

# Sprint Planning and Delivery Optimization Model (SCRUM Domain)

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## 1 1. Sets (Entities)

- $\mathcal{P}$  = Projects (Entity: **Project**)
- $\mathcal{T}$  = Teams (Entity: **Team**)
- $\mathcal{W}$  = Workers (Entity: **Worker**)
- $\mathcal{F}$  = Features (Entity: **Feature**)
- $\mathcal{S}$  = Skills (Entity: **Skill**)
- $\mathcal{R}$  = Roles (Entity: **Role**)
- $\mathcal{PO}$  = Product Owners (Entity: **ProductOwner**)
- $\mathcal{SM}$  = Scrum Masters (Entity: **ScrumMaster**)
- $\mathcal{PB}$  = Product Backlogs (Entity: **ProductBacklog**)
- $\mathcal{SP}$  = Sprints (Entity: **Sprint**)
- $\mathcal{SPP}$  = Sprint Plannings (Entity: **SprintPlanning**)
- $\mathcal{DS}$  = Daily Scrums (Entity: **DailyScrum**)
- $\mathcal{SR}$  = Sprint Reviews (Entity: **SprintReview**)
- $\mathcal{SRE}$  = Sprint Retrospectives (Entity: **SprintRetrospective**)
- $\mathcal{SBL}$  = Sprint Backlogs (Entity: **SprintBacklog**)
- $\mathcal{SG}$  = Sprint Goals (Entity: **SprintGoal**)
- $\mathcal{E}$  = Epics (Entity: **Epic**)
- $\mathcal{US}$  = User Stories (Entity: **UserStory**)
- $\mathcal{TSK}$  = Tasks (Entity: **Task**)
- $\mathcal{DEV}$  = Development Snapshots (Entity: **DevelopmentSnapshot**)
- $\mathcal{BL}$  = Blockers (Entity: **Blocker**)
- $\mathcal{SH}$  = Stakeholders (Entity: **Stakeholder**)
- $\mathcal{VEL}$  = Velocities (Entity: **Velocity**)
- $\mathcal{REP}$  = Release Plans (Entity: **ReleasePlan**)
- $\mathcal{RM}$  = Roadmaps (Entity: **Roadmap**)
- $\mathcal{SCB}$  = Scrum Boards (Entity: **ScrumBoard**)
- $\mathcal{FED}$  = Feature Documentations (Entity: **FeatureDocumentation**)

### Relationship-induced index maps (from Relationships.csv).

- $U(s) \subseteq \mathcal{US}$ : user stories contained in epic  $s \in \mathcal{E}$  (R9).
- $K(u) \subseteq \mathcal{TSK}$ : tasks belonging to user story  $u \in \mathcal{US}$  (R10).
- $B(u) \subseteq \mathcal{SBL}$ : sprint backlogs that include user story  $u$  (R11).
- $S(sp) \in \mathcal{SBL}$ : the sprint backlog of sprint  $sp$  (R12).
- $G(sp) \in \mathcal{SG}$ : the goal pursued by sprint  $sp$  (R13).
- $L(scb) \subseteq \mathcal{TSK}$ : tasks on scrum board  $scb$  (R14).
- $D(sp) \in \mathcal{DEV}$ : snapshot generated by sprint  $sp$  (R22).
- $H(rep) \subseteq \mathcal{F}$ : features planned in release plan  $rep$  (R20).

## 2 2. Indices

- $p \in \mathcal{P}, t \in \mathcal{T}, w \in \mathcal{W}, f \in \mathcal{F}, s \in \mathcal{S}, r \in \mathcal{R}$ .
- $po \in \mathcal{PO}, sm \in \mathcal{SM}, pb \in \mathcal{PB}, sp \in \mathcal{SP}$ .
- $spp \in \mathcal{SPP}, ds \in \mathcal{DS}, sr \in \mathcal{SR}, sre \in \mathcal{SRE}$ .
- $sbl \in \mathcal{SBL}, g \in \mathcal{SG}, e \in \mathcal{E}, u \in \mathcal{US}, k \in \mathcal{TSK}$ .
- $d \in \mathcal{DEV}, b \in \mathcal{BL}, sh \in \mathcal{SH}, v \in \mathcal{VEL}, rep \in \mathcal{REP}, rm \in \mathcal{RM}, scb \in \mathcal{SCB}, fed \in \mathcal{FED}$ .

