Optimization Model for Agile Software Development using SCRUM

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1 Sets (Entities)

This section defines the fundamental sets of objects in the domain model, derived from Entities.csv.

- \mathcal{P} : Set of all Projects (E0)
- \mathcal{T} : Set of all Teams (E1)
- W: Set of all Workers (E2)
- \mathcal{F} : Set of all Features (E3)
- S: Set of all Skills (E4)
- \mathcal{R} : Set of all Roles (E5)
- \mathcal{PO} : Set of all Product Owners (E6)
- \mathcal{SM} : Set of all Scrum Masters (E7)
- \mathcal{PB} : Set of all Product Backlogs (E8)
- \mathcal{SP} : Set of all Sprints (E9)
- SPP: Set of all Sprint Plannings (E10)
- \mathcal{DS} : Set of all Daily Scrums (E11)
- \mathcal{SR} : Set of all Sprint Reviews (E12)
- \mathcal{SRE} : Set of all Sprint Retrospectives (E13)
- \mathcal{SBL} : Set of all Sprint Backlogs (E14)
- SG: Set of all Sprint Goals (E15)
- \mathcal{E} : Set of all Epics (E16)
- US: Set of all User Stories (E17)
- TSK: Set of all Tasks (E18)
- \mathcal{DEV} : Set of all Development Snapshots (E19)
- \mathcal{BL} : Set of all Blockers (E20)
- \mathcal{SH} : Set of all Stakeholders (E21)
- VEL: Set of all Velocity metrics (E22)
- \mathcal{REP} : Set of all Release Plans (E23)
- \mathcal{RM} : Set of all Roadmaps (E24)
- SCB: Set of all Scrum Boards (E25)
- \mathcal{FED} : Set of all Feature Documentations (E26)

2 Indices

This section defines the indices used to iterate over the sets defined above.

- $p \in \mathcal{P}$: Index for a Project
- $t \in \mathcal{T}$: Index for a Team
- $w \in \mathcal{W}$: Index for a Worker
- $f \in \mathcal{F}$: Index for a Feature
- $s \in \mathcal{S}$: Index for a Skill
- $us \in \mathcal{US}$: Index for a User Story
- $tsk \in TSK$: Index for a Task
- $sp \in \mathcal{SP}$: Index for a Sprint
- $rep \in \mathcal{REP}$: Index for a Release Plan

3 Decision Variables

This section defines the variables that the optimization model will solve for, derived from DecisionVariables.csv.

- **DV0** $(X_{us,sp})$: Binary variable, 1 if User Story us is assigned to Sprint sp, 0 otherwise.
- DV1 $(Y_{w,tsk})$: Binary variable, 1 if Worker w is assigned to Task tsk, 0 otherwise.
- DV2 $(A_{t,p})$: Binary variable, 1 if Team t is assigned to Project p, 0 otherwise.
- DV3 $(I_{f,rep})$: Binary variable, 1 if Feature f is included in Release Plan rep, 0 otherwise.
- **DV4** $(M_{w,t})$: Binary variable, 1 if Worker w is a member of Team t, 0 otherwise.
- DV5 (S_{sp}) : Integer variable representing the start day of Sprint sp.
- **DV6** (N_t) : Integer variable representing the number of members in Team t.
- DV7 (P_{us}) : Integer variable representing the assigned priority of User Story us.
- DV8 (C_w) : Continuous variable [0,1] representing the capacity allocation of Worker w.
- **DV9** (B_p) : Binary variable, 1 if Project p is active, 0 if on hold.
- **DV10** (D_{sp}): Integer variable representing the duration in days of Sprint sp.

4 Goals (Objective Functions)

This section translates the goals from Goals.csv into mathematical objective functions. We define parameters where necessary (e.g., $StoryPoints_{us}$ is the given story points value for User Story us).

• G0: maximize_story_points_in_sprint

$$\text{Maximize } \sum_{us \in \mathcal{US}} StoryPoints_{us} \cdot X_{us,sp} \quad \forall sp \in \mathcal{SP}$$

• G1: minimize_effort_for_features

$$Minimize \sum_{f \in \mathcal{F}} EstimatedEffort_f \cdot I_{f,rep} \quad \forall rep \in \mathcal{REP}$$

• G2: maximize_priority_of_user_stories

$$\text{Maximize} \sum_{us \in \mathcal{US}} \sum_{sp \in \mathcal{SP}} Priority_{us} \cdot X_{us,sp}$$

