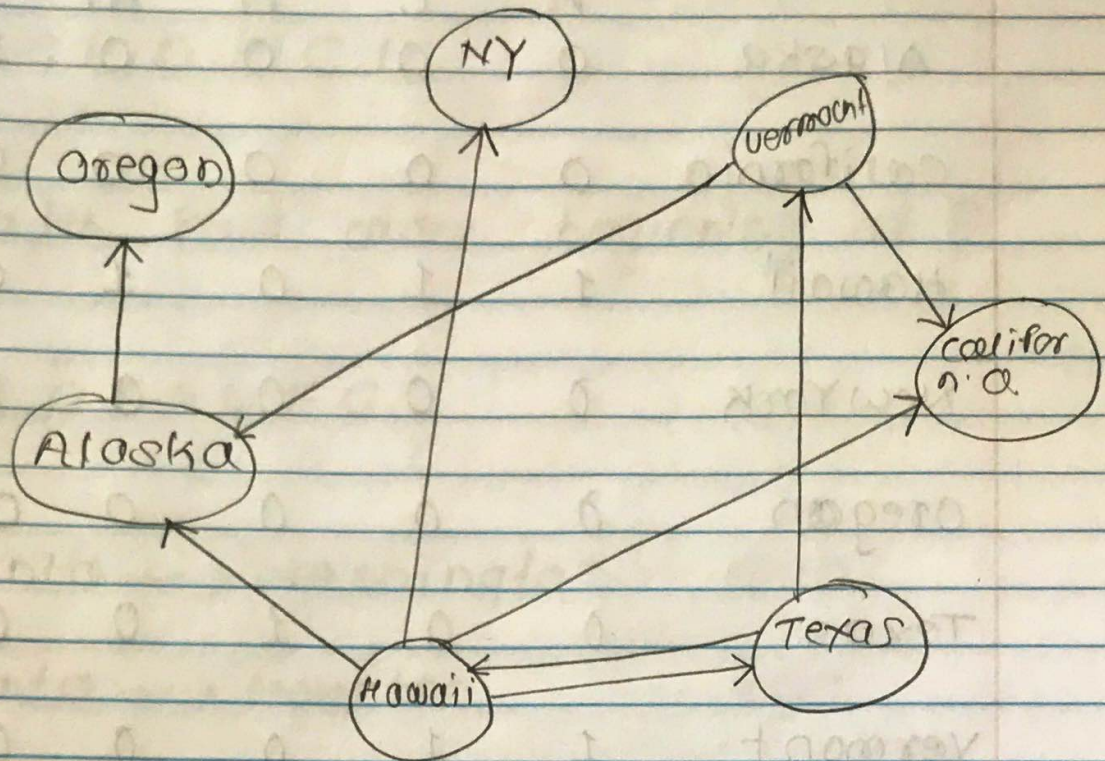


1) Draw the state graph.



Formal graph notation

$$V(\text{State Graph}) = \{O, A, T, H, V, N, C\}$$

$$E(\text{State Graph}) = \{(A, O), (H, A), (H, T), (T, H), (H, N), (H, V), (T, V), (V, C), (V, A)\}$$

2.

a) There is no path between Oregon to any other state in the graph.

b) Yes. There is a path from Hawaii to every other state in the graph.