### Data parameters from Entities.csv (attributes).

- $sp(u) \in \mathbb{Z}_{\geq 0}$ : story points of user story  $u$  (`UserStory.story_points`).
- $stat^{US}(u) \in \{0, 1\}$ : eligibility/status mask for user story  $u$  (`UserStory.status`).
- $eff(k) \in \mathbb{Z}_{\geq 0}$ : effort of task  $k$  (`Task.effort`);  $type(k)$  is its type.
- $stat^{TSK}(k) \in \{0, 1\}$ : task status mask (1 = allowed).
- $sev(b) \in \mathbb{Z}_{\geq 0}$ : blocker severity (`Blocker.severity`);  $act(b) \in \{0, 1\}$  active mask.
- $prio(f) \in \mathbb{Z}_{\geq 0}$ : feature priority (`Feature.priority`).
- $rel(sh) \in \mathbb{Z}_{\geq 0}$ : stakeholder relevance to feature (`Stakeholder.relevance_to_feature`).
- $infl(sh) \in \mathbb{Z}_{\geq 0}$ : stakeholder influence (`Stakeholder.influence_level`).
- $ach(g) \in [0, 1]$ : sprint goal achievement status (`SprintGoal.achievement_status`).
- $\overline{SP} \in \mathbb{Z}_{\geq 0}$ : reference average story points (`Velocity.avg_story_points`).
- $nb(pb) \in \mathbb{Z}_{\geq 0}$ : number of entries in product backlog (`ProductBacklog.number_of_entries`).
- $bud(p) \in \mathbb{R}_{\geq 0}$ : project budget (`Project.budget`).
- $tst(d) \in [0, 1]$ : snapshot test status (`DevelopmentSnapshot.test_status`).
- $avail(w) \in \mathbb{R}_{\geq 0}$ : worker availability fraction (`Worker.availability`).

### 3. Goals

We aggregate the multiple goals from `Goals.csv` via a weighted-sum objective. Let  $w_i$  denote each goal's weight. For goals of type `max`, we minimize the negative of their measure.

**Decision variables (used by goals/constraints).** See Section 5 for domains; here we recall symbols:

$$x_u \in \{0, 1\} \forall u \in \mathcal{US}; \quad x_k \in \{0, 1\} \forall k \in \mathcal{TSK}; \quad z_f \in \{0, 1\} \forall f \in \mathcal{F}; \quad y_{w,k} \in \{0, 1\} \forall w \in \mathcal{W}, k \in \mathcal{TSK};$$

$$s^{SP}, s^{CAP}, e^{BUF} \in \mathbb{Z}_{\geq 0}; \quad b_b \in \{0, 1\} \forall b \in \mathcal{BL}; \quad v^{TGT}, a^{COV}, r^{RISK} \in [0, 1]; \quad p^{TH} \in \mathbb{Z}_{\geq 0}.$$

#### Objective

$$\begin{aligned} \min J = & \underbrace{w_0 \sum_{u \in \mathcal{US}} \text{sp}(u) x_u}_{\text{G0: minimize\_total\_story\_points}} + \underbrace{w_1 \sum_{k \in \mathcal{TSK}} \text{eff}(k) x_k}_{\text{G1: minimize\_total\_task\_effort}} - \underbrace{w_2 \sum_{g \in \mathcal{SG}} \text{ach}(g)}_{\text{G2: maximize\_sprint\_goal\_achievement}} \\ & + \underbrace{w_4 \sum_{b \in \mathcal{BL}} \text{sev}(b) \text{act}(b) (1 - b_b)}_{\text{G4: minimize\_open\_blocker\_severity}} + \underbrace{w_5 \sum_{pb \in \mathcal{PB}} \text{nb}(pb)}_{\text{G5: minimize\_product\_backlog\_size}} - \underbrace{w_6 \sum_{sh \in \mathcal{SH}} \text{rel}(sh)}_{\text{G6: maximize\_stakeholder\_relevance}} \\ & + \underbrace{w_7 \sum_{p \in \mathcal{P}} \text{bud}(p)}_{\text{G7: minimize\_project\_budget}} - \underbrace{w_8 \sum_{d \in \mathcal{DEV}} \text{tst}(d)}_{\text{G8: maximize\_test\_status}} - \underbrace{w_9 \sum_{w \in \mathcal{W}} \text{avail}(w)}_{\text{G9: maximize\_team\_availability}} \\ & + \underbrace{w_{10} \left( \sum_{\text{sbl} \in \mathcal{SBL}} \text{TotEff}(\text{sbl}) \right)}_{\text{G10: minimize\_sprint\_backlog\_total\_effort}} - \underbrace{w_{11} \sum_{f \in \mathcal{F}} \text{prio}(f) z_f}_{\text{G11: maximize\_feature\_priority\_delivery}} \end{aligned}$$

