

Advanced Control Lab

Lab Report-5

Student Name	Student Number
Zhiyuan Li	941190894
Shubhankar Jadhav	941190704

Objective:

We want to design a controller for the pendulum angle, C_θ for a dampening of the pendulum oscillations, and it also need to fulfill requirements regarding open/closed loop gain. We will compare the system with and without this controller to verify its performance.

C_θ upholds the following requirements:

- the gain of the full closed loop should be no more than 3 [dB]
- the controller gain should be less than 0 [dB] for frequencies higher than 200 $\left[\frac{rad}{s}\right]$
- the controller slope should be at least $-20 \left[\frac{db}{decade}\right]$

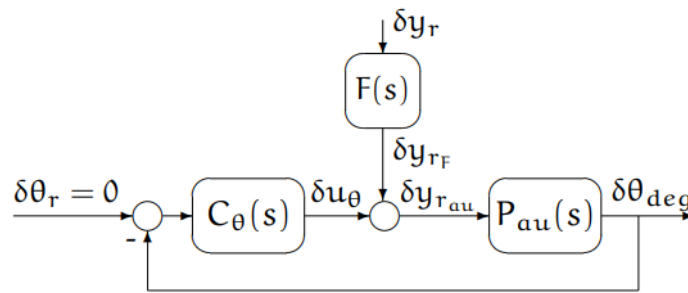


Figure:1 Dampening loop with P_{au}

P_{au} is given by:

$$P_{au} = \frac{C_y P_y P_\theta}{1 + C_y P_y}$$

Substituting values we get previous lab, we get

$$P_{au} = \frac{-214.19 s^4 (s + 5.78) (s + 7.549) (s + 23.68) (s + 1.17) (s^2 + 0.1679s + 35.96) (s^2 + 1.586s + 42.34)}{s^2 (s + 23.68) (s + 7.549) (s + 3.671) (s + 1.619) (s^2 + 1.295s + 32.49) (s^2 + 0.1679s + 35.96) (s^2 + 1.586s + 42.34) (s^2 + 26.23s + 255.6)}$$

The lead controller we have

We get the lead controller from the given gain crossover frequency 4.061 rad/s. We then find the phase of the controller ϕ using the formula of the phase margin: $PM = \pi + \text{phase of } (P) - 5.7^\circ - \phi$

We use the ϕ to obtain the lead coefficient of the lead controller $\alpha = \frac{1+\sin\phi}{1-\sin\phi}$ and we get α as 7.584 and we apply the lead controller formula

$$C_{lead} = \frac{2.754 s + 4.061}{s + 11.18}$$

We choose to design the controller in the following form:

$$C_\theta = -\frac{1}{C_{lead}} \cdot C_{LPF},$$

Where $C_{LPF} = \frac{200}{s+200}$ so that we could largely attenuate the signal when the frequency is higher than $200 \left[\frac{\text{rad}}{s} \right]$.

In the end, we get:

