

SCRUM Domain Optimization Model

From Entities, Relationships, Goals, Conditions, Decision Variables

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1 1. Sets (Entities)

- \mathcal{P} (Project): The product or initiative to be developed.
- \mathcal{T} (Team): Self-organized, cross-functional development team.
- \mathcal{W} (Worker/Employee): Individual team member working on the project. (*Alias “Employee” in relationships*)
- \mathcal{F} (Feature): Mid-sized functionality.
- \mathcal{S} (Skill): Professional or social competence of a worker.
- \mathcal{R} (Role): Defined responsibilities within the Scrum team.
- \mathcal{PO} (ProductOwner): Responsible for product vision and Product Backlog.
- \mathcal{SM} (ScrumMaster): Supports the team in applying Scrum.
- \mathcal{PB} (ProductBacklog): Ordered list of all requirements.
- \mathcal{SP} (Sprint): Fixed time period for creating an increment.
- \mathcal{SPP} (SprintPlanning): Kick-off meeting for Sprint preparation.
- \mathcal{DS} (DailyScrum): Daily 15-minute team meeting.
- \mathcal{SR} (SprintReview): Presentation and acceptance of results.
- \mathcal{SRE} (SprintRetrospective): Retrospective for process improvement.
- \mathcal{SBL} (SprintBacklog): Selected backlog items + implementation plan.
- \mathcal{SG} (SprintGoal): Objective to be achieved within the sprint.
- \mathcal{E} (Epic): Large requirement that can be split into stories.
- \mathcal{US} (UserStory): Requirement from the perspective of a user.
- \mathcal{TSK} (Task): Smallest unit of work within a sprint.
- \mathcal{DEV} (DevelopmentSnapshot): Product at the end of a sprint.
- \mathcal{BL} (Blocker): Obstacle hindering progress.
- \mathcal{SH} (Stakeholder): Interested party in the product.
- \mathcal{VEL} (Velocity): Average amount of work per sprint.
- \mathcal{REP} (ReleasePlan): Plan for releasing specific features.
- \mathcal{RM} (Roadmap): Long-term planning across releases.
- \mathcal{SCB} (ScrumBoard): Visual representation of tasks during the sprint.
- \mathcal{FED} (FeatureDocumentation): Documentation for a specific feature.

Relationship-induced feasibility subsets (from Relationships.csv)

- $\mathcal{T} \rightarrow \mathcal{P}$: allowed team–project assignments (R1).
- $\mathcal{W} \rightarrow \mathcal{T}$: allowed worker–team memberships (R2).
- $\mathcal{W} \rightarrow \mathcal{S}, \mathcal{W} \rightarrow \mathcal{R}$: worker–skill and worker–role links (R3,R4).
- $\mathcal{PO} \leftrightarrow \mathcal{PB}$: one-to-one (R5).
- $\mathcal{T} \leftrightarrow \mathcal{SM}$: one-to-one (R6).
- $\mathcal{PB} \rightarrow \mathcal{F}, \mathcal{PB} \rightarrow \mathcal{E}$: backlog contains features/epics (R7,R8).
- $\mathcal{E} \rightarrow \mathcal{US}$: epic contains user stories (R9).
- $\mathcal{US} \rightarrow \mathcal{TSK}$: user story consists of tasks (R10).
- $\mathcal{US} \leftrightarrow \mathcal{SBL}$: user story assigned to sprint backlog (many-to-many) (R11). Feasible pair set $\mathcal{A}_{US,SBL} \subseteq \mathcal{US} \times \mathcal{SBL}$.
- $\mathcal{SBL} \rightarrow \mathcal{SP}$: each sprint backlog belongs to one sprint (R12).
- $\mathcal{SP} \rightarrow \mathcal{SG}$: each sprint pursues one goal (R13).
- $\mathcal{SCB} \rightarrow \mathcal{TSK}$: board contains sprint tasks (R14).
- $\mathcal{FED} \leftrightarrow \mathcal{F}$: documentation belongs to feature (R15).
- $\mathcal{TSK} \leftrightarrow \mathcal{BL}$: tasks can be blocked by blockers (R16).
- $\mathcal{SH} \rightarrow \mathcal{SR}$: stakeholders participate in sprint reviews (R17).
- $\mathcal{SM} \rightarrow \mathcal{SRE}$: SM moderates retrospectives (R18).
- $\mathcal{VEL} \leftrightarrow \mathcal{T}$: velocity refers to team (R19).
- $\mathcal{REP} \rightarrow \mathcal{F}$: release plan includes features (R20). Feasible pair set $\mathcal{A}_{F,REP} \subseteq \mathcal{F} \times \mathcal{REP}$.
- $\mathcal{REP} \rightarrow \mathcal{RM}$: release plan is part of roadmap (R21).
- $\mathcal{SP} \rightarrow \mathcal{DEV}$: sprint generates development snapshot (R22).

