

# Optimization Model for SCRUM-based Software Development

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## Entities

Let the following sets represent core entities in the model:

- $P$ : Set of Projects
- $T$ : Set of Teams
- $E$ : Set of Employees
- $F$ : Set of Features
- $S$ : Set of Skills
- $R$ : Set of Roles
- $PO$ : Set of Product Owners
- $SM$ : Set of Scrum Masters
- $PB$ : Set of Product Backlogs
- $SP$ : Set of Sprints
- $EP$ : Set of Epics
- $US$ : Set of User Stories
- $TS$ : Set of Tasks / Sub-Tasks
- $BL$ : Set of Blockers
- $SH$ : Set of Stakeholders
- $V$ : Set of Velocity records

## Decision Variables

$$\begin{aligned}x_{e,t} &= \begin{cases} 1 & \text{if employee } e \in E \text{ is assigned to team } t \in T \\ 0 & \text{otherwise} \end{cases} \\y_{us,sp} &= \begin{cases} 1 & \text{if user story } us \in US \text{ is assigned to sprint } sp \in SP \\ 0 & \text{otherwise} \end{cases} \\a_{ts,e} &= \begin{cases} 1 & \text{if task } ts \in TS \text{ is assigned to employee } e \in E \\ 0 & \text{otherwise} \end{cases} \\v_t &\in \mathbb{Z}^+ \\b_p &\in \mathbb{R}^+ \\d_{sp} &\in \mathbb{Z}^+ \\\alpha_e &\in [0, 1]\end{aligned}$$

Velocity of team  $t \in T$   
Budget allocated to project  $p \in P$   
Duration of sprint  $sp \in SP$   
Availability of employee  $e \in E$

## Objective Function

Maximize overall project efficiency:

$$\max \sum_{t \in T} v_t - \sum_{p \in P} b_p - \sum_{bl \in BL} \text{severity}_{bl}$$

## Constraints

$\sum_{e \in E} x_{e,t} \leq 9 \quad \forall t \in T$	(C1: Team Size Limit)
$a_{ts,e} \leq \text{skill\_match}(ts, e) \quad \forall ts \in TS, e \in E$	(C2: Skill Matching)
$\sum_{sp \in SP_p} 1 \leq 8 \quad \forall p \in P$	(C3: Max Sprints per Project)
$\text{sprint\_goal\_defined}(sp) = 1 \quad \forall sp \in SP$	(C4: Sprint Goal Alignment)
$\text{daily\_scrum\_duration} \leq 15$	(C5: Daily Scrum Duration Limit)
$\text{effort}_{ts} \leq 8 \quad \forall ts \in TS$	(C6: Task Effort Limit)
$a_{ts,e} \leq \alpha_e \quad \forall ts \in TS, e \in E$	(C7: Employee Availability)
$\text{moderated}(\text{retro}) = 1 \quad \forall \text{retro} \in \text{Retrospectives}$	(C8: Retrospective Moderation)
$\text{doc\_linked}(f) = 1 \quad \forall f \in F$	(C9: Documentation Completeness)
$\text{resolve\_time}(bl) \leq 3 \quad \forall bl \in BL$	(C10: Blocker Resolution Time)

## Notes

- Constraints and objective functions are aligned with goals and conditions, ensuring optimal SCRUM process efficiency.
- Each variable and constraint corresponds to a real-world relationship or attribute in the domain model.