$$C_\theta = \frac{-200 s - 2237}{2.754 s^2 + 554.8 s + 812.3}$$

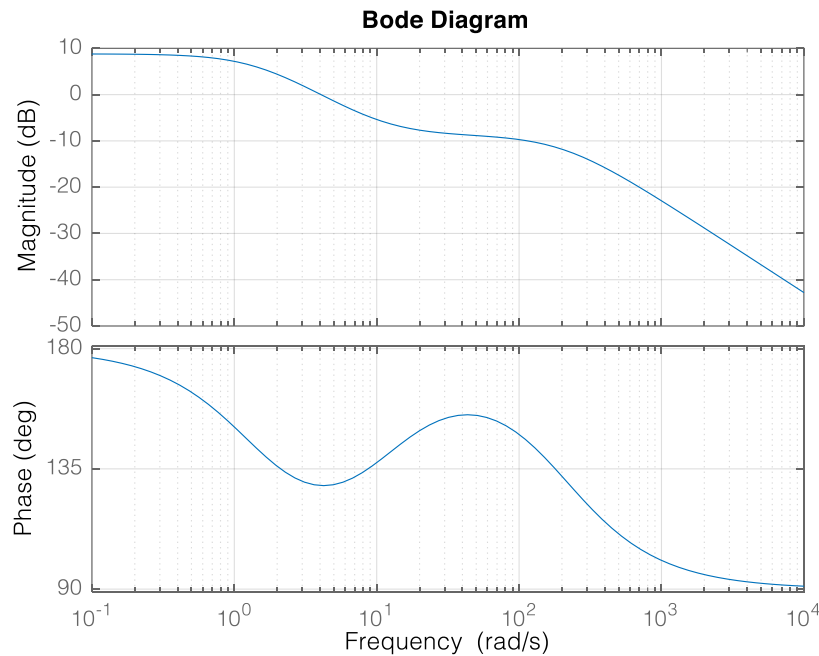


Figure 2: bode diagram of C_θ

It is clear that the controller gain is less than 0[dB] for the frequencies from 200[rad/sec] to infinity, the controller **slope** is around $\frac{-43.2dB+23.1dB}{dec} = -20.1 \frac{dB}{dec}$, which also satisfies the related requirements.

Add the designed $C_\theta(s)$ to Figure 4 in lab 4, we get the new Simulink:

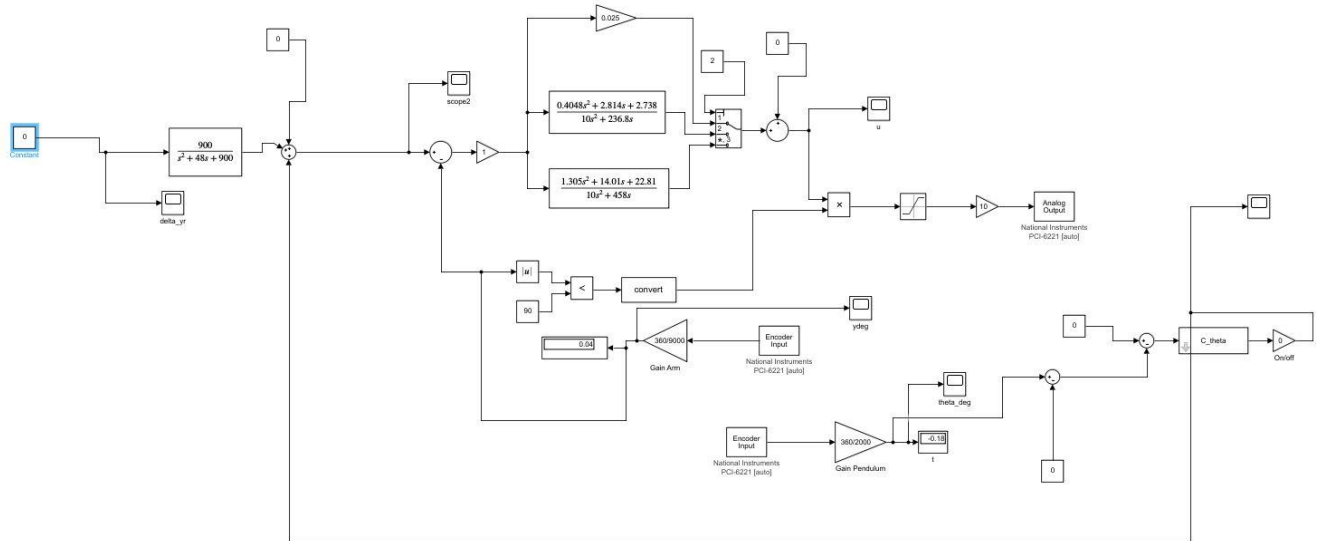


Figure:3 Simulink built in lab 5

Now, let's start to plot the related graphs.