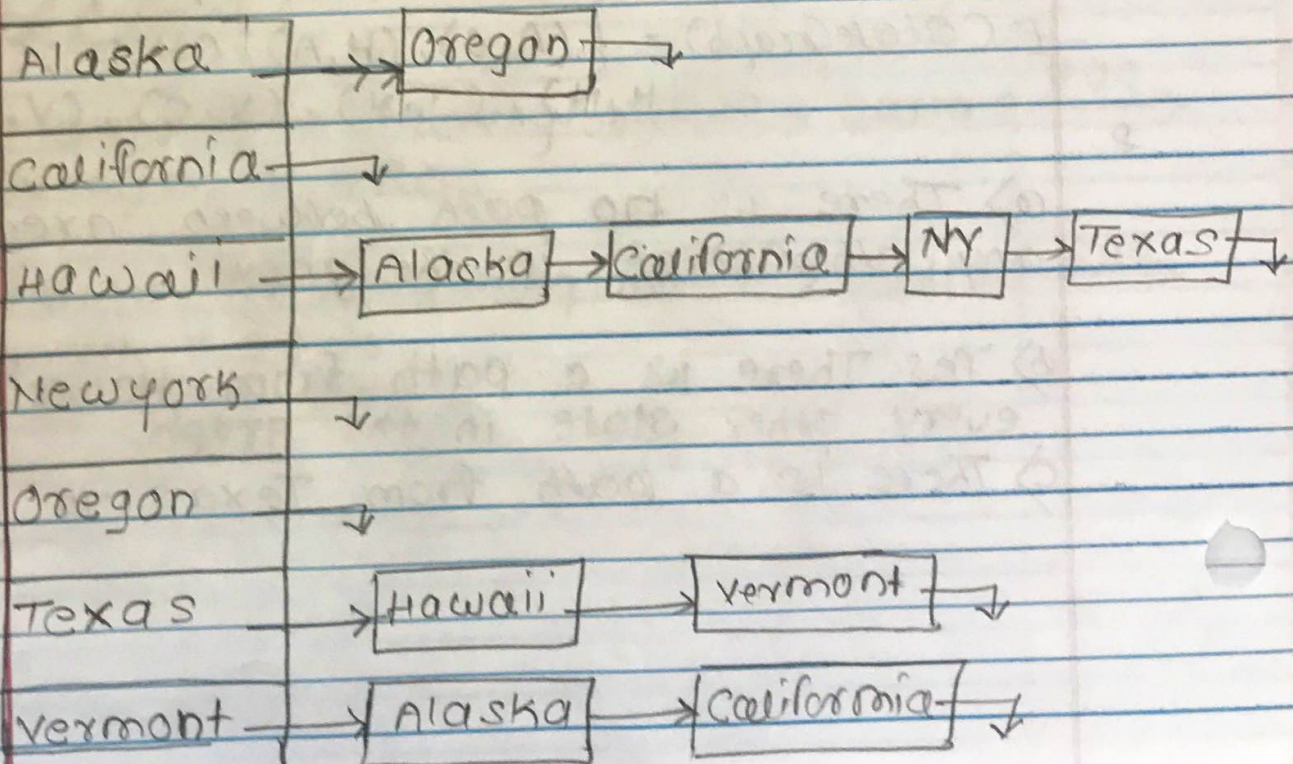
c) There is a path from Texas to Hawaii.

3. a

adjacency matrix

	A	C	H	NY	O	T	V
Alaska	0	0	0	0	1	0	0
California	0	0	0	0	0	0	0
Hawaii	1	1	0	1	0	1	0
New York	0	0	0	0	0	0	0
Oregon	0	0	0	0	0	0	0
Texas	0	0	1	0	0	0	1
Vermont	1	1	0	0	0	0	0

3. b) adjacency lists



4.a) Depth first order beginning with E

⇒ E G A D F C B

4.b) Breadth first order beginning at F

⇒ F D C A E F G
F C D A B E G

5) Atlanta → Washington — 600

Atlanta → Houston — 800

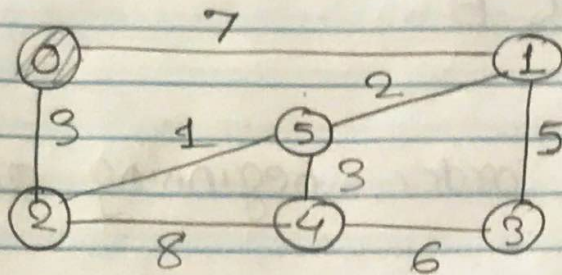
Atlanta $\xrightarrow{600}$ Washington $\xrightarrow{1300}$ Dallas — 1900

Atlanta $\xrightarrow{600}$ Washington $\xrightarrow{1300}$ Dallas $\xrightarrow{780}$ Denver
⇒ 2680

Atlanta $\xrightarrow{600}$ Washington $\xrightarrow{1300}$ Dallas $\xrightarrow{900}$ Chicago = 2800

Atlanta $\xrightarrow{600}$ Washington $\xrightarrow{1300}$ Dallas $\xrightarrow{200}$ Austin = 2100

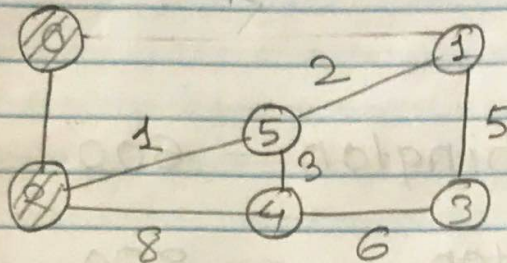
6) minimal spanning tree using prim's algorithm.