2 2. Indices

- $p \in \mathcal{P}, t \in \mathcal{T}, w \in \mathcal{W}, f \in \mathcal{F}, s \in \mathcal{S}, r \in \mathcal{R}$.
- $po \in \mathcal{PO}, sm \in \mathcal{SM}, pb \in \mathcal{PB}, sp \in \mathcal{SP}, spp \in \mathcal{SPP}$.
- $ds \in \mathcal{DS}, sr \in \mathcal{SR}, sre \in \mathcal{SRE}, sbl \in \mathcal{SBL}, sg \in \mathcal{SG}$.
- $e \in \mathcal{E}, us \in \mathcal{US}, tsk \in \mathcal{TSK}, dev \in \mathcal{DEV}, bl \in \mathcal{BL}$.
- $sh \in \mathcal{SH}, v \in \mathcal{VEL}, rep \in \mathcal{REP}, rm \in \mathcal{RM}, scb \in \mathcal{SCB}, fed \in \mathcal{FED}$.

Parameters (selected attributes as numeric inputs) For each referenced entity attribute in Goals/Conditions we assume given nonnegative parameters:

- effort_{tsk} (Task.effort), priority_f (Feature.priority), severity_{bl} (Blocker.severity).
- $\overline{\text{storypts}}_{us}$ (UserStory.story_points), attendees_{sr} (SprintReview.attendees_count).
- milestones_{rm} (Roadmap.milestones), entries_{pb} (ProductBacklog.number_of_entries).
- avgSP_v , maxV_v , minV_v (Velocity.avg_story_points, max_velocity, min_velocity).
- goalach_{sg} (SprintGoal.achievement_status), sat_{sre} (SprintRetrospective.team_satisfaction).
- budgetCap_p (cap for Project.budget), $\text{statusActive}_p \in \{0, 1\}$ (Project.status).
- numTasks_{sbl} , capEffort_{sbl} (SprintBacklog.number_of_tasks, total_effort).
- cards_{scb} (ScrumBoard.number_of_cards), prio_f (Feature.priority).
- $\text{open}_{bl} \in \{0, 1\}$ (Blocker.status indicator “open”), $\text{done}_{tsk} \in \{0, 1\}$ (Task.status indicator “done”).
- avail_{po} (ProductOwner.availability).

Incidence/helper sets

- $\mathcal{A}_{US,SBL} \subseteq \mathcal{US} \times \mathcal{SBL}$ (feasible user story \leftrightarrow sprint backlog pairs).
- $\mathcal{A}_{F,REP} \subseteq \mathcal{F} \times \mathcal{REP}$ (feasible feature \leftrightarrow release plan pairs).
- $\mathcal{B}(tsk) = \{bl \in \mathcal{BL} : (tsk, bl) \text{ linked (R16)}\}$ (blockers of a task).

3 3. Goals

We aggregate multiple (min/max) goals into a single weighted objective:

$$\max Z = \sum_{g \in \mathcal{G}} \omega_g s_g G_g(\cdot),$$

where $\omega_g > 0$ is the weight from `Goals.csv`, $s_g = +1$ for `GoalType = max` and $s_g = -1$ for `GoalType = min`, and $G_g(\cdot)$ is the corresponding goal expression.

- **G0 maximize_total_story_points** (ID: G0)

Logical: Maximize total planned story points of user stories selected into any sprint backlog.

Mathematical:

$$G_0 = \sum_{(us, sbl) \in \mathcal{A}_{US,SBL}} \overline{\text{storypts}}_{us} x_{us, sbl}.$$

- **G1 minimize_total_task_effort** (ID: G1)

Logical: Minimize the aggregate estimated effort of tasks in scope.

Mathematical:

$$G_1 = \sum_{tsk \in \mathcal{TSK}} \text{effort}_{tsk}.$$

- **G2 maximize_sprint_goal_achievement** (ID: G2)

Logical: Maximize reported achievement of sprint goals.

Mathematical:

$$G_2 = \sum_{sg \in \mathcal{SG}} \text{goalach}_{sg}.$$

- **G3 minimize_blocker_severity** (ID: G3)

Logical: Reduce severity of blockers impacting work.