1. Bode plot, Nyquist plot (or Nichols plot) of the open loop transfer function $L(s) = P_{au}(s)C_\theta(s)$,

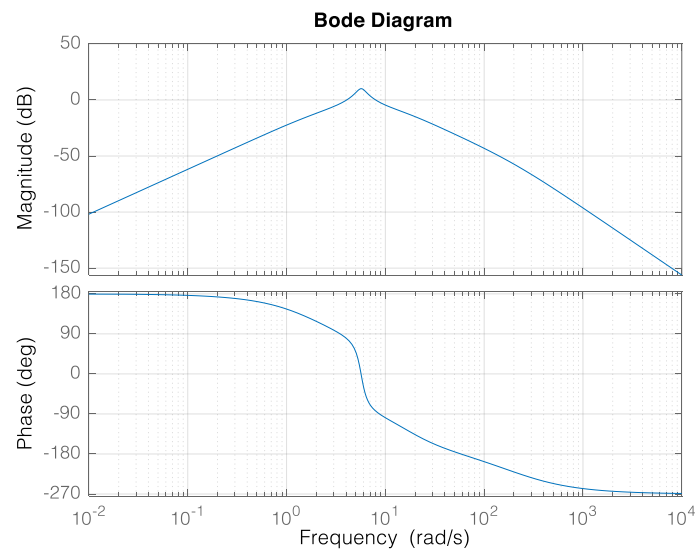


Figure 4: Bode plot of the open loop transfer function $L(s) = P_{au}(s)C_\theta(s)$

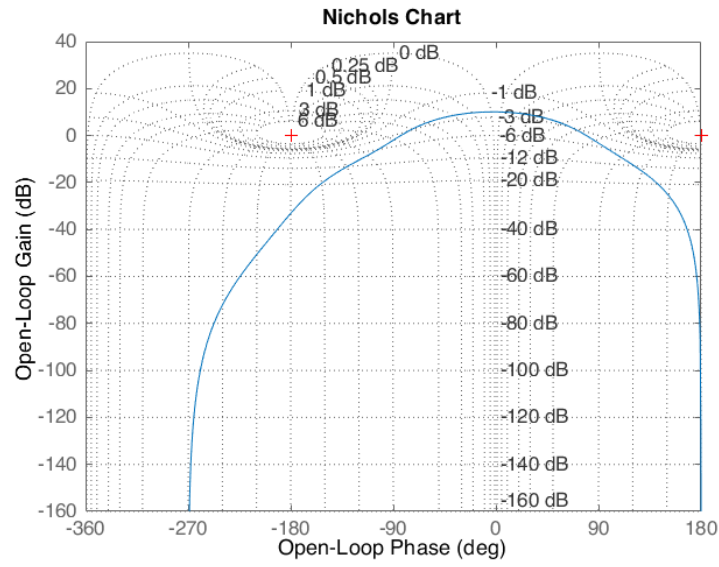


Figure:5 Nichols plot of the open loop transfer function $L(s) = P_{au}(s)C_{\theta}(s)$

2. Bode plots of the transfer functions from δy_r to $\delta \theta_{deg}$ in open loop (with $C_{\theta}(s) = 0$) and in closed loop (with designed $C_{\theta}(s)$),

In open loop:

$$\frac{\delta \theta_{deg}}{\delta y_r} = F(s)P_{au}(s)$$

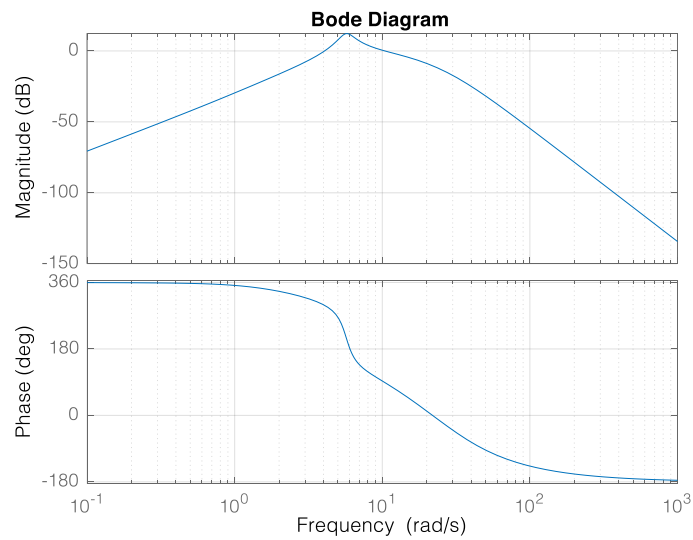


Figure:8 Bode plots of the transfer functions from δy_r to $\delta \theta_{deg}$ in open loop (with $C_{\theta}(s) = 0$)

