

Problems

1.1

(a) picosecond: ps; femtosecond: fs.

$$1 \text{ ps} = 10^{-12} \text{ s}$$

$$1 \text{ fs} = 1 \times 10^{-15} \text{ s}$$

→ $1 \text{ ps} = 1 \times 10^3 \text{ fs}$, the order of time interval is 3

$$(b) 1 \text{ nm} = 10^{-3} \text{ μm} = 10^{-6} \text{ mm} = 10^{-7} \text{ cm} = 10^{-8} \text{ dm} = 10^{-9} \text{ m} = 10^{-12} \text{ km}.$$

(c) Electron volt (eV) is a unit of energy

$$1 \text{ MeV} = 1 \times 10^6 \text{ eV}$$

M: million

$$1 \text{ GeV} = 1 \times 10^9 \text{ eV}$$

G: gillion

$$1.3 \quad m = 5.98 \times 10^{24} \text{ kg} = 5.98 \times 10^{25} \text{ mol?}$$

1.8. Use parameters (M, R) of a spherically symmetric distribution of mass and gravitational constant G to construct a quantity of dimension of speed.

$$\sqrt{\frac{GM}{R}}$$

$$\Rightarrow v = \sqrt{\frac{GM}{R}}, \text{ and it has the dimension of speed.}$$

$$1.12 \quad C_V = \frac{3}{2} T^3 + rT$$

$$\epsilon_{ki} = (n_i + \frac{1}{2}) \hbar \omega_i$$

$$C_V = \left(\frac{\partial E}{\partial T} \right)_V = k \sum_{i=1}^{3N} \left(\frac{\hbar \omega_i}{kT} \right)^2 \frac{e^{\hbar \omega_i / kT}}{(e^{\hbar \omega_i / kT} - 1)^2}$$

When the temperature is extreme low, $T \ll \frac{\hbar \omega_i}{k}$

$$C_{Vi} = k \left(\frac{\hbar \omega_i}{kT} \right)^2 e^{-\frac{\hbar \omega_i}{kT}}$$

$$3N: C_V = 3Nk \left(\frac{\hbar \omega_i}{T} \right)^2 e^{-\frac{\hbar \omega_i}{T}}, \text{ have the same order of magnitude with.}$$

KOKUYO



1.14 $\vec{A}, \vec{B}, \vec{C}$ are polar vectors

$(\vec{B} \times \vec{C})$ is axial vector

$\Rightarrow \vec{A} \times (\vec{B} \times \vec{C})$ is (polar vector) \times (axial vector)

= a polar vector

1.17

$$b_1 \cdot a_1 = 2\pi$$

$$b_1 \cdot a_2 = 2\pi \frac{a_2}{a_1}$$

$$b_1 \cdot a_3 = 2\pi \frac{a_3}{a_1}$$

...

$$b_i \cdot a_j = 2\pi \frac{a_j}{a_i}$$

1.22 $\vec{A} = (2, 1, 1)$ $\vec{B} = (5, 2, 0)$ $\vec{C} = (1, 1, 1)$

(a) $\vec{A} \cdot \vec{B}$

$$= 10 + 2 = 12$$

(d) $\vec{A} \times (\vec{B} \times \vec{C})$

$$= (2, 1, 1) \times (2, 5, 3)$$

$$= (8, -4, -12)$$

(f) $\vec{A}(\vec{B} \times \vec{C}) - \vec{A} \times \vec{B}$

$$= \vec{A} \cdot (4, -10, 4)$$

$$= 8 - 10 + 4 = 2$$

(b) $\vec{A} \times \vec{B}$

$$= \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 2 & 1 & 1 \\ 5 & 2 & 0 \end{vmatrix}$$

$$= -2\vec{i} + 5\vec{j} - \vec{k}$$

$$= (-2, 5, -1)$$

(e) $\vec{A} \times (\vec{A} + \vec{B} \times \vec{C})$

$$= (2, 1, 1) \times (4, -4, 4)$$

$$= (8, -4, -12)$$

(c) $\vec{B} \times \vec{C}$

$$= (2, 5, 3)$$

$\vec{A} \cdot (\vec{B} \times \vec{C})$

Campus $4 - 5 + 3 = 2$

