# ml24-a02-lr-anguyea-anhnnguy

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# 1 Machine Learning Assignment 2

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```
[267]: import matplotlib.pyplot as plt
       import numpy as np
       import numpy.random
       import numpy.linalg
       import scipy.io
       import scipy.stats
       import sklearn.metrics
       # setup plotting
       from IPython import get_ipython
       import psutil
       inTerminal = not "IPKernelApp" in get_ipython().config
       inJupyterNb = any(filter(lambda x: x.endswith("jupyter-notebook"), psutil.
        →Process().parent().cmdline()))
       get_ipython().run_line_magic("matplotlib", "" if inTerminal else "notebook" if_
        →inJupyterNb else "widget")
       def nextplot():
           if inTerminal:
               plt.clf()
                             # this clears the current plot
           else:
               plt.figure() # this creates a new plot
```

```
[268]: %matplotlib widget
```

#### 2 Load the data

```
[269]: data = scipy.io.loadmat("data/spamData.mat")
    X = data["Xtrain"]
    N = X.shape[0]
    D = X.shape[1]
    Xtest = data["Xtest"]
    Ntest = Xtest.shape[0]
```

```
y = data["ytrain"].squeeze().astype(int)
ytest = data["ytest"].squeeze().astype(int)
features = np.array(
    Γ
        "word_freq_make",
        "word_freq_address",
        "word_freq_all",
        "word freq 3d",
        "word_freq_our",
        "word freq over",
        "word_freq_remove",
        "word_freq_internet",
        "word_freq_order",
        "word_freq_mail",
        "word_freq_receive",
        "word_freq_will",
        "word_freq_people",
        "word_freq_report",
        "word_freq_addresses",
        "word_freq_free",
        "word freq business",
        "word_freq_email",
        "word freq you",
        "word_freq_credit",
        "word freq your",
        "word_freq_font",
        "word_freq_000",
        "word_freq_money",
        "word_freq_hp",
        "word_freq_hpl",
        "word_freq_george",
        "word_freq_650",
        "word_freq_lab",
        "word_freq_labs",
        "word_freq_telnet",
        "word freq 857",
        "word_freq_data",
        "word freq 415",
        "word_freq_85",
        "word_freq_technology",
        "word_freq_1999",
        "word_freq_parts",
        "word_freq_pm",
        "word_freq_direct",
        "word_freq_cs",
        "word_freq_meeting",
```

```
"word_freq_original",
        "word_freq_project",
        "word_freq_re",
        "word_freq_edu",
        "word_freq_table",
        "word_freq_conference",
        "char_freq_;",
        "char_freq_(",
        "char_freq_[",
        "char freq !",
        "char freq $",
        "char_freq_#",
        "capital_run_length_average",
        "capital_run_length_longest",
        "capital_run_length_total",
    ]
)
```

#### 3 1. Dataset Statistics

```
[270]: # look some dataset statistics
      scipy.stats.describe(X)
[270]: DescribeResult(nobs=3065, minmax=(array([0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
      0., 0., 0., 0., 0., 0., 0.,
            0., 0., 0., 1., 1., 1.]), array([4.5400e+00, 1.4280e+01, 5.1000e+00,
      4.2810e+01, 9.0900e+00,
            3.5700e+00, 7.2700e+00, 1.1110e+01, 3.3300e+00, 1.8180e+01,
            2.0000e+00, 9.6700e+00, 5.5500e+00, 5.5500e+00, 2.8600e+00,
            1.0160e+01, 7.1400e+00, 9.0900e+00, 1.8750e+01, 6.3200e+00,
            1.1110e+01, 1.7100e+01, 5.4500e+00, 9.0900e+00, 2.0000e+01,
            1.4280e+01, 3.3330e+01, 4.7600e+00, 1.4280e+01, 4.7600e+00,
            4.7600e+00, 4.7600e+00, 1.8180e+01, 4.7600e+00, 2.0000e+01,
            7.6900e+00, 6.8900e+00, 7.4000e+00, 9.7500e+00, 4.7600e+00,
            7.1400e+00, 1.4280e+01, 3.5700e+00, 2.0000e+01, 2.1420e+01,
            1.6700e+01, 2.1200e+00, 1.0000e+01, 4.3850e+00, 9.7520e+00,
            4.0810e+00, 3.2478e+01, 6.0030e+00, 1.9829e+01, 1.1025e+03,
            9.9890e+03, 1.5841e+04])), mean=array([1.10818923e-01, 2.28486134e-01,
      2.74153344e-01, 6.29690049e-02,
            3.17787928e-01, 9.57553018e-02, 1.13546493e-01, 1.07216966e-01,
            8.89233279e-02, 2.41719413e-01, 5.81305057e-02, 5.37432300e-01,
            9.26231648e-02, 4.96639478e-02, 5.07210440e-02, 2.35334421e-01,
            1.47197390e-01, 1.86600326e-01, 1.66121044e+00, 7.63066884e-02,
            8.19592170e-01, 1.22727569e-01, 1.02006525e-01, 8.90799347e-02,
```

```
5.29800979e-01, 2.62071778e-01, 7.71507341e-01, 1.14323002e-01,
      1.09487765e-01, 9.92952692e-02, 6.28156607e-02, 4.90342577e-02,
      9.27471452e-02, 4.96019576e-02, 1.02156607e-01, 9.93050571e-02,
      1.43285481e-01, 1.24274062e-02, 7.55921697e-02, 6.60456770e-02,
      4.63360522e-02, 1.32176183e-01, 4.88580750e-02, 7.11876020e-02,
      3.06590538e-01, 1.79794454e-01, 5.28874388e-03, 3.13768352e-02,
      3.79543230e-02, 1.38396411e-01, 1.81830343e-02, 2.65470799e-01,
      7.91275693e-02, 5.34218597e-02, 4.90062936e+00, 5.26750408e+01,
      2.82203915e+02]), variance=array([1.07094140e-01, 1.88742036e+00,
2.34317437e-01, 1.78161723e+00,
      4.40325719e-01, 6.79193461e-02, 1.39844435e-01, 1.72001423e-01,
      6.97247542e-02, 4.69800274e-01, 3.58302179e-02, 7.59167719e-01,
      9.28365241e-02, 8.26118648e-02, 7.00470321e-02, 4.29393369e-01,
      2.00636301e-01, 2.92991898e-01, 3.18992370e+00, 1.65626303e-01,
       1.44315254e+00, 1.01505046e+00, 1.19749530e-01, 1.43862796e-01,
      2.45800502e+00, 7.38036013e-01, 1.13920029e+01, 2.31010973e-01,
      4.31507668e-01, 1.90528093e-01, 1.24671084e-01, 1.07425177e-01,
      2.95159161e-01, 1.07745599e-01, 3.08154062e-01, 1.67896547e-01,
      1.85791650e-01, 4.34829439e-02, 1.42525114e-01, 1.16865102e-01,
      1.50361473e-01, 6.09903912e-01, 5.73945833e-02, 3.19259425e-01,
      1.01935877e+00, 8.17471270e-01, 4.63438951e-03, 7.50333517e-02,
      5.54612799e-02, 7.77968333e-02, 1.48045497e-02, 7.59181612e-01,
      6.74541224e-02, 2.69600271e-01, 7.42311765e+02, 4.86573219e+04,
      3.68952901e+05]), skewness=array([ 5.92257918, 9.5555492, 2.94110789,
27.15035267, 4.22000271,
       4.55490419, 6.21454549, 10.63604439, 4.44795353, 9.63368819,
       5.1601559, 3.12797362, 7.99555783, 10.07103212, 6.44051978,
       5.9017492 , 5.71193665 , 5.63845456 , 1.6918398 , 8.05102821 ,
       2.36131511, 9.70708774, 5.74851972, 13.62929854, 5.51200726,
       5.77490458, 5.72163481, 5.84582426, 11.30526457, 6.67894971,
       8.78006633, 10.35563132, 16.1291286, 10.31146394, 17.98980105,
       7.86085564, 5.29526945, 27.69555992, 10.51869112, 9.12514394,
       12.60532735, 9.42688905, 7.88762618, 19.69945392, 9.63372543,
       8.97501221, 18.94255005, 20.98217881, 14.12336521, 16.36382061,
       21.32440567, 21.32959254, 10.88427173, 26.25786993, 27.34951229,
      31.14016596, 9.80477376]), kurtosis=array([ 51.71558405,
                                                                 93.89016173,
13.18839908, 785.40163828,
                                      66.53150801, 198.68010939,
        28.69487647,
                       31.20576951,
        28.29530115, 185.40607771,
                                      34.48800593,
                                                     15.18712484,
       109.66544541, 138.05561341,
                                      44.19188958,
                                                     55.62892
        47.49151277,
                      52.75647121,
                                       6.32523058,
                                                     77.87379384,
         8.48736408, 103.7022867,
                                     49.37553046, 272.09125904,
        42.43992409,
                     49.41302953,
                                      33.63974328,
                                                    39.86629858,
       166.19735746, 53.12216402,
                                      91.72439904, 124.79234055,
       433.42661801, 123.97955409,
                                     555.16708959,
                                                   86.72460731,
        43.92486688, 865.39968623,
                                     181.33012173, 100.87592785,
       189.11563172, 111.21705016,
                                      81.96093958, 567.75150773,
```

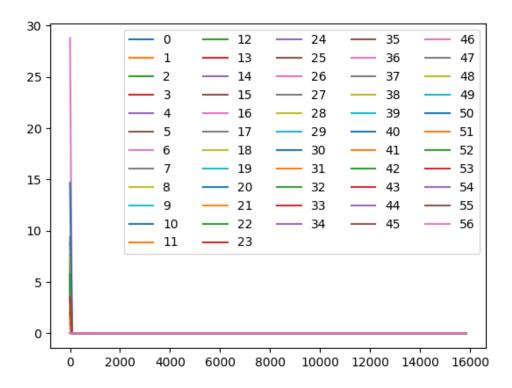
```
147.5283386 , 107.79164424 , 445.8361165 , 634.57001982 , 228.75884956 , 499.07842266 , 588.19774644 , 688.05527222 , 184.31757803 , 851.48819158 , 954.59095344 , 1348.49464105 , 183.78053905]))
```

#### [271]: scipy.stats.describe(y)

[271]: DescribeResult(nobs=3065, minmax=(np.int64(0), np.int64(1)),
 mean=np.float64(0.39738988580750406), variance=np.float64(0.23954932085067235),
 skewness=np.float64(0.41936632478193103),
 kurtosis=np.float64(-1.824131885638896))

```
[272]: # plot the distribution of all features
nextplot()
densities = [scipy.stats.gaussian_kde(X[:, j]) for j in range(D)]
xs = np.linspace(0, np.max(X), 200)
for j in range(D):
    plt.plot(xs, densities[j](xs), label=j)
plt.legend(ncol=5)
```

[272]: <matplotlib.legend.Legend at 0x7be9dbb03ac0>



```
[273]: # this plots is not really helpful; go now explore further # YOUR CODE HERE
```

#### 4 First Observation

• there is a very high spike around [0, 1]

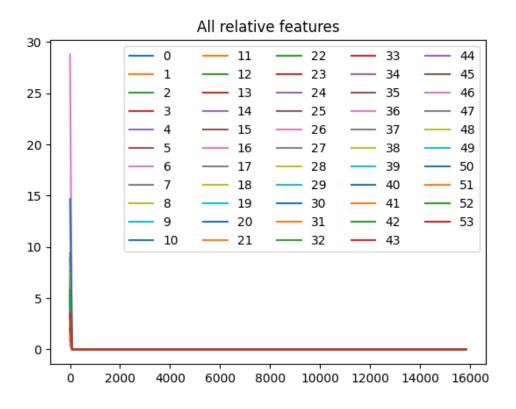
```
[274]: import pandas as pd
      df = pd.DataFrame(X)
      df.head()
[274]:
           0
                                  4
                                        5
                  1
                       2
                            3
                                              6
                                                    7
                                                          8
                                                                9
                                                                        47
                                                                             48
                                     0.28
         0.21
               0.28
                               0.14
                                            0.21
                                                  0.07
                                                        0.00
                                                              0.94
                                                                       0.0
                      0.5
                          0.0
                                                                            0.0
         0.00 0.00
                     0.0 0.0
                               0.63
                                     0.00
                                            0.31
                                                  0.63
                                                        0.31
                                                              0.63
                                                                            0.0
         0.00 0.00
                      0.0 0.0 0.63
                                     0.00
                                           0.31
                                                  0.63
                                                        0.31
                                                              0.63
                                                                       0.0
      3 0.00 0.00
                     0.0 0.0
                               1.85
                                     0.00 0.00
                                                 1.85 0.00
                                                              0.00
                                                                       0.0
                                                                            0.0
      4 0.00 0.00
                     0.0 0.0
                               1.92
                                     0.00
                                           0.00
                                                  0.00
                                                       0.00
                                                              0.64
                                                                       0.0
                                                                            0.0
             49
                 50
                        51
                                52
                                       53
                                              54
                                                     55
                                                             56
         0.132
                     0.372
                            0.180
                                                         1028.0
                0.0
                                   0.048
                                          5.114
                                                  101.0
         0.137
                            0.000 0.000
                 0.0
                      0.137
                                          3.537
                                                   40.0
                                                          191.0
         0.135
                0.0
                      0.135
                            0.000 0.000
                                          3.537
                                                   40.0
                                                          191.0
      3 0.223
                0.0
                     0.000 0.000 0.000
                                          3.000
                                                   15.0
                                                           54.0
      4 0.054
                0.0
                     0.164 0.054 0.000
                                          1.671
                                                    4.0
                                                          112.0
      [5 rows x 57 columns]
```

#### 5 Second Observation

- the last 3 features are absolute features representing direct measurements -> this can be derived from the fact that they are not in the range of 0 and 1
- the first 54 features are relative features since they represent ratios from 0 to 1.

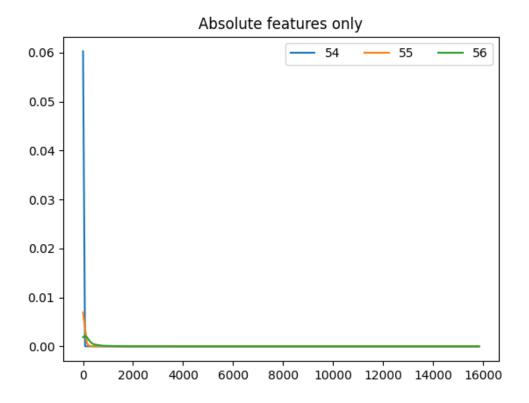
```
[275]: nextplot()
  densities = [scipy.stats.gaussian_kde(X[:, j]) for j in range(D-3)]
  xs = np.linspace(0, np.max(X), 200)
  for j in range(D-3):
     plt.plot(xs, densities[j](xs), label=j)
  plt.legend(ncol=5)
  plt.title('All relative features')
```

[275]: Text(0.5, 1.0, 'All relative features')

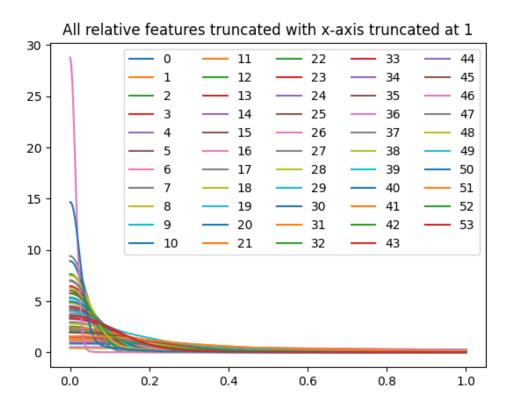


```
[276]: nextplot()
densities = [scipy.stats.gaussian_kde(X[:, j]) for j in range(D)]
xs = np.linspace(0, np.max(X), 200)
for j in range(D-3, D):
    plt.plot(xs, densities[j](xs), label=j)
plt.legend(ncol=5)
plt.title('Absolute features only')
```

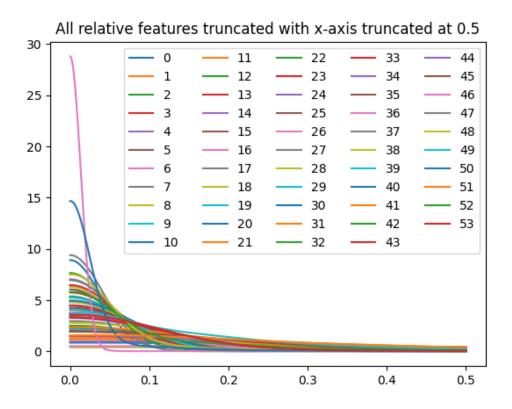
[276]: Text(0.5, 1.0, 'Absolute features only')



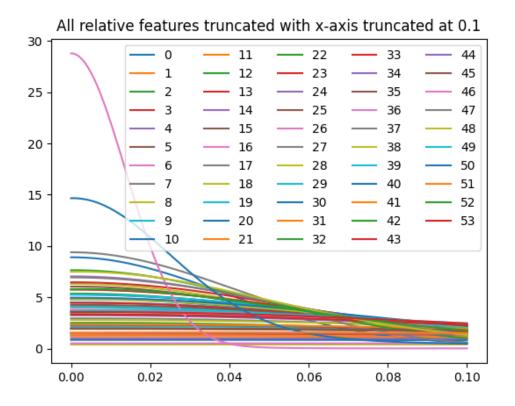
[277]: Text(0.5, 1.0, 'All relative features truncated with x-axis truncated at 1')



[278]: Text(0.5, 1.0, 'All relative features truncated with x-axis truncated at 0.5')



[279]: Text(0.5, 1.0, 'All relative features truncated with x-axis truncated at 0.1')



```
5.56379304e-17 0.00000000e+00 -1.85459768e-17 -2.43415945e-17
-4.63649420e-17 1.85459768e-17 1.85459768e-17 3.70919536e-17
-3.70919536e-17 -9.27298839e-17 -1.66913791e-16 9.27298839e-18
 1.85459768e-17 9.27298839e-18 -5.56379304e-17 -1.85459768e-17
-6.49109188e-17 -3.70919536e-17 -1.85459768e-17 1.85459768e-17
-2.78189652e-17 4.63649420e-17 -1.85459768e-17 5.56379304e-17
 0.0000000e+00 -1.85459768e-17 3.70919536e-17 1.85459768e-17
-9.27298839e-18 4.63649420e-18 1.85459768e-17 9.27298839e-18
 2.31824710e-17 -2.78189652e-17 -9.27298839e-18 4.63649420e-18
-9.27298839e-18 -9.27298839e-18 1.39094826e-17 -2.78189652e-17
-3.70919536e-17 -6.49109188e-17 4.63649420e-18 3.70919536e-17
-3.70919536e-17 9.27298839e-18 -9.27298839e-18 9.27298839e-18
-7.41839072e-17]
Standard deviation of each feature in Xz (should be ~1): [1. 1. 1. 1. 1. 1. 1.
1. 1. 1. 1. 1. 1. 1. 1. 1.]
Mean of each feature in Xtestz (should be ~0): [-5.73600192e-02 -3.37389835e-02
4.02481250e-02 5.51233798e-03
-2.51229644e-02 1.67364997e-03 5.29785531e-03 -1.38875040e-02
 1.29802458e-02 -1.00804532e-02 2.68026912e-02 1.46804853e-02
 1.28455840e-02 9.34193448e-02 -1.71666713e-02 6.17841473e-02
-3.08405298e-02 -1.02710095e-02 1.49139906e-03 6.82438979e-02
-2.45179646e-02 -4.53675036e-03 -3.12737328e-03 4.09841941e-02
 3.76515934e-02 1.15494599e-02 -3.73018154e-03 6.55839018e-02
-4.82178216e-02 2.44089391e-02 1.64408852e-02 -1.81514851e-02
 2.47142980e-02 -1.61248615e-02 1.75684573e-02 -1.33686432e-02
-4.40153254e-02 1.11212504e-02 2.40959269e-02 -1.06211719e-02
-2.06246544e-02 6.23149655e-04 -3.45073187e-02 4.24615929e-02
-1.59254291e-02 9.77429328e-05 6.85319587e-03 5.38462415e-03
 7.89156240e-03 6.81007462e-03 -2.97234292e-02 1.23785037e-02
-3.82610483e-02 -5.29891640e-02 3.19860888e-02 -6.82149671e-03
 5.35333143e-03]
Standard deviation of each feature in Xtestz (should be ~1): [0.7814603
0.8046511 1.11934658 1.13025046 1.03980406 1.14531115
1.13444999 0.89784017 1.15746733 0.80953007 1.18336095 0.96669832
0.96372882 1.43973845 0.93263701 1.66122883 0.97373622 0.94276053
0.98235473 1.64369068 0.99870796 1.05350786 1.03641016 1.4433867
1.18666147 1.09440781 0.99312029 1.32788084 0.66861325 1.13288279
1.38368011 1.00735735 1.06805083 1.01097984 0.87092113 0.9470354
0.94580152 1.16565989 1.40553929 1.06920116 0.77698549 0.9448789
0.78635376 1.27804343 1.00616124 1.02310589 1.32862863 1.12439059
1.09839086 0.9050551 0.65235216 0.79362614 0.82984222 0.22581694
1.43766401 0.58571989 0.99488232]
```

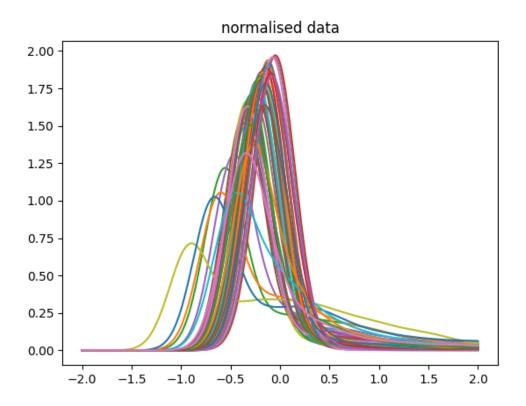
[281]: # Let's check. Xz and Xtestz refer to the normalized datasets just created. We # will use them throughout.

```
np.mean(Xz, axis=0) # should be all 0
      np.var(Xz, axis=0) # should be all 1
      np.mean(Xtestz, axis=0) # what do you get here?
      np.var(Xtestz, axis=0)
      np.sum(Xz ** 3) # should be: 1925261.15
[281]: np.float64(1925261.1560010156)
[282]: # Explore the normalized data
      # YOUR CODE HERE
      # Let's check. Xz and Xtestz refer to the normalized datasets just created. We
      # will use them throughout.
      print(np.mean(Xz, axis=0)) # should be all 0
      print(np.var(Xz, axis=0)) # should be all 1
      print(np.mean(Xtestz, axis=0)) # what do you get here?
      print(np.var(Xtestz, axis=0))
      print(np.sum(Xz ** 3)) # should be: 1925261.15
     5.56379304e-17 3.70919536e-17 0.0000000e+00 -7.41839072e-17
       5.56379304e-17 0.00000000e+00 -1.85459768e-17 -2.43415945e-17
      -4.63649420e-17 1.85459768e-17 1.85459768e-17 3.70919536e-17
      -3.70919536e-17 -9.27298839e-17 -1.66913791e-16 9.27298839e-18
       1.85459768e-17 9.27298839e-18 -5.56379304e-17 -1.85459768e-17
      -6.49109188e-17 -3.70919536e-17 -1.85459768e-17 1.85459768e-17
      -2.78189652e-17 4.63649420e-17 -1.85459768e-17 5.56379304e-17
       0.00000000e+00 -1.85459768e-17 3.70919536e-17 1.85459768e-17
      -9.27298839e-18 4.63649420e-18 1.85459768e-17 9.27298839e-18
       2.31824710e-17 -2.78189652e-17 -9.27298839e-18 4.63649420e-18
      -9.27298839e-18 -9.27298839e-18 1.39094826e-17 -2.78189652e-17
      -3.70919536e-17 -6.49109188e-17 4.63649420e-18 3.70919536e-17
      -3.70919536e-17 9.27298839e-18 -9.27298839e-18 9.27298839e-18
      -7.41839072e-17]
     1. 1. 1. 1. 1. 1. 1. 1. 1.]
     [-5.73600192e-02 -3.37389835e-02 4.02481250e-02 5.51233798e-03
      -2.51229644e-02 1.67364997e-03 5.29785531e-03 -1.38875040e-02
       1.29802458e-02 -1.00804532e-02 2.68026912e-02 1.46804853e-02
       1.28455840e-02 9.34193448e-02 -1.71666713e-02 6.17841473e-02
      -3.08405298e-02 -1.02710095e-02 1.49139906e-03 6.82438979e-02
      -2.45179646e-02 -4.53675036e-03 -3.12737328e-03 4.09841941e-02
       3.76515934e-02 1.15494599e-02 -3.73018154e-03 6.55839018e-02
```

-4.82178216e-02 2.44089391e-02 1.64408852e-02 -1.81514851e-02 2.47142980e-02 -1.61248615e-02 1.75684573e-02 -1.33686432e-02

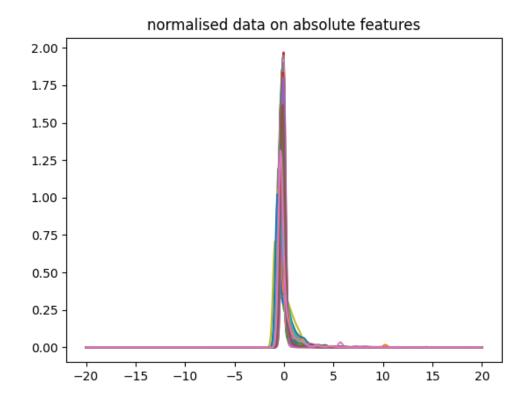
```
-4.40153254e-02 1.11212504e-02 2.40959269e-02 -1.06211719e-02
       -2.06246544e-02 6.23149655e-04 -3.45073187e-02 4.24615929e-02
       -1.59254291e-02 9.77429328e-05 6.85319587e-03 5.38462415e-03
        7.89156240e-03 6.81007462e-03 -2.97234292e-02 1.23785037e-02
       -3.82610483e-02 -5.29891640e-02 3.19860888e-02 -6.82149671e-03
        5.35333143e-031
      [0.61068019 0.64746339 1.25293677 1.2774661 1.08119249 1.31173762
       1.28697678 0.80611698 1.33973062 0.65533893 1.40034314 0.93450565
       0.92877323 2.0728468 0.86981179 2.75968123 0.94816223 0.88879741
       0.96502082 2.70171906 0.99741759 1.1098788 1.07414603 2.08336518
       1.40816544 1.19772845 0.9862879 1.76326753 0.44704368 1.28342341
       1.91457064 1.01476883 1.14073258 1.02208023 0.75850361 0.89687605
       0.89454052 1.35876298 1.97554069 1.14319113 0.60370645 0.89279613
       0.61835224 1.633395
                            1.01236044 1.04674566 1.76525404 1.2642542
       1.20646248 0.81912474 0.42556335 0.62984245 0.68863812 0.05099329
       2.06687781 0.34306778 0.98979083]
      1925261.1560010156
[283]: nextplot()
       densities = [scipy.stats.gaussian_kde(Xz[:, j]) for j in range(D)]
       xs = np.linspace(-2, 2, 500) # changing the x axis scale: most of the density_
       \hookrightarrow is between 0 and 0.4
       for j in range(D):
          plt.plot(xs, densities[j](xs)) # or features[j]
       #plt.legend(ncol=5)
       plt.title('normalised data')
```

[283]: Text(0.5, 1.0, 'normalised data')



```
[284]: nextplot()
  densities = [scipy.stats.gaussian_kde(Xz[:, j]) for j in range(D)]
  xs = np.linspace(-20, 20, 500)
  for j in range(D):
     plt.plot(xs, densities[j](xs)) # or features[j]
  #plt.legend(ncol=5)
  plt.title('normalised data on absolute features')
```

[284]: Text(0.5, 1.0, 'normalised data on absolute features')



## 6 2. Maximum Likelihood Estimation

#### 6.1 Helper functions

# and vectors.
def sigma(x):

```
[285]: def logsumexp(x):
    """Computes log(sum(exp(x)).

    Uses offset trick to reduce risk of numeric over- or underflow. When x is a
    1D ndarray, computes logsumexp of its entries. When x is a 2D ndarray,
    computes logsumexp of each column.

    Keyword arguments:
    x : a 1D or 2D ndarray
    """
    offset = np.max(x, axis=0)
    return offset + np.log(np.sum(np.exp(x - offset), axis=0))
[286]: # Define the logistic function. Make sure it operates on both scalars
```

[287]: # this should give: # [0.5, array([0.26894142, 0.5, 0.73105858])] [sigma(0), sigma(np.array([-1, 0, 1]))]

[287]: [array(0.5), array([0.26894142, 0.5 , 0.73105858])]

Logistic function

$$\log(\sigma(x)) = \log\left(\frac{1}{1+e^{-x}}\right) = -\log(1+e^{-x})$$

```
[289]: # this should give:
# [-0.69314718055994529, array([-1.31326169, -0.69314718, -0.31326169])]
[logsigma(0), logsigma(np.array([-1, 0, 1]))]
```

[289]: [array(-0.69314718), array([-1.31326169, -0.69314718, -0.31326169])]

#### 6.2 2b Log-likelihood and gradient

$$\text{log-likelihood} = \sum_{i=1}^{N} \left( y_i \cdot \log(\sigma(X_i \cdot w)) + (1 - y_i) \cdot \log(1 - \sigma(X_i \cdot w)) \right)$$

```
[290]: def l(y, X, w):
    """Log-likelihood of the logistic regression model.

Parameters
-----
y: ndarray of shape (N,)
Binary labels (either 0 or 1).
X: ndarray of shape (N,D)
```

```
Design matrix.

w: ndarray of shape (D,)
Weight vector.

"""

# YOUR CODE HERE
# Compute the linear combination X @ w once
z = np.dot(X, w)

# Use z and -z in logsigma, avoiding recomputation
return np.sum(y * logsigma(z) + (1 - y) * logsigma(-z))
```

```
[291]: # this should give:
# -47066.641667825766
l(y, Xz, np.linspace(-5, 5, D))
```

[291]: np.float64(-47066.64166782577)

The gradient is calculated as

$$\frac{\partial l}{\partial w} = X^T \cdot (y - \sigma(X \cdot w))$$

```
[292]: def dl(y, X, w):
           """Gradient of the log-likelihood of the logistic regression model.
           Parameters
           y : ndarray \ of \ shape \ (N,)
               Binary labels (either 0 or 1).
           X: ndarray of shape (N,D)
              Design matrix.
           w: ndarray of shape (D,)
               Weight vector.
           Returns
           ndarray of shape (D,)
           # YOUR CODE HERE
           # Compute the predicted probabilities
           predictions = sigma(np.dot(X, w))
           # Calculate the gradient as X.T @ (y - predictions)
           return np.dot(X.T, (y - predictions))
```

```
[293]: # this should give:

# array([ 551.33985842, 143.84116318, 841.83373606, 156.87237578,

# 802.61217579, 795.96202907, 920.69045803, 621.96516752,
```

```
470.81259805,
                                          771.32406968,
                                                        352.40325626,
          659.18724769,
                                                        864.83981264,
                          234.36600888, 562.45454038,
          455.66972482,
          787.19723703,
                          649.48042176, 902.6478154,
                                                        544.00539886,
#
                          120.3598967, 839.61141672,
                                                        633.30453444,
          1174.78638035,
#
          -706.66815087,
                         -630.2039816 ,
                                        -569.3451386 ,
                                                        -527.50996698,
#
         -359.53701083, -476.64334832, -411.60620464,
                                                        -375.11950586,
#
          -345.37195689,
                         -376.22044258, -407.31761977,
                                                        -456.23251936,
#
         -596.86960184,
                         -107.97072355, -394.82170044,
                                                        -229.18125598,
          -288.46356547,
                         -362.13402385, -450.87896465,
                                                        -277.03932676,
          -414.99293368, -452.28771693, -167.54649092,
                                                        -270.9043748 ,
                        -357.72497343, -259.12468742,
                                                        418.35938483,
#
          -252.20140951,
#
          604.54173228,
                          43.10390907, 152.24258478,
                                                         378.16731033,
          416.12032881])
dl(y, Xz, np.linspace(-5, 5, D))
```

```
[293]: array([ 551.33985842, 143.84116318, 841.83373606, 156.87237578,
              802.61217579, 795.96202907,
                                            920.69045803, 621.96516752,
              659.18724769, 470.81259805, 771.32406968, 352.40325626,
              455.66972482, 234.36600888, 562.45454038, 864.83981264,
              787.19723703, 649.48042176, 902.6478154, 544.00539886,
             1174.78638035, 120.3598967, 839.61141672, 633.30453444,
             -706.66815087, -630.2039816 , -569.3451386 , -527.50996698,
             -359.53701083, -476.64334832, -411.60620464, -375.11950586,
             -345.37195689, -376.22044258, -407.31761977, -456.23251936,
             -596.86960184, -107.97072355, -394.82170044, -229.18125598,
             -288.46356547, -362.13402385, -450.87896465, -277.03932676,
             -414.99293368, -452.28771693, -167.54649092, -270.9043748 ,
             -252.20140951, -357.72497343, -259.12468742, 418.35938483,
              604.54173228,
                              43.10390907, 152.24258478, 378.16731033,
              416.12032881])
```

#### 6.3 2c Gradient descent

```
[294]: # you don't need to modify this function

def optimize(obj_up, theta0, nepochs=50, eps0=0.01, verbose=True):
    """Iteratively minimize a function.

We use it here to run either gradient descent or stochastic gradient
    descent, using arbitrarly optimization criteria.

Parameters
-----
obj_up: a tuple of form (f, update) containing two functions f and update.
    f(theta) computes the value of the objective function.
        update(theta,eps) performs an epoch of parameter update with step_

size
eps and returns the result.
```

```
theta0 : ndarray of shape (D,)
          Initial parameter vector.
nepochs: int
          How many epochs (calls to update) to run.
eps0
        : float
          Initial step size.
verbose : boolean
          Whether to print progress information.
Returns
_____
A triple consisting of the fitted parameter vector, the values of the
objective function after every epoch, and the step sizes that were used.
11 11 11
f, update = obj_up
# initialize results
theta = theta0
values = np.zeros(nepochs + 1)
eps = np.zeros(nepochs + 1)
values[0] = f(theta0)
eps[0] = eps0
# now run the update function nepochs times
for epoch in range(nepochs):
    if verbose:
        print(
            "Epoch {:3d}: f={:10.3f}, eps={:10.9f}".format(
                epoch, values[epoch], eps[epoch]
            )
    theta = update(theta, eps[epoch])
    # we use the bold driver heuristic
    values[epoch + 1] = f(theta)
    if values[epoch] < values[epoch + 1]:</pre>
        eps[epoch + 1] = eps[epoch] / 2.0
    else:
        eps[epoch + 1] = eps[epoch] * 1.05
# all done
if verbose:
    print("Result after {} epochs: f={}".format(nepochs, values[-1]))
return theta, values, eps
```

```
[295]: | # define the objective and update function for one gradient-descent epoch for
       # fitting an MLE estimate of logistic regression with gradient descent (should
       # return a tuple of two functions; see optimize)
       def gd(y, X):
            """Defines the objective and update functions for one gradient descent_{\sqcup}
        \hookrightarrow epoch
            to fit an MLE estimate of logistic regression.
           Parameters
            y : ndarray of shape (N,)
                Binary labels (either 0 or 1).
           X : ndarray \ of \ shape \ (N, D)
                Design matrix.
           Returns
            _____
            tuple
                A tuple containing:
                - objective: Function that computes the negative log-likelihood.
                - update: Function that updates weights with a single gradient descent \sqcup
         \hookrightarrow step.
            11 11 11
           def objective(w):
                """Objective function: Negative log-likelihood of logistic regression.
         \hookrightarrow " " "
                return -l(y, X, w)
           def update(w, eps):
                """Update function: Performs a gradient descent step."""
                return w + eps * dl(y, X, w)
           return (objective, update)
```

```
[296]: # this should give
      # [47066.641667825766,
      # array([ 4.13777838e+01, -1.56745627e+01, 5.75882538e+01,
      #
                  1.14225143e+01, 5.54249703e+01, 5.99229049e+01,
                  7.11220141e+01,
                                  4.84761728e+01, 5.78067289e+01,
      #
                  4.54794720e+01, 7.14638492e+01, 1.51369386e+01,
                  3.36375739e+01,
      #
                                  2.15061217e+01, 5.78014255e+01,
      #
                 6.72743066e+01, 7.00829312e+01, 5.29328088e+01,
      #
                 6.16042473e+01, 5.50018510e+01, 8.94624817e+01,
      #
                 2.74784480e+01, 8.51763599e+01,
                                                   5.60363965e+01,
      #
                 -2.55865589e+01, -1.53788213e+01, -4.67015412e+01,
                 -2.50356570e+00, -3.85357592e+00, -2.21819155e+00,
```

```
3.32098671e+00,
                                    3.86933390e+00,
                                                     -2.00309898e+01,
                  3.84684492e+00,
                                   -2.19847927e-01,
                                                     -1.29775457e+00,
                 -1.28374302e+01,
       #
                                   -2.78303173e+00,
                                                     -5.61671182e+00,
       #
                  1.73657121e+01,
                                   -6.81197570e+00,
                                                     -1.20249002e+01,
                  2.65789491e+00,
                                   -1.39557852e+01,
                                                     -2.01135653e+01,
       #
                 -2.72134051e+01, -9.45952961e-01,
                                                    -1.02239111e+01,
       #
                  1.52794293e-04, -5.18938123e-01,
                                                    -3.19717561e+00,
       #
                  4.62953437e+01,
                                   7.87893022e+01,
                                                    1.88618651e+01,
                  2.85195027e+01,
                                   5.04698358e+01,
                                                    6.41240689e+01])
      f, update = gd(y, Xz)
       [f(np.linspace(-5, 5, D)), update(np.linspace(-5, -5, D), 0.1)]
[296]: [np.float64(47066.64166782577),
       array([ 4.13777838e+01, -1.56745627e+01, 5.75882538e+01, 1.14225143e+01,
               5.54249703e+01, 5.99229049e+01, 7.11220141e+01, 4.84761728e+01,
               5.78067289e+01, 4.54794720e+01, 7.14638492e+01, 1.51369386e+01,
               3.36375739e+01, 2.15061217e+01, 5.78014255e+01, 6.72743066e+01,
               7.00829312e+01, 5.29328088e+01, 6.16042473e+01, 5.50018510e+01,
               8.94624817e+01, 2.74784480e+01, 8.51763599e+01, 5.60363965e+01,
              -2.55865589e+01, -1.53788213e+01, -4.67015412e+01, -2.50356570e+00,
              -3.85357592e+00, -2.21819155e+00, 3.32098671e+00, 3.86933390e+00,
              -2.00309898e+01, 3.84684492e+00, -2.19847927e-01, -1.29775457e+00,
              -1.28374302e+01, -2.78303173e+00, -5.61671182e+00, 1.73657121e+01,
              -6.81197570e+00, -1.20249002e+01, 2.65789491e+00, -1.39557852e+01,
              -2.01135653e+01, -2.72134051e+01, -9.45952961e-01, -1.02239111e+01,
               1.52794293e-04, -5.18938123e-01, -3.19717561e+00, 4.62953437e+01,
               7.87893022e+01, 1.88618651e+01, 2.85195027e+01, 5.04698358e+01,
               6.41240689e+01])]
[297]: # you can run gradient descent!
      numpy.random.seed(0)
      w0 = np.random.normal(size=D)
      wz_gd, vz_gd, ez_gd = optimize(gd(y, Xz), w0, nepochs=500)
             0: f= 6636.208, eps=0.010000000
      Epoch
      Epoch
             1: f= 4216.957, eps=0.010500000
      Epoch
             2: f= 2657.519, eps=0.011025000
             3: f= 1926.135, eps=0.011576250
      Epoch
      Epoch
             4: f= 1449.495, eps=0.012155063
      Epoch
             5: f= 1207.529, eps=0.012762816
      Epoch
             6: f= 1052.489, eps=0.013400956
      Epoch 7: f=
                     957.275, eps=0.014071004
      Epoch
             8: f=
                      899.610, eps=0.014774554
      Epoch
             9: f=
                      882.904, eps=0.015513282
      Epoch 10: f= 1017.083, eps=0.007756641
      Epoch 11: f=
                     840.760, eps=0.008144473
      Epoch 12: f=
                      805.649, eps=0.008551697
```

```
Epoch 13: f=
                822.108, eps=0.004275848
Epoch
      14: f=
                746.377, eps=0.004489641
Epoch
      15: f=
                735.803, eps=0.004714123
                729.780, eps=0.004949829
Epoch
      16: f=
Epoch
      17: f=
                724.467, eps=0.005197320
                719.408, eps=0.005457186
Epoch
      18: f=
Epoch
      19: f=
                714.564, eps=0.005730046
Epoch 20: f=
                709.932, eps=0.006016548
Epoch 21: f=
                705.514, eps=0.006317375
Epoch 22: f=
                701.321, eps=0.006633244
Epoch 23: f=
                697.373, eps=0.006964906
Epoch 24: f=
                693.728, eps=0.007313152
                690.591, eps=0.007678809
Epoch 25: f=
Epoch 26: f=
                688.614, eps=0.008062750
Epoch 27: f=
                688.607, eps=0.008465887
Epoch 28: f=
                690.854, eps=0.004232944
Epoch 29: f=
                679.967, eps=0.004444591
Epoch 30: f=
                678.649, eps=0.004666820
Epoch 31: f=
                677.447, eps=0.004900161
Epoch
      32: f=
                676.292, eps=0.005145169
Epoch
      33: f=
                675.182, eps=0.005402428
Epoch 34: f=
                674.120, eps=0.005672549
Epoch 35: f=
                673.114, eps=0.005956177
Epoch 36: f=
                672.177, eps=0.006253986
                671.334, eps=0.006566685
Epoch 37: f=
Epoch 38: f=
                670.656, eps=0.006895019
                670.397, eps=0.007239770
Epoch 39: f=
Epoch 40: f=
                671.342, eps=0.003619885
Epoch 41: f=
                668.932, eps=0.003800879
Epoch 42: f=
                668.378, eps=0.003990923
Epoch 43: f=
                668.027, eps=0.004190469
Epoch 44: f=
                667.720, eps=0.004399993
Epoch 45: f=
                667.433, eps=0.004619993
Epoch 46: f=
                667.159, eps=0.004850992
Epoch 47: f=
                666.897, eps=0.005093542
Epoch 48: f=
                666.650, eps=0.005348219
Epoch 49: f=
                666.417, eps=0.005615630
Epoch 50: f=
                666.201, eps=0.005896411
Epoch 51: f=
                666.008, eps=0.006191232
Epoch 52: f=
                665.858, eps=0.006500794
Epoch 53: f=
                665.812, eps=0.006825833
Epoch 54: f=
                666.068, eps=0.003412917
Epoch 55: f=
                665.424, eps=0.003583562
Epoch 56: f=
                665.290, eps=0.003762741
Epoch 57: f=
                665.204, eps=0.003950878
Epoch 58: f=
                665.128, eps=0.004148421
Epoch 59: f=
                665.054, eps=0.004355843
Epoch 60: f=
                664.982, eps=0.004573635
```

```
Epoch 61: f=
                664.911, eps=0.004802316
Epoch 62: f=
                664.842, eps=0.005042432
                664.773, eps=0.005294554
Epoch
      63: f=
                664.707, eps=0.005559282
Epoch
      64: f=
Epoch 65: f=
                664.641, eps=0.005837246
                664.578, eps=0.006129108
Epoch
      66: f=
Epoch
      67: f=
                664.518, eps=0.006435563
Epoch 68: f=
                664.467, eps=0.006757341
Epoch 69: f=
                664.446, eps=0.007095208
Epoch 70: f=
                664.544, eps=0.003547604
Epoch 71: f=
                664.339, eps=0.003724984
Epoch 72: f=
                664.278, eps=0.003911234
Epoch 73: f=
                664.239, eps=0.004106795
Epoch 74: f=
                664.206, eps=0.004312135
Epoch 75: f=
                664.173, eps=0.004527742
Epoch 76: f=
                664.139, eps=0.004754129
Epoch 77: f=
                664.106, eps=0.004991835
Epoch 78: f=
                664.072, eps=0.005241427
Epoch 79: f=
                664.037, eps=0.005503499
Epoch 80: f=
                664.002, eps=0.005778674
Epoch
      81: f=
                663.967, eps=0.006067607
Epoch 82: f=
                663.936, eps=0.006370988
Epoch 83: f=
                663.918, eps=0.006689537
Epoch 84: f=
                663.948, eps=0.003344768
Epoch 85: f=
                663.839, eps=0.003512007
Epoch 86: f=
                663.807, eps=0.003687607
                663.783, eps=0.003871988
Epoch 87: f=
Epoch 88: f=
                663.760, eps=0.004065587
                663.737, eps=0.004268866
Epoch 89: f=
Epoch 90: f=
                663.713, eps=0.004482310
Epoch 91: f=
                663.688, eps=0.004706425
Epoch 92: f=
                663.661, eps=0.004941746
Epoch 93: f=
                663.634, eps=0.005188834
Epoch 94: f=
                663.606, eps=0.005448275
Epoch 95: f=
                663.576, eps=0.005720689
Epoch 96: f=
                663.546, eps=0.006006724
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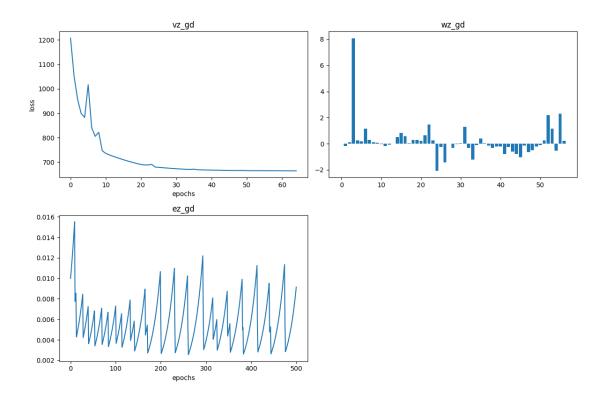
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                656.504, eps=0.007464239
Epoch 436: f=
                656.482, eps=0.007837451
Epoch 437: f=
                656.459, eps=0.008229324
Epoch 438: f=
                656.435, eps=0.008640790
Epoch 439: f=
                656.410, eps=0.009072829
Epoch 440: f=
                656.388, eps=0.009526471
Epoch 441: f=
                656.406, eps=0.004763235
Epoch 442: f=
                656.387, eps=0.005001397
Epoch 443: f=
                656.379, eps=0.005251467
Epoch 444: f=
                656.381, eps=0.002625734
```

```
Epoch 445: f=
                656.303, eps=0.002757020
Epoch 446: f=
                656.295, eps=0.002894871
Epoch 447: f=
                656.286, eps=0.003039615
                656.277, eps=0.003191596
Epoch 448: f=
Epoch 449: f=
                656.268, eps=0.003351175
Epoch 450: f=
                656.258, eps=0.003518734
Epoch 451: f=
                656.248, eps=0.003694671
Epoch 452: f=
                656.237, eps=0.003879404
Epoch 453: f=
                656.226, eps=0.004073375
Epoch 454: f=
                656.214, eps=0.004277043
Epoch 455: f=
                656.202, eps=0.004490895
Epoch 456: f=
                656.189, eps=0.004715440
Epoch 457: f=
                656.175, eps=0.004951212
Epoch 458: f=
                656.161, eps=0.005198773
Epoch 459: f=
                656.145, eps=0.005458711
Epoch 460: f=
                656.130, eps=0.005731647
Epoch 461: f=
                656.113, eps=0.006018229
Epoch 462: f=
                656.096, eps=0.006319141
Epoch 463: f=
                656.077, eps=0.006635098
Epoch 464: f=
                656.058, eps=0.006966853
Epoch 465: f=
                656.038, eps=0.007315195
Epoch 466: f=
                656.017, eps=0.007680955
Epoch 467: f=
                655.995, eps=0.008065003
Epoch 468: f=
                655.972, eps=0.008468253
Epoch 469: f=
                655.948, eps=0.008891666
Epoch 470: f=
                655.923, eps=0.009336249
Epoch 471: f=
                655.896, eps=0.009803061
Epoch 472: f=
                655.868, eps=0.010293215
Epoch 473: f=
                655.841, eps=0.010807875
Epoch 474: f=
                655.835, eps=0.011348269
Epoch 475: f=
                656.135, eps=0.005674135
Epoch 476: f=
                656.301, eps=0.002837067
Epoch 477: f=
                655.760, eps=0.002978921
Epoch 478: f=
                655.744, eps=0.003127867
Epoch 479: f=
                655.735, eps=0.003284260
Epoch 480: f=
                655.725, eps=0.003448473
Epoch 481: f=
                655.716, eps=0.003620897
Epoch 482: f=
                655.705, eps=0.003801941
Epoch 483: f=
                655.695, eps=0.003992039
Epoch 484: f=
                655.684, eps=0.004191640
Epoch 485: f=
                655.672, eps=0.004401222
Epoch 486: f=
                655.659, eps=0.004621284
Epoch 487: f=
                655.646, eps=0.004852348
Epoch 488: f=
                655.633, eps=0.005094965
Epoch 489: f=
                655.619, eps=0.005349713
Epoch 490: f=
                655.604, eps=0.005617199
Epoch 491: f=
                655.588, eps=0.005898059
Epoch 492: f=
                655.571, eps=0.006192962
```

```
Epoch 493: f=
                      655.554, eps=0.006502610
      Epoch 494: f=
                      655.536, eps=0.006827741
      Epoch 495: f=
                      655.517, eps=0.007169128
      Epoch 496: f=
                      655.497, eps=0.007527584
      Epoch 497: f=
                      655.476, eps=0.007903963
                      655.454, eps=0.008299161
      Epoch 498: f=
      Epoch 499: f=
                      655.432, eps=0.008714119
      Result after 500 epochs: f=655.413496469947
[298]: # Visualize the progress of gradient descent for vz_gd, wz_gd, and ez_gd
       fig, axes = plt.subplots(2, 2, figsize=(12, 8)) # Create a 2x2 grid for_
        \hookrightarrow subplots
       # Plot vz_gd progress
       axes[0, 0].plot(vz_gd[5:70])
       axes[0, 0].set_xlabel('epochs')
       axes[0, 0].set_ylabel('loss')
       axes[0, 0].set_title('vz_gd')
       # Plot wz_qd as a bar chart
       axes[0, 1].bar(range(len(wz_gd)), wz_gd)
       axes[0, 1].set_title('wz_gd')
       # Plot ez_gd convergence
       axes[1, 0].plot(ez_gd)
       axes[1, 0].set_xlabel('epochs')
       axes[1, 0].set_title('ez_gd')
       # Hide the unused subplot (bottom-right)
       axes[1, 1].axis('off')
       plt.tight_layout() # Adjust spacing between plots
       plt.show()
```



## 6.4 2d Stochastic gradient descent

```
[299]: def sgdepoch(y, X, w, eps):
           """Run one SGD epoch and return the updated weight vector. """
           # Run N stochastic gradient steps (without replacement). Do not rescale each
           \# step by factor N (i.e., proceed differently than in the lecture slides).
           # YOUR CODE HERE
           # Shuffle indices for stochastic updates
          for i in np.random.permutation(len(X)):
               # Store the feature vector of the i-th sample
               xi = X[i]
               # Update weights with the stochastic gradient
               w = w + eps * (y[i] - sigma(np.dot(w, xi))) * xi
          return w
[300]: # when you run this multiple times, with 50% probability you should get the
       # following result (there is one other result which is very close):
       # array([ -3.43689655e+02, -1.71161311e+02,
                                                     -5.71093536e+02,
       #
                 -5.16478220e+01, 4.66294348e+02, -3.71589878e+02,
       #
                  5.21493183e+02,
                                  1.25699230e+03,
                                                      8.33804130e+02,
       #
                  5.63185399e+02, 1.32761302e+03, -2.64104011e+02,
       #
                  7.10693307e+02, -1.75497331e+02,
                                                     -1.94174427e+02,
```

1.11641507e+02, -3.30817509e+02, -3.46754913e+02,

```
8.48722111e+02, -1.89136304e+02,
                                                     -4.25693844e+02,
                 -1.23084189e+02, -2.95894797e+02,
       #
                                                     -2.35789333e+02,
       #
                 -3.38695243e+02, -3.05642830e+02, -2.28975383e+02,
       #
                 -2.38075137e+02, -1.66702530e+02,
                                                    -2.27341599e+02,
       #
                 -1.77575620e+02, -1.49093855e+02,
                                                     -1.70028859e+02,
       #
                 -1.50243833e+02, -1.82986008e+02, -2.41143708e+02,
                 -3.31047159e+02, -5.79991185e+01, -1.98477863e+02,
       #
       #
                 -1.91264948e+02, -1.17371919e+02,
                                                     -1.66953779e+02,
       #
                 -2.01472565e+02, -1.23330949e+02,
                                                     -3.00857740e+02,
       #
                 -1.95853348e+02, -7.44868073e+01, -1.11172370e+02,
       #
                 -1.57618226e+02, -1.25729512e+00,
                                                    -1.45536466e+02,
                 -1.43362438e+02, -3.00429708e+02, -9.84391082e+01,
                 -4.54152047e+01, -5.26492232e+01, -1.45175427e+02])
      sgdepoch(y[1:3], Xz[1:3, :], np.linspace(-5, 5, D), 1000)
      /tmp/ipykernel_32055/4243986844.py:8: RuntimeWarning: overflow encountered in
      exp
        np.exp(x) / (1 + np.exp(x)))
      /tmp/ipykernel_32055/4243986844.py:8: RuntimeWarning: invalid value encountered
      in scalar divide
        np.exp(x) / (1 + np.exp(x)))
[300]: array([-3.43689655e+02, -1.71161311e+02, -5.71093536e+02, -5.16478220e+01,
              4.66294348e+02, -3.71589878e+02, 5.21493183e+02, 1.25699230e+03,
              8.33804130e+02, 5.63185399e+02, 1.32761302e+03, -2.64104011e+02,
              7.10693307e+02, -1.75497331e+02, -1.94174427e+02, 1.11641507e+02,
             -3.30817509e+02, -3.46754913e+02, 8.48722111e+02, -1.89136304e+02,
             -4.25693844e+02, -1.23084189e+02, -2.95894797e+02, -2.35789333e+02,
             -3.38695243e+02, -3.05642830e+02, -2.28975383e+02, -2.38075137e+02,
             -1.66702530e+02, -2.27341599e+02, -1.77575620e+02, -1.49093855e+02,
             -1.70028859e+02, -1.50243833e+02, -1.82986008e+02, -2.41143708e+02,
             -3.31047159e+02, -5.79991185e+01, -1.98477863e+02, -1.91264948e+02,
             -1.17371919e+02, -1.66953779e+02, -2.01472565e+02, -1.23330949e+02,
             -3.00857740e+02, -1.95853348e+02, -7.44868073e+01, -1.11172370e+02,
             -1.57618226e+02, -1.25729512e+00, -1.45536466e+02, -1.43362438e+02,
             -3.00429708e+02, -9.84391082e+01, -4.54152047e+01, -5.26492232e+01,
             -1.45175427e+02])
[301]: | # define the objective and update function for one gradient-descent epoch for
       # fitting an MLE estimate of logistic regression with stochastic gradient,
        \hookrightarrow descent
       # (should return a tuple of two functions; see optimize)
      def sgd(y, X):
          def objective(w):
               # YOUR CODE HERE
               """Objective function: Negative log-likelihood of logistic regression.
```

```
return -1(y, X, w)

def update(w, eps):
    return sgdepoch(y, X, w, eps)

return (objective, update)

[302]: # with 50% probability, you should get:
    # [40.864973045695081,
    # array([ -3.43689655e+02, -1.71161311e+02, -5.71093536e+02,
    # -5.16478220e+01, 4.66294348e+02, -3.71589878e+02,
    # 5.21493183e+02, 1.25699230e+03, 8.33804130e+02.
```

```
5.21493183e+02, 1.25699230e+03, 8.33804130e+02,
#
           5.63185399e+02, 1.32761302e+03, -2.64104011e+02,
           7.10693307e+02, -1.75497331e+02, -1.94174427e+02,
#
#
           1.11641507e+02, -3.30817509e+02, -3.46754913e+02,
#
           8.48722111e+02,
                            -1.89136304e+02,
                                             -4.25693844e+02,
#
           -1.23084189e+02, -2.95894797e+02,
                                             -2.35789333e+02,
#
           -3.38695243e+02,
                            -3.05642830e+02,
                                              -2.28975383e+02,
#
           -2.38075137e+02,
                            -1.66702530e+02,
                                             -2.27341599e+02,
#
          -1.77575620e+02, -1.49093855e+02,
                                             -1.70028859e+02,
#
          -1.50243833e+02, -1.82986008e+02, -2.41143708e+02,
#
          -3.31047159e+02, -5.79991185e+01,
                                             -1.98477863e+02,
#
          -1.91264948e+02,
                            -1.17371919e+02,
                                             -1.66953779e+02,
#
          -2.01472565e+02, -1.23330949e+02, -3.00857740e+02,
#
           -1.95853348e+02,
                            -7.44868073e+01,
                                             -1.11172370e+02,
#
           -1.57618226e+02, -1.25729512e+00, -1.45536466e+02,
#
           -1.43362438e+02, -3.00429708e+02, -9.84391082e+01,
           -4.54152047e+01, -5.26492232e+01, -1.45175427e+02])]
f, update = sgd(y[1:3], Xz[1:3, :])
[f(np.linspace(-5, 5, D)), update(np.linspace(-5, 5, D), 1000)]
```

```
-1.70028859e+02, -1.50243833e+02, -1.82986008e+02, -2.41143708e+02,
               -3.31047159e+02, -5.79991185e+01, -1.98477863e+02, -1.91264948e+02,
               -1.17371919e+02, -1.66953779e+02, -2.01472565e+02, -1.23330949e+02,
               -3.00857740e+02, -1.95853348e+02, -7.44868073e+01, -1.11172370e+02,
               -1.57618226e+02, -1.25729512e+00, -1.45536466e+02, -1.43362438e+02,
               -3.00429708e+02, -9.84391082e+01, -4.54152047e+01, -5.26492232e+01,
               -1.45175427e+02])]
[303]: # you can run stochastic gradient descent!
      wz_sgd, vz_sgd, ez_sgd = optimize(sgd(y, Xz), w0, nepochs=500)
      Epoch
              0: f=
                     6636.208, eps=0.010000000
      Epoch
                      958.654, eps=0.010500000
              1: f=
      Epoch
              2: f=
                      786.651, eps=0.011025000
      Epoch
              3: f=
                      738.739, eps=0.011576250
      Epoch
              4: f=
                      718.166, eps=0.012155063
      Epoch
              5: f=
                      709.413, eps=0.012762816
      Epoch
              6: f=
                      696.048, eps=0.013400956
             7: f=
      Epoch
                      701.674, eps=0.006700478
      Epoch
              8: f=
                      686.406, eps=0.007035502
      Epoch
              9: f=
                      683.692, eps=0.007387277
      Epoch 10: f=
                      684.500, eps=0.003693639
      Epoch 11: f=
                      679.969, eps=0.003878321
      Epoch 12: f=
                      679.230, eps=0.004072237
      Epoch 13: f=
                      678.181, eps=0.004275848
      Epoch 14: f=
                      677.570, eps=0.004489641
      Epoch 15: f=
                      676.763, eps=0.004714123
                      675.966, eps=0.004949829
      Epoch 16: f=
      Epoch 17: f=
                      676.625, eps=0.002474914
      Epoch 18: f=
                      675.185, eps=0.002598660
      Epoch 19: f=
                      674.531, eps=0.002728593
      Epoch 20: f=
                      674.095, eps=0.002865023
      Epoch 21: f=
                      673.692, eps=0.003008274
      Epoch 22: f=
                      673.359, eps=0.003158688
      Epoch 23: f=
                      673.075, eps=0.003316622
      Epoch 24: f=
                      672.914, eps=0.003482453
      Epoch 25: f=
                      672.549, eps=0.003656576
      Epoch 26: f=
                      672.208, eps=0.003839405
      Epoch 27: f=
                      672.128, eps=0.004031375
      Epoch 28: f=
                      671.943, eps=0.004232944
      Epoch 29: f=
                      671.364, eps=0.004444591
```

671.437, eps=0.002222295

670.780, eps=0.002333410

670.619, eps=0.002450081

670.405, eps=0.002572585 670.230, eps=0.002701214

670.065, eps=0.002836275

Epoch 30: f=

Epoch 31: f=

Epoch 32: f=

Epoch 33: f=

Epoch 34: f= Epoch 35: f=

```
Epoch 36: f=
                669.883, eps=0.002978088
Epoch 37: f=
                669.804, eps=0.003126993
                669.708, eps=0.003283342
Epoch
      38: f=
                669.592, eps=0.003447510
Epoch
      39: f=
Epoch 40: f=
                669.531, eps=0.003619885
                669.408, eps=0.003800879
Epoch 41: f=
Epoch 42: f=
                669.209, eps=0.003990923
Epoch 43: f=
                669.264, eps=0.001995462
Epoch 44: f=
                668.761, eps=0.002095235
Epoch 45: f=
                668.598, eps=0.002199996
                668.608, eps=0.001099998
Epoch
      46: f=
Epoch 47: f=
                668.502, eps=0.001154998
                668.400, eps=0.001212748
Epoch 48: f=
Epoch
      49: f=
                668.324, eps=0.001273385
Epoch 50: f=
                668.278, eps=0.001337055
Epoch 51: f=
                668.235, eps=0.001403907
Epoch 52: f=
                668.189, eps=0.001474103
Epoch 53: f=
                668.134, eps=0.001547808
Epoch 54: f=
                668.080, eps=0.001625198
Epoch 55: f=
                668.035, eps=0.001706458
Epoch
      56: f=
                667.966, eps=0.001791781
Epoch 57: f=
                667.927, eps=0.001881370
Epoch 58: f=
                667.878, eps=0.001975439
Epoch 59: f=
                667.813, eps=0.002074211
                667.757, eps=0.002177921
Epoch 60: f=
Epoch 61: f=
                667.722, eps=0.002286817
                667.667, eps=0.002401158
Epoch
      62: f=
Epoch
      63: f=
                667.613, eps=0.002521216
Epoch 64: f=
                667.515, eps=0.002647277
Epoch 65: f=
                667.483, eps=0.002779641
Epoch 66: f=
                667.370, eps=0.002918623
Epoch 67: f=
                667.319, eps=0.003064554
Epoch 68: f=
                667.369, eps=0.001532277
Epoch 69: f=
                667.264, eps=0.001608891
      70: f=
Epoch
                667.200, eps=0.001689335
Epoch
      71: f=
                667.172, eps=0.001773802
Epoch 72: f=
                667.112, eps=0.001862492
Epoch 73: f=
                667.006, eps=0.001955617
Epoch 74: f=
                667.045, eps=0.000977808
Epoch 75: f=
                666.973, eps=0.001026699
Epoch 76: f=
                666.911, eps=0.001078034
Epoch 77: f=
                666.884, eps=0.001131935
      78: f=
                666.844, eps=0.001188532
Epoch
Epoch 79: f=
                666.823, eps=0.001247959
Epoch 80: f=
                666.794, eps=0.001310357
Epoch
      81: f=
                666.766, eps=0.001375875
Epoch
      82: f=
                666.745, eps=0.001444668
Epoch 83: f=
                666.708, eps=0.001516902
```

```
Epoch 84: f=
                666.707, eps=0.001592747
Epoch 85: f=
                666.649, eps=0.001672384
Epoch
      86: f=
                666.632, eps=0.001756003
                666.610, eps=0.001843804
Epoch
      87: f=
Epoch 88: f=
                666.579, eps=0.001935994
Epoch
      89: f=
                666.532, eps=0.002032793
Epoch
      90: f=
                666.482, eps=0.002134433
Epoch 91: f=
                666.461, eps=0.002241155
Epoch 92: f=
                666.440, eps=0.002353213
Epoch 93: f=
                666.365, eps=0.002470873
                666.433, eps=0.001235437
Epoch 94: f=
Epoch 95: f=
                666.342, eps=0.001297208
                666.294, eps=0.001362069
Epoch
      96: f=
Epoch
      97: f=
                666.259, eps=0.001430172
Epoch 98: f=
                666.240, eps=0.001501681
Epoch 99: f=
                666.209, eps=0.001576765
Epoch 100: f=
                666.185, eps=0.001655603
Epoch 101: f=
                666.153, eps=0.001738383
Epoch 102: f=
                666.153, eps=0.001825303
Epoch 103: f=
                666.166, eps=0.000912651
Epoch 104: f=
                666.137, eps=0.000958284
Epoch 105: f=
                666.104, eps=0.001006198
Epoch 106: f=
                666.091, eps=0.001056508
Epoch 107: f=
                666.047, eps=0.001109333
Epoch 108: f=
                666.025, eps=0.001164800
Epoch 109: f=
                666.006, eps=0.001223040
Epoch 110: f=
                665.992, eps=0.001284192
Epoch 111: f=
                665.967, eps=0.001348402
Epoch 112: f=
                665.966, eps=0.001415822
Epoch 113: f=
                665.960, eps=0.001486613
Epoch 114: f=
                665.916, eps=0.001560943
Epoch 115: f=
                665.935, eps=0.000780472
Epoch 116: f=
                665.913, eps=0.000819495
Epoch 117: f=
                665.879, eps=0.000860470
Epoch 118: f=
                665.865, eps=0.000903494
Epoch 119: f=
                665.855, eps=0.000948668
Epoch 120: f=
                665.834, eps=0.000996102
Epoch 121: f=
                665.824, eps=0.001045907
Epoch 122: f=
                665.811, eps=0.001098202
Epoch 123: f=
                665.786, eps=0.001153112
Epoch 124: f=
                665.777, eps=0.001210768
Epoch 125: f=
                665.778, eps=0.000605384
Epoch 126: f=
                665.761, eps=0.000635653
Epoch 127: f=
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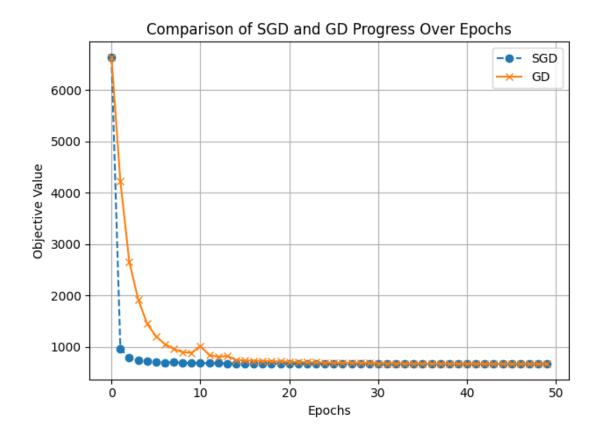
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                663.490, eps=0.000649847
Epoch 462: f=
                663.489, eps=0.000682339
Epoch 463: f=
                663.486, eps=0.000716456
Epoch 464: f=
                663.479, eps=0.000752279
Epoch 465: f=
                663.476, eps=0.000789893
Epoch 466: f=
                663.468, eps=0.000829387
Epoch 467: f=
                663.463, eps=0.000870857
```

```
Epoch 468: f=
                663.460, eps=0.000914399
Epoch 469: f=
                663.456, eps=0.000960119
Epoch 470: f=
                663.455, eps=0.001008125
                663.446, eps=0.001058532
Epoch 471: f=
Epoch 472: f=
                663.438, eps=0.001111458
                663.432, eps=0.001167031
Epoch 473: f=
Epoch 474: f=
                663.428, eps=0.001225383
Epoch 475: f=
                663.418, eps=0.001286652
Epoch 476: f=
                663.417, eps=0.001350984
Epoch 477: f=
                663.423, eps=0.000675492
Epoch 478: f=
                663.418, eps=0.000709267
Epoch 479: f=
                663.409, eps=0.000744730
Epoch 480: f=
                663.403, eps=0.000781967
Epoch 481: f=
                663.396, eps=0.000821065
Epoch 482: f=
                663.393, eps=0.000862118
Epoch 483: f=
                663.388, eps=0.000905224
Epoch 484: f=
                663.384, eps=0.000950485
Epoch 485: f=
                663.377, eps=0.000998010
Epoch 486: f=
                663.363, eps=0.001047910
Epoch 487: f=
                663.362, eps=0.001100306
Epoch 488: f=
                663.356, eps=0.001155321
Epoch 489: f=
                663.358, eps=0.000577660
Epoch 490: f=
                663.351, eps=0.000606543
Epoch 491: f=
                663.343, eps=0.000636871
Epoch 492: f=
                663.342, eps=0.000668714
Epoch 493: f=
                663.339, eps=0.000702150
                663.336, eps=0.000737257
Epoch 494: f=
Epoch 495: f=
                663.333, eps=0.000774120
Epoch 496: f=
                663.322, eps=0.000812826
Epoch 497: f=
                663.317, eps=0.000853468
Epoch 498: f=
                663.314, eps=0.000896141
Epoch 499: f=
                663.311, eps=0.000940948
Result after 500 epochs: f=663.3023109198815
```

## 6.5 2e Compare GD and SGD

```
[304]: # YOUR CODE HERE
nextplot()
plt.plot(vz_sgd[0:50], label='SGD', linestyle='--', marker='o')
plt.plot(vz_gd[0:50], label='GD', linestyle='-', marker='x')
plt.xlabel('Epochs')
plt.ylabel('Objective Value')
plt.title('Comparison of SGD and GD Progress Over Epochs')
plt.legend()
plt.grid(True) # Optional: Adds a grid for better readability
plt.tight_layout()
plt.show()
```



## 7 3 Prediction

```
[305]: def predict(Xtest, w):
    """Compute predicted confidence values for logistic regression.