In closed loop:

$$\frac{\delta\theta_{deg}}{\delta y_r} = \frac{F(s)P_{au}(s)}{1 + C_\theta(s)P_{au}(s)}$$

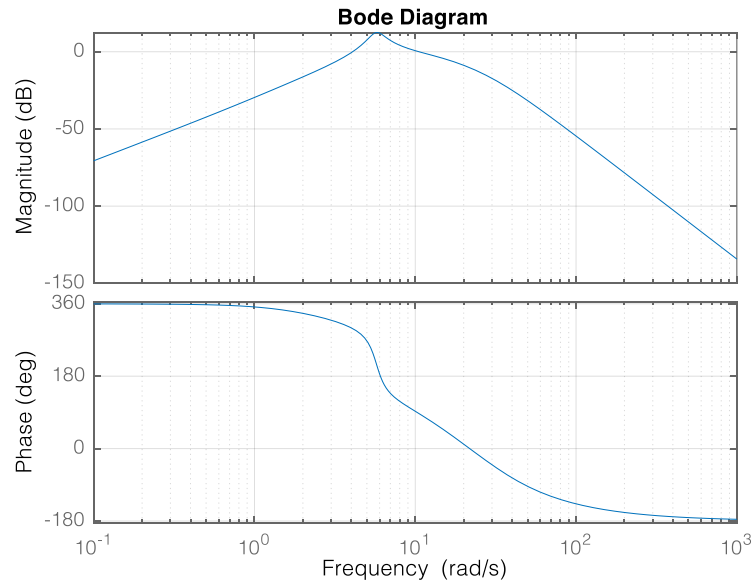


Figure 9: Bode plots of the transfer functions from δy_r to $\delta\theta_{deg}$ in closed loop (with designed $C_\theta(s)$)

3. Bode plots of the transfer functions from δy_r to δy_{deg} in open loop (with $C_\theta(s) = 0$) and in closed loop (with designed $C_\theta(s)$)

In open loop:

$$\frac{\delta y_{deg}}{\delta y_r} = \frac{F(s)C_y(s)P_y(s)}{1 + C_y(s)P_y(s)}$$

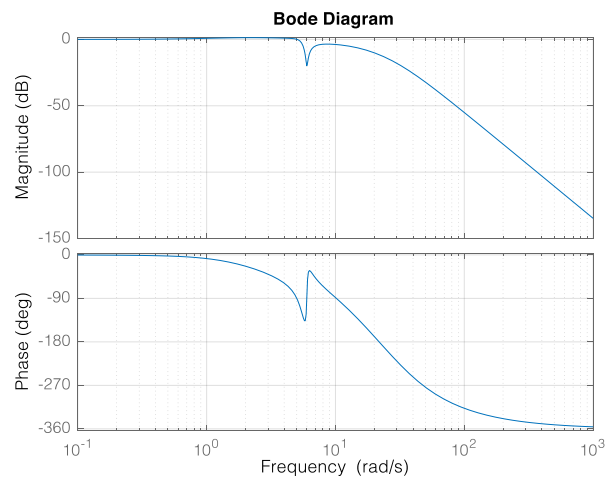


Figure:6 Bode plots of the transfer functions from δy_r to δy_{deg} in open loop (with $C_\theta(s) = 0$)

In closed loop:

$$\frac{\delta y_{deg}}{\delta y_r} = \frac{F(s)P_{au}(s)}{P_\theta(1 + C_\theta(s)P_{au}(s))}$$

