Algorithms for Graph-Based Supervised Learning

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Hello

Modified Adsorption 1

This routine is described in Talukdar below.

Prerequisites 1.1

I'm looking for a good parallelization strategy for this function. I'm going to expand it as far as I can to see if something presents itself. We are aiming to find c_v and d_v for each vertex in the graph. First, let's define

$$m(x) = \sum_{u} W_{u,x} \tag{1}$$

$$m(x) = \sum_{u} W_{u,x}$$

$$l(x) = \sum_{u} W_{u,x} \log W_{u,x}$$

$$(1)$$

Okay, check my math here...

$$p(a|b) = \frac{W_{a,b}}{\sum_{u} W_{u,b}} \tag{3}$$

$$= \frac{W_{a,b}}{m(b)} \tag{4}$$

$$H(x) = -\sum_{y}^{y} p(y|x) \log p(y|x)$$
 (5)

$$= -\sum_{y} \left(\frac{W_{y,x}}{\sum_{u} W_{u,x}} \right) \log \left(\frac{W_{y,x}}{\sum_{u} W_{u,x}} \right)$$
 (6)

$$= -\sum_{y} \left(\frac{W_{y,x}}{m(x)}\right) \log \left(\frac{W_{y,x}}{m(x)}\right) \tag{7}$$

$$= \frac{-1}{m(x)} \sum_{y} W_{y,x} \left[\log W_{y,x} - \log m(x) \right]$$
 (8)

$$= \frac{-1}{m(x)} \left[\sum_{y} W_{y,x} \log W_{y,x} - \sum_{y} W_{y,x} \log m(x) \right]$$
 (9)

$$= \frac{-1}{m(x)} \left[\sum_{y} W_{y,x} \log W_{y,x} - m(x) \log m(x) \right]$$
 (10)

$$= \log m(x) - \frac{1}{m(x)} \sum_{y} W_{y,x} \log W_{y,x}$$
 (11)

$$= \log m(x) - \frac{l(x)}{m(x)} \tag{12}$$

Next we have the smoothing function for a given β

$$f(x) = \frac{\log \beta}{\log(\beta + e^x)} \tag{13}$$

$$c_x = f(H(x)) (14)$$

$$= \log \beta \left[\log(\beta + e^{H(x)})\right]^{-1} \tag{15}$$

$$d_x = (1 - c_x)\sqrt{H(x)} \tag{16}$$

$$z_x = \max(c_x + d_x, 1) \tag{17}$$

Given these values, the authors define

$$p_v^{cont} = \frac{c_v}{z_v}, p_v^{inj} = \frac{d_v}{z_v}, p_v^{abnd} = 1 - p_v^{cont} - p_v^{inj}$$

1.2 Algorithm 3: Modified Adsoprtion

Taken from the book reference below

Algorithm 1 Modified Adsoprtion

```
1: procedure INPUT:

2: G = (V, E, W)

3: Labels = Y_v \in \mathcal{R}^{m+1} for v \in V

4: Probabilities p_v^{inj}, p_v^{cont}, p_v^{abnd} for v \in V

5: procedure OUTPUT:

6: \hat{Y}
```

2 References

BibTeX is a pain, so for right now I'm going to do

```
@article{doi:10.2200/S00590ED1V01Y201408AIM029,
author = { Amarnag
  Subramanya and Partha Pratim
  Talukdar },
title = {Graph-Based Semi-Supervised Learning},
journal = {Synthesis Lectures on Artificial Intelligence and Machine Learning},
volume = \{8\},
number = \{4\},
pages = \{1-125\},
year = \{2014\},\
doi = {10.2200/S00590ED1V01Y201408AIM029},
URL = {
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