**Lemma.** In SRLC1 (Section 5.3 and Algorithm 7), the chosen m fulfills  $m = O\left(\kappa \log^2{(\kappa)} \log{(\epsilon_F^{-1})}\right)$ .

The expression used to choose m (Algorithm 7, GenParams, line 2) can be bounded as follows:

Since  $0 < \epsilon_F < 1$  and  $1 < \kappa$ , we have:

$$1 - \prod_{i=1}^{\kappa} \left( 1 - \left( 1 - \frac{3}{\kappa} \right)^{m-i+1} \right)$$

$$\leq 1 - \prod_{i=1}^{\kappa} \left( 1 - \left( 1 - \frac{3}{\kappa} \right)^{m-\kappa+1} \right)$$

$$\leq 1 - \left( 1 - \kappa \left( 1 - \frac{3}{\kappa} \right)^{m-\kappa+1} \right)$$

$$= 1 - \left( 1 - \left( 1 - \frac{3}{\kappa} \right)^{m-\kappa+1} \right)^{\kappa}$$

$$\leq \kappa \left( 1 - \frac{3}{\kappa} \right)^{m-\kappa}$$

Therefore,  $\kappa(1-\frac{3}{\kappa})^{m-\kappa} \leq \epsilon$  suffices for the expression in GenParams to be fulfilled.

We also have:

$$\kappa \left(1 - \frac{3}{\kappa}\right)^{m-\kappa} \leq \epsilon_{F}$$

$$\Leftrightarrow \log\left(\kappa \left(1 - \frac{3}{\kappa}\right)^{m-\kappa}\right) \leq \log\left(\epsilon_{F}\right)$$

$$\Leftrightarrow \log\left(\kappa\right) + (m - \kappa)\log\left(1 - \frac{3}{\kappa}\right) \leq \log\left(\epsilon_{F}\right)$$

$$\Leftrightarrow m\log\left(1 - \frac{3}{\kappa}\right) \leq \log\left(\epsilon_{F}\right) - \log\left(\kappa\right) + \kappa\log\left(1 - \frac{3}{\kappa}\right)$$

$$\Leftrightarrow m \geq \frac{\log\left(\epsilon_{F}/\kappa\right)}{\log\left(1 - \frac{3}{\kappa}\right)} + \kappa$$

$$\Leftrightarrow m \geq \frac{-\log\left(\epsilon_{F}/\kappa\right)}{-\log\left(1 - \frac{3}{\kappa}\right)} + \kappa$$

$$\Leftrightarrow m \geq \frac{\log\left(\epsilon_{F}/\kappa\right)}{-\log\left(1 - \frac{3}{\kappa}\right)} + \kappa$$

$$\Leftrightarrow m \geq \frac{\log\left(\epsilon_{F}/\kappa\right)}{-\log\left(1 - \frac{3}{\kappa}\right)} + \kappa$$

Since  $\frac{\log(\epsilon_F^{-1}\kappa)}{-\log(1-\frac{3}{\kappa})} = O\left(\kappa\log^2(\kappa)\log(\epsilon_F^{-1})\right)$  and we choose the smallest m possible for algorithm 7, we get  $m = O\left(\kappa\log^2(\kappa)\log(\epsilon_F^{-1})\right)$ .