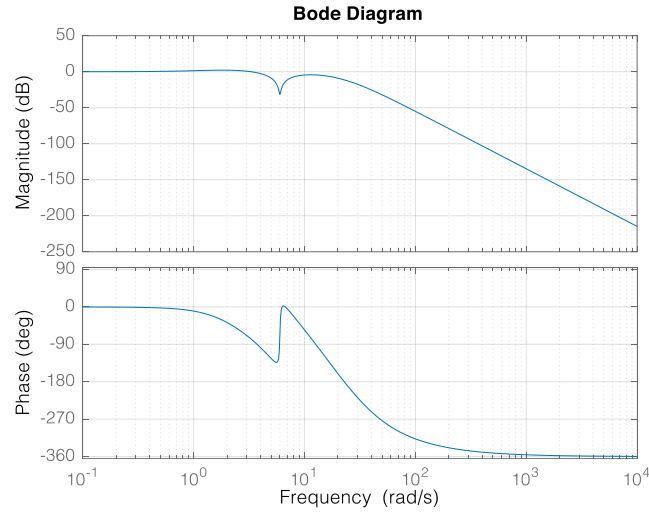


Figure 7: Bode plots of the transfer functions from δy_r to δy_{deg} in closed loop (with designed $C_\theta(s)$)

4. compare the signals obtained by the experiment to the corresponding signals in the simulations with the linear and nonlinear models of the experimental setup.