Mathematical:

$$G_3 = \sum_{bl \in \mathcal{BL}} \text{severity}_{bl}.$$

- **G4 maximize_delivery_of_high_priority_features** (ID: G4)

Logical: Favor inclusion of higher-priority features into releases.

Mathematical:

$$G_4 = \sum_{(f, rep) \in \mathcal{A}_{F, REP}} \text{priority}_f y_{f, rep}.$$

- **G5 maximize_velocity_average_story_points** (ID: G5)

Logical: Increase average velocity (story points) over observed sprints.

Mathematical:

$$G_5 = \sum_{v \in \mathcal{VEL}} \text{avgSP}_v.$$

- **G6 minimize_daily_scrum_time** (ID: G6)

Logical: Keep the total scheduled Daily Scrum time low.

Mathematical:

$$G_6 = \sum_{ds \in \mathcal{DS}} \text{durDS}_{ds},$$

where durDS_{ds} is the decision variable for Daily Scrum duration (see Section 5).

- **G7 minimize_wip_in_sprint_backlog** (ID: G7)

Logical: Reduce the number of tasks in each sprint backlog (proxy for WIP).

Mathematical:

$$G_7 = \sum_{sbl \in \mathcal{SBL}} \text{numTasks}_{sbl}.$$

- **G8 maximize_team_satisfaction** (ID: G8)

Logical: Maximize team satisfaction reported in retrospectives.

Mathematical:

$$G_8 = \sum_{sre \in \mathcal{SRE}} \text{sat}_{sre}.$$

- **G9 minimize_product_backlog_size** (ID: G9)

Logical: Keep the number of entries in the product backlog lean.

Mathematical:

$$G_9 = \sum_{pb \in \mathcal{PB}} \text{entries}_{pb}.$$

- **G10 maximize_release_feature_coverage** (ID: G10)

Logical: Maximize the number of features included across releases.

Mathematical:

$$G_{10} = \sum_{(f, rep) \in \mathcal{A}_{F, REP}} y_{f, rep}.$$

- **G11 maximize_roadmap_milestones** (ID: G11)

Logical: Maximize the milestones realized on the roadmap.

Mathematical:

$$G_{11} = \sum_{rm \in \mathcal{RM}} \text{milestones}_{rm}.$$

4 4. Conditions

All conditions apply simultaneously. When a condition naturally limits a decision variable it is stated as a hard constraint.

- **C0 project_status_active_only** (ID: C0)

Logical: Only projects with active status are considered.

Mathematical:

$$\forall p \in \mathcal{P} : \text{statusActive}_p = 1 \quad (\text{filter/feasibility}).$$

- **C1 budget_cannot_exceed_limit** (ID: C1)

Logical: Allocated budget per project must not exceed the approved cap.

Mathematical:

$$\forall p \in \mathcal{P} : \text{budget}_p \leq \text{budgetCap}_p.$$

- **C2 minimum_team_size** (ID: C2)

Logical: Teams must meet a minimum effective size.

Mathematical:

$$\forall t \in \mathcal{T} : \text{teamsize}_t \geq \underline{n}^{\text{team}} \quad (\text{here } \underline{n}^{\text{team}} = 3 \text{ from DV11 bounds}).$$

- **C3 maximum_daily_scrum_duration** (ID: C3)

Logical: Daily Scrum duration should not exceed the target.

Mathematical:

$$\forall ds \in \mathcal{DS} : \text{durDS}_{ds} \leq \overline{d}^{\text{DS}} \quad (\text{e.g., } \overline{d}^{\text{DS}} = 30 \text{ minutes from DV4}).$$

- **C4 po_availability_required** (ID: C4)

Logical: Product Owner availability must be present during sprint.

Mathematical:

$$\forall po \in \mathcal{PO} : \text{avail}_{po} \geq \underline{a}^{\text{PO}} \quad (\text{feasibility threshold}).$$

- **C5 scrum_master_experience_required** (ID: C5)

Logical: Scrum Master experience must meet a minimum.

Mathematical:

$$\forall sm \in \mathcal{SM} : \text{exp}_{sm} \geq \underline{e}^{\text{SM}} \quad (\text{feasibility threshold}).$$

- **C6 limit_wip_on_board** (ID: C6)

Logical: Number of cards on Scrum Board must not exceed its WIP cap.

Mathematical:

$$\forall scb \in \mathcal{SCB} : \text{cards}_{scb} \leq \text{wipcap}_{scb}.$$

- **C7 feature_effort_cap** (ID: C7)

Logical: Do not pull features above an effort threshold.