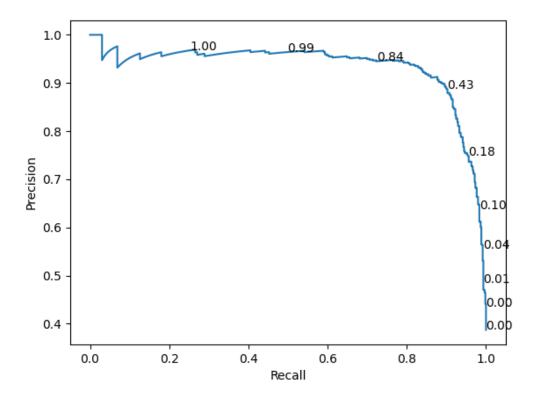
Parameters
------
Xtest : ndarray of shape (Ntest, D)
    Test data.
    w : ndarray of shape (D,)
    Weight vector for logistic regression.

Returns
-----
ndarray of shape (Ntest,)
    Vector of predicted confidence values (probabilities).
"""
return sigma(np.dot(Xtest, w))
```

```
def classify(Xtest, w):
           """Compute predicted class labels (0 or 1) for logistic regression.
           Parameters
           _____
           Xtest: ndarray of shape (Ntest, D)
               Test data.
           w : ndarray of shape (D,)
               Weight vector for logistic regression.
           Returns
           ndarray of shape (Ntest,)
               Vector of predicted class labels (0 or 1).
           return np.where(predict(Xtest, w) >= 0.5, 1, 0)
[306]: # Example: confusion matrix
       yhat = predict(Xtestz, wz_gd)
       ypred = classify(Xtestz, wz_gd)
       print(sklearn.metrics.confusion_matrix(ytest, ypred)) # true x predicted
      [[887 54]
       [ 71 524]]
[307]: # Example: classification report
       print(sklearn.metrics.classification_report(ytest, ypred))
                    precision
                                 recall f1-score
                                                     support
                 0
                         0.93
                                   0.94
                                             0.93
                                                         941
                         0.91
                                   0.88
                                             0.89
                                                         595
                 1
                                                        1536
                                             0.92
          accuracy
                                             0.91
                                                        1536
         macro avg
                         0.92
                                   0.91
      weighted avg
                         0.92
                                   0.92
                                             0.92
                                                        1536
[308]: # Example: precision-recall curve (with annotated thresholds)
       nextplot()
       precision, recall, thresholds = sklearn.metrics.precision_recall_curve(ytest,_
        →yhat)
       plt.plot(recall, precision)
       for x in np.linspace(0, 1, 10, endpoint=False):
           index = int(x * (precision.size - 1))
           plt.text(recall[index], precision[index], "{:3.2f}".
        ⇔format(thresholds[index]))
```

```
plt.xlabel("Recall")
plt.ylabel("Precision")
```

[308]: Text(0, 0.5, 'Precision')



```
[309]: # Explore which features are considered important
# both the gradient descent (wz_gd) and stochastic gradient descent (wz_sgd)

→models

# YOUR CODE HERE

for feature, weight_gd, weight_sgd in zip(features, wz_gd, wz_sgd):

print(f"{feature}: GD odds ratio = {np.exp(weight_gd):.3f}, SGD odds ratio

→= {np.exp(weight_sgd):.3f}")
```

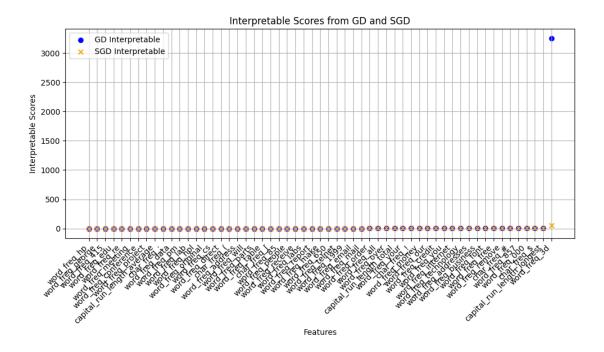
word\_freq\_make: GD odds ratio = 0.991, SGD odds ratio = 0.992
word\_freq\_address: GD odds ratio = 0.829, SGD odds ratio = 0.833
word\_freq\_all: GD odds ratio = 1.129, SGD odds ratio = 1.130
word\_freq\_3d: GD odds ratio = 3249.503, SGD odds ratio = 52.309
word\_freq\_our: GD odds ratio = 1.296, SGD odds ratio = 1.295
word\_freq\_over: GD odds ratio = 1.198, SGD odds ratio = 1.197
word\_freq\_remove: GD odds ratio = 3.169, SGD odds ratio = 3.292
word\_freq\_internet: GD odds ratio = 1.337, SGD odds ratio = 1.338

```
word_freq_order: GD odds ratio = 1.120, SGD odds ratio = 1.118
word_freq_mail: GD odds ratio = 1.068, SGD odds ratio = 1.064
word_freq_receive: GD odds ratio = 0.954, SGD odds ratio = 0.953
word_freq_will: GD odds ratio = 0.847, SGD odds ratio = 0.850
word freq people: GD odds ratio = 0.937, SGD odds ratio = 0.937
word_freq_report: GD odds ratio = 0.989, SGD odds ratio = 0.988
word freq addresses: GD odds ratio = 1.639, SGD odds ratio = 1.696
word_freq_free: GD odds ratio = 2.325, SGD odds ratio = 2.344
word freq business: GD odds ratio = 1.757, SGD odds ratio = 1.770
word_freq_email: GD odds ratio = 1.056, SGD odds ratio = 1.059
word_freq_you: GD odds ratio = 1.335, SGD odds ratio = 1.338
word_freq_credit: GD odds ratio = 1.330, SGD odds ratio = 1.358
word_freq_your: GD odds ratio = 1.243, SGD odds ratio = 1.236
word_freq_font: GD odds ratio = 1.944, SGD odds ratio = 2.001
word_freq_000: GD odds ratio = 4.313, SGD odds ratio = 4.997
word_freq_money: GD odds ratio = 1.290, SGD odds ratio = 1.304
word_freq_hp: GD odds ratio = 0.125, SGD odds ratio = 0.134
word_freq_hpl: GD odds ratio = 0.768, SGD odds ratio = 0.772
word_freq_george: GD odds ratio = 0.243, SGD odds ratio = 0.318
word freq 650: GD odds ratio = 0.999, SGD odds ratio = 1.011
word freq lab: GD odds ratio = 0.736, SGD odds ratio = 0.758
word freq labs: GD odds ratio = 0.969, SGD odds ratio = 0.962
word_freq_telnet: GD odds ratio = 1.043, SGD odds ratio = 1.067
word freq 857: GD odds ratio = 3.631, SGD odds ratio = 3.454
word_freq_data: GD odds ratio = 0.720, SGD odds ratio = 0.724
word_freq_415: GD odds ratio = 0.294, SGD odds ratio = 0.314
word_freq_85: GD odds ratio = 0.914, SGD odds ratio = 0.922
word_freq_technology: GD odds ratio = 1.497, SGD odds ratio = 1.494
word_freq_1999: GD odds ratio = 1.047, SGD odds ratio = 1.045
word_freq_parts: GD odds ratio = 0.859, SGD odds ratio = 0.858
word_freq_pm: GD odds ratio = 0.727, SGD odds ratio = 0.731
word_freq_direct: GD odds ratio = 0.806, SGD odds ratio = 0.811
word_freq_cs: GD odds ratio = 0.804, SGD odds ratio = 0.829
word_freq_meeting: GD odds ratio = 0.464, SGD odds ratio = 0.488
word freq original: GD odds ratio = 0.786, SGD odds ratio = 0.791
word freq project: GD odds ratio = 0.541, SGD odds ratio = 0.551
word freq re: GD odds ratio = 0.450, SGD odds ratio = 0.454
word_freq_edu: GD odds ratio = 0.350, SGD odds ratio = 0.369
word_freq_table: GD odds ratio = 0.861, SGD odds ratio = 0.855
word_freq_conference: GD odds ratio = 0.527, SGD odds ratio = 0.544
char_freq_;: GD odds ratio = 0.603, SGD odds ratio = 0.597
char_freq_(: GD odds ratio = 0.818, SGD odds ratio = 0.813
char_freq_[: GD odds ratio = 0.897, SGD odds ratio = 0.894
char_freq_!: GD odds ratio = 1.268, SGD odds ratio = 1.274
char_freq_$: GD odds ratio = 8.929, SGD odds ratio = 9.525
char_freq_#: GD odds ratio = 3.173, SGD odds ratio = 3.082
capital_run_length_average: GD odds ratio = 0.596, SGD odds ratio = 0.616
capital_run_length_longest: GD odds ratio = 10.111, SGD odds ratio = 9.049
```

```
capital_run_length_total: GD odds ratio = 1.240, SGD odds ratio = 1.255
```

```
features = list(gd_interpretable.keys())
# Extracting values for plotting
gd_values = [gd_interpretable[feature] for feature in features]
sgd_values = [sgd_interpretable[feature] for feature in features]
# Setting up the scatter plot
plt.figure(figsize=(10, 6))
# Scatter plot for GD values
plt.scatter(features, gd_values, color='blue', label='GD Interpretable', __

marker='o')
# Scatter plot for SGD values
plt.scatter(features, sgd_values, color='orange', label='SGD Interpretable', u
 # Adding labels and title
plt.xlabel('Features')
plt.ylabel('Interpretable Scores')
plt.title('Interpretable Scores from GD and SGD')
plt.xticks(rotation=45, ha='right')
plt.legend()
plt.grid(True)
# Show the plot
plt.tight_layout()
plt.show()
```



# 8 4 Maximum Aposteriori Estimation

## 8.1 4a Gradient Descent

```
[312]: def l_l2(y, X, w, lambda_):
           # YOUR CODE HERE
           """Log-density of posterior of logistic regression with weights w and L2
           regularization parameter lambda_.
           Parameters
           y: ndarray of shape (N,)
               Binary labels (either 0 or 1).
           X : ndarray \ of \ shape \ (N, D)
               Design matrix.
           w: ndarray of shape (D,)
               Weight vector.
           lambda_{-}: float
               L2 regularization parameter.
           Returns
           _____
           float
               Log-density of the posterior with L2 regularization.
```

```
return 1(y, X, w) - (lambda_ / 2) * (np.linalg.norm(w) ** 2)
[313]: # this should give:
      # [-47066.641667825766, -47312.623810682911]
       [1_12(y, Xz, np.linspace(-5, 5, D), 0), 1_12(y, Xz, np.linspace(-5, 5, D), 1)]
[313]: [np.float64(-47066.64166782577), np.float64(-47312.62381068291)]
[314]: def dl_l2(y, X, w, lambda_):
           # YOUR CODE HERE
           """Gradient of the log-density of the posterior of logistic regression with
          L2 regularization.
          Parameters
           y: ndarray of shape (N,)
              Binary labels (either 0 or 1).
          X: ndarray of shape (N, D)
              Design matrix.
          w: ndarray of shape (D,)
              Weight vector.
           lambda_{-}:float
              L2 regularization parameter.
          Returns
          ndarray of shape (D,)
              The gradient of the log-density of the posterior with L2 regularization.
          # Compute the gradient with the L2 regularization term
          return dl(y, X, w) - lambda_ * w
[315]: # this should give:
      # [array([ 551.33985842,
                                 143.84116318, 841.83373606, 156.87237578,
      #
                  802.61217579,
                                795.96202907,
                                                  920.69045803, 621.96516752,
      #
                  659.18724769,
                                470.81259805,
                                                 771.32406968, 352.40325626,
       #
                  455.66972482,
                                 234.36600888,
                                                 562.45454038, 864.83981264,
       #
                                                  902.6478154 , 544.00539886,
                  787.19723703,
                                649.48042176,
       #
                 1174.78638035,
                                 120.3598967 ,
                                                  839.61141672,
                                                                 633.30453444,
       #
                 -706.66815087,
                                -630.2039816 ,
                                                 -569.3451386 , -527.50996698,
       #
                 -359.53701083,
                                 -476.64334832,
                                                -411.60620464, -375.11950586,
       #
                 -345.37195689,
                                 -376.22044258, -407.31761977, -456.23251936,
       #
                 -596.86960184,
                                 -107.97072355,
                                                -394.82170044, -229.18125598,
       #
                 -288.46356547,
                                 -362.13402385,
                                                 -450.87896465, -277.03932676,
       #
                 -414.99293368,
                                 -452.28771693, -167.54649092, -270.9043748,
       #
                                 -357.72497343, -259.12468742,
                 -252.20140951,
                                                                 418.35938483,
                  604.54173228,
                                                 152.24258478, 378.16731033,
                                 43.10390907,
```

```
416.12032881]),
   array([
#
            556.33985842,
                             148.66259175,
                                             846.4765932 ,
                                                              161.33666149,
#
            806.89789007,
                             800.06917193,
                                             924.61902946,
                                                              625.71516752,
#
                                             774.5383554 ,
            662.75867626,
                            474.20545519,
                                                              355.43897054,
#
            458.52686767,
                             237.04458031,
                                             564.95454038,
                                                              867.16124121,
                                             904.43352968,
                                                              545.61254171,
#
            789.34009417,
                            651.44470748,
                                                              634.19739158,
#
                            121.6098967 ,
                                             840.68284529,
           1176.21495178,
#
           -705.95386516,
                           -629.66826731,
                                            -568.98799574,
                                                             -527.33139555,
           -359.53701083,
                                                             -375.65522015,
                            -476.82191975,
                                             -411.9633475 ,
           -346.08624261,
                            -377.11329972,
                                             -408.38904835,
                                                             -457.48251936,
#
           -598.29817327,
                            -109.57786641,
                                            -396.60741472,
                                                             -231.14554169,
                                                             -279.71789819,
           -290.60642261,
                            -364.45545242,
                                            -453.37896465,
#
           -417.85007654,
                            -455.32343122,
                                            -170.76077664,
                                                             -274.29723194,
#
           -255.77283808,
                            -361.47497343,
                                            -263.05325885,
                                                              414.25224198,
#
                              38.63962335,
                                                              373.34588176,
            600.25601799,
                                             147.59972763,
            411.12032881])]
[dl_12(y, Xz, np.linspace(-5, 5, D), 0), dl_12(y, Xz, np.linspace(-5, 5, D), 1)]
```

```
[315]: [array([ 551.33985842,
                              143.84116318,
                                             841.83373606,
                                                             156.87237578,
               802.61217579,
                              795.96202907,
                                             920.69045803,
                                                             621.96516752,
               659.18724769,
                              470.81259805,
                                             771.32406968,
                                                             352.40325626,
               455.66972482,
                              234.36600888, 562.45454038,
                                                            864.83981264,
                              649.48042176, 902.6478154,
                                                            544.00539886,
               787.19723703,
               1174.78638035,
                              120.3598967 , 839.61141672,
                                                             633.30453444,
               -706.66815087, -630.2039816 , -569.3451386 , -527.50996698,
               -359.53701083, -476.64334832, -411.60620464, -375.11950586,
               -345.37195689, -376.22044258, -407.31761977, -456.23251936,
               -596.86960184, -107.97072355, -394.82170044, -229.18125598,
               -288.46356547, -362.13402385, -450.87896465, -277.03932676,
               -414.99293368, -452.28771693, -167.54649092, -270.9043748 ,
               -252.20140951, -357.72497343, -259.12468742, 418.35938483,
                                43.10390907, 152.24258478, 378.16731033,
               604.54173228,
               416.12032881]),
       array([ 556.33985842, 148.66259175, 846.4765932,
                                                            161.33666149,
               806.89789007,
                              800.06917193,
                                             924.61902946,
                                                             625.71516752,
                              474.20545519, 774.5383554,
                                                            355.43897054,
               662.75867626,
               458.52686767,
                              237.04458031, 564.95454038, 867.16124121,
                              651.44470748, 904.43352968,
               789.34009417,
                                                             545.61254171,
               1176.21495178,
                              121.6098967 , 840.68284529,
                                                             634.19739158,
               -705.95386516, -629.66826731, -568.98799574, -527.33139555,
               -359.53701083, \ -476.82191975, \ -411.9633475 \ , \ -375.65522015,
               -346.08624261, -377.11329972, -408.38904835, -457.48251936,
               -598.29817327, -109.57786641, -396.60741472, -231.14554169,
               -290.60642261, -364.45545242, -453.37896465, -279.71789819,
               -417.85007654, -455.32343122, -170.76077664, -274.29723194,
               -255.77283808, -361.47497343, -263.05325885, 414.25224198,
               600.25601799,
                               38.63962335, 147.59972763,
                                                             373.34588176,
```

## 411.12032881])]

```
[316]: | # now define the (f,update) tuple for optimize for logistic regression, L2
       # regularization, and gradient descent
       def gd_12(y, X, lambda_):
           # YOUR CODE HERE
          def objective(w):
               """Objective function: Negative log-density of the posterior with L2_{\sqcup}
        \neg regularization."""
               return -1_12(y, X, w, lambda_)
          def update(w, eps):
               """Update function: Performs a gradient descent step with L2\Box
        \hookrightarrow regularization."""
               return w + eps * dl_l2(y, X, w, lambda_)
          return (objective, update)
[317]: # let's run!
       lambda = 100
       wz_gd_12, vz_gd_12, ez_gd_12 = optimize(gd_12(y, Xz, lambda_), w0, nepochs=500)
              0: f= 9992.358, eps=0.010000000
      Epoch
      Epoch
             1: f= 23977.384, eps=0.005000000
              2: f= 5534.851, eps=0.005250000
      Epoch
      Epoch 3: f= 1427.453, eps=0.005512500
      Epoch 4: f= 1131.716, eps=0.005788125
      Epoch 5: f= 1540.933, eps=0.002894063
      Epoch 6: f= 1323.168, eps=0.003038766
      Epoch 7: f= 1049.068, eps=0.003190704
      Epoch
             8: f= 1067.960, eps=0.001595352
      Epoch
             9: f=
                      989.861, eps=0.001675120
      Epoch 10: f=
                      988.742, eps=0.001758876
      Epoch 11: f=
                      988.585, eps=0.001846819
      Epoch 12: f=
                      988.539, eps=0.001939160
      Epoch 13: f=
                      988.522, eps=0.002036118
      Epoch 14: f=
                      988.516, eps=0.002137924
      Epoch 15: f=
                      988.513, eps=0.002244820
                      988.512, eps=0.002357061
      Epoch 16: f=
      Epoch 17: f=
                      988.512, eps=0.002474914
      Epoch 18: f=
                      988.512, eps=0.002598660
      Epoch 19: f=
                      988.512, eps=0.002728593
      Epoch 20: f=
                      988.512, eps=0.002865023
      Epoch 21: f=
                      988.512, eps=0.003008274
      Epoch 22: f=
                      988.512, eps=0.003158688
                      988.512, eps=0.003316622
      Epoch 23: f=
      Epoch 24: f=
                      988.512, eps=0.001658311
      Epoch 25: f=
                      988.512, eps=0.001741227
```

```
Epoch 26: f=
                988.512, eps=0.001828288
Epoch 27: f=
                988.512, eps=0.001919702
Epoch
                988.512, eps=0.002015687
      28: f=
      29: f=
                988.512, eps=0.002116472
Epoch
Epoch 30: f=
                988.512, eps=0.002222295
Epoch
                988.512, eps=0.002333410
      31: f=
Epoch
      32: f=
                988.512, eps=0.002450081
Epoch 33: f=
                988.512, eps=0.002572585
Epoch 34: f=
                988.512, eps=0.002701214
Epoch 35: f=
                988.512, eps=0.002836275
Epoch 36: f=
                988.512, eps=0.002978088
Epoch 37: f=
                988.512, eps=0.003126993
Epoch 38: f=
                988.512, eps=0.003283342
Epoch
      39: f=
                988.512, eps=0.003447510
Epoch 40: f=
                988.512, eps=0.003619885
Epoch 41: f=
                988.512, eps=0.001809943
Epoch 42: f=
                988.512, eps=0.001900440
                988.512, eps=0.001995462
Epoch 43: f=
Epoch 44: f=
                988.512, eps=0.002095235
Epoch 45: f=
                988.512, eps=0.002199996
Epoch
      46: f=
                988.512, eps=0.002309996
Epoch 47: f=
                988.512, eps=0.002425496
Epoch 48: f=
                988.512, eps=0.002546771
Epoch 49: f=
                988.512, eps=0.001273385
Epoch 50: f=
                988.512, eps=0.001337055
Epoch 51: f=
                988.512, eps=0.001403907
                988.512, eps=0.001474103
Epoch 52: f=
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      72: f=
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Epoch
     73: f=
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                988.512, eps=0.000000000
Epoch 455: f=
Epoch 456: f=
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Epoch 457: f=
                988.512, eps=0.000000000
```

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988.512, eps=0.000000000
Epoch 458: f=
Epoch 459: f=
                988.512, eps=0.000000000
Epoch 460: f=
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Epoch 461: f=
                988.512, eps=0.000000000
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                988.512, eps=0.000000000
Epoch 469: f=
Epoch 470: f=
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Epoch 471: f=
                988.512, eps=0.000000000
Epoch 472: f=
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Epoch 474: f=
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Epoch 476: f=
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Epoch 477: f=
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Epoch 478: f=
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Epoch 479: f=
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Epoch 480: f=
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Epoch 482: f=
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Epoch 484: f=
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Epoch 485: f=
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Epoch 486: f=
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Epoch 487: f=
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Epoch 488: f=
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Epoch 489: f=
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Epoch 492: f=
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Epoch 493: f=
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Epoch 494: f=
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Epoch 495: f=
                988.512, eps=0.000000000
Epoch 496: f=
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Epoch 497: f=
                988.512, eps=0.000000000
Epoch 498: f=
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Epoch 499: f=
                988.512, eps=0.000000000
Result after 500 epochs: f=988.511839602703
```

#### 8.2 4b Effect of Prior

```
[318]: # YOUR CODE HERE
       # Define a range of lambda values to explore the effect of L2 regularization \Box
        \hookrightarrowstrength
       lam_values = [0, 0.01, 0.1, 0.5, 1, 2, 3, 4, 5, 10, 20, 100, 200, 500]
       results = {} # Initialize a dictionary to store results for each lambda
       # Loop over each lambda value, performing gradient descent with L2_{\sqcup}
        \rightarrow regularization
       for lam in lam values:
           np.random.seed(0) # Set a seed for reproducibility in weight initialization
           w0 = np.random.normal(size=D) # Initialize weights randomly
           # Optimize logistic regression with L2 regularization for the current lambda
           wz, vz, ez = optimize(gd_12(y, Xz, lam), w0, nepochs=500)
           # Store final weights and objective value after training
           results[str(lam)] = {
               'final_weights': wz, # Final weight vector after optimization
               'final_nll_values': vz,
               'final_objective': ez[-1] # Final value of the objective function
           }
       # Print out the final objective values for each lambda to compare_
        ⇔regularization effects
       for lam, res in results.items():
           print(f"Lambda = {lam}: Final Objective = {res['final_objective']:.4f}")
      Epoch
              0: f= 6636.208, eps=0.010000000
```

```
Epoch 1: f= 4216.957, eps=0.010500000
Epoch 2: f= 2657.519, eps=0.011025000
Epoch 3: f= 1926.135, eps=0.011576250
Epoch 4: f= 1449.495, eps=0.012155063
Epoch 5: f= 1207.529, eps=0.012762816
Epoch 6: f= 1052.489, eps=0.013400956
Epoch 7: f= 957.275, eps=0.014071004
Epoch 8: f= 899.610, eps=0.014774554
Epoch 9: f=
               882.904, eps=0.015513282
Epoch 10: f= 1017.083, eps=0.007756641
Epoch 11: f=
               840.760, eps=0.008144473
Epoch 12: f=
               805.649, eps=0.008551697
Epoch 13: f=
               822.108, eps=0.004275848
Epoch 14: f=
               746.377, eps=0.004489641
Epoch 15: f=
               735.803, eps=0.004714123
Epoch 16: f=
               729.780, eps=0.004949829
               724.467, eps=0.005197320
Epoch 17: f=
Epoch 18: f=
               719.408, eps=0.005457186
```

```
Epoch 19: f=
                714.564, eps=0.005730046
Epoch 20: f=
                709.932, eps=0.006016548
Epoch 21: f=
                705.514, eps=0.006317375
      22: f=
                701.321, eps=0.006633244
Epoch
Epoch 23: f=
                697.373, eps=0.006964906
Epoch
      24: f=
                693.728, eps=0.007313152
Epoch 25: f=
                690.591, eps=0.007678809
Epoch 26: f=
                688.614, eps=0.008062750
Epoch 27: f=
                688.607, eps=0.008465887
Epoch 28: f=
                690.854, eps=0.004232944
Epoch 29: f=
                679.967, eps=0.004444591
Epoch 30: f=
                678.649, eps=0.004666820
Epoch
                677.447, eps=0.004900161
      31: f=
Epoch 32: f=
                676.292, eps=0.005145169
Epoch 33: f=
                675.182, eps=0.005402428
Epoch 34: f=
                674.120, eps=0.005672549
Epoch 35: f=
                673.114, eps=0.005956177
                672.177, eps=0.006253986
Epoch 36: f=
Epoch 37: f=
                671.334, eps=0.006566685
Epoch 38: f=
                670.656, eps=0.006895019
Epoch
      39: f=
                670.397, eps=0.007239770
Epoch 40: f=
                671.342, eps=0.003619885
Epoch 41: f=
                668.932, eps=0.003800879
Epoch 42: f=
                668.378, eps=0.003990923
Epoch 43: f=
                668.027, eps=0.004190469
Epoch 44: f=
                667.720, eps=0.004399993
Epoch 45: f=
                667.433, eps=0.004619993
Epoch 46: f=
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                666.897, eps=0.005093542
Epoch 47: f=
Epoch 48: f=
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Epoch 49: f=
                666.417, eps=0.005615630
Epoch 50: f=
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Epoch 51: f=
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Epoch 52: f=
                665.858, eps=0.006500794
Epoch 53: f=
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Epoch 54: f=
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Epoch 55: f=
                665.424, eps=0.003583562
Epoch 56: f=
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Epoch 57: f=
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Epoch 58: f=
                665.128, eps=0.004148421
Epoch 59: f=
                665.054, eps=0.004355843
Epoch 60: f=
                664.982, eps=0.004573635
Epoch
      61: f=
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Epoch 62: f=
                664.842, eps=0.005042432
Epoch 63: f=
                664.773, eps=0.005294554
      64: f=
Epoch
                664.707, eps=0.005559282
Epoch
      65: f=
                664.641, eps=0.005837246
Epoch 66: f=
                664.578, eps=0.006129108
```

```
Epoch 67: f=
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Epoch 68: f=
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Epoch
      69: f=
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Epoch
      70: f=
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Epoch
      71: f=
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                664.278, eps=0.003911234
Epoch
      72: f=
Epoch 73: f=
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Epoch 74: f=
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Epoch 75: f=
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Epoch 76: f=
                664.139, eps=0.004754129
Epoch 77: f=
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Epoch 78: f=
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                664.037, eps=0.005503499
Epoch 79: f=
Epoch
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Epoch
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Epoch 96: f=
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Epoch 103: f=
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Epoch 104: f=
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```

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Epoch 122: f=
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```

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Epoch 165: f=
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```

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Epoch 232: f=
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Epoch 242: f=
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Epoch 243: f=
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Epoch 246: f=
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Epoch 247: f=
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Epoch 248: f=
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Epoch 249: f=
                660.009, eps=0.006286479
Epoch 250: f=
                659.985, eps=0.006600803
Epoch 251: f=
                659.961, eps=0.006930843
Epoch 252: f=
                659.935, eps=0.007277385
Epoch 253: f=
                659.908, eps=0.007641254
Epoch 254: f=
                659.880, eps=0.008023317
Epoch 255: f=
                659.850, eps=0.008424483
Epoch 256: f=
                659.819, eps=0.008845707
Epoch 257: f=
                659.787, eps=0.009287992
Epoch 258: f=
                659.754, eps=0.009752392
```

```
Epoch 259: f=
                659.737, eps=0.010240012
Epoch 260: f=
                659.888, eps=0.005120006
Epoch 261: f=
                659.906, eps=0.002560003
Epoch 262: f=
                659.651, eps=0.002688003
Epoch 263: f=
                659.641, eps=0.002822403
Epoch 264: f=
                659.631, eps=0.002963523
Epoch 265: f=
                659.620, eps=0.003111700
Epoch 266: f=
                659.609, eps=0.003267285
Epoch 267: f=
                659.597, eps=0.003430649
Epoch 268: f=
                659.585, eps=0.003602181
Epoch 269: f=
                659.572, eps=0.003782290
Epoch 270: f=
                659.558, eps=0.003971405
Epoch 271: f=
                659.543, eps=0.004169975
Epoch 272: f=
                659.528, eps=0.004378474
                659.513, eps=0.004597397
Epoch 273: f=
Epoch 274: f=
                659.496, eps=0.004827267
Epoch 275: f=
                659.479, eps=0.005068631
Epoch 276: f=
                659.460, eps=0.005322062
Epoch 277: f=
                659.441, eps=0.005588165
Epoch 278: f=
                659.421, eps=0.005867574
Epoch 279: f=
                659.400, eps=0.006160952
Epoch 280: f=
                659.378, eps=0.006469000
Epoch 281: f=
                659.355, eps=0.006792450
Epoch 282: f=
                659.331, eps=0.007132072
Epoch 283: f=
                659.305, eps=0.007488676
Epoch 284: f=
                659.279, eps=0.007863110
Epoch 285: f=
                659.251, eps=0.008256265
Epoch 286: f=
                659.222, eps=0.008669078
Epoch 287: f=
                659.191, eps=0.009102532
Epoch 288: f=
                659.159, eps=0.009557659
Epoch 289: f=
                659.125, eps=0.010035542
Epoch 290: f=
                659.090, eps=0.010537319
Epoch 291: f=
                659.053, eps=0.011064185
Epoch 292: f=
                659.016, eps=0.011617394
Epoch 293: f=
                658.992, eps=0.012198264
Epoch 294: f=
                659.226, eps=0.006099132
Epoch 295: f=
                659.526, eps=0.003049566
Epoch 296: f=
                658.916, eps=0.003202044
Epoch 297: f=
                658.891, eps=0.003362147
Epoch 298: f=
                658.878, eps=0.003530254
Epoch 299: f=
                658.865, eps=0.003706767
Epoch 300: f=
                658.852, eps=0.003892105
Epoch 301: f=
                658.839, eps=0.004086710
Epoch 302: f=
                658.825, eps=0.004291046
Epoch 303: f=
                658.810, eps=0.004505598
Epoch 304: f=
                658.795, eps=0.004730878
Epoch 305: f=
                658.778, eps=0.004967422
Epoch 306: f=
                658.761, eps=0.005215793
```

```
Epoch 307: f=
                658.743, eps=0.005476582
Epoch 308: f=
                658.725, eps=0.005750412
Epoch 309: f=
                658.705, eps=0.006037932
Epoch 310: f=
                658.684, eps=0.006339829
Epoch 311: f=
                658.663, eps=0.006656820
Epoch 312: f=
                658.640, eps=0.006989661
Epoch 313: f=
                658.617, eps=0.007339144
Epoch 314: f=
                658.593, eps=0.007706101
Epoch 315: f=
                658.573, eps=0.008091406
Epoch 316: f=
                658.582, eps=0.004045703
Epoch 317: f=
                658.544, eps=0.004247988
Epoch 318: f=
                658.521, eps=0.004460388
Epoch 319: f=
                658.503, eps=0.004683407
Epoch 320: f=
                658.486, eps=0.004917578
Epoch 321: f=
                658.470, eps=0.005163456
Epoch 322: f=
                658.455, eps=0.005421629
Epoch 323: f=
                658.443, eps=0.005692711
Epoch 324: f=
                658.436, eps=0.005977346
Epoch 325: f=
                658.450, eps=0.002988673
Epoch 326: f=
                658.381, eps=0.003138107
Epoch 327: f=
                658.368, eps=0.003295012
Epoch 328: f=
                658.356, eps=0.003459763
Epoch 329: f=
                658.345, eps=0.003632751
Epoch 330: f=
                658.333, eps=0.003814388
Epoch 331: f=
                658.320, eps=0.004005108
Epoch 332: f=
                658.307, eps=0.004205363
Epoch 333: f=
                658.293, eps=0.004415631
Epoch 334: f=
                658.278, eps=0.004636413
Epoch 335: f=
                658.263, eps=0.004868234
Epoch 336: f=
                658.247, eps=0.005111645
Epoch 337: f=
                658.230, eps=0.005367228
Epoch 338: f=
                658.212, eps=0.005635589
Epoch 339: f=
                658.193, eps=0.005917368
Epoch 340: f=
                658.174, eps=0.006213237
Epoch 341: f=
                658.153, eps=0.006523899
Epoch 342: f=
                658.132, eps=0.006850094
Epoch 343: f=
                658.109, eps=0.007192598
Epoch 344: f=
                658.086, eps=0.007552228
Epoch 345: f=
                658.061, eps=0.007929840
Epoch 346: f=
                658.036, eps=0.008326332
Epoch 347: f=
                658.017, eps=0.008742648
Epoch 348: f=
                658.040, eps=0.004371324
Epoch 349: f=
                658.004, eps=0.004589890
Epoch 350: f=
                657.981, eps=0.004819385
Epoch 351: f=
                657.965, eps=0.005060354
Epoch 352: f=
                657.954, eps=0.005313372
Epoch 353: f=
                657.953, eps=0.005579040
Epoch 354: f=
                657.969, eps=0.002789520
```

```
Epoch 355: f=
                657.876, eps=0.002928996
Epoch 356: f=
                657.864, eps=0.003075446
Epoch 357: f=
                657.854, eps=0.003229218
Epoch 358: f=
                657.844, eps=0.003390679
Epoch 359: f=
                657.833, eps=0.003560213
Epoch 360: f=
                657.821, eps=0.003738224
Epoch 361: f=
                657.809, eps=0.003925135
Epoch 362: f=
                657.797, eps=0.004121392
Epoch 363: f=
                657.783, eps=0.004327461
Epoch 364: f=
                657.770, eps=0.004543834
                657.755, eps=0.004771026
Epoch 365: f=
Epoch 366: f=
                657.740, eps=0.005009577
Epoch 367: f=
                657.724, eps=0.005260056
Epoch 368: f=
                657.707, eps=0.005523059
Epoch 369: f=
                657.689, eps=0.005799212
Epoch 370: f=
                657.671, eps=0.006089173
Epoch 371: f=
                657.651, eps=0.006393631
Epoch 372: f=
                657.631, eps=0.006713313
Epoch 373: f=
                657.609, eps=0.007048978
Epoch 374: f=
                657.587, eps=0.007401427
Epoch 375: f=
                657.564, eps=0.007771499
Epoch 376: f=
                657.539, eps=0.008160074
Epoch 377: f=
                657.513, eps=0.008568077
Epoch 378: f=
                657.486, eps=0.008996481
Epoch 379: f=
                657.460, eps=0.009446305
Epoch 380: f=
                657.445, eps=0.009918621
Epoch 381: f=
                657.554, eps=0.004959310
Epoch 382: f=
                657.540, eps=0.005207276
Epoch 383: f=
                657.567, eps=0.002603638
Epoch 384: f=
                657.357, eps=0.002733820
Epoch 385: f=
                657.348, eps=0.002870511
Epoch 386: f=
                657.339, eps=0.003014036
Epoch 387: f=
                657.330, eps=0.003164738
Epoch 388: f=
                657.320, eps=0.003322975
Epoch 389: f=
                657.310, eps=0.003489124
Epoch 390: f=
                657.299, eps=0.003663580
Epoch 391: f=
                657.287, eps=0.003846759
Epoch 392: f=
                657.275, eps=0.004039097
Epoch 393: f=
                657.263, eps=0.004241052
Epoch 394: f=
                657.250, eps=0.004453104
Epoch 395: f=
                657.236, eps=0.004675760
Epoch 396: f=
                657.221, eps=0.004909548
                657.206, eps=0.005155025
Epoch 397: f=
Epoch 398: f=
                657.190, eps=0.005412776
Epoch 399: f=
                657.173, eps=0.005683415
Epoch 400: f=
                657.156, eps=0.005967586
Epoch 401: f=
                657.138, eps=0.006265965
Epoch 402: f=
                657.118, eps=0.006579263
```

```
Epoch 403: f=
                657.098, eps=0.006908226
Epoch 404: f=
                657.077, eps=0.007253638
Epoch 405: f=
                657.054, eps=0.007616320
Epoch 406: f=
                657.031, eps=0.007997136
Epoch 407: f=
                657.007, eps=0.008396992
Epoch 408: f=
                656.981, eps=0.008816842
Epoch 409: f=
                656.954, eps=0.009257684
Epoch 410: f=
                656.926, eps=0.009720568
Epoch 411: f=
                656.896, eps=0.010206597
Epoch 412: f=
                656.866, eps=0.010716927
Epoch 413: f=
                656.838, eps=0.011252773
Epoch 414: f=
                656.871, eps=0.005626387
Epoch 415: f=
                656.908, eps=0.002813193
Epoch 416: f=
                656.776, eps=0.002953853
Epoch 417: f=
                656.765, eps=0.003101546
Epoch 418: f=
                656.755, eps=0.003256623
Epoch 419: f=
                656.745, eps=0.003419454
Epoch 420: f=
                656.735, eps=0.003590427
Epoch 421: f=
                656.724, eps=0.003769948
Epoch 422: f=
                656.713, eps=0.003958445
Epoch 423: f=
                656.701, eps=0.004156368
Epoch 424: f=
                656.689, eps=0.004364186
Epoch 425: f=
                656.676, eps=0.004582395
Epoch 426: f=
                656.662, eps=0.004811515
Epoch 427: f=
                656.648, eps=0.005052091
                656.632, eps=0.005304695
Epoch 428: f=
                656.617, eps=0.005569930
Epoch 429: f=
Epoch 430: f=
                656.600, eps=0.005848427
Epoch 431: f=
                656.583, eps=0.006140848
Epoch 432: f=
                656.564, eps=0.006447890
Epoch 433: f=
                656.545, eps=0.006770285
Epoch 434: f=
                656.525, eps=0.007108799
Epoch 435: f=
                656.504, eps=0.007464239
Epoch 436: f=
                656.482, eps=0.007837451
Epoch 437: f=
                656.459, eps=0.008229324
Epoch 438: f=
                656.435, eps=0.008640790
Epoch 439: f=
                656.410, eps=0.009072829
Epoch 440: f=
                656.388, eps=0.009526471
Epoch 441: f=
                656.406, eps=0.004763235
Epoch 442: f=
                656.387, eps=0.005001397
Epoch 443: f=
                656.379, eps=0.005251467
Epoch 444: f=
                656.381, eps=0.002625734
Epoch 445: f=
                656.303, eps=0.002757020
Epoch 446: f=
                656.295, eps=0.002894871
Epoch 447: f=
                656.286, eps=0.003039615
Epoch 448: f=
                656.277, eps=0.003191596
Epoch 449: f=
                656.268, eps=0.003351175
Epoch 450: f=
                656.258, eps=0.003518734
```

```
Epoch 451: f=
                656.248, eps=0.003694671
Epoch 452: f=
                656.237, eps=0.003879404
Epoch 453: f=
                656.226, eps=0.004073375
Epoch 454: f=
                656.214, eps=0.004277043
Epoch 455: f=
                656.202, eps=0.004490895
Epoch 456: f=
                656.189, eps=0.004715440
Epoch 457: f=
                656.175, eps=0.004951212
Epoch 458: f=
                656.161, eps=0.005198773
Epoch 459: f=
                656.145, eps=0.005458711
Epoch 460: f=
                656.130, eps=0.005731647
Epoch 461: f=
                656.113, eps=0.006018229
Epoch 462: f=
                656.096, eps=0.006319141
                656.077, eps=0.006635098
Epoch 463: f=
Epoch 464: f=
                656.058, eps=0.006966853
Epoch 465: f=
                656.038, eps=0.007315195
Epoch 466: f=
                656.017, eps=0.007680955
Epoch 467: f=
                655.995, eps=0.008065003
Epoch 468: f=
                655.972, eps=0.008468253
Epoch 469: f=
                655.948, eps=0.008891666
Epoch 470: f=
                655.923, eps=0.009336249
Epoch 471: f=
                655.896, eps=0.009803061
Epoch 472: f=
                655.868, eps=0.010293215
Epoch 473: f=
                655.841, eps=0.010807875
Epoch 474: f=
                655.835, eps=0.011348269
Epoch 475: f=
                656.135, eps=0.005674135
Epoch 476: f=
                656.301, eps=0.002837067
Epoch 477: f=
                655.760, eps=0.002978921
Epoch 478: f=
                655.744, eps=0.003127867
Epoch 479: f=
                655.735, eps=0.003284260
Epoch 480: f=
                655.725, eps=0.003448473
Epoch 481: f=
                655.716, eps=0.003620897
Epoch 482: f=
                655.705, eps=0.003801941
Epoch 483: f=
                655.695, eps=0.003992039
Epoch 484: f=
                655.684, eps=0.004191640
Epoch 485: f=
                655.672, eps=0.004401222
Epoch 486: f=
                655.659, eps=0.004621284
Epoch 487: f=
                655.646, eps=0.004852348
Epoch 488: f=
                655.633, eps=0.005094965
Epoch 489: f=
                655.619, eps=0.005349713
Epoch 490: f=
                655.604, eps=0.005617199
Epoch 491: f=
                655.588, eps=0.005898059
Epoch 492: f=
                655.571, eps=0.006192962
Epoch 493: f=
                655.554, eps=0.006502610
Epoch 494: f=
                655.536, eps=0.006827741
Epoch 495: f=
                655.517, eps=0.007169128
Epoch 496: f=
                655.497, eps=0.007527584
Epoch 497: f=
                655.476, eps=0.007903963
Epoch 498: f=
                655.454, eps=0.008299161
```

```
655.432, eps=0.008714119
Epoch 499: f=
Result after 500 epochs: f=655.413496469947
               6636.544, eps=0.010000000
Epoch
        0: f=
               4218.624, eps=0.010500000
Epoch
        1: f=
Epoch
        2: f=
               2658.502, eps=0.011025000
               1926.666, eps=0.011576250
Epoch
        3: f=
Epoch
        4: f=
               1449.805, eps=0.012155063
Epoch
        5: f=
               1207.714, eps=0.012762816
Epoch
        6: f=
               1052.586, eps=0.013400956
Epoch
        7: f=
                957.321, eps=0.014071004
        8: f=
                899.611, eps=0.014774554
Epoch
Epoch
        9: f=
                882.634, eps=0.015513282
               1015.190, eps=0.007756641
Epoch
       10: f=
Epoch
       11: f=
                841.020, eps=0.008144473
Epoch
      12: f=
                806.237, eps=0.008551697
Epoch
      13: f=
                823.099, eps=0.004275848
Epoch
      14: f=
                746.486, eps=0.004489641
Epoch
      15: f=
                735.810, eps=0.004714123
Epoch
      16: f=
                729.776, eps=0.004949829
Epoch
                724.465, eps=0.005197320
       17: f=
Epoch
       18: f=
                719.410, eps=0.005457186
Epoch
      19: f=
                714.572, eps=0.005730046
Epoch
      20: f=
                709.945, eps=0.006016548
Epoch 21: f=
                705.535, eps=0.006317375
      22: f=
                701.350, eps=0.006633244
Epoch
Epoch 23: f=
                697.412, eps=0.006964906
                693.781, eps=0.007313152
Epoch
      24: f=
Epoch 25: f=
                690.670, eps=0.007678809
Epoch
      26: f=
                688.746, eps=0.008062750
Epoch 27: f=
                688.785, eps=0.004031375
                682.821, eps=0.004232944
Epoch 28: f=
Epoch
      29: f=
                681.344, eps=0.004444591
Epoch 30: f=
                680.005, eps=0.004666820
                678.724, eps=0.004900161
Epoch
      31: f=
Epoch
      32: f=
                677.494, eps=0.005145169
Epoch
      33: f=
                676.315, eps=0.005402428
Epoch
      34: f=
                675.202, eps=0.005672549
Epoch
                674.176, eps=0.005956177
      35: f=
Epoch
      36: f=
                673.301, eps=0.006253986
Epoch 37: f=
                672.684, eps=0.006566685
Epoch 38: f=
                672.603, eps=0.006895019
Epoch
      39: f=
                673.096, eps=0.003447510
Epoch
      40: f=
                669.981, eps=0.003619885
      41: f=
Epoch
                669.557, eps=0.003800879
Epoch
      42: f=
                669.189, eps=0.003990923
Epoch
      43: f=
                668.837, eps=0.004190469
Epoch
      44: f=
                668.497, eps=0.004399993
                668.168, eps=0.004619993
Epoch
      45: f=
```

```
Epoch 46: f=
                667.852, eps=0.004850992
Epoch 47: f=
                667.549, eps=0.005093542
                667.260, eps=0.005348219
Epoch 48: f=
                666.986, eps=0.005615630
Epoch
      49: f=
Epoch 50: f=
                666.728, eps=0.005896411
                666.487, eps=0.006191232
Epoch 51: f=
Epoch 52: f=
                666.267, eps=0.006500794
Epoch 53: f=
                666.074, eps=0.006825833
Epoch 54: f=
                665.940, eps=0.007167125
Epoch 55: f=
                665.996, eps=0.003583562
Epoch 56: f=
                665.656, eps=0.003762741
Epoch 57: f=
                665.532, eps=0.003950878
Epoch 58: f=
                665.443, eps=0.004148421
Epoch
      59: f=
                665.362, eps=0.004355843
Epoch 60: f=
                665.286, eps=0.004573635
Epoch 61: f=
                665.211, eps=0.004802316
Epoch 62: f=
                665.139, eps=0.005042432
Epoch 63: f=
                665.068, eps=0.005294554
Epoch 64: f=
                665.000, eps=0.005559282
Epoch
                664.934, eps=0.005837246
      65: f=
Epoch
      66: f=
                664.873, eps=0.006129108
Epoch 67: f=
                664.823, eps=0.006435563
Epoch 68: f=
                664.805, eps=0.006757341
Epoch 69: f=
                664.895, eps=0.003378671
Epoch 70: f=
                664.671, eps=0.003547604
Epoch 71: f=
                664.615, eps=0.003724984
Epoch 72: f=
                664.579, eps=0.003911234
Epoch 73: f=
                664.546, eps=0.004106795
Epoch 74: f=
                664.513, eps=0.004312135
Epoch 75: f=
                664.480, eps=0.004527742
                664.446, eps=0.004754129
Epoch 76: f=
Epoch 77: f=
                664.412, eps=0.004991835
Epoch 78: f=
                664.377, eps=0.005241427
                664.341, eps=0.005503499
Epoch 79: f=
Epoch 80: f=
                664.305, eps=0.005778674
Epoch 81: f=
                664.268, eps=0.006067607
Epoch 82: f=
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Epoch 83: f=
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Epoch 424: f=
Epoch 425: f=
                657.314, eps=0.009623030
Epoch 426: f=
                657.407, eps=0.004811515
Epoch 427: f=
                657.380, eps=0.005052091
Epoch 428: f=
                657.385, eps=0.002526045
Epoch 429: f=
                657.238, eps=0.002652348
```

```
Epoch 430: f=
                657.231, eps=0.002784965
Epoch 431: f=
                657.223, eps=0.002924213
Epoch 432: f=
                657.215, eps=0.003070424
Epoch 433: f=
                657.206, eps=0.003223945
Epoch 434: f=
                657.197, eps=0.003385142
Epoch 435: f=
                657.188, eps=0.003554400
Epoch 436: f=
                657.178, eps=0.003732120
Epoch 437: f=
                657.168, eps=0.003918726
Epoch 438: f=
                657.157, eps=0.004114662
Epoch 439: f=
                657.146, eps=0.004320395
Epoch 440: f=
                657.134, eps=0.004536415
Epoch 441: f=
                657.121, eps=0.004763235
Epoch 442: f=
                657.108, eps=0.005001397
Epoch 443: f=
                657.094, eps=0.005251467
Epoch 444: f=
                657.080, eps=0.005514040
Epoch 445: f=
                657.065, eps=0.005789742
Epoch 446: f=
                657.049, eps=0.006079230
Epoch 447: f=
                657.032, eps=0.006383191
Epoch 448: f=
                657.015, eps=0.006702351
Epoch 449: f=
                656.997, eps=0.007037468
Epoch 450: f=
                656.978, eps=0.007389342
Epoch 451: f=
                656.958, eps=0.007758809
Epoch 452: f=
                656.936, eps=0.008146749
Epoch 453: f=
                656.914, eps=0.008554086
Epoch 454: f=
                656.891, eps=0.008981791
Epoch 455: f=
                656.867, eps=0.009430880
Epoch 456: f=
                656.842, eps=0.009902424
Epoch 457: f=
                656.815, eps=0.010397546
Epoch 458: f=
                656.787, eps=0.010917423
Epoch 459: f=
                656.758, eps=0.011463294
Epoch 460: f=
                656.729, eps=0.012036459
Epoch 461: f=
                656.721, eps=0.012638282
Epoch 462: f=
                657.104, eps=0.006319141
Epoch 463: f=
                657.572, eps=0.003159570
Epoch 464: f=
                656.679, eps=0.003317549
Epoch 465: f=
                656.633, eps=0.003483426
Epoch 466: f=
                656.619, eps=0.003657598
Epoch 467: f=
                656.609, eps=0.003840478
Epoch 468: f=
                656.599, eps=0.004032501
Epoch 469: f=
                656.588, eps=0.004234127
Epoch 470: f=
                656.577, eps=0.004445833
Epoch 471: f=
                656.565, eps=0.004668125
Epoch 472: f=
                656.553, eps=0.004901531
Epoch 473: f=
                656.540, eps=0.005146607
Epoch 474: f=
                656.526, eps=0.005403938
Epoch 475: f=
                656.512, eps=0.005674135
Epoch 476: f=
                656.497, eps=0.005957841
Epoch 477: f=
                656.482, eps=0.006255733
```

```
Epoch 478: f=
                656.466, eps=0.006568520
Epoch 479: f=
                656.449, eps=0.006896946
Epoch 480: f=
                656.434, eps=0.007241793
Epoch 481: f=
                656.425, eps=0.007603883
Epoch 482: f=
                656.457, eps=0.003801941
Epoch 483: f=
                656.402, eps=0.003992039
Epoch 484: f=
                656.380, eps=0.004191640
Epoch 485: f=
                656.365, eps=0.004401222
Epoch 486: f=
                656.352, eps=0.004621284
Epoch 487: f=
                656.340, eps=0.004852348
                656.327, eps=0.005094965
Epoch 488: f=
Epoch 489: f=
                656.314, eps=0.005349713
Epoch 490: f=
                656.302, eps=0.005617199
Epoch 491: f=
                656.292, eps=0.005898059
                656.286, eps=0.006192962
Epoch 492: f=
Epoch 493: f=
                656.296, eps=0.003096481
Epoch 494: f=
                656.247, eps=0.003251305
Epoch 495: f=
                656.236, eps=0.003413870
Epoch 496: f=
                656.227, eps=0.003584564
Epoch 497: f=
                656.217, eps=0.003763792
Epoch 498: f=
                656.208, eps=0.003951982
Epoch 499: f=
                656.198, eps=0.004149581
Result after 500 epochs: f=656.1869767255795
Epoch
        0: f=
               6639.565, eps=0.010000000
Epoch
        1: f=
               4233.632, eps=0.010500000
        2: f=
               2667.324, eps=0.011025000
Epoch
        3: f=
               1931.401, eps=0.011576250
Epoch
Epoch
        4: f=
               1452.545, eps=0.012155063
Epoch
        5: f=
               1209.329, eps=0.012762816
        6: f=
               1053.408, eps=0.013400956
Epoch
Epoch
        7: f=
                957.678, eps=0.014071004
        8: f=
                899.563, eps=0.014774554
Epoch
Epoch
        9: f=
                880.065, eps=0.015513282
Epoch
       10: f=
                996.169, eps=0.007756641
       11: f=
                843.339, eps=0.008144473
Epoch
Epoch
       12: f=
                811.849, eps=0.008551697
Epoch
       13: f=
                832.190, eps=0.004275848
Epoch
                747.520, eps=0.004489641
       14: f=
Epoch
       15: f=
                735.848, eps=0.004714123
                729.721, eps=0.004949829
Epoch 16: f=
Epoch
      17: f=
                724.428, eps=0.005197320
Epoch
       18: f=
                719.411, eps=0.005457186
Epoch
       19: f=
                714.622, eps=0.005730046
Epoch
      20: f=
                710.053, eps=0.006016548
Epoch
      21: f=
                705.708, eps=0.006317375
Epoch
       22: f=
                701.601, eps=0.006633244
Epoch
      23: f=
                697.759, eps=0.006964906
                694.274, eps=0.007313152
Epoch 24: f=
```

```
Epoch 25: f=
                691.447, eps=0.007678809
Epoch 26: f=
                690.066, eps=0.008062750
Epoch 27: f=
                690.431, eps=0.004031375
Epoch
      28: f=
                683.569, eps=0.004232944
Epoch 29: f=
                682.144, eps=0.004444591
Epoch
      30: f=
                680.859, eps=0.004666820
Epoch
      31: f=
                679.635, eps=0.004900161
Epoch 32: f=
                678.463, eps=0.005145169
Epoch 33: f=
                677.345, eps=0.005402428
Epoch 34: f=
                676.294, eps=0.005672549
Epoch 35: f=
                675.333, eps=0.005956177
Epoch 36: f=
                674.523, eps=0.006253986
Epoch
      37: f=
                673.975, eps=0.006566685
Epoch 38: f=
                673.974, eps=0.006895019
Epoch 39: f=
                674.571, eps=0.003447510
Epoch 40: f=
                671.438, eps=0.003619885
Epoch 41: f=
                671.042, eps=0.003800879
Epoch 42: f=
                670.706, eps=0.003990923
Epoch 43: f=
                670.387, eps=0.004190469
Epoch 44: f=
                670.080, eps=0.004399993
Epoch
      45: f=
                669.785, eps=0.004619993
Epoch 46: f=
                669.503, eps=0.004850992
Epoch 47: f=
                669.234, eps=0.005093542
Epoch 48: f=
                668.978, eps=0.005348219
                668.738, eps=0.005615630
Epoch 49: f=
Epoch 50: f=
                668.513, eps=0.005896411
Epoch 51: f=
                668.305, eps=0.006191232
Epoch 52: f=
                668.116, eps=0.006500794
Epoch 53: f=
                667.955, eps=0.006825833
Epoch 54: f=
                667.858, eps=0.007167125
Epoch 55: f=
                667.970, eps=0.003583562
Epoch 56: f=
                667.610, eps=0.003762741
Epoch 57: f=
                667.493, eps=0.003950878
Epoch 58: f=
                667.415, eps=0.004148421
Epoch
      59: f=
                667.347, eps=0.004355843
Epoch
      60: f=
                667.283, eps=0.004573635
Epoch 61: f=
                667.221, eps=0.004802316
Epoch 62: f=
                667.161, eps=0.005042432
Epoch 63: f=
                667.103, eps=0.005294554
Epoch 64: f=
                667.047, eps=0.005559282
Epoch 65: f=
                666.994, eps=0.005837246
Epoch
      66: f=
                666.946, eps=0.006129108
      67: f=
                666.911, eps=0.006435563
Epoch
Epoch 68: f=
                666.914, eps=0.003217782
Epoch
      69: f=
                666.812, eps=0.003378671
Epoch
      70: f=
                666.780, eps=0.003547604
Epoch
      71: f=
                666.753, eps=0.003724984
Epoch 72: f=
                666.728, eps=0.003911234
```

```
Epoch 73: f=
                666.701, eps=0.004106795
Epoch 74: f=
                666.675, eps=0.004312135
                666.648, eps=0.004527742
Epoch 75: f=
                666.621, eps=0.004754129
Epoch
      76: f=
Epoch
      77: f=
                666.593, eps=0.004991835
Epoch 78: f=
                666.565, eps=0.005241427
Epoch 79: f=
                666.536, eps=0.005503499
Epoch 80: f=
                666.507, eps=0.005778674
Epoch 81: f=
                666.477, eps=0.006067607
Epoch 82: f=
                666.447, eps=0.006370988
                666.416, eps=0.006689537
Epoch 83: f=
Epoch 84: f=
                666.385, eps=0.007024014
                666.355, eps=0.007375214
Epoch 85: f=
Epoch
      86: f=
                666.333, eps=0.007743975
Epoch 87: f=
                666.352, eps=0.003871988
Epoch 88: f=
                666.293, eps=0.004065587
Epoch 89: f=
                666.263, eps=0.004268866
Epoch 90: f=
                666.240, eps=0.004482310
Epoch 91: f=
                666.220, eps=0.004706425
Epoch 92: f=
                666.200, eps=0.004941746
Epoch
      93: f=
                666.180, eps=0.005188834
Epoch 94: f=
                666.161, eps=0.005448275
Epoch 95: f=
                666.143, eps=0.005720689
Epoch 96: f=
                666.131, eps=0.006006724
                666.132, eps=0.003003362
Epoch 97: f=
Epoch 98: f=
                666.078, eps=0.003153530
Epoch 99: f=
                666.063, eps=0.003311206
Epoch 100: f=
                666.050, eps=0.003476767
Epoch 101: f=
                666.037, eps=0.003650605
Epoch 102: f=
                666.023, eps=0.003833135
Epoch 103: f=
                666.009, eps=0.004024792
Epoch 104: f=
                665.993, eps=0.004226032
Epoch 105: f=
                665.978, eps=0.004437333
Epoch 106: f=
                665.961, eps=0.004659200
Epoch 107: f=
                665.944, eps=0.004892160
Epoch 108: f=
                665.926, eps=0.005136768
Epoch 109: f=
                665.907, eps=0.005393606
Epoch 110: f=
                665.888, eps=0.005663287
Epoch 111: f=
                665.868, eps=0.005946451
Epoch 112: f=
                665.846, eps=0.006243773
Epoch 113: f=
                665.824, eps=0.006555962
Epoch 114: f=
                665.801, eps=0.006883760
                665.777, eps=0.007227948
Epoch 115: f=
Epoch 116: f=
                665.752, eps=0.007589346
Epoch 117: f=
                665.726, eps=0.007968813
Epoch 118: f=
                665.701, eps=0.008367254
Epoch 119: f=
                665.686, eps=0.008785616
Epoch 120: f=
                665.751, eps=0.004392808
```

```
Epoch 121: f=
                665.694, eps=0.004612449
Epoch 122: f=
                665.667, eps=0.004843071
Epoch 123: f=
                665.650, eps=0.005085225
                665.646, eps=0.005339486
Epoch 124: f=
Epoch 125: f=
                665.657, eps=0.002669743
Epoch 126: f=
                665.551, eps=0.002803230
Epoch 127: f=
                665.541, eps=0.002943392
Epoch 128: f=
                665.531, eps=0.003090561
Epoch 129: f=
                665.521, eps=0.003245089
Epoch 130: f=
                665.511, eps=0.003407344
Epoch 131: f=
                665.499, eps=0.003577711
Epoch 132: f=
                665.488, eps=0.003756596
Epoch 133: f=
                665.476, eps=0.003944426
Epoch 134: f=
                665.463, eps=0.004141647
Epoch 135: f=
                665.449, eps=0.004348730
Epoch 136: f=
                665.436, eps=0.004566166
Epoch 137: f=
                665.421, eps=0.004794475
Epoch 138: f=
                665.406, eps=0.005034198
Epoch 139: f=
                665.390, eps=0.005285908
Epoch 140: f=
                665.373, eps=0.005550204
Epoch 141: f=
                665.355, eps=0.005827714
Epoch 142: f=
                665.337, eps=0.006119100
Epoch 143: f=
                665.318, eps=0.006425055
Epoch 144: f=
                665.298, eps=0.006746307
Epoch 145: f=
                665.277, eps=0.007083623
Epoch 146: f=
                665.255, eps=0.007437804
Epoch 147: f=
                665.232, eps=0.007809694
Epoch 148: f=
                665.208, eps=0.008200179
Epoch 149: f=
                665.183, eps=0.008610188
Epoch 150: f=
                665.157, eps=0.009040697
Epoch 151: f=
                665.130, eps=0.009492732
Epoch 152: f=
                665.102, eps=0.009967368
Epoch 153: f=
                665.077, eps=0.010465737
                665.104, eps=0.005232868
Epoch 154: f=
Epoch 155: f=
                665.109, eps=0.002616434
Epoch 156: f=
                665.018, eps=0.002747256
Epoch 157: f=
                665.009, eps=0.002884619
Epoch 158: f=
                665.001, eps=0.003028850
Epoch 159: f=
                664.992, eps=0.003180292
Epoch 160: f=
                664.983, eps=0.003339307
Epoch 161: f=
                664.973, eps=0.003506272
Epoch 162: f=
                664.963, eps=0.003681586
Epoch 163: f=
                664.952, eps=0.003865665
Epoch 164: f=
                664.941, eps=0.004058948
Epoch 165: f=
                664.929, eps=0.004261896
Epoch 166: f=
                664.917, eps=0.004474990
Epoch 167: f=
                664.904, eps=0.004698740
Epoch 168: f=
                664.891, eps=0.004933677
```

```
Epoch 169: f=
                664.877, eps=0.005180361
Epoch 170: f=
                664.862, eps=0.005439379
Epoch 171: f=
                664.846, eps=0.005711348
Epoch 172: f=
                664.830, eps=0.005996915
Epoch 173: f=
                664.813, eps=0.006296761
Epoch 174: f=
                664.796, eps=0.006611599
Epoch 175: f=
                664.777, eps=0.006942179
Epoch 176: f=
                664.758, eps=0.007289288
Epoch 177: f=
                664.738, eps=0.007653752
Epoch 178: f=
                664.716, eps=0.008036440
Epoch 179: f=
                664.694, eps=0.008438262
Epoch 180: f=
                664.671, eps=0.008860175
                664.647, eps=0.009303184
Epoch 181: f=
Epoch 182: f=
                664.622, eps=0.009768343
Epoch 183: f=
                664.596, eps=0.010256760
Epoch 184: f=
                664.570, eps=0.010769598
Epoch 185: f=
                664.566, eps=0.011308078
Epoch 186: f=
                664.871, eps=0.005654039
Epoch 187: f=
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Epoch 188: f=
                664.495, eps=0.002968370
Epoch 189: f=
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Epoch 190: f=
                664.471, eps=0.003272628
Epoch 191: f=
                664.462, eps=0.003436260
Epoch 192: f=
                664.453, eps=0.003608073
Epoch 193: f=
                664.444, eps=0.003788476
Epoch 194: f=
                664.434, eps=0.003977900
Epoch 195: f=
                664.424, eps=0.004176795
Epoch 196: f=
                664.413, eps=0.004385635
Epoch 197: f=
                664.401, eps=0.004604917
Epoch 198: f=
                664.389, eps=0.004835163
Epoch 199: f=
                664.377, eps=0.005076921
Epoch 200: f=
                664.364, eps=0.005330767
Epoch 201: f=
                664.350, eps=0.005597305
Epoch 202: f=
                664.336, eps=0.005877170
Epoch 203: f=
                664.321, eps=0.006171029
Epoch 204: f=
                664.305, eps=0.006479580
Epoch 205: f=
                664.289, eps=0.006803559
Epoch 206: f=
                664.272, eps=0.007143737
Epoch 207: f=
                664.254, eps=0.007500924
Epoch 208: f=
                664.235, eps=0.007875970
Epoch 209: f=
                664.215, eps=0.008269769
Epoch 210: f=
                664.196, eps=0.008683257
Epoch 211: f=
                664.179, eps=0.009117420
Epoch 212: f=
                664.196, eps=0.004558710
Epoch 213: f=
                664.174, eps=0.004786646
Epoch 214: f=
                664.162, eps=0.005025978
Epoch 215: f=
                664.155, eps=0.005277277
Epoch 216: f=
                664.158, eps=0.002638638
```

```
Epoch 217: f=
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Epoch 218: f=
                664.090, eps=0.002909099
Epoch 219: f=
                664.083, eps=0.003054554
Epoch 220: f=
                664.075, eps=0.003207282
Epoch 221: f=
                664.068, eps=0.003367646
Epoch 222: f=
                664.059, eps=0.003536028
Epoch 223: f=
                664.051, eps=0.003712829
Epoch 224: f=
                664.042, eps=0.003898471
Epoch 225: f=
                664.033, eps=0.004093394
Epoch 226: f=
                664.023, eps=0.004298064
Epoch 227: f=
                664.013, eps=0.004512967
Epoch 228: f=
                664.002, eps=0.004738616
                663.991, eps=0.004975546
Epoch 229: f=
Epoch 230: f=
                663.979, eps=0.005224324
Epoch 231: f=
                663.967, eps=0.005485540
Epoch 232: f=
                663.954, eps=0.005759817
Epoch 233: f=
                663.940, eps=0.006047808
Epoch 234: f=
                663.926, eps=0.006350198
Epoch 235: f=
                663.911, eps=0.006667708
Epoch 236: f=
                663.895, eps=0.007001093
Epoch 237: f=
                663.879, eps=0.007351148
Epoch 238: f=
                663.862, eps=0.007718705
Epoch 239: f=
                663.844, eps=0.008104641
Epoch 240: f=
                663.826, eps=0.008509873
Epoch 241: f=
                663.806, eps=0.008935366
Epoch 242: f=
                663.786, eps=0.009382135
Epoch 243: f=
                663.765, eps=0.009851241
Epoch 244: f=
                663.743, eps=0.010343803
Epoch 245: f=
                663.723, eps=0.010860994
Epoch 246: f=
                663.747, eps=0.005430497
Epoch 247: f=
                663.762, eps=0.002715248
Epoch 248: f=
                663.678, eps=0.002851011
Epoch 249: f=
                663.671, eps=0.002993561
Epoch 250: f=
                663.664, eps=0.003143239
Epoch 251: f=
                663.657, eps=0.003300401
Epoch 252: f=
                663.650, eps=0.003465421
Epoch 253: f=
                663.642, eps=0.003638693
Epoch 254: f=
                663.634, eps=0.003820627
Epoch 255: f=
                663.626, eps=0.004011659
Epoch 256: f=
                663.617, eps=0.004212241
Epoch 257: f=
                663.608, eps=0.004422854
Epoch 258: f=
                663.598, eps=0.004643996
Epoch 259: f=
                663.588, eps=0.004876196
Epoch 260: f=
                663.577, eps=0.005120006
Epoch 261: f=
                663.566, eps=0.005376006
Epoch 262: f=
                663.555, eps=0.005644806
Epoch 263: f=
                663.543, eps=0.005927047
Epoch 264: f=
                663.530, eps=0.006223399
```

```
Epoch 265: f=
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Epoch 266: f=
                663.502, eps=0.006861297
Epoch 267: f=
                663.488, eps=0.007204362
Epoch 268: f=
                663.473, eps=0.007564580
Epoch 269: f=
                663.457, eps=0.007942809
Epoch 270: f=
                663.440, eps=0.008339950
Epoch 271: f=
                663.422, eps=0.008756947
Epoch 272: f=
                663.404, eps=0.009194795
Epoch 273: f=
                663.385, eps=0.009654535
Epoch 274: f=
                663.370, eps=0.010137261
Epoch 275: f=
                663.394, eps=0.005068631
Epoch 276: f=
                663.395, eps=0.002534315
Epoch 277: f=
                663.328, eps=0.002661031
Epoch 278: f=
                663.323, eps=0.002794083
Epoch 279: f=
                663.317, eps=0.002933787
Epoch 280: f=
                663.311, eps=0.003080476
Epoch 281: f=
                663.305, eps=0.003234500
Epoch 282: f=
                663.298, eps=0.003396225
Epoch 283: f=
                663.291, eps=0.003566036
Epoch 284: f=
                663.284, eps=0.003744338
Epoch 285: f=
                663.276, eps=0.003931555
Epoch 286: f=
                663.269, eps=0.004128133
Epoch 287: f=
                663.260, eps=0.004334539
Epoch 288: f=
                663.251, eps=0.004551266
Epoch 289: f=
                663.242, eps=0.004778830
Epoch 290: f=
                663.233, eps=0.005017771
Epoch 291: f=
                663.223, eps=0.005268660
Epoch 292: f=
                663.212, eps=0.005532093
Epoch 293: f=
                663.201, eps=0.005808697
Epoch 294: f=
                663.190, eps=0.006099132
Epoch 295: f=
                663.177, eps=0.006404089
Epoch 296: f=
                663.165, eps=0.006724293
Epoch 297: f=
                663.152, eps=0.007060508
Epoch 298: f=
                663.138, eps=0.007413533
Epoch 299: f=
                663.123, eps=0.007784210
Epoch 300: f=
                663.108, eps=0.008173420
Epoch 301: f=
                663.092, eps=0.008582091
Epoch 302: f=
                663.075, eps=0.009011196
Epoch 303: f=
                663.058, eps=0.009461756
Epoch 304: f=
                663.040, eps=0.009934843
Epoch 305: f=
                663.021, eps=0.010431585
Epoch 306: f=
                663.001, eps=0.010953165
Epoch 307: f=
                662.981, eps=0.011500823
Epoch 308: f=
                662.965, eps=0.012075864
Epoch 309: f=
                663.032, eps=0.006037932
Epoch 310: f=
                663.136, eps=0.003018966
Epoch 311: f=
                662.928, eps=0.003169914
Epoch 312: f=
                662.914, eps=0.003328410
```