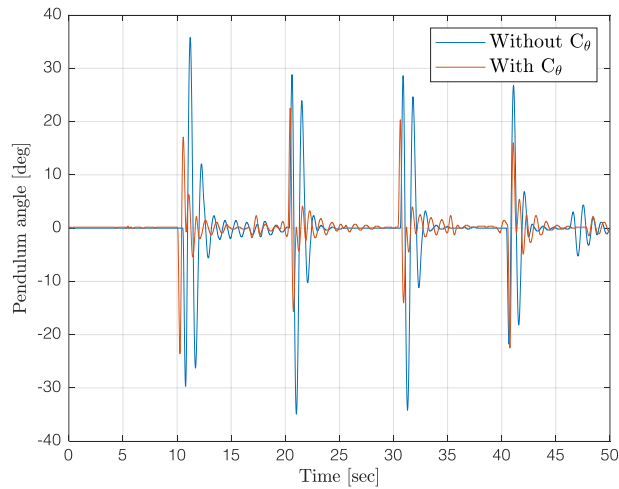


Figure 10: comparison of pendulum degree vs time with and without C_θ

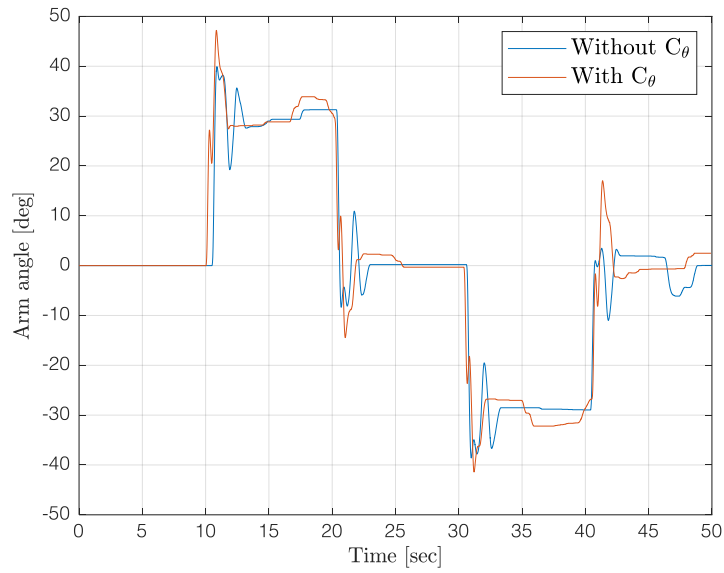


Figure 11: comparison of arm degree vs time with and without C_θ

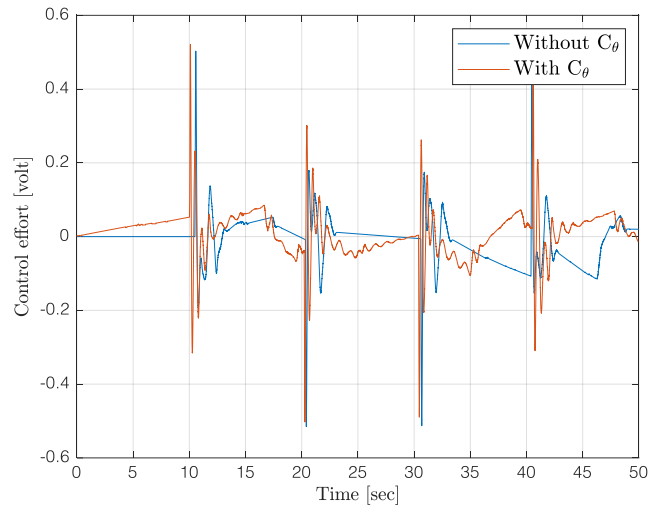


Figure 12: comparison of control effort vs time with and without C_θ

The controller C_θ not only reduced the oscillations of the system, but also yielded faster convergence to the steady state of the system. The improved performance is evident in the systems abilities to achieve desired results more accurately and efficiently.

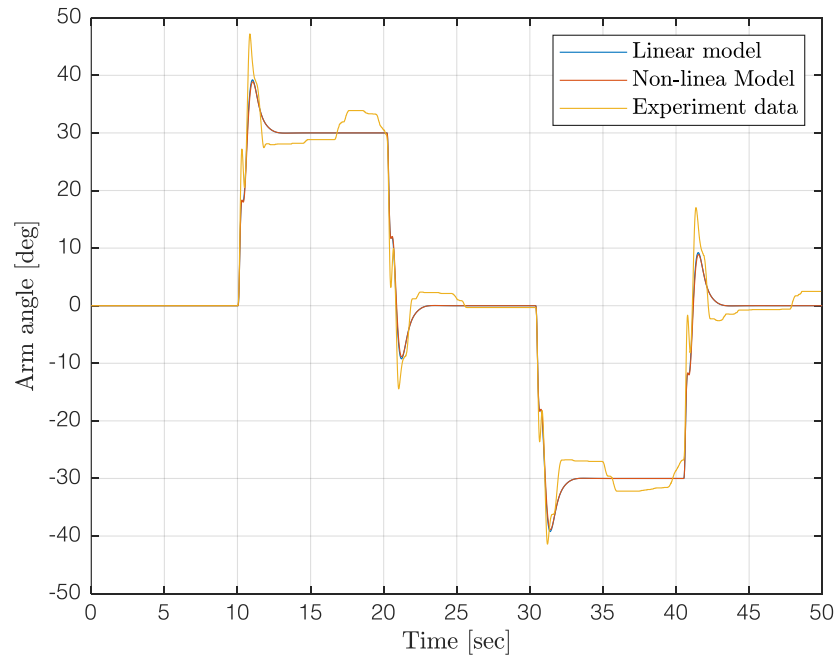


Figure 13: comparison of arm angle vs time between linear model, non-linear model, and experimental data