$$V(T) = \{0\}$$

$$E(T) = \emptyset$$

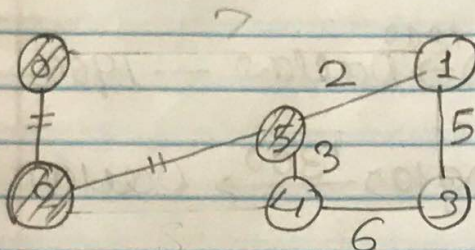
$$N = \{1, 2, 3, 4, 5\}$$



$$V(T) = \{0, 2\}$$

$$E(T) = \{(0, 2)\}$$

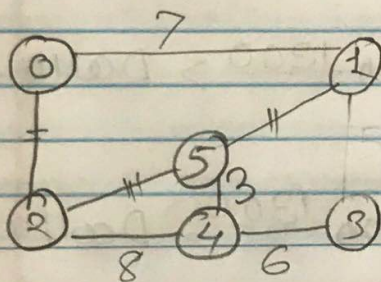
$$N = \{1, 3, 4, 5\}$$



$$V(T) = \{0, 2, 5\}$$

$$E(T) = \{(0, 2), (2, 5)\}$$

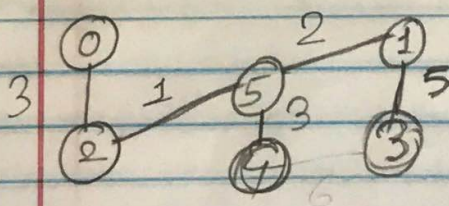
$$N = \{1, 3, 4\}$$



$$V(T) = \{0, 1, 2, 5\}$$

$$E(T) = \{(0, 2), (2, 5), (5, 1)\}$$

$$N = \{3, 4\}$$



$$V(T) = \{0, 1, 2, 3, 5\}$$

$$E(T) = \{(0, 2), (2, 5), (5, 1), (3, 4)\}$$

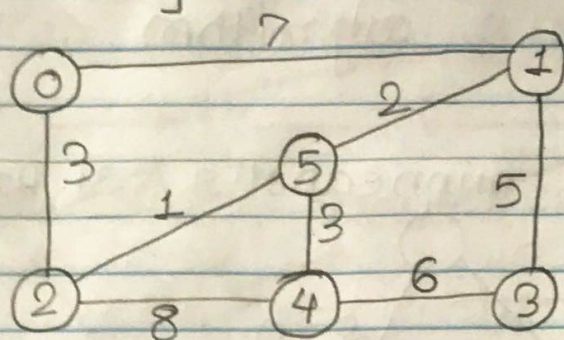
$$N = \{4\}$$

$$V(T) = \{0, 1, 2, 3, 4, 5\}$$

$$E(T) = \{(0, 2), (2, 5), (5, 1), (3, 4), (4, 3)\}$$

N -

7) MST using Kruskal's algorithm



edge weight

0-2 (3)

2-5 (1)

0-1 (7)

5-1 (2)

2-5 (1)

5-4 (3)

2-4 (8)

0-2 (3)

5-1 (2)

1-3 (5)

5-4 (3)

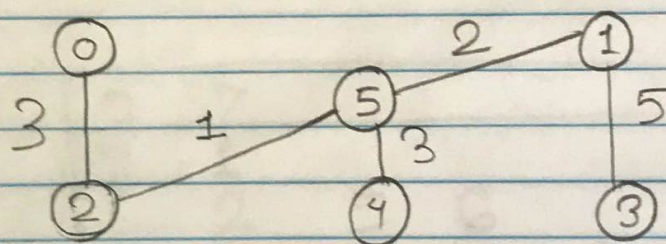
4-3 (6)

4-3 (6)

0-1 (7)