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Epoch 313: f=
                662.907, eps=0.003494831
Epoch 314: f=
                662.901, eps=0.003669572
Epoch 315: f=
                662.894, eps=0.003853051
                662.887, eps=0.004045703
Epoch 316: f=
Epoch 317: f=
                662.879, eps=0.004247988
Epoch 318: f=
                662.871, eps=0.004460388
Epoch 319: f=
                662.863, eps=0.004683407
Epoch 320: f=
                662.855, eps=0.004917578
Epoch 321: f=
                662.846, eps=0.005163456
Epoch 322: f=
                662.836, eps=0.005421629
Epoch 323: f=
                662.826, eps=0.005692711
Epoch 324: f=
                662.816, eps=0.005977346
Epoch 325: f=
                662.805, eps=0.006276214
Epoch 326: f=
                662.794, eps=0.006590024
Epoch 327: f=
                662.782, eps=0.006919525
Epoch 328: f=
                662.770, eps=0.007265502
Epoch 329: f=
                662.757, eps=0.007628777
Epoch 330: f=
                662.745, eps=0.008010216
Epoch 331: f=
                662.741, eps=0.008410726
Epoch 332: f=
                662.791, eps=0.004205363
Epoch 333: f=
                662.746, eps=0.004415631
Epoch 334: f=
                662.726, eps=0.004636413
Epoch 335: f=
                662.714, eps=0.004868234
Epoch 336: f=
                662.706, eps=0.005111645
Epoch 337: f=
                662.703, eps=0.005367228
Epoch 338: f=
                662.708, eps=0.002683614
Epoch 339: f=
                662.659, eps=0.002817794
Epoch 340: f=
                662.654, eps=0.002958684
Epoch 341: f=
                662.649, eps=0.003106618
Epoch 342: f=
                662.643, eps=0.003261949
Epoch 343: f=
                662.638, eps=0.003425047
Epoch 344: f=
                662.632, eps=0.003596299
Epoch 345: f=
                662.626, eps=0.003776114
Epoch 346: f=
                662.619, eps=0.003964920
Epoch 347: f=
                662.612, eps=0.004163166
Epoch 348: f=
                662.605, eps=0.004371324
Epoch 349: f=
                662.598, eps=0.004589890
Epoch 350: f=
                662.590, eps=0.004819385
Epoch 351: f=
                662.582, eps=0.005060354
Epoch 352: f=
                662.573, eps=0.005313372
Epoch 353: f=
                662.564, eps=0.005579040
Epoch 354: f=
                662.554, eps=0.005857992
Epoch 355: f=
                662.544, eps=0.006150892
Epoch 356: f=
                662.534, eps=0.006458437
Epoch 357: f=
                662.523, eps=0.006781358
Epoch 358: f=
                662.512, eps=0.007120426
Epoch 359: f=
                662.500, eps=0.007476448
Epoch 360: f=
                662.487, eps=0.007850270
```

```
Epoch 361: f=
                662.474, eps=0.008242783
Epoch 362: f=
                662.461, eps=0.008654923
Epoch 363: f=
                662.446, eps=0.009087669
Epoch 364: f=
                662.431, eps=0.009542052
Epoch 365: f=
                662.416, eps=0.010019155
Epoch 366: f=
                662.404, eps=0.010520113
Epoch 367: f=
                662.430, eps=0.005260056
Epoch 368: f=
                662.441, eps=0.002630028
Epoch 369: f=
                662.370, eps=0.002761530
Epoch 370: f=
                662.365, eps=0.002899606
Epoch 371: f=
                662.360, eps=0.003044586
Epoch 372: f=
                662.355, eps=0.003196816
Epoch 373: f=
                662.350, eps=0.003356656
Epoch 374: f=
                662.345, eps=0.003524489
Epoch 375: f=
                662.339, eps=0.003700714
Epoch 376: f=
                662.333, eps=0.003885749
Epoch 377: f=
                662.327, eps=0.004080037
Epoch 378: f=
                662.321, eps=0.004284039
Epoch 379: f=
                662.314, eps=0.004498241
Epoch 380: f=
                662.307, eps=0.004723153
Epoch 381: f=
                662.299, eps=0.004959310
Epoch 382: f=
                662.291, eps=0.005207276
Epoch 383: f=
                662.283, eps=0.005467640
Epoch 384: f=
                662.275, eps=0.005741022
Epoch 385: f=
                662.266, eps=0.006028073
Epoch 386: f=
                662.256, eps=0.006329476
Epoch 387: f=
                662.246, eps=0.006645950
Epoch 388: f=
                662.236, eps=0.006978248
Epoch 389: f=
                662.225, eps=0.007327160
Epoch 390: f=
                662.214, eps=0.007693518
Epoch 391: f=
                662.202, eps=0.008078194
Epoch 392: f=
                662.189, eps=0.008482104
Epoch 393: f=
                662.176, eps=0.008906209
Epoch 394: f=
                662.163, eps=0.009351519
Epoch 395: f=
                662.148, eps=0.009819095
Epoch 396: f=
                662.134, eps=0.010310050
Epoch 397: f=
                662.121, eps=0.010825552
Epoch 398: f=
                662.134, eps=0.005412776
Epoch 399: f=
                662.143, eps=0.002706388
Epoch 400: f=
                662.090, eps=0.002841708
Epoch 401: f=
                662.085, eps=0.002983793
Epoch 402: f=
                662.081, eps=0.003132983
Epoch 403: f=
                662.076, eps=0.003289632
Epoch 404: f=
                662.071, eps=0.003454113
Epoch 405: f=
                662.066, eps=0.003626819
Epoch 406: f=
                662.061, eps=0.003808160
Epoch 407: f=
                662.055, eps=0.003998568
Epoch 408: f=
                662.049, eps=0.004198496
```

```
Epoch 409: f=
                662.043, eps=0.004408421
Epoch 410: f=
                662.037, eps=0.004628842
Epoch 411: f=
                662.030, eps=0.004860284
Epoch 412: f=
                662.023, eps=0.005103298
Epoch 413: f=
                662.015, eps=0.005358463
Epoch 414: f=
                662.007, eps=0.005626387
Epoch 415: f=
                661.999, eps=0.005907706
Epoch 416: f=
                661.991, eps=0.006203091
Epoch 417: f=
                661.982, eps=0.006513246
Epoch 418: f=
                661.972, eps=0.006838908
Epoch 419: f=
                661.962, eps=0.007180853
Epoch 420: f=
                661.952, eps=0.007539896
                661.941, eps=0.007916891
Epoch 421: f=
Epoch 422: f=
                661.930, eps=0.008312735
Epoch 423: f=
                661.918, eps=0.008728372
Epoch 424: f=
                661.906, eps=0.009164791
Epoch 425: f=
                661.893, eps=0.009623030
Epoch 426: f=
                661.881, eps=0.010104182
Epoch 427: f=
                661.884, eps=0.005052091
Epoch 428: f=
                661.881, eps=0.005304695
Epoch 429: f=
                661.883, eps=0.002652348
Epoch 430: f=
                661.847, eps=0.002784965
Epoch 431: f=
                661.843, eps=0.002924213
Epoch 432: f=
                661.839, eps=0.003070424
Epoch 433: f=
                661.835, eps=0.003223945
Epoch 434: f=
                661.830, eps=0.003385142
Epoch 435: f=
                661.826, eps=0.003554400
Epoch 436: f=
                661.821, eps=0.003732120
Epoch 437: f=
                661.816, eps=0.003918726
Epoch 438: f=
                661.810, eps=0.004114662
Epoch 439: f=
                661.804, eps=0.004320395
Epoch 440: f=
                661.799, eps=0.004536415
Epoch 441: f=
                661.792, eps=0.004763235
Epoch 442: f=
                661.786, eps=0.005001397
Epoch 443: f=
                661.779, eps=0.005251467
Epoch 444: f=
                661.772, eps=0.005514040
Epoch 445: f=
                661.764, eps=0.005789742
Epoch 446: f=
                661.757, eps=0.006079230
Epoch 447: f=
                661.748, eps=0.006383191
Epoch 448: f=
                661.740, eps=0.006702351
Epoch 449: f=
                661.731, eps=0.007037468
Epoch 450: f=
                661.721, eps=0.007389342
Epoch 451: f=
                661.711, eps=0.007758809
Epoch 452: f=
                661.701, eps=0.008146749
Epoch 453: f=
                661.690, eps=0.008554086
Epoch 454: f=
                661.679, eps=0.008981791
Epoch 455: f=
                661.667, eps=0.009430880
Epoch 456: f=
                661.655, eps=0.009902424
```

```
Epoch 457: f=
                661.642, eps=0.010397546
Epoch 458: f=
                661.635, eps=0.010917423
Epoch 459: f=
                661.703, eps=0.005458711
Epoch 460: f=
                661.746, eps=0.002729356
Epoch 461: f=
                661.605, eps=0.002865824
Epoch 462: f=
                661.600, eps=0.003009115
Epoch 463: f=
                661.596, eps=0.003159570
Epoch 464: f=
                661.592, eps=0.003317549
Epoch 465: f=
                661.588, eps=0.003483426
Epoch 466: f=
                661.583, eps=0.003657598
Epoch 467: f=
                661.578, eps=0.003840478
Epoch 468: f=
                661.574, eps=0.004032501
Epoch 469: f=
                661.568, eps=0.004234127
Epoch 470: f=
                661.563, eps=0.004445833
Epoch 471: f=
                661.557, eps=0.004668125
Epoch 472: f=
                661.551, eps=0.004901531
Epoch 473: f=
                661.545, eps=0.005146607
Epoch 474: f=
                661.539, eps=0.005403938
Epoch 475: f=
                661.532, eps=0.005674135
Epoch 476: f=
                661.525, eps=0.005957841
Epoch 477: f=
                661.517, eps=0.006255733
Epoch 478: f=
                661.510, eps=0.006568520
Epoch 479: f=
                661.501, eps=0.006896946
Epoch 480: f=
                661.493, eps=0.007241793
Epoch 481: f=
                661.484, eps=0.007603883
Epoch 482: f=
                661.474, eps=0.007984077
Epoch 483: f=
                661.464, eps=0.008383281
Epoch 484: f=
                661.454, eps=0.008802445
Epoch 485: f=
                661.444, eps=0.009242567
Epoch 486: f=
                661.433, eps=0.009704696
Epoch 487: f=
                661.431, eps=0.010189930
Epoch 488: f=
                661.519, eps=0.005094965
Epoch 489: f=
                661.530, eps=0.002547483
Epoch 490: f=
                661.399, eps=0.002674857
Epoch 491: f=
                661.395, eps=0.002808600
Epoch 492: f=
                661.392, eps=0.002949030
Epoch 493: f=
                661.389, eps=0.003096481
Epoch 494: f=
                661.385, eps=0.003251305
Epoch 495: f=
                661.381, eps=0.003413870
Epoch 496: f=
                661.377, eps=0.003584564
Epoch 497: f=
                661.373, eps=0.003763792
Epoch 498: f=
                661.368, eps=0.003951982
Epoch 499: f=
                661.363, eps=0.004149581
Result after 500 epochs: f=661.3584589394447
Epoch
               6652.989, eps=0.010000000
        0: f=
Epoch
        1: f=
               4300.327, eps=0.010500000
Epoch
               2705.946, eps=0.011025000
        2: f=
               1951.518, eps=0.011576250
Epoch
        3: f=
```

```
Epoch
               1463.730, eps=0.012155063
       4: f=
Epoch
        5: f=
               1215.472, eps=0.012762816
Epoch
        6: f=
               1055.995, eps=0.013400956
       7: f=
                958.296, eps=0.014071004
Epoch
Epoch
        8: f=
                899.029, eps=0.014774554
Epoch
        9: f=
                871.206, eps=0.015513282
Epoch
      10: f=
                886.721, eps=0.007756641
Epoch
      11: f=
                820.444, eps=0.008144473
Epoch
      12: f=
                800.657, eps=0.008551697
Epoch
      13: f=
                832.124, eps=0.004275848
      14: f=
                746.346, eps=0.004489641
Epoch
Epoch
      15: f=
                733.413, eps=0.004714123
                727.538, eps=0.004949829
Epoch
      16: f=
Epoch
      17: f=
                722.609, eps=0.005197320
Epoch 18: f=
                717.979, eps=0.005457186
Epoch 19: f=
                713.593, eps=0.005730046
Epoch 20: f=
                709.449, eps=0.006016548
Epoch
      21: f=
                705.556, eps=0.006317375
Epoch 22: f=
                701.942, eps=0.006633244
Epoch
      23: f=
                698.684, eps=0.006964906
Epoch
      24: f=
                696.021, eps=0.007313152
Epoch 25: f=
                694.553, eps=0.007678809
Epoch 26: f=
                695.168, eps=0.003839405
Epoch 27: f=
                688.767, eps=0.004031375
Epoch 28: f=
                687.488, eps=0.004232944
Epoch 29: f=
                686.352, eps=0.004444591
                685.272, eps=0.004666820
Epoch
      30: f=
Epoch
      31: f=
                684.239, eps=0.004900161
Epoch
      32: f=
                683.253, eps=0.005145169
Epoch 33: f=
                682.319, eps=0.005402428
Epoch 34: f=
                681.442, eps=0.005672549
Epoch
      35: f=
                680.628, eps=0.005956177
Epoch 36: f=
                679.890, eps=0.006253986
                679.261, eps=0.006566685
Epoch
      37: f=
      38: f=
Epoch
                678.837, eps=0.006895019
Epoch
      39: f=
                678.917, eps=0.003447510
Epoch
      40: f=
                677.822, eps=0.003619885
Epoch 41: f=
                677.503, eps=0.003800879
Epoch 42: f=
                677.262, eps=0.003990923
Epoch 43: f=
                677.043, eps=0.004190469
Epoch 44: f=
                676.838, eps=0.004399993
Epoch
      45: f=
                676.645, eps=0.004619993
      46: f=
                676.464, eps=0.004850992
Epoch
Epoch
      47: f=
                676.294, eps=0.005093542
Epoch
      48: f=
                676.138, eps=0.005348219
Epoch
      49: f=
                675.993, eps=0.005615630
Epoch 50: f=
                675.861, eps=0.005896411
Epoch 51: f=
                675.744, eps=0.006191232
```

```
Epoch 52: f=
                675.644, eps=0.006500794
Epoch 53: f=
                675.580, eps=0.006825833
Epoch 54: f=
                675.615, eps=0.003412917
Epoch
      55: f=
                675.423, eps=0.003583562
Epoch 56: f=
                675.365, eps=0.003762741
Epoch 57: f=
                675.324, eps=0.003950878
Epoch
      58: f=
                675.287, eps=0.004148421
Epoch 59: f=
                675.252, eps=0.004355843
Epoch 60: f=
                675.218, eps=0.004573635
Epoch 61: f=
                675.186, eps=0.004802316
      62: f=
                675.156, eps=0.005042432
Epoch
Epoch 63: f=
                675.126, eps=0.005294554
Epoch
      64: f=
                675.098, eps=0.005559282
Epoch
      65: f=
                675.072, eps=0.005837246
Epoch 66: f=
                675.047, eps=0.006129108
Epoch 67: f=
                675.025, eps=0.006435563
Epoch 68: f=
                675.009, eps=0.006757341
Epoch 69: f=
                675.013, eps=0.003378671
Epoch 70: f=
                674.972, eps=0.003547604
Epoch
                674.957, eps=0.003724984
      71: f=
Epoch
      72: f=
                674.945, eps=0.003911234
Epoch 73: f=
                674.935, eps=0.004106795
Epoch 74: f=
                674.924, eps=0.004312135
Epoch 75: f=
                674.914, eps=0.004527742
                674.903, eps=0.004754129
Epoch 76: f=
Epoch 77: f=
                674.893, eps=0.004991835
Epoch 78: f=
                674.883, eps=0.005241427
Epoch 79: f=
                674.872, eps=0.005503499
Epoch 80: f=
                674.862, eps=0.005778674
Epoch 81: f=
                674.851, eps=0.006067607
Epoch 82: f=
                674.841, eps=0.006370988
Epoch
      83: f=
                674.831, eps=0.006689537
Epoch 84: f=
                674.824, eps=0.007024014
Epoch 85: f=
                674.829, eps=0.003512007
      86: f=
Epoch
                674.808, eps=0.003687607
Epoch
      87: f=
                674.799, eps=0.003871988
Epoch 88: f=
                674.793, eps=0.004065587
Epoch 89: f=
                674.787, eps=0.004268866
Epoch 90: f=
                674.781, eps=0.004482310
Epoch 91: f=
                674.775, eps=0.004706425
Epoch 92: f=
                674.769, eps=0.004941746
Epoch 93: f=
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                674.756, eps=0.005448275
Epoch
      94: f=
Epoch 95: f=
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Epoch 96: f=
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Epoch
      97: f=
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Epoch 98: f=
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                674.730, eps=0.006953533
Epoch 99: f=
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Epoch 102: f=
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                674.701, eps=0.004024792
Epoch 103: f=
Epoch 104: f=
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Epoch 105: f=
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Epoch 106: f=
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Epoch 107: f=
                674.682, eps=0.004892160
Epoch 108: f=
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Epoch 109: f=
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Epoch 110: f=
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Epoch 111: f=
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Epoch 112: f=
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Epoch 113: f=
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Epoch 114: f=
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Epoch 115: f=
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Epoch 116: f=
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Epoch 117: f=
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Epoch 118: f=
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Epoch 119: f=
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Epoch 120: f=
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Epoch 121: f=
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Epoch 122: f=
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Epoch 123: f=
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Epoch 124: f=
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Epoch 125: f=
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Epoch 126: f=
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Epoch 127: f=
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Epoch 128: f=
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Epoch 129: f=
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Epoch 130: f=
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Epoch 131: f=
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Epoch 132: f=
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Epoch 133: f=
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Epoch 136: f=
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Epoch 137: f=
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Epoch 138: f=
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Epoch 139: f=
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Epoch 140: f=
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Epoch 141: f=
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                674.534, eps=0.006119100
Epoch 142: f=
Epoch 143: f=
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Epoch 144: f=
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Epoch 145: f=
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Epoch 147: f=
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Epoch 151: f=
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Epoch 152: f=
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Epoch 153: f=
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Epoch 154: f=
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Epoch 155: f=
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Epoch 156: f=
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Epoch 157: f=
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Epoch 159: f=
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                674.473, eps=0.007012544
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Epoch 162: f=
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Epoch 163: f=
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Epoch 164: f=
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Epoch 165: f=
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Epoch 166: f=
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Epoch 167: f=
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Epoch 171: f=
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Epoch 175: f=
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Epoch 183: f=
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Epoch 184: f=
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Epoch 186: f=
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Epoch 187: f=
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Epoch 188: f=
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Epoch 189: f=
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                674.394, eps=0.006872520
Epoch 190: f=
Epoch 191: f=
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Epoch 192: f=
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Epoch 193: f=
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Epoch 194: f=
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Epoch 195: f=
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Epoch 204: f=
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Epoch 207: f=
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Epoch 208: f=
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Epoch 209: f=
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                674.349, eps=0.004134885
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Epoch 211: f=
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Epoch 213: f=
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Epoch 214: f=
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Epoch 215: f=
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Epoch 216: f=
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Epoch 217: f=
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Epoch 218: f=
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Epoch 223: f=
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Epoch 225: f=
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Epoch 230: f=
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Epoch 243: f=
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Epoch 251: f=
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Epoch 252: f=
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Epoch 253: f=
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Epoch 254: f=
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Epoch 255: f=
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Epoch 256: f=
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Epoch 270: f=
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Epoch 274: f=
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Epoch 277: f=
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Epoch 278: f=
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Epoch 279: f=
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Epoch 280: f=
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Epoch 281: f=
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Epoch 282: f=
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Epoch 283: f=
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Epoch 284: f=
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Epoch 286: f=
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Epoch 287: f=
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Epoch 288: f=
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Epoch 289: f=
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Epoch 291: f=
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Epoch 296: f=
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Epoch 308: f=
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Epoch 335: f=
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Epoch 336: f=
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Epoch 337: f=
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Epoch 339: f=
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Epoch 343: f=
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Epoch 347: f=
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Epoch 374: f=
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Epoch 385: f=
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Epoch 386: f=
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Epoch 387: f=
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Epoch 392: f=
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Epoch 399: f=
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Epoch 406: f=
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Epoch 407: f=
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Epoch 409: f=
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Epoch 412: f=
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Epoch 419: f=
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Epoch 432: f=
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Epoch 433: f=
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Epoch 435: f=
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Epoch 436: f=
                674.118, eps=0.007837451
Epoch 437: f=
                674.118, eps=0.008229324
Epoch 438: f=
                674.117, eps=0.008640790
                674.117, eps=0.009072829
Epoch 439: f=
Epoch 440: f=
                674.116, eps=0.009526471
Epoch 441: f=
                674.116, eps=0.010002794
Epoch 442: f=
                674.116, eps=0.010502934
Epoch 443: f=
                674.121, eps=0.005251467
Epoch 444: f=
                674.124, eps=0.002625734
Epoch 445: f=
                674.114, eps=0.002757020
                674.114, eps=0.002894871
Epoch 446: f=
Epoch 447: f=
                674.114, eps=0.003039615
Epoch 448: f=
                674.113, eps=0.003191596
Epoch 449: f=
                674.113, eps=0.003351175
Epoch 450: f=
                674.113, eps=0.003518734
Epoch 451: f=
                674.113, eps=0.003694671
Epoch 452: f=
                674.113, eps=0.003879404
Epoch 453: f=
                674.113, eps=0.004073375
Epoch 454: f=
                674.112, eps=0.004277043
Epoch 455: f=
                674.112, eps=0.004490895
Epoch 456: f=
                674.112, eps=0.004715440
Epoch 457: f=
                674.112, eps=0.004951212
Epoch 458: f=
                674.111, eps=0.005198773
Epoch 459: f=
                674.111, eps=0.005458711
Epoch 460: f=
                674.111, eps=0.005731647
Epoch 461: f=
                674.111, eps=0.006018229
Epoch 462: f=
                674.110, eps=0.006319141
Epoch 463: f=
                674.110, eps=0.006635098
Epoch 464: f=
                674.110, eps=0.006966853
                674.109, eps=0.007315195
Epoch 465: f=
Epoch 466: f=
                674.109, eps=0.007680955
Epoch 467: f=
                674.109, eps=0.008065003
Epoch 468: f=
                674.108, eps=0.008468253
Epoch 469: f=
                674.108, eps=0.008891666
                674.107, eps=0.009336249
Epoch 470: f=
                674.107, eps=0.009803061
Epoch 471: f=
Epoch 472: f=
                674.107, eps=0.010293215
Epoch 473: f=
                674.107, eps=0.005146607
Epoch 474: f=
                674.107, eps=0.002573304
Epoch 475: f=
                674.106, eps=0.002701969
Epoch 476: f=
                674.106, eps=0.002837067
Epoch 477: f=
                674.106, eps=0.002978921
Epoch 478: f=
                674.105, eps=0.003127867
Epoch 479: f=
                674.105, eps=0.003284260
Epoch 480: f=
                674.105, eps=0.003448473
Epoch 481: f=
                674.105, eps=0.003620897
Epoch 482: f=
                674.105, eps=0.003801941
Epoch 483: f=
                674.105, eps=0.003992039
```

```
Epoch 484: f=
                674.105, eps=0.004191640
Epoch 485: f=
                674.104, eps=0.004401222
Epoch 486: f=
                674.104, eps=0.004621284
Epoch 487: f=
                674.104, eps=0.004852348
Epoch 488: f=
                674.104, eps=0.005094965
Epoch 489: f=
                674.104, eps=0.005349713
Epoch 490: f=
                674.103, eps=0.005617199
Epoch 491: f=
                674.103, eps=0.005898059
Epoch 492: f=
                674.103, eps=0.006192962
Epoch 493: f=
                674.103, eps=0.006502610
                674.103, eps=0.006827741
Epoch 494: f=
Epoch 495: f=
                674.102, eps=0.007169128
Epoch 496: f=
                674.102, eps=0.007527584
Epoch 497: f=
                674.102, eps=0.007903963
Epoch 498: f=
                674.101, eps=0.008299161
Epoch 499: f=
                674.101, eps=0.008714119
Result after 500 epochs: f=674.1008281100459
Epoch
        0: f=
               6669.770, eps=0.010000000
Epoch
        1: f=
               4383.683, eps=0.010500000
               2752.887, eps=0.011025000
Epoch
        2: f=
Epoch
        3: f=
               1974.583, eps=0.011576250
Epoch
        4: f=
               1475.521, eps=0.012155063
Epoch
        5: f=
               1220.853, eps=0.012762816
Epoch
        6: f=
               1057.063, eps=0.013400956
        7: f=
Epoch
                957.284, eps=0.014071004
                900.055, eps=0.014774554
        8: f=
Epoch
                877.595, eps=0.015513282
Epoch
        9: f=
Epoch
       10: f=
                909.332, eps=0.007756641
Epoch
       11: f=
                822.850, eps=0.008144473
                781.300, eps=0.008551697
Epoch
      12: f=
Epoch 13: f=
                798.122, eps=0.004275848
                738.850, eps=0.004489641
Epoch
       14: f=
Epoch
      15: f=
                731.040, eps=0.004714123
Epoch
       16: f=
                726.009, eps=0.004949829
       17: f=
Epoch
                721.535, eps=0.005197320
Epoch
       18: f=
                717.358, eps=0.005457186
Epoch
      19: f=
                713.453, eps=0.005730046
Epoch
      20: f=
                709.837, eps=0.006016548
Epoch 21: f=
                706.559, eps=0.006317375
Epoch 22: f=
                703.753, eps=0.006633244
Epoch
      23: f=
                701.690, eps=0.006964906
Epoch
      24: f=
                700.826, eps=0.007313152
Epoch
      25: f=
                701.209, eps=0.003656576
Epoch 26: f=
                694.511, eps=0.003839405
Epoch
      27: f=
                693.303, eps=0.004031375
Epoch
      28: f=
                692.297, eps=0.004232944
Epoch
      29: f=
                691.359, eps=0.004444591
                690.473, eps=0.004666820
Epoch 30: f=
```

```
Epoch 31: f=
                689.637, eps=0.004900161
Epoch 32: f=
                688.852, eps=0.005145169
Epoch 33: f=
                688.122, eps=0.005402428
Epoch
      34: f=
                687.450, eps=0.005672549
Epoch 35: f=
                686.842, eps=0.005956177
Epoch
      36: f=
                686.310, eps=0.006253986
Epoch
      37: f=
                685.885, eps=0.006566685
Epoch 38: f=
                685.676, eps=0.006895019
Epoch 39: f=
                686.028, eps=0.003447510
Epoch 40: f=
                684.915, eps=0.003619885
                684.667, eps=0.003800879
Epoch
      41: f=
Epoch 42: f=
                684.504, eps=0.003990923
                684.364, eps=0.004190469
Epoch 43: f=
Epoch
      44: f=
                684.236, eps=0.004399993
Epoch 45: f=
                684.119, eps=0.004619993
Epoch 46: f=
                684.011, eps=0.004850992
Epoch 47: f=
                683.911, eps=0.005093542
Epoch 48: f=
                683.821, eps=0.005348219
Epoch 49: f=
                683.739, eps=0.005615630
Epoch 50: f=
                683.666, eps=0.005896411
Epoch
      51: f=
                683.605, eps=0.006191232
Epoch 52: f=
                683.563, eps=0.006500794
Epoch 53: f=
                683.568, eps=0.003250397
Epoch 54: f=
                683.465, eps=0.003412917
                683.432, eps=0.003583562
Epoch 55: f=
Epoch 56: f=
                683.408, eps=0.003762741
Epoch 57: f=
                683.386, eps=0.003950878
Epoch 58: f=
                683.365, eps=0.004148421
Epoch 59: f=
                683.345, eps=0.004355843
Epoch 60: f=
                683.326, eps=0.004573635
Epoch 61: f=
                683.307, eps=0.004802316
Epoch
      62: f=
                683.290, eps=0.005042432
Epoch 63: f=
                683.273, eps=0.005294554
                683.257, eps=0.005559282
Epoch 64: f=
      65: f=
Epoch
                683.241, eps=0.005837246
Epoch
      66: f=
                683.227, eps=0.006129108
Epoch 67: f=
                683.213, eps=0.006435563
Epoch
                683.200, eps=0.006757341
      68: f=
Epoch 69: f=
                683.191, eps=0.007095208
Epoch 70: f=
                683.191, eps=0.003547604
Epoch 71: f=
                683.172, eps=0.003724984
Epoch 72: f=
                683.164, eps=0.003911234
Epoch 73: f=
                683.158, eps=0.004106795
Epoch 74: f=
                683.152, eps=0.004312135
                683.146, eps=0.004527742
Epoch 75: f=
Epoch
      76: f=
                683.140, eps=0.004754129
Epoch
      77: f=
                683.134, eps=0.004991835
                683.128, eps=0.005241427
Epoch
      78: f=
```

```
Epoch 79: f=
                683.122, eps=0.005503499
Epoch 80: f=
                683.117, eps=0.005778674
Epoch 81: f=
                683.111, eps=0.006067607
                683.107, eps=0.006370988
Epoch
      82: f=
Epoch 83: f=
                683.105, eps=0.006689537
Epoch 84: f=
                683.113, eps=0.003344768
Epoch
      85: f=
                683.093, eps=0.003512007
Epoch 86: f=
                683.087, eps=0.003687607
Epoch 87: f=
                683.084, eps=0.003871988
Epoch 88: f=
                683.080, eps=0.004065587
                683.077, eps=0.004268866
Epoch
      89: f=
Epoch 90: f=
                683.074, eps=0.004482310
                683.070, eps=0.004706425
Epoch 91: f=
Epoch
      92: f=
                683.067, eps=0.004941746
Epoch 93: f=
                683.063, eps=0.005188834
Epoch 94: f=
                683.059, eps=0.005448275
Epoch 95: f=
                683.056, eps=0.005720689
Epoch 96: f=
                683.052, eps=0.006006724
                683.048, eps=0.006307060
Epoch 97: f=
Epoch 98: f=
                683.044, eps=0.006622413
Epoch 99: f=
                683.042, eps=0.006953533
Epoch 100: f=
                683.044, eps=0.003476767
Epoch 101: f=
                683.035, eps=0.003650605
Epoch 102: f=
                683.032, eps=0.003833135
Epoch 103: f=
                683.029, eps=0.004024792
Epoch 104: f=
                683.027, eps=0.004226032
Epoch 105: f=
                683.024, eps=0.004437333
Epoch 106: f=
                683.022, eps=0.004659200
Epoch 107: f=
                683.019, eps=0.004892160
Epoch 108: f=
                683.017, eps=0.005136768
Epoch 109: f=
                683.014, eps=0.005393606
Epoch 110: f=
                683.011, eps=0.005663287
Epoch 111: f=
                683.009, eps=0.005946451
                683.006, eps=0.006243773
Epoch 112: f=
Epoch 113: f=
                683.004, eps=0.006555962
Epoch 114: f=
                683.003, eps=0.006883760
Epoch 115: f=
                683.008, eps=0.003441880
Epoch 116: f=
                682.997, eps=0.003613974
Epoch 117: f=
                682.994, eps=0.003794673
Epoch 118: f=
                682.992, eps=0.003984406
Epoch 119: f=
                682.990, eps=0.004183627
Epoch 120: f=
                682.988, eps=0.004392808
                682.986, eps=0.004612449
Epoch 121: f=
Epoch 122: f=
                682.984, eps=0.004843071
Epoch 123: f=
                682.982, eps=0.005085225
Epoch 124: f=
                682.980, eps=0.005339486
Epoch 125: f=
                682.978, eps=0.005606460
Epoch 126: f=
                682.976, eps=0.005886783
```

```
Epoch 127: f=
                682.974, eps=0.006181122
Epoch 128: f=
                682.972, eps=0.006490178
Epoch 129: f=
                682.971, eps=0.006814687
Epoch 130: f=
                682.975, eps=0.003407344
Epoch 131: f=
                682.967, eps=0.003577711
Epoch 132: f=
                682.964, eps=0.003756596
Epoch 133: f=
                682.963, eps=0.003944426
Epoch 134: f=
                682.961, eps=0.004141647
Epoch 135: f=
                682.960, eps=0.004348730
Epoch 136: f=
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                682.957, eps=0.004794475
Epoch 137: f=
Epoch 138: f=
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                682.954, eps=0.005285908
Epoch 139: f=
Epoch 140: f=
                682.952, eps=0.005550204
Epoch 141: f=
                682.950, eps=0.005827714
Epoch 142: f=
                682.948, eps=0.006119100
Epoch 143: f=
                682.947, eps=0.006425055
Epoch 144: f=
                682.946, eps=0.006746307
Epoch 145: f=
                682.946, eps=0.003373154
Epoch 146: f=
                682.942, eps=0.003541811
Epoch 147: f=
                682.941, eps=0.003718902
Epoch 148: f=
                682.940, eps=0.003904847
Epoch 149: f=
                682.939, eps=0.004100089
Epoch 150: f=
                682.938, eps=0.004305094
Epoch 151: f=
                682.936, eps=0.004520348
Epoch 152: f=
                682.935, eps=0.004746366
Epoch 153: f=
                682.934, eps=0.004983684
Epoch 154: f=
                682.933, eps=0.005232868
Epoch 155: f=
                682.931, eps=0.005494512
Epoch 156: f=
                682.930, eps=0.005769237
Epoch 157: f=
                682.929, eps=0.006057699
Epoch 158: f=
                682.927, eps=0.006360584
Epoch 159: f=
                682.926, eps=0.006678613
Epoch 160: f=
                682.925, eps=0.007012544
Epoch 161: f=
                682.925, eps=0.003506272
Epoch 162: f=
                682.922, eps=0.003681586
Epoch 163: f=
                682.921, eps=0.003865665
Epoch 164: f=
                682.920, eps=0.004058948
Epoch 165: f=
                682.919, eps=0.004261896
Epoch 166: f=
                682.918, eps=0.004474990
Epoch 167: f=
                682.917, eps=0.004698740
Epoch 168: f=
                682.916, eps=0.004933677
Epoch 169: f=
                682.915, eps=0.005180361
Epoch 170: f=
                682.914, eps=0.005439379
Epoch 171: f=
                682.913, eps=0.005711348
Epoch 172: f=
                682.912, eps=0.005996915
Epoch 173: f=
                682.911, eps=0.006296761
Epoch 174: f=
                682.910, eps=0.006611599
```

```
Epoch 175: f=
                682.910, eps=0.006942179
Epoch 176: f=
                682.914, eps=0.003471089
Epoch 177: f=
                682.908, eps=0.003644644
                682.907, eps=0.003826876
Epoch 178: f=
Epoch 179: f=
                682.906, eps=0.004018220
Epoch 180: f=
                682.905, eps=0.004219131
Epoch 181: f=
                682.904, eps=0.004430087
Epoch 182: f=
                682.903, eps=0.004651592
Epoch 183: f=
                682.903, eps=0.004884171
Epoch 184: f=
                682.902, eps=0.005128380
                682.901, eps=0.005384799
Epoch 185: f=
Epoch 186: f=
                682.900, eps=0.005654039
Epoch 187: f=
                682.899, eps=0.005936741
Epoch 188: f=
                682.899, eps=0.006233578
Epoch 189: f=
                682.898, eps=0.006545257
Epoch 190: f=
                682.899, eps=0.003272628
Epoch 191: f=
                682.896, eps=0.003436260
Epoch 192: f=
                682.896, eps=0.003608073
Epoch 193: f=
                682.895, eps=0.003788476
Epoch 194: f=
                682.895, eps=0.003977900
Epoch 195: f=
                682.894, eps=0.004176795
Epoch 196: f=
                682.893, eps=0.004385635
Epoch 197: f=
                682.893, eps=0.004604917
Epoch 198: f=
                682.892, eps=0.004835163
Epoch 199: f=
                682.892, eps=0.005076921
Epoch 200: f=
                682.891, eps=0.005330767
Epoch 201: f=
                682.890, eps=0.005597305
Epoch 202: f=
                682.890, eps=0.005877170
Epoch 203: f=
                682.889, eps=0.006171029
Epoch 204: f=
                682.888, eps=0.006479580
Epoch 205: f=
                682.887, eps=0.006803559
Epoch 206: f=
                682.887, eps=0.007143737
Epoch 207: f=
                682.887, eps=0.007500924
Epoch 208: f=
                682.889, eps=0.003750462
Epoch 209: f=
                682.886, eps=0.003937985
Epoch 210: f=
                682.885, eps=0.004134885
Epoch 211: f=
                682.884, eps=0.004341629
Epoch 212: f=
                682.883, eps=0.004558710
Epoch 213: f=
                682.883, eps=0.004786646
Epoch 214: f=
                682.882, eps=0.005025978
Epoch 215: f=
                682.882, eps=0.005277277
Epoch 216: f=
                682.882, eps=0.005541141
Epoch 217: f=
                682.881, eps=0.005818198
Epoch 218: f=
                682.881, eps=0.002909099
Epoch 219: f=
                682.880, eps=0.003054554
Epoch 220: f=
                682.880, eps=0.003207282
Epoch 221: f=
                682.879, eps=0.003367646
Epoch 222: f=
                682.879, eps=0.003536028
```

```
Epoch 223: f=
                682.879, eps=0.003712829
Epoch 224: f=
                682.878, eps=0.003898471
Epoch 225: f=
                682.878, eps=0.004093394
Epoch 226: f=
                682.878, eps=0.004298064
Epoch 227: f=
                682.877, eps=0.004512967
Epoch 228: f=
                682.877, eps=0.004738616
Epoch 229: f=
                682.876, eps=0.004975546
Epoch 230: f=
                682.876, eps=0.005224324
Epoch 231: f=
                682.876, eps=0.005485540
Epoch 232: f=
                682.875, eps=0.005759817
                682.875, eps=0.006047808
Epoch 233: f=
Epoch 234: f=
                682.874, eps=0.006350198
                682.874, eps=0.006667708
Epoch 235: f=
Epoch 236: f=
                682.873, eps=0.007001093
                682.873, eps=0.007351148
Epoch 237: f=
Epoch 238: f=
                682.872, eps=0.007718705
Epoch 239: f=
                682.872, eps=0.008104641
Epoch 240: f=
                682.871, eps=0.008509873
Epoch 241: f=
                682.871, eps=0.008935366
Epoch 242: f=
                682.873, eps=0.004467683
Epoch 243: f=
                682.872, eps=0.004691067
Epoch 244: f=
                682.871, eps=0.004925621
Epoch 245: f=
                682.871, eps=0.005171902
Epoch 246: f=
                682.872, eps=0.002585951
Epoch 247: f=
                682.869, eps=0.002715248
Epoch 248: f=
                682.868, eps=0.002851011
Epoch 249: f=
                682.868, eps=0.002993561
Epoch 250: f=
                682.868, eps=0.003143239
Epoch 251: f=
                682.868, eps=0.003300401
Epoch 252: f=
                682.868, eps=0.003465421
Epoch 253: f=
                682.868, eps=0.003638693
Epoch 254: f=
                682.867, eps=0.003820627
Epoch 255: f=
                682.867, eps=0.004011659
                682.867, eps=0.004212241
Epoch 256: f=
Epoch 257: f=
                682.867, eps=0.004422854
Epoch 258: f=
                682.866, eps=0.004643996
Epoch 259: f=
                682.866, eps=0.004876196
Epoch 260: f=
                682.866, eps=0.005120006
Epoch 261: f=
                682.866, eps=0.005376006
Epoch 262: f=
                682.865, eps=0.005644806
Epoch 263: f=
                682.865, eps=0.005927047
Epoch 264: f=
                682.865, eps=0.006223399
Epoch 265: f=
                682.865, eps=0.006534569
Epoch 266: f=
                682.864, eps=0.006861297
Epoch 267: f=
                682.864, eps=0.007204362
Epoch 268: f=
                682.864, eps=0.007564580
                682.863, eps=0.007942809
Epoch 269: f=
Epoch 270: f=
                682.863, eps=0.008339950
```

```
Epoch 271: f=
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Epoch 272: f=
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Epoch 273: f=
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Epoch 274: f=
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Epoch 275: f=
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Epoch 276: f=
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Epoch 277: f=
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Epoch 278: f=
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Epoch 279: f=
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Epoch 280: f=
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Epoch 281: f=
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Epoch 282: f=
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Epoch 283: f=
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Epoch 284: f=
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                682.860, eps=0.003931555
Epoch 285: f=
Epoch 286: f=
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Epoch 287: f=
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Epoch 288: f=
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Epoch 289: f=
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Epoch 293: f=
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Epoch 294: f=
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Epoch 295: f=
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Epoch 296: f=
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Epoch 297: f=
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Epoch 298: f=
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Epoch 299: f=
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Epoch 300: f=
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Epoch 301: f=
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Epoch 302: f=
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Epoch 303: f=
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Epoch 304: f=
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Epoch 305: f=
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Epoch 306: f=
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Epoch 307: f=
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Epoch 308: f=
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Epoch 309: f=
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Epoch 310: f=
                682.856, eps=0.003018966
Epoch 311: f=
                682.856, eps=0.003169914
Epoch 312: f=
                682.856, eps=0.003328410
Epoch 313: f=
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Epoch 314: f=
                682.856, eps=0.003669572
Epoch 315: f=
                682.855, eps=0.003853051
Epoch 316: f=
                682.855, eps=0.004045703
Epoch 317: f=
                682.855, eps=0.004247988
Epoch 318: f=
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```

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Epoch 319: f=
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Epoch 320: f=
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Epoch 321: f=
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Epoch 322: f=
                682.855, eps=0.005421629
Epoch 323: f=
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Epoch 324: f=
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Epoch 325: f=
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Epoch 326: f=
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Epoch 327: f=
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Epoch 328: f=
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Epoch 329: f=
                682.854, eps=0.007628777
Epoch 330: f=
                682.854, eps=0.008010216
Epoch 331: f=
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Epoch 332: f=
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Epoch 333: f=
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Epoch 334: f=
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Epoch 335: f=
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Epoch 336: f=
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Epoch 337: f=
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Epoch 338: f=
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Epoch 339: f=
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Epoch 340: f=
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Epoch 341: f=
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Epoch 343: f=
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Epoch 344: f=
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Epoch 345: f=
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Epoch 346: f=
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Epoch 347: f=
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Epoch 348: f=
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Epoch 349: f=
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Epoch 350: f=
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Epoch 351: f=
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Epoch 352: f=
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Epoch 353: f=
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Epoch 354: f=
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Epoch 355: f=
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Epoch 356: f=
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Epoch 357: f=
                682.852, eps=0.006781358
Epoch 358: f=
                682.852, eps=0.007120426
Epoch 359: f=
                682.852, eps=0.007476448
Epoch 360: f=
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Epoch 361: f=
                682.852, eps=0.008242783
Epoch 362: f=
                682.852, eps=0.008654923
Epoch 363: f=
                682.852, eps=0.009087669
Epoch 364: f=
                682.852, eps=0.009542052
Epoch 365: f=
                682.852, eps=0.004771026
Epoch 366: f=
                682.852, eps=0.005009577
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Epoch 367: f=
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Epoch 368: f=
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Epoch 369: f=
                682.851, eps=0.002761530
Epoch 370: f=
                682.851, eps=0.002899606
Epoch 371: f=
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Epoch 372: f=
                682.851, eps=0.003196816
Epoch 373: f=
                682.851, eps=0.003356656
Epoch 374: f=
                682.851, eps=0.003524489
Epoch 375: f=
                682.851, eps=0.003700714
Epoch 376: f=
                682.851, eps=0.003885749
Epoch 377: f=
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Epoch 378: f=
                682.851, eps=0.004284039
Epoch 379: f=
                682.851, eps=0.004498241
Epoch 380: f=
                682.851, eps=0.004723153
Epoch 381: f=
                682.851, eps=0.004959310
Epoch 382: f=
                682.851, eps=0.005207276
Epoch 383: f=
                682.851, eps=0.005467640
Epoch 384: f=
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Epoch 385: f=
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Epoch 386: f=
                682.851, eps=0.006329476
Epoch 387: f=
                682.851, eps=0.006645950
Epoch 388: f=
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Epoch 389: f=
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Epoch 390: f=
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Epoch 391: f=
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Epoch 392: f=
                682.851, eps=0.008482104
Epoch 393: f=
                682.851, eps=0.008906209
Epoch 394: f=
                682.851, eps=0.009351519
Epoch 395: f=
                682.851, eps=0.009819095
Epoch 396: f=
                682.851, eps=0.010310050
Epoch 397: f=
                682.851, eps=0.005155025
Epoch 398: f=
                682.851, eps=0.002577512
Epoch 399: f=
                682.850, eps=0.002706388
Epoch 400: f=
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Epoch 401: f=
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Epoch 402: f=
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Epoch 403: f=
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Epoch 404: f=
                682.850, eps=0.003454113
Epoch 405: f=
                682.850, eps=0.003626819
Epoch 406: f=
                682.850, eps=0.003808160
Epoch 407: f=
                682.850, eps=0.003998568
Epoch 408: f=
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Epoch 409: f=
                682.850, eps=0.004408421
Epoch 410: f=
                682.850, eps=0.004628842
Epoch 411: f=
                682.850, eps=0.004860284
Epoch 412: f=
                682.850, eps=0.005103298
Epoch 413: f=
                682.850, eps=0.005358463
                682.850, eps=0.005626387
Epoch 414: f=
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Epoch 415: f=
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Epoch 416: f=
                682.850, eps=0.006203091
Epoch 417: f=
                682.850, eps=0.006513246
Epoch 418: f=
                682.850, eps=0.006838908
Epoch 419: f=
                682.850, eps=0.007180853
Epoch 420: f=
                682.850, eps=0.007539896
Epoch 421: f=
                682.850, eps=0.007916891
Epoch 422: f=
                682.850, eps=0.008312735
Epoch 423: f=
                682.850, eps=0.008728372
Epoch 424: f=
                682.850, eps=0.009164791
Epoch 425: f=
                682.850, eps=0.009623030
Epoch 426: f=
                682.850, eps=0.010104182
Epoch 427: f=
                682.850, eps=0.010609391
Epoch 428: f=
                682.850, eps=0.011139860
Epoch 429: f=
                682.850, eps=0.005569930
Epoch 430: f=
                682.850, eps=0.002784965
Epoch 431: f=
                682.850, eps=0.002924213
Epoch 432: f=
                682.850, eps=0.003070424
Epoch 433: f=
                682.850, eps=0.003223945
Epoch 434: f=
                682.850, eps=0.003385142
Epoch 435: f=
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Epoch 436: f=
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Epoch 437: f=
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Epoch 438: f=
                682.850, eps=0.004114662
Epoch 439: f=
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Epoch 440: f=
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Epoch 441: f=
                682.850, eps=0.004763235
Epoch 442: f=
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Epoch 443: f=
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Epoch 444: f=
                682.850, eps=0.005514040
Epoch 445: f=
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Epoch 446: f=
                682.850, eps=0.006079230
Epoch 447: f=
                682.850, eps=0.006383191
Epoch 448: f=
                682.850, eps=0.006702351
Epoch 449: f=
                682.850, eps=0.007037468
Epoch 450: f=
                682.850, eps=0.007389342
Epoch 451: f=
                682.850, eps=0.007758809
Epoch 452: f=
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Epoch 453: f=
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Epoch 454: f=
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Epoch 455: f=
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Epoch 456: f=
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Epoch 457: f=
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Epoch 458: f=
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                682.850, eps=0.002599386
Epoch 459: f=
Epoch 460: f=
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Epoch 461: f=
                682.850, eps=0.002865824
Epoch 462: f=
                682.850, eps=0.003009115
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Epoch 463: f=
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Epoch 464: f=
                682.850, eps=0.003317549
Epoch 465: f=
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Epoch 466: f=
                682.850, eps=0.003657598
Epoch 467: f=
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Epoch 468: f=
                682.850, eps=0.004032501
Epoch 469: f=
                682.850, eps=0.004234127
Epoch 470: f=
                682.850, eps=0.004445833
Epoch 471: f=
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Epoch 472: f=
                682.849, eps=0.004901531
Epoch 473: f=
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Epoch 474: f=
                682.849, eps=0.005403938
Epoch 475: f=
                682.849, eps=0.005674135
Epoch 476: f=
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Epoch 477: f=
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Epoch 478: f=
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Epoch 479: f=
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Epoch 480: f=
                682.849, eps=0.007241793
Epoch 481: f=
                682.849, eps=0.007603883
Epoch 482: f=
                682.849, eps=0.007984077
Epoch 483: f=
                682.849, eps=0.008383281
Epoch 484: f=
                682.849, eps=0.008802445
Epoch 485: f=
                682.849, eps=0.009242567
Epoch 486: f=
                682.849, eps=0.009704696
Epoch 487: f=
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                682.849, eps=0.010699427
Epoch 488: f=
Epoch 489: f=
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Epoch 490: f=
                682.849, eps=0.011796118
Epoch 491: f=
                682.849, eps=0.005898059
Epoch 492: f=
                682.849, eps=0.002949030
Epoch 493: f=
                682.849, eps=0.003096481
Epoch 494: f=
                682.849, eps=0.003251305
Epoch 495: f=
                682.849, eps=0.003413870
Epoch 496: f=
                682.849, eps=0.003584564
Epoch 497: f=
                682.849, eps=0.003763792
Epoch 498: f=
                682.849, eps=0.003951982
Epoch 499: f=
                682.849, eps=0.004149581
Result after 500 epochs: f=682.8492956819674
Epoch
        0: f=
               6703.331, eps=0.010000000
Epoch
        1: f=
               4550.363, eps=0.010500000
Epoch
        2: f=
               2842.373, eps=0.011025000
Epoch
        3: f=
               2014.048, eps=0.011576250
               1492.397, eps=0.012155063
Epoch
        4: f=
Epoch
        5: f=
               1224.571, eps=0.012762816
        6: f=
               1053.240, eps=0.013400956
Epoch
Epoch
        7: f=
                950.429, eps=0.014071004
Epoch
        8: f=
                906.709, eps=0.014774554
                952.738, eps=0.007387277
Epoch
        9: f=
```

```
Epoch 10: f=
                831.529, eps=0.007756641
Epoch
      11: f=
                818.434, eps=0.008144473
Epoch
      12: f=
                849.404, eps=0.004072237
Epoch
      13: f=
                763.185, eps=0.004275848
Epoch
      14: f=
                747.639, eps=0.004489641
Epoch
      15: f=
                740.861, eps=0.004714123
Epoch
      16: f=
                735.408, eps=0.004949829
Epoch 17: f=
                730.460, eps=0.005197320
Epoch 18: f=
                725.921, eps=0.005457186
Epoch 19: f=
                721.765, eps=0.005730046
                717.996, eps=0.006016548
Epoch
      20: f=
Epoch 21: f=
                714.616, eps=0.006317375
                711.667, eps=0.006633244
Epoch
      22: f=
Epoch 23: f=
                709.262, eps=0.006964906
Epoch 24: f=
                707.968, eps=0.007313152
Epoch 25: f=
                709.731, eps=0.003656576
Epoch 26: f=
                704.608, eps=0.003839405
Epoch 27: f=
                702.999, eps=0.004031375
Epoch 28: f=
                702.066, eps=0.004232944
Epoch
                701.292, eps=0.004444591
      29: f=
Epoch
      30: f=
                700.608, eps=0.004666820
Epoch 31: f=
                699.990, eps=0.004900161
Epoch 32: f=
                699.436, eps=0.005145169
Epoch 33: f=
                698.945, eps=0.005402428
                698.525, eps=0.005672549
Epoch 34: f=
Epoch 35: f=
                698.197, eps=0.005956177
Epoch 36: f=
                698.033, eps=0.006253986
Epoch 37: f=
                698.241, eps=0.003126993
Epoch 38: f=
                697.356, eps=0.003283342
Epoch 39: f=
                697.172, eps=0.003447510
Epoch 40: f=
                697.051, eps=0.003619885
Epoch
      41: f=
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Epoch 42: f=
                696.844, eps=0.003990923
Epoch 43: f=
                696.751, eps=0.004190469
Epoch 44: f=
                696.665, eps=0.004399993
Epoch 45: f=
                696.586, eps=0.004619993
Epoch 46: f=
                696.512, eps=0.004850992
Epoch 47: f=
                696.444, eps=0.005093542
Epoch 48: f=
                696.381, eps=0.005348219
Epoch 49: f=
                696.324, eps=0.005615630
Epoch 50: f=
                696.271, eps=0.005896411
Epoch 51: f=
                696.222, eps=0.006191232
      52: f=
                696.178, eps=0.006500794
Epoch
Epoch 53: f=
                696.138, eps=0.006825833
Epoch 54: f=
                696.106, eps=0.007167125
Epoch
      55: f=
                696.101, eps=0.007525481
Epoch 56: f=
                696.224, eps=0.003762741
                696.076, eps=0.003950878
Epoch 57: f=
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Epoch 58: f=
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Epoch 59: f=
                695.995, eps=0.004355843
Epoch
      60: f=
                695.974, eps=0.004573635
                695.957, eps=0.004802316
Epoch
      61: f=
Epoch 62: f=
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Epoch
      63: f=
                695.929, eps=0.005294554
Epoch
      64: f=
                695.921, eps=0.005559282
Epoch 65: f=
                695.924, eps=0.002779641
Epoch 66: f=
                695.877, eps=0.002918623
Epoch 67: f=
                695.868, eps=0.003064554
                695.860, eps=0.003217782
Epoch 68: f=
Epoch 69: f=
                695.852, eps=0.003378671
                695.843, eps=0.003547604
Epoch 70: f=
Epoch 71: f=
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Epoch 72: f=
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Epoch 73: f=
                695.817, eps=0.004106795
Epoch 74: f=
                695.808, eps=0.004312135
Epoch 75: f=
                695.799, eps=0.004527742
Epoch 76: f=
                695.789, eps=0.004754129
Epoch 77: f=
                695.779, eps=0.004991835
Epoch
      78: f=
                695.769, eps=0.005241427
Epoch 79: f=
                695.759, eps=0.005503499
Epoch 80: f=
                695.749, eps=0.005778674
Epoch 81: f=
                695.739, eps=0.006067607
Epoch 82: f=
                695.728, eps=0.006370988
Epoch 83: f=
                695.718, eps=0.006689537
                695.707, eps=0.007024014
Epoch 84: f=
Epoch 85: f=
                695.696, eps=0.007375214
Epoch 86: f=
                695.685, eps=0.007743975
Epoch 87: f=
                695.674, eps=0.008131174
Epoch 88: f=
                695.663, eps=0.008537733
Epoch 89: f=
                695.652, eps=0.008964619
Epoch 90: f=
                695.650, eps=0.009412850
                695.721, eps=0.004706425
Epoch 91: f=
Epoch 92: f=
                695.713, eps=0.004941746
Epoch 93: f=
                695.723, eps=0.002470873
Epoch 94: f=
                695.615, eps=0.002594417
Epoch 95: f=
                695.612, eps=0.002724138
Epoch 96: f=
                695.609, eps=0.002860345
Epoch 97: f=
                695.606, eps=0.003003362
Epoch 98: f=
                695.603, eps=0.003153530
Epoch 99: f=
                695.600, eps=0.003311206
                695.597, eps=0.003476767
Epoch 100: f=
Epoch 101: f=
                695.593, eps=0.003650605
Epoch 102: f=
                695.590, eps=0.003833135
Epoch 103: f=
                695.586, eps=0.004024792
Epoch 104: f=
                695.582, eps=0.004226032
Epoch 105: f=
                695.578, eps=0.004437333
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Epoch 106: f=
                695.574, eps=0.004659200
Epoch 107: f=
                695.570, eps=0.004892160
Epoch 108: f=
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Epoch 454: f=
                695.400, eps=0.008981791
Epoch 455: f=
                695.400, eps=0.009430880
                695.400, eps=0.004715440
Epoch 456: f=
Epoch 457: f=
                695.400, eps=0.004951212
Epoch 458: f=
                695.400, eps=0.005198773
Epoch 459: f=
                695.400, eps=0.002599386
Epoch 460: f=
                695.400, eps=0.002729356
Epoch 461: f=
                695.400, eps=0.002865824
Epoch 462: f=
                695.400, eps=0.003009115
Epoch 463: f=
                695.400, eps=0.003159570
Epoch 464: f=
                695.400, eps=0.003317549
Epoch 465: f=
                695.400, eps=0.003483426
Epoch 466: f=
                695.400, eps=0.003657598
Epoch 467: f=
                695.400, eps=0.003840478
Epoch 468: f=
                695.400, eps=0.004032501
Epoch 469: f=
                695.400, eps=0.004234127
Epoch 470: f=
                695.400, eps=0.004445833
                695.400, eps=0.004668125
Epoch 471: f=
Epoch 472: f=
                695.400, eps=0.004901531
Epoch 473: f=
                695.400, eps=0.005146607
Epoch 474: f=
                695.400, eps=0.005403938
Epoch 475: f=
                695.400, eps=0.005674135
Epoch 476: f=
                695.400, eps=0.005957841
Epoch 477: f=
                695.400, eps=0.006255733
Epoch 478: f=
                695.400, eps=0.006568520
Epoch 479: f=
                695.400, eps=0.006896946
Epoch 480: f=
                695.400, eps=0.007241793
Epoch 481: f=
                695.400, eps=0.007603883
Epoch 482: f=
                695.400, eps=0.007984077
Epoch 483: f=
                695.400, eps=0.008383281
Epoch 484: f=
                695.400, eps=0.008802445
Epoch 485: f=
                695.400, eps=0.009242567
                695.400, eps=0.009704696
Epoch 486: f=
Epoch 487: f=
                695.400, eps=0.010189930
Epoch 488: f=
                695.400, eps=0.005094965
Epoch 489: f=
                695.400, eps=0.002547483
```

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Epoch 490: f=
                695.400, eps=0.002674857
Epoch 491: f=
                695.400, eps=0.002808600
Epoch 492: f=
                695.400, eps=0.002949030
Epoch 493: f=
                695.400, eps=0.003096481
Epoch 494: f=
                695.400, eps=0.003251305
Epoch 495: f=
                695.400, eps=0.003413870
Epoch 496: f=
                695.400, eps=0.003584564
Epoch 497: f=
                695.400, eps=0.003763792
Epoch 498: f=
                695.400, eps=0.003951982
Epoch 499: f=
                695.400, eps=0.004149581
Result after 500 epochs: f=695.3995518029757
Epoch
        0: f=
               6736.893, eps=0.010000000
Epoch
        1: f=
               4717.013, eps=0.010500000
Epoch
        2: f=
               2926.106, eps=0.011025000
Epoch
        3: f=
               2045.068, eps=0.011576250
Epoch
        4: f=
               1501.277, eps=0.012155063
               1220.344, eps=0.012762816
Epoch
        5: f=
Epoch
        6: f=
               1043.506, eps=0.013400956
        7: f=
Epoch
                942.603, eps=0.014071004
                936.434, eps=0.014774554
Epoch
        8: f=
Epoch
        9: f=
               1212.410, eps=0.007387277
Epoch
      10: f=
                868.406, eps=0.007756641
Epoch
       11: f=
                838.963, eps=0.008144473
Epoch
       12: f=
                906.272, eps=0.004072237
Epoch
      13: f=
                775.845, eps=0.004275848
                749.536, eps=0.004489641
Epoch
      14: f=
Epoch
                741.223, eps=0.004714123
       15: f=
Epoch
       16: f=
                735.865, eps=0.004949829
Epoch
      17: f=
                731.367, eps=0.005197320
      18: f=
                727.447, eps=0.005457186
Epoch
Epoch
      19: f=
                724.017, eps=0.005730046
       20: f=
                721.118, eps=0.006016548
Epoch
Epoch
      21: f=
                718.839, eps=0.006317375
Epoch
       22: f=
                717.703, eps=0.006633244
       23: f=
Epoch
                719.040, eps=0.003316622
Epoch
       24: f=
                713.642, eps=0.003482453
Epoch
      25: f=
                712.405, eps=0.003656576
Epoch
      26: f=
                711.627, eps=0.003839405
Epoch
      27: f=
                710.958, eps=0.004031375
                710.354, eps=0.004232944
Epoch 28: f=
Epoch
      29: f=
                709.806, eps=0.004444591
Epoch
       30: f=
                709.312, eps=0.004666820
                708.870, eps=0.004900161
Epoch
       31: f=
Epoch
       32: f=
                708.477, eps=0.005145169
Epoch
       33: f=
                708.132, eps=0.005402428
Epoch
       34: f=
                707.832, eps=0.005672549
Epoch
       35: f=
                707.575, eps=0.005956177
                707.366, eps=0.006253986
Epoch
      36: f=
```