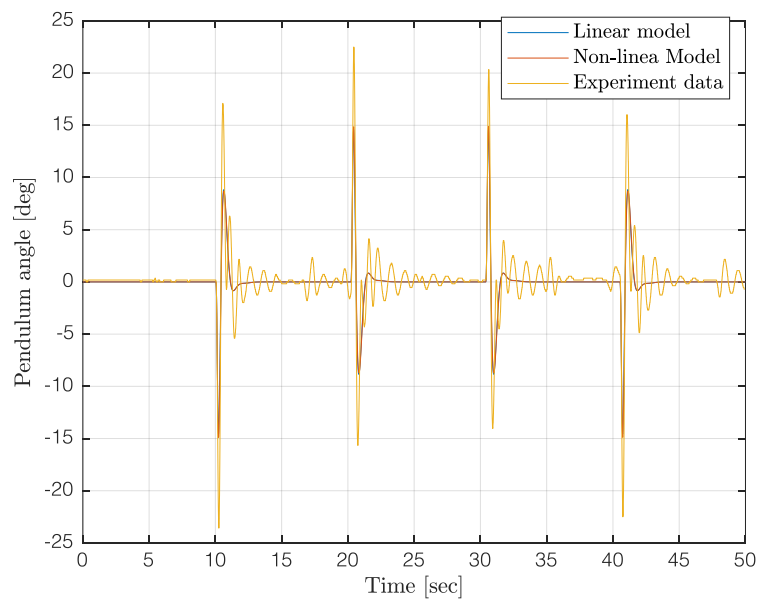


Figure 14: comparison of pendulum angle vs time between linear model, non-linear model, and experimental data

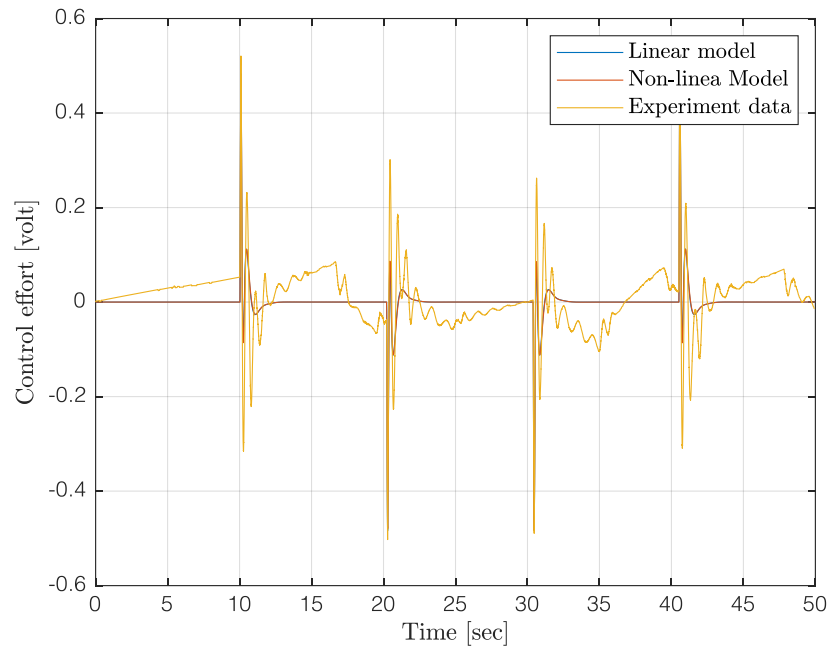


Figure 15: comparison of control effort vs time between linear model, non-linear model, and experimental data

Here we can see that the experimental results specifically for the ones with the pendulum angles oscillate a lot, whereas we see that the Linear and Non-Linear model reaches steady state very quickly.

Conclusion:

In this experiment, we design a C_θ for a dampening of the pendulum oscillations, we've verified that the controller gain is less than 0[dB] for the frequencies from 200[rad/sec] to infinity, the controller slope is around $-20.1 \frac{db}{dec} < 20 \frac{db}{dec}$, and the peak magnitude of the closed loop is $2.93dB < 3dB$. We also see that due to the implementation of the C_θ controller in our system yielded very good results that are in very good agreement with our theoretical results, and exhibited better control and performance compared to other controllers implemented. The controller C_θ not only reduced the oscillations of the system, but also yielded faster convergence to the steady state of the system. The improved performance is evident in the systems abilities to achieve desired results more accurately and efficiently. We can clearly see the difference in the outputs where the controller C_θ was and wasn't implemented, the systems in which the controller wasn't implemented showed increased oscillations and slower convergence rates. These results serve as a testament to the impact of the C_θ controller for the enhancement of the control of our system.