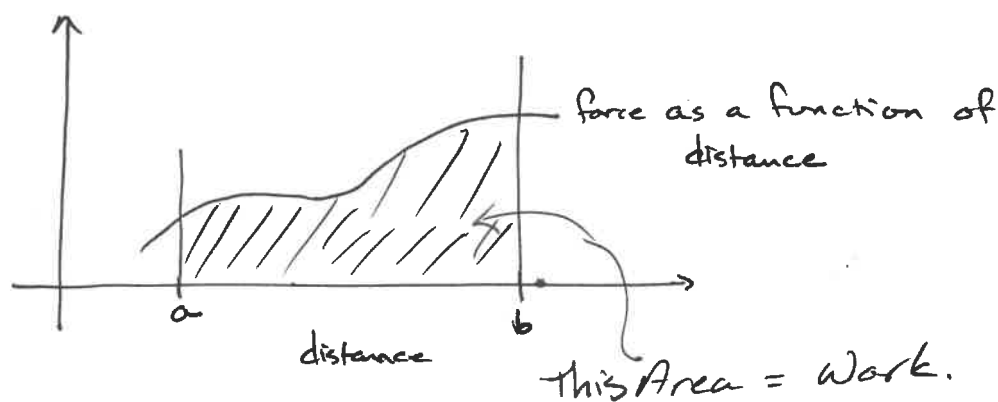


6.4 $Work = Force \cdot Distance$

if force is constant.

But, what if force is not constant? Then work equals force integrated with respect to distance:

$$\begin{array}{l} \text{Work} \\ \text{done in moving} \\ \text{object from } a \\ \text{to } b \end{array} = \int_a^b \text{force}(x) dx$$



Metric Units

$$\begin{aligned} F &= \text{Force} = \text{mass} \cdot \text{acceleration} \\ &= \text{kg} \cdot \text{m/sec}^2 \\ &= N = \text{Newton} = 1 \frac{\text{kg} \cdot \text{m}}{\text{sec}^2} \end{aligned}$$

$$d = \text{distance} = \text{meters}$$

$$\begin{aligned} W &= \text{work} = \text{Newton-meter} \\ &= J = \text{Joule} \end{aligned}$$

$$\begin{aligned} g &= \text{acceleration due to gravity} \\ &\quad \text{at Earth's surface} \\ &= 9.8 \text{ m/sec}^2 \end{aligned}$$

"English" Units

$$F = \text{force} = \text{pounds}$$

$$d = \text{distance} = \text{feet}$$

$$\begin{aligned} W &= \text{work} = \text{foot-pounds} \\ &= \text{ft} \cdot \text{lbs.} \end{aligned}$$

$$1 \text{ ft} \cdot \text{lb} \approx 1.36 \text{ J}$$

$$\begin{aligned} g &= \text{acceleration due to gravity} \\ &\quad \text{at Earth's surface} \\ &= 32 \text{ ft/sec}^2 \end{aligned}$$

6.4 WORK

$$\text{WORK} = \text{FORCE} \cdot \text{DISTANCE}$$

ex How much work is done in lifting a 2 pound book from the floor onto a 3 foot table?

$$\text{work} = (\text{force})(\text{distance})$$
$$\text{work} = (2 \text{ lbs})(3 \text{ feet})$$

$$= 6 \text{ ft-lbs.}$$

ex How much work is done in lifting a 12 kilogram dog onto a tall counter?

1.5 meter

$$\text{Work} = (\text{force})(\text{distance})$$

$$= (\text{mass} \cdot \text{acceleration})(\text{distance})$$

$$= (12 \text{ kg})(9.8 \text{ m/s}^2)(1.5 \text{ meters})$$

$$= (117.6 \text{ kg} \cdot \text{m/s}^2)(1.5 \text{ meters})$$

N = Newton!

$$= 176.4 \text{ N} \cdot \text{m}$$

J = Joule!

Notice!

In metric:

$$\text{Work} = \text{mass} \cdot \text{accel} \cdot \text{dist}$$

$$\text{J} = \text{kg} \cdot \frac{\text{m}}{\text{s}^2} \cdot \text{m}$$

In "English" units

$$\text{Work} = \text{force} \cdot \text{dist}$$

$$\text{ft-lbs} = \text{lbs} \cdot \text{ft}$$