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Epoch 37: f=
                707.225, eps=0.006566685
Epoch 38: f=
                707.248, eps=0.003283342
Epoch 39: f=
                706.948, eps=0.003447510
                706.847, eps=0.003619885
Epoch 40: f=
Epoch 41: f=
                706.776, eps=0.003800879
                706.714, eps=0.003990923
Epoch 42: f=
Epoch 43: f=
                706.655, eps=0.004190469
Epoch 44: f=
                706.599, eps=0.004399993
Epoch 45: f=
                706.546, eps=0.004619993
Epoch 46: f=
                706.496, eps=0.004850992
Epoch 47: f=
                706.448, eps=0.005093542
Epoch 48: f=
                706.402, eps=0.005348219
Epoch 49: f=
                706.359, eps=0.005615630
Epoch 50: f=
                706.317, eps=0.005896411
Epoch 51: f=
                706.279, eps=0.006191232
Epoch 52: f=
                706.247, eps=0.006500794
Epoch 53: f=
                706.234, eps=0.006825833
                706.297, eps=0.003412917
Epoch 54: f=
Epoch 55: f=
                706.174, eps=0.003583562
Epoch 56: f=
                706.136, eps=0.003762741
Epoch
      57: f=
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Epoch 58: f=
                706.094, eps=0.004148421
Epoch 59: f=
                706.076, eps=0.004355843
Epoch 60: f=
                706.057, eps=0.004573635
                706.039, eps=0.004802316
Epoch 61: f=
Epoch 62: f=
                706.021, eps=0.005042432
Epoch
      63: f=
                706.003, eps=0.005294554
Epoch
      64: f=
                705.985, eps=0.005559282
Epoch 65: f=
                705.969, eps=0.005837246
Epoch 66: f=
                705.955, eps=0.006129108
Epoch 67: f=
                705.950, eps=0.006435563
Epoch 68: f=
                705.979, eps=0.003217782
Epoch 69: f=
                705.911, eps=0.003378671
Epoch 70: f=
                705.893, eps=0.003547604
Epoch 71: f=
                705.883, eps=0.003724984
Epoch 72: f=
                705.873, eps=0.003911234
Epoch 73: f=
                705.863, eps=0.004106795
Epoch 74: f=
                705.853, eps=0.004312135
Epoch 75: f=
                705.843, eps=0.004527742
Epoch 76: f=
                705.833, eps=0.004754129
Epoch 77: f=
                705.822, eps=0.004991835
Epoch 78: f=
                705.812, eps=0.005241427
Epoch 79: f=
                705.801, eps=0.005503499
Epoch 80: f=
                705.791, eps=0.005778674
Epoch 81: f=
                705.780, eps=0.006067607
Epoch
      82: f=
                705.770, eps=0.006370988
Epoch 83: f=
                705.761, eps=0.006689537
                705.758, eps=0.007024014
Epoch 84: f=
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```
Epoch 85: f=
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Epoch 86: f=
                705.743, eps=0.003687607
Epoch 87: f=
                705.730, eps=0.003871988
                705.722, eps=0.004065587
Epoch
      88: f=
Epoch 89: f=
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Epoch 90: f=
                705.710, eps=0.004482310
Epoch 91: f=
                705.704, eps=0.004706425
Epoch 92: f=
                705.698, eps=0.004941746
Epoch 93: f=
                705.692, eps=0.005188834
Epoch 94: f=
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                705.682, eps=0.005720689
Epoch 95: f=
Epoch 96: f=
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                705.679, eps=0.003003362
Epoch 97: f=
Epoch
      98: f=
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Epoch 99: f=
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Epoch 100: f=
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Epoch 101: f=
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Epoch 102: f=
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Epoch 103: f=
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Epoch 104: f=
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Epoch 105: f=
                705.641, eps=0.004437333
Epoch 106: f=
                705.637, eps=0.004659200
Epoch 107: f=
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Epoch 108: f=
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Epoch 109: f=
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                705.623, eps=0.005663287
Epoch 110: f=
Epoch 111: f=
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Epoch 112: f=
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Epoch 113: f=
                705.611, eps=0.006555962
Epoch 114: f=
                705.607, eps=0.006883760
Epoch 115: f=
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Epoch 116: f=
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Epoch 117: f=
                705.599, eps=0.007968813
Epoch 118: f=
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Epoch 119: f=
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Epoch 120: f=
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Epoch 121: f=
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Epoch 122: f=
                705.590, eps=0.004843071
Epoch 123: f=
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Epoch 124: f=
                705.589, eps=0.002542612
Epoch 125: f=
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Epoch 126: f=
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                705.578, eps=0.002943392
Epoch 127: f=
Epoch 128: f=
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Epoch 129: f=
                705.576, eps=0.003245089
Epoch 130: f=
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Epoch 131: f=
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Epoch 132: f=
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Epoch 133: f=
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Epoch 134: f=
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Epoch 135: f=
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                705.567, eps=0.004566166
Epoch 136: f=
Epoch 137: f=
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Epoch 138: f=
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Epoch 139: f=
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Epoch 140: f=
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Epoch 141: f=
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Epoch 142: f=
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Epoch 143: f=
Epoch 144: f=
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Epoch 145: f=
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Epoch 146: f=
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Epoch 147: f=
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Epoch 148: f=
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Epoch 149: f=
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Epoch 150: f=
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Epoch 151: f=
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Epoch 152: f=
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Epoch 153: f=
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Epoch 154: f=
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Epoch 155: f=
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Epoch 156: f=
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Epoch 158: f=
Epoch 159: f=
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Epoch 160: f=
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Epoch 161: f=
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Epoch 162: f=
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Epoch 163: f=
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Epoch 164: f=
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Epoch 165: f=
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Epoch 166: f=
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Epoch 167: f=
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Epoch 168: f=
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Epoch 169: f=
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Epoch 170: f=
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Epoch 171: f=
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Epoch 172: f=
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Epoch 173: f=
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Epoch 174: f=
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Epoch 175: f=
Epoch 176: f=
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Epoch 177: f=
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Epoch 178: f=
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Epoch 179: f=
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Epoch 180: f=
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Epoch 181: f=
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Epoch 182: f=
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Epoch 184: f=
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Epoch 185: f=
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Epoch 187: f=
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Epoch 193: f=
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Epoch 194: f=
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Epoch 198: f=
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Epoch 199: f=
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Epoch 200: f=
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Epoch 205: f=
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Epoch 213: f=
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Epoch 218: f=
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Epoch 219: f=
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Epoch 220: f=
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Epoch 221: f=
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Epoch 222: f=
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Epoch 223: f=
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Epoch 224: f=
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Epoch 225: f=
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Epoch 226: f=
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Epoch 227: f=
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Epoch 232: f=
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Epoch 244: f=
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Epoch 245: f=
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Epoch 263: f=
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Epoch 265: f=
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Epoch 267: f=
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Epoch 270: f=
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Epoch 271: f=
                705.529, eps=0.008756947
Epoch 272: f=
                705.529, eps=0.009194795
Epoch 273: f=
                705.529, eps=0.004597397
Epoch 274: f=
                705.529, eps=0.004827267
Epoch 275: f=
                705.529, eps=0.002413634
Epoch 276: f=
                705.529, eps=0.002534315
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Epoch 277: f=
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Epoch 278: f=
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Epoch 279: f=
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Epoch 280: f=
                705.528, eps=0.003080476
Epoch 281: f=
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Epoch 282: f=
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Epoch 283: f=
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Epoch 287: f=
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Epoch 288: f=
                705.528, eps=0.004551266
Epoch 289: f=
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Epoch 290: f=
                705.528, eps=0.005017771
Epoch 291: f=
                705.528, eps=0.005268660
Epoch 292: f=
                705.528, eps=0.005532093
Epoch 293: f=
                705.528, eps=0.005808697
Epoch 294: f=
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Epoch 295: f=
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Epoch 296: f=
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Epoch 297: f=
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Epoch 298: f=
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Epoch 299: f=
                705.528, eps=0.007784210
Epoch 300: f=
                705.528, eps=0.008173420
Epoch 301: f=
                705.528, eps=0.008582091
Epoch 302: f=
                705.528, eps=0.009011196
Epoch 303: f=
                705.528, eps=0.009461756
Epoch 304: f=
                705.528, eps=0.009934843
Epoch 305: f=
                705.528, eps=0.010431585
Epoch 306: f=
                705.528, eps=0.010953165
Epoch 307: f=
                705.528, eps=0.011500823
Epoch 308: f=
                705.528, eps=0.005750412
Epoch 309: f=
                705.528, eps=0.002875206
Epoch 310: f=
                705.528, eps=0.003018966
Epoch 311: f=
                705.528, eps=0.003169914
Epoch 312: f=
                705.528, eps=0.003328410
Epoch 313: f=
                705.528, eps=0.003494831
Epoch 314: f=
                705.528, eps=0.003669572
Epoch 315: f=
                705.528, eps=0.003853051
Epoch 316: f=
                705.528, eps=0.004045703
Epoch 317: f=
                705.528, eps=0.004247988
Epoch 318: f=
                705.528, eps=0.004460388
Epoch 319: f=
                705.528, eps=0.004683407
Epoch 320: f=
                705.528, eps=0.004917578
Epoch 321: f=
                705.528, eps=0.005163456
Epoch 322: f=
                705.528, eps=0.005421629
Epoch 323: f=
                705.528, eps=0.005692711
Epoch 324: f=
                705.528, eps=0.005977346
```

```
Epoch 325: f=
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Epoch 326: f=
                705.528, eps=0.006590024
Epoch 327: f=
                705.528, eps=0.006919525
Epoch 328: f=
                705.528, eps=0.007265502
Epoch 329: f=
                705.528, eps=0.007628777
Epoch 330: f=
                705.528, eps=0.008010216
Epoch 331: f=
                705.528, eps=0.004005108
Epoch 332: f=
                705.528, eps=0.004205363
Epoch 333: f=
                705.528, eps=0.004415631
Epoch 334: f=
                705.528, eps=0.004636413
Epoch 335: f=
                705.528, eps=0.004868234
Epoch 336: f=
                705.528, eps=0.005111645
Epoch 337: f=
                705.528, eps=0.002555823
Epoch 338: f=
                705.528, eps=0.002683614
Epoch 339: f=
                705.528, eps=0.002817794
Epoch 340: f=
                705.528, eps=0.002958684
Epoch 341: f=
                705.528, eps=0.003106618
Epoch 342: f=
                705.528, eps=0.003261949
Epoch 343: f=
                705.528, eps=0.003425047
Epoch 344: f=
                705.528, eps=0.003596299
Epoch 345: f=
                705.528, eps=0.003776114
Epoch 346: f=
                705.528, eps=0.003964920
Epoch 347: f=
                705.528, eps=0.004163166
Epoch 348: f=
                705.528, eps=0.004371324
Epoch 349: f=
                705.528, eps=0.004589890
Epoch 350: f=
                705.528, eps=0.004819385
Epoch 351: f=
                705.528, eps=0.005060354
Epoch 352: f=
                705.528, eps=0.005313372
Epoch 353: f=
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Epoch 354: f=
                705.528, eps=0.005857992
Epoch 355: f=
                705.528, eps=0.006150892
Epoch 356: f=
                705.528, eps=0.006458437
Epoch 357: f=
                705.528, eps=0.006781358
Epoch 358: f=
                705.528, eps=0.007120426
Epoch 359: f=
                705.528, eps=0.007476448
Epoch 360: f=
                705.528, eps=0.007850270
Epoch 361: f=
                705.528, eps=0.008242783
Epoch 362: f=
                705.528, eps=0.008654923
Epoch 363: f=
                705.528, eps=0.009087669
Epoch 364: f=
                705.528, eps=0.009542052
Epoch 365: f=
                705.528, eps=0.010019155
Epoch 366: f=
                705.528, eps=0.005009577
Epoch 367: f=
                705.528, eps=0.002504789
Epoch 368: f=
                705.528, eps=0.002630028
Epoch 369: f=
                705.528, eps=0.002761530
Epoch 370: f=
                705.528, eps=0.002899606
Epoch 371: f=
                705.528, eps=0.003044586
Epoch 372: f=
                705.528, eps=0.003196816
```

```
Epoch 373: f=
                705.528, eps=0.003356656
Epoch 374: f=
                705.528, eps=0.003524489
Epoch 375: f=
                705.528, eps=0.003700714
Epoch 376: f=
                705.528, eps=0.003885749
Epoch 377: f=
                705.528, eps=0.004080037
Epoch 378: f=
                705.528, eps=0.004284039
Epoch 379: f=
                705.528, eps=0.004498241
Epoch 380: f=
                705.528, eps=0.004723153
Epoch 381: f=
                705.528, eps=0.004959310
Epoch 382: f=
                705.528, eps=0.005207276
Epoch 383: f=
                705.528, eps=0.005467640
Epoch 384: f=
                705.528, eps=0.005741022
Epoch 385: f=
                705.528, eps=0.006028073
Epoch 386: f=
                705.528, eps=0.006329476
Epoch 387: f=
                705.528, eps=0.006645950
Epoch 388: f=
                705.528, eps=0.006978248
Epoch 389: f=
                705.528, eps=0.007327160
Epoch 390: f=
                705.528, eps=0.007693518
Epoch 391: f=
                705.528, eps=0.008078194
Epoch 392: f=
                705.528, eps=0.008482104
Epoch 393: f=
                705.528, eps=0.008906209
Epoch 394: f=
                705.528, eps=0.009351519
Epoch 395: f=
                705.528, eps=0.009819095
Epoch 396: f=
                705.528, eps=0.010310050
Epoch 397: f=
                705.528, eps=0.010825552
Epoch 398: f=
                705.528, eps=0.005412776
Epoch 399: f=
                705.528, eps=0.002706388
Epoch 400: f=
                705.528, eps=0.002841708
Epoch 401: f=
                705.528, eps=0.002983793
Epoch 402: f=
                705.528, eps=0.003132983
Epoch 403: f=
                705.528, eps=0.003289632
Epoch 404: f=
                705.528, eps=0.003454113
Epoch 405: f=
                705.528, eps=0.003626819
Epoch 406: f=
                705.528, eps=0.003808160
Epoch 407: f=
                705.528, eps=0.003998568
Epoch 408: f=
                705.528, eps=0.004198496
Epoch 409: f=
                705.528, eps=0.004408421
Epoch 410: f=
                705.528, eps=0.004628842
Epoch 411: f=
                705.528, eps=0.004860284
Epoch 412: f=
                705.528, eps=0.005103298
Epoch 413: f=
                705.528, eps=0.005358463
Epoch 414: f=
                705.528, eps=0.005626387
Epoch 415: f=
                705.528, eps=0.005907706
Epoch 416: f=
                705.528, eps=0.006203091
Epoch 417: f=
                705.528, eps=0.006513246
Epoch 418: f=
                705.528, eps=0.006838908
Epoch 419: f=
                705.528, eps=0.007180853
Epoch 420: f=
                705.528, eps=0.007539896
```

```
Epoch 421: f=
                705.528, eps=0.007916891
Epoch 422: f=
                705.528, eps=0.008312735
Epoch 423: f=
                705.528, eps=0.008728372
Epoch 424: f=
                705.528, eps=0.004364186
Epoch 425: f=
                705.528, eps=0.004582395
Epoch 426: f=
                705.528, eps=0.004811515
Epoch 427: f=
                705.528, eps=0.005052091
Epoch 428: f=
                705.528, eps=0.002526045
Epoch 429: f=
                705.528, eps=0.002652348
Epoch 430: f=
                705.528, eps=0.002784965
Epoch 431: f=
                705.528, eps=0.002924213
Epoch 432: f=
                705.528, eps=0.003070424
Epoch 433: f=
                705.528, eps=0.003223945
Epoch 434: f=
                705.528, eps=0.003385142
Epoch 435: f=
                705.528, eps=0.003554400
Epoch 436: f=
                705.528, eps=0.003732120
Epoch 437: f=
                705.528, eps=0.003918726
Epoch 438: f=
                705.528, eps=0.004114662
Epoch 439: f=
                705.528, eps=0.004320395
Epoch 440: f=
                705.528, eps=0.004536415
Epoch 441: f=
                705.528, eps=0.004763235
Epoch 442: f=
                705.528, eps=0.005001397
Epoch 443: f=
                705.528, eps=0.005251467
Epoch 444: f=
                705.528, eps=0.005514040
Epoch 445: f=
                705.528, eps=0.005789742
Epoch 446: f=
                705.528, eps=0.006079230
Epoch 447: f=
                705.528, eps=0.006383191
Epoch 448: f=
                705.528, eps=0.006702351
Epoch 449: f=
                705.528, eps=0.007037468
Epoch 450: f=
                705.528, eps=0.007389342
Epoch 451: f=
                705.528, eps=0.007758809
Epoch 452: f=
                705.528, eps=0.008146749
Epoch 453: f=
                705.528, eps=0.008554086
Epoch 454: f=
                705.528, eps=0.008981791
Epoch 455: f=
                705.528, eps=0.009430880
Epoch 456: f=
                705.528, eps=0.009902424
Epoch 457: f=
                705.528, eps=0.010397546
Epoch 458: f=
                705.528, eps=0.005198773
Epoch 459: f=
                705.528, eps=0.002599386
Epoch 460: f=
                705.528, eps=0.002729356
Epoch 461: f=
                705.528, eps=0.002865824
Epoch 462: f=
                705.528, eps=0.003009115
Epoch 463: f=
                705.528, eps=0.003159570
Epoch 464: f=
                705.528, eps=0.003317549
Epoch 465: f=
                705.528, eps=0.003483426
Epoch 466: f=
                705.528, eps=0.003657598
Epoch 467: f=
                705.528, eps=0.003840478
Epoch 468: f=
                705.528, eps=0.004032501
```

```
Epoch 469: f=
                705.528, eps=0.004234127
Epoch 470: f=
                705.528, eps=0.004445833
Epoch 471: f=
                705.528, eps=0.004668125
Epoch 472: f=
                705.528, eps=0.004901531
Epoch 473: f=
                705.528, eps=0.005146607
Epoch 474: f=
                705.528, eps=0.005403938
Epoch 475: f=
                705.528, eps=0.005674135
Epoch 476: f=
                705.528, eps=0.005957841
Epoch 477: f=
                705.528, eps=0.006255733
Epoch 478: f=
                705.528, eps=0.006568520
Epoch 479: f=
                705.528, eps=0.006896946
Epoch 480: f=
                705.528, eps=0.007241793
Epoch 481: f=
                705.528, eps=0.007603883
Epoch 482: f=
                705.528, eps=0.007984077
Epoch 483: f=
                705.528, eps=0.008383281
Epoch 484: f=
                705.528, eps=0.008802445
Epoch 485: f=
                705.528, eps=0.009242567
Epoch 486: f=
                705.528, eps=0.009704696
Epoch 487: f=
                705.528, eps=0.004852348
Epoch 488: f=
                705.528, eps=0.002426174
Epoch 489: f=
                705.528, eps=0.002547483
Epoch 490: f=
                705.528, eps=0.002674857
Epoch 491: f=
                705.528, eps=0.002808600
Epoch 492: f=
                705.528, eps=0.002949030
Epoch 493: f=
                705.528, eps=0.003096481
Epoch 494: f=
                705.528, eps=0.003251305
Epoch 495: f=
                705.528, eps=0.003413870
Epoch 496: f=
                705.528, eps=0.003584564
Epoch 497: f=
                705.528, eps=0.003763792
Epoch 498: f=
                705.528, eps=0.003951982
Epoch 499: f=
                705.528, eps=0.004149581
Result after 500 epochs: f=705.5283790137129
Epoch
        0: f=
               6770.454, eps=0.010000000
Epoch
        1: f=
               4883.652, eps=0.010500000
        2: f=
               3004.218, eps=0.011025000
Epoch
Epoch
        3: f=
               2068.167, eps=0.011576250
Epoch
        4: f=
               1503.254, eps=0.012155063
Epoch
        5: f=
               1210.041, eps=0.012762816
Epoch
        6: f=
               1030.827, eps=0.013400956
        7: f=
Epoch
                940.218, eps=0.014071004
Epoch
        8: f=
               1012.452, eps=0.007035502
Epoch
        9: f=
                991.542, eps=0.007387277
Epoch
       10: f=
                882.766, eps=0.007756641
Epoch
       11: f=
                936.365, eps=0.003878321
       12: f=
                774.532, eps=0.004072237
Epoch
Epoch
       13: f=
                762.350, eps=0.004275848
Epoch
       14: f=
                754.957, eps=0.004489641
                748.766, eps=0.004714123
Epoch
       15: f=
```

```
Epoch 16: f=
                743.375, eps=0.004949829
Epoch
      17: f=
                738.647, eps=0.005197320
Epoch
      18: f=
                734.513, eps=0.005457186
                730.931, eps=0.005730046
Epoch
      19: f=
Epoch 20: f=
                727.865, eps=0.006016548
Epoch
      21: f=
                725.286, eps=0.006317375
Epoch 22: f=
                723.184, eps=0.006633244
Epoch 23: f=
                721.640, eps=0.006964906
Epoch 24: f=
                721.108, eps=0.007313152
Epoch 25: f=
                723.326, eps=0.003656576
                719.090, eps=0.003839405
Epoch
      26: f=
Epoch 27: f=
                718.197, eps=0.004031375
                717.685, eps=0.004232944
Epoch 28: f=
Epoch 29: f=
                717.300, eps=0.004444591
Epoch 30: f=
                716.990, eps=0.004666820
Epoch 31: f=
                716.734, eps=0.004900161
Epoch 32: f=
                716.532, eps=0.005145169
Epoch 33: f=
                716.399, eps=0.005402428
Epoch 34: f=
                716.388, eps=0.005672549
Epoch
                716.647, eps=0.002836275
      35: f=
Epoch
      36: f=
                715.836, eps=0.002978088
Epoch 37: f=
                715.732, eps=0.003126993
Epoch 38: f=
                715.666, eps=0.003283342
Epoch 39: f=
                715.605, eps=0.003447510
                715.546, eps=0.003619885
Epoch 40: f=
Epoch 41: f=
                715.489, eps=0.003800879
Epoch 42: f=
                715.434, eps=0.003990923
Epoch 43: f=
                715.381, eps=0.004190469
Epoch 44: f=
                715.330, eps=0.004399993
Epoch 45: f=
                715.281, eps=0.004619993
Epoch 46: f=
                715.234, eps=0.004850992
Epoch 47: f=
                715.188, eps=0.005093542
Epoch 48: f=
                715.143, eps=0.005348219
Epoch 49: f=
                715.100, eps=0.005615630
Epoch 50: f=
                715.058, eps=0.005896411
Epoch 51: f=
                715.017, eps=0.006191232
Epoch 52: f=
                714.978, eps=0.006500794
Epoch 53: f=
                714.940, eps=0.006825833
Epoch 54: f=
                714.903, eps=0.007167125
Epoch 55: f=
                714.871, eps=0.007525481
Epoch 56: f=
                714.856, eps=0.007901755
Epoch 57: f=
                714.948, eps=0.003950878
                714.863, eps=0.004148421
Epoch 58: f=
Epoch 59: f=
                714.820, eps=0.004355843
Epoch 60: f=
                714.795, eps=0.004573635
Epoch
      61: f=
                714.780, eps=0.004802316
Epoch
      62: f=
                714.775, eps=0.005042432
                714.785, eps=0.002521216
Epoch 63: f=
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```
Epoch 64: f=
                714.695, eps=0.002647277
Epoch
      65: f=
                714.686, eps=0.002779641
Epoch
      66: f=
                714.678, eps=0.002918623
Epoch
       67: f=
                714.670, eps=0.003064554
Epoch
      68: f=
                714.662, eps=0.003217782
Epoch
      69: f=
                714.653, eps=0.003378671
Epoch
      70: f=
                714.645, eps=0.003547604
Epoch 71: f=
                714.636, eps=0.003724984
Epoch 72: f=
                714.627, eps=0.003911234
Epoch 73: f=
                714.618, eps=0.004106795
Epoch 74: f=
                714.609, eps=0.004312135
Epoch 75: f=
                714.599, eps=0.004527742
                714.590, eps=0.004754129
Epoch 76: f=
Epoch 77: f=
                714.581, eps=0.004991835
Epoch 78: f=
                714.571, eps=0.005241427
Epoch 79: f=
                714.562, eps=0.005503499
Epoch 80: f=
                714.553, eps=0.005778674
Epoch 81: f=
                714.543, eps=0.006067607
Epoch 82: f=
                714.534, eps=0.006370988
Epoch
      83: f=
                714.525, eps=0.006689537
Epoch
      84: f=
                714.516, eps=0.007024014
Epoch 85: f=
                714.507, eps=0.007375214
Epoch 86: f=
                714.498, eps=0.007743975
Epoch 87: f=
                714.490, eps=0.008131174
                714.482, eps=0.008537733
Epoch 88: f=
Epoch 89: f=
                714.474, eps=0.008964619
Epoch 90: f=
                714.466, eps=0.009412850
Epoch 91: f=
                714.462, eps=0.009883493
Epoch 92: f=
                714.495, eps=0.004941746
Epoch 93: f=
                714.507, eps=0.002470873
Epoch 94: f=
                714.447, eps=0.002594417
Epoch 95: f=
                714.445, eps=0.002724138
Epoch 96: f=
                714.443, eps=0.002860345
                714.441, eps=0.003003362
Epoch 97: f=
Epoch 98: f=
                714.440, eps=0.003153530
Epoch 99: f=
                714.438, eps=0.003311206
Epoch 100: f=
                714.436, eps=0.003476767
Epoch 101: f=
                714.434, eps=0.003650605
Epoch 102: f=
                714.432, eps=0.003833135
Epoch 103: f=
                714.431, eps=0.004024792
Epoch 104: f=
                714.429, eps=0.004226032
Epoch 105: f=
                714.427, eps=0.004437333
                714.425, eps=0.004659200
Epoch 106: f=
Epoch 107: f=
                714.423, eps=0.004892160
Epoch 108: f=
                714.421, eps=0.005136768
Epoch 109: f=
                714.419, eps=0.005393606
Epoch 110: f=
                714.417, eps=0.005663287
Epoch 111: f=
                714.415, eps=0.005946451
```

```
Epoch 112: f=
                714.413, eps=0.006243773
Epoch 113: f=
                714.411, eps=0.006555962
Epoch 114: f=
                714.409, eps=0.006883760
                714.407, eps=0.007227948
Epoch 115: f=
Epoch 116: f=
                714.406, eps=0.007589346
Epoch 117: f=
                714.404, eps=0.007968813
Epoch 118: f=
                714.402, eps=0.008367254
Epoch 119: f=
                714.400, eps=0.008785616
Epoch 120: f=
                714.399, eps=0.009224897
Epoch 121: f=
                714.397, eps=0.009686142
Epoch 122: f=
                714.397, eps=0.010170449
Epoch 123: f=
                714.409, eps=0.005085225
Epoch 124: f=
                714.416, eps=0.002542612
Epoch 125: f=
                714.394, eps=0.002669743
Epoch 126: f=
                714.393, eps=0.002803230
Epoch 127: f=
                714.393, eps=0.002943392
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Epoch 474: f=
                714.380, eps=0.005403938
Epoch 475: f=
                714.380, eps=0.005674135
Epoch 476: f=
                714.380, eps=0.005957841
Epoch 477: f=
                714.380, eps=0.006255733
Epoch 478: f=
                714.380, eps=0.006568520
Epoch 479: f=
                714.380, eps=0.006896946
Epoch 480: f=
                714.380, eps=0.007241793
Epoch 481: f=
                714.380, eps=0.007603883
Epoch 482: f=
                714.380, eps=0.007984077
Epoch 483: f=
                714.380, eps=0.008383281
Epoch 484: f=
                714.380, eps=0.008802445
Epoch 485: f=
                714.380, eps=0.009242567
Epoch 486: f=
                714.380, eps=0.009704696
Epoch 487: f=
                714.380, eps=0.010189930
Epoch 488: f=
                714.380, eps=0.010699427
Epoch 489: f=
                714.380, eps=0.011234398
Epoch 490: f=
                714.380, eps=0.005617199
Epoch 491: f=
                714.380, eps=0.002808600
Epoch 492: f=
                714.380, eps=0.002949030
Epoch 493: f=
                714.380, eps=0.003096481
Epoch 494: f=
                714.380, eps=0.003251305
                714.380, eps=0.003413870
Epoch 495: f=
```

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Epoch 496: f=
                714.380, eps=0.003584564
Epoch 497: f=
                714.380, eps=0.003763792
Epoch 498: f=
                714.380, eps=0.003951982
Epoch 499: f=
                714.380, eps=0.004149581
Result after 500 epochs: f=714.3804990993457
Epoch
        0: f=
               6804.016, eps=0.010000000
Epoch
        1: f=
               5050.300, eps=0.010500000
               3076.838, eps=0.011025000
Epoch
        2: f=
Epoch
        3: f=
               2083.891, eps=0.011576250
Epoch
        4: f=
               1499.379, eps=0.012155063
               1195.530, eps=0.012762816
Epoch
        5: f=
Epoch
        6: f=
               1019.030, eps=0.013400956
        7: f=
                953.913, eps=0.014071004
Epoch
Epoch
        8: f=
               1182.814, eps=0.007035502
               1289.182, eps=0.003517751
Epoch
        9: f=
Epoch
      10: f=
                932.116, eps=0.003693639
       11: f=
                816.850, eps=0.003878321
Epoch
Epoch
       12: f=
                787.315, eps=0.004072237
       13: f=
Epoch
                773.170, eps=0.004275848
Epoch
                763.643, eps=0.004489641
       14: f=
Epoch
       15: f=
                756.260, eps=0.004714123
Epoch
      16: f=
                750.180, eps=0.004949829
Epoch
      17: f=
                745.068, eps=0.005197320
Epoch 18: f=
                740.749, eps=0.005457186
Epoch
      19: f=
                737.116, eps=0.005730046
Epoch
      20: f=
                734.094, eps=0.006016548
Epoch
      21: f=
                731.615, eps=0.006317375
Epoch
      22: f=
                729.613, eps=0.006633244
Epoch
      23: f=
                728.024, eps=0.006964906
Epoch 24: f=
                726.785, eps=0.007313152
Epoch 25: f=
                725.842, eps=0.007678809
Epoch
      26: f=
                725.176, eps=0.008062750
Epoch 27: f=
                725.006, eps=0.008465887
Epoch
      28: f=
                727.355, eps=0.004232944
Epoch
      29: f=
                726.206, eps=0.004444591
Epoch
      30: f=
                725.706, eps=0.004666820
Epoch
      31: f=
                725.729, eps=0.002333410
Epoch
                723.693, eps=0.002450081
      32: f=
Epoch
      33: f=
                723.635, eps=0.002572585
Epoch 34: f=
                723.580, eps=0.002701214
Epoch
      35: f=
                723.526, eps=0.002836275
Epoch
      36: f=
                723.474, eps=0.002978088
      37: f=
Epoch
                723.424, eps=0.003126993
Epoch
      38: f=
                723.374, eps=0.003283342
Epoch
      39: f=
                723.326, eps=0.003447510
Epoch
      40: f=
                723.278, eps=0.003619885
Epoch
      41: f=
                723.232, eps=0.003800879
                723.187, eps=0.003990923
Epoch
      42: f=
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Epoch 43: f=
                723.143, eps=0.004190469
Epoch
      44: f=
                723.101, eps=0.004399993
Epoch
      45: f=
                723.059, eps=0.004619993
Epoch
      46: f=
                723.019, eps=0.004850992
Epoch 47: f=
                722.979, eps=0.005093542
Epoch
      48: f=
                722.941, eps=0.005348219
Epoch
      49: f=
                722.903, eps=0.005615630
Epoch 50: f=
                722.867, eps=0.005896411
Epoch 51: f=
                722.832, eps=0.006191232
Epoch 52: f=
                722.798, eps=0.006500794
      53: f=
                722.765, eps=0.006825833
Epoch
Epoch 54: f=
                722.733, eps=0.007167125
                722.703, eps=0.007525481
Epoch
      55: f=
Epoch
      56: f=
                722.674, eps=0.007901755
Epoch 57: f=
                722.646, eps=0.008296843
Epoch 58: f=
                722.620, eps=0.008711685
Epoch 59: f=
                722.595, eps=0.009147269
Epoch
      60: f=
                722.571, eps=0.009604633
Epoch 61: f=
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Epoch
      62: f=
                722.529, eps=0.010589108
Epoch
      63: f=
                722.511, eps=0.011118563
Epoch 64: f=
                722.509, eps=0.011674491
Epoch 65: f=
                722.778, eps=0.005837246
Epoch
      66: f=
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                722.536, eps=0.003064554
Epoch
      67: f=
                722.472, eps=0.003217782
Epoch 68: f=
Epoch
      69: f=
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Epoch
      70: f=
                722.456, eps=0.003547604
Epoch
      71: f=
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Epoch 72: f=
                722.448, eps=0.003911234
Epoch 73: f=
                722.445, eps=0.004106795
Epoch 74: f=
                722.441, eps=0.004312135
Epoch 75: f=
                722.438, eps=0.004527742
Epoch
      76: f=
                722.434, eps=0.004754129
Epoch
      77: f=
                722.431, eps=0.004991835
                722.427, eps=0.005241427
Epoch
      78: f=
Epoch
      79: f=
                722.424, eps=0.005503499
Epoch 80: f=
                722.421, eps=0.005778674
Epoch 81: f=
                722.418, eps=0.006067607
Epoch 82: f=
                722.416, eps=0.006370988
Epoch 83: f=
                722.416, eps=0.003185494
Epoch
      84: f=
                722.410, eps=0.003344768
                722.408, eps=0.003512007
Epoch
      85: f=
Epoch
      86: f=
                722.407, eps=0.003687607
Epoch
      87: f=
                722.405, eps=0.003871988
Epoch
      88: f=
                722.404, eps=0.004065587
Epoch
      89: f=
                722.402, eps=0.004268866
      90: f=
                722.401, eps=0.004482310
Epoch
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Epoch 91: f=
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Epoch 92: f=
                722.398, eps=0.004941746
Epoch
      93: f=
                722.396, eps=0.005188834
Epoch
      94: f=
                722.395, eps=0.005448275
Epoch
      95: f=
                722.393, eps=0.005720689
Epoch
      96: f=
                722.392, eps=0.006006724
Epoch
      97: f=
                722.391, eps=0.006307060
Epoch 98: f=
                722.390, eps=0.006622413
Epoch 99: f=
                722.392, eps=0.003311206
Epoch 100: f=
                722.388, eps=0.003476767
Epoch 101: f=
                722.387, eps=0.003650605
Epoch 102: f=
                722.386, eps=0.003833135
Epoch 103: f=
                722.385, eps=0.004024792
Epoch 104: f=
                722.385, eps=0.004226032
Epoch 105: f=
                722.384, eps=0.004437333
Epoch 106: f=
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Epoch 107: f=
                722.383, eps=0.004892160
Epoch 108: f=
                722.382, eps=0.005136768
Epoch 109: f=
                722.382, eps=0.005393606
Epoch 110: f=
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Epoch 111: f=
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Epoch 112: f=
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Epoch 113: f=
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Epoch 114: f=
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Epoch 115: f=
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Epoch 116: f=
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Epoch 117: f=
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Epoch 118: f=
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Epoch 119: f=
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Epoch 120: f=
                722.378, eps=0.004392808
Epoch 121: f=
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Epoch 122: f=
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Epoch 123: f=
                722.377, eps=0.005085225
Epoch 124: f=
                722.376, eps=0.005339486
Epoch 125: f=
                722.376, eps=0.005606460
Epoch 126: f=
                722.376, eps=0.005886783
Epoch 127: f=
                722.376, eps=0.006181122
Epoch 128: f=
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Epoch 129: f=
                722.375, eps=0.006814687
Epoch 130: f=
                722.375, eps=0.007155422
Epoch 131: f=
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Epoch 132: f=
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Epoch 133: f=
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Epoch 135: f=
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Epoch 136: f=
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Epoch 137: f=
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Epoch 138: f=
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Epoch 142: f=
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Epoch 143: f=
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Epoch 144: f=
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Epoch 145: f=
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Epoch 146: f=
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Epoch 147: f=
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Epoch 149: f=
Epoch 150: f=
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Epoch 152: f=
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Epoch 162: f=
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Epoch 163: f=
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Epoch 164: f=
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Epoch 166: f=
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Epoch 167: f=
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Epoch 169: f=
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Epoch 170: f=
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Epoch 171: f=
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Epoch 172: f=
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Epoch 173: f=
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Epoch 174: f=
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Epoch 175: f=
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Epoch 176: f=
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Epoch 182: f=
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Epoch 183: f=
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Epoch 184: f=
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Epoch 185: f=
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Epoch 186: f=
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Epoch 190: f=
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Epoch 191: f=
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Epoch 194: f=
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Epoch 195: f=
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Epoch 221: f=
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Epoch 232: f=
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Epoch 236: f=
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Epoch 281: f=
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Epoch 282: f=
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Epoch 284: f=
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Epoch 306: f=
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                722.372, eps=0.005476582
Epoch 307: f=
Epoch 308: f=
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Epoch 309: f=
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Epoch 310: f=
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Epoch 311: f=
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Epoch 312: f=
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Epoch 313: f=
                722.372, eps=0.007339144
Epoch 314: f=
                722.372, eps=0.007706101
Epoch 315: f=
                722.372, eps=0.008091406
Epoch 316: f=
                722.372, eps=0.008495977
Epoch 317: f=
                722.372, eps=0.008920776
Epoch 318: f=
                722.372, eps=0.004460388
Epoch 319: f=
                722.372, eps=0.004683407
Epoch 320: f=
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Epoch 321: f=
                722.372, eps=0.002458789
Epoch 322: f=
                722.372, eps=0.002581728
Epoch 323: f=
                722.372, eps=0.002710815
Epoch 324: f=
                722.372, eps=0.002846355
Epoch 325: f=
                722.372, eps=0.002988673
Epoch 326: f=
                722.372, eps=0.003138107
Epoch 327: f=
                722.372, eps=0.003295012
Epoch 328: f=
                722.372, eps=0.003459763
Epoch 329: f=
                722.372, eps=0.003632751
Epoch 330: f=
                722.372, eps=0.003814388
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Epoch 331: f=
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Epoch 332: f=
                722.372, eps=0.004205363
Epoch 333: f=
                722.372, eps=0.004415631
Epoch 334: f=
                722.372, eps=0.004636413
Epoch 335: f=
                722.372, eps=0.004868234
Epoch 336: f=
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Epoch 337: f=
                722.372, eps=0.005367228
Epoch 338: f=
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Epoch 339: f=
                722.372, eps=0.005917368
Epoch 340: f=
                722.372, eps=0.006213237
Epoch 341: f=
                722.372, eps=0.006523899
Epoch 342: f=
                722.372, eps=0.006850094
Epoch 343: f=
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Epoch 344: f=
                722.372, eps=0.007552228
Epoch 345: f=
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Epoch 346: f=
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Epoch 347: f=
                722.372, eps=0.008742648
Epoch 348: f=
                722.372, eps=0.009179781
Epoch 349: f=
                722.372, eps=0.009638770
Epoch 350: f=
                722.372, eps=0.004819385
Epoch 351: f=
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Epoch 352: f=
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Epoch 353: f=
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Epoch 354: f=
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Epoch 355: f=
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Epoch 356: f=
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Epoch 357: f=
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Epoch 358: f=
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Epoch 359: f=
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Epoch 360: f=
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Epoch 361: f=
                722.372, eps=0.003925135
Epoch 362: f=
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Epoch 363: f=
                722.372, eps=0.004327461
Epoch 364: f=
                722.372, eps=0.004543834
Epoch 365: f=
                722.372, eps=0.004771026
Epoch 366: f=
                722.372, eps=0.005009577
Epoch 367: f=
                722.372, eps=0.005260056
Epoch 368: f=
                722.372, eps=0.005523059
Epoch 369: f=
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Epoch 370: f=
                722.372, eps=0.006089173
Epoch 371: f=
                722.372, eps=0.006393631
Epoch 372: f=
                722.372, eps=0.006713313
Epoch 373: f=
                722.372, eps=0.007048978
Epoch 374: f=
                722.372, eps=0.007401427
Epoch 375: f=
                722.372, eps=0.007771499
Epoch 376: f=
                722.372, eps=0.008160074
Epoch 377: f=
                722.372, eps=0.008568077
Epoch 378: f=
                722.372, eps=0.008996481
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Epoch 379: f=
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Epoch 380: f=
                722.372, eps=0.009918621
Epoch 381: f=
                722.372, eps=0.004959310
Epoch 382: f=
                722.372, eps=0.002479655
Epoch 383: f=
                722.372, eps=0.002603638
Epoch 384: f=
                722.372, eps=0.002733820
Epoch 385: f=
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Epoch 386: f=
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Epoch 387: f=
                722.372, eps=0.003164738
Epoch 388: f=
                722.372, eps=0.003322975
Epoch 389: f=
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Epoch 390: f=
                722.372, eps=0.003663580
Epoch 391: f=
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Epoch 392: f=
                722.372, eps=0.004039097
Epoch 393: f=
                722.372, eps=0.004241052
Epoch 394: f=
                722.372, eps=0.004453104
Epoch 395: f=
                722.372, eps=0.004675760
Epoch 396: f=
                722.372, eps=0.004909548
Epoch 397: f=
                722.372, eps=0.005155025
Epoch 398: f=
                722.372, eps=0.005412776
Epoch 399: f=
                722.372, eps=0.005683415
Epoch 400: f=
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Epoch 401: f=
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Epoch 402: f=
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Epoch 403: f=
                722.372, eps=0.006908226
Epoch 404: f=
                722.372, eps=0.007253638
Epoch 405: f=
                722.372, eps=0.007616320
Epoch 406: f=
                722.372, eps=0.007997136
Epoch 407: f=
                722.372, eps=0.008396992
Epoch 408: f=
                722.372, eps=0.008816842
Epoch 409: f=
                722.372, eps=0.009257684
Epoch 410: f=
                722.372, eps=0.009720568
Epoch 411: f=
                722.372, eps=0.004860284
Epoch 412: f=
                722.372, eps=0.002430142
Epoch 413: f=
                722.372, eps=0.002551649
Epoch 414: f=
                722.372, eps=0.002679232
Epoch 415: f=
                722.372, eps=0.002813193
Epoch 416: f=
                722.372, eps=0.002953853
Epoch 417: f=
                722.372, eps=0.003101546
Epoch 418: f=
                722.372, eps=0.003256623
Epoch 419: f=
                722.372, eps=0.003419454
Epoch 420: f=
                722.372, eps=0.003590427
Epoch 421: f=
                722.372, eps=0.003769948
Epoch 422: f=
                722.372, eps=0.003958445
Epoch 423: f=
                722.372, eps=0.004156368
Epoch 424: f=
                722.372, eps=0.004364186
Epoch 425: f=
                722.372, eps=0.004582395
Epoch 426: f=
                722.372, eps=0.004811515
```

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Epoch 427: f=
                722.372, eps=0.005052091
Epoch 428: f=
                722.372, eps=0.005304695
Epoch 429: f=
                722.372, eps=0.005569930
Epoch 430: f=
                722.372, eps=0.005848427
Epoch 431: f=
                722.372, eps=0.006140848
Epoch 432: f=
                722.372, eps=0.006447890
Epoch 433: f=
                722.372, eps=0.006770285
Epoch 434: f=
                722.372, eps=0.007108799
Epoch 435: f=
                722.372, eps=0.007464239
Epoch 436: f=
                722.372, eps=0.007837451
Epoch 437: f=
                722.372, eps=0.008229324
Epoch 438: f=
                722.372, eps=0.008640790
Epoch 439: f=
                722.372, eps=0.009072829
Epoch 440: f=
                722.372, eps=0.009526471
Epoch 441: f=
                722.372, eps=0.004763235
Epoch 442: f=
                722.372, eps=0.002381618
Epoch 443: f=
                722.372, eps=0.002500699
Epoch 444: f=
                722.372, eps=0.002625734
Epoch 445: f=
                722.372, eps=0.002757020
Epoch 446: f=
                722.372, eps=0.002894871
Epoch 447: f=
                722.372, eps=0.003039615
Epoch 448: f=
                722.372, eps=0.003191596
Epoch 449: f=
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Epoch 450: f=
                722.372, eps=0.003518734
Epoch 451: f=
                722.372, eps=0.003694671
Epoch 452: f=
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Epoch 453: f=
                722.372, eps=0.004073375
Epoch 454: f=
                722.372, eps=0.004277043
Epoch 455: f=
                722.372, eps=0.004490895
Epoch 456: f=
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Epoch 457: f=
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Epoch 458: f=
                722.372, eps=0.005198773
Epoch 459: f=
                722.372, eps=0.005458711
Epoch 460: f=
                722.372, eps=0.005731647
Epoch 461: f=
                722.372, eps=0.006018229
Epoch 462: f=
                722.372, eps=0.006319141
Epoch 463: f=
                722.372, eps=0.006635098
Epoch 464: f=
                722.372, eps=0.006966853
Epoch 465: f=
                722.372, eps=0.007315195
Epoch 466: f=
                722.372, eps=0.007680955
Epoch 467: f=
                722.372, eps=0.008065003
Epoch 468: f=
                722.372, eps=0.008468253
Epoch 469: f=
                722.372, eps=0.008891666
Epoch 470: f=
                722.372, eps=0.009336249
Epoch 471: f=
                722.372, eps=0.009803061
Epoch 472: f=
                722.372, eps=0.010293215
Epoch 473: f=
                722.372, eps=0.010807875
                722.372, eps=0.005403938
Epoch 474: f=
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Epoch 475: f=
                722.372, eps=0.002701969
Epoch 476: f=
                722.372, eps=0.002837067
Epoch 477: f=
                722.372, eps=0.002978921
Epoch 478: f=
                722.372, eps=0.003127867
Epoch 479: f=
                722.372, eps=0.003284260
Epoch 480: f=
                722.372, eps=0.003448473
Epoch 481: f=
                722.372, eps=0.003620897
Epoch 482: f=
                722.372, eps=0.003801941
Epoch 483: f=
                722.372, eps=0.003992039
Epoch 484: f=
                722.372, eps=0.004191640
                722.372, eps=0.004401222
Epoch 485: f=
Epoch 486: f=
                722.372, eps=0.004621284
Epoch 487: f=
                722.372, eps=0.004852348
Epoch 488: f=
                722.372, eps=0.005094965
                722.372, eps=0.005349713
Epoch 489: f=
Epoch 490: f=
                722.372, eps=0.005617199
Epoch 491: f=
                722.372, eps=0.005898059
Epoch 492: f=
                722.372, eps=0.006192962
Epoch 493: f=
                722.372, eps=0.006502610
Epoch 494: f=
                722.372, eps=0.006827741
Epoch 495: f=
                722.372, eps=0.007169128
Epoch 496: f=
                722.372, eps=0.007527584
Epoch 497: f=
                722.372, eps=0.003763792
Epoch 498: f=
                722.372, eps=0.003951982
                722.372, eps=0.004149581
Epoch 499: f=
Result after 500 epochs: f=722.3720587338794
Epoch
               6971.823, eps=0.010000000
        0: f=
Epoch
        1: f=
               5884.379, eps=0.010500000
Epoch
        2: f=
               3362.081, eps=0.011025000
        3: f=
               2071.367, eps=0.011576250
Epoch
Epoch
        4: f=
               1422.221, eps=0.012155063
               1117.981, eps=0.012762816
Epoch
        5: f=
Epoch
        6: f=
               1121.186, eps=0.006381408
        7: f=
Epoch
               1103.258, eps=0.006700478
        8: f=
                912.910, eps=0.007035502
Epoch
Epoch
        9: f=
                960.266, eps=0.003517751
Epoch
       10: f=
                802.075, eps=0.003693639
Epoch
       11: f=
                788.727, eps=0.003878321
Epoch
       12: f=
                780.836, eps=0.004072237
Epoch
       13: f=
                774.777, eps=0.004275848
Epoch
       14: f=
                770.021, eps=0.004489641
Epoch
       15: f=
                766.302, eps=0.004714123
                763.437, eps=0.004949829
Epoch
       16: f=
Epoch
       17: f=
                761.272, eps=0.005197320
                759.693, eps=0.005457186
Epoch
       18: f=
Epoch
       19: f=
                758.642, eps=0.005730046
Epoch
       20: f=
                758.257, eps=0.006016548
                759.378, eps=0.003008274
Epoch
      21: f=
```

```
Epoch 22: f=
                757.011, eps=0.003158688
Epoch 23: f=
                756.515, eps=0.003316622
Epoch
      24: f=
                756.267, eps=0.003482453
                756.087, eps=0.003656576
Epoch
      25: f=
Epoch 26: f=
                755.936, eps=0.003839405
                755.806, eps=0.004031375
Epoch
      27: f=
Epoch
      28: f=
                755.692, eps=0.004232944
Epoch 29: f=
                755.591, eps=0.004444591
Epoch 30: f=
                755.503, eps=0.004666820
Epoch 31: f=
                755.425, eps=0.004900161
      32: f=
                755.361, eps=0.005145169
Epoch
Epoch 33: f=
                755.314, eps=0.005402428
Epoch
      34: f=
                755.306, eps=0.005672549
Epoch 35: f=
                755.414, eps=0.002836275
Epoch 36: f=
                755.180, eps=0.002978088
Epoch 37: f=
                755.134, eps=0.003126993
Epoch 38: f=
                755.109, eps=0.003283342
Epoch 39: f=
                755.088, eps=0.003447510
Epoch 40: f=
                755.068, eps=0.003619885
Epoch 41: f=
                755.049, eps=0.003800879
Epoch
      42: f=
                755.031, eps=0.003990923
Epoch 43: f=
                755.014, eps=0.004190469
Epoch 44: f=
                754.998, eps=0.004399993
Epoch 45: f=
                754.983, eps=0.004619993
Epoch 46: f=
                754.969, eps=0.004850992
Epoch 47: f=
                754.956, eps=0.005093542
Epoch
      48: f=
                754.944, eps=0.005348219
Epoch
      49: f=
                754.933, eps=0.005615630
Epoch 50: f=
                754.924, eps=0.005896411
Epoch 51: f=
                754.921, eps=0.006191232
Epoch 52: f=
                754.937, eps=0.003095616
Epoch 53: f=
                754.908, eps=0.003250397
Epoch 54: f=
                754.899, eps=0.003412917
                754.894, eps=0.003583562
Epoch 55: f=
      56: f=
Epoch
                754.890, eps=0.003762741
Epoch 57: f=
                754.887, eps=0.003950878
Epoch 58: f=
                754.883, eps=0.004148421
Epoch 59: f=
                754.881, eps=0.004355843
Epoch 60: f=
                754.878, eps=0.004573635
Epoch 61: f=
                754.875, eps=0.004802316
Epoch 62: f=
                754.873, eps=0.005042432
Epoch
      63: f=
                754.871, eps=0.005294554
                754.871, eps=0.005559282
Epoch
      64: f=
Epoch 65: f=
                754.875, eps=0.002779641
Epoch
      66: f=
                754.866, eps=0.002918623
Epoch
      67: f=
                754.864, eps=0.003064554
Epoch
      68: f=
                754.863, eps=0.003217782
                754.863, eps=0.003378671
Epoch
      69: f=
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Epoch 70: f=
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Epoch
      71: f=
                754.861, eps=0.003724984
Epoch
      72: f=
                754.860, eps=0.003911234
Epoch
      73: f=
                754.860, eps=0.004106795
Epoch
      74: f=
                754.859, eps=0.004312135
Epoch
      75: f=
                754.858, eps=0.004527742
Epoch
      76: f=
                754.858, eps=0.004754129
Epoch
      77: f=
                754.857, eps=0.004991835
Epoch 78: f=
                754.857, eps=0.005241427
Epoch 79: f=
                754.856, eps=0.005503499
                754.856, eps=0.005778674
Epoch
      80: f=
Epoch 81: f=
                754.855, eps=0.006067607
Epoch
      82: f=
                754.855, eps=0.006370988
Epoch
      83: f=
                754.856, eps=0.003185494
Epoch 84: f=
                754.855, eps=0.003344768
Epoch 85: f=
                754.854, eps=0.003512007
Epoch 86: f=
                754.854, eps=0.003687607
Epoch
      87: f=
                754.854, eps=0.003871988
Epoch 88: f=
                754.854, eps=0.004065587
Epoch
                754.854, eps=0.004268866
      89: f=
Epoch
      90: f=
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Epoch 91: f=
                754.854, eps=0.004706425
Epoch 92: f=
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Epoch 93: f=
                754.853, eps=0.005188834
Epoch 94: f=
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Epoch 95: f=
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Epoch
      96: f=
                754.853, eps=0.002860345
Epoch
      97: f=
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Epoch
      98: f=
                754.853, eps=0.003153530
Epoch 99: f=
                754.853, eps=0.003311206
Epoch 100: f=
                754.853, eps=0.003476767
Epoch 101: f=
                754.853, eps=0.003650605
Epoch 102: f=
                754.853, eps=0.003833135
Epoch 103: f=
                754.853, eps=0.004024792
Epoch 104: f=
                754.853, eps=0.004226032
Epoch 105: f=
                754.853, eps=0.004437333
Epoch 106: f=
                754.853, eps=0.004659200
Epoch 107: f=
                754.853, eps=0.004892160
Epoch 108: f=
                754.853, eps=0.005136768
Epoch 109: f=
                754.853, eps=0.005393606
Epoch 110: f=
                754.853, eps=0.005663287
Epoch 111: f=
                754.853, eps=0.005946451
Epoch 112: f=
                754.853, eps=0.006243773
Epoch 113: f=
                754.853, eps=0.006555962
Epoch 114: f=
                754.853, eps=0.006883760
Epoch 115: f=
                754.853, eps=0.007227948
Epoch 116: f=
                754.853, eps=0.003613974
Epoch 117: f=
                754.853, eps=0.003794673
```

```
Epoch 118: f=
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Epoch 119: f=
                754.852, eps=0.004183627
Epoch 120: f=
                754.852, eps=0.004392808
Epoch 121: f=
                754.852, eps=0.004612449
Epoch 122: f=
                754.852, eps=0.002306224
Epoch 123: f=
                754.852, eps=0.002421535
Epoch 124: f=
                754.852, eps=0.002542612
Epoch 125: f=
                754.852, eps=0.002669743
Epoch 126: f=
                754.852, eps=0.002803230
Epoch 127: f=
                754.852, eps=0.002943392
Epoch 128: f=
                754.852, eps=0.003090561
Epoch 129: f=
                754.852, eps=0.003245089
Epoch 130: f=
                754.852, eps=0.003407344
Epoch 131: f=
                754.852, eps=0.003577711
Epoch 132: f=
                754.852, eps=0.003756596
Epoch 133: f=
                754.852, eps=0.003944426
Epoch 134: f=
                754.852, eps=0.004141647
Epoch 135: f=
                754.852, eps=0.004348730
Epoch 136: f=
                754.852, eps=0.004566166
Epoch 137: f=
                754.852, eps=0.004794475
Epoch 138: f=
                754.852, eps=0.005034198
Epoch 139: f=
                754.852, eps=0.005285908
Epoch 140: f=
                754.852, eps=0.005550204
Epoch 141: f=
                754.852, eps=0.005827714
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Epoch 496: f=
                754.852, eps=0.000000000
Epoch 497: f=
                754.852, eps=0.000000000
Epoch 498: f=
                754.852, eps=0.000000000
Epoch 499: f=
                754.852, eps=0.000000000
Result after 500 epochs: f=754.8524204027967
        0: f=
               7307.438, eps=0.010000000
Epoch
```

```
Epoch
               7566.155, eps=0.005000000
        1: f=
Epoch
        2: f=
               5325.636, eps=0.005250000
               3761.037, eps=0.005512500
Epoch
        3: f=
               2648.710, eps=0.005788125
Epoch
        4: f=
Epoch
        5: f=
               1878.665, eps=0.006077531
               1406.862, eps=0.006381408
Epoch
        6: f=
Epoch
        7: f=
               1127.193, eps=0.006700478
Epoch
        8: f=
                964.727, eps=0.007035502
Epoch
        9: f=
                882.554, eps=0.007387277
Epoch
      10: f=
                875.652, eps=0.007756641
               1024.660, eps=0.003878321
Epoch
       11: f=
Epoch
       12: f=
                834.536, eps=0.004072237
                819.226, eps=0.004275848
Epoch
       13: f=
Epoch
       14: f=
                817.127, eps=0.004489641
Epoch
      15: f=
                821.922, eps=0.002244820
Epoch
      16: f=
                804.290, eps=0.002357061
Epoch 17: f=
                803.780, eps=0.002474914
Epoch
      18: f=
                803.425, eps=0.002598660
Epoch
      19: f=
                803.142, eps=0.002728593
Epoch
      20: f=
                802.913, eps=0.002865023
Epoch
      21: f=
                802.727, eps=0.003008274
Epoch
      22: f=
                802.576, eps=0.003158688
Epoch 23: f=
                802.452, eps=0.003316622
Epoch 24: f=
                802.351, eps=0.003482453
                802.269, eps=0.003656576
Epoch
      25: f=
Epoch 26: f=
                802.201, eps=0.003839405
Epoch
      27: f=
                802.145, eps=0.004031375
Epoch
      28: f=
                802.099, eps=0.004232944
Epoch
      29: f=
                802.062, eps=0.004444591
Epoch
      30: f=
                802.031, eps=0.004666820
Epoch 31: f=
                802.005, eps=0.004900161
Epoch
      32: f=
                801.985, eps=0.005145169
Epoch 33: f=
                801.968, eps=0.005402428
Epoch
      34: f=
                801.955, eps=0.005672549
       35: f=
Epoch
                801.945, eps=0.005956177
Epoch
      36: f=
                801.937, eps=0.006253986
Epoch
      37: f=
                801.931, eps=0.006566685
Epoch
                801.927, eps=0.006895019
      38: f=
Epoch
      39: f=
                801.932, eps=0.003447510
      40: f=
Epoch
                801.927, eps=0.003619885
Epoch
      41: f=
                801.925, eps=0.003800879
Epoch
      42: f=
                801.923, eps=0.003990923
                801.924, eps=0.001995462
Epoch
      43: f=
Epoch
      44: f=
                801.917, eps=0.002095235
Epoch
      45: f=
                801.917, eps=0.002199996
Epoch
      46: f=
                801.916, eps=0.002309996
Epoch
      47: f=
                801.916, eps=0.002425496
                801.916, eps=0.002546771
Epoch
      48: f=
```

```
Epoch 49: f=
                801.915, eps=0.002674109
Epoch 50: f=
                801.915, eps=0.002807815
Epoch 51: f=
                801.915, eps=0.002948206
                801.914, eps=0.003095616
Epoch
      52: f=
Epoch 53: f=
                801.914, eps=0.003250397
Epoch 54: f=
                801.914, eps=0.003412917
Epoch 55: f=
                801.914, eps=0.003583562
Epoch 56: f=
                801.914, eps=0.003762741
Epoch 57: f=
                801.914, eps=0.003950878
Epoch 58: f=
                801.913, eps=0.004148421
Epoch 59: f=
                801.913, eps=0.004355843
Epoch 60: f=
                801.913, eps=0.004573635
Epoch
                801.913, eps=0.004802316
      61: f=
Epoch
      62: f=
                801.913, eps=0.005042432
Epoch 63: f=
                801.913, eps=0.005294554
Epoch 64: f=
                801.913, eps=0.005559282
Epoch 65: f=
                801.913, eps=0.005837246
Epoch
      66: f=
                801.913, eps=0.006129108
Epoch 67: f=
                801.913, eps=0.006435563
Epoch
                801.913, eps=0.006757341
      68: f=
Epoch
      69: f=
                801.913, eps=0.007095208
Epoch 70: f=
                801.913, eps=0.007449969
Epoch 71: f=
                801.913, eps=0.007822467
Epoch 72: f=
                801.913, eps=0.008213591
Epoch 73: f=
                801.913, eps=0.008624270
Epoch 74: f=
                801.913, eps=0.004312135
Epoch 75: f=
                801.913, eps=0.002156068
Epoch 76: f=
                801.913, eps=0.002263871
Epoch 77: f=
                801.913, eps=0.002377064
Epoch 78: f=
                801.913, eps=0.002495918
Epoch 79: f=
                801.913, eps=0.002620714
Epoch 80: f=
                801.913, eps=0.002751749
Epoch 81: f=
                801.913, eps=0.002889337
Epoch
      82: f=
                801.913, eps=0.003033804
Epoch
      83: f=
                801.913, eps=0.003185494
Epoch 84: f=
                801.913, eps=0.003344768
Epoch 85: f=
                801.913, eps=0.003512007
Epoch 86: f=
                801.913, eps=0.003687607
Epoch 87: f=
                801.913, eps=0.003871988
Epoch 88: f=
                801.913, eps=0.004065587
Epoch 89: f=
                801.913, eps=0.004268866
Epoch
      90: f=
                801.913, eps=0.004482310
Epoch
      91: f=
                801.913, eps=0.004706425
Epoch
      92: f=
                801.913, eps=0.004941746
Epoch 93: f=
                801.913, eps=0.005188834
Epoch
      94: f=
                801.913, eps=0.005448275
Epoch 95: f=
                801.913, eps=0.005720689
Epoch 96: f=
                801.913, eps=0.006006724
```

```
Epoch 97: f=
                801.913, eps=0.006307060
Epoch 98: f=
                801.913, eps=0.006622413
Epoch 99: f=
                801.913, eps=0.006953533
Epoch 100: f=
                801.913, eps=0.003476767
Epoch 101: f=
                801.913, eps=0.003650605
Epoch 102: f=
                801.913, eps=0.003833135
Epoch 103: f=
                801.913, eps=0.004024792
Epoch 104: f=
                801.913, eps=0.004226032
Epoch 105: f=
                801.913, eps=0.002113016
Epoch 106: f=
                801.913, eps=0.002218667
Epoch 107: f=
                801.913, eps=0.002329600
Epoch 108: f=
                801.913, eps=0.002446080
                801.913, eps=0.002568384
Epoch 109: f=
Epoch 110: f=
                801.913, eps=0.002696803
Epoch 111: f=
                801.913, eps=0.002831643
Epoch 112: f=
                801.913, eps=0.002973225
Epoch 113: f=
                801.913, eps=0.003121887
Epoch 114: f=
                801.913, eps=0.003277981
Epoch 115: f=
                801.913, eps=0.003441880
Epoch 116: f=
                801.913, eps=0.003613974
Epoch 117: f=
                801.913, eps=0.003794673
Epoch 118: f=
                801.913, eps=0.003984406
Epoch 119: f=
                801.913, eps=0.004183627
Epoch 120: f=
                801.913, eps=0.004392808
Epoch 121: f=
                801.913, eps=0.004612449
                801.913, eps=0.004843071
Epoch 122: f=
Epoch 123: f=
                801.913, eps=0.005085225
Epoch 124: f=
                801.913, eps=0.005339486
Epoch 125: f=
                801.913, eps=0.005606460
Epoch 126: f=
                801.913, eps=0.005886783
Epoch 127: f=
                801.913, eps=0.006181122
Epoch 128: f=
                801.913, eps=0.006490178
Epoch 129: f=
                801.913, eps=0.006814687
Epoch 130: f=
                801.913, eps=0.007155422
Epoch 131: f=
                801.913, eps=0.007513193
Epoch 132: f=
                801.913, eps=0.003756596
Epoch 133: f=
                801.913, eps=0.003944426
Epoch 134: f=
                801.913, eps=0.001972213
Epoch 135: f=
                801.913, eps=0.002070824
Epoch 136: f=
                801.913, eps=0.002174365
Epoch 137: f=
                801.913, eps=0.002283083
Epoch 138: f=
                801.913, eps=0.002397237
                801.913, eps=0.002517099
Epoch 139: f=
Epoch 140: f=
                801.913, eps=0.002642954
Epoch 141: f=
                801.913, eps=0.002775102
Epoch 142: f=
                801.913, eps=0.002913857
Epoch 143: f=
                801.913, eps=0.003059550
Epoch 144: f=
                801.913, eps=0.003212527
```