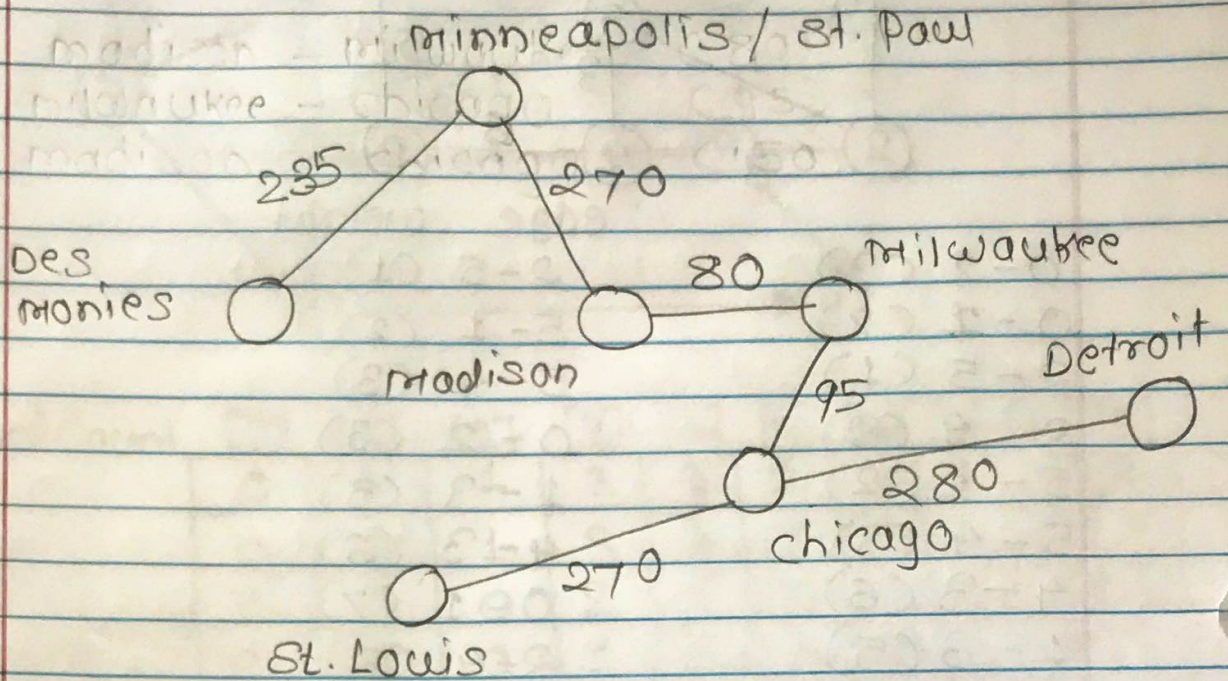
1-3 (5)

2-4 (8)

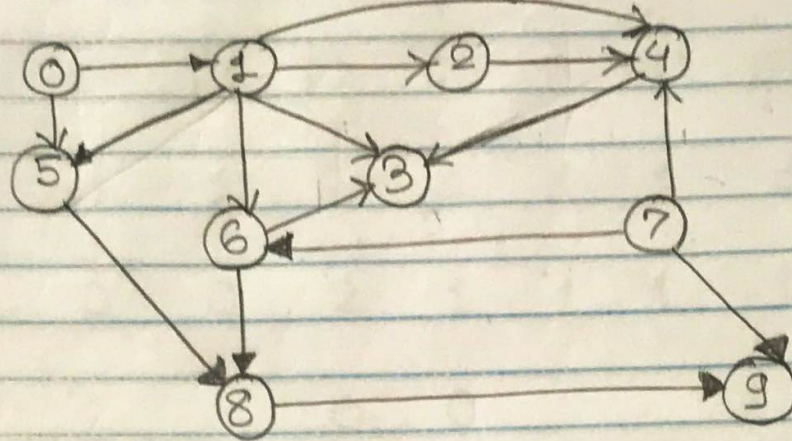


$$V = \{0, 1, 2, 3, 4, 5, 6\}$$

⑧ minimal spanning tree using
prim's algorithm



9) Breadth first topological order.



predCount	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	0	1	1	3	3	2	2	0	2	2
1	0	0	1	3	3	1	1	0	2	1
2	0	0	0	2	1	0	0	0	2	1
3	0	0	0	1	0	0	0	0	0	1
4	0	0	0	0	0	0	0	0	0	0

queue

0	7									
7	1									
1	2	5	6							
2	5	6	4	8						
5	6	4	8	3	9					
0	7	1	2	6	5	4	8	3	9	

topological
order

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
0	7	1	2	5	6	4	8	3	9

10) Nodes of the graph in a breadth first topological ordering.

Start	DM	P1	P2	CO	A	HLL	OS	TC	SS	C	End
0	1	1	2	1	1	1	1	1	4	1	1
	0	0	2	1	1	1	1	1	4	1	1
			0	0							
					0	0	0				
								0	2	0	
									0		0

Topological ordering

Start, Discrete Math, programming 1, programming 2, Computer Organization, Algorithms, High level Languages, operating system, Theory of Computation, computers, Senior Seminar, End.

[0] [1] [2] [3] [4] [5] [6] [7] [8] [9] [10] [11]

S | DM | P1 | P2 | CO | A | HLL | OS | TC | C | SS | End