Mathematical:

$$\forall f \in \mathcal{F} : \text{estEffort}_f \leq \overline{E}^{\text{feat}} \quad (\text{feasibility threshold}).$$

- **C8 sprint_backlog_effort_cap** (ID: C8)

Logical: Total planned effort in a sprint backlog must stay within its capacity.

Mathematical (story-points proxy):

$$\forall sbl \in \mathcal{SBL} : \sum_{\substack{us \in \mathcal{US} \\ (us, sbl) \in \mathcal{A}_{US, SBL}}} \overline{\text{storypts}}_{us} x_{us, sbl} \leq \text{capEffort}_{sbl}.$$

- **C9 min_sprint_review_attendees** (ID: C9)
Logical: Sprint Review must have at least a minimum number of attendees.
Mathematical:

$$\forall sr \in \mathcal{SR} : \text{attendees}_{sr} \geq \underline{A}^{\text{SR}}.$$

- **C10 min_velocity_floor** (ID: C10)
Logical: Maintain a minimum team velocity across sprints.
Mathematical:

$$\forall v \in \mathcal{VEL} : \min V_v \geq \underline{V}.$$

- **C11 blocker_status_cannot_be_open_in_done** (ID: C11)
Logical: No open blockers are allowed on tasks marked “done”.
Mathematical (implication as linear constraint via big- M indicator):

$$\forall task \in \mathcal{TSK}, \forall bl \in \mathcal{B}(task) : \text{done}_{task} = 1 \Rightarrow \text{open}_{bl} = 0.$$

(In MILP one may encode $\text{open}_{bl} \leq 1 - \text{done}_{task}$.)

5. Decision Variables

- **DV0 assign_user_story_to_sprint:**
 $x_{us,sbl} \in \{0, 1\}$ for $(us, sbl) \in \mathcal{A}_{US,SBL}$ (assign user story to a sprint backlog).
- **DV1 select_feature_for_release:**
 $y_{f,rep} \in \{0, 1\}$ for $(f, rep) \in \mathcal{A}_{F,REP}$ (include feature in a release plan).
- **DV2 allocate_worker_to_team:**
 $a_{w,t} \in \{0, 1\}$ (assign worker to team for a sprint).
- **DV3 set_task_priority_level:**
 $\text{prioVar}_{task} \in \mathbb{Z}$ with $1 \leq \text{prioVar}_{task} \leq 5$.
- **DV4 schedule_daily_scrum_duration:**
 $\text{durDS}_{ds} \in \mathbb{Z}$ with $10 \leq \text{durDS}_{ds} \leq 30$ (minutes).
- **DV5 budget_allocation_per_project:**
 $\text{budget}_p \in \mathbb{R}_+$ with $0 \leq \text{budget}_p \leq 1,000,000$.
- **DV6 limit_wip_tasks_per_board:**
 $\text{wipcap}_{scb} \in \mathbb{Z}_+$ with $0 \leq \text{wipcap}_{scb} \leq 200$.
- **DV7 assign_scrum_master_to_team:**
 $z_{sm,t}^{SM} \in \{0, 1\}$ (Scrum Master to team).
- **DV8 prioritize_user_story:**
 $\pi_{us} \in \mathbb{Z}_+$ with $1 \leq \pi_{us} \leq 100$ (ordering rank).
- **DV9 estimate_story_points:**
 $\widehat{\text{SP}}_{us} \in \mathbb{Z}_+$ with $1 \leq \widehat{\text{SP}}_{us} \leq 13$ (planning estimate, if used in place of $\overline{\text{storypts}}_{us}$).
- **DV10 set_sprint_length_days:**
 $L_{sp} \in \mathbb{Z}_+$ with $7 \leq L_{sp} \leq 28$ (days).
- **DV11 set_team_size:**
 $\text{teamsize}_t \in \mathbb{Z}_+$ with $3 \leq \text{teamsize}_t \leq 12$.

Common logical/domain constraints

- Each user story assigned at most once:

$$\forall us \in \mathcal{US} : \sum_{\substack{ubl \in \mathcal{SBL} \\ (us,ubl) \in \mathcal{A}_{US,SBL}}} x_{us,ubl} \leq 1.$$

- Feature selection respects release feasibility:

$$\forall rep \in \mathcal{REP} : \sum_{\substack{f \in \mathcal{F} \\ (f,rep) \in \mathcal{A}_{F,REP}}} y_{f,rep} \leq \overline{N}_{rep}^{\text{feat}} \quad (\text{optional capacity}).$$

- Unique Scrum Master per team (if required):

$$\forall t \in \mathcal{T} : \sum_{sm \in \mathcal{SM}} z_{sm,t}^{SM} = 1.$$