```
Epoch 145: f=
                801.913, eps=0.003373154
Epoch 146: f=
                801.913, eps=0.003541811
Epoch 147: f=
                801.913, eps=0.003718902
Epoch 148: f=
                801.913, eps=0.003904847
Epoch 149: f=
                801.913, eps=0.004100089
Epoch 150: f=
                801.913, eps=0.004305094
Epoch 151: f=
                801.913, eps=0.004520348
Epoch 152: f=
                801.913, eps=0.004746366
Epoch 153: f=
                801.913, eps=0.004983684
Epoch 154: f=
                801.913, eps=0.005232868
                801.913, eps=0.005494512
Epoch 155: f=
Epoch 156: f=
                801.913, eps=0.005769237
Epoch 157: f=
                801.913, eps=0.006057699
Epoch 158: f=
                801.913, eps=0.006360584
Epoch 159: f=
                801.913, eps=0.006678613
Epoch 160: f=
                801.913, eps=0.007012544
Epoch 161: f=
                801.913, eps=0.007363171
Epoch 162: f=
                801.913, eps=0.007731330
Epoch 163: f=
                801.913, eps=0.008117896
Epoch 164: f=
                801.913, eps=0.008523791
Epoch 165: f=
                801.913, eps=0.008949981
Epoch 166: f=
                801.913, eps=0.004474990
Epoch 167: f=
                801.913, eps=0.002237495
Epoch 168: f=
                801.913, eps=0.002349370
Epoch 169: f=
                801.913, eps=0.002466838
Epoch 170: f=
                801.913, eps=0.002590180
Epoch 171: f=
                801.913, eps=0.001295090
Epoch 172: f=
                801.913, eps=0.001359845
Epoch 173: f=
                801.913, eps=0.000679922
Epoch 174: f=
                801.913, eps=0.000713918
Epoch 175: f=
                801.913, eps=0.000749614
Epoch 176: f=
                801.913, eps=0.000787095
Epoch 177: f=
                801.913, eps=0.000826450
Epoch 178: f=
                801.913, eps=0.000413225
Epoch 179: f=
                801.913, eps=0.000433886
Epoch 180: f=
                801.913, eps=0.000455580
Epoch 181: f=
                801.913, eps=0.000478360
Epoch 182: f=
                801.913, eps=0.000502277
Epoch 183: f=
                801.913, eps=0.000527391
Epoch 184: f=
                801.913, eps=0.000553761
Epoch 185: f=
                801.913, eps=0.000276880
Epoch 186: f=
                801.913, eps=0.000290724
                801.913, eps=0.000145362
Epoch 187: f=
Epoch 188: f=
                801.913, eps=0.000152630
Epoch 189: f=
                801.913, eps=0.000160262
Epoch 190: f=
                801.913, eps=0.000168275
Epoch 191: f=
                801.913, eps=0.000176689
Epoch 192: f=
                801.913, eps=0.000185523
```

```
Epoch 193: f=
                801.913, eps=0.000194799
Epoch 194: f=
                801.913, eps=0.000097400
Epoch 195: f=
                801.913, eps=0.000102270
Epoch 196: f=
                801.913, eps=0.000107383
Epoch 197: f=
                801.913, eps=0.000053692
Epoch 198: f=
                801.913, eps=0.000056376
Epoch 199: f=
                801.913, eps=0.000059195
Epoch 200: f=
                801.913, eps=0.000029597
Epoch 201: f=
                801.913, eps=0.000031077
Epoch 202: f=
                801.913, eps=0.000032631
Epoch 203: f=
                801.913, eps=0.000034263
Epoch 204: f=
                801.913, eps=0.000035976
Epoch 205: f=
                801.913, eps=0.000037775
Epoch 206: f=
                801.913, eps=0.000039663
Epoch 207: f=
                801.913, eps=0.000041647
Epoch 208: f=
                801.913, eps=0.000043729
Epoch 209: f=
                801.913, eps=0.000045915
Epoch 210: f=
                801.913, eps=0.000022958
Epoch 211: f=
                801.913, eps=0.000024106
Epoch 212: f=
                801.913, eps=0.000025311
Epoch 213: f=
                801.913, eps=0.000026576
Epoch 214: f=
                801.913, eps=0.000013288
Epoch 215: f=
                801.913, eps=0.000013953
Epoch 216: f=
                801.913, eps=0.000006976
Epoch 217: f=
                801.913, eps=0.000007325
Epoch 218: f=
                801.913, eps=0.000007691
Epoch 219: f=
                801.913, eps=0.000008076
Epoch 220: f=
                801.913, eps=0.000008480
Epoch 221: f=
                801.913, eps=0.000004240
Epoch 222: f=
                801.913, eps=0.000004452
Epoch 223: f=
                801.913, eps=0.000004674
Epoch 224: f=
                801.913, eps=0.000002337
Epoch 225: f=
                801.913, eps=0.000002454
Epoch 226: f=
                801.913, eps=0.000002577
Epoch 227: f=
                801.913, eps=0.000001288
Epoch 228: f=
                801.913, eps=0.000000644
Epoch 229: f=
                801.913, eps=0.000000676
Epoch 230: f=
                801.913, eps=0.000000710
Epoch 231: f=
                801.913, eps=0.000000746
Epoch 232: f=
                801.913, eps=0.000000783
Epoch 233: f=
                801.913, eps=0.000000392
Epoch 234: f=
                801.913, eps=0.000000411
Epoch 235: f=
                801.913, eps=0.000000432
Epoch 236: f=
                801.913, eps=0.000000216
Epoch 237: f=
                801.913, eps=0.000000227
Epoch 238: f=
                801.913, eps=0.000000238
Epoch 239: f=
                801.913, eps=0.000000119
Epoch 240: f=
                801.913, eps=0.000000125
```

```
Epoch 241: f=
                801.913, eps=0.000000062
Epoch 242: f=
                801.913, eps=0.000000066
Epoch 243: f=
                801.913, eps=0.000000069
Epoch 244: f=
                801.913, eps=0.000000072
Epoch 245: f=
                801.913, eps=0.000000076
Epoch 246: f=
                801.913, eps=0.000000038
Epoch 247: f=
                801.913, eps=0.000000040
                801.913, eps=0.000000042
Epoch 248: f=
Epoch 249: f=
                801.913, eps=0.000000044
Epoch 250: f=
                801.913, eps=0.000000022
Epoch 251: f=
                801.913, eps=0.000000023
Epoch 252: f=
                801.913, eps=0.000000012
Epoch 253: f=
                801.913, eps=0.000000012
Epoch 254: f=
                801.913, eps=0.000000013
Epoch 255: f=
                801.913, eps=0.000000013
Epoch 256: f=
                801.913, eps=0.000000014
Epoch 257: f=
                801.913, eps=0.000000015
Epoch 258: f=
                801.913, eps=0.000000007
Epoch 259: f=
                801.913, eps=0.000000008
Epoch 260: f=
                801.913, eps=0.000000008
Epoch 261: f=
                801.913, eps=0.000000009
Epoch 262: f=
                801.913, eps=0.000000009
Epoch 263: f=
                801.913, eps=0.000000009
Epoch 264: f=
                801.913, eps=0.000000005
Epoch 265: f=
                801.913, eps=0.000000005
Epoch 266: f=
                801.913, eps=0.000000005
Epoch 267: f=
                801.913, eps=0.000000003
Epoch 268: f=
                801.913, eps=0.000000003
Epoch 269: f=
                801.913, eps=0.000000003
Epoch 270: f=
                801.913, eps=0.000000003
Epoch 271: f=
                801.913, eps=0.000000003
Epoch 272: f=
                801.913, eps=0.000000003
Epoch 273: f=
                801.913, eps=0.000000003
Epoch 274: f=
                801.913, eps=0.000000004
Epoch 275: f=
                801.913, eps=0.000000004
Epoch 276: f=
                801.913, eps=0.000000004
Epoch 277: f=
                801.913, eps=0.000000004
Epoch 278: f=
                801.913, eps=0.000000004
Epoch 279: f=
                801.913, eps=0.000000005
Epoch 280: f=
                801.913, eps=0.000000005
Epoch 281: f=
                801.913, eps=0.000000005
Epoch 282: f=
                801.913, eps=0.000000005
Epoch 283: f=
                801.913, eps=0.000000006
Epoch 284: f=
                801.913, eps=0.000000006
Epoch 285: f=
                801.913, eps=0.000000006
                801.913, eps=0.000000003
Epoch 286: f=
Epoch 287: f=
                801.913, eps=0.000000003
Epoch 288: f=
                801.913, eps=0.000000003
```

```
Epoch 289: f=
                801.913, eps=0.000000004
Epoch 290: f=
                801.913, eps=0.000000004
Epoch 291: f=
                801.913, eps=0.000000004
Epoch 292: f=
                801.913, eps=0.000000004
Epoch 293: f=
                801.913, eps=0.000000004
Epoch 294: f=
                801.913, eps=0.000000002
Epoch 295: f=
                801.913, eps=0.000000002
                801.913, eps=0.000000001
Epoch 296: f=
Epoch 297: f=
                801.913, eps=0.000000001
Epoch 298: f=
                801.913, eps=0.000000001
Epoch 299: f=
                801.913, eps=0.000000001
Epoch 300: f=
                801.913, eps=0.000000001
Epoch 301: f=
                801.913, eps=0.000000001
Epoch 302: f=
                801.913, eps=0.000000001
Epoch 303: f=
                801.913, eps=0.000000001
Epoch 304: f=
                801.913, eps=0.000000001
Epoch 305: f=
                801.913, eps=0.000000001
Epoch 306: f=
                801.913, eps=0.000000001
Epoch 307: f=
                801.913, eps=0.000000001
Epoch 308: f=
                801.913, eps=0.000000001
Epoch 309: f=
                801.913, eps=0.000000001
Epoch 310: f=
                801.913, eps=0.000000001
Epoch 311: f=
                801.913, eps=0.000000001
Epoch 312: f=
                801.913, eps=0.000000001
Epoch 313: f=
                801.913, eps=0.000000001
Epoch 314: f=
                801.913, eps=0.000000001
Epoch 315: f=
                801.913, eps=0.000000001
Epoch 316: f=
                801.913, eps=0.000000001
Epoch 317: f=
                801.913, eps=0.000000002
Epoch 318: f=
                801.913, eps=0.000000002
Epoch 319: f=
                801.913, eps=0.000000002
Epoch 320: f=
                801.913, eps=0.000000002
Epoch 321: f=
                801.913, eps=0.000000002
Epoch 322: f=
                801.913, eps=0.000000002
Epoch 323: f=
                801.913, eps=0.000000002
Epoch 324: f=
                801.913, eps=0.000000002
Epoch 325: f=
                801.913, eps=0.000000002
Epoch 326: f=
                801.913, eps=0.000000002
Epoch 327: f=
                801.913, eps=0.000000002
Epoch 328: f=
                801.913, eps=0.000000003
Epoch 329: f=
                801.913, eps=0.000000003
Epoch 330: f=
                801.913, eps=0.000000003
Epoch 331: f=
                801.913, eps=0.000000003
Epoch 332: f=
                801.913, eps=0.000000003
Epoch 333: f=
                801.913, eps=0.000000003
                801.913, eps=0.000000003
Epoch 334: f=
Epoch 335: f=
                801.913, eps=0.000000004
Epoch 336: f=
                801.913, eps=0.000000004
```

```
Epoch 337: f=
                801.913, eps=0.000000004
Epoch 338: f=
                801.913, eps=0.000000004
Epoch 339: f=
                801.913, eps=0.000000002
                801.913, eps=0.000000002
Epoch 340: f=
Epoch 341: f=
                801.913, eps=0.000000002
Epoch 342: f=
                801.913, eps=0.000000002
Epoch 343: f=
                801.913, eps=0.000000003
                801.913, eps=0.000000003
Epoch 344: f=
Epoch 345: f=
                801.913, eps=0.000000003
Epoch 346: f=
                801.913, eps=0.000000003
Epoch 347: f=
                801.913, eps=0.000000001
Epoch 348: f=
                801.913, eps=0.000000002
Epoch 349: f=
                801.913, eps=0.000000002
Epoch 350: f=
                801.913, eps=0.000000001
Epoch 351: f=
                801.913, eps=0.000000001
Epoch 352: f=
                801.913, eps=0.000000001
Epoch 353: f=
                801.913, eps=0.000000001
Epoch 354: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000001
Epoch 355: f=
Epoch 356: f=
                801.913, eps=0.000000001
Epoch 357: f=
                801.913, eps=0.000000000
Epoch 358: f=
                801.913, eps=0.000000000
Epoch 359: f=
                801.913, eps=0.000000000
Epoch 360: f=
                801.913, eps=0.000000000
Epoch 361: f=
                801.913, eps=0.000000000
Epoch 362: f=
                801.913, eps=0.000000000
Epoch 363: f=
                801.913, eps=0.000000000
Epoch 364: f=
                801.913, eps=0.000000000
Epoch 365: f=
                801.913, eps=0.000000000
Epoch 366: f=
                801.913, eps=0.000000000
Epoch 367: f=
                801.913, eps=0.000000000
Epoch 368: f=
                801.913, eps=0.000000000
Epoch 369: f=
                801.913, eps=0.000000000
Epoch 370: f=
                801.913, eps=0.000000000
Epoch 371: f=
                801.913, eps=0.000000000
Epoch 372: f=
                801.913, eps=0.000000000
Epoch 373: f=
                801.913, eps=0.000000000
Epoch 374: f=
                801.913, eps=0.000000000
Epoch 375: f=
                801.913, eps=0.000000000
Epoch 376: f=
                801.913, eps=0.000000000
Epoch 377: f=
                801.913, eps=0.000000000
Epoch 378: f=
                801.913, eps=0.000000000
Epoch 379: f=
                801.913, eps=0.000000000
Epoch 380: f=
                801.913, eps=0.000000000
Epoch 381: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 382: f=
Epoch 383: f=
                801.913, eps=0.000000000
Epoch 384: f=
                801.913, eps=0.000000000
```

```
Epoch 385: f=
                801.913, eps=0.000000000
Epoch 386: f=
                801.913, eps=0.000000000
Epoch 387: f=
                801.913, eps=0.000000000
Epoch 388: f=
                801.913, eps=0.000000000
Epoch 389: f=
                801.913, eps=0.000000000
Epoch 390: f=
                801.913, eps=0.000000000
Epoch 391: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 392: f=
Epoch 393: f=
                801.913, eps=0.000000000
Epoch 394: f=
                801.913, eps=0.000000000
Epoch 395: f=
                801.913, eps=0.000000000
Epoch 396: f=
                801.913, eps=0.000000000
Epoch 397: f=
                801.913, eps=0.000000000
Epoch 398: f=
                801.913, eps=0.000000000
Epoch 399: f=
                801.913, eps=0.000000000
Epoch 400: f=
                801.913, eps=0.000000000
Epoch 401: f=
                801.913, eps=0.000000000
Epoch 402: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 403: f=
Epoch 404: f=
                801.913, eps=0.000000000
Epoch 405: f=
                801.913, eps=0.000000000
Epoch 406: f=
                801.913, eps=0.000000000
Epoch 407: f=
                801.913, eps=0.000000000
Epoch 408: f=
                801.913, eps=0.000000000
Epoch 409: f=
                801.913, eps=0.000000000
Epoch 410: f=
                801.913, eps=0.000000000
Epoch 411: f=
                801.913, eps=0.000000000
Epoch 412: f=
                801.913, eps=0.000000000
Epoch 413: f=
                801.913, eps=0.000000000
Epoch 414: f=
                801.913, eps=0.000000000
Epoch 415: f=
                801.913, eps=0.000000000
Epoch 416: f=
                801.913, eps=0.000000000
Epoch 417: f=
                801.913, eps=0.000000000
Epoch 418: f=
                801.913, eps=0.000000000
Epoch 419: f=
                801.913, eps=0.000000000
Epoch 420: f=
                801.913, eps=0.000000000
Epoch 421: f=
                801.913, eps=0.000000000
Epoch 422: f=
                801.913, eps=0.000000000
Epoch 423: f=
                801.913, eps=0.000000000
Epoch 424: f=
                801.913, eps=0.000000000
Epoch 425: f=
                801.913, eps=0.000000000
Epoch 426: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 427: f=
Epoch 428: f=
                801.913, eps=0.000000000
Epoch 429: f=
                801.913, eps=0.000000000
Epoch 430: f=
                801.913, eps=0.000000000
Epoch 431: f=
                801.913, eps=0.000000000
Epoch 432: f=
                801.913, eps=0.000000000
```

```
Epoch 433: f=
                801.913, eps=0.000000000
Epoch 434: f=
                801.913, eps=0.000000000
Epoch 435: f=
                801.913, eps=0.000000000
Epoch 436: f=
                801.913, eps=0.000000000
Epoch 437: f=
                801.913, eps=0.000000000
Epoch 438: f=
                801.913, eps=0.000000000
Epoch 439: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 440: f=
Epoch 441: f=
                801.913, eps=0.000000000
Epoch 442: f=
                801.913, eps=0.000000000
Epoch 443: f=
                801.913, eps=0.000000000
Epoch 444: f=
                801.913, eps=0.000000000
Epoch 445: f=
                801.913, eps=0.000000000
Epoch 446: f=
                801.913, eps=0.000000000
Epoch 447: f=
                801.913, eps=0.000000000
Epoch 448: f=
                801.913, eps=0.000000000
Epoch 449: f=
                801.913, eps=0.000000000
Epoch 450: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 451: f=
Epoch 452: f=
                801.913, eps=0.000000000
Epoch 453: f=
                801.913, eps=0.000000000
Epoch 454: f=
                801.913, eps=0.000000000
Epoch 455: f=
                801.913, eps=0.000000000
Epoch 456: f=
                801.913, eps=0.000000000
Epoch 457: f=
                801.913, eps=0.000000000
Epoch 458: f=
                801.913, eps=0.000000000
Epoch 459: f=
                801.913, eps=0.000000000
Epoch 460: f=
                801.913, eps=0.000000000
Epoch 461: f=
                801.913, eps=0.000000000
Epoch 462: f=
                801.913, eps=0.000000000
Epoch 463: f=
                801.913, eps=0.000000000
Epoch 464: f=
                801.913, eps=0.000000000
Epoch 465: f=
                801.913, eps=0.000000000
Epoch 466: f=
                801.913, eps=0.000000000
Epoch 467: f=
                801.913, eps=0.000000000
Epoch 468: f=
                801.913, eps=0.000000000
Epoch 469: f=
                801.913, eps=0.000000000
Epoch 470: f=
                801.913, eps=0.000000000
Epoch 471: f=
                801.913, eps=0.000000000
Epoch 472: f=
                801.913, eps=0.000000000
Epoch 473: f=
                801.913, eps=0.000000000
Epoch 474: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 475: f=
Epoch 476: f=
                801.913, eps=0.000000000
Epoch 477: f=
                801.913, eps=0.000000000
Epoch 478: f=
                801.913, eps=0.000000000
Epoch 479: f=
                801.913, eps=0.000000000
Epoch 480: f=
                801.913, eps=0.000000000
```

```
Epoch 481: f=
                801.913, eps=0.000000000
Epoch 482: f=
                801.913, eps=0.000000000
Epoch 483: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 484: f=
Epoch 485: f=
                801.913, eps=0.000000000
Epoch 486: f=
                801.913, eps=0.000000000
Epoch 487: f=
                801.913, eps=0.000000000
Epoch 488: f=
                801.913, eps=0.000000000
Epoch 489: f=
                801.913, eps=0.000000000
Epoch 490: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 491: f=
Epoch 492: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 493: f=
Epoch 494: f=
                801.913, eps=0.000000000
Epoch 495: f=
                801.913, eps=0.000000000
Epoch 496: f=
                801.913, eps=0.000000000
Epoch 497: f=
                801.913, eps=0.000000000
Epoch 498: f=
                801.913, eps=0.000000000
                801.913, eps=0.000000000
Epoch 499: f=
Result after 500 epochs: f=801.9128109439285
Epoch
        0: f=
               9992.358, eps=0.010000000
Epoch
        1: f= 23977.384, eps=0.005000000
Epoch
        2: f=
               5534.851, eps=0.005250000
Epoch
        3: f=
               1427.453, eps=0.005512500
Epoch
        4: f=
               1131.716, eps=0.005788125
        5: f=
               1540.933, eps=0.002894063
Epoch
Epoch
        6: f=
               1323.168, eps=0.003038766
Epoch
        7: f=
               1049.068, eps=0.003190704
Epoch
        8: f=
               1067.960, eps=0.001595352
        9: f=
                989.861, eps=0.001675120
Epoch
Epoch
      10: f=
                988.742, eps=0.001758876
       11: f=
                988.585, eps=0.001846819
Epoch
Epoch
      12: f=
                988.539, eps=0.001939160
Epoch
       13: f=
                988.522, eps=0.002036118
Epoch
       14: f=
                988.516, eps=0.002137924
Epoch
       15: f=
                988.513, eps=0.002244820
Epoch
       16: f=
                988.512, eps=0.002357061
Epoch
                988.512, eps=0.002474914
       17: f=
Epoch
       18: f=
                988.512, eps=0.002598660
Epoch
                988.512, eps=0.002728593
      19: f=
Epoch
      20: f=
                988.512, eps=0.002865023
Epoch
      21: f=
                988.512, eps=0.003008274
      22: f=
                988.512, eps=0.003158688
Epoch
Epoch
      23: f=
                988.512, eps=0.003316622
Epoch
      24: f=
                988.512, eps=0.001658311
Epoch
       25: f=
                988.512, eps=0.001741227
Epoch
      26: f=
                988.512, eps=0.001828288
                988.512, eps=0.001919702
Epoch
      27: f=
```

```
Epoch 28: f=
                988.512, eps=0.002015687
     29: f=
Epoch
                988.512, eps=0.002116472
                988.512, eps=0.002222295
Epoch 30: f=
                988.512, eps=0.002333410
Epoch
      31: f=
Epoch 32: f=
                988.512, eps=0.002450081
Epoch
      33: f=
                988.512, eps=0.002572585
Epoch
      34: f=
                988.512, eps=0.002701214
Epoch 35: f=
                988.512, eps=0.002836275
Epoch 36: f=
                988.512, eps=0.002978088
Epoch 37: f=
                988.512, eps=0.003126993
                988.512, eps=0.003283342
Epoch
      38: f=
Epoch 39: f=
                988.512, eps=0.003447510
                988.512, eps=0.003619885
Epoch 40: f=
Epoch
      41: f=
                988.512, eps=0.001809943
Epoch 42: f=
                988.512, eps=0.001900440
Epoch 43: f=
                988.512, eps=0.001995462
Epoch 44: f=
                988.512, eps=0.002095235
Epoch 45: f=
                988.512, eps=0.002199996
Epoch 46: f=
                988.512, eps=0.002309996
Epoch 47: f=
                988.512, eps=0.002425496
Epoch
      48: f=
                988.512, eps=0.002546771
Epoch 49: f=
                988.512, eps=0.001273385
Epoch 50: f=
                988.512, eps=0.001337055
Epoch 51: f=
                988.512, eps=0.001403907
Epoch 52: f=
                988.512, eps=0.001474103
Epoch 53: f=
                988.512, eps=0.001547808
                988.512, eps=0.000773904
Epoch 54: f=
Epoch 55: f=
                988.512, eps=0.000812599
Epoch 56: f=
                988.512, eps=0.000853229
Epoch 57: f=
                988.512, eps=0.000426615
Epoch 58: f=
                988.512, eps=0.000447945
Epoch 59: f=
                988.512, eps=0.000470343
Epoch 60: f=
                988.512, eps=0.000493860
                988.512, eps=0.000246930
Epoch 61: f=
Epoch
      62: f=
                988.512, eps=0.000259276
Epoch
      63: f=
                988.512, eps=0.000272240
Epoch 64: f=
                988.512, eps=0.000285852
Epoch
      65: f=
                988.512, eps=0.000142926
Epoch 66: f=
                988.512, eps=0.000150072
Epoch 67: f=
                988.512, eps=0.000157576
Epoch 68: f=
                988.512, eps=0.000078788
Epoch
      69: f=
                988.512, eps=0.000082727
      70: f=
                988.512, eps=0.000086864
Epoch
Epoch
      71: f=
                988.512, eps=0.000043432
Epoch
      72: f=
                988.512, eps=0.000045603
Epoch
      73: f=
                988.512, eps=0.000047884
Epoch
      74: f=
                988.512, eps=0.000023942
                988.512, eps=0.000025139
Epoch
      75: f=
```

```
Epoch 76: f=
                988.512, eps=0.000026396
Epoch
      77: f=
                988.512, eps=0.000013198
                988.512, eps=0.000013858
Epoch 78: f=
                988.512, eps=0.000006929
Epoch 79: f=
Epoch 80: f=
                988.512, eps=0.000007275
Epoch 81: f=
                988.512, eps=0.000007639
Epoch
      82: f=
                988.512, eps=0.000008021
Epoch 83: f=
                988.512, eps=0.000004011
Epoch 84: f=
                988.512, eps=0.000004211
Epoch 85: f=
                988.512, eps=0.000004422
Epoch 86: f=
                988.512, eps=0.000002211
Epoch 87: f=
                988.512, eps=0.000002321
Epoch 88: f=
                988.512, eps=0.000001161
Epoch
      89: f=
                988.512, eps=0.000001219
Epoch 90: f=
                988.512, eps=0.000000609
Epoch 91: f=
                988.512, eps=0.000000640
Epoch 92: f=
                988.512, eps=0.000000672
                988.512, eps=0.000000336
Epoch 93: f=
Epoch 94: f=
                988.512, eps=0.000000353
Epoch 95: f=
                988.512, eps=0.000000176
Epoch
      96: f=
                988.512, eps=0.000000185
Epoch 97: f=
                988.512, eps=0.000000093
Epoch 98: f=
                988.512, eps=0.000000097
Epoch 99: f=
                988.512, eps=0.000000102
Epoch 100: f=
                988.512, eps=0.000000107
Epoch 101: f=
                988.512, eps=0.000000113
                988.512, eps=0.000000056
Epoch 102: f=
Epoch 103: f=
                988.512, eps=0.000000059
Epoch 104: f=
                988.512, eps=0.000000062
Epoch 105: f=
                988.512, eps=0.000000065
Epoch 106: f=
                988.512, eps=0.000000068
Epoch 107: f=
                988.512, eps=0.000000072
Epoch 108: f=
                988.512, eps=0.000000075
Epoch 109: f=
                988.512, eps=0.000000079
Epoch 110: f=
                988.512, eps=0.000000083
Epoch 111: f=
                988.512, eps=0.000000042
Epoch 112: f=
                988.512, eps=0.000000044
Epoch 113: f=
                988.512, eps=0.000000046
Epoch 114: f=
                988.512, eps=0.000000023
Epoch 115: f=
                988.512, eps=0.000000024
Epoch 116: f=
                988.512, eps=0.000000025
                988.512, eps=0.00000013
Epoch 117: f=
Epoch 118: f=
                988.512, eps=0.00000013
Epoch 119: f=
                988.512, eps=0.000000014
Epoch 120: f=
                988.512, eps=0.00000015
Epoch 121: f=
                988.512, eps=0.000000007
Epoch 122: f=
                988.512, eps=0.000000008
Epoch 123: f=
                988.512, eps=0.000000004
```

```
Epoch 124: f=
                988.512, eps=0.000000004
Epoch 125: f=
                988.512, eps=0.000000002
Epoch 126: f=
                988.512, eps=0.000000002
Epoch 127: f=
                988.512, eps=0.000000002
Epoch 128: f=
                988.512, eps=0.000000002
Epoch 129: f=
                988.512, eps=0.000000002
Epoch 130: f=
                988.512, eps=0.000000003
Epoch 131: f=
                988.512, eps=0.000000003
Epoch 132: f=
                988.512, eps=0.000000003
Epoch 133: f=
                988.512, eps=0.000000003
Epoch 134: f=
                988.512, eps=0.000000003
Epoch 135: f=
                988.512, eps=0.000000003
Epoch 136: f=
                988.512, eps=0.000000003
Epoch 137: f=
                988.512, eps=0.000000004
Epoch 138: f=
                988.512, eps=0.000000002
Epoch 139: f=
                988.512, eps=0.000000002
Epoch 140: f=
                988.512, eps=0.000000002
Epoch 141: f=
                988.512, eps=0.000000002
Epoch 142: f=
                988.512, eps=0.000000001
Epoch 143: f=
                988.512, eps=0.000000001
Epoch 144: f=
                988.512, eps=0.000000001
Epoch 145: f=
                988.512, eps=0.000000001
Epoch 146: f=
                988.512, eps=0.00000001
Epoch 147: f=
                988.512, eps=0.00000001
Epoch 148: f=
                988.512, eps=0.00000001
Epoch 149: f=
                988.512, eps=0.00000001
                988.512, eps=0.00000001
Epoch 150: f=
Epoch 151: f=
                988.512, eps=0.00000001
Epoch 152: f=
                988.512, eps=0.000000000
Epoch 153: f=
                988.512, eps=0.000000000
Epoch 154: f=
                988.512, eps=0.000000000
Epoch 155: f=
                988.512, eps=0.000000000
Epoch 156: f=
                988.512, eps=0.000000000
Epoch 157: f=
                988.512, eps=0.000000000
Epoch 158: f=
                988.512, eps=0.000000001
Epoch 159: f=
                988.512, eps=0.000000001
Epoch 160: f=
                988.512, eps=0.000000001
Epoch 161: f=
                988.512, eps=0.000000001
Epoch 162: f=
                988.512, eps=0.00000001
Epoch 163: f=
                988.512, eps=0.00000001
Epoch 164: f=
                988.512, eps=0.00000001
                988.512, eps=0.000000001
Epoch 165: f=
Epoch 166: f=
                988.512, eps=0.000000001
Epoch 167: f=
                988.512, eps=0.00000001
Epoch 168: f=
                988.512, eps=0.000000001
Epoch 169: f=
                988.512, eps=0.000000001
Epoch 170: f=
                988.512, eps=0.000000001
Epoch 171: f=
                988.512, eps=0.000000001
```

```
Epoch 172: f=
                988.512, eps=0.000000001
Epoch 173: f=
                988.512, eps=0.000000001
Epoch 174: f=
                988.512, eps=0.00000001
                988.512, eps=0.00000001
Epoch 175: f=
Epoch 176: f=
                988.512, eps=0.000000001
                988.512, eps=0.00000001
Epoch 177: f=
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Epoch 220: f=
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Epoch 268: f=
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Epoch 364: f=
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Epoch 400: f=
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Epoch 401: f=
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Epoch 402: f=
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Epoch 403: f=
                988.512, eps=0.00000001
Epoch 404: f=
                988.512, eps=0.00000001
Epoch 405: f=
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                988.512, eps=0.000000000
Epoch 406: f=
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Epoch 410: f=
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Epoch 411: f=
                988.512, eps=0.000000000
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Epoch 412: f=
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Epoch 413: f=
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Epoch 414: f=
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Epoch 460: f=
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Epoch 461: f=
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Epoch 462: f=
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                988.512, eps=0.000000000
Epoch 498: f=
                988.512, eps=0.000000000
Epoch 499: f=
                988.512, eps=0.000000000
Result after 500 epochs: f=988.511839602703
Epoch
        0: f= 13348.508, eps=0.010000000
        1: f= 63618.781, eps=0.005000000
Epoch
Epoch
               5529.171, eps=0.005250000
        3: f= 25633.447, eps=0.002625000
Epoch
Epoch
        4: f=
               5261.229, eps=0.002756250
Epoch
        5: f=
               1444.512, eps=0.002894063
        6: f= 1140.676, eps=0.003038766
Epoch
```

```
Epoch
               1140.260, eps=0.003190704
        7: f=
Epoch
        8: f=
               1154.808, eps=0.001595352
        9: f=
               1112.206, eps=0.001675120
Epoch
               1110.068, eps=0.001758876
Epoch
       10: f=
Epoch
       11: f=
               1109.401, eps=0.001846819
               1109.220, eps=0.001939160
Epoch
       12: f=
Epoch
       13: f=
               1109.135, eps=0.002036118
Epoch
       14: f=
               1109.118, eps=0.002137924
Epoch
       15: f=
               1109.127, eps=0.001068962
Epoch
       16: f=
               1108.946, eps=0.001122410
Epoch
               1108.946, eps=0.001178531
       17: f=
Epoch
       18: f=
               1108.946, eps=0.001237457
               1108.946, eps=0.001299330
Epoch
       19: f=
Epoch
       20: f=
               1108.946, eps=0.001364297
Epoch
       21: f=
               1108.946, eps=0.001432511
Epoch
       22: f=
               1108.946, eps=0.001504137
Epoch
       23: f=
               1108.946, eps=0.001579344
Epoch
       24: f=
               1108.946, eps=0.001658311
Epoch
               1108.946, eps=0.001741227
       25: f=
Epoch
               1108.946, eps=0.001828288
       26: f=
Epoch
       27: f=
               1108.946, eps=0.001919702
Epoch
       28: f=
               1108.946, eps=0.002015687
Epoch
       29: f=
               1108.946, eps=0.002116472
Epoch
       30: f=
               1108.946, eps=0.002222295
               1108.946, eps=0.002333410
Epoch
       31: f=
Epoch
       32: f=
               1108.946, eps=0.002450081
Epoch
       33: f=
               1108.946, eps=0.002572585
Epoch
       34: f=
               1108.946, eps=0.001286292
Epoch
       35: f=
               1108.946, eps=0.001350607
Epoch
       36: f=
               1108.946, eps=0.001418137
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       37: f=
Epoch
       38: f=
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       39: f=
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               1108.946, eps=0.001723755
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       40: f=
Epoch
       41: f=
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               1108.946, eps=0.001900440
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       42: f=
Epoch
       43: f=
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               1108.946, eps=0.000997731
       44: f=
Epoch
       45: f=
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               1108.946, eps=0.001099998
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       46: f=
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       47: f=
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       48: f=
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               1108.946, eps=0.001273385
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       49: f=
Epoch
       50: f=
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Epoch
       51: f=
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       52: f=
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       53: f=
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               1108.946, eps=0.000773904
Epoch
      54: f=
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       56: f=
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               1108.946, eps=0.000895891
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       57: f=
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       58: f=
Epoch
       59: f=
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               1108.946, eps=0.001037105
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       60: f=
Epoch
       61: f=
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Epoch
       62: f=
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       63: f=
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Epoch
       64: f=
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               1108.946, eps=0.001323638
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               1108.946, eps=0.000694910
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       67: f=
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       69: f=
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       70: f=
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       71: f=
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               1108.946, eps=0.000201111
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       72: f=
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       74: f=
Epoch
       75: f=
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       77: f=
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       79: f=
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       81: f=
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       82: f=
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       83: f=
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       84: f=
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               1108.946, eps=0.000019499
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       85: f=
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       86: f=
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       87: f=
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               1108.946, eps=0.000022573
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       88: f=
Epoch
       89: f=
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       90: f=
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       91: f=
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Epoch
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Epoch
       93: f=
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       94: f=
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Epoch
       95: f=
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       96: f=
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       97: f=
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       98: f=
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Epoch 100: f=
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Epoch 101: f=
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Epoch 102: f=
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Epoch 105: f=
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               1108.946, eps=0.000012318
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Epoch 107: f=
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               1108.946, eps=0.000013581
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Epoch 109: f=
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Epoch 110: f=
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Epoch 111: f=
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Epoch 112: f=
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Epoch 114: f=
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               1108.946, eps=0.000009100
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Epoch 116: f=
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Epoch 117: f=
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Epoch 118: f=
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Epoch 120: f=
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Epoch 121: f=
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Epoch 122: f=
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Epoch 123: f=
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Epoch 124: f=
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Epoch 125: f=
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Epoch 126: f=
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Epoch 127: f=
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Epoch 128: f=
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Epoch 129: f=
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Epoch 130: f=
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Epoch 131: f=
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Epoch 133: f=
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Epoch 134: f=
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Epoch 135: f=
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Epoch 136: f=
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Epoch 137: f=
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Epoch 138: f=
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Epoch 139: f=
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Epoch 140: f=
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Epoch 141: f=
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Epoch 142: f=
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Epoch 143: f=
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Epoch 144: f=
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               1108.946, eps=0.000008918
Epoch 145: f=
Epoch 146: f=
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Epoch 147: f=
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Epoch 148: f=
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Epoch 149: f=
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Epoch 150: f=
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               1108.946, eps=0.000013835
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Epoch 155: f=
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Epoch 156: f=
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Epoch 157: f=
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               1108.946, eps=0.000016817
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Epoch 159: f=
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               1108.946, eps=0.000009270
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Epoch 162: f=
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               1108.946, eps=0.000010220
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Epoch 164: f=
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Epoch 165: f=
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Epoch 166: f=
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Epoch 167: f=
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Epoch 168: f=
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Epoch 169: f=
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Epoch 170: f=
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Epoch 171: f=
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Epoch 172: f=
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Epoch 173: f=
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               1108.946, eps=0.000018354
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Epoch 177: f=
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Epoch 178: f=
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Epoch 180: f=
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Epoch 181: f=
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               1108.946, eps=0.000006457
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Epoch 185: f=
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Epoch 186: f=
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Epoch 187: f=
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Epoch 188: f=
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Epoch 189: f=
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Epoch 190: f=
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Epoch 191: f=
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Epoch 192: f=
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               1108.946, eps=0.000002271
Epoch 193: f=
Epoch 194: f=
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Epoch 195: f=
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Epoch 196: f=
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Epoch 197: f=
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Epoch 198: f=
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               1108.946, eps=0.000001678
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Epoch 203: f=
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Epoch 205: f=
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               1108.946, eps=0.000002039
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Epoch 207: f=
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Epoch 208: f=
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Epoch 209: f=
Epoch 210: f=
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Epoch 212: f=
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Epoch 213: f=
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Epoch 214: f=
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Epoch 215: f=
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Epoch 216: f=
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Epoch 217: f=
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Epoch 219: f=
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Epoch 220: f=
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Epoch 221: f=
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Epoch 222: f=
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Epoch 223: f=
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Epoch 224: f=
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Epoch 225: f=
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Epoch 226: f=
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Epoch 227: f=
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Epoch 232: f=
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Epoch 234: f=
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Epoch 235: f=
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Epoch 238: f=
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Epoch 239: f=
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Epoch 240: f=
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               1108.946, eps=0.000002551
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Epoch 242: f=
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Epoch 243: f=
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Epoch 244: f=
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Epoch 245: f=
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               1108.946, eps=0.000003256
Epoch 246: f=
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Epoch 249: f=
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Epoch 250: f=
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               1108.946, eps=0.000002652
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Epoch 258: f=
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Epoch 259: f=
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Epoch 260: f=
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Epoch 262: f=
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Epoch 263: f=
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Epoch 264: f=
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Epoch 265: f=
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Epoch 268: f=
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Epoch 283: f=
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Epoch 284: f=
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Epoch 285: f=
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Epoch 286: f=
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Epoch 292: f=
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Epoch 293: f=
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Epoch 294: f=
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Epoch 307: f=
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Epoch 308: f=
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Epoch 309: f=
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Epoch 310: f=
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Epoch 311: f=
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Epoch 312: f=
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Epoch 313: f=
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Epoch 321: f=
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Epoch 322: f=
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Epoch 323: f=
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Epoch 326: f=
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Epoch 327: f=
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Epoch 328: f=
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Epoch 329: f=
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Epoch 330: f=
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Epoch 331: f=
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Epoch 332: f=
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Epoch 333: f=
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Epoch 334: f=
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Epoch 335: f=
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Epoch 336: f=
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               1108.946, eps=0.000001532
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Epoch 338: f=
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Epoch 339: f=
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Epoch 340: f=
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Epoch 341: f=
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Epoch 342: f=
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Epoch 347: f=
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Epoch 348: f=
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Epoch 349: f=
               1108.946, eps=0.000002752
Epoch 350: f=
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Epoch 351: f=
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Epoch 352: f=
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               1108.946, eps=0.000003345
Epoch 353: f=
Epoch 354: f=
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Epoch 355: f=
               1108.946, eps=0.000003688
Epoch 356: f=
               1108.946, eps=0.000003872
               1108.946, eps=0.000004066
Epoch 357: f=
Epoch 358: f=
               1108.946, eps=0.000004269
Epoch 359: f=
               1108.946, eps=0.000004482
Epoch 360: f=
               1108.946, eps=0.000004706
Epoch 361: f=
               1108.946, eps=0.000004942
Epoch 362: f=
               1108.946, eps=0.000005189
Epoch 363: f=
               1108.946, eps=0.000005448
Epoch 364: f=
               1108.946, eps=0.000005721
Epoch 365: f=
               1108.946, eps=0.000006007
Epoch 366: f=
               1108.946, eps=0.000006307
Epoch 367: f=
               1108.946, eps=0.000006622
Epoch 368: f=
               1108.946, eps=0.000006954
Epoch 369: f=
               1108.946, eps=0.000007301
Epoch 370: f=
               1108.946, eps=0.000007666
Epoch 371: f=
               1108.946, eps=0.000008050
Epoch 372: f=
               1108.946, eps=0.000008452
Epoch 373: f=
               1108.946, eps=0.000008875
Epoch 374: f=
               1108.946, eps=0.000009318
Epoch 375: f=
               1108.946, eps=0.000009784
Epoch 376: f=
               1108.946, eps=0.000010274
Epoch 377: f=
               1108.946, eps=0.000005137
Epoch 378: f=
               1108.946, eps=0.000005394
Epoch 379: f=
               1108.946, eps=0.000005663
Epoch 380: f=
               1108.946, eps=0.000005946
Epoch 381: f=
               1108.946, eps=0.000006244
Epoch 382: f=
               1108.946, eps=0.000006556
Epoch 383: f=
               1108.946, eps=0.000006884
Epoch 384: f=
               1108.946, eps=0.000007228
               1108.946, eps=0.000007589
Epoch 385: f=
Epoch 386: f=
               1108.946, eps=0.000007969
               1108.946, eps=0.000008367
Epoch 387: f=
Epoch 388: f=
               1108.946, eps=0.000008786
Epoch 389: f=
               1108.946, eps=0.000009225
               1108.946, eps=0.000009686
Epoch 390: f=
```

```
Epoch 391: f=
               1108.946, eps=0.000010170
Epoch 392: f=
               1108.946, eps=0.000010679
Epoch 393: f=
               1108.946, eps=0.000011213
Epoch 394: f=
               1108.946, eps=0.000011774
Epoch 395: f=
               1108.946, eps=0.000012362
Epoch 396: f=
               1108.946, eps=0.000012980
Epoch 397: f=
               1108.946, eps=0.000013629
Epoch 398: f=
               1108.946, eps=0.000014311
Epoch 399: f=
               1108.946, eps=0.000015026
Epoch 400: f=
               1108.946, eps=0.000007513
               1108.946, eps=0.000007889
Epoch 401: f=
Epoch 402: f=
               1108.946, eps=0.000008283
Epoch 403: f=
               1108.946, eps=0.000008697
Epoch 404: f=
               1108.946, eps=0.000004349
Epoch 405: f=
               1108.946, eps=0.000004566
Epoch 406: f=
               1108.946, eps=0.000004794
Epoch 407: f=
               1108.946, eps=0.000005034
Epoch 408: f=
               1108.946, eps=0.000005286
Epoch 409: f=
               1108.946, eps=0.000005550
Epoch 410: f=
               1108.946, eps=0.000005828
Epoch 411: f=
               1108.946, eps=0.000006119
Epoch 412: f=
               1108.946, eps=0.000003060
Epoch 413: f=
               1108.946, eps=0.000003213
Epoch 414: f=
               1108.946, eps=0.000003373
Epoch 415: f=
               1108.946, eps=0.000001687
Epoch 416: f=
               1108.946, eps=0.000001771
Epoch 417: f=
               1108.946, eps=0.000001859
Epoch 418: f=
               1108.946, eps=0.000000930
Epoch 419: f=
               1108.946, eps=0.000000976
Epoch 420: f=
               1108.946, eps=0.000001025
Epoch 421: f=
               1108.946, eps=0.000001076
Epoch 422: f=
               1108.946, eps=0.000001130
Epoch 423: f=
               1108.946, eps=0.000001187
Epoch 424: f=
               1108.946, eps=0.000001246
Epoch 425: f=
               1108.946, eps=0.000001308
Epoch 426: f=
               1108.946, eps=0.000001374
Epoch 427: f=
               1108.946, eps=0.000001442
Epoch 428: f=
               1108.946, eps=0.000001514
Epoch 429: f=
               1108.946, eps=0.000001590
Epoch 430: f=
               1108.946, eps=0.000001670
Epoch 431: f=
               1108.946, eps=0.000001753
Epoch 432: f=
               1108.946, eps=0.000001841
               1108.946, eps=0.000001933
Epoch 433: f=
Epoch 434: f=
               1108.946, eps=0.000000966
               1108.946, eps=0.000001015
Epoch 435: f=
Epoch 436: f=
               1108.946, eps=0.000001065
Epoch 437: f=
               1108.946, eps=0.000001119
               1108.946, eps=0.000001175
Epoch 438: f=
```

```
Epoch 439: f=
               1108.946, eps=0.000001233
Epoch 440: f=
               1108.946, eps=0.000001295
Epoch 441: f=
               1108.946, eps=0.000001360
Epoch 442: f=
               1108.946, eps=0.000001428
Epoch 443: f=
               1108.946, eps=0.000001499
Epoch 444: f=
               1108.946, eps=0.000001574
Epoch 445: f=
               1108.946, eps=0.000001653
Epoch 446: f=
               1108.946, eps=0.000001736
Epoch 447: f=
               1108.946, eps=0.000001822
Epoch 448: f=
               1108.946, eps=0.000001913
               1108.946, eps=0.000002009
Epoch 449: f=
Epoch 450: f=
               1108.946, eps=0.000002110
Epoch 451: f=
               1108.946, eps=0.000002215
Epoch 452: f=
               1108.946, eps=0.000002326
               1108.946, eps=0.000002442
Epoch 453: f=
Epoch 454: f=
               1108.946, eps=0.000002564
Epoch 455: f=
               1108.946, eps=0.000002692
Epoch 456: f=
               1108.946, eps=0.000002827
Epoch 457: f=
               1108.946, eps=0.000002968
               1108.946, eps=0.000003117
Epoch 458: f=
Epoch 459: f=
               1108.946, eps=0.000003273
Epoch 460: f=
               1108.946, eps=0.000003436
Epoch 461: f=
               1108.946, eps=0.000003608
Epoch 462: f=
               1108.946, eps=0.000003788
Epoch 463: f=
               1108.946, eps=0.000003978
Epoch 464: f=
               1108.946, eps=0.000004177
Epoch 465: f=
               1108.946, eps=0.000004386
Epoch 466: f=
               1108.946, eps=0.000004605
Epoch 467: f=
               1108.946, eps=0.000004835
               1108.946, eps=0.000005077
Epoch 468: f=
Epoch 469: f=
               1108.946, eps=0.000005331
Epoch 470: f=
               1108.946, eps=0.000005597
Epoch 471: f=
               1108.946, eps=0.000005877
Epoch 472: f=
               1108.946, eps=0.000006171
Epoch 473: f=
               1108.946, eps=0.000006480
Epoch 474: f=
               1108.946, eps=0.000006804
Epoch 475: f=
               1108.946, eps=0.000007144
Epoch 476: f=
               1108.946, eps=0.000007501
Epoch 477: f=
               1108.946, eps=0.000007876
Epoch 478: f=
               1108.946, eps=0.000008270
Epoch 479: f=
               1108.946, eps=0.000008683
Epoch 480: f=
               1108.946, eps=0.000004342
               1108.946, eps=0.000004559
Epoch 481: f=
Epoch 482: f=
               1108.946, eps=0.000004787
               1108.946, eps=0.000005026
Epoch 483: f=
Epoch 484: f=
               1108.946, eps=0.000005277
Epoch 485: f=
               1108.946, eps=0.000005541
               1108.946, eps=0.000005818
Epoch 486: f=
```

```
Epoch 487: f=
               1108.946, eps=0.000006109
Epoch 488: f=
               1108.946, eps=0.000006415
Epoch 489: f=
               1108.946, eps=0.000006735
               1108.946, eps=0.000007072
Epoch 490: f=
Epoch 491: f=
               1108.946, eps=0.000007426
Epoch 492: f=
               1108.946, eps=0.000007797
Epoch 493: f=
               1108.946, eps=0.000008187
Epoch 494: f=
               1108.946, eps=0.000008596
Epoch 495: f=
               1108.946, eps=0.000004298
Epoch 496: f=
               1108.946, eps=0.000004513
               1108.946, eps=0.000004739
Epoch 497: f=
Epoch 498: f=
               1108.946, eps=0.000004976
               1108.946, eps=0.000005224
Epoch 499: f=
Result after 500 epochs: f=1108.9460399053748
Epoch
        0: f= 23416.957, eps=0.010000000
Epoch
        1: f=502022.764, eps=0.005000000
        2: f=1284214.042, eps=0.002500000
Epoch
Epoch
        3: f=136841.925, eps=0.002625000
Epoch
        4: f= 37045.897, eps=0.002756250
        5: f= 45292.816, eps=0.001378125
Epoch
Epoch
               4492.761, eps=0.001447031
Epoch
        7: f=
               1386.173, eps=0.001519383
Epoch
        8: f=
               1378.369, eps=0.001595352
Epoch
        9: f=
               1393.755, eps=0.000797676
Epoch
       10: f=
               1315.023, eps=0.000837560
       11: f=
               1304.811, eps=0.000879438
Epoch
Epoch
               1304.439, eps=0.000923410
       12: f=
Epoch
       13: f=
               1304.393, eps=0.000969580
Epoch
       14: f=
               1304.386, eps=0.001018059
       15: f=
               1304.384, eps=0.001068962
Epoch
Epoch
       16: f=
               1304.384, eps=0.001122410
               1304.384, eps=0.001178531
Epoch
       17: f=
Epoch
       18: f=
               1304.384, eps=0.001237457
Epoch
       19: f=
               1304.384, eps=0.001299330
       20: f=
               1304.384, eps=0.000649665
Epoch
Epoch
       21: f=
               1304.383, eps=0.000682148
Epoch
       22: f=
               1304.383, eps=0.000716256
               1304.383, eps=0.000752069
Epoch
       23: f=
Epoch
       24: f=
               1304.383, eps=0.000789672
               1304.383, eps=0.000829156
Epoch
       25: f=
Epoch
       26: f=
               1304.383, eps=0.000870613
Epoch
       27: f=
               1304.383, eps=0.000914144
Epoch
       28: f=
               1304.383, eps=0.000959851
Epoch
       29: f=
               1304.383, eps=0.001007844
Epoch
       30: f=
               1304.383, eps=0.001058236
Epoch
       31: f=
               1304.383, eps=0.001111148
Epoch
       32: f=
               1304.383, eps=0.001166705
               1304.383, eps=0.000583353
Epoch
       33: f=
```

```
Epoch
       34: f=
               1304.383, eps=0.000612520
Epoch
       35: f=
               1304.383, eps=0.000643146
Epoch
       36: f=
               1304.383, eps=0.000675303
Epoch
       37: f=
               1304.383, eps=0.000709069
Epoch
       38: f=
               1304.383, eps=0.000744522
Epoch
       39: f=
               1304.383, eps=0.000781748
Epoch
       40: f=
               1304.383, eps=0.000390874
Epoch
       41: f=
               1304.383, eps=0.000410418
Epoch
       42: f=
               1304.383, eps=0.000430939
Epoch
       43: f=
               1304.383, eps=0.000452486
               1304.383, eps=0.000226243
Epoch
       44: f=
Epoch
       45: f=
               1304.383, eps=0.000237555
               1304.383, eps=0.000249433
Epoch
       46: f=
Epoch
       47: f=
               1304.383, eps=0.000124716
               1304.383, eps=0.000130952
Epoch
       48: f=
Epoch
       49: f=
               1304.383, eps=0.000137500
Epoch
       50: f=
               1304.383, eps=0.000144375
Epoch
       51: f=
               1304.383, eps=0.000151594
       52: f=
               1304.383, eps=0.000075797
Epoch
Epoch
               1304.383, eps=0.000079587
       53: f=
Epoch
       54: f=
               1304.383, eps=0.000083566
Epoch
       55: f=
               1304.383, eps=0.000041783
Epoch
       56: f=
               1304.383, eps=0.000043872
Epoch
       57: f=
               1304.383, eps=0.000046066
               1304.383, eps=0.000048369
Epoch
       58: f=
Epoch
       59: f=
               1304.383, eps=0.000024184
Epoch
       60: f=
               1304.383, eps=0.000025394
Epoch
       61: f=
               1304.383, eps=0.000026663
Epoch
       62: f=
               1304.383, eps=0.000027997
Epoch
       63: f=
               1304.383, eps=0.000029396
Epoch
       64: f=
               1304.383, eps=0.000030866
Epoch
       65: f=
               1304.383, eps=0.000032410
Epoch
       66: f=
               1304.383, eps=0.000034030
Epoch
       67: f=
               1304.383, eps=0.000035732
Epoch
       68: f=
               1304.383, eps=0.000037518
Epoch
       69: f=
               1304.383, eps=0.000039394
Epoch
       70: f=
               1304.383, eps=0.000041364
Epoch
               1304.383, eps=0.000043432
       71: f=
Epoch
       72: f=
               1304.383, eps=0.000021716
      73: f=
               1304.383, eps=0.000022802
Epoch
Epoch
       74: f=
               1304.383, eps=0.000023942
       75: f=
Epoch
               1304.383, eps=0.000011971
               1304.383, eps=0.000012569
Epoch
       76: f=
Epoch
       77: f=
               1304.383, eps=0.000013198
Epoch
       78: f=
               1304.383, eps=0.000013858
Epoch
       79: f=
               1304.383, eps=0.000014551
Epoch
       80: f=
               1304.383, eps=0.000015278
               1304.383, eps=0.000016042
Epoch
       81: f=
```

```
Epoch
       82: f=
               1304.383, eps=0.000016844
Epoch
       83: f=
               1304.383, eps=0.000017686
Epoch
       84: f=
               1304.383, eps=0.000018571
Epoch
               1304.383, eps=0.000019499
       85: f=
Epoch
       86: f=
               1304.383, eps=0.000020474
Epoch
       87: f=
               1304.383, eps=0.000021498
Epoch
       88: f=
               1304.383, eps=0.000022573
Epoch
       89: f=
               1304.383, eps=0.000023702
Epoch
       90: f=
               1304.383, eps=0.000024887
Epoch
       91: f=
               1304.383, eps=0.000026131
               1304.383, eps=0.000027438
Epoch
       92: f=
Epoch
       93: f=
               1304.383, eps=0.000028809
               1304.383, eps=0.000030250
Epoch
       94: f=
Epoch
       95: f=
               1304.383, eps=0.000031762
Epoch
       96: f=
               1304.383, eps=0.000033351
Epoch
       97: f=
               1304.383, eps=0.000035018
Epoch
       98: f=
               1304.383, eps=0.000017509
Epoch 99: f=
               1304.383, eps=0.000018384
Epoch 100: f=
               1304.383, eps=0.000009192
Epoch 101: f=
               1304.383, eps=0.000009652
Epoch 102: f=
               1304.383, eps=0.000010134
Epoch 103: f=
               1304.383, eps=0.000010641
Epoch 104: f=
               1304.383, eps=0.000011173
Epoch 105: f=
               1304.383, eps=0.000011732
Epoch 106: f=
               1304.383, eps=0.000012318
Epoch 107: f=
               1304.383, eps=0.000012934
Epoch 108: f=
               1304.383, eps=0.000013581
Epoch 109: f=
               1304.383, eps=0.000006791
Epoch 110: f=
               1304.383, eps=0.000007130
Epoch 111: f=
               1304.383, eps=0.000007487
Epoch 112: f=
               1304.383, eps=0.000007861
Epoch 113: f=
               1304.383, eps=0.000008254
Epoch 114: f=
               1304.383, eps=0.000008667
Epoch 115: f=
               1304.383, eps=0.000009100
Epoch 116: f=
               1304.383, eps=0.000009555
Epoch 117: f=
               1304.383, eps=0.000010033
Epoch 118: f=
               1304.383, eps=0.000010534
Epoch 119: f=
               1304.383, eps=0.000011061
Epoch 120: f=
               1304.383, eps=0.000011614
Epoch 121: f=
               1304.383, eps=0.000012195
Epoch 122: f=
               1304.383, eps=0.000012805
Epoch 123: f=
               1304.383, eps=0.000013445
               1304.383, eps=0.000006722
Epoch 124: f=
Epoch 125: f=
               1304.383, eps=0.000007059
Epoch 126: f=
               1304.383, eps=0.000007411
Epoch 127: f=
               1304.383, eps=0.000007782
Epoch 128: f=
               1304.383, eps=0.000008171
               1304.383, eps=0.000008580
Epoch 129: f=
```

```
Epoch 130: f=
               1304.383, eps=0.000009009
Epoch 131: f=
               1304.383, eps=0.000009459
Epoch 132: f=
               1304.383, eps=0.000009932
Epoch 133: f=
               1304.383, eps=0.000010429
Epoch 134: f=
               1304.383, eps=0.000010950
Epoch 135: f=
               1304.383, eps=0.000011498
Epoch 136: f=
               1304.383, eps=0.000012073
               1304.383, eps=0.000012676
Epoch 137: f=
Epoch 138: f=
               1304.383, eps=0.000013310
Epoch 139: f=
               1304.383, eps=0.000013975
               1304.383, eps=0.000014674
Epoch 140: f=
Epoch 141: f=
               1304.383, eps=0.000015408
               1304.383, eps=0.000016178
Epoch 142: f=
Epoch 143: f=
               1304.383, eps=0.000016987
Epoch 144: f=
               1304.383, eps=0.000008494
Epoch 145: f=
               1304.383, eps=0.000008918
Epoch 146: f=
               1304.383, eps=0.000009364
Epoch 147: f=
               1304.383, eps=0.000009832
Epoch 148: f=
               1304.383, eps=0.000010324
Epoch 149: f=
               1304.383, eps=0.000010840
Epoch 150: f=
               1304.383, eps=0.000011382
Epoch 151: f=
               1304.383, eps=0.000011951
Epoch 152: f=
               1304.383, eps=0.000012549
Epoch 153: f=
               1304.383, eps=0.000013176
Epoch 154: f=
               1304.383, eps=0.000013835
Epoch 155: f=
               1304.383, eps=0.000014527
Epoch 156: f=
               1304.383, eps=0.000015253
Epoch 157: f=
               1304.383, eps=0.000016016
Epoch 158: f=
               1304.383, eps=0.000016817
Epoch 159: f=
               1304.383, eps=0.000008408
Epoch 160: f=
               1304.383, eps=0.000008829
Epoch 161: f=
               1304.383, eps=0.000009270
Epoch 162: f=
               1304.383, eps=0.000009734
Epoch 163: f=
               1304.383, eps=0.000004867
Epoch 164: f=
               1304.383, eps=0.000005110
Epoch 165: f=
               1304.383, eps=0.000005366
Epoch 166: f=
               1304.383, eps=0.000002683
Epoch 167: f=
               1304.383, eps=0.000002817
Epoch 168: f=
               1304.383, eps=0.000002958
Epoch 169: f=
               1304.383, eps=0.000003106
Epoch 170: f=
               1304.383, eps=0.000003261
Epoch 171: f=
               1304.383, eps=0.000003424
               1304.383, eps=0.000003595
Epoch 172: f=
Epoch 173: f=
               1304.383, eps=0.000003775
Epoch 174: f=
               1304.383, eps=0.000003964
Epoch 175: f=
               1304.383, eps=0.000004162
Epoch 176: f=
               1304.383, eps=0.000004370
               1304.383, eps=0.000004589
Epoch 177: f=
```

```
Epoch 178: f=
               1304.383, eps=0.000004818
Epoch 179: f=
               1304.383, eps=0.000005059
Epoch 180: f=
               1304.383, eps=0.000005312
Epoch 181: f=
               1304.383, eps=0.000005577
Epoch 182: f=
               1304.383, eps=0.000005856
Epoch 183: f=
               1304.383, eps=0.000002928
Epoch 184: f=
               1304.383, eps=0.000003075
Epoch 185: f=
               1304.383, eps=0.000003228
Epoch 186: f=
               1304.383, eps=0.000003390
Epoch 187: f=
               1304.383, eps=0.000001695
               1304.383, eps=0.000001780
Epoch 188: f=
Epoch 189: f=
               1304.383, eps=0.000001869
Epoch 190: f=
               1304.383, eps=0.000001962
Epoch 191: f=
               1304.383, eps=0.000002060
Epoch 192: f=
               1304.383, eps=0.000002163
Epoch 193: f=
               1304.383, eps=0.000002271
Epoch 194: f=
               1304.383, eps=0.000002385
Epoch 195: f=
               1304.383, eps=0.000002504
Epoch 196: f=
               1304.383, eps=0.000002629
Epoch 197: f=
               1304.383, eps=0.000002761
Epoch 198: f=
               1304.383, eps=0.000002899
Epoch 199: f=
               1304.383, eps=0.000003044
Epoch 200: f=
               1304.383, eps=0.000003196
Epoch 201: f=
               1304.383, eps=0.000003356
Epoch 202: f=
               1304.383, eps=0.000003524
Epoch 203: f=
               1304.383, eps=0.000003700
Epoch 204: f=
               1304.383, eps=0.000003885
Epoch 205: f=
               1304.383, eps=0.000004079
Epoch 206: f=
               1304.383, eps=0.000004283
Epoch 207: f=
               1304.383, eps=0.000004497
Epoch 208: f=
               1304.383, eps=0.000004722
Epoch 209: f=
               1304.383, eps=0.000002361
Epoch 210: f=
               1304.383, eps=0.000002479
Epoch 211: f=
               1304.383, eps=0.000002603
Epoch 212: f=
               1304.383, eps=0.000002733
Epoch 213: f=
               1304.383, eps=0.000002870
Epoch 214: f=
               1304.383, eps=0.000003013
Epoch 215: f=
               1304.383, eps=0.000003164
Epoch 216: f=
               1304.383, eps=0.000003322
Epoch 217: f=
               1304.383, eps=0.000003488
Epoch 218: f=
               1304.383, eps=0.000003663
Epoch 219: f=
               1304.383, eps=0.000001831
Epoch 220: f=
               1304.383, eps=0.000001923
Epoch 221: f=
               1304.383, eps=0.000002019
Epoch 222: f=
               1304.383, eps=0.000002120
Epoch 223: f=
               1304.383, eps=0.000002226
Epoch 224: f=
               1304.383, eps=0.000002337
Epoch 225: f=
               1304.383, eps=0.000002454
```

```
Epoch 226: f=
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Epoch 227: f=
               1304.383, eps=0.000002706
Epoch 228: f=
               1304.383, eps=0.000002841
Epoch 229: f=
               1304.383, eps=0.000002983
Epoch 230: f=
               1304.383, eps=0.000003132
Epoch 231: f=
               1304.383, eps=0.000003289
Epoch 232: f=
               1304.383, eps=0.000003453
Epoch 233: f=
               1304.383, eps=0.000003626
Epoch 234: f=
               1304.383, eps=0.000003807
Epoch 235: f=
               1304.383, eps=0.000003997
Epoch 236: f=
               1304.383, eps=0.000004197
Epoch 237: f=
               1304.383, eps=0.000004407
Epoch 238: f=
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Epoch 239: f=
               1304.383, eps=0.000004859
Epoch 240: f=
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Epoch 241: f=
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Epoch 242: f=
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Epoch 243: f=
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Epoch 244: f=
               1304.383, eps=0.000006201
Epoch 245: f=
               1304.383, eps=0.000006511
Epoch 246: f=
               1304.383, eps=0.000006837
Epoch 247: f=
               1304.383, eps=0.000007179
Epoch 248: f=
               1304.383, eps=0.000003589
Epoch 249: f=
               1304.383, eps=0.000003769
Epoch 250: f=
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Epoch 251: f=
               1304.383, eps=0.000001979
Epoch 252: f=
               1304.383, eps=0.000002078
Epoch 253: f=
               1304.383, eps=0.000002181
Epoch 254: f=
               1304.383, eps=0.000001091
Epoch 255: f=
               1304.383, eps=0.000001145
Epoch 256: f=
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Epoch 257: f=
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Epoch 258: f=
               1304.383, eps=0.000000631
Epoch 259: f=
               1304.383, eps=0.000000663
Epoch 260: f=
               1304.383, eps=0.000000696
Epoch 261: f=
               1304.383, eps=0.000000731
Epoch 262: f=
               1304.383, eps=0.000000767
Epoch 263: f=
               1304.383, eps=0.000000806
Epoch 264: f=
               1304.383, eps=0.000000403
Epoch 265: f=
               1304.383, eps=0.000000423
Epoch 266: f=
               1304.383, eps=0.000000444
Epoch 267: f=
               1304.383, eps=0.000000466
Epoch 268: f=
               1304.383, eps=0.000000490
Epoch 269: f=
               1304.383, eps=0.000000514
Epoch 270: f=
               1304.383, eps=0.000000540
Epoch 271: f=
               1304.383, eps=0.000000567
Epoch 272: f=
               1304.383, eps=0.000000595
Epoch 273: f=
               1304.383, eps=0.000000625
```

