

SCRUM-Based Software Development Optimization Model

Domain Modeling System

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1. Sets (Entities)

\mathcal{P} : Set of Projects (*E0*)

\mathcal{T} : Set of Teams (*E1*)

\mathcal{W} : Set of Workers (*E2*)

\mathcal{F} : Set of Features (*E3*)

\mathcal{S} : Set of Skills (*E4*)

\mathcal{R} : Set of Roles (*E5*)

\mathcal{PO} : Set of Product Owners (*E6*)

\mathcal{SM} : Set of Scrum Masters (*E7*)

\mathcal{PB} : Set of Product Backlogs (*E8*)

\mathcal{SP} : Set of Sprints (*E9*)

\mathcal{US} : Set of User Stories (*E17*)

\mathcal{TSK} : Set of Tasks (*E18*)

\mathcal{BL} : Set of Blockers (*E20*)

\mathcal{SH} : Set of Stakeholders (*E21*)

\mathcal{VEL} : Set of Velocity records (*E22*)

\mathcal{REP} : Set of Release Plans (*E23*)

\mathcal{RM} : Set of Roadmaps (*E24*)

\mathcal{DEV} : Set of Development Snapshots (*E19*)

\mathcal{FED} : Set of Feature Documentations (*E26*)

2. Indices

$p \in \mathcal{P}$: Index for projects

$t \in \mathcal{T}$: Index for teams

$w \in \mathcal{W}$: Index for workers

$f \in \mathcal{F}$: Index for features

$s \in \mathcal{S}$: Index for skills

$r \in \mathcal{R}$: Index for roles

$sp \in \mathcal{SP}$: Index for sprints

$u \in \mathcal{US}$: Index for user stories

$k \in \mathcal{TSK}$: Index for tasks

$b \in \mathcal{BL}$: Index for blockers

$sh \in \mathcal{SH}$: Index for stakeholders

$v \in \mathcal{VEL}$: Index for velocity entries

$rp \in \mathcal{REP}$: Index for release plans

3. Goals

maximize_project_budget: $\max \sum_{p \in \mathcal{P}} \text{budget}_p \times 1.5$
 minimize_project_duration: $\min \sum_{p \in \mathcal{P}} (\text{project_end}_p - \text{project_start}_p) \times 1.2$
 maximize_team_size: $\max \sum_{t \in \mathcal{T}} \text{team_size}_t \times 1.0$
 minimize_worker_unavailability: $\min \sum_{w \in \mathcal{W}} I(\text{status}_w = \text{"unavailable"}) \times 1.3$
 maximize_feature_priority: $\max \sum_{f \in \mathcal{F}} \text{priority}_f \times 1.4$
 minimize_effort_estimation: $\min \sum_{f \in \mathcal{F}} \text{estimated_effort}_f \times 1.1$
 maximize_story_points: $\max \sum_{u \in \mathcal{US}} \text{story_points}_u \times 1.6$
 minimize_sprint_duration: $\min \sum_{sp \in \mathcal{SP}} (\text{end_date}_{sp} - \text{start_date}_{sp}) \times 1.0$
 maximize_velocity_trend: $\max \sum_{v \in \mathcal{VEL}} \text{trend}_v \times 1.7$
 minimize_blocker_severity: $\min \sum_{b \in \mathcal{BL}} \text{severity}_b \times 1.3$
 maximize_stakeholder_influence: $\max \sum_{sh \in \mathcal{SH}} \text{influence_level}_{sh} \times 1.2$
 minimize_task_effort: $\min \sum_{k \in \mathcal{TSK}} \text{effort}_k \times 1.1$
 maximize_release_inclusion: $\max \sum_{rp \in \mathcal{REP}} |\text{included_features}_{rp}| \times 1.4$
 minimize_documentation_age: $\min \sum_{f \in \mathcal{FED}} (\text{current_time} - \text{creation_date}_f) \times 1.0$

4. Conditions

require_project_status_active: $\forall p \in \mathcal{P} : \text{status}_p = \text{"active"}$
 require_team_status_active: $\forall t \in \mathcal{T} : \text{team_status}_t = \text{"active"}$
 require_worker_availability: $\forall w \in \mathcal{W} : \text{availability}_w > 0$
 require_feature_status_not_done: $\forall f \in \mathcal{F} : \text{status}_f \neq \text{"done"}$
 require_user_story_status_todo: $\forall u \in \mathcal{US} : \text{status}_u = \text{"To Do"}$
 require_sprint_status_planned: $\forall sp \in \mathcal{SP} : \text{status}_{sp} = \text{"planned"}$
 require_task_status_not_blocked: $\forall k \in \mathcal{TSK} : \text{status}_k \neq \text{"blocked"}$
 require_blocker_resolved: $\forall b \in \mathcal{BL} : \text{resolved_on}_b \leq \text{current_date}$
 require_skill_certified: $\forall s \in \mathcal{S} : \text{certified}_s = \text{True}$
 require_role_assigned: $\forall w \in \mathcal{W}, \exists r \in \mathcal{R} : \text{takes_on_role}(w, r)$
 require_velocity_positive: $\forall v \in \mathcal{VEL} : \text{avg_story_points}_v > 0$
 require_sprint_goal_defined: $\forall sp \in \mathcal{SP}, \exists g \in \mathcal{SG} : \text{pursues_goal}(sp, g) \wedge \text{objective_description}_g \neq \emptyset$
 require_release_status_draft: $\forall rp \in \mathcal{REP} : \text{status}_{rp} = \text{"draft"}$
 require_board_updated_daily: $\forall t \in \mathcal{T} : \text{last_updated}_{\text{scb}(t)} \geq \text{current_date} - 1$

5. Decision Variables

$x_{w,t} \in \{0, 1\}$: Worker w assigned to team t

$y_f \in \{0, 1\}$: Feature f selected for backlog

$z_u \in \{0, 1\}$: User story u included in sprint

$e_k \in [0, 40]$: Estimated effort for task k

$d_{sp} \in [1, 30]$: Duration of sprint sp in days

$s_u \in [1, 13]$: Story points assigned to user story u

$b_p \in [0, 10^6]$: Budget allocated to project p

$st_{sp} \in [0, 365]$: Start day of sprint sp

$m_t \in [1, 20]$: Size of team t

$m_{sm,sp} \in \{0, 1\}$: Scrum Master moderates retrospective of sprint sp

$r_b \in [0, 30]$: Days taken to resolve blocker b

$d_f \in \{0, 1\}$: Documentation for feature f updated

$v_{target} \in [0, 100]$: Target velocity for next sprint

$rd_{rp} \in [0, 730]$: Release date of plan rp in days from start

$mpo_{po} \in \{0, 1\}$: Product Owner po actively manages backlog