where  $\text{TotEff}(\text{sbl}) := \sum_{k \in L(\text{scb}): \text{scb} \leftrightarrow \text{sbl}} \text{eff}(k) x_k$  is the total effort represented for a sprint backlog via its scrum board (R14,R12). Weights ( $w_i$ ) come from `Goals.csv`.

#### Goal items (IDs, Names, representations).

- **G0 (minimize\_total\_story\_points):**  $\min \sum_u \text{sp}(u) x_u$
- **G1 (minimize\_total\_task\_effort):**  $\min \sum_k \text{eff}(k) x_k$
- **G2 (maximize\_sprint\_goal\_achievement):**  $\max \sum_g \text{ach}(g) \equiv \min - \sum_g \text{ach}(g)$
- **G3 (maximize\_average\_velocity):**  $\max \overline{\text{SP}} \equiv \min - \overline{\text{SP}}$
- **G4 (minimize\_open\_blocker\_severity):**  $\min \sum_b \text{sev}(b) \text{act}(b) (1 - b_b)$
- **G5 (minimize\_product\_backlog\_size):**  $\min \sum_{pb} \text{nb}(pb)$
- **G6 (maximize\_stakeholder\_relevance):**  $\max \sum_{sh} \text{rel}(sh) \equiv \min - \sum_{sh} \text{rel}(sh)$
- **G7 (minimize\_project\_budget):**  $\min \sum_p \text{bud}(p)$
- **G8 (maximize\_test\_status):**  $\max \sum_d \text{tst}(d) \equiv \min - \sum_d \text{tst}(d)$
- **G9 (maximize\_team\_availability):**  $\max \sum_w \text{avail}(w) \equiv \min - \sum_w \text{avail}(w)$
- **G10 (minimize\_sprint\_backlog\_total\_effort):**  $\min \sum_{\text{sbl}} \text{TotEff}(\text{sbl})$
- **G11 (maximize\_feature\_priority\_delivery):**  $\max \sum_f \text{prio}(f) z_f \equiv \min - \sum_f \text{prio}(f) z_f$

## 4 4. Conditions

Let  $M$  be a sufficiently large constant (Big-M) when needed. The following constraints implement `Conditions.csv` and respect `Relationships.csv`.

### Feasibility, selection, and linkage

- **Link tasks to user stories (R10):**  $\forall u \in \mathcal{US}, \forall k \in K(u) : x_k \leq x_u$ .
- **Sprint capacity (definition):**

$$s^{SP} = \sum_{u \in \mathcal{US}} \text{sp}(u) x_u, \quad \sum_{k \in \mathcal{TSK}} \text{eff}(k) x_k \leq s^{CAP} + e^{BUF}.$$

- **Task assignment feasibility:**  $\forall k \in \mathcal{TSK} : \sum_{w \in \mathcal{W}} y_{w,k} = x_k$ .
- **Worker availability limit:**  $\forall w \in \mathcal{W} : \sum_{k \in \mathcal{TSK}} \text{eff}(k) y_{w,k} \leq \text{AvailEff}(w)$ , where  $\text{AvailEff}(w)$  is derived from `Worker.availability`.
- **Release-feature link (R20):**  $\forall f \in \mathcal{F} : z_f \leq \mathbf{1}\{f \in H(\text{rep})\}$ .