```
Epoch 274: f=
               1304.383, eps=0.000000656
Epoch 275: f=
               1304.383, eps=0.000000689
Epoch 276: f=
               1304.383, eps=0.000000345
Epoch 277: f=
               1304.383, eps=0.000000362
Epoch 278: f=
               1304.383, eps=0.000000380
Epoch 279: f=
               1304.383, eps=0.000000399
Epoch 280: f=
               1304.383, eps=0.000000419
Epoch 281: f=
               1304.383, eps=0.000000440
Epoch 282: f=
               1304.383, eps=0.000000220
Epoch 283: f=
               1304.383, eps=0.000000231
Epoch 284: f=
               1304.383, eps=0.000000242
Epoch 285: f=
               1304.383, eps=0.000000255
Epoch 286: f=
               1304.383, eps=0.000000267
Epoch 287: f=
               1304.383, eps=0.000000281
Epoch 288: f=
               1304.383, eps=0.000000295
Epoch 289: f=
               1304.383, eps=0.000000309
Epoch 290: f=
               1304.383, eps=0.000000325
Epoch 291: f=
               1304.383, eps=0.000000341
Epoch 292: f=
               1304.383, eps=0.000000171
Epoch 293: f=
               1304.383, eps=0.000000179
Epoch 294: f=
               1304.383, eps=0.000000188
Epoch 295: f=
               1304.383, eps=0.000000197
Epoch 296: f=
               1304.383, eps=0.000000207
Epoch 297: f=
               1304.383, eps=0.000000218
Epoch 298: f=
               1304.383, eps=0.000000109
Epoch 299: f=
               1304.383, eps=0.000000114
Epoch 300: f=
               1304.383, eps=0.000000120
Epoch 301: f=
               1304.383, eps=0.000000126
Epoch 302: f=
               1304.383, eps=0.000000132
Epoch 303: f=
               1304.383, eps=0.000000139
Epoch 304: f=
               1304.383, eps=0.000000146
Epoch 305: f=
               1304.383, eps=0.000000153
Epoch 306: f=
               1304.383, eps=0.000000161
Epoch 307: f=
               1304.383, eps=0.000000169
Epoch 308: f=
               1304.383, eps=0.000000177
Epoch 309: f=
               1304.383, eps=0.000000186
Epoch 310: f=
               1304.383, eps=0.000000195
Epoch 311: f=
               1304.383, eps=0.000000205
Epoch 312: f=
               1304.383, eps=0.000000215
Epoch 313: f=
               1304.383, eps=0.000000226
Epoch 314: f=
               1304.383, eps=0.000000238
Epoch 315: f=
               1304.383, eps=0.000000249
Epoch 316: f=
               1304.383, eps=0.000000262
Epoch 317: f=
               1304.383, eps=0.000000131
Epoch 318: f=
               1304.383, eps=0.000000137
Epoch 319: f=
               1304.383, eps=0.000000144
Epoch 320: f=
               1304.383, eps=0.000000152
Epoch 321: f=
               1304.383, eps=0.000000159
```

```
Epoch 322: f=
               1304.383, eps=0.000000167
Epoch 323: f=
               1304.383, eps=0.000000175
Epoch 324: f=
               1304.383, eps=0.000000184
Epoch 325: f=
               1304.383, eps=0.000000092
Epoch 326: f=
               1304.383, eps=0.000000097
Epoch 327: f=
               1304.383, eps=0.000000102
Epoch 328: f=
               1304.383, eps=0.000000107
Epoch 329: f=
               1304.383, eps=0.000000112
Epoch 330: f=
               1304.383, eps=0.000000056
Epoch 331: f=
               1304.383, eps=0.000000059
Epoch 332: f=
               1304.383, eps=0.000000062
Epoch 333: f=
               1304.383, eps=0.000000065
Epoch 334: f=
               1304.383, eps=0.000000068
Epoch 335: f=
               1304.383, eps=0.000000071
Epoch 336: f=
               1304.383, eps=0.000000075
Epoch 337: f=
               1304.383, eps=0.000000079
Epoch 338: f=
               1304.383, eps=0.000000083
Epoch 339: f=
               1304.383, eps=0.000000087
Epoch 340: f=
               1304.383, eps=0.000000091
Epoch 341: f=
               1304.383, eps=0.000000096
Epoch 342: f=
               1304.383, eps=0.000000101
Epoch 343: f=
               1304.383, eps=0.000000106
Epoch 344: f=
               1304.383, eps=0.000000111
Epoch 345: f=
               1304.383, eps=0.000000116
Epoch 346: f=
               1304.383, eps=0.000000122
Epoch 347: f=
               1304.383, eps=0.000000128
Epoch 348: f=
               1304.383, eps=0.000000135
Epoch 349: f=
               1304.383, eps=0.000000141
Epoch 350: f=
               1304.383, eps=0.000000149
Epoch 351: f=
               1304.383, eps=0.000000156
Epoch 352: f=
               1304.383, eps=0.000000164
Epoch 353: f=
               1304.383, eps=0.000000082
Epoch 354: f=
               1304.383, eps=0.000000086
Epoch 355: f=
               1304.383, eps=0.000000090
Epoch 356: f=
               1304.383, eps=0.000000095
Epoch 357: f=
               1304.383, eps=0.000000100
Epoch 358: f=
               1304.383, eps=0.000000105
Epoch 359: f=
               1304.383, eps=0.000000110
Epoch 360: f=
               1304.383, eps=0.000000115
Epoch 361: f=
               1304.383, eps=0.000000121
Epoch 362: f=
               1304.383, eps=0.000000127
Epoch 363: f=
               1304.383, eps=0.000000133
Epoch 364: f=
               1304.383, eps=0.000000140
Epoch 365: f=
               1304.383, eps=0.000000147
Epoch 366: f=
               1304.383, eps=0.000000154
Epoch 367: f=
               1304.383, eps=0.000000162
Epoch 368: f=
               1304.383, eps=0.000000170
Epoch 369: f=
               1304.383, eps=0.000000179
```

```
Epoch 370: f=
               1304.383, eps=0.000000188
Epoch 371: f=
               1304.383, eps=0.000000197
Epoch 372: f=
               1304.383, eps=0.000000207
Epoch 373: f=
               1304.383, eps=0.000000217
Epoch 374: f=
               1304.383, eps=0.000000228
Epoch 375: f=
               1304.383, eps=0.000000240
Epoch 376: f=
               1304.383, eps=0.000000252
Epoch 377: f=
               1304.383, eps=0.000000264
Epoch 378: f=
               1304.383, eps=0.000000277
Epoch 379: f=
               1304.383, eps=0.000000139
               1304.383, eps=0.000000146
Epoch 380: f=
Epoch 381: f=
               1304.383, eps=0.000000153
Epoch 382: f=
               1304.383, eps=0.000000161
Epoch 383: f=
               1304.383, eps=0.000000169
Epoch 384: f=
               1304.383, eps=0.000000177
Epoch 385: f=
               1304.383, eps=0.000000186
Epoch 386: f=
               1304.383, eps=0.000000195
Epoch 387: f=
               1304.383, eps=0.000000205
Epoch 388: f=
               1304.383, eps=0.000000215
Epoch 389: f=
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Epoch 390: f=
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Epoch 391: f=
               1304.383, eps=0.000000119
Epoch 392: f=
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Epoch 393: f=
               1304.383, eps=0.000000131
Epoch 394: f=
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Epoch 395: f=
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Epoch 396: f=
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Epoch 397: f=
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Epoch 398: f=
               1304.383, eps=0.000000079
Epoch 399: f=
               1304.383, eps=0.000000083
Epoch 400: f=
               1304.383, eps=0.000000088
Epoch 401: f=
               1304.383, eps=0.000000092
Epoch 402: f=
               1304.383, eps=0.000000097
Epoch 403: f=
               1304.383, eps=0.000000101
Epoch 404: f=
               1304.383, eps=0.000000106
Epoch 405: f=
               1304.383, eps=0.000000112
Epoch 406: f=
               1304.383, eps=0.000000117
Epoch 407: f=
               1304.383, eps=0.000000123
Epoch 408: f=
               1304.383, eps=0.000000129
Epoch 409: f=
               1304.383, eps=0.000000136
Epoch 410: f=
               1304.383, eps=0.000000143
Epoch 411: f=
               1304.383, eps=0.000000150
Epoch 412: f=
               1304.383, eps=0.000000157
Epoch 413: f=
               1304.383, eps=0.000000165
Epoch 414: f=
               1304.383, eps=0.000000173
Epoch 415: f=
               1304.383, eps=0.000000182
Epoch 416: f=
               1304.383, eps=0.000000191
               1304.383, eps=0.000000201
Epoch 417: f=
```

```
Epoch 418: f=
               1304.383, eps=0.000000100
Epoch 419: f=
               1304.383, eps=0.000000105
Epoch 420: f=
               1304.383, eps=0.000000111
Epoch 421: f=
               1304.383, eps=0.000000116
Epoch 422: f=
               1304.383, eps=0.000000122
Epoch 423: f=
               1304.383, eps=0.000000128
Epoch 424: f=
               1304.383, eps=0.000000135
Epoch 425: f=
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Epoch 426: f=
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Epoch 427: f=
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Epoch 428: f=
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Epoch 429: f=
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Epoch 430: f=
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Epoch 431: f=
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Epoch 432: f=
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Epoch 433: f=
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Epoch 434: f=
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Epoch 435: f=
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Epoch 436: f=
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Epoch 437: f=
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Epoch 438: f=
               1304.383, eps=0.000000029
Epoch 439: f=
               1304.383, eps=0.000000030
Epoch 440: f=
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Epoch 441: f=
               1304.383, eps=0.000000033
Epoch 442: f=
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Epoch 443: f=
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Epoch 444: f=
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Epoch 445: f=
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Epoch 446: f=
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Epoch 447: f=
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Epoch 448: f=
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Epoch 449: f=
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Epoch 450: f=
               1304.383, eps=0.000000052
Epoch 451: f=
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Epoch 452: f=
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Epoch 453: f=
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Epoch 454: f=
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Epoch 455: f=
               1304.383, eps=0.000000066
Epoch 456: f=
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Epoch 457: f=
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Epoch 458: f=
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Epoch 459: f=
               1304.383, eps=0.000000080
Epoch 460: f=
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Epoch 461: f=
               1304.383, eps=0.000000088
Epoch 462: f=
               1304.383, eps=0.000000093
Epoch 463: f=
               1304.383, eps=0.000000097
Epoch 464: f=
               1304.383, eps=0.000000102
               1304.383, eps=0.000000107
Epoch 465: f=
```

```
Epoch 466: f=
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Epoch 467: f=
               1304.383, eps=0.000000118
Epoch 468: f=
               1304.383, eps=0.000000124
Epoch 469: f=
               1304.383, eps=0.000000131
Epoch 470: f=
               1304.383, eps=0.000000137
Epoch 471: f=
               1304.383, eps=0.000000144
Epoch 472: f=
               1304.383, eps=0.000000151
Epoch 473: f=
               1304.383, eps=0.000000159
Epoch 474: f=
               1304.383, eps=0.000000079
Epoch 475: f=
               1304.383, eps=0.000000083
               1304.383, eps=0.000000087
Epoch 476: f=
Epoch 477: f=
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Epoch 478: f=
               1304.383, eps=0.000000046
Epoch 479: f=
               1304.383, eps=0.000000048
Epoch 480: f=
               1304.383, eps=0.000000051
Epoch 481: f=
               1304.383, eps=0.000000053
Epoch 482: f=
               1304.383, eps=0.000000056
Epoch 483: f=
               1304.383, eps=0.000000059
Epoch 484: f=
               1304.383, eps=0.000000062
Epoch 485: f=
               1304.383, eps=0.000000065
Epoch 486: f=
               1304.383, eps=0.000000068
Epoch 487: f=
               1304.383, eps=0.000000071
Epoch 488: f=
               1304.383, eps=0.000000075
Epoch 489: f=
               1304.383, eps=0.000000079
Epoch 490: f=
               1304.383, eps=0.000000082
               1304.383, eps=0.000000041
Epoch 491: f=
Epoch 492: f=
               1304.383, eps=0.000000043
Epoch 493: f=
               1304.383, eps=0.000000045
Epoch 494: f=
               1304.383, eps=0.000000048
               1304.383, eps=0.000000050
Epoch 495: f=
Epoch 496: f=
               1304.383, eps=0.000000053
               1304.383, eps=0.000000055
Epoch 497: f=
Epoch 498: f=
               1304.383, eps=0.000000028
               1304.383, eps=0.000000029
Epoch 499: f=
Result after 500 epochs: f=1304.383410297585
Lambda = 0: Final Objective = 0.0091
Lambda = 0.01: Final Objective = 0.0044
Lambda = 0.1: Final Objective = 0.0044
Lambda = 0.5: Final Objective = 0.0091
Lambda = 1: Final Objective = 0.0044
Lambda = 2: Final Objective = 0.0044
Lambda = 3: Final Objective = 0.0044
Lambda = 4: Final Objective = 0.0044
Lambda = 5: Final Objective = 0.0044
Lambda = 10: Final Objective = 0.0000
Lambda = 20: Final Objective = 0.0000
Lambda = 100: Final Objective = 0.0000
Lambda = 200: Final Objective = 0.0000
```

```
[319]: results
[319]: {'0': {'final_weights': array([-8.86805803e-03, -1.87711722e-01,
      1.21527679e-01, 8.08625721e+00,
                 2.59086182e-01, 1.81011961e-01, 1.15333583e+00, 2.90298799e-01,
                 1.13527420e-01, 6.60449223e-02, -4.68398587e-02, -1.65669222e-01,
                -6.53149090e-02, -1.09479222e-02, 4.94021994e-01, 8.43700154e-01,
                 5.63710277e-01, 5.46097770e-02, 2.89015689e-01, 2.84882797e-01,
                 2.17373273e-01, 6.64971958e-01, 1.46174692e+00,
                                                                   2.54294549e-01,
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[320]: train nll = {}
       for k, v in results.items():
           print("lambda " + k + ": " + str(v["final_nll_values"][-1]))
           train nll[k] = v["final nll values"][-1]
      lambda 0: 655.413496469947
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      lambda 0.1: 661.3584589394447
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      lambda 20: 801.9128109439285
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      lambda 500: 1304.383410297585
[321]: results
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                  , -0.0482469 , 0.03343173, 0.03033862, 0.11977169,
          0.3018289 , 0.19016671 , 0.1334908 , 0.1351504 , 0.13378584
          0.23640097, 0.12083363, 0.27283738, 0.18300137, -0.16246059,
         -0.11256028, -0.12430894, -0.06345646, -0.05016659, -0.07076662,
         -0.0295907, -0.01461309, -0.08332194, -0.01563813, -0.04454267,
         -0.00945624, -0.08015203, -0.03803851, -0.08624723, 0.01982017,
         -0.05072923, -0.09981163, -0.0633398 , -0.07699937, -0.1247063 ,
         -0.12398245, -0.03486434, -0.06828286, -0.06484093, -0.04590349,
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  'final_nll_values': array([ 23416.95655204,
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'final_objective': np.float64(3.045683694619516e-08)}}
```

```
[322]: lambdas = list(train_nll.keys())

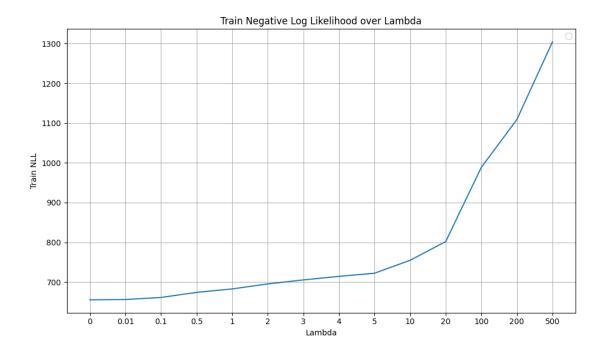
# Extracting values for plotting
train_nll_values = [train_nll[lam] for lam in lambdas]
# Setting up the scatter plot
plt.figure(figsize=(10, 6))

plt.plot(lambdas, train_nll_values)

# Adding labels and title
plt.xlabel('Lambda')
plt.ylabel('Train NLL')
plt.title('Train Negative Log Likelihood over Lambda')
plt.legend()
plt.grid(True)

# Show the plot
plt.tight_layout()
plt.show()
```

/tmp/ipykernel\_32055/158038987.py:14: UserWarning: No artists with labels found
to put in legend. Note that artists whose label start with an underscore are
ignored when legend() is called with no argument.
 plt.legend()



```
[323]: test_nll_results = {}
       for lam in lam_values:
           np.random.seed(0) # Set a seed for reproducibility in weight initialization
           w0 = np.random.normal(size=D) # Initialize weights randomly
           # Optimize logistic regression with L2 regularization for the current lambda
           wz, vz, ez = optimize(gd_12(ytest, Xtestz, lam), w0, nepochs=500)
           # Store final weights and objective value after training
           test_nll_results[str(lam)] = {
               'final weights': wz, # Final weight vector after optimization
               'final nll values': vz,
               'final_objective': ez[-1] # Final value of the objective function
           }
       # for la in lam_values:
             print("lambda" + str(la) + ":" + str(-l_l2(ytest, Xtestz, label{eq:label}))
        →results[str(la)]["final_weights"], la)))
             test_nll_results[la] = -l_l2(ytest, Xtestz, 
        →results[str(la)]["final_weights"], la)
       test_nll = {}
       for k, v in test_nll_results.items():
           print("lambda " + k + ": " + str(v["final_nll_values"][-1]))
           test_nll[k] = v["final_nll_values"][-1]
```

```
Epoch
       0: f= 3403.516, eps=0.010000000
Epoch
      1: f= 1331.469, eps=0.010500000
Epoch 2: f=
               814.794, eps=0.011025000
      3: f=
               591.367, eps=0.011576250
Epoch
Epoch 4: f=
               542.260, eps=0.012155063
Epoch 5: f=
               478.074, eps=0.012762816
Epoch 6: f=
               507.435, eps=0.006381408
Epoch 7: f=
               428.317, eps=0.006700478
Epoch 8: f=
               398.864, eps=0.007035502
Epoch 9: f=
               393.582, eps=0.007387277
Epoch 10: f=
               393.082, eps=0.007756641
Epoch 11: f=
               400.829, eps=0.003878321
Epoch 12: f=
               380.008, eps=0.004072237
               375.293, eps=0.004275848
Epoch 13: f=
Epoch 14: f=
               373.575, eps=0.004489641
Epoch 15: f=
               372.095, eps=0.004714123
Epoch 16: f=
               370.685, eps=0.004949829
Epoch 17: f=
               369.463, eps=0.005197320
Epoch 18: f=
               368.339, eps=0.005457186
Epoch 19: f=
               367.161, eps=0.005730046
Epoch 20: f=
               366.638, eps=0.006016548
```

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Epoch 21: f=
                365.255, eps=0.006317375
Epoch
      22: f=
                366.171, eps=0.003158688
Epoch
      23: f=
                358.210, eps=0.003316622
Epoch
      24: f=
                357.446, eps=0.003482453
Epoch
      25: f=
                356.688, eps=0.003656576
Epoch
      26: f=
                355.922, eps=0.003839405
Epoch
      27: f=
                355.140, eps=0.004031375
Epoch 28: f=
                354.350, eps=0.004232944
Epoch 29: f=
                353.549, eps=0.004444591
Epoch 30: f=
                352.770, eps=0.004666820
                352.017, eps=0.004900161
Epoch
      31: f=
Epoch
      32: f=
                351.481, eps=0.005145169
                350.944, eps=0.005402428
Epoch
      33: f=
Epoch
      34: f=
                351.294, eps=0.002701214
                348.723, eps=0.002836275
Epoch 35: f=
Epoch 36: f=
                348.210, eps=0.002978088
Epoch 37: f=
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      47: f=
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      62: f=
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      63: f=
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      64: f=
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      65: f=
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       66: f=
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      67: f=
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Epoch
      68: f=
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      73: f=
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      74: f=
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      75: f=
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Epoch 77: f=
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      82: f=
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      96: f=
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      97: f=
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Epoch 376: f=
                321.369, eps=0.003885749
Epoch 377: f=
                321.356, eps=0.004080037
Epoch 378: f=
                321.343, eps=0.004284039
Epoch 379: f=
                321.330, eps=0.004498241
Epoch 380: f=
                321.316, eps=0.004723153
Epoch 381: f=
                321.301, eps=0.004959310
Epoch 382: f=
                321.285, eps=0.005207276
Epoch 383: f=
                321.268, eps=0.005467640
Epoch 384: f=
                321.251, eps=0.005741022
Epoch 385: f=
                321.233, eps=0.006028073
Epoch 386: f=
                321.214, eps=0.006329476
Epoch 387: f=
                321.195, eps=0.006645950
Epoch 388: f=
                321.174, eps=0.006978248
Epoch 389: f=
                321.152, eps=0.007327160
Epoch 390: f=
                321.130, eps=0.007693518
Epoch 391: f=
                321.106, eps=0.008078194
Epoch 392: f=
                321.082, eps=0.008482104
Epoch 393: f=
                321.058, eps=0.008906209
Epoch 394: f=
                321.054, eps=0.009351519
Epoch 395: f=
                321.262, eps=0.004675760
Epoch 396: f=
                321.370, eps=0.002337880
Epoch 397: f=
                320.989, eps=0.002454774
Epoch 398: f=
                320.972, eps=0.002577512
Epoch 399: f=
                320.964, eps=0.002706388
Epoch 400: f=
                320.956, eps=0.002841708
Epoch 401: f=
                320.948, eps=0.002983793
Epoch 402: f=
                320.939, eps=0.003132983
Epoch 403: f=
                320.930, eps=0.003289632
Epoch 404: f=
                320.920, eps=0.003454113
```

```
Epoch 405: f=
                320.910, eps=0.003626819
Epoch 406: f=
                320.899, eps=0.003808160
Epoch 407: f=
                320.888, eps=0.003998568
Epoch 408: f=
                320.876, eps=0.004198496
Epoch 409: f=
                320.864, eps=0.004408421
Epoch 410: f=
                320.851, eps=0.004628842
Epoch 411: f=
                320.837, eps=0.004860284
Epoch 412: f=
                320.823, eps=0.005103298
Epoch 413: f=
                320.808, eps=0.005358463
Epoch 414: f=
                320.792, eps=0.005626387
Epoch 415: f=
                320.776, eps=0.005907706
Epoch 416: f=
                320.759, eps=0.006203091
Epoch 417: f=
                320.741, eps=0.006513246
Epoch 418: f=
                320.722, eps=0.006838908
Epoch 419: f=
                320.703, eps=0.007180853
Epoch 420: f=
                320.682, eps=0.007539896
Epoch 421: f=
                320.661, eps=0.007916891
Epoch 422: f=
                320.639, eps=0.008312735
Epoch 423: f=
                320.615, eps=0.008728372
Epoch 424: f=
                320.591, eps=0.009164791
Epoch 425: f=
                320.566, eps=0.009623030
Epoch 426: f=
                320.548, eps=0.010104182
Epoch 427: f=
                320.639, eps=0.005052091
Epoch 428: f=
                320.658, eps=0.002526045
Epoch 429: f=
                320.499, eps=0.002652348
Epoch 430: f=
                320.483, eps=0.002784965
Epoch 431: f=
                320.475, eps=0.002924213
Epoch 432: f=
                320.467, eps=0.003070424
Epoch 433: f=
                320.458, eps=0.003223945
Epoch 434: f=
                320.449, eps=0.003385142
Epoch 435: f=
                320.440, eps=0.003554400
Epoch 436: f=
                320.430, eps=0.003732120
Epoch 437: f=
                320.420, eps=0.003918726
Epoch 438: f=
                320.410, eps=0.004114662
Epoch 439: f=
                320.399, eps=0.004320395
Epoch 440: f=
                320.387, eps=0.004536415
Epoch 441: f=
                320.375, eps=0.004763235
Epoch 442: f=
                320.362, eps=0.005001397
Epoch 443: f=
                320.348, eps=0.005251467
Epoch 444: f=
                320.334, eps=0.005514040
Epoch 445: f=
                320.320, eps=0.005789742
Epoch 446: f=
                320.304, eps=0.006079230
Epoch 447: f=
                320.288, eps=0.006383191
Epoch 448: f=
                320.271, eps=0.006702351
Epoch 449: f=
                320.254, eps=0.007037468
Epoch 450: f=
                320.235, eps=0.007389342
Epoch 451: f=
                320.216, eps=0.007758809
Epoch 452: f=
                320.196, eps=0.008146749
```

```
Epoch 453: f=
                320.180, eps=0.008554086
Epoch 454: f=
                320.200, eps=0.004277043
Epoch 455: f=
                320.192, eps=0.004490895
Epoch 456: f=
                320.176, eps=0.004715440
Epoch 457: f=
                320.186, eps=0.002357720
Epoch 458: f=
                320.112, eps=0.002475606
Epoch 459: f=
                320.105, eps=0.002599386
Epoch 460: f=
                320.099, eps=0.002729356
Epoch 461: f=
                320.092, eps=0.002865824
Epoch 462: f=
                320.084, eps=0.003009115
                320.077, eps=0.003159570
Epoch 463: f=
Epoch 464: f=
                320.069, eps=0.003317549
Epoch 465: f=
                320.060, eps=0.003483426
Epoch 466: f=
                320.051, eps=0.003657598
Epoch 467: f=
                320.042, eps=0.003840478
Epoch 468: f=
                320.033, eps=0.004032501
Epoch 469: f=
                320.022, eps=0.004234127
Epoch 470: f=
                320.012, eps=0.004445833
Epoch 471: f=
                320.001, eps=0.004668125
Epoch 472: f=
                319.989, eps=0.004901531
Epoch 473: f=
                319.977, eps=0.005146607
Epoch 474: f=
                319.964, eps=0.005403938
Epoch 475: f=
                319.950, eps=0.005674135
Epoch 476: f=
                319.936, eps=0.005957841
Epoch 477: f=
                319.922, eps=0.006255733
Epoch 478: f=
                319.906, eps=0.006568520
Epoch 479: f=
                319.890, eps=0.006896946
Epoch 480: f=
                319.873, eps=0.007241793
Epoch 481: f=
                319.856, eps=0.007603883
Epoch 482: f=
                319.837, eps=0.007984077
Epoch 483: f=
                319.818, eps=0.008383281
Epoch 484: f=
                319.798, eps=0.008802445
Epoch 485: f=
                319.776, eps=0.009242567
Epoch 486: f=
                319.754, eps=0.009704696
Epoch 487: f=
                319.731, eps=0.010189930
Epoch 488: f=
                319.708, eps=0.010699427
Epoch 489: f=
                319.699, eps=0.011234398
Epoch 490: f=
                319.942, eps=0.005617199
Epoch 491: f=
                320.102, eps=0.002808600
Epoch 492: f=
                319.709, eps=0.002949030
Epoch 493: f=
                319.634, eps=0.003096481
Epoch 494: f=
                319.623, eps=0.003251305
Epoch 495: f=
                319.614, eps=0.003413870
Epoch 496: f=
                319.606, eps=0.003584564
Epoch 497: f=
                319.598, eps=0.003763792
Epoch 498: f=
                319.589, eps=0.003951982
Epoch 499: f=
                319.580, eps=0.004149581
Result after 500 epochs: f=319.5707412596371
```

```
Epoch
               3403.852, eps=0.010000000
        0: f=
Epoch
        1: f=
               1331.988, eps=0.010500000
Epoch
        2: f=
                815.117, eps=0.011025000
Epoch
        3: f=
                591.649, eps=0.011576250
Epoch
        4: f=
                542.541, eps=0.012155063
Epoch
        5: f=
                478.372, eps=0.012762816
Epoch
        6: f=
                507.782, eps=0.006381408
Epoch
        7: f=
                428.537, eps=0.006700478
Epoch
        8: f=
                399.056, eps=0.007035502
Epoch
        9: f=
                393.751, eps=0.007387277
      10: f=
                393.231, eps=0.007756641
Epoch
Epoch
       11: f=
                401.006, eps=0.003878321
                380.182, eps=0.004072237
Epoch
       12: f=
Epoch
      13: f=
                375.486, eps=0.004275848
Epoch
      14: f=
                373.767, eps=0.004489641
Epoch 15: f=
                372.284, eps=0.004714123
Epoch 16: f=
                370.875, eps=0.004949829
Epoch
      17: f=
                369.648, eps=0.005197320
      18: f=
Epoch
                368.528, eps=0.005457186
Epoch
                367.343, eps=0.005730046
       19: f=
Epoch
      20: f=
                366.827, eps=0.006016548
Epoch
      21: f=
                365.435, eps=0.006317375
Epoch 22: f=
                366.364, eps=0.003158688
Epoch 23: f=
                358.388, eps=0.003316622
                357.624, eps=0.003482453
Epoch
      24: f=
Epoch 25: f=
                356.865, eps=0.003656576
                356.097, eps=0.003839405
Epoch
      26: f=
Epoch
      27: f=
                355.315, eps=0.004031375
Epoch
      28: f=
                354.524, eps=0.004232944
Epoch 29: f=
                353.724, eps=0.004444591
Epoch 30: f=
                352.946, eps=0.004666820
Epoch
      31: f=
                352.195, eps=0.004900161
Epoch 32: f=
                351.667, eps=0.005145169
Epoch
      33: f=
                351.130, eps=0.005402428
      34: f=
Epoch
                351.489, eps=0.002701214
Epoch
      35: f=
                348.894, eps=0.002836275
Epoch
      36: f=
                348.381, eps=0.002978088
Epoch
                347.901, eps=0.003126993
      37: f=
Epoch
      38: f=
                347.410, eps=0.003283342
Epoch 39: f=
                346.906, eps=0.003447510
Epoch
      40: f=
                346.387, eps=0.003619885
Epoch
      41: f=
                345.853, eps=0.003800879
      42: f=
                345.305, eps=0.003990923
Epoch
Epoch
      43: f=
                344.742, eps=0.004190469
Epoch
      44: f=
                344.165, eps=0.004399993
Epoch
      45: f=
                343.576, eps=0.004619993
Epoch
      46: f=
                342.973, eps=0.004850992
      47: f=
                342.360, eps=0.005093542
Epoch
```

```
Epoch 48: f=
                341.739, eps=0.005348219
Epoch 49: f=
                341.115, eps=0.005615630
Epoch 50: f=
                340.501, eps=0.005896411
Epoch
      51: f=
                339.966, eps=0.006191232
Epoch 52: f=
                339.640, eps=0.006500794
Epoch 53: f=
                340.343, eps=0.003250397
Epoch
      54: f=
                338.242, eps=0.003412917
Epoch 55: f=
                337.889, eps=0.003583562
Epoch 56: f=
                337.562, eps=0.003762741
Epoch 57: f=
                337.233, eps=0.003950878
                336.901, eps=0.004148421
Epoch
      58: f=
Epoch 59: f=
                336.568, eps=0.004355843
                336.234, eps=0.004573635
Epoch
      60: f=
Epoch
      61: f=
                335.902, eps=0.004802316
Epoch 62: f=
                335.574, eps=0.005042432
Epoch 63: f=
                335.254, eps=0.005294554
Epoch 64: f=
                334.946, eps=0.005559282
Epoch
      65: f=
                334.658, eps=0.005837246
Epoch 66: f=
                334.416, eps=0.006129108
Epoch
                334.258, eps=0.006435563
      67: f=
Epoch
      68: f=
                334.501, eps=0.003217782
Epoch
      69: f=
                333.683, eps=0.003378671
Epoch 70: f=
                333.550, eps=0.003547604
Epoch 71: f=
                333.424, eps=0.003724984
Epoch 72: f=
                333.297, eps=0.003911234
Epoch 73: f=
                333.169, eps=0.004106795
Epoch
      74: f=
                333.040, eps=0.004312135
Epoch 75: f=
                332.909, eps=0.004527742
Epoch 76: f=
                332.777, eps=0.004754129
Epoch 77: f=
                332.643, eps=0.004991835
Epoch 78: f=
                332.507, eps=0.005241427
Epoch 79: f=
                332.369, eps=0.005503499
Epoch 80: f=
                332.230, eps=0.005778674
Epoch 81: f=
                332.089, eps=0.006067607
      82: f=
Epoch
                331.946, eps=0.006370988
Epoch
      83: f=
                331.801, eps=0.006689537
Epoch 84: f=
                331.655, eps=0.007024014
Epoch 85: f=
                331.511, eps=0.007375214
Epoch 86: f=
                331.382, eps=0.007743975
Epoch 87: f=
                331.352, eps=0.008131174
Epoch 88: f=
                331.865, eps=0.004065587
Epoch
      89: f=
                331.525, eps=0.004268866
      90: f=
                331.044, eps=0.004482310
Epoch
Epoch
      91: f=
                330.952, eps=0.004706425
Epoch 92: f=
                330.846, eps=0.004941746
Epoch
      93: f=
                330.798, eps=0.005188834
Epoch 94: f=
                330.742, eps=0.005448275
                330.804, eps=0.002724138
Epoch 95: f=
```

```
Epoch 96: f=
                330.443, eps=0.002860345
Epoch 97: f=
                330.394, eps=0.003003362
Epoch 98: f=
                330.348, eps=0.003153530
Epoch 99: f=
                330.300, eps=0.003311206
Epoch 100: f=
                330.250, eps=0.003476767
Epoch 101: f=
                330.198, eps=0.003650605
Epoch 102: f=
                330.144, eps=0.003833135
Epoch 103: f=
                330.088, eps=0.004024792
Epoch 104: f=
                330.031, eps=0.004226032
Epoch 105: f=
                329.971, eps=0.004437333
                329.910, eps=0.004659200
Epoch 106: f=
Epoch 107: f=
                329.846, eps=0.004892160
Epoch 108: f=
                329.780, eps=0.005136768
Epoch 109: f=
                329.713, eps=0.005393606
Epoch 110: f=
                329.643, eps=0.005663287
Epoch 111: f=
                329.570, eps=0.005946451
Epoch 112: f=
                329.496, eps=0.006243773
Epoch 113: f=
                329.419, eps=0.006555962
Epoch 114: f=
                329.340, eps=0.006883760
Epoch 115: f=
                329.259, eps=0.007227948
Epoch 116: f=
                329.175, eps=0.007589346
Epoch 117: f=
                329.089, eps=0.007968813
Epoch 118: f=
                329.001, eps=0.008367254
Epoch 119: f=
                328.910, eps=0.008785616
Epoch 120: f=
                328.817, eps=0.009224897
Epoch 121: f=
                328.722, eps=0.009686142
Epoch 122: f=
                328.635, eps=0.010170449
Epoch 123: f=
                328.661, eps=0.005085225
Epoch 124: f=
                328.617, eps=0.005339486
Epoch 125: f=
                328.703, eps=0.002669743
Epoch 126: f=
                328.396, eps=0.002803230
Epoch 127: f=
                328.369, eps=0.002943392
Epoch 128: f=
                328.341, eps=0.003090561
Epoch 129: f=
                328.312, eps=0.003245089
Epoch 130: f=
                328.282, eps=0.003407344
Epoch 131: f=
                328.250, eps=0.003577711
Epoch 132: f=
                328.218, eps=0.003756596
Epoch 133: f=
                328.183, eps=0.003944426
Epoch 134: f=
                328.148, eps=0.004141647
Epoch 135: f=
                328.111, eps=0.004348730
Epoch 136: f=
                328.072, eps=0.004566166
Epoch 137: f=
                328.032, eps=0.004794475
                327.990, eps=0.005034198
Epoch 138: f=
Epoch 139: f=
                327.946, eps=0.005285908
Epoch 140: f=
                327.901, eps=0.005550204
Epoch 141: f=
                327.854, eps=0.005827714
Epoch 142: f=
                327.805, eps=0.006119100
Epoch 143: f=
                327.754, eps=0.006425055
```

```
Epoch 144: f=
                327.701, eps=0.006746307
Epoch 145: f=
                327.646, eps=0.007083623
Epoch 146: f=
                327.589, eps=0.007437804
Epoch 147: f=
                327.530, eps=0.007809694
Epoch 148: f=
                327.468, eps=0.008200179
Epoch 149: f=
                327.405, eps=0.008610188
Epoch 150: f=
                327.339, eps=0.009040697
Epoch 151: f=
                327.274, eps=0.009492732
Epoch 152: f=
                327.240, eps=0.009967368
Epoch 153: f=
                327.569, eps=0.004983684
                327.808, eps=0.002491842
Epoch 154: f=
Epoch 155: f=
                327.108, eps=0.002616434
                327.054, eps=0.002747256
Epoch 156: f=
Epoch 157: f=
                327.034, eps=0.002884619
Epoch 158: f=
                327.013, eps=0.003028850
Epoch 159: f=
                326.991, eps=0.003180292
Epoch 160: f=
                326.969, eps=0.003339307
Epoch 161: f=
                326.945, eps=0.003506272
Epoch 162: f=
                326.921, eps=0.003681586
Epoch 163: f=
                326.895, eps=0.003865665
Epoch 164: f=
                326.868, eps=0.004058948
Epoch 165: f=
                326.840, eps=0.004261896
Epoch 166: f=
                326.811, eps=0.004474990
Epoch 167: f=
                326.780, eps=0.004698740
Epoch 168: f=
                326.748, eps=0.004933677
Epoch 169: f=
                326.714, eps=0.005180361
Epoch 170: f=
                326.680, eps=0.005439379
Epoch 171: f=
                326.643, eps=0.005711348
Epoch 172: f=
                326.605, eps=0.005996915
Epoch 173: f=
                326.566, eps=0.006296761
Epoch 174: f=
                326.524, eps=0.006611599
Epoch 175: f=
                326.481, eps=0.006942179
Epoch 176: f=
                326.437, eps=0.007289288
Epoch 177: f=
                326.390, eps=0.007653752
Epoch 178: f=
                326.341, eps=0.008036440
Epoch 179: f=
                326.291, eps=0.008438262
Epoch 180: f=
                326.238, eps=0.008860175
Epoch 181: f=
                326.184, eps=0.009303184
Epoch 182: f=
                326.131, eps=0.009768343
Epoch 183: f=
                326.115, eps=0.010256760
Epoch 184: f=
                326.575, eps=0.005128380
Epoch 185: f=
                326.972, eps=0.002564190
Epoch 186: f=
                326.019, eps=0.002692399
Epoch 187: f=
                325.946, eps=0.002827019
Epoch 188: f=
                325.928, eps=0.002968370
Epoch 189: f=
                325.911, eps=0.003116789
Epoch 190: f=
                325.892, eps=0.003272628
Epoch 191: f=
                325.873, eps=0.003436260
```

```
Epoch 192: f=
                325.853, eps=0.003608073
Epoch 193: f=
                325.832, eps=0.003788476
Epoch 194: f=
                325.810, eps=0.003977900
Epoch 195: f=
                325.788, eps=0.004176795
Epoch 196: f=
                325.764, eps=0.004385635
Epoch 197: f=
                325.739, eps=0.004604917
Epoch 198: f=
                325.712, eps=0.004835163
Epoch 199: f=
                325.685, eps=0.005076921
Epoch 200: f=
                325.656, eps=0.005330767
Epoch 201: f=
                325.627, eps=0.005597305
Epoch 202: f=
                325.595, eps=0.005877170
Epoch 203: f=
                325.563, eps=0.006171029
Epoch 204: f=
                325.529, eps=0.006479580
Epoch 205: f=
                325.493, eps=0.006803559
                325.456, eps=0.007143737
Epoch 206: f=
Epoch 207: f=
                325.417, eps=0.007500924
Epoch 208: f=
                325.377, eps=0.007875970
Epoch 209: f=
                325.335, eps=0.008269769
Epoch 210: f=
                325.292, eps=0.008683257
Epoch 211: f=
                325.252, eps=0.009117420
Epoch 212: f=
                325.267, eps=0.004558710
Epoch 213: f=
                325.229, eps=0.004786646
Epoch 214: f=
                325.228, eps=0.005025978
Epoch 215: f=
                325.217, eps=0.005277277
Epoch 216: f=
                325.285, eps=0.002638638
Epoch 217: f=
                325.082, eps=0.002770570
Epoch 218: f=
                325.068, eps=0.002909099
Epoch 219: f=
                325.053, eps=0.003054554
Epoch 220: f=
                325.037, eps=0.003207282
Epoch 221: f=
                325.021, eps=0.003367646
Epoch 222: f=
                325.004, eps=0.003536028
Epoch 223: f=
                324.986, eps=0.003712829
Epoch 224: f=
                324.967, eps=0.003898471
Epoch 225: f=
                324.948, eps=0.004093394
Epoch 226: f=
                324.927, eps=0.004298064
Epoch 227: f=
                324.906, eps=0.004512967
Epoch 228: f=
                324.883, eps=0.004738616
Epoch 229: f=
                324.860, eps=0.004975546
Epoch 230: f=
                324.835, eps=0.005224324
Epoch 231: f=
                324.810, eps=0.005485540
Epoch 232: f=
                324.783, eps=0.005759817
Epoch 233: f=
                324.755, eps=0.006047808
Epoch 234: f=
                324.725, eps=0.006350198
Epoch 235: f=
                324.695, eps=0.006667708
Epoch 236: f=
                324.663, eps=0.007001093
Epoch 237: f=
                324.629, eps=0.007351148
Epoch 238: f=
                324.594, eps=0.007718705
Epoch 239: f=
                324.558, eps=0.008104641
```

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Epoch 240: f=
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Epoch 241: f=
                324.480, eps=0.008935366
Epoch 242: f=
                324.438, eps=0.009382135
Epoch 243: f=
                324.396, eps=0.009851241
Epoch 244: f=
                324.365, eps=0.010343803
Epoch 245: f=
                324.506, eps=0.005171902
Epoch 246: f=
                324.672, eps=0.002585951
Epoch 247: f=
                324.271, eps=0.002715248
Epoch 248: f=
                324.255, eps=0.002851011
Epoch 249: f=
                324.242, eps=0.002993561
Epoch 250: f=
                324.229, eps=0.003143239
Epoch 251: f=
                324.215, eps=0.003300401
Epoch 252: f=
                324.200, eps=0.003465421
Epoch 253: f=
                324.185, eps=0.003638693
                324.169, eps=0.003820627
Epoch 254: f=
Epoch 255: f=
                324.152, eps=0.004011659
Epoch 256: f=
                324.134, eps=0.004212241
Epoch 257: f=
                324.115, eps=0.004422854
Epoch 258: f=
                324.096, eps=0.004643996
Epoch 259: f=
                324.076, eps=0.004876196
Epoch 260: f=
                324.054, eps=0.005120006
Epoch 261: f=
                324.032, eps=0.005376006
Epoch 262: f=
                324.009, eps=0.005644806
Epoch 263: f=
                323.984, eps=0.005927047
Epoch 264: f=
                323.959, eps=0.006223399
Epoch 265: f=
                323.932, eps=0.006534569
Epoch 266: f=
                323.904, eps=0.006861297
Epoch 267: f=
                323.875, eps=0.007204362
Epoch 268: f=
                323.844, eps=0.007564580
Epoch 269: f=
                323.813, eps=0.007942809
Epoch 270: f=
                323.780, eps=0.008339950
Epoch 271: f=
                323.746, eps=0.008756947
Epoch 272: f=
                323.725, eps=0.009194795
Epoch 273: f=
                323.828, eps=0.004597397
Epoch 274: f=
                323.767, eps=0.004827267
Epoch 275: f=
                323.811, eps=0.002413634
Epoch 276: f=
                323.623, eps=0.002534315
Epoch 277: f=
                323.612, eps=0.002661031
Epoch 278: f=
                323.601, eps=0.002794083
Epoch 279: f=
                323.590, eps=0.002933787
Epoch 280: f=
                323.578, eps=0.003080476
Epoch 281: f=
                323.565, eps=0.003234500
Epoch 282: f=
                323.552, eps=0.003396225
Epoch 283: f=
                323.538, eps=0.003566036
Epoch 284: f=
                323.524, eps=0.003744338
Epoch 285: f=
                323.509, eps=0.003931555
Epoch 286: f=
                323.493, eps=0.004128133
Epoch 287: f=
                323.477, eps=0.004334539
```

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Epoch 288: f=
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Epoch 289: f=
                323.442, eps=0.004778830
Epoch 290: f=
                323.423, eps=0.005017771
Epoch 291: f=
                323.403, eps=0.005268660
Epoch 292: f=
                323.382, eps=0.005532093
Epoch 293: f=
                323.361, eps=0.005808697
Epoch 294: f=
                323.338, eps=0.006099132
Epoch 295: f=
                323.314, eps=0.006404089
Epoch 296: f=
                323.289, eps=0.006724293
Epoch 297: f=
                323.263, eps=0.007060508
                323.236, eps=0.007413533
Epoch 298: f=
Epoch 299: f=
                323.208, eps=0.007784210
Epoch 300: f=
                323.178, eps=0.008173420
Epoch 301: f=
                323.147, eps=0.008582091
Epoch 302: f=
                323.115, eps=0.009011196
Epoch 303: f=
                323.081, eps=0.009461756
Epoch 304: f=
                323.047, eps=0.009934843
Epoch 305: f=
                323.028, eps=0.010431585
Epoch 306: f=
                323.214, eps=0.005215793
Epoch 307: f=
                323.232, eps=0.002607896
Epoch 308: f=
                322.966, eps=0.002738291
Epoch 309: f=
                322.933, eps=0.002875206
Epoch 310: f=
                322.922, eps=0.003018966
Epoch 311: f=
                322.911, eps=0.003169914
Epoch 312: f=
                322.899, eps=0.003328410
Epoch 313: f=
                322.887, eps=0.003494831
Epoch 314: f=
                322.874, eps=0.003669572
Epoch 315: f=
                322.861, eps=0.003853051
Epoch 316: f=
                322.847, eps=0.004045703
Epoch 317: f=
                322.833, eps=0.004247988
Epoch 318: f=
                322.818, eps=0.004460388
Epoch 319: f=
                322.802, eps=0.004683407
Epoch 320: f=
                322.785, eps=0.004917578
Epoch 321: f=
                322.767, eps=0.005163456
Epoch 322: f=
                322.749, eps=0.005421629
Epoch 323: f=
                322.730, eps=0.005692711
Epoch 324: f=
                322.710, eps=0.005977346
Epoch 325: f=
                322.689, eps=0.006276214
Epoch 326: f=
                322.667, eps=0.006590024
Epoch 327: f=
                322.644, eps=0.006919525
Epoch 328: f=
                322.620, eps=0.007265502
Epoch 329: f=
                322.595, eps=0.007628777
Epoch 330: f=
                322.570, eps=0.008010216
Epoch 331: f=
                322.551, eps=0.008410726
Epoch 332: f=
                322.587, eps=0.004205363
Epoch 333: f=
                322.543, eps=0.004415631
Epoch 334: f=
                322.533, eps=0.004636413
Epoch 335: f=
                322.516, eps=0.004868234
```

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Epoch 336: f=
                322.529, eps=0.002434117
Epoch 337: f=
                322.443, eps=0.002555823
Epoch 338: f=
                322.435, eps=0.002683614
Epoch 339: f=
                322.426, eps=0.002817794
Epoch 340: f=
                322.416, eps=0.002958684
Epoch 341: f=
                322.406, eps=0.003106618
Epoch 342: f=
                322.396, eps=0.003261949
Epoch 343: f=
                322.385, eps=0.003425047
Epoch 344: f=
                322.374, eps=0.003596299
Epoch 345: f=
                322.362, eps=0.003776114
Epoch 346: f=
                322.349, eps=0.003964920
Epoch 347: f=
                322.336, eps=0.004163166
Epoch 348: f=
                322.322, eps=0.004371324
Epoch 349: f=
                322.308, eps=0.004589890
Epoch 350: f=
                322.293, eps=0.004819385
Epoch 351: f=
                322.277, eps=0.005060354
Epoch 352: f=
                322.261, eps=0.005313372
Epoch 353: f=
                322.243, eps=0.005579040
Epoch 354: f=
                322.225, eps=0.005857992
Epoch 355: f=
                322.206, eps=0.006150892
Epoch 356: f=
                322.187, eps=0.006458437
Epoch 357: f=
                322.166, eps=0.006781358
Epoch 358: f=
                322.144, eps=0.007120426
Epoch 359: f=
                322.122, eps=0.007476448
Epoch 360: f=
                322.098, eps=0.007850270
Epoch 361: f=
                322.073, eps=0.008242783
Epoch 362: f=
                322.047, eps=0.008654923
Epoch 363: f=
                322.020, eps=0.009087669
Epoch 364: f=
                321.992, eps=0.009542052
Epoch 365: f=
                321.962, eps=0.010019155
Epoch 366: f=
                321.931, eps=0.010520113
Epoch 367: f=
                321.900, eps=0.011046118
Epoch 368: f=
                321.881, eps=0.011598424
Epoch 369: f=
                322.106, eps=0.005799212
Epoch 370: f=
                322.570, eps=0.002899606
Epoch 371: f=
                321.808, eps=0.003044586
Epoch 372: f=
                321.796, eps=0.003196816
Epoch 373: f=
                321.786, eps=0.003356656
Epoch 374: f=
                321.776, eps=0.003524489
Epoch 375: f=
                321.765, eps=0.003700714
Epoch 376: f=
                321.754, eps=0.003885749
Epoch 377: f=
                321.743, eps=0.004080037
Epoch 378: f=
                321.731, eps=0.004284039
Epoch 379: f=
                321.718, eps=0.004498241
Epoch 380: f=
                321.705, eps=0.004723153
Epoch 381: f=
                321.691, eps=0.004959310
Epoch 382: f=
                321.676, eps=0.005207276
Epoch 383: f=
                321.661, eps=0.005467640
```

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Epoch 384: f=
                321.645, eps=0.005741022
Epoch 385: f=
                321.628, eps=0.006028073
Epoch 386: f=
                321.611, eps=0.006329476
Epoch 387: f=
                321.593, eps=0.006645950
Epoch 388: f=
                321.574, eps=0.006978248
Epoch 389: f=
                321.557, eps=0.007327160
Epoch 390: f=
                321.552, eps=0.007693518
Epoch 391: f=
                321.631, eps=0.003846759
Epoch 392: f=
                321.541, eps=0.004039097
Epoch 393: f=
                321.522, eps=0.004241052
Epoch 394: f=
                321.500, eps=0.004453104
Epoch 395: f=
                321.492, eps=0.004675760
Epoch 396: f=
                321.482, eps=0.004909548
Epoch 397: f=
                321.488, eps=0.002454774
Epoch 398: f=
                321.430, eps=0.002577512
Epoch 399: f=
                321.423, eps=0.002706388
Epoch 400: f=
                321.415, eps=0.002841708
Epoch 401: f=
                321.407, eps=0.002983793
Epoch 402: f=
                321.399, eps=0.003132983
Epoch 403: f=
                321.390, eps=0.003289632
Epoch 404: f=
                321.381, eps=0.003454113
Epoch 405: f=
                321.372, eps=0.003626819
Epoch 406: f=
                321.362, eps=0.003808160
Epoch 407: f=
                321.351, eps=0.003998568
Epoch 408: f=
                321.340, eps=0.004198496
Epoch 409: f=
                321.329, eps=0.004408421
Epoch 410: f=
                321.317, eps=0.004628842
Epoch 411: f=
                321.304, eps=0.004860284
Epoch 412: f=
                321.291, eps=0.005103298
Epoch 413: f=
                321.277, eps=0.005358463
Epoch 414: f=
                321.262, eps=0.005626387
Epoch 415: f=
                321.247, eps=0.005907706
Epoch 416: f=
                321.231, eps=0.006203091
Epoch 417: f=
                321.215, eps=0.006513246
Epoch 418: f=
                321.197, eps=0.006838908
Epoch 419: f=
                321.179, eps=0.007180853
Epoch 420: f=
                321.160, eps=0.007539896
Epoch 421: f=
                321.140, eps=0.007916891
Epoch 422: f=
                321.119, eps=0.008312735
Epoch 423: f=
                321.097, eps=0.008728372
Epoch 424: f=
                321.074, eps=0.009164791
Epoch 425: f=
                321.052, eps=0.009623030
Epoch 426: f=
                321.038, eps=0.010104182
Epoch 427: f=
                321.157, eps=0.005052091
Epoch 428: f=
                321.177, eps=0.002526045
Epoch 429: f=
                320.992, eps=0.002652348
Epoch 430: f=
                320.974, eps=0.002784965
Epoch 431: f=
                320.966, eps=0.002924213
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Epoch 432: f=
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Epoch 433: f=
                320.951, eps=0.003223945
Epoch 434: f=
                320.943, eps=0.003385142
Epoch 435: f=
                320.934, eps=0.003554400
Epoch 436: f=
                320.925, eps=0.003732120
Epoch 437: f=
                320.916, eps=0.003918726
Epoch 438: f=
                320.906, eps=0.004114662
Epoch 439: f=
                320.896, eps=0.004320395
Epoch 440: f=
                320.885, eps=0.004536415
Epoch 441: f=
                320.874, eps=0.004763235
Epoch 442: f=
                320.862, eps=0.005001397
Epoch 443: f=
                320.849, eps=0.005251467
Epoch 444: f=
                320.836, eps=0.005514040
Epoch 445: f=
                320.823, eps=0.005789742
Epoch 446: f=
                320.808, eps=0.006079230
Epoch 447: f=
                320.793, eps=0.006383191
Epoch 448: f=
                320.778, eps=0.006702351
Epoch 449: f=
                320.761, eps=0.007037468
Epoch 450: f=
                320.744, eps=0.007389342
Epoch 451: f=
                320.726, eps=0.007758809
Epoch 452: f=
                320.708, eps=0.008146749
Epoch 453: f=
                320.694, eps=0.008554086
Epoch 454: f=
                320.720, eps=0.004277043
Epoch 455: f=
                320.713, eps=0.004490895
Epoch 456: f=
                320.696, eps=0.004715440
Epoch 457: f=
                320.709, eps=0.002357720
Epoch 458: f=
                320.630, eps=0.002475606
Epoch 459: f=
                320.624, eps=0.002599386
Epoch 460: f=
                320.617, eps=0.002729356
Epoch 461: f=
                320.611, eps=0.002865824
Epoch 462: f=
                320.604, eps=0.003009115
Epoch 463: f=
                320.597, eps=0.003159570
Epoch 464: f=
                320.590, eps=0.003317549
Epoch 465: f=
                320.582, eps=0.003483426
Epoch 466: f=
                320.574, eps=0.003657598
Epoch 467: f=
                320.565, eps=0.003840478
Epoch 468: f=
                320.556, eps=0.004032501
Epoch 469: f=
                320.547, eps=0.004234127
Epoch 470: f=
                320.537, eps=0.004445833
Epoch 471: f=
                320.527, eps=0.004668125
Epoch 472: f=
                320.516, eps=0.004901531
Epoch 473: f=
                320.505, eps=0.005146607
Epoch 474: f=
                320.493, eps=0.005403938
Epoch 475: f=
                320.480, eps=0.005674135
Epoch 476: f=
                320.467, eps=0.005957841
Epoch 477: f=
                320.454, eps=0.006255733
Epoch 478: f=
                320.439, eps=0.006568520
                320.424, eps=0.006896946
Epoch 479: f=
```

```
Epoch 480: f=
                320.409, eps=0.007241793
Epoch 481: f=
                320.392, eps=0.007603883
Epoch 482: f=
                320.375, eps=0.007984077
Epoch 483: f=
                320.358, eps=0.008383281
Epoch 484: f=
                320.339, eps=0.008802445
Epoch 485: f=
                320.319, eps=0.009242567
Epoch 486: f=
                320.299, eps=0.009704696
Epoch 487: f=
                320.278, eps=0.010189930
Epoch 488: f=
                320.258, eps=0.010699427
Epoch 489: f=
                320.275, eps=0.005349713
Epoch 490: f=
                320.319, eps=0.002674857
Epoch 491: f=
                320.216, eps=0.002808600
Epoch 492: f=
                320.209, eps=0.002949030
Epoch 493: f=
                320.202, eps=0.003096481
Epoch 494: f=
                320.196, eps=0.003251305
Epoch 495: f=
                320.189, eps=0.003413870
Epoch 496: f=
                320.181, eps=0.003584564
Epoch 497: f=
                320.174, eps=0.003763792
Epoch 498: f=
                320.166, eps=0.003951982
                320.157, eps=0.004149581
Epoch 499: f=
Result after 500 epochs: f=320.1482561851763
Epoch
        0: f=
               3406.872, eps=0.010000000
Epoch
        1: f=
               1336.651, eps=0.010500000
Epoch
        2: f=
                818.017, eps=0.011025000
Epoch
        3: f=
                594.169, eps=0.011576250
        4: f=
                545.052, eps=0.012155063
Epoch
        5: f=
                481.039, eps=0.012762816
Epoch
Epoch
        6: f=
                510.863, eps=0.006381408
Epoch
        7: f=
                430.499, eps=0.006700478
        8: f=
                400.757, eps=0.007035502
Epoch
Epoch
        9: f=
                395.242, eps=0.007387277
       10: f=
                394.469, eps=0.007756641
Epoch
Epoch
       11: f=
                402.487, eps=0.003878321
Epoch
       12: f=
                381.671, eps=0.004072237
       13: f=
                377.206, eps=0.004275848
Epoch
Epoch
       14: f=
                375.472, eps=0.004489641
Epoch
       15: f=
                373.954, eps=0.004714123
Epoch
       16: f=
                372.547, eps=0.004949829
Epoch
      17: f=
                371.279, eps=0.005197320
                370.187, eps=0.005457186
Epoch
      18: f=
Epoch
      19: f=
                368.944, eps=0.005730046
Epoch
       20: f=
                368.487, eps=0.006016548
Epoch
       21: f=
                367.012, eps=0.006317375
Epoch
      22: f=
                368.054, eps=0.003158688
Epoch
      23: f=
                359.953, eps=0.003316622
Epoch
       24: f=
                359.177, eps=0.003482453
Epoch
      25: f=
                358.409, eps=0.003656576
                357.635, eps=0.003839405
Epoch
      26: f=
```

```
Epoch 27: f=
                356.846, eps=0.004031375
Epoch
      28: f=
                356.053, eps=0.004232944
Epoch
      29: f=
                355.252, eps=0.004444591
                354.487, eps=0.004666820
Epoch
      30: f=
Epoch
      31: f=
                353.756, eps=0.004900161
Epoch
      32: f=
                353.304, eps=0.005145169
Epoch
      33: f=
                352.751, eps=0.005402428
Epoch 34: f=
                353.174, eps=0.002701214
Epoch 35: f=
                350.391, eps=0.002836275
Epoch 36: f=
                349.866, eps=0.002978088
                349.385, eps=0.003126993
Epoch
      37: f=
Epoch 38: f=
                348.895, eps=0.003283342
                348.392, eps=0.003447510
Epoch
      39: f=
Epoch
      40: f=
                347.875, eps=0.003619885
Epoch 41: f=
                347.345, eps=0.003800879
Epoch 42: f=
                346.800, eps=0.003990923
Epoch 43: f=
                346.242, eps=0.004190469
Epoch
      44: f=
                345.671, eps=0.004399993
                345.088, eps=0.004619993
Epoch
      45: f=
Epoch
                344.494, eps=0.004850992
      46: f=
Epoch
      47: f=
                343.892, eps=0.005093542
Epoch 48: f=
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      53: f=
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      54: f=
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Epoch 59: f=
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      61: f=
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      62: f=
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Epoch 63: f=
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      65: f=
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      69: f=
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      70: f=
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      71: f=
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      72: f=
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      73: f=
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      78: f=
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      79: f=
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      80: f=
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      81: f=
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      82: f=
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      87: f=
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      88: f=
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      92: f=
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Epoch 93: f=
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      95: f=
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Epoch 387: f=
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Epoch 388: f=
                325.907, eps=0.006978248
Epoch 389: f=
                325.894, eps=0.007327160
Epoch 390: f=
                325.886, eps=0.007693518
Epoch 391: f=
                325.900, eps=0.003846759
Epoch 392: f=
                325.881, eps=0.004039097
Epoch 393: f=
                325.864, eps=0.004241052
Epoch 394: f=
                325.855, eps=0.004453104
Epoch 395: f=
                325.846, eps=0.004675760
Epoch 396: f=
                325.841, eps=0.004909548
Epoch 397: f=
                325.838, eps=0.005155025
Epoch 398: f=
                325.845, eps=0.002577512
Epoch 399: f=
                325.805, eps=0.002706388
Epoch 400: f=
                325.800, eps=0.002841708
Epoch 401: f=
                325.795, eps=0.002983793
Epoch 402: f=
                325.789, eps=0.003132983
Epoch 403: f=
                325.784, eps=0.003289632
Epoch 404: f=
                325.778, eps=0.003454113
Epoch 405: f=
                325.772, eps=0.003626819
Epoch 406: f=
                325.766, eps=0.003808160
Epoch 407: f=
                325.759, eps=0.003998568
Epoch 408: f=
                325.752, eps=0.004198496
Epoch 409: f=
                325.745, eps=0.004408421
Epoch 410: f=
                325.737, eps=0.004628842
```

```
Epoch 411: f=
                325.729, eps=0.004860284
Epoch 412: f=
                325.721, eps=0.005103298
Epoch 413: f=
                325.712, eps=0.005358463
Epoch 414: f=
                325.703, eps=0.005626387
Epoch 415: f=
                325.693, eps=0.005907706
Epoch 416: f=
                325.683, eps=0.006203091
Epoch 417: f=
                325.673, eps=0.006513246
Epoch 418: f=
                325.662, eps=0.006838908
Epoch 419: f=
                325.650, eps=0.007180853
Epoch 420: f=
                325.639, eps=0.007539896
Epoch 421: f=
                325.626, eps=0.007916891
Epoch 422: f=
                325.613, eps=0.008312735
Epoch 423: f=
                325.600, eps=0.008728372
Epoch 424: f=
                325.592, eps=0.009164791
Epoch 425: f=
                325.638, eps=0.004582395
Epoch 426: f=
                325.653, eps=0.002291198
Epoch 427: f=
                325.560, eps=0.002405758
Epoch 428: f=
                325.556, eps=0.002526045
Epoch 429: f=
                325.552, eps=0.002652348
Epoch 430: f=
                325.548, eps=0.002784965
Epoch 431: f=
                325.543, eps=0.002924213
Epoch 432: f=
                325.539, eps=0.003070424
Epoch 433: f=
                325.534, eps=0.003223945
Epoch 434: f=
                325.529, eps=0.003385142
Epoch 435: f=
                325.523, eps=0.003554400
Epoch 436: f=
                325.518, eps=0.003732120
Epoch 437: f=
                325.512, eps=0.003918726
Epoch 438: f=
                325.506, eps=0.004114662
Epoch 439: f=
                325.500, eps=0.004320395
Epoch 440: f=
                325.493, eps=0.004536415
Epoch 441: f=
                325.486, eps=0.004763235
Epoch 442: f=
                325.479, eps=0.005001397
Epoch 443: f=
                325.471, eps=0.005251467
Epoch 444: f=
                325.463, eps=0.005514040
Epoch 445: f=
                325.455, eps=0.005789742
Epoch 446: f=
                325.446, eps=0.006079230
Epoch 447: f=
                325.437, eps=0.006383191
Epoch 448: f=
                325.427, eps=0.006702351
Epoch 449: f=
                325.417, eps=0.007037468
Epoch 450: f=
                325.407, eps=0.007389342
Epoch 451: f=
                325.396, eps=0.007758809
Epoch 452: f=
                325.385, eps=0.008146749
Epoch 453: f=
                325.373, eps=0.008554086
Epoch 454: f=
                325.360, eps=0.008981791
                325.347, eps=0.009430880
Epoch 455: f=
Epoch 456: f=
                325.334, eps=0.009902424
Epoch 457: f=
                325.320, eps=0.010397546
                325.307, eps=0.010917423
Epoch 458: f=
```

```
Epoch 459: f=
                325.324, eps=0.005458711
Epoch 460: f=
                325.348, eps=0.002729356
Epoch 461: f=
                325.285, eps=0.002865824
Epoch 462: f=
                325.275, eps=0.003009115
Epoch 463: f=
                325.271, eps=0.003159570
Epoch 464: f=
                325.266, eps=0.003317549
Epoch 465: f=
                325.262, eps=0.003483426
Epoch 466: f=
                325.257, eps=0.003657598
Epoch 467: f=
                325.252, eps=0.003840478
Epoch 468: f=
                325.247, eps=0.004032501
                325.241, eps=0.004234127
Epoch 469: f=
Epoch 470: f=
                325.236, eps=0.004445833
Epoch 471: f=
                325.230, eps=0.004668125
Epoch 472: f=
                325.223, eps=0.004901531
Epoch 473: f=
                325.217, eps=0.005146607
Epoch 474: f=
                325.210, eps=0.005403938
Epoch 475: f=
                325.203, eps=0.005674135
Epoch 476: f=
                325.195, eps=0.005957841
Epoch 477: f=
                325.187, eps=0.006255733
Epoch 478: f=
                325.179, eps=0.006568520
Epoch 479: f=
                325.171, eps=0.006896946
Epoch 480: f=
                325.162, eps=0.007241793
Epoch 481: f=
                325.155, eps=0.007603883
Epoch 482: f=
                325.159, eps=0.003801941
Epoch 483: f=
                325.148, eps=0.003992039
Epoch 484: f=
                325.139, eps=0.004191640
Epoch 485: f=
                325.133, eps=0.004401222
Epoch 486: f=
                325.127, eps=0.004621284
Epoch 487: f=
                325.122, eps=0.004852348
                325.118, eps=0.005094965
Epoch 488: f=
Epoch 489: f=
                325.119, eps=0.002547483
Epoch 490: f=
                325.101, eps=0.002674857
Epoch 491: f=
                325.097, eps=0.002808600
Epoch 492: f=
                325.094, eps=0.002949030
Epoch 493: f=
                325.090, eps=0.003096481
Epoch 494: f=
                325.086, eps=0.003251305
Epoch 495: f=
                325.082, eps=0.003413870
Epoch 496: f=
                325.078, eps=0.003584564
Epoch 497: f=
                325.073, eps=0.003763792
Epoch 498: f=
                325.069, eps=0.003951982
Epoch 499: f=
                325.064, eps=0.004149581
Result after 500 epochs: f=325.0589707546104
               3420.297, eps=0.010000000
Epoch
        0: f=
Epoch
        1: f=
               1357.315, eps=0.010500000
        2: f=
                830.666, eps=0.011025000
Epoch
Epoch
        3: f=
                605.028, eps=0.011576250
Epoch
        4: f=
                555.800, eps=0.012155063
                492.418, eps=0.012762816
Epoch
        5: f=
```

```
Epoch
        6: f=
                523.818, eps=0.006381408
Epoch
       7: f=
                438.739, eps=0.006700478
Epoch
       8: f=
                407.741, eps=0.007035502
Epoch
        9: f=
                401.463, eps=0.007387277
Epoch
      10: f=
                397.962, eps=0.007756641
                405.507, eps=0.003878321
Epoch
       11: f=
Epoch
      12: f=
                386.305, eps=0.004072237
Epoch
      13: f=
                383.879, eps=0.004275848
Epoch 14: f=
                382.163, eps=0.004489641
Epoch 15: f=
                380.567, eps=0.004714123
                379.223, eps=0.004949829
Epoch 16: f=
Epoch 17: f=
                377.763, eps=0.005197320
Epoch
      18: f=
                376.830, eps=0.005457186
Epoch
      19: f=
                375.254, eps=0.005730046
Epoch 20: f=
                375.094, eps=0.006016548
Epoch 21: f=
                373.183, eps=0.006317375
Epoch 22: f=
                374.766, eps=0.003158688
                366.097, eps=0.003316622
Epoch
      23: f=
Epoch 24: f=
                365.264, eps=0.003482453
Epoch
      25: f=
                364.448, eps=0.003656576
Epoch
      26: f=
                363.644, eps=0.003839405
Epoch 27: f=
                362.826, eps=0.004031375
Epoch 28: f=
                362.031, eps=0.004232944
Epoch 29: f=
                361.236, eps=0.004444591
                360.570, eps=0.004666820
Epoch 30: f=
Epoch 31: f=
                359.908, eps=0.004900161
Epoch
      32: f=
                359.753, eps=0.005145169
Epoch
      33: f=
                358.988, eps=0.005402428
Epoch 34: f=
                359.503, eps=0.002701214
Epoch 35: f=
                356.160, eps=0.002836275
Epoch 36: f=
                355.627, eps=0.002978088
Epoch 37: f=
                355.147, eps=0.003126993
Epoch 38: f=
                354.662, eps=0.003283342
Epoch
      39: f=
                354.168, eps=0.003447510
Epoch
      40: f=
                353.662, eps=0.003619885
Epoch
      41: f=
                353.147, eps=0.003800879
Epoch 42: f=
                352.621, eps=0.003990923
Epoch 43: f=
                352.087, eps=0.004190469
Epoch 44: f=
                351.546, eps=0.004399993
Epoch 45: f=
                350.998, eps=0.004619993
Epoch 46: f=
                350.447, eps=0.004850992
Epoch
      47: f=
                349.896, eps=0.005093542
                349.355, eps=0.005348219
Epoch
      48: f=
Epoch
      49: f=
                348.857, eps=0.005615630
Epoch 50: f=
                348.477, eps=0.005896411
Epoch
      51: f=
                348.626, eps=0.002948206
Epoch 52: f=
                347.415, eps=0.003095616
                347.151, eps=0.003250397
Epoch 53: f=
```

```
Epoch 54: f=
                346.888, eps=0.003412917
Epoch 55: f=
                346.624, eps=0.003583562
Epoch
      56: f=
                346.359, eps=0.003762741
                346.096, eps=0.003950878
Epoch
      57: f=
Epoch
      58: f=
                345.836, eps=0.004148421
Epoch
      59: f=
                345.579, eps=0.004355843
Epoch
      60: f=
                345.329, eps=0.004573635
Epoch 61: f=
                345.085, eps=0.004802316
Epoch 62: f=
                344.850, eps=0.005042432
Epoch
      63: f=
                344.624, eps=0.005294554
                344.407, eps=0.005559282
Epoch
      64: f=
Epoch
      65: f=
                344.200, eps=0.005837246
                344.006, eps=0.006129108
Epoch
      66: f=
Epoch
      67: f=
                343.843, eps=0.006435563
Epoch
      68: f=
                343.780, eps=0.006757341
Epoch 69: f=
                344.223, eps=0.003378671
Epoch 70: f=
                343.365, eps=0.003547604
Epoch
      71: f=
                343.264, eps=0.003724984
      72: f=
Epoch
                343.172, eps=0.003911234
Epoch
                343.081, eps=0.004106795
      73: f=
Epoch
      74: f=
                342.990, eps=0.004312135
Epoch 75: f=
                342.899, eps=0.004527742
Epoch 76: f=
                342.807, eps=0.004754129
Epoch 77: f=
                342.716, eps=0.004991835
                342.627, eps=0.005241427
Epoch 78: f=
Epoch 79: f=
                342.546, eps=0.005503499
Epoch 80: f=
                342.482, eps=0.005778674
Epoch
      81: f=
                342.505, eps=0.002889337
Epoch 82: f=
                342.284, eps=0.003033804
Epoch 83: f=
                342.232, eps=0.003185494
Epoch 84: f=
                342.182, eps=0.003344768
Epoch
      85: f=
                342.131, eps=0.003512007
Epoch 86: f=
                342.079, eps=0.003687607
                342.026, eps=0.003871988
Epoch
      87: f=
      88: f=
Epoch
                341.971, eps=0.004065587
Epoch
      89: f=
                341.915, eps=0.004268866
Epoch 90: f=
                341.858, eps=0.004482310
Epoch 91: f=
                341.800, eps=0.004706425
Epoch 92: f=
                341.740, eps=0.004941746
Epoch 93: f=
                341.679, eps=0.005188834
Epoch 94: f=
                341.618, eps=0.005448275
Epoch
      95: f=
                341.555, eps=0.005720689
                341.491, eps=0.006006724
Epoch
      96: f=
Epoch
      97: f=
                341.426, eps=0.006307060
Epoch
      98: f=
                341.362, eps=0.006622413
Epoch 99: f=
                341.299, eps=0.006953533
Epoch 100: f=
                341.252, eps=0.007301210
Epoch 101: f=
                341.295, eps=0.003650605
```

```
Epoch 102: f=
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Epoch 103: f=
                341.109, eps=0.004024792
Epoch 104: f=
                341.066, eps=0.004226032
Epoch 105: f=
                341.029, eps=0.004437333
Epoch 106: f=
                340.991, eps=0.004659200
Epoch 107: f=
                340.955, eps=0.004892160
Epoch 108: f=
                340.920, eps=0.005136768
Epoch 109: f=
                340.890, eps=0.005393606
Epoch 110: f=
                340.870, eps=0.005663287
Epoch 111: f=
                340.893, eps=0.002831643
Epoch 112: f=
                340.766, eps=0.002973225
Epoch 113: f=
                340.741, eps=0.003121887
Epoch 114: f=
                340.719, eps=0.003277981
Epoch 115: f=
                340.696, eps=0.003441880
Epoch 116: f=
                340.672, eps=0.003613974
Epoch 117: f=
                340.648, eps=0.003794673
Epoch 118: f=
                340.622, eps=0.003984406
Epoch 119: f=
                340.596, eps=0.004183627
Epoch 120: f=
                340.569, eps=0.004392808
Epoch 121: f=
                340.541, eps=0.004612449
Epoch 122: f=
                340.513, eps=0.004843071
Epoch 123: f=
                340.483, eps=0.005085225
Epoch 124: f=
                340.453, eps=0.005339486
Epoch 125: f=
                340.421, eps=0.005606460
Epoch 126: f=
                340.389, eps=0.005886783
                340.356, eps=0.006181122
Epoch 127: f=
Epoch 128: f=
                340.322, eps=0.006490178
Epoch 129: f=
                340.287, eps=0.006814687
Epoch 130: f=
                340.252, eps=0.007155422
Epoch 131: f=
                340.216, eps=0.007513193
Epoch 132: f=
                340.183, eps=0.007888852
Epoch 133: f=
                340.175, eps=0.008283295
Epoch 134: f=
                340.351, eps=0.004141647
Epoch 135: f=
                340.241, eps=0.004348730
Epoch 136: f=
                340.170, eps=0.004566166
Epoch 137: f=
                340.146, eps=0.004794475
Epoch 138: f=
                340.141, eps=0.005034198
Epoch 139: f=
                340.165, eps=0.002517099
Epoch 140: f=
                339.990, eps=0.002642954
Epoch 141: f=
                339.975, eps=0.002775102
Epoch 142: f=
                339.963, eps=0.002913857
Epoch 143: f=
                339.951, eps=0.003059550
                339.938, eps=0.003212527
Epoch 144: f=
Epoch 145: f=
                339.925, eps=0.003373154
Epoch 146: f=
                339.911, eps=0.003541811
Epoch 147: f=
                339.897, eps=0.003718902
Epoch 148: f=
                339.882, eps=0.003904847
Epoch 149: f=
                339.867, eps=0.004100089
```

```
Epoch 150: f=
                339.851, eps=0.004305094
Epoch 151: f=
                339.834, eps=0.004520348
Epoch 152: f=
                339.817, eps=0.004746366
                339.800, eps=0.004983684
Epoch 153: f=
Epoch 154: f=
                339.781, eps=0.005232868
Epoch 155: f=
                339.762, eps=0.005494512
Epoch 156: f=
                339.742, eps=0.005769237
Epoch 157: f=
                339.722, eps=0.006057699
Epoch 158: f=
                339.701, eps=0.006360584
Epoch 159: f=
                339.679, eps=0.006678613
                339.657, eps=0.007012544
Epoch 160: f=
Epoch 161: f=
                339.634, eps=0.007363171
Epoch 162: f=
                339.610, eps=0.007731330
Epoch 163: f=
                339.586, eps=0.008117896
Epoch 164: f=
                339.561, eps=0.008523791
Epoch 165: f=
                339.535, eps=0.008949981
Epoch 166: f=
                339.509, eps=0.009397480
Epoch 167: f=
                339.489, eps=0.009867354
Epoch 168: f=
                339.540, eps=0.004933677
Epoch 169: f=
                339.541, eps=0.002466838
Epoch 170: f=
                339.435, eps=0.002590180
Epoch 171: f=
                339.426, eps=0.002719689
Epoch 172: f=
                339.419, eps=0.002855674
Epoch 173: f=
                339.411, eps=0.002998458
Epoch 174: f=
                339.403, eps=0.003148380
                339.395, eps=0.003305799
Epoch 175: f=
Epoch 176: f=
                339.386, eps=0.003471089
Epoch 177: f=
                339.377, eps=0.003644644
Epoch 178: f=
                339.368, eps=0.003826876
Epoch 179: f=
                339.358, eps=0.004018220
Epoch 180: f=
                339.348, eps=0.004219131
Epoch 181: f=
                339.337, eps=0.004430087
Epoch 182: f=
                339.326, eps=0.004651592
Epoch 183: f=
                339.315, eps=0.004884171
Epoch 184: f=
                339.303, eps=0.005128380
Epoch 185: f=
                339.291, eps=0.005384799
Epoch 186: f=
                339.278, eps=0.005654039
Epoch 187: f=
                339.265, eps=0.005936741
Epoch 188: f=
                339.251, eps=0.006233578
Epoch 189: f=
                339.237, eps=0.006545257
Epoch 190: f=
                339.222, eps=0.006872520
Epoch 191: f=
                339.207, eps=0.007216146
                339.191, eps=0.007576953
Epoch 192: f=
Epoch 193: f=
                339.175, eps=0.007955801
                339.158, eps=0.008353591
Epoch 194: f=
Epoch 195: f=
                339.141, eps=0.008771270
Epoch 196: f=
                339.123, eps=0.009209834
Epoch 197: f=
                339.105, eps=0.009670325
```

```
Epoch 198: f=
                339.092, eps=0.010153842
Epoch 199: f=
                339.138, eps=0.005076921
Epoch 200: f=
                339.180, eps=0.002538460
Epoch 201: f=
                339.052, eps=0.002665383
Epoch 202: f=
                339.047, eps=0.002798653
Epoch 203: f=
                339.042, eps=0.002938585
Epoch 204: f=
                339.037, eps=0.003085514
Epoch 205: f=
                339.031, eps=0.003239790
Epoch 206: f=
                339.025, eps=0.003401780
Epoch 207: f=
                339.019, eps=0.003571869
Epoch 208: f=
                339.013, eps=0.003750462
Epoch 209: f=
                339.006, eps=0.003937985
Epoch 210: f=
                338.999, eps=0.004134885
Epoch 211: f=
                338.992, eps=0.004341629
Epoch 212: f=
                338.985, eps=0.004558710
Epoch 213: f=
                338.977, eps=0.004786646
Epoch 214: f=
                338.969, eps=0.005025978
Epoch 215: f=
                338.961, eps=0.005277277
Epoch 216: f=
                338.952, eps=0.005541141
Epoch 217: f=
                338.943, eps=0.005818198
Epoch 218: f=
                338.933, eps=0.006109108
Epoch 219: f=
                338.924, eps=0.006414563
Epoch 220: f=
                338.914, eps=0.006735291
Epoch 221: f=
                338.903, eps=0.007072056
Epoch 222: f=
                338.892, eps=0.007425659
Epoch 223: f=
                338.881, eps=0.007796941
Epoch 224: f=
                338.869, eps=0.008186788
Epoch 225: f=
                338.857, eps=0.008596128
Epoch 226: f=
                338.845, eps=0.009025934
Epoch 227: f=
                338.832, eps=0.009477231
Epoch 228: f=
                338.819, eps=0.009951093
Epoch 229: f=
                338.809, eps=0.010448647
Epoch 230: f=
                338.837, eps=0.005224324
Epoch 231: f=
                338.853, eps=0.002612162
Epoch 232: f=
                338.785, eps=0.002742770
Epoch 233: f=
                338.778, eps=0.002879908
Epoch 234: f=
                338.774, eps=0.003023904
Epoch 235: f=
                338.770, eps=0.003175099
Epoch 236: f=
                338.766, eps=0.003333854
Epoch 237: f=
                338.762, eps=0.003500547
Epoch 238: f=
                338.758, eps=0.003675574
Epoch 239: f=
                338.753, eps=0.003859353
Epoch 240: f=
                338.748, eps=0.004052320
Epoch 241: f=
                338.743, eps=0.004254936
Epoch 242: f=
                338.738, eps=0.004467683
Epoch 243: f=
                338.733, eps=0.004691067
Epoch 244: f=
                338.727, eps=0.004925621
Epoch 245: f=
                338.721, eps=0.005171902
```

