Compiler Design - Notes Week 7

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9. Menhir In Practice

9.1 Menhir Output

You can get verbose ocamlyacc debugging information by doing:

```
menhir --examplain
or, if using ocamlbuild:
ocamlbuild -use-menhir -yaccflag --explain
```

The result is a <basename>.conflicts file describing the error. The flag --dump generates a full description of the automaton.

9.2 Precedence and Associativity Declarations

Parser generators often support **precedence/associativity declarations**. Those hint to the parser about how to resolve conflicts.

- Pros:
 - Avoids having to manually resolve those ambiguities by manually introducing extra non-terminals
 - Easier to maintain the grammar
- Cons:
 - Can't as easily re-use the same terminal
 - Introduces another level of debugging

10 Untyped Lambda Calculus

10.1 Functional Languages

Languages like ML, Haskell, Scheme, Python etc. support different operations on and with functions:

- Functions can be passed as arguments (e.g. map or fold)
- Functions can be returned as values (e.g. compose)
- Functions can be nested, i.e. inner functions refer to variables bound in the outer function

Example:

```
let add = fun x -> fun y -> x + y
let inc = add 1
let dec = add -1
let compose = fun f -> fun g -> fun x -> f (g x)
let id = compose inc dec
```

But how do we implement such functions in an interpreter or in a compiled language?

10.2 Lambda Calculus

The **lambda calculus** is a minimal programming language. It has variables, functions, and function application. That's it! It is, however, still touring complete.

The abstract syntax in OCaml is:

10.3 Values and Substitution

The only values of the lambda calculus are (closed) functions:

To substitute value v for variable x in expression e:

- Replace all free occurrences of x in e by v
- In OCaml written as subst v x e

Function application is interpreted by substitution:

```
(\text{fun } x \rightarrow \text{fun } y \rightarrow x + y) 1
= subst 1 x (fun y -> x + y)
= (fun y -> 1 + y)
```

10.4 Lambda Calculus Operational Semantics

10.5 Free Variables and Scoping

We look at the following example code:

```
let add = fun x -> fun y -> x + y
let inc = add 1
```

The result of add 1 is a function. After calling add, we can't throw away its arguments (or its local variables) because those are needed in the function returned by add.

- We say that variable x is free in fun y -> x + y (the variable is defined in the outer scope)
- We say that variable y is bound by fun y. Its scope is the body x + y in fun $y \rightarrow x + y$

A term with no free variables is called **closed**. In contrast, a term with one or more free variables is called **open**.

10.6 Free Variable Calculation

The following OCaml code computes the set of free variables in lambda expressions:

We then say a lambda expression e is closed if free vars e is VarSet.empty.

10.7 Variable Capture

Note that if we try to naively substitute an open term, a bound variable might capture the free variables. Example:

```
(fun x -> (x y)) {(fun z -> x)/y} // x is free in (fun z -> x) = fun x -> (x (fun z -> x)) // the free x is now captured
```

This is usually not the desired behavior! The meaning of x is determined by where it is bound dynamically, not where it is bound statically ($dynamic\ scoping$).

10.8 Alpha Equivalence

Note that the names of bound variables don't matter. (fun $x \rightarrow y x$) is the same as (fun $z \rightarrow y z$). Two terms that differ only by consistent renaming of bound variables are called **alpha equivalent**.

However, the names of free variables do matter! (fun $x \rightarrow y x$) is not the same as (fun $x \rightarrow z x$).

10.9 Fixing Substitution

We can fix the substitution problem. For this, let us consider the following substitution operation: e_1e_2/x

To avoid capture, we define the substitution to pick an alpha equivalent version of e_1 , such that the bound names of e_1 don't mention the free names of e_2 . Then we can do the simple naive substitution.

Example:

```
(\text{fun } x \rightarrow (x y)) \{(\text{fun } z \rightarrow x)/y\}
= (\text{fun } x' \rightarrow (x' (\text{fun } z \rightarrow x))) // rename x to x'
```

10.10 Operational Semantics

exp₁ exp₂ ↓ w

[&]quot;To evaluate function application: Evaluate the function to a value, evaluate the argument to a value, and then substitute the argument for the function."