### Condition items (IDs, Names, representations)

- **C0 (user\_stories\_must\_be\_ready):**  $\forall u : x_u \leq \text{stat}^{US}(u)$  (must-match readiness mask).
- **C1 (tasks\_cannot\_be\_blocked):**  $\forall k : x_k \leq \text{stat}^{TSK}(k)$  (cannot select blocked tasks).
- **C2 (only\_available\_workers):**  $\forall w : \sum_k \text{eff}(k) y_{w,k} \leq \text{AvailEff}(w)$ .
- **C3 (sprint\_goal\_may\_match):** prefer higher  $\text{ach}(g)$  via objective (soft preference; no hard constraint).
- **C4 (blockers\_must\_be\_low\_severity):**  $\forall b : \text{sev}(b) > \tau^{BL} \Rightarrow b_b = 0$ ; equivalently  $b_b \leq \mathbf{1}\{\text{sev}(b) \leq \tau^{BL}\}$ .
- **C5 (features\_may\_match\_high\_priority):** soft preference by objective; optionally enforce  $z_f = 0$  if  $\text{prio}(f) < p^{TH}$ .
- **C6 (product\_backlog\_status\_must\_match):**  $\forall pb : \text{stat}^{PB}(pb) = 1$  required; infeasible otherwise (data pre-filter).
- **C7 (sprint\_status\_must\_match):**  $\forall \text{sp} : \text{stat}^{SP}(\text{sp}) = 1$  required; else no planning on that sprint.
- **C8 (dev\_snapshot\_must\_match\_test\_status):**  $\forall d : \text{tst}(d) \geq a^{COV}$ .
- **C9 (stakeholder\_may\_match\_high\_influence):** soft preference by objective using  $\text{infl}(sh)$ .
- **C10 (sprint\_backlog\_status\_must\_match):**  $\forall \text{sbl} : \text{stat}^{SBL}(\text{sbl}) = 1$  precondition to commit tasks.
- **C11 (task\_type\_cannot\_match\_excluded):**  $\forall k : \mathbf{1}\{\text{type}(k) \in \mathcal{X}^{EXCL}\} = 1 \Rightarrow x_k = 0$ .

### Additional structure from relationships

- **Blockers on tasks (R16):** If task  $k$  is blocked by any  $b \in \mathcal{BL}$  not resolved in sprint, then  $x_k \leq b_b$  for each linked blocker; equivalently  $x_k \leq \min_{b \in \mathcal{B}(k)} b_b$ .
- **Sprint backlog linkage (R11,R12):** User stories planned for sprint backlog  $\text{sbl}$  satisfy  $x_u \leq \mathbf{1}\{u \in \text{sbl}\}$  and  $\text{sbl} = S(\text{sp})$  for the active sprint.

## 5. Decision Variables

- **DV0** (**x\_us\_selected**):  $x_u \in \{0, 1\}$  for  $u \in \mathcal{US}$  — select user story in sprint.
- **DV1** (**x\_task\_selected**):  $x_k \in \{0, 1\}$  for  $k \in \mathcal{TSK}$  — select task in sprint backlog.
- **DV2** (**z\_feature\_in\_release**):  $z_f \in \{0, 1\}$  for  $f \in \mathcal{F}$  — include feature in release plan.
- **DV3** (**y\_worker\_task\_assignment**):  $y_{w,k} \in \{0, 1\}$  — assign worker  $w$  to task  $k$ .
- **DV4** (**s\_story\_points\_committed**):  $s^{SP} \in \mathbb{Z}_{\geq 0}$  — total committed story points (min 0, max by data).
- **DV5** (**s\_sprint\_capacity**):  $s^{CAP} \in \mathbb{Z}_{\geq 0}$  — estimated capacity in story points (bounded by team velocity).
- **DV6** (**e\_effort\_buffer**):  $e^{BUF} \in \mathbb{Z}_{\geq 0}$  — buffer for unplanned work.
- **DV7** (**b\_blocker\_resolved**):  $b_b \in \{0, 1\}$  for  $b \in \mathcal{BL}$  — resolve blocker in sprint.
- **DV8** (**v\_target\_velocity**):  $v^{TGT} \in \mathbb{R}_{\geq 0}$  — planning target velocity.
- **DV9** (**a\_test\_coverage\_target**):  $a^{COV} \in [0, 1]$  — minimum acceptable test/snapshot status.
- **DV10** (**p\_priority\_threshold**):  $p^{TH} \in \mathbb{Z}_{\geq 0}$  — cutoff priority for features/stories.
- **DV11** (**r\_risk\_tolerance**):  $r^{RISK} \in [0, 1]$  — allowable normalized risk level.

**Model type.** With the above binary/integer/continuous variables and linear expressions, the model is a Mixed-Integer Linear Program (MILP). Weighted multi-objective handling is via scalarization in Section 3.