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Epoch 246: f=
                338.715, eps=0.005430497
Epoch 247: f=
                338.709, eps=0.005702022
Epoch 248: f=
                338.702, eps=0.005987123
Epoch 249: f=
                338.695, eps=0.006286479
Epoch 250: f=
                338.688, eps=0.006600803
Epoch 251: f=
                338.681, eps=0.006930843
Epoch 252: f=
                338.673, eps=0.007277385
Epoch 253: f=
                338.665, eps=0.007641254
Epoch 254: f=
                338.657, eps=0.008023317
Epoch 255: f=
                338.649, eps=0.008424483
Epoch 256: f=
                338.642, eps=0.008845707
Epoch 257: f=
                338.650, eps=0.004422854
Epoch 258: f=
                338.646, eps=0.004643996
Epoch 259: f=
                338.641, eps=0.004876196
                338.645, eps=0.002438098
Epoch 260: f=
Epoch 261: f=
                338.615, eps=0.002560003
Epoch 262: f=
                338.612, eps=0.002688003
Epoch 263: f=
                338.610, eps=0.002822403
Epoch 264: f=
                338.607, eps=0.002963523
Epoch 265: f=
                338.604, eps=0.003111700
Epoch 266: f=
                338.601, eps=0.003267285
Epoch 267: f=
                338.598, eps=0.003430649
Epoch 268: f=
                338.595, eps=0.003602181
Epoch 269: f=
                338.591, eps=0.003782290
Epoch 270: f=
                338.588, eps=0.003971405
Epoch 271: f=
                338.584, eps=0.004169975
Epoch 272: f=
                338.580, eps=0.004378474
Epoch 273: f=
                338.576, eps=0.004597397
Epoch 274: f=
                338.572, eps=0.004827267
Epoch 275: f=
                338.568, eps=0.005068631
Epoch 276: f=
                338.563, eps=0.005322062
Epoch 277: f=
                338.559, eps=0.005588165
Epoch 278: f=
                338.554, eps=0.005867574
Epoch 279: f=
                338.549, eps=0.006160952
Epoch 280: f=
                338.544, eps=0.006469000
Epoch 281: f=
                338.538, eps=0.006792450
Epoch 282: f=
                338.532, eps=0.007132072
Epoch 283: f=
                338.527, eps=0.007488676
Epoch 284: f=
                338.521, eps=0.007863110
Epoch 285: f=
                338.514, eps=0.008256265
Epoch 286: f=
                338.508, eps=0.008669078
Epoch 287: f=
                338.501, eps=0.009102532
Epoch 288: f=
                338.494, eps=0.009557659
Epoch 289: f=
                338.487, eps=0.010035542
Epoch 290: f=
                338.480, eps=0.010537319
Epoch 291: f=
                338.476, eps=0.011064185
Epoch 292: f=
                338.530, eps=0.005532093
Epoch 293: f=
                338.578, eps=0.002766046
```

```
Epoch 294: f=
                338.470, eps=0.002904349
Epoch 295: f=
                338.457, eps=0.003049566
Epoch 296: f=
                338.454, eps=0.003202044
Epoch 297: f=
                338.452, eps=0.003362147
Epoch 298: f=
                338.450, eps=0.003530254
Epoch 299: f=
                338.447, eps=0.003706767
Epoch 300: f=
                338.445, eps=0.003892105
Epoch 301: f=
                338.442, eps=0.004086710
Epoch 302: f=
                338.440, eps=0.004291046
Epoch 303: f=
                338.437, eps=0.004505598
                338.434, eps=0.004730878
Epoch 304: f=
Epoch 305: f=
                338.431, eps=0.004967422
Epoch 306: f=
                338.428, eps=0.005215793
Epoch 307: f=
                338.424, eps=0.005476582
Epoch 308: f=
                338.421, eps=0.005750412
Epoch 309: f=
                338.417, eps=0.006037932
Epoch 310: f=
                338.414, eps=0.006339829
Epoch 311: f=
                338.410, eps=0.006656820
Epoch 312: f=
                338.406, eps=0.006989661
Epoch 313: f=
                338.402, eps=0.007339144
Epoch 314: f=
                338.399, eps=0.007706101
Epoch 315: f=
                338.402, eps=0.003853051
Epoch 316: f=
                338.396, eps=0.004045703
Epoch 317: f=
                338.391, eps=0.004247988
Epoch 318: f=
                338.388, eps=0.004460388
Epoch 319: f=
                338.386, eps=0.004683407
Epoch 320: f=
                338.384, eps=0.004917578
Epoch 321: f=
                338.382, eps=0.005163456
Epoch 322: f=
                338.382, eps=0.005421629
Epoch 323: f=
                338.384, eps=0.002710815
Epoch 324: f=
                338.372, eps=0.002846355
Epoch 325: f=
                338.370, eps=0.002988673
Epoch 326: f=
                338.368, eps=0.003138107
Epoch 327: f=
                338.366, eps=0.003295012
Epoch 328: f=
                338.365, eps=0.003459763
Epoch 329: f=
                338.363, eps=0.003632751
Epoch 330: f=
                338.361, eps=0.003814388
Epoch 331: f=
                338.359, eps=0.004005108
Epoch 332: f=
                338.357, eps=0.004205363
Epoch 333: f=
                338.355, eps=0.004415631
Epoch 334: f=
                338.352, eps=0.004636413
Epoch 335: f=
                338.350, eps=0.004868234
Epoch 336: f=
                338.348, eps=0.005111645
Epoch 337: f=
                338.345, eps=0.005367228
Epoch 338: f=
                338.343, eps=0.005635589
Epoch 339: f=
                338.340, eps=0.005917368
Epoch 340: f=
                338.337, eps=0.006213237
Epoch 341: f=
                338.334, eps=0.006523899
```

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Epoch 342: f=
                338.331, eps=0.006850094
Epoch 343: f=
                338.328, eps=0.007192598
Epoch 344: f=
                338.325, eps=0.007552228
Epoch 345: f=
                338.321, eps=0.007929840
Epoch 346: f=
                338.318, eps=0.008326332
Epoch 347: f=
                338.319, eps=0.004163166
Epoch 348: f=
                338.316, eps=0.004371324
Epoch 349: f=
                338.314, eps=0.004589890
Epoch 350: f=
                338.312, eps=0.004819385
Epoch 351: f=
                338.311, eps=0.005060354
Epoch 352: f=
                338.311, eps=0.002530177
Epoch 353: f=
                338.303, eps=0.002656686
Epoch 354: f=
                338.302, eps=0.002789520
Epoch 355: f=
                338.301, eps=0.002928996
Epoch 356: f=
                338.300, eps=0.003075446
Epoch 357: f=
                338.299, eps=0.003229218
Epoch 358: f=
                338.297, eps=0.003390679
Epoch 359: f=
                338.296, eps=0.003560213
Epoch 360: f=
                338.294, eps=0.003738224
Epoch 361: f=
                338.293, eps=0.003925135
Epoch 362: f=
                338.291, eps=0.004121392
Epoch 363: f=
                338.290, eps=0.004327461
Epoch 364: f=
                338.288, eps=0.004543834
Epoch 365: f=
                338.286, eps=0.004771026
Epoch 366: f=
                338.285, eps=0.005009577
Epoch 367: f=
                338.283, eps=0.005260056
Epoch 368: f=
                338.281, eps=0.005523059
Epoch 369: f=
                338.279, eps=0.005799212
Epoch 370: f=
                338.276, eps=0.006089173
Epoch 371: f=
                338.274, eps=0.006393631
Epoch 372: f=
                338.272, eps=0.006713313
Epoch 373: f=
                338.270, eps=0.007048978
Epoch 374: f=
                338.267, eps=0.007401427
Epoch 375: f=
                338.264, eps=0.007771499
Epoch 376: f=
                338.262, eps=0.008160074
Epoch 377: f=
                338.259, eps=0.008568077
Epoch 378: f=
                338.256, eps=0.008996481
Epoch 379: f=
                338.253, eps=0.009446305
Epoch 380: f=
                338.252, eps=0.009918621
Epoch 381: f=
                338.267, eps=0.004959310
Epoch 382: f=
                338.276, eps=0.002479655
Epoch 383: f=
                338.245, eps=0.002603638
Epoch 384: f=
                338.244, eps=0.002733820
Epoch 385: f=
                338.243, eps=0.002870511
Epoch 386: f=
                338.242, eps=0.003014036
Epoch 387: f=
                338.241, eps=0.003164738
Epoch 388: f=
                338.240, eps=0.003322975
Epoch 389: f=
                338.239, eps=0.003489124
```

```
Epoch 390: f=
                338.238, eps=0.003663580
Epoch 391: f=
                338.237, eps=0.003846759
Epoch 392: f=
                338.236, eps=0.004039097
Epoch 393: f=
                338.235, eps=0.004241052
Epoch 394: f=
                338.233, eps=0.004453104
Epoch 395: f=
                338.232, eps=0.004675760
Epoch 396: f=
                338.231, eps=0.004909548
Epoch 397: f=
                338.229, eps=0.005155025
Epoch 398: f=
                338.228, eps=0.005412776
Epoch 399: f=
                338.226, eps=0.005683415
                338.225, eps=0.005967586
Epoch 400: f=
Epoch 401: f=
                338.223, eps=0.006265965
Epoch 402: f=
                338.221, eps=0.006579263
Epoch 403: f=
                338.220, eps=0.006908226
Epoch 404: f=
                338.218, eps=0.007253638
Epoch 405: f=
                338.216, eps=0.007616320
Epoch 406: f=
                338.214, eps=0.007997136
Epoch 407: f=
                338.212, eps=0.008396992
Epoch 408: f=
                338.210, eps=0.008816842
Epoch 409: f=
                338.207, eps=0.009257684
Epoch 410: f=
                338.205, eps=0.009720568
Epoch 411: f=
                338.204, eps=0.010206597
Epoch 412: f=
                338.219, eps=0.005103298
Epoch 413: f=
                338.227, eps=0.002551649
Epoch 414: f=
                338.199, eps=0.002679232
Epoch 415: f=
                338.198, eps=0.002813193
Epoch 416: f=
                338.197, eps=0.002953853
Epoch 417: f=
                338.197, eps=0.003101546
Epoch 418: f=
                338.196, eps=0.003256623
Epoch 419: f=
                338.195, eps=0.003419454
Epoch 420: f=
                338.194, eps=0.003590427
Epoch 421: f=
                338.193, eps=0.003769948
Epoch 422: f=
                338.193, eps=0.003958445
Epoch 423: f=
                338.192, eps=0.004156368
Epoch 424: f=
                338.191, eps=0.004364186
Epoch 425: f=
                338.190, eps=0.004582395
Epoch 426: f=
                338.189, eps=0.004811515
Epoch 427: f=
                338.188, eps=0.005052091
Epoch 428: f=
                338.187, eps=0.005304695
Epoch 429: f=
                338.186, eps=0.005569930
Epoch 430: f=
                338.184, eps=0.005848427
Epoch 431: f=
                338.183, eps=0.006140848
Epoch 432: f=
                338.182, eps=0.006447890
Epoch 433: f=
                338.181, eps=0.006770285
Epoch 434: f=
                338.179, eps=0.007108799
Epoch 435: f=
                338.178, eps=0.007464239
Epoch 436: f=
                338.176, eps=0.007837451
Epoch 437: f=
                338.175, eps=0.008229324
```

```
Epoch 438: f=
                338.173, eps=0.008640790
Epoch 439: f=
                338.172, eps=0.009072829
Epoch 440: f=
                338.177, eps=0.004536415
Epoch 441: f=
                338.176, eps=0.004763235
Epoch 442: f=
                338.177, eps=0.002381618
Epoch 443: f=
                338.168, eps=0.002500699
Epoch 444: f=
                338.167, eps=0.002625734
Epoch 445: f=
                338.167, eps=0.002757020
Epoch 446: f=
                338.166, eps=0.002894871
Epoch 447: f=
                338.166, eps=0.003039615
Epoch 448: f=
                338.165, eps=0.003191596
Epoch 449: f=
                338.165, eps=0.003351175
Epoch 450: f=
                338.164, eps=0.003518734
Epoch 451: f=
                338.164, eps=0.003694671
Epoch 452: f=
                338.163, eps=0.003879404
Epoch 453: f=
                338.162, eps=0.004073375
Epoch 454: f=
                338.162, eps=0.004277043
Epoch 455: f=
                338.161, eps=0.004490895
Epoch 456: f=
                338.160, eps=0.004715440
Epoch 457: f=
                338.159, eps=0.004951212
Epoch 458: f=
                338.159, eps=0.005198773
Epoch 459: f=
                338.158, eps=0.005458711
Epoch 460: f=
                338.157, eps=0.005731647
Epoch 461: f=
                338.156, eps=0.006018229
Epoch 462: f=
                338.155, eps=0.006319141
Epoch 463: f=
                338.154, eps=0.006635098
Epoch 464: f=
                338.153, eps=0.006966853
Epoch 465: f=
                338.152, eps=0.007315195
Epoch 466: f=
                338.151, eps=0.007680955
Epoch 467: f=
                338.149, eps=0.008065003
Epoch 468: f=
                338.148, eps=0.008468253
Epoch 469: f=
                338.147, eps=0.008891666
Epoch 470: f=
                338.146, eps=0.009336249
Epoch 471: f=
                338.144, eps=0.009803061
Epoch 472: f=
                338.143, eps=0.010293215
Epoch 473: f=
                338.142, eps=0.010807875
Epoch 474: f=
                338.142, eps=0.005403938
Epoch 475: f=
                338.143, eps=0.002701969
Epoch 476: f=
                338.139, eps=0.002837067
Epoch 477: f=
                338.139, eps=0.002978921
Epoch 478: f=
                338.138, eps=0.003127867
Epoch 479: f=
                338.138, eps=0.003284260
                338.137, eps=0.003448473
Epoch 480: f=
Epoch 481: f=
                338.137, eps=0.003620897
Epoch 482: f=
                338.137, eps=0.003801941
Epoch 483: f=
                338.136, eps=0.003992039
Epoch 484: f=
                338.136, eps=0.004191640
Epoch 485: f=
                338.135, eps=0.004401222
```

```
Epoch 486: f=
                338.134, eps=0.004621284
Epoch 487: f=
                338.134, eps=0.004852348
Epoch 488: f=
                338.133, eps=0.005094965
Epoch 489: f=
                338.133, eps=0.005349713
Epoch 490: f=
                338.132, eps=0.005617199
Epoch 491: f=
                338.131, eps=0.005898059
Epoch 492: f=
                338.131, eps=0.006192962
Epoch 493: f=
                338.130, eps=0.006502610
Epoch 494: f=
                338.129, eps=0.006827741
Epoch 495: f=
                338.128, eps=0.007169128
Epoch 496: f=
                338.128, eps=0.007527584
Epoch 497: f=
                338.127, eps=0.007903963
Epoch 498: f=
                338.126, eps=0.008299161
Epoch 499: f=
                338.126, eps=0.004149581
Result after 500 epochs: f=338.1256197756515
Epoch
        0: f=
               3437.078, eps=0.010000000
Epoch
        1: f=
               1383.004, eps=0.010500000
Epoch
        2: f=
                845.939, eps=0.011025000
        3: f=
Epoch
                617.843, eps=0.011576250
Epoch
        4: f=
                568.291, eps=0.012155063
Epoch
        5: f=
                505.428, eps=0.012762816
Epoch
        6: f=
                538.784, eps=0.006381408
Epoch
        7: f=
                447.927, eps=0.006700478
Epoch
        8: f=
                415.280, eps=0.007035502
Epoch
        9: f=
                408.716, eps=0.007387277
      10: f=
                402.908, eps=0.007756641
Epoch
                404.614, eps=0.003878321
Epoch
       11: f=
Epoch
       12: f=
                393.981, eps=0.004072237
Epoch
      13: f=
                390.998, eps=0.004275848
                389.170, eps=0.004489641
Epoch
      14: f=
Epoch 15: f=
                387.329, eps=0.004714123
                385.975, eps=0.004949829
Epoch
      16: f=
Epoch 17: f=
                384.267, eps=0.005197320
Epoch
       18: f=
                383.436, eps=0.005457186
Epoch
       19: f=
                381.534, eps=0.005730046
Epoch
      20: f=
                381.627, eps=0.002865023
Epoch
      21: f=
                375.424, eps=0.003008274
Epoch 22: f=
                374.547, eps=0.003158688
Epoch 23: f=
                373.670, eps=0.003316622
                372.788, eps=0.003482453
Epoch 24: f=
Epoch
      25: f=
                371.894, eps=0.003656576
Epoch
      26: f=
                370.991, eps=0.003839405
                370.079, eps=0.004031375
Epoch
      27: f=
Epoch 28: f=
                369.169, eps=0.004232944
Epoch
      29: f=
                368.269, eps=0.004444591
Epoch
      30: f=
                367.439, eps=0.004666820
Epoch
      31: f=
                366.716, eps=0.004900161
                366.427, eps=0.005145169
Epoch
      32: f=
```

```
Epoch 33: f=
                366.014, eps=0.005402428
Epoch
      34: f=
                366.514, eps=0.002701214
Epoch
      35: f=
                362.907, eps=0.002836275
Epoch
      36: f=
                362.399, eps=0.002978088
Epoch
      37: f=
                361.908, eps=0.003126993
Epoch
      38: f=
                361.412, eps=0.003283342
Epoch
      39: f=
                360.907, eps=0.003447510
Epoch 40: f=
                360.396, eps=0.003619885
Epoch 41: f=
                359.877, eps=0.003800879
Epoch 42: f=
                359.354, eps=0.003990923
                358.826, eps=0.004190469
Epoch
      43: f=
Epoch 44: f=
                358.297, eps=0.004399993
                357.768, eps=0.004619993
Epoch 45: f=
Epoch
      46: f=
                357.244, eps=0.004850992
Epoch 47: f=
                356.734, eps=0.005093542
Epoch 48: f=
                356.263, eps=0.005348219
Epoch 49: f=
                355.933, eps=0.005615630
                355.907, eps=0.005896411
Epoch 50: f=
Epoch 51: f=
                357.038, eps=0.002948206
Epoch 52: f=
                354.510, eps=0.003095616
Epoch
      53: f=
                354.265, eps=0.003250397
Epoch 54: f=
                354.042, eps=0.003412917
Epoch 55: f=
                353.823, eps=0.003583562
Epoch 56: f=
                353.608, eps=0.003762741
                353.397, eps=0.003950878
Epoch 57: f=
Epoch 58: f=
                353.192, eps=0.004148421
                352.992, eps=0.004355843
Epoch 59: f=
Epoch
      60: f=
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      66: f=
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      67: f=
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      68: f=
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Epoch 76: f=
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      78: f=
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      79: f=
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      84: f=
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      85: f=
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      86: f=
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      87: f=
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      91: f=
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      92: f=
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      93: f=
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      94: f=
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Epoch 174: f=
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                347.873, eps=0.002983793
Epoch 402: f=
                347.872, eps=0.003132983
Epoch 403: f=
                347.872, eps=0.003289632
Epoch 404: f=
                347.872, eps=0.003454113
Epoch 405: f=
                347.872, eps=0.003626819
Epoch 406: f=
                347.871, eps=0.003808160
Epoch 407: f=
                347.871, eps=0.003998568
Epoch 408: f=
                347.871, eps=0.004198496
Epoch 409: f=
                347.870, eps=0.004408421
Epoch 410: f=
                347.870, eps=0.004628842
Epoch 411: f=
                347.870, eps=0.004860284
Epoch 412: f=
                347.869, eps=0.005103298
Epoch 413: f=
                347.869, eps=0.005358463
Epoch 414: f=
                347.869, eps=0.005626387
Epoch 415: f=
                347.868, eps=0.005907706
Epoch 416: f=
                347.868, eps=0.006203091
```

```
Epoch 417: f=
                347.867, eps=0.006513246
Epoch 418: f=
                347.867, eps=0.006838908
Epoch 419: f=
                347.866, eps=0.007180853
Epoch 420: f=
                347.866, eps=0.007539896
Epoch 421: f=
                347.866, eps=0.007916891
Epoch 422: f=
                347.866, eps=0.003958445
Epoch 423: f=
                347.866, eps=0.004156368
Epoch 424: f=
                347.865, eps=0.004364186
Epoch 425: f=
                347.865, eps=0.004582395
Epoch 426: f=
                347.865, eps=0.002291198
Epoch 427: f=
                347.864, eps=0.002405758
Epoch 428: f=
                347.864, eps=0.002526045
Epoch 429: f=
                347.864, eps=0.002652348
Epoch 430: f=
                347.863, eps=0.002784965
Epoch 431: f=
                347.863, eps=0.002924213
Epoch 432: f=
                347.863, eps=0.003070424
Epoch 433: f=
                347.863, eps=0.003223945
Epoch 434: f=
                347.863, eps=0.003385142
Epoch 435: f=
                347.863, eps=0.003554400
Epoch 436: f=
                347.862, eps=0.003732120
Epoch 437: f=
                347.862, eps=0.003918726
Epoch 438: f=
                347.862, eps=0.004114662
Epoch 439: f=
                347.862, eps=0.004320395
Epoch 440: f=
                347.861, eps=0.004536415
Epoch 441: f=
                347.861, eps=0.004763235
Epoch 442: f=
                347.861, eps=0.005001397
Epoch 443: f=
                347.861, eps=0.005251467
Epoch 444: f=
                347.860, eps=0.005514040
Epoch 445: f=
                347.860, eps=0.005789742
Epoch 446: f=
                347.860, eps=0.006079230
Epoch 447: f=
                347.860, eps=0.006383191
Epoch 448: f=
                347.859, eps=0.006702351
Epoch 449: f=
                347.859, eps=0.007037468
Epoch 450: f=
                347.859, eps=0.007389342
Epoch 451: f=
                347.858, eps=0.007758809
Epoch 452: f=
                347.858, eps=0.008146749
Epoch 453: f=
                347.858, eps=0.008554086
Epoch 454: f=
                347.857, eps=0.008981791
Epoch 455: f=
                347.857, eps=0.009430880
Epoch 456: f=
                347.857, eps=0.009902424
Epoch 457: f=
                347.856, eps=0.010397546
Epoch 458: f=
                347.857, eps=0.005198773
Epoch 459: f=
                347.859, eps=0.002599386
Epoch 460: f=
                347.856, eps=0.002729356
                347.855, eps=0.002865824
Epoch 461: f=
Epoch 462: f=
                347.855, eps=0.003009115
Epoch 463: f=
                347.855, eps=0.003159570
Epoch 464: f=
                347.855, eps=0.003317549
```

```
Epoch 465: f=
                347.855, eps=0.003483426
Epoch 466: f=
                347.855, eps=0.003657598
Epoch 467: f=
                347.855, eps=0.003840478
Epoch 468: f=
                347.855, eps=0.004032501
Epoch 469: f=
                347.854, eps=0.004234127
Epoch 470: f=
                347.854, eps=0.004445833
Epoch 471: f=
                347.854, eps=0.004668125
Epoch 472: f=
                347.854, eps=0.004901531
Epoch 473: f=
                347.854, eps=0.005146607
Epoch 474: f=
                347.854, eps=0.005403938
Epoch 475: f=
                347.854, eps=0.005674135
Epoch 476: f=
                347.853, eps=0.005957841
Epoch 477: f=
                347.853, eps=0.006255733
Epoch 478: f=
                347.853, eps=0.006568520
                347.853, eps=0.006896946
Epoch 479: f=
Epoch 480: f=
                347.853, eps=0.007241793
Epoch 481: f=
                347.852, eps=0.007603883
Epoch 482: f=
                347.852, eps=0.007984077
Epoch 483: f=
                347.854, eps=0.003992039
Epoch 484: f=
                347.853, eps=0.004191640
Epoch 485: f=
                347.853, eps=0.004401222
Epoch 486: f=
                347.853, eps=0.002200611
Epoch 487: f=
                347.852, eps=0.002310642
Epoch 488: f=
                347.851, eps=0.002426174
Epoch 489: f=
                347.851, eps=0.002547483
Epoch 490: f=
                347.851, eps=0.002674857
Epoch 491: f=
                347.851, eps=0.002808600
Epoch 492: f=
                347.851, eps=0.002949030
Epoch 493: f=
                347.851, eps=0.003096481
Epoch 494: f=
                347.851, eps=0.003251305
Epoch 495: f=
                347.851, eps=0.003413870
Epoch 496: f=
                347.851, eps=0.003584564
Epoch 497: f=
                347.851, eps=0.003763792
Epoch 498: f=
                347.851, eps=0.003951982
Epoch 499: f=
                347.851, eps=0.004149581
Result after 500 epochs: f=347.85049245754726
Epoch
        0: f=
               3470.639, eps=0.010000000
Epoch
        1: f=
               1433.919, eps=0.010500000
        2: f=
                874.733, eps=0.011025000
Epoch
        3: f=
Epoch
                641.063, eps=0.011576250
Epoch
        4: f=
                590.250, eps=0.012155063
Epoch
        5: f=
                527.407, eps=0.012762816
Epoch
        6: f=
                566.323, eps=0.006381408
Epoch
        7: f=
                462.868, eps=0.006700478
        8: f=
                427.009, eps=0.007035502
Epoch
Epoch
        9: f=
                421.484, eps=0.007387277
Epoch
       10: f=
                421.126, eps=0.007756641
Epoch
       11: f=
                422.055, eps=0.003878321
```

```
Epoch 12: f=
                405.514, eps=0.004072237
Epoch
      13: f=
                400.657, eps=0.004275848
Epoch
      14: f=
                398.816, eps=0.004489641
Epoch
       15: f=
                396.854, eps=0.004714123
Epoch
      16: f=
                395.520, eps=0.004949829
Epoch
       17: f=
                393.421, eps=0.005197320
Epoch
      18: f=
                392.767, eps=0.005457186
Epoch
      19: f=
                390.296, eps=0.005730046
Epoch 20: f=
                390.877, eps=0.002865023
Epoch 21: f=
                384.085, eps=0.003008274
      22: f=
                383.096, eps=0.003158688
Epoch
Epoch 23: f=
                382.137, eps=0.003316622
                381.192, eps=0.003482453
Epoch
      24: f=
Epoch 25: f=
                380.247, eps=0.003656576
Epoch 26: f=
                379.311, eps=0.003839405
Epoch 27: f=
                378.385, eps=0.004031375
Epoch 28: f=
                377.505, eps=0.004232944
Epoch 29: f=
                376.692, eps=0.004444591
Epoch 30: f=
                376.101, eps=0.004666820
Epoch
                375.638, eps=0.004900161
      31: f=
Epoch
      32: f=
                375.669, eps=0.002450081
Epoch 33: f=
                373.114, eps=0.002572585
Epoch 34: f=
                372.665, eps=0.002701214
Epoch 35: f=
                372.214, eps=0.002836275
                371.758, eps=0.002978088
Epoch 36: f=
Epoch 37: f=
                371.299, eps=0.003126993
Epoch 38: f=
                370.838, eps=0.003283342
Epoch
      39: f=
                370.375, eps=0.003447510
Epoch 40: f=
                369.913, eps=0.003619885
Epoch 41: f=
                369.454, eps=0.003800879
Epoch 42: f=
                368.998, eps=0.003990923
Epoch
      43: f=
                368.549, eps=0.004190469
Epoch 44: f=
                368.108, eps=0.004399993
Epoch 45: f=
                367.678, eps=0.004619993
      46: f=
Epoch
                367.260, eps=0.004850992
Epoch
      47: f=
                366.858, eps=0.005093542
Epoch 48: f=
                366.474, eps=0.005348219
Epoch 49: f=
                366.114, eps=0.005615630
Epoch 50: f=
                365.793, eps=0.005896411
Epoch 51: f=
                365.585, eps=0.006191232
Epoch 52: f=
                365.853, eps=0.003095616
Epoch 53: f=
                365.317, eps=0.003250397
                365.003, eps=0.003412917
Epoch
      54: f=
Epoch 55: f=
                364.855, eps=0.003583562
Epoch 56: f=
                364.708, eps=0.003762741
Epoch
      57: f=
                364.599, eps=0.003950878
Epoch 58: f=
                364.492, eps=0.004148421
                364.449, eps=0.004355843
Epoch 59: f=
```

```
Epoch 60: f=
                364.426, eps=0.004573635
Epoch 61: f=
                364.637, eps=0.002286817
Epoch
      62: f=
                363.958, eps=0.002401158
Epoch
      63: f=
                363.900, eps=0.002521216
Epoch
      64: f=
                363.841, eps=0.002647277
Epoch
      65: f=
                363.781, eps=0.002779641
Epoch
      66: f=
                363.720, eps=0.002918623
Epoch
      67: f=
                363.659, eps=0.003064554
Epoch 68: f=
                363.597, eps=0.003217782
Epoch
      69: f=
                363.534, eps=0.003378671
      70: f=
                363.470, eps=0.003547604
Epoch
Epoch 71: f=
                363.406, eps=0.003724984
                363.341, eps=0.003911234
Epoch
      72: f=
Epoch 73: f=
                363.275, eps=0.004106795
Epoch 74: f=
                363.209, eps=0.004312135
Epoch 75: f=
                363.143, eps=0.004527742
Epoch 76: f=
                363.077, eps=0.004754129
Epoch 77: f=
                363.010, eps=0.004991835
Epoch 78: f=
                362.944, eps=0.005241427
Epoch
                362.877, eps=0.005503499
      79: f=
Epoch
      80: f=
                362.811, eps=0.005778674
Epoch 81: f=
                362.745, eps=0.006067607
Epoch 82: f=
                362.679, eps=0.006370988
Epoch 83: f=
                362.615, eps=0.006689537
                362.556, eps=0.007024014
Epoch 84: f=
Epoch 85: f=
                362.540, eps=0.007375214
Epoch 86: f=
                362.878, eps=0.003687607
Epoch 87: f=
                362.824, eps=0.003871988
Epoch 88: f=
                362.634, eps=0.004065587
Epoch 89: f=
                362.719, eps=0.002032793
Epoch 90: f=
                362.317, eps=0.002134433
Epoch 91: f=
                362.299, eps=0.002241155
Epoch 92: f=
                362.283, eps=0.002353213
Epoch 93: f=
                362.266, eps=0.002470873
      94: f=
Epoch
                362.249, eps=0.002594417
Epoch 95: f=
                362.231, eps=0.002724138
Epoch 96: f=
                362.213, eps=0.002860345
Epoch 97: f=
                362.195, eps=0.003003362
Epoch 98: f=
                362.176, eps=0.003153530
Epoch 99: f=
                362.156, eps=0.003311206
Epoch 100: f=
                362.136, eps=0.003476767
Epoch 101: f=
                362.115, eps=0.003650605
                362.094, eps=0.003833135
Epoch 102: f=
Epoch 103: f=
                362.072, eps=0.004024792
Epoch 104: f=
                362.050, eps=0.004226032
Epoch 105: f=
                362.028, eps=0.004437333
Epoch 106: f=
                362.005, eps=0.004659200
Epoch 107: f=
                361.982, eps=0.004892160
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Epoch 108: f=
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Epoch 109: f=
                361.934, eps=0.005393606
Epoch 110: f=
                361.909, eps=0.005663287
Epoch 111: f=
                361.885, eps=0.005946451
Epoch 112: f=
                361.860, eps=0.006243773
Epoch 113: f=
                361.835, eps=0.006555962
Epoch 114: f=
                361.810, eps=0.006883760
Epoch 115: f=
                361.784, eps=0.007227948
Epoch 116: f=
                361.759, eps=0.007589346
Epoch 117: f=
                361.736, eps=0.007968813
Epoch 118: f=
                361.742, eps=0.003984406
Epoch 119: f=
                361.735, eps=0.004183627
Epoch 120: f=
                361.748, eps=0.002091813
Epoch 121: f=
                361.677, eps=0.002196404
Epoch 122: f=
                361.670, eps=0.002306224
Epoch 123: f=
                361.664, eps=0.002421535
Epoch 124: f=
                361.657, eps=0.002542612
Epoch 125: f=
                361.650, eps=0.002669743
Epoch 126: f=
                361.642, eps=0.002803230
Epoch 127: f=
                361.635, eps=0.002943392
Epoch 128: f=
                361.627, eps=0.003090561
Epoch 129: f=
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Epoch 130: f=
                361.611, eps=0.003407344
Epoch 131: f=
                361.602, eps=0.003577711
Epoch 132: f=
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Epoch 133: f=
                361.585, eps=0.003944426
Epoch 134: f=
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Epoch 135: f=
                361.566, eps=0.004348730
Epoch 136: f=
                361.556, eps=0.004566166
Epoch 137: f=
                361.546, eps=0.004794475
Epoch 138: f=
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Epoch 139: f=
                361.526, eps=0.005285908
Epoch 140: f=
                361.515, eps=0.005550204
Epoch 141: f=
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Epoch 142: f=
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Epoch 143: f=
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Epoch 144: f=
                361.471, eps=0.006746307
Epoch 145: f=
                361.460, eps=0.007083623
Epoch 146: f=
                361.448, eps=0.007437804
Epoch 147: f=
                361.437, eps=0.007809694
Epoch 148: f=
                361.431, eps=0.008200179
Epoch 149: f=
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                361.508, eps=0.002050045
Epoch 150: f=
Epoch 151: f=
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Epoch 152: f=
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Epoch 153: f=
                361.399, eps=0.002373183
Epoch 154: f=
                361.396, eps=0.002491842
Epoch 155: f=
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```

```
Epoch 156: f=
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Epoch 157: f=
                361.386, eps=0.002884619
Epoch 158: f=
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Epoch 159: f=
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Epoch 160: f=
                361.375, eps=0.003339307
Epoch 161: f=
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Epoch 162: f=
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Epoch 163: f=
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Epoch 164: f=
                361.358, eps=0.004058948
Epoch 165: f=
                361.354, eps=0.004261896
Epoch 166: f=
                361.349, eps=0.004474990
Epoch 167: f=
                361.345, eps=0.004698740
Epoch 168: f=
                361.340, eps=0.004933677
Epoch 169: f=
                361.335, eps=0.005180361
Epoch 170: f=
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Epoch 171: f=
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Epoch 172: f=
                361.320, eps=0.005996915
Epoch 173: f=
                361.314, eps=0.006296761
Epoch 174: f=
                361.309, eps=0.006611599
Epoch 175: f=
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Epoch 176: f=
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Epoch 177: f=
                361.292, eps=0.007653752
Epoch 178: f=
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Epoch 179: f=
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Epoch 180: f=
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                361.320, eps=0.004430087
Epoch 181: f=
Epoch 182: f=
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Epoch 183: f=
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Epoch 184: f=
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Epoch 185: f=
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Epoch 186: f=
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Epoch 187: f=
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Epoch 188: f=
                361.258, eps=0.002968370
Epoch 189: f=
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Epoch 190: f=
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Epoch 191: f=
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Epoch 192: f=
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Epoch 193: f=
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Epoch 194: f=
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Epoch 195: f=
                361.245, eps=0.004176795
Epoch 196: f=
                361.242, eps=0.004385635
Epoch 197: f=
                361.240, eps=0.004604917
Epoch 198: f=
                361.238, eps=0.004835163
Epoch 199: f=
                361.236, eps=0.005076921
Epoch 200: f=
                361.234, eps=0.005330767
Epoch 201: f=
                361.231, eps=0.005597305
Epoch 202: f=
                361.229, eps=0.005877170
Epoch 203: f=
                361.226, eps=0.006171029
```

```
Epoch 204: f=
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Epoch 205: f=
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Epoch 206: f=
                361.220, eps=0.007143737
Epoch 207: f=
                361.230, eps=0.003571869
Epoch 208: f=
                361.227, eps=0.003750462
Epoch 209: f=
                361.225, eps=0.003937985
Epoch 210: f=
                361.227, eps=0.001968993
Epoch 211: f=
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Epoch 212: f=
                361.211, eps=0.002170814
Epoch 213: f=
                361.210, eps=0.002279355
Epoch 214: f=
                361.209, eps=0.002393323
Epoch 215: f=
                361.208, eps=0.002512989
Epoch 216: f=
                361.207, eps=0.002638638
Epoch 217: f=
                361.207, eps=0.002770570
Epoch 218: f=
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Epoch 219: f=
                361.205, eps=0.003054554
Epoch 220: f=
                361.204, eps=0.003207282
Epoch 221: f=
                361.203, eps=0.003367646
Epoch 222: f=
                361.202, eps=0.003536028
Epoch 223: f=
                361.201, eps=0.003712829
Epoch 224: f=
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Epoch 225: f=
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Epoch 226: f=
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Epoch 227: f=
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Epoch 228: f=
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Epoch 229: f=
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Epoch 230: f=
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Epoch 231: f=
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Epoch 232: f=
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Epoch 233: f=
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Epoch 234: f=
                361.188, eps=0.006350198
Epoch 235: f=
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Epoch 236: f=
                361.185, eps=0.007001093
Epoch 237: f=
                361.183, eps=0.007351148
Epoch 238: f=
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Epoch 239: f=
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Epoch 240: f=
                361.179, eps=0.008509873
Epoch 241: f=
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Epoch 242: f=
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Epoch 243: f=
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Epoch 244: f=
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Epoch 245: f=
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Epoch 246: f=
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Epoch 247: f=
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Epoch 248: f=
                361.172, eps=0.002851011
Epoch 249: f=
                361.172, eps=0.002993561
Epoch 250: f=
                361.171, eps=0.003143239
Epoch 251: f=
                361.171, eps=0.003300401
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Epoch 253: f=
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Epoch 254: f=
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Epoch 255: f=
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Epoch 256: f=
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Epoch 257: f=
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Epoch 259: f=
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Epoch 260: f=
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Epoch 261: f=
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Epoch 262: f=
Epoch 263: f=
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Epoch 264: f=
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Epoch 265: f=
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Epoch 266: f=
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Epoch 267: f=
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Epoch 268: f=
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Epoch 269: f=
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Epoch 270: f=
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Epoch 271: f=
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Epoch 272: f=
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Epoch 273: f=
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Epoch 274: f=
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Epoch 275: f=
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Epoch 277: f=
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Epoch 278: f=
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Epoch 279: f=
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Epoch 280: f=
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Epoch 283: f=
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Epoch 287: f=
Epoch 288: f=
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Epoch 296: f=
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Epoch 297: f=
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Epoch 298: f=
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Epoch 299: f=
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Epoch 301: f=
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Epoch 302: f=
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Epoch 303: f=
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Epoch 304: f=
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Epoch 307: f=
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Epoch 308: f=
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Epoch 310: f=
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Epoch 311: f=
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Epoch 312: f=
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Epoch 313: f=
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Epoch 314: f=
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Epoch 315: f=
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Epoch 316: f=
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Epoch 317: f=
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Epoch 318: f=
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Epoch 319: f=
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Epoch 320: f=
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Epoch 321: f=
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Epoch 322: f=
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Epoch 323: f=
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Epoch 324: f=
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Epoch 325: f=
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Epoch 326: f=
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Epoch 327: f=
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Epoch 328: f=
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Epoch 329: f=
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Epoch 330: f=
                361.148, eps=0.008010216
Epoch 331: f=
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Epoch 332: f=
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Epoch 333: f=
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Epoch 334: f=
                361.147, eps=0.002207816
                361.147, eps=0.002318206
Epoch 335: f=
Epoch 336: f=
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Epoch 337: f=
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Epoch 338: f=
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Epoch 339: f=
                361.147, eps=0.002817794
Epoch 340: f=
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Epoch 341: f=
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Epoch 342: f=
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Epoch 343: f=
                361.146, eps=0.003425047
Epoch 344: f=
                361.146, eps=0.003596299
Epoch 345: f=
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Epoch 346: f=
                361.146, eps=0.003964920
Epoch 347: f=
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Epoch 348: f=
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Epoch 349: f=
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Epoch 350: f=
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Epoch 351: f=
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Epoch 352: f=
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Epoch 353: f=
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Epoch 354: f=
                361.145, eps=0.005857992
Epoch 355: f=
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Epoch 356: f=
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Epoch 357: f=
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Epoch 358: f=
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Epoch 359: f=
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Epoch 360: f=
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Epoch 361: f=
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Epoch 362: f=
                361.146, eps=0.001962567
Epoch 363: f=
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Epoch 364: f=
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Epoch 365: f=
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Epoch 366: f=
                361.145, eps=0.002385513
Epoch 367: f=
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Epoch 368: f=
                361.145, eps=0.002630028
                361.144, eps=0.002761530
Epoch 369: f=
Epoch 370: f=
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Epoch 371: f=
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Epoch 372: f=
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Epoch 373: f=
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Epoch 374: f=
                361.144, eps=0.003524489
Epoch 375: f=
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Epoch 376: f=
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Epoch 377: f=
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Epoch 378: f=
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Epoch 379: f=
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Epoch 380: f=
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Epoch 381: f=
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Epoch 382: f=
                361.144, eps=0.005207276
Epoch 383: f=
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Epoch 384: f=
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Epoch 385: f=
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Epoch 386: f=
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Epoch 387: f=
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Epoch 388: f=
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Epoch 389: f=
                361.144, eps=0.007327160
Epoch 390: f=
                361.143, eps=0.007693518
Epoch 391: f=
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Epoch 392: f=
                361.143, eps=0.008482104
Epoch 393: f=
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Epoch 394: f=
                361.143, eps=0.004453104
Epoch 395: f=
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Epoch 397: f=
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Epoch 398: f=
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Epoch 399: f=
                361.143, eps=0.002706388
Epoch 400: f=
                361.143, eps=0.002841708
Epoch 401: f=
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Epoch 402: f=
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Epoch 403: f=
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Epoch 404: f=
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Epoch 405: f=
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Epoch 406: f=
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Epoch 407: f=
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Epoch 408: f=
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Epoch 409: f=
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Epoch 410: f=
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Epoch 411: f=
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Epoch 412: f=
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Epoch 413: f=
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Epoch 414: f=
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Epoch 415: f=
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Epoch 416: f=
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Epoch 417: f=
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Epoch 418: f=
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Epoch 419: f=
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Epoch 420: f=
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Epoch 421: f=
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Epoch 422: f=
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Epoch 423: f=
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Epoch 424: f=
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Epoch 425: f=
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Epoch 426: f=
                361.143, eps=0.002291198
Epoch 427: f=
                361.143, eps=0.002405758
Epoch 428: f=
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Epoch 429: f=
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Epoch 430: f=
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Epoch 431: f=
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Epoch 432: f=
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Epoch 433: f=
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Epoch 434: f=
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Epoch 435: f=
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Epoch 436: f=
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Epoch 437: f=
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Epoch 438: f=
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Epoch 439: f=
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Epoch 440: f=
                361.142, eps=0.004536415
Epoch 441: f=
                361.142, eps=0.004763235
Epoch 442: f=
                361.142, eps=0.005001397
Epoch 443: f=
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Epoch 444: f=
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Epoch 445: f=
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Epoch 446: f=
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Epoch 447: f=
                361.142, eps=0.006383191
Epoch 448: f=
                361.142, eps=0.006702351
Epoch 449: f=
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Epoch 450: f=
                361.142, eps=0.007389342
Epoch 451: f=
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Epoch 452: f=
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Epoch 453: f=
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Epoch 454: f=
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Epoch 456: f=
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Epoch 457: f=
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Epoch 458: f=
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Epoch 459: f=
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Epoch 461: f=
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Epoch 462: f=
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Epoch 463: f=
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Epoch 464: f=
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Epoch 465: f=
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Epoch 466: f=
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Epoch 467: f=
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Epoch 468: f=
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Epoch 469: f=
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Epoch 470: f=
                361.142, eps=0.004445833
Epoch 471: f=
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Epoch 472: f=
                361.142, eps=0.004901531
Epoch 473: f=
                361.142, eps=0.005146607
Epoch 474: f=
                361.142, eps=0.005403938
Epoch 475: f=
                361.142, eps=0.005674135
Epoch 476: f=
                361.142, eps=0.005957841
Epoch 477: f=
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Epoch 478: f=
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Epoch 479: f=
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Epoch 480: f=
                361.142, eps=0.003448473
Epoch 481: f=
                361.142, eps=0.003620897
Epoch 482: f=
                361.142, eps=0.003801941
Epoch 483: f=
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Epoch 484: f=
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Epoch 485: f=
                361.142, eps=0.004401222
Epoch 486: f=
                361.142, eps=0.002200611
Epoch 487: f=
                361.142, eps=0.002310642
Epoch 488: f=
                361.142, eps=0.002426174
Epoch 489: f=
                361.142, eps=0.002547483
Epoch 490: f=
                361.142, eps=0.002674857
Epoch 491: f=
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Epoch 492: f=
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Epoch 493: f=
                361.142, eps=0.003096481
Epoch 494: f=
                361.142, eps=0.003251305
Epoch 495: f=
                361.142, eps=0.003413870
Epoch 496: f=
                361.142, eps=0.003584564
Epoch 497: f=
                361.142, eps=0.003763792
Epoch 498: f=
                361.142, eps=0.003951982
Epoch 499: f=
                361.142, eps=0.004149581
Result after 500 epochs: f=361.1419871051869
Epoch
        0: f=
               3504.201, eps=0.010000000
               1484.232, eps=0.010500000
Epoch
        1: f=
Epoch
        2: f=
                901.263, eps=0.011025000
Epoch
        3: f=
                661.272, eps=0.011576250
Epoch
        4: f=
                608.524, eps=0.012155063
Epoch
        5: f=
                544.888, eps=0.012762816
Epoch
        6: f=
                592.502, eps=0.006381408
        7: f=
                474.161, eps=0.006700478
Epoch
Epoch
        8: f=
                435.176, eps=0.007035502
        9: f=
Epoch
                430.963, eps=0.007387277
                433.337, eps=0.003693639
Epoch
       10: f=
Epoch
       11: f=
                416.932, eps=0.003878321
Epoch
       12: f=
                412.242, eps=0.004072237
Epoch
       13: f=
                409.856, eps=0.004275848
Epoch
       14: f=
                407.274, eps=0.004489641
                405.557, eps=0.004714123
Epoch
      15: f=
                402.987, eps=0.004949829
Epoch
       16: f=
Epoch
       17: f=
                402.050, eps=0.005197320
Epoch
       18: f=
                399.100, eps=0.005457186
Epoch
       19: f=
                399.350, eps=0.002728593
      20: f=
                393.180, eps=0.002865023
Epoch
Epoch
      21: f=
                392.040, eps=0.003008274
       22: f=
                390.977, eps=0.003158688
Epoch
Epoch
      23: f=
                389.934, eps=0.003316622
Epoch
       24: f=
                388.903, eps=0.003482453
Epoch
       25: f=
                387.884, eps=0.003656576
Epoch
       26: f=
                386.883, eps=0.003839405
Epoch
      27: f=
                385.917, eps=0.004031375
Epoch
                385.013, eps=0.004232944
      28: f=
Epoch
      29: f=
                384.250, eps=0.004444591
Epoch 30: f=
                383.712, eps=0.004666820
Epoch
      31: f=
                383.535, eps=0.004900161
Epoch
       32: f=
                383.475, eps=0.005145169
                383.201, eps=0.005402428
Epoch
       33: f=
Epoch
       34: f=
                383.690, eps=0.002701214
Epoch
       35: f=
                378.989, eps=0.002836275
Epoch
       36: f=
                378.595, eps=0.002978088
Epoch
       37: f=
                378.216, eps=0.003126993
                377.844, eps=0.003283342
Epoch
       38: f=
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Epoch 39: f=
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Epoch 40: f=
                377.121, eps=0.003619885
Epoch 41: f=
                376.772, eps=0.003800879
Epoch
      42: f=
                376.434, eps=0.003990923
Epoch 43: f=
                376.112, eps=0.004190469
Epoch 44: f=
                375.812, eps=0.004399993
Epoch
      45: f=
                375.554, eps=0.004619993
Epoch 46: f=
                375.400, eps=0.004850992
Epoch 47: f=
                375.486, eps=0.002425496
Epoch 48: f=
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                374.692, eps=0.002674109
Epoch
      49: f=
Epoch 50: f=
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                374.438, eps=0.002948206
Epoch 51: f=
Epoch
      52: f=
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                374.198, eps=0.003250397
Epoch 53: f=
Epoch 54: f=
                374.079, eps=0.003412917
Epoch 55: f=
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Epoch 56: f=
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Epoch 57: f=
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Epoch
                373.621, eps=0.004148421
      58: f=
Epoch
      59: f=
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Epoch 60: f=
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Epoch 61: f=
                373.306, eps=0.004802316
Epoch 62: f=
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Epoch 63: f=
Epoch 64: f=
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Epoch
      65: f=
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Epoch
      66: f=
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Epoch 67: f=
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Epoch 68: f=
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Epoch 69: f=
                372.741, eps=0.003378671
Epoch 70: f=
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Epoch 71: f=
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Epoch 72: f=
                372.589, eps=0.003911234
Epoch
      73: f=
                372.541, eps=0.004106795
Epoch 74: f=
                372.496, eps=0.004312135
Epoch 75: f=
                372.461, eps=0.004527742
Epoch 76: f=
                372.461, eps=0.004754129
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Epoch 422: f=
                371.139, eps=0.003958445
```

```
Epoch 423: f=
                371.139, eps=0.004156368
Epoch 424: f=
                371.139, eps=0.004364186
Epoch 425: f=
                371.139, eps=0.004582395
Epoch 426: f=
                371.139, eps=0.004811515
Epoch 427: f=
                371.139, eps=0.005052091
Epoch 428: f=
                371.139, eps=0.005304695
Epoch 429: f=
                371.139, eps=0.005569930
Epoch 430: f=
                371.139, eps=0.005848427
Epoch 431: f=
                371.139, eps=0.006140848
Epoch 432: f=
                371.139, eps=0.006447890
Epoch 433: f=
                371.139, eps=0.006770285
Epoch 434: f=
                371.139, eps=0.007108799
Epoch 435: f=
                371.139, eps=0.007464239
Epoch 436: f=
                371.139, eps=0.007837451
Epoch 437: f=
                371.139, eps=0.003918726
Epoch 438: f=
                371.139, eps=0.001959363
Epoch 439: f=
                371.139, eps=0.002057331
Epoch 440: f=
                371.139, eps=0.002160197
Epoch 441: f=
                371.139, eps=0.002268207
Epoch 442: f=
                371.139, eps=0.002381618
Epoch 443: f=
                371.139, eps=0.002500699
Epoch 444: f=
                371.139, eps=0.002625734
Epoch 445: f=
                371.139, eps=0.002757020
Epoch 446: f=
                371.139, eps=0.002894871
Epoch 447: f=
                371.139, eps=0.003039615
Epoch 448: f=
                371.139, eps=0.003191596
Epoch 449: f=
                371.139, eps=0.003351175
Epoch 450: f=
                371.139, eps=0.003518734
Epoch 451: f=
                371.139, eps=0.003694671
Epoch 452: f=
                371.139, eps=0.003879404
Epoch 453: f=
                371.139, eps=0.004073375
Epoch 454: f=
                371.139, eps=0.004277043
Epoch 455: f=
                371.139, eps=0.004490895
Epoch 456: f=
                371.139, eps=0.004715440
Epoch 457: f=
                371.139, eps=0.004951212
Epoch 458: f=
                371.139, eps=0.005198773
Epoch 459: f=
                371.139, eps=0.005458711
Epoch 460: f=
                371.139, eps=0.005731647
Epoch 461: f=
                371.139, eps=0.006018229
Epoch 462: f=
                371.139, eps=0.006319141
Epoch 463: f=
                371.139, eps=0.006635098
Epoch 464: f=
                371.139, eps=0.006966853
Epoch 465: f=
                371.139, eps=0.007315195
Epoch 466: f=
                371.139, eps=0.003657598
Epoch 467: f=
                371.139, eps=0.001828799
Epoch 468: f=
                371.139, eps=0.001920239
Epoch 469: f=
                371.139, eps=0.002016251
Epoch 470: f=
                371.139, eps=0.002117063
```

```
Epoch 471: f=
                371.139, eps=0.002222916
Epoch 472: f=
                371.139, eps=0.002334062
Epoch 473: f=
                371.139, eps=0.002450765
Epoch 474: f=
                371.139, eps=0.002573304
Epoch 475: f=
                371.139, eps=0.002701969
Epoch 476: f=
                371.139, eps=0.002837067
Epoch 477: f=
                371.139, eps=0.002978921
Epoch 478: f=
                371.139, eps=0.003127867
Epoch 479: f=
                371.139, eps=0.003284260
Epoch 480: f=
                371.139, eps=0.003448473
                371.139, eps=0.003620897
Epoch 481: f=
Epoch 482: f=
                371.139, eps=0.003801941
Epoch 483: f=
                371.139, eps=0.003992039
Epoch 484: f=
                371.139, eps=0.004191640
Epoch 485: f=
                371.139, eps=0.004401222
Epoch 486: f=
                371.139, eps=0.004621284
Epoch 487: f=
                371.139, eps=0.004852348
Epoch 488: f=
                371.139, eps=0.005094965
Epoch 489: f=
                371.139, eps=0.005349713
Epoch 490: f=
                371.139, eps=0.005617199
Epoch 491: f=
                371.139, eps=0.005898059
Epoch 492: f=
                371.139, eps=0.006192962
Epoch 493: f=
                371.139, eps=0.006502610
Epoch 494: f=
                371.139, eps=0.006827741
Epoch 495: f=
                371.139, eps=0.007169128
Epoch 496: f=
                371.139, eps=0.007527584
Epoch 497: f=
                371.139, eps=0.007903963
Epoch 498: f=
                371.139, eps=0.008299161
Epoch 499: f=
                371.139, eps=0.004149581
Result after 500 epochs: f=371.1389275935148
Epoch
        0: f=
               3537.762, eps=0.010000000
               1533.962, eps=0.010500000
Epoch
        1: f=
Epoch
        2: f=
                925.611, eps=0.011025000
Epoch
        3: f=
                678.698, eps=0.011576250
        4: f=
                623.594, eps=0.012155063
Epoch
Epoch
        5: f=
                559.072, eps=0.012762816
                618.976, eps=0.006381408
Epoch
        6: f=
Epoch
        7: f=
                482.920, eps=0.006700478
Epoch
        8: f=
                440.697, eps=0.007035502
        9: f=
Epoch
                437.285, eps=0.007387277
Epoch
       10: f=
                441.657, eps=0.003693639
Epoch
       11: f=
                422.980, eps=0.003878321
Epoch
       12: f=
                416.092, eps=0.004072237
Epoch
       13: f=
                413.571, eps=0.004275848
                411.182, eps=0.004489641
Epoch
       14: f=
Epoch
       15: f=
                409.539, eps=0.004714123
Epoch
       16: f=
                406.994, eps=0.004949829
                406.279, eps=0.005197320
Epoch
       17: f=
```

```
Epoch 18: f=
                403.037, eps=0.005457186
Epoch
      19: f=
                403.756, eps=0.002728593
Epoch
      20: f=
                397.360, eps=0.002865023
                396.197, eps=0.003008274
Epoch
      21: f=
Epoch
      22: f=
                395.177, eps=0.003158688
Epoch
      23: f=
                394.192, eps=0.003316622
Epoch
      24: f=
                393.236, eps=0.003482453
Epoch 25: f=
                392.308, eps=0.003656576
Epoch 26: f=
                391.420, eps=0.003839405
Epoch 27: f=
                390.591, eps=0.004031375
                389.875, eps=0.004232944
Epoch
      28: f=
Epoch 29: f=
                389.344, eps=0.004444591
                389.133, eps=0.004666820
Epoch
      30: f=
Epoch
      31: f=
                389.036, eps=0.004900161
Epoch 32: f=
                389.384, eps=0.002450081
Epoch 33: f=
                386.092, eps=0.002572585
Epoch 34: f=
                385.751, eps=0.002701214
Epoch 35: f=
                385.424, eps=0.002836275
Epoch 36: f=
                385.103, eps=0.002978088
Epoch
                384.788, eps=0.003126993
      37: f=
Epoch
      38: f=
                384.481, eps=0.003283342
Epoch
      39: f=
                384.182, eps=0.003447510
Epoch 40: f=
                383.892, eps=0.003619885
Epoch 41: f=
                383.613, eps=0.003800879
                383.346, eps=0.003990923
Epoch 42: f=
Epoch
      43: f=
                383.092, eps=0.004190469
Epoch 44: f=
                382.852, eps=0.004399993
Epoch
      45: f=
                382.630, eps=0.004619993
Epoch 46: f=
                382.442, eps=0.004850992
Epoch 47: f=
                382.347, eps=0.005093542
Epoch 48: f=
                382.579, eps=0.002546771
Epoch
      49: f=
                381.981, eps=0.002674109
Epoch 50: f=
                381.840, eps=0.002807815
Epoch 51: f=
                381.735, eps=0.002948206
Epoch
      52: f=
                381.641, eps=0.003095616
Epoch 53: f=
                381.551, eps=0.003250397
Epoch 54: f=
                381.462, eps=0.003412917
Epoch 55: f=
                381.374, eps=0.003583562
Epoch 56: f=
                381.289, eps=0.003762741
Epoch 57: f=
                381.206, eps=0.003950878
Epoch 58: f=
                381.129, eps=0.004148421
Epoch
      59: f=
                381.064, eps=0.004355843
      60: f=
                381.034, eps=0.004573635
Epoch
Epoch
      61: f=
                381.107, eps=0.002286817
Epoch
      62: f=
                380.851, eps=0.002401158
Epoch
      63: f=
                380.792, eps=0.002521216
Epoch
      64: f=
                380.749, eps=0.002647277
                380.709, eps=0.002779641
Epoch
      65: f=
```

```
Epoch 66: f=
                380.668, eps=0.002918623
Epoch
      67: f=
                380.627, eps=0.003064554
Epoch
      68: f=
                380.586, eps=0.003217782
Epoch
       69: f=
                380.545, eps=0.003378671
Epoch
      70: f=
                380.503, eps=0.003547604
Epoch
      71: f=
                380.461, eps=0.003724984
Epoch
      72: f=
                380.420, eps=0.003911234
Epoch 73: f=
                380.378, eps=0.004106795
Epoch 74: f=
                380.336, eps=0.004312135
Epoch 75: f=
                380.295, eps=0.004527742
                380.255, eps=0.004754129
Epoch
      76: f=
Epoch 77: f=
                380.220, eps=0.004991835
                380.201, eps=0.005241427
Epoch 78: f=
Epoch 79: f=
                380.260, eps=0.002620714
Epoch 80: f=
                380.149, eps=0.002751749
Epoch 81: f=
                380.107, eps=0.002889337
Epoch 82: f=
                380.080, eps=0.003033804
Epoch 83: f=
                380.058, eps=0.003185494
Epoch 84: f=
                380.037, eps=0.003344768
Epoch
                380.016, eps=0.003512007
      85: f=
Epoch
      86: f=
                379.996, eps=0.003687607
Epoch 87: f=
                379.977, eps=0.003871988
Epoch 88: f=
                379.960, eps=0.004065587
Epoch 89: f=
                379.949, eps=0.004268866
                379.955, eps=0.002134433
Epoch 90: f=
Epoch 91: f=
                379.901, eps=0.002241155
Epoch 92: f=
                379.888, eps=0.002353213
Epoch
      93: f=
                379.877, eps=0.002470873
Epoch 94: f=
                379.866, eps=0.002594417
Epoch 95: f=
                379.855, eps=0.002724138
Epoch 96: f=
                379.844, eps=0.002860345
Epoch 97: f=
                379.832, eps=0.003003362
Epoch 98: f=
                379.821, eps=0.003153530
Epoch 99: f=
                379.809, eps=0.003311206
Epoch 100: f=
                379.796, eps=0.003476767
Epoch 101: f=
                379.784, eps=0.003650605
Epoch 102: f=
                379.772, eps=0.003833135
Epoch 103: f=
                379.759, eps=0.004024792
Epoch 104: f=
                379.747, eps=0.004226032
Epoch 105: f=
                379.734, eps=0.004437333
Epoch 106: f=
                379.721, eps=0.004659200
Epoch 107: f=
                379.709, eps=0.004892160
                379.696, eps=0.005136768
Epoch 108: f=
Epoch 109: f=
                379.684, eps=0.005393606
Epoch 110: f=
                379.673, eps=0.005663287
Epoch 111: f=
                379.669, eps=0.005946451
Epoch 112: f=
                379.713, eps=0.002973225
Epoch 113: f=
                379.676, eps=0.003121887
```

```
Epoch 114: f=
                379.660, eps=0.003277981
Epoch 115: f=
                379.650, eps=0.003441880
Epoch 116: f=
                379.646, eps=0.003613974
                379.647, eps=0.001806987
Epoch 117: f=
Epoch 118: f=
                379.612, eps=0.001897336
Epoch 119: f=
                379.609, eps=0.001992203
Epoch 120: f=
                379.606, eps=0.002091813
Epoch 121: f=
                379.603, eps=0.002196404
Epoch 122: f=
                379.599, eps=0.002306224
Epoch 123: f=
                379.596, eps=0.002421535
                379.592, eps=0.002542612
Epoch 124: f=
Epoch 125: f=
                379.589, eps=0.002669743
Epoch 126: f=
                379.585, eps=0.002803230
Epoch 127: f=
                379.581, eps=0.002943392
Epoch 128: f=
                379.577, eps=0.003090561
Epoch 129: f=
                379.573, eps=0.003245089
Epoch 130: f=
                379.569, eps=0.003407344
Epoch 131: f=
                379.565, eps=0.003577711
Epoch 132: f=
                379.561, eps=0.003756596
Epoch 133: f=
                379.556, eps=0.003944426
Epoch 134: f=
                379.552, eps=0.004141647
Epoch 135: f=
                379.548, eps=0.004348730
Epoch 136: f=
                379.543, eps=0.004566166
Epoch 137: f=
                379.539, eps=0.004794475
Epoch 138: f=
                379.535, eps=0.005034198
Epoch 139: f=
                379.530, eps=0.005285908
Epoch 140: f=
                379.526, eps=0.005550204
Epoch 141: f=
                379.522, eps=0.005827714
Epoch 142: f=
                379.517, eps=0.006119100
Epoch 143: f=
                379.513, eps=0.006425055
Epoch 144: f=
                379.509, eps=0.006746307
Epoch 145: f=
                379.504, eps=0.007083623
Epoch 146: f=
                379.500, eps=0.007437804
Epoch 147: f=
                379.498, eps=0.007809694
Epoch 148: f=
                379.508, eps=0.003904847
Epoch 149: f=
                379.518, eps=0.001952423
Epoch 150: f=
                379.490, eps=0.002050045
Epoch 151: f=
                379.489, eps=0.002152547
Epoch 152: f=
                379.488, eps=0.002260174
Epoch 153: f=
                379.487, eps=0.002373183
Epoch 154: f=
                379.486, eps=0.002491842
Epoch 155: f=
                379.485, eps=0.002616434
Epoch 156: f=
                379.484, eps=0.002747256
Epoch 157: f=
                379.483, eps=0.002884619
Epoch 158: f=
                379.482, eps=0.003028850
Epoch 159: f=
                379.481, eps=0.003180292
Epoch 160: f=
                379.479, eps=0.003339307
Epoch 161: f=
                379.478, eps=0.003506272
```

```
Epoch 162: f=
                379.477, eps=0.003681586
Epoch 163: f=
                379.476, eps=0.003865665
Epoch 164: f=
                379.475, eps=0.004058948
Epoch 165: f=
                379.474, eps=0.004261896
Epoch 166: f=
                379.472, eps=0.004474990
Epoch 167: f=
                379.471, eps=0.004698740
Epoch 168: f=
                379.470, eps=0.004933677
Epoch 169: f=
                379.469, eps=0.005180361
Epoch 170: f=
                379.467, eps=0.005439379
Epoch 171: f=
                379.466, eps=0.005711348
Epoch 172: f=
                379.465, eps=0.005996915
Epoch 173: f=
                379.464, eps=0.006296761
Epoch 174: f=
                379.463, eps=0.006611599
Epoch 175: f=
                379.469, eps=0.003305799
                379.468, eps=0.003471089
Epoch 176: f=
Epoch 177: f=
                379.468, eps=0.001735545
Epoch 178: f=
                379.460, eps=0.001822322
Epoch 179: f=
                379.460, eps=0.001913438
Epoch 180: f=
                379.459, eps=0.002009110
Epoch 181: f=
                379.459, eps=0.002109565
Epoch 182: f=
                379.459, eps=0.002215044
Epoch 183: f=
                379.458, eps=0.002325796
Epoch 184: f=
                379.458, eps=0.002442086
Epoch 185: f=
                379.458, eps=0.002564190
Epoch 186: f=
                379.457, eps=0.002692399
Epoch 187: f=
                379.457, eps=0.002827019
Epoch 188: f=
                379.457, eps=0.002968370
Epoch 189: f=
                379.456, eps=0.003116789
Epoch 190: f=
                379.456, eps=0.003272628
Epoch 191: f=
                379.455, eps=0.003436260
Epoch 192: f=
                379.455, eps=0.003608073
Epoch 193: f=
                379.455, eps=0.003788476
Epoch 194: f=
                379.454, eps=0.003977900
Epoch 195: f=
                379.454, eps=0.004176795
Epoch 196: f=
                379.453, eps=0.004385635
Epoch 197: f=
                379.453, eps=0.004604917
Epoch 198: f=
                379.453, eps=0.004835163
Epoch 199: f=
                379.452, eps=0.005076921
Epoch 200: f=
                379.452, eps=0.005330767
Epoch 201: f=
                379.451, eps=0.005597305
Epoch 202: f=
                379.451, eps=0.005877170
Epoch 203: f=
                379.450, eps=0.006171029
Epoch 204: f=
                379.450, eps=0.006479580
Epoch 205: f=
                379.450, eps=0.006803559
Epoch 206: f=
                379.449, eps=0.007143737
Epoch 207: f=
                379.449, eps=0.007500924
Epoch 208: f=
                379.448, eps=0.007875970
Epoch 209: f=
                379.448, eps=0.008269769
```

```
Epoch 210: f=
                379.448, eps=0.008683257
Epoch 211: f=
                379.453, eps=0.004341629
Epoch 212: f=
                379.461, eps=0.002170814
Epoch 213: f=
                379.448, eps=0.002279355
Epoch 214: f=
                379.447, eps=0.002393323
Epoch 215: f=
                379.447, eps=0.002512989
Epoch 216: f=
                379.447, eps=0.002638638
Epoch 217: f=
                379.447, eps=0.002770570
Epoch 218: f=
                379.447, eps=0.002909099
Epoch 219: f=
                379.447, eps=0.003054554
Epoch 220: f=
                379.446, eps=0.003207282
Epoch 221: f=
                379.446, eps=0.003367646
Epoch 222: f=
                379.446, eps=0.003536028
Epoch 223: f=
                379.446, eps=0.003712829
Epoch 224: f=
                379.446, eps=0.003898471
Epoch 225: f=
                379.446, eps=0.004093394
Epoch 226: f=
                379.446, eps=0.004298064
Epoch 227: f=
                379.446, eps=0.004512967
Epoch 228: f=
                379.446, eps=0.004738616
Epoch 229: f=
                379.446, eps=0.004975546
Epoch 230: f=
                379.446, eps=0.005224324
Epoch 231: f=
                379.446, eps=0.002612162
Epoch 232: f=
                379.445, eps=0.002742770
Epoch 233: f=
                379.445, eps=0.002879908
Epoch 234: f=
                379.445, eps=0.003023904
Epoch 235: f=
                379.445, eps=0.003175099
Epoch 236: f=
                379.445, eps=0.003333854
Epoch 237: f=
                379.445, eps=0.003500547
Epoch 238: f=
                379.445, eps=0.003675574
Epoch 239: f=
                379.445, eps=0.003859353
Epoch 240: f=
                379.445, eps=0.004052320
Epoch 241: f=
                379.445, eps=0.004254936
Epoch 242: f=
                379.445, eps=0.002127468
Epoch 243: f=
                379.445, eps=0.002233842
Epoch 244: f=
                379.445, eps=0.002345534
Epoch 245: f=
                379.445, eps=0.002462810
Epoch 246: f=
                379.445, eps=0.002585951
Epoch 247: f=
                379.445, eps=0.002715248
Epoch 248: f=
                379.445, eps=0.002851011
Epoch 249: f=
                379.445, eps=0.002993561
Epoch 250: f=
                379.444, eps=0.003143239
Epoch 251: f=
                379.444, eps=0.003300401
Epoch 252: f=
                379.444, eps=0.003465421
Epoch 253: f=
                379.444, eps=0.003638693
Epoch 254: f=
                379.444, eps=0.003820627
Epoch 255: f=
                379.444, eps=0.004011659
Epoch 256: f=
                379.444, eps=0.004212241
                379.444, eps=0.004422854
Epoch 257: f=
```

```
Epoch 258: f=
                379.444, eps=0.004643996
Epoch 259: f=
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Epoch 260: f=
                379.444, eps=0.005120006
Epoch 261: f=
                379.444, eps=0.005376006
Epoch 262: f=
                379.444, eps=0.005644806
Epoch 263: f=
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Epoch 264: f=
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Epoch 265: f=
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Epoch 266: f=
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Epoch 267: f=
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                379.444, eps=0.003602181
Epoch 268: f=
Epoch 269: f=
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Epoch 270: f=
                379.444, eps=0.001891145
Epoch 271: f=
                379.444, eps=0.001985702
Epoch 272: f=
                379.444, eps=0.002084987
Epoch 273: f=
                379.444, eps=0.002189237
Epoch 274: f=
                379.444, eps=0.002298699
Epoch 275: f=
                379.444, eps=0.002413634
Epoch 276: f=
                379.444, eps=0.002534315
Epoch 277: f=
                379.444, eps=0.002661031
Epoch 278: f=
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Epoch 279: f=
                379.444, eps=0.002933787
Epoch 280: f=
                379.444, eps=0.003080476
Epoch 281: f=
                379.444, eps=0.003234500
Epoch 282: f=
                379.444, eps=0.003396225
Epoch 283: f=
                379.444, eps=0.003566036
Epoch 284: f=
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Epoch 285: f=
                379.444, eps=0.003931555
Epoch 286: f=
                379.444, eps=0.004128133
Epoch 287: f=
                379.444, eps=0.004334539
Epoch 288: f=
                379.444, eps=0.004551266
Epoch 289: f=
                379.444, eps=0.004778830
Epoch 290: f=
                379.444, eps=0.005017771
Epoch 291: f=
                379.444, eps=0.005268660
Epoch 292: f=
                379.444, eps=0.005532093
Epoch 293: f=
                379.444, eps=0.005808697
Epoch 294: f=
                379.444, eps=0.006099132
Epoch 295: f=
                379.444, eps=0.006404089
Epoch 296: f=
                379.444, eps=0.006724293
Epoch 297: f=
                379.444, eps=0.007060508
Epoch 298: f=
                379.444, eps=0.007413533
Epoch 299: f=
                379.444, eps=0.007784210
Epoch 300: f=
                379.444, eps=0.003892105
Epoch 301: f=
                379.444, eps=0.001946052
Epoch 302: f=
                379.443, eps=0.002043355
Epoch 303: f=
                379.443, eps=0.002145523
Epoch 304: f=
                379.443, eps=0.002252799
Epoch 305: f=
                379.443, eps=0.002365439
```

```
Epoch 306: f=
                379.443, eps=0.002483711
Epoch 307: f=
                379.443, eps=0.002607896
Epoch 308: f=
                379.443, eps=0.002738291
Epoch 309: f=
                379.443, eps=0.002875206
Epoch 310: f=
                379.443, eps=0.003018966
Epoch 311: f=
                379.443, eps=0.003169914
Epoch 312: f=
                379.443, eps=0.003328410
Epoch 313: f=
                379.443, eps=0.003494831
Epoch 314: f=
                379.443, eps=0.003669572
Epoch 315: f=
                379.443, eps=0.003853051
Epoch 316: f=
                379.443, eps=0.004045703
Epoch 317: f=
                379.443, eps=0.004247988
Epoch 318: f=
                379.443, eps=0.004460388
Epoch 319: f=
                379.443, eps=0.004683407
Epoch 320: f=
                379.443, eps=0.004917578
Epoch 321: f=
                379.443, eps=0.005163456
Epoch 322: f=
                379.443, eps=0.005421629
Epoch 323: f=
                379.443, eps=0.005692711
Epoch 324: f=
                379.443, eps=0.005977346
Epoch 325: f=
                379.443, eps=0.006276214
Epoch 326: f=
                379.443, eps=0.006590024
Epoch 327: f=
                379.443, eps=0.003295012
Epoch 328: f=
                379.443, eps=0.003459763
Epoch 329: f=
                379.443, eps=0.003632751
Epoch 330: f=
                379.443, eps=0.001816375
Epoch 331: f=
                379.443, eps=0.001907194
Epoch 332: f=
                379.443, eps=0.002002554
Epoch 333: f=
                379.443, eps=0.002102682
Epoch 334: f=
                379.443, eps=0.002207816
Epoch 335: f=
                379.443, eps=0.002318206
Epoch 336: f=
                379.443, eps=0.002434117
Epoch 337: f=
                379.443, eps=0.002555823
Epoch 338: f=
                379.443, eps=0.002683614
Epoch 339: f=
                379.443, eps=0.002817794
Epoch 340: f=
                379.443, eps=0.002958684
Epoch 341: f=
                379.443, eps=0.003106618
Epoch 342: f=
                379.443, eps=0.003261949
Epoch 343: f=
                379.443, eps=0.003425047
Epoch 344: f=
                379.443, eps=0.003596299
Epoch 345: f=
                379.443, eps=0.003776114
Epoch 346: f=
                379.443, eps=0.003964920
Epoch 347: f=
                379.443, eps=0.004163166
Epoch 348: f=
                379.443, eps=0.004371324
Epoch 349: f=
                379.443, eps=0.004589890
Epoch 350: f=
                379.443, eps=0.004819385
Epoch 351: f=
                379.443, eps=0.005060354
Epoch 352: f=
                379.443, eps=0.005313372
Epoch 353: f=
                379.443, eps=0.005579040
```

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Epoch 354: f=
                379.443, eps=0.005857992
Epoch 355: f=
                379.443, eps=0.006150892
Epoch 356: f=
                379.443, eps=0.006458437
Epoch 357: f=
                379.443, eps=0.006781358
Epoch 358: f=
                379.443, eps=0.007120426
Epoch 359: f=
                379.443, eps=0.007476448
Epoch 360: f=
                379.443, eps=0.003738224
Epoch 361: f=
                379.443, eps=0.001869112
Epoch 362: f=
                379.443, eps=0.001962567
Epoch 363: f=
                379.443, eps=0.002060696
Epoch 364: f=
                379.443, eps=0.002163731
Epoch 365: f=
                379.443, eps=0.002271917
Epoch 366: f=
                379.443, eps=0.002385513
Epoch 367: f=
                379.443, eps=0.002504789
Epoch 368: f=
                379.443, eps=0.002630028
Epoch 369: f=
                379.443, eps=0.002761530
Epoch 370: f=
                379.443, eps=0.002899606
Epoch 371: f=
                379.443, eps=0.003044586
Epoch 372: f=
                379.443, eps=0.003196816
Epoch 373: f=
                379.443, eps=0.003356656
Epoch 374: f=
                379.443, eps=0.003524489
Epoch 375: f=
                379.443, eps=0.003700714
Epoch 376: f=
                379.443, eps=0.003885749
Epoch 377: f=
                379.443, eps=0.004080037
Epoch 378: f=
                379.443, eps=0.004284039
Epoch 379: f=
                379.443, eps=0.004498241
Epoch 380: f=
                379.443, eps=0.004723153
Epoch 381: f=
                379.443, eps=0.004959310
Epoch 382: f=
                379.443, eps=0.005207276
Epoch 383: f=
                379.443, eps=0.005467640
Epoch 384: f=
                379.443, eps=0.005741022
Epoch 385: f=
                379.443, eps=0.006028073
Epoch 386: f=
                379.443, eps=0.006329476
Epoch 387: f=
                379.443, eps=0.006645950
Epoch 388: f=
                379.443, eps=0.006978248
Epoch 389: f=
                379.443, eps=0.007327160
Epoch 390: f=
                379.443, eps=0.003663580
Epoch 391: f=
                379.443, eps=0.001831790
Epoch 392: f=
                379.443, eps=0.001923379
Epoch 393: f=
                379.443, eps=0.002019548
Epoch 394: f=
                379.443, eps=0.002120526
Epoch 395: f=
                379.443, eps=0.002226552
Epoch 396: f=
                379.443, eps=0.002337880
Epoch 397: f=
                379.443, eps=0.002454774
Epoch 398: f=
                379.443, eps=0.002577512
Epoch 399: f=
                379.443, eps=0.002706388
Epoch 400: f=
                379.443, eps=0.002841708
Epoch 401: f=
                379.443, eps=0.002983793
```

```
Epoch 402: f=
                379.443, eps=0.003132983
Epoch 403: f=
                379.443, eps=0.003289632
Epoch 404: f=
                379.443, eps=0.003454113
Epoch 405: f=
                379.443, eps=0.003626819
Epoch 406: f=
                379.443, eps=0.003808160
Epoch 407: f=
                379.443, eps=0.003998568
Epoch 408: f=
                379.443, eps=0.004198496
Epoch 409: f=
                379.443, eps=0.004408421
Epoch 410: f=
                379.443, eps=0.004628842
Epoch 411: f=
                379.443, eps=0.004860284
Epoch 412: f=
                379.443, eps=0.005103298
Epoch 413: f=
                379.443, eps=0.005358463
Epoch 414: f=
                379.443, eps=0.005626387
Epoch 415: f=
                379.443, eps=0.005907706
Epoch 416: f=
                379.443, eps=0.006203091
Epoch 417: f=
                379.443, eps=0.006513246
Epoch 418: f=
                379.443, eps=0.006838908
Epoch 419: f=
                379.443, eps=0.007180853
Epoch 420: f=
                379.443, eps=0.007539896
Epoch 421: f=
                379.443, eps=0.003769948
Epoch 422: f=
                379.443, eps=0.001884974
Epoch 423: f=
                379.443, eps=0.001979223
Epoch 424: f=
                379.443, eps=0.002078184
Epoch 425: f=
                379.443, eps=0.002182093
Epoch 426: f=
                379.443, eps=0.002291198
Epoch 427: f=
                379.443, eps=0.002405758
Epoch 428: f=
                379.443, eps=0.002526045
Epoch 429: f=
                379.443, eps=0.002652348
Epoch 430: f=
                379.443, eps=0.002784965
Epoch 431: f=
                379.443, eps=0.002924213
Epoch 432: f=
                379.443, eps=0.003070424
Epoch 433: f=
                379.443, eps=0.003223945
Epoch 434: f=
                379.443, eps=0.003385142
Epoch 435: f=
                379.443, eps=0.003554400
Epoch 436: f=
                379.443, eps=0.003732120
Epoch 437: f=
                379.443, eps=0.003918726
Epoch 438: f=
                379.443, eps=0.004114662
Epoch 439: f=
                379.443, eps=0.004320395
Epoch 440: f=
                379.443, eps=0.004536415
Epoch 441: f=
                379.443, eps=0.004763235
Epoch 442: f=
                379.443, eps=0.005001397
Epoch 443: f=
                379.443, eps=0.005251467
Epoch 444: f=
                379.443, eps=0.005514040
Epoch 445: f=
                379.443, eps=0.005789742
Epoch 446: f=
                379.443, eps=0.006079230
Epoch 447: f=
                379.443, eps=0.006383191
Epoch 448: f=
                379.443, eps=0.006702351
Epoch 449: f=
                379.443, eps=0.003351175
```

```
Epoch 450: f=
                379.443, eps=0.003518734
Epoch 451: f=
                379.443, eps=0.003694671
Epoch 452: f=
                379.443, eps=0.001847335
Epoch 453: f=
                379.443, eps=0.001939702
Epoch 454: f=
                379.443, eps=0.002036687
Epoch 455: f=
                379.443, eps=0.002138522
Epoch 456: f=
                379.443, eps=0.002245448
Epoch 457: f=
                379.443, eps=0.002357720
Epoch 458: f=
                379.443, eps=0.002475606
Epoch 459: f=
                379.443, eps=0.002599386
Epoch 460: f=
                379.443, eps=0.002729356
Epoch 461: f=
                379.443, eps=0.002865824
Epoch 462: f=
                379.443, eps=0.003009115
Epoch 463: f=
                379.443, eps=0.003159570
Epoch 464: f=
                379.443, eps=0.003317549
Epoch 465: f=
                379.443, eps=0.003483426
Epoch 466: f=
                379.443, eps=0.003657598
Epoch 467: f=
                379.443, eps=0.003840478
Epoch 468: f=
                379.443, eps=0.004032501
Epoch 469: f=
                379.443, eps=0.004234127
Epoch 470: f=
                379.443, eps=0.004445833
Epoch 471: f=
                379.443, eps=0.004668125
Epoch 472: f=
                379.443, eps=0.004901531
Epoch 473: f=
                379.443, eps=0.005146607
Epoch 474: f=
                379.443, eps=0.005403938
Epoch 475: f=
                379.443, eps=0.005674135
Epoch 476: f=
                379.443, eps=0.005957841
Epoch 477: f=
                379.443, eps=0.006255733
Epoch 478: f=
                379.443, eps=0.006568520
Epoch 479: f=
                379.443, eps=0.006896946
Epoch 480: f=
                379.443, eps=0.007241793
Epoch 481: f=
                379.443, eps=0.007603883
Epoch 482: f=
                379.443, eps=0.003801941
Epoch 483: f=
                379.443, eps=0.001900971
Epoch 484: f=
                379.443, eps=0.001996019
Epoch 485: f=
                379.443, eps=0.002095820
Epoch 486: f=
                379.443, eps=0.002200611
Epoch 487: f=
                379.443, eps=0.002310642
Epoch 488: f=
                379.443, eps=0.002426174
Epoch 489: f=
                379.443, eps=0.002547483
Epoch 490: f=
                379.443, eps=0.002674857
Epoch 491: f=
                379.443, eps=0.002808600
Epoch 492: f=
                379.443, eps=0.002949030
Epoch 493: f=
                379.443, eps=0.003096481
Epoch 494: f=
                379.443, eps=0.003251305
Epoch 495: f=
                379.443, eps=0.003413870
Epoch 496: f=
                379.443, eps=0.003584564
Epoch 497: f=
                379.443, eps=0.003763792
```

```
Epoch 498: f=
                379.443, eps=0.003951982
Epoch 499: f=
                379.443, eps=0.004149581
Result after 500 epochs: f=379.44334033241876
Epoch
        0: f=
               3571.324, eps=0.010000000
Epoch
        1: f=
               1583.127, eps=0.010500000
                947.857, eps=0.011025000
Epoch
        2: f=
Epoch
        3: f=
                693.550, eps=0.011576250
Epoch
        4: f=
                635.926, eps=0.012155063
Epoch
        5: f=
                570.957, eps=0.012762816
Epoch
        6: f=
                647.160, eps=0.006381408
        7: f=
                490.047, eps=0.006700478
Epoch
Epoch
        8: f=
                444.285, eps=0.007035502
                440.912, eps=0.007387277
Epoch
        9: f=
Epoch
      10: f=
                446.954, eps=0.003693639
Epoch
      11: f=
                426.953, eps=0.003878321
Epoch
      12: f=
                418.657, eps=0.004072237
Epoch
      13: f=
                415.928, eps=0.004275848
Epoch
      14: f=
                413.540, eps=0.004489641
Epoch
      15: f=
                411.871, eps=0.004714123
Epoch
                409.908, eps=0.004949829
       16: f=
Epoch
       17: f=
                409.495, eps=0.005197320
Epoch
      18: f=
                406.112, eps=0.005457186
Epoch
      19: f=
                407.358, eps=0.002728593
Epoch 20: f=
                400.862, eps=0.002865023
                399.721, eps=0.003008274
Epoch
      21: f=
Epoch 22: f=
                398.804, eps=0.003158688
Epoch
      23: f=
                397.930, eps=0.003316622
Epoch
      24: f=
                397.103, eps=0.003482453
Epoch
      25: f=
                396.314, eps=0.003656576
Epoch 26: f=
                395.586, eps=0.003839405
Epoch 27: f=
                394.929, eps=0.004031375
Epoch
                394.433, eps=0.004232944
      28: f=
Epoch 29: f=
                394.112, eps=0.004444591
Epoch
      30: f=
                394.219, eps=0.002222295
      31: f=
Epoch
                392.382, eps=0.002333410
Epoch
      32: f=
                392.096, eps=0.002450081
Epoch
      33: f=
                391.813, eps=0.002572585
Epoch
                391.535, eps=0.002701214
      34: f=
Epoch
      35: f=
                391.263, eps=0.002836275
Epoch 36: f=
                390.997, eps=0.002978088
Epoch 37: f=
                390.739, eps=0.003126993
Epoch
      38: f=
                390.488, eps=0.003283342
                390.247, eps=0.003447510
Epoch
      39: f=
Epoch
      40: f=
                390.015, eps=0.003619885
Epoch
      41: f=
                389.793, eps=0.003800879
Epoch
      42: f=
                389.581, eps=0.003990923
Epoch
      43: f=
                389.378, eps=0.004190469
                389.185, eps=0.004399993
Epoch 44: f=
```

```
Epoch 45: f=
                389.002, eps=0.004619993
Epoch 46: f=
                388.828, eps=0.004850992
Epoch 47: f=
                388.663, eps=0.005093542
                388.506, eps=0.005348219
Epoch
      48: f=
Epoch 49: f=
                388.358, eps=0.005615630
Epoch 50: f=
                388.218, eps=0.005896411
Epoch 51: f=
                388.088, eps=0.006191232
Epoch 52: f=
                387.978, eps=0.006500794
Epoch 53: f=
                387.991, eps=0.003250397
Epoch 54: f=
                387.918, eps=0.003412917
                387.868, eps=0.003583562
Epoch
      55: f=
Epoch 56: f=
                387.852, eps=0.003762741
                387.873, eps=0.001881370
Epoch 57: f=
Epoch 58: f=
                387.610, eps=0.001975439
                387.582, eps=0.002074211
Epoch 59: f=
Epoch 60: f=
                387.556, eps=0.002177921
Epoch 61: f=
                387.530, eps=0.002286817
Epoch
      62: f=
                387.504, eps=0.002401158
Epoch 63: f=
                387.477, eps=0.002521216
Epoch
                387.449, eps=0.002647277
      64: f=
Epoch
      65: f=
                387.422, eps=0.002779641
Epoch 66: f=
                387.394, eps=0.002918623
Epoch 67: f=
                387.366, eps=0.003064554
Epoch 68: f=
                387.338, eps=0.003217782
                387.310, eps=0.003378671
Epoch 69: f=
Epoch 70: f=
                387.282, eps=0.003547604
Epoch
      71: f=
                387.253, eps=0.003724984
Epoch
      72: f=
                387.225, eps=0.003911234
Epoch 73: f=
                387.197, eps=0.004106795
Epoch 74: f=
                387.169, eps=0.004312135
Epoch 75: f=
                387.142, eps=0.004527742
Epoch 76: f=
                387.114, eps=0.004754129
Epoch 77: f=
                387.088, eps=0.004991835
Epoch
      78: f=
                387.061, eps=0.005241427
Epoch
      79: f=
                387.035, eps=0.005503499
Epoch
      80: f=
                387.010, eps=0.005778674
Epoch 81: f=
                386.985, eps=0.006067607
Epoch 82: f=
                386.962, eps=0.006370988
Epoch 83: f=
                386.943, eps=0.006689537
Epoch 84: f=
                386.961, eps=0.003344768
Epoch 85: f=
                386.951, eps=0.003512007
Epoch
      86: f=
                386.952, eps=0.001756003
      87: f=
                386.890, eps=0.001843804
Epoch
Epoch
      88: f=
                386.885, eps=0.001935994
Epoch
      89: f=
                386.880, eps=0.002032793
Epoch
      90: f=
                386.874, eps=0.002134433
Epoch 91: f=
                386.869, eps=0.002241155
Epoch 92: f=
                386.863, eps=0.002353213
```

```
Epoch 93: f=
                386.858, eps=0.002470873
Epoch 94: f=
                386.852, eps=0.002594417
Epoch 95: f=
                386.846, eps=0.002724138
Epoch
      96: f=
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                386.665, eps=0.005001397
Epoch 443: f=
                386.665, eps=0.005251467
Epoch 444: f=
                386.665, eps=0.005514040
Epoch 445: f=
                386.665, eps=0.005789742
Epoch 446: f=
                386.665, eps=0.006079230
Epoch 447: f=
                386.665, eps=0.006383191
Epoch 448: f=
                386.665, eps=0.006702351
Epoch 449: f=
                386.665, eps=0.007037468
Epoch 450: f=
                386.665, eps=0.007389342
Epoch 451: f=
                386.665, eps=0.003694671
Epoch 452: f=
                386.665, eps=0.001847335
Epoch 453: f=
                386.665, eps=0.001939702
Epoch 454: f=
                386.665, eps=0.002036687
Epoch 455: f=
                386.665, eps=0.002138522
Epoch 456: f=
                386.665, eps=0.002245448
Epoch 457: f=
                386.665, eps=0.002357720
Epoch 458: f=
                386.665, eps=0.002475606
Epoch 459: f=
                386.665, eps=0.002599386
Epoch 460: f=
                386.665, eps=0.002729356
Epoch 461: f=
                386.665, eps=0.002865824
Epoch 462: f=
                386.665, eps=0.003009115
Epoch 463: f=
                386.665, eps=0.003159570
Epoch 464: f=
                386.665, eps=0.003317549
Epoch 465: f=
                386.665, eps=0.003483426
Epoch 466: f=
                386.665, eps=0.003657598
Epoch 467: f=
                386.665, eps=0.003840478
Epoch 468: f=
                386.665, eps=0.004032501
Epoch 469: f=
                386.665, eps=0.004234127
Epoch 470: f=
                386.665, eps=0.004445833
Epoch 471: f=
                386.665, eps=0.004668125
Epoch 472: f=
                386.665, eps=0.004901531
Epoch 473: f=
                386.665, eps=0.005146607
Epoch 474: f=
                386.665, eps=0.005403938
Epoch 475: f=
                386.665, eps=0.005674135
Epoch 476: f=
                386.665, eps=0.005957841
```

```
Epoch 477: f=
                386.665, eps=0.006255733
Epoch 478: f=
                386.665, eps=0.006568520
Epoch 479: f=
                386.665, eps=0.006896946
Epoch 480: f=
                386.665, eps=0.003448473
Epoch 481: f=
                386.665, eps=0.001724236
Epoch 482: f=
                386.665, eps=0.001810448
Epoch 483: f=
                386.665, eps=0.001900971
Epoch 484: f=
                386.665, eps=0.001996019
Epoch 485: f=
                386.665, eps=0.002095820
Epoch 486: f=
                386.665, eps=0.002200611
Epoch 487: f=
                386.665, eps=0.002310642
Epoch 488: f=
                386.665, eps=0.002426174
Epoch 489: f=
                386.665, eps=0.002547483
Epoch 490: f=
                386.665, eps=0.002674857
                386.665, eps=0.002808600
Epoch 491: f=
Epoch 492: f=
                386.665, eps=0.002949030
Epoch 493: f=
                386.665, eps=0.003096481
Epoch 494: f=
                386.665, eps=0.003251305
Epoch 495: f=
                386.665, eps=0.003413870
Epoch 496: f=
                386.665, eps=0.003584564
Epoch 497: f=
                386.665, eps=0.003763792
Epoch 498: f=
                386.665, eps=0.003951982
Epoch 499: f=
                386.665, eps=0.004149581
Result after 500 epochs: f=386.6645111344998
Epoch
        0: f=
               3739.131, eps=0.010000000
Epoch
        1: f=
               1821.126, eps=0.010500000
        2: f=
               1030.380, eps=0.011025000
Epoch
Epoch
        3: f=
                735.608, eps=0.011576250
Epoch
        4: f=
                669.348, eps=0.012155063
        5: f=
Epoch
                617.248, eps=0.012762816
Epoch
        6: f=
                849.649, eps=0.006381408
        7: f=
                526.653, eps=0.006700478
Epoch
        8: f=
                458.812, eps=0.007035502
Epoch
Epoch
        9: f=
                448.438, eps=0.007387277
       10: f=
                461.064, eps=0.003693639
Epoch
Epoch
       11: f=
                433.430, eps=0.003878321
Epoch
       12: f=
                427.388, eps=0.004072237
Epoch
       13: f=
                425.643, eps=0.004275848
Epoch
       14: f=
                424.239, eps=0.004489641
Epoch
      15: f=
                423.884, eps=0.004714123
Epoch
       16: f=
                422.486, eps=0.004949829
Epoch
       17: f=
                423.952, eps=0.002474914
Epoch
       18: f=
                419.543, eps=0.002598660
Epoch
      19: f=
                418.671, eps=0.002728593
Epoch
                418.223, eps=0.002865023
       20: f=
Epoch
       21: f=
                417.814, eps=0.003008274
Epoch
      22: f=
                417.442, eps=0.003158688
                417.097, eps=0.003316622
Epoch
      23: f=
```

```
Epoch 24: f=
                416.783, eps=0.003482453
Epoch
      25: f=
                416.496, eps=0.003656576
Epoch
      26: f=
                416.241, eps=0.003839405
                416.021, eps=0.004031375
Epoch
      27: f=
Epoch
      28: f=
                415.867, eps=0.004232944
                415.814, eps=0.004444591
Epoch
      29: f=
Epoch
      30: f=
                416.134, eps=0.002222295
Epoch 31: f=
                415.292, eps=0.002333410
Epoch 32: f=
                415.211, eps=0.002450081
Epoch 33: f=
                415.136, eps=0.002572585
                415.063, eps=0.002701214
Epoch
      34: f=
Epoch 35: f=
                414.992, eps=0.002836275
                414.924, eps=0.002978088
Epoch
      36: f=
Epoch
      37: f=
                414.858, eps=0.003126993
Epoch 38: f=
                414.796, eps=0.003283342
Epoch 39: f=
                414.736, eps=0.003447510
Epoch 40: f=
                414.678, eps=0.003619885
Epoch
      41: f=
                414.624, eps=0.003800879
Epoch 42: f=
                414.573, eps=0.003990923
Epoch 43: f=
                414.525, eps=0.004190469
Epoch
      44: f=
                414.480, eps=0.004399993
Epoch 45: f=
                414.439, eps=0.004619993
Epoch 46: f=
                414.402, eps=0.004850992
Epoch 47: f=
                414.373, eps=0.005093542
                414.377, eps=0.002546771
Epoch 48: f=
Epoch
      49: f=
                414.328, eps=0.002674109
                414.307, eps=0.002807815
Epoch 50: f=
Epoch 51: f=
                414.291, eps=0.002948206
Epoch 52: f=
                414.276, eps=0.003095616
Epoch 53: f=
                414.263, eps=0.003250397
Epoch 54: f=
                414.250, eps=0.003412917
Epoch 55: f=
                414.238, eps=0.003583562
Epoch 56: f=
                414.228, eps=0.003762741
Epoch 57: f=
                414.219, eps=0.003950878
      58: f=
Epoch
                414.215, eps=0.004148421
Epoch
      59: f=
                414.222, eps=0.002074211
Epoch
      60: f=
                414.192, eps=0.002177921
Epoch 61: f=
                414.185, eps=0.002286817
Epoch
      62: f=
                414.180, eps=0.002401158
Epoch 63: f=
                414.175, eps=0.002521216
Epoch 64: f=
                414.171, eps=0.002647277
Epoch
      65: f=
                414.167, eps=0.002779641
                414.163, eps=0.002918623
Epoch
      66: f=
Epoch
      67: f=
                414.159, eps=0.003064554
Epoch
      68: f=
                414.155, eps=0.003217782
Epoch
       69: f=
                414.151, eps=0.003378671
Epoch
      70: f=
                414.148, eps=0.003547604
      71: f=
                414.144, eps=0.003724984
Epoch
```

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Epoch 72: f=
                414.141, eps=0.003911234
Epoch
      73: f=
                414.138, eps=0.004106795
Epoch 74: f=
                414.135, eps=0.004312135
                414.132, eps=0.004527742
Epoch
      75: f=
Epoch 76: f=
                414.130, eps=0.004754129
Epoch 77: f=
                414.128, eps=0.004991835
Epoch 78: f=
                414.126, eps=0.005241427
Epoch 79: f=
                414.129, eps=0.002620714
Epoch 80: f=
                414.125, eps=0.002751749
Epoch 81: f=
                414.123, eps=0.002889337
Epoch
      82: f=
                414.122, eps=0.003033804
Epoch 83: f=
                414.121, eps=0.003185494
                414.120, eps=0.003344768
Epoch
      84: f=
Epoch
      85: f=
                414.119, eps=0.003512007
Epoch 86: f=
                414.119, eps=0.003687607
Epoch 87: f=
                414.119, eps=0.003871988
Epoch 88: f=
                414.119, eps=0.001935994
Epoch
      89: f=
                414.116, eps=0.002032793
Epoch 90: f=
                414.116, eps=0.002134433
Epoch 91: f=
                414.116, eps=0.002241155
Epoch
      92: f=
                414.116, eps=0.002353213
Epoch 93: f=
                414.115, eps=0.002470873
Epoch 94: f=
                414.115, eps=0.002594417
Epoch 95: f=
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                414.115, eps=0.002860345
Epoch 96: f=
Epoch
      97: f=
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                414.114, eps=0.003153530
Epoch
      98: f=
Epoch 99: f=
                414.114, eps=0.003311206
Epoch 100: f=
                414.114, eps=0.003476767
Epoch 101: f=
                414.113, eps=0.003650605
Epoch 102: f=
                414.113, eps=0.003833135
Epoch 103: f=
                414.113, eps=0.004024792
Epoch 104: f=
                414.113, eps=0.004226032
Epoch 105: f=
                414.113, eps=0.004437333
Epoch 106: f=
                414.112, eps=0.004659200
Epoch 107: f=
                414.112, eps=0.004892160
Epoch 108: f=
                414.112, eps=0.005136768
Epoch 109: f=
                414.112, eps=0.005393606
Epoch 110: f=
                414.112, eps=0.005663287
Epoch 111: f=
                414.112, eps=0.005946451
Epoch 112: f=
                414.112, eps=0.002973225
Epoch 113: f=
                414.112, eps=0.003121887
                414.112, eps=0.003277981
Epoch 114: f=
Epoch 115: f=
                414.112, eps=0.003441880
Epoch 116: f=
                414.112, eps=0.001720940
Epoch 117: f=
                414.111, eps=0.001806987
Epoch 118: f=
                414.111, eps=0.001897336
Epoch 119: f=
                414.111, eps=0.001992203
```

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Epoch 120: f=
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Epoch 121: f=
                414.111, eps=0.002196404
Epoch 122: f=
                414.111, eps=0.002306224
                414.111, eps=0.002421535
Epoch 123: f=
Epoch 124: f=
                414.111, eps=0.002542612
                414.111, eps=0.002669743
Epoch 125: f=
Epoch 126: f=
                414.111, eps=0.002803230
Epoch 127: f=
                414.111, eps=0.002943392
Epoch 128: f=
                414.111, eps=0.003090561
Epoch 129: f=
                414.111, eps=0.003245089
Epoch 130: f=
                414.111, eps=0.003407344
Epoch 131: f=
                414.111, eps=0.003577711
                414.111, eps=0.003756596
Epoch 132: f=
Epoch 133: f=
                414.111, eps=0.003944426
Epoch 134: f=
                414.111, eps=0.004141647
Epoch 135: f=
                414.111, eps=0.004348730
Epoch 136: f=
                414.111, eps=0.004566166
Epoch 137: f=
                414.111, eps=0.004794475
Epoch 138: f=
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Epoch 139: f=
                414.111, eps=0.005285908
Epoch 140: f=
                414.111, eps=0.005550204
Epoch 141: f=
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Epoch 142: f=
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Epoch 143: f=
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Epoch 144: f=
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Epoch 145: f=
                414.111, eps=0.007083623
                414.111, eps=0.007437804
Epoch 146: f=
Epoch 147: f=
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Epoch 148: f=
                414.111, eps=0.001859451
Epoch 149: f=
                414.111, eps=0.001952423
Epoch 150: f=
                414.111, eps=0.002050045
Epoch 151: f=
                414.111, eps=0.002152547
Epoch 152: f=
                414.111, eps=0.002260174
Epoch 153: f=
                414.111, eps=0.002373183
Epoch 154: f=
                414.111, eps=0.002491842
                414.111, eps=0.002616434
Epoch 155: f=
Epoch 156: f=
                414.111, eps=0.002747256
Epoch 157: f=
                414.111, eps=0.002884619
Epoch 158: f=
                414.111, eps=0.003028850
Epoch 159: f=
                414.111, eps=0.003180292
Epoch 160: f=
                414.111, eps=0.003339307
Epoch 161: f=
                414.111, eps=0.003506272
                414.111, eps=0.003681586
Epoch 162: f=
Epoch 163: f=
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Epoch 164: f=
                414.111, eps=0.004058948
Epoch 165: f=
                414.111, eps=0.004261896
Epoch 166: f=
                414.111, eps=0.004474990
Epoch 167: f=
                414.111, eps=0.004698740
```

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Epoch 168: f=
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Epoch 169: f=
                414.111, eps=0.005180361
Epoch 170: f=
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                414.111, eps=0.005711348
Epoch 171: f=
Epoch 172: f=
                414.111, eps=0.005996915
                414.111, eps=0.002998458
Epoch 173: f=
Epoch 174: f=
                414.111, eps=0.003148380
Epoch 175: f=
                414.111, eps=0.003305799
Epoch 176: f=
                414.111, eps=0.003471089
Epoch 177: f=
                414.111, eps=0.001735545
Epoch 178: f=
                414.111, eps=0.001822322
Epoch 179: f=
                414.111, eps=0.001913438
                414.111, eps=0.002009110
Epoch 180: f=
Epoch 181: f=
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Epoch 182: f=
                414.111, eps=0.002215044
Epoch 183: f=
                414.111, eps=0.002325796
Epoch 184: f=
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Epoch 185: f=
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Epoch 186: f=
                414.111, eps=0.002692399
Epoch 187: f=
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Epoch 188: f=
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Epoch 189: f=
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Epoch 190: f=
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Epoch 191: f=
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Epoch 193: f=
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Epoch 194: f=
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Epoch 195: f=
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Epoch 196: f=
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Epoch 197: f=
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Epoch 198: f=
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Epoch 199: f=
                414.111, eps=0.005076921
Epoch 200: f=
                414.111, eps=0.005330767
Epoch 201: f=
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Epoch 202: f=
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                414.111, eps=0.006171029
Epoch 203: f=
Epoch 204: f=
                414.111, eps=0.006479580
Epoch 205: f=
                414.111, eps=0.006803559
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Epoch 207: f=
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Epoch 208: f=
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Epoch 209: f=
                414.111, eps=0.001875231
Epoch 210: f=
                414.111, eps=0.001968993
Epoch 211: f=
                414.111, eps=0.002067442
Epoch 212: f=
                414.111, eps=0.002170814
Epoch 213: f=
                414.111, eps=0.002279355
Epoch 214: f=
                414.111, eps=0.002393323
Epoch 215: f=
                414.111, eps=0.002512989
```

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Epoch 216: f=
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Epoch 217: f=
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Epoch 218: f=
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Epoch 219: f=
                414.111, eps=0.003054554
Epoch 220: f=
                414.111, eps=0.003207282
Epoch 221: f=
                414.111, eps=0.003367646
Epoch 222: f=
                414.111, eps=0.003536028
Epoch 223: f=
                414.111, eps=0.003712829
Epoch 224: f=
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Epoch 225: f=
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Epoch 227: f=
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Epoch 233: f=
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Epoch 234: f=
                414.111, eps=0.006350198
Epoch 235: f=
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Epoch 237: f=
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Epoch 239: f=
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Epoch 240: f=
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Epoch 241: f=
                414.111, eps=0.002026160
Epoch 242: f=
                414.111, eps=0.002127468
Epoch 243: f=
                414.111, eps=0.002233842
Epoch 244: f=
                414.111, eps=0.002345534
Epoch 245: f=
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Epoch 246: f=
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Epoch 247: f=
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Epoch 248: f=
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Epoch 249: f=
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Epoch 250: f=
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Epoch 251: f=
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Epoch 252: f=
                414.111, eps=0.003465421
Epoch 253: f=
                414.111, eps=0.003638693
Epoch 254: f=
                414.111, eps=0.003820627
Epoch 255: f=
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Epoch 256: f=
                414.111, eps=0.004212241
Epoch 257: f=
                414.111, eps=0.004422854
                414.111, eps=0.004643996
Epoch 258: f=
Epoch 259: f=
                414.111, eps=0.004876196
Epoch 260: f=
                414.111, eps=0.005120006
Epoch 261: f=
                414.111, eps=0.005376006
Epoch 262: f=
                414.111, eps=0.005644806
Epoch 263: f=
                414.111, eps=0.005927047
```

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Epoch 264: f=
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Epoch 265: f=
                414.111, eps=0.006534569
Epoch 266: f=
                414.111, eps=0.006861297
                414.111, eps=0.007204362
Epoch 267: f=
Epoch 268: f=
                414.111, eps=0.003602181
Epoch 269: f=
                414.111, eps=0.001801091
Epoch 270: f=
                414.111, eps=0.001891145
Epoch 271: f=
                414.111, eps=0.001985702
Epoch 272: f=
                414.111, eps=0.002084987
Epoch 273: f=
                414.111, eps=0.002189237
Epoch 274: f=
                414.111, eps=0.002298699
Epoch 275: f=
                414.111, eps=0.002413634
                414.111, eps=0.002534315
Epoch 276: f=
Epoch 277: f=
                414.111, eps=0.002661031
Epoch 278: f=
                414.111, eps=0.002794083
Epoch 279: f=
                414.111, eps=0.002933787
Epoch 280: f=
                414.111, eps=0.003080476
Epoch 281: f=
                414.111, eps=0.003234500
Epoch 282: f=
                414.111, eps=0.003396225
Epoch 283: f=
                414.111, eps=0.003566036
Epoch 284: f=
                414.111, eps=0.003744338
Epoch 285: f=
                414.111, eps=0.003931555
Epoch 286: f=
                414.111, eps=0.004128133
Epoch 287: f=
                414.111, eps=0.004334539
Epoch 288: f=
                414.111, eps=0.004551266
Epoch 289: f=
                414.111, eps=0.004778830
Epoch 290: f=
                414.111, eps=0.005017771
Epoch 291: f=
                414.111, eps=0.005268660
Epoch 292: f=
                414.111, eps=0.005532093
Epoch 293: f=
                414.111, eps=0.005808697
Epoch 294: f=
                414.111, eps=0.006099132
Epoch 295: f=
                414.111, eps=0.006404089
Epoch 296: f=
                414.111, eps=0.003202044
                414.111, eps=0.003362147
Epoch 297: f=
Epoch 298: f=
                414.111, eps=0.003530254
Epoch 299: f=
                414.111, eps=0.001765127
Epoch 300: f=
                414.111, eps=0.001853383
Epoch 301: f=
                414.111, eps=0.001946052
Epoch 302: f=
                414.111, eps=0.002043355
Epoch 303: f=
                414.111, eps=0.002145523
Epoch 304: f=
                414.111, eps=0.002252799
Epoch 305: f=
                414.111, eps=0.002365439
Epoch 306: f=
                414.111, eps=0.002483711
Epoch 307: f=
                414.111, eps=0.002607896
Epoch 308: f=
                414.111, eps=0.002738291
Epoch 309: f=
                414.111, eps=0.002875206
Epoch 310: f=
                414.111, eps=0.003018966
Epoch 311: f=
                414.111, eps=0.003169914
```

```
Epoch 312: f=
                414.111, eps=0.003328410
Epoch 313: f=
                414.111, eps=0.003494831
Epoch 314: f=
                414.111, eps=0.003669572
                414.111, eps=0.003853051
Epoch 315: f=
Epoch 316: f=
                414.111, eps=0.004045703
Epoch 317: f=
                414.111, eps=0.004247988
Epoch 318: f=
                414.111, eps=0.004460388
Epoch 319: f=
                414.111, eps=0.004683407
Epoch 320: f=
                414.111, eps=0.004917578
Epoch 321: f=
                414.111, eps=0.005163456
Epoch 322: f=
                414.111, eps=0.005421629
Epoch 323: f=
                414.111, eps=0.005692711
Epoch 324: f=
                414.111, eps=0.005977346
Epoch 325: f=
                414.111, eps=0.006276214
Epoch 326: f=
                414.111, eps=0.006590024
Epoch 327: f=
                414.111, eps=0.006919525
Epoch 328: f=
                414.111, eps=0.003459763
Epoch 329: f=
                414.111, eps=0.001729881
Epoch 330: f=
                414.111, eps=0.001816375
Epoch 331: f=
                414.111, eps=0.001907194
Epoch 332: f=
                414.111, eps=0.002002554
Epoch 333: f=
                414.111, eps=0.002102682
Epoch 334: f=
                414.111, eps=0.002207816
Epoch 335: f=
                414.111, eps=0.002318206
Epoch 336: f=
                414.111, eps=0.002434117
Epoch 337: f=
                414.111, eps=0.002555823
Epoch 338: f=
                414.111, eps=0.002683614
Epoch 339: f=
                414.111, eps=0.002817794
Epoch 340: f=
                414.111, eps=0.002958684
Epoch 341: f=
                414.111, eps=0.003106618
Epoch 342: f=
                414.111, eps=0.003261949
Epoch 343: f=
                414.111, eps=0.003425047
Epoch 344: f=
                414.111, eps=0.003596299
Epoch 345: f=
                414.111, eps=0.003776114
Epoch 346: f=
                414.111, eps=0.003964920
Epoch 347: f=
                414.111, eps=0.004163166
Epoch 348: f=
                414.111, eps=0.004371324
Epoch 349: f=
                414.111, eps=0.004589890
Epoch 350: f=
                414.111, eps=0.004819385
Epoch 351: f=
                414.111, eps=0.005060354
Epoch 352: f=
                414.111, eps=0.005313372
Epoch 353: f=
                414.111, eps=0.005579040
Epoch 354: f=
                414.111, eps=0.005857992
Epoch 355: f=
                414.111, eps=0.006150892
Epoch 356: f=
                414.111, eps=0.006458437
Epoch 357: f=
                414.111, eps=0.006781358
Epoch 358: f=
                414.111, eps=0.007120426
Epoch 359: f=
                414.111, eps=0.003560213
```

```
Epoch 360: f=
                414.111, eps=0.003738224
Epoch 361: f=
                414.111, eps=0.001869112
Epoch 362: f=
                414.111, eps=0.001962567
                414.111, eps=0.002060696
Epoch 363: f=
Epoch 364: f=
                414.111, eps=0.002163731
Epoch 365: f=
                414.111, eps=0.002271917
Epoch 366: f=
                414.111, eps=0.002385513
Epoch 367: f=
                414.111, eps=0.002504789
Epoch 368: f=
                414.111, eps=0.002630028
Epoch 369: f=
                414.111, eps=0.002761530
Epoch 370: f=
                414.111, eps=0.002899606
Epoch 371: f=
                414.111, eps=0.003044586
Epoch 372: f=
                414.111, eps=0.003196816
Epoch 373: f=
                414.111, eps=0.003356656
Epoch 374: f=
                414.111, eps=0.003524489
Epoch 375: f=
                414.111, eps=0.003700714
Epoch 376: f=
                414.111, eps=0.003885749
Epoch 377: f=
                414.111, eps=0.004080037
Epoch 378: f=
                414.111, eps=0.004284039
Epoch 379: f=
                414.111, eps=0.002142019
Epoch 380: f=
                414.111, eps=0.002249120
Epoch 381: f=
                414.111, eps=0.002361576
Epoch 382: f=
                414.111, eps=0.002479655
Epoch 383: f=
                414.111, eps=0.001239828
                414.111, eps=0.001301819
Epoch 384: f=
Epoch 385: f=
                414.111, eps=0.001366910
Epoch 386: f=
                414.111, eps=0.001435255
Epoch 387: f=
                414.111, eps=0.001507018
Epoch 388: f=
                414.111, eps=0.001582369
Epoch 389: f=
                414.111, eps=0.000791185
Epoch 390: f=
                414.111, eps=0.000395592
Epoch 391: f=
                414.111, eps=0.000415372
Epoch 392: f=
                414.111, eps=0.000436140
Epoch 393: f=
                414.111, eps=0.000457947
Epoch 394: f=
                414.111, eps=0.000228974
Epoch 395: f=
                414.111, eps=0.000240422
Epoch 396: f=
                414.111, eps=0.000252444
Epoch 397: f=
                414.111, eps=0.000265066
Epoch 398: f=
                414.111, eps=0.000278319
Epoch 399: f=
                414.111, eps=0.000292235
Epoch 400: f=
                414.111, eps=0.000146117
Epoch 401: f=
                414.111, eps=0.000153423
                414.111, eps=0.000161095
Epoch 402: f=
Epoch 403: f=
                414.111, eps=0.000080547
Epoch 404: f=
                414.111, eps=0.000084575
Epoch 405: f=
                414.111, eps=0.000042287
Epoch 406: f=
                414.111, eps=0.000044402
Epoch 407: f=
                414.111, eps=0.000046622
```

```
Epoch 408: f=
                414.111, eps=0.000048953
Epoch 409: f=
                414.111, eps=0.000051400
Epoch 410: f=
                414.111, eps=0.000053971
                414.111, eps=0.000056669
Epoch 411: f=
Epoch 412: f=
                414.111, eps=0.000059502
Epoch 413: f=
                414.111, eps=0.000029751
Epoch 414: f=
                414.111, eps=0.000031239
Epoch 415: f=
                414.111, eps=0.000032801
Epoch 416: f=
                414.111, eps=0.000034441
Epoch 417: f=
                414.111, eps=0.000017220
                414.111, eps=0.000008610
Epoch 418: f=
Epoch 419: f=
                414.111, eps=0.000009041
                414.111, eps=0.000009493
Epoch 420: f=
Epoch 421: f=
                414.111, eps=0.000009967
Epoch 422: f=
                414.111, eps=0.000010466
Epoch 423: f=
                414.111, eps=0.000005233
Epoch 424: f=
                414.111, eps=0.000005495
Epoch 425: f=
                414.111, eps=0.000005769
                414.111, eps=0.000006058
Epoch 426: f=
Epoch 427: f=
                414.111, eps=0.000006361
Epoch 428: f=
                414.111, eps=0.000006679
Epoch 429: f=
                414.111, eps=0.000007013
Epoch 430: f=
                414.111, eps=0.000003506
Epoch 431: f=
                414.111, eps=0.000003682
                414.111, eps=0.000003866
Epoch 432: f=
Epoch 433: f=
                414.111, eps=0.000001933
Epoch 434: f=
                414.111, eps=0.000002029
Epoch 435: f=
                414.111, eps=0.000002131
Epoch 436: f=
                414.111, eps=0.000002237
Epoch 437: f=
                414.111, eps=0.000002349
Epoch 438: f=
                414.111, eps=0.000002467
Epoch 439: f=
                414.111, eps=0.000001233
Epoch 440: f=
                414.111, eps=0.000001295
                414.111, eps=0.000001360
Epoch 441: f=
Epoch 442: f=
                414.111, eps=0.000001428
Epoch 443: f=
                414.111, eps=0.000001499
Epoch 444: f=
                414.111, eps=0.000000750
                414.111, eps=0.000000787
Epoch 445: f=
Epoch 446: f=
                414.111, eps=0.000000826
Epoch 447: f=
                414.111, eps=0.000000868
Epoch 448: f=
                414.111, eps=0.000000911
Epoch 449: f=
                414.111, eps=0.000000456
                414.111, eps=0.000000478
Epoch 450: f=
Epoch 451: f=
                414.111, eps=0.000000502
Epoch 452: f=
                414.111, eps=0.000000527
Epoch 453: f=
                414.111, eps=0.000000554
Epoch 454: f=
                414.111, eps=0.000000581
Epoch 455: f=
                414.111, eps=0.000000611
```