• G3: minimize_number_of_blockers

Minimize
$$\sum_{bl \in \mathcal{BL}} Active Status_{bl}$$

• G4: maximize_team_satisfaction

 $Maximize \ Team Satisfaction_{sre} \quad \forall sre \in \mathcal{SRE}$

• G5: maximize_sprint_goal_achievement

Maximize
$$AchievementStatus_{sg} \quad \forall sg \in \mathcal{SG}$$

• G6: minimize_project_timeline_slippage

$$Minimize (ActualEndDate_p - PlannedEndDate_p) \quad \forall p \in \mathcal{P}$$

• G7: maximize_feature_stakeholder_relevance

$$\text{Maximize} \sum_{f \in \mathcal{F}} \sum_{sh \in \mathcal{SH}} Relevance_{f,sh} \cdot Influence_{sh} \cdot I_{f,rep}$$

• G8: minimize_task_effort_variance

$$\operatorname{Minimize} \sum_{tsk \in \mathcal{TSK}} |ActualEffort_{tsk} - EstimatedEffort_{tsk}|$$

• G9: maximize_velocity_trend

Maximize
$$Trend_{vel} \quad \forall vel \in \mathcal{VEL}$$

• G10: maximize_skill_level_on_tasks

$$\text{Maximize} \sum_{w \in \mathcal{W}} \sum_{tsk \in \mathcal{TSK}} \sum_{s \in \mathcal{S}} SkillLevel_{w,s} \cdot TaskRequiresSkill_{tsk,s} \cdot Y_{w,tsk}$$

5 Conditions (Constraints)

This section translates the conditions from Conditions.csv into mathematical constraints.

• C0: constrain_sprint_capacity_by_velocity

$$\sum_{us \in \mathcal{US}} StoryPoints_{us} \cdot X_{us,sp} \leq Velocity_t \quad \forall sp \in \mathcal{SP} \text{ (where Team } t \text{ runs Sprint } sp)$$

• C1: constrain_worker_availability

$$\sum_{tsk \in \mathcal{TSK}} TaskEffort_{tsk} \cdot Y_{w,tsk} \leq Availability_w \quad \forall w \in \mathcal{W}$$

• C2: enforce_minimum_team_size

$$N_t > 3 \quad \forall t \in \mathcal{T}$$

• C3: enforce_maximum_team_size

$$N_t < 9 \quad \forall t \in \mathcal{T}$$

• C4: require_mandatory_product_owner

$$\sum_{w \in \mathcal{PO}} M_{w,t} = 1 \quad \forall t \in \mathcal{T}$$

• C5: require_mandatory_scrum_master

$$\sum_{w \in SM} M_{w,t} = 1 \quad \forall t \in \mathcal{T}$$

• C6: prevent_assignment_of_inactive_workers Let $W_{inactive} = \{w \in W \mid Status_w = \text{'inactive'}\}$

$$\sum_{tsk \in \mathcal{TSK}} Y_{w,tsk} = 0 \quad \forall w \in \mathcal{W}_{inactive}$$

• C7: require_sprint_goal

$$\sum_{sg \in \mathcal{SG}} BelongsToSprint_{sg,sp} = 1 \quad \forall sp \in \mathcal{SP}$$

• C8: task_must_belong_to_sprint_user_story

$$Y_{w,tsk} \leq X_{us,sp} \quad \forall w, tsk, us, sp \text{ (where Task } tsk \text{ belongs to US } us)$$

• C9: budget_must_not_be_exceeded

$$\sum_{t \in \mathcal{T}} Cost_t + \sum_{\text{other}} OtherCosts \leq Budget_p \quad \forall p \in \mathcal{P}$$

• C10: epic_cannot_be_in_sprint_backlog No decision variable exists for assigning epics to sprints, enforcing this implicitly.

$$X_{e,sp}$$
 is undefined and assumed to be $0 \quad \forall e \in \mathcal{E}, sp \in \mathcal{SP}$

• C11: certified_skill_for_critical_tasks Let $TSK_{crit} = \{tsk \in TSK \mid Type_{tsk} = \text{`critical'}\}$

$$Y_{w,tsk} \cdot (1 - IsCertified_{w,s}) = 0 \quad \forall w \in \mathcal{W}, tsk \in \mathcal{TSK}_{crit}, s \in \mathcal{S}$$

• C12: feature_must_have_documentation

$$I_{f,rep} \leq \exists fed \in \mathcal{FED} \text{ s.t. } Documents_{fed,f} \quad \forall f \in \mathcal{F}, rep \in \mathcal{REP}$$