10.11 Adding Integers to Lambda Calculus

We might extend our previously described Lambda Calculus with **integer values** by modifying our previous definitions in the following way:

11. Static Analysis

11.1 Variable Scoping

We have the following problem: How do we determine whether a declared variable is in scope?

Example: The code below is syntactically correct, but not well-formed! y and q are used without being defined anywhere.

```
int fact(int x) {
    var acc = 1;
    while(x > 0) {
        acc = acc * y;
        x = q - 1;
    }
    return acc;
}
```

11.2 Contexts and Inference Rules

We somehow need to keep track of **contextual information**, i.e. what variables are in the current scope and what their types are.

One way to describe this is that the compiler keeps a mapping from variables to information about them using a symbol table.

11.2.1 Inference Rules

A judgement is of the form $G; L \vdash e : t$ is read as "the expression e is well typed and has type t".

For any environment G; L, expression e, and statements s1, s2:

$$G; L; rt \vdash if (e) s_1 else s_2$$

holds if $G; L \vdash e : bool, G; L; rt \vdash s_1, G; L; rt \vdash s_2$ all hold.

More succinctly, we can summarize these constraints as an **inference rule**:

$$\frac{G; L \vdash e : \text{bool} \quad G; L; rt \vdash s_1 \quad G; L; rt \vdash s_2}{G; L; rt \vdash \text{if } (e) \ s_1 \text{ else } s_2}$$

11.2.2 Checking Derivations

We can build a **derivation tree** by making the nodes to be judgements and the edges to connect premises to a conclusion (according to the inference rules). Leaves of the tree are **axioms**, i.e. rules with no premises. The goal of the **type checker** is to verify that such a *tree exists*.

11.2.3 Compilation as Translating Judgements

Consider the typing judgement for source expressions: $C \vdash e : t$. How do we interpret this information in the target language? I.e. $[[C \vdash e : t]] = ?$ We have that:

- [[t]] is a target type
- [[e]] translates to a (possibly empty) sequence of instructions

We can state the following invariant: If $[[C \vdash e : t]] = ty$, operand, stream, then the type of the operand is ty = [[t]].

Example: What is $[[C \vdash 341 + 5 : int]]$?

11.2.4 Contexts

What is [[C]]? Source level C has bindings like x: int, y: bool, etc. [[C]] maps source identifiers x to source types [[x]].

The interpretation of a variable [[x]] can is:

11.2.5 Other Judgements

Establish invariant for expressions:

Statements:

$$x:t \in L \quad G; L \vdash exp:t \\ G; L; rt \vdash x = exp; \Rightarrow L \\ \text{as addresses} \\ \text{(which can be assigned)} \\ \text{where (t, $\$id_x$) = lookup [L] x} \\ \text{and } [G; L \vdash exp:t] = ([t]], opn, stream)$$

$$[\![C; rt \vdash stmt \Rightarrow C']\!] = [\![C']\!]$$
, stream

Declaration:

11.3 Compiling Control

11.3.1 Translating while

```
[C;rt \to while(e) s \Rightarrow C'] = [C'],

lpre:
    opn = [C \to e : bool]
    %test = icmp eq i1 opn, 0
    br %test, label %lpost, label %lbody
lbody:
    [C;rt \to s \Rightarrow C']
    br %lpre
lpost:
```

11.3.2 Translating If-Then-Else

```
[C; rt \vdash if (e_1) s_1 else s_2 \Rightarrow C'] = [C'],
```

```
\begin{array}{l} \text{opn} = [\![ \texttt{C} \vdash \texttt{e} : \texttt{bool} ]\!] \\ \text{%test} = \texttt{icmp} \ \texttt{eq} \ \texttt{il} \ \texttt{opn}, \ \texttt{0} \\ \text{br} \ \text{%test}, \ \texttt{label} \ \text{%else}, \ \texttt{label} \ \text{%then} \\ \text{then:} \\ [\![ \texttt{C}; \texttt{rt} \vdash \texttt{s}_1 \Rightarrow \texttt{C}' ]\!] \\ \text{br} \ \text{%merge} \\ \text{else:} \\ [\![ \texttt{C}; \texttt{rt} \vdash \texttt{s}_2 \Rightarrow \texttt{C}' ]\!] \\ \text{br} \ \text{%merge} \\ \text{merge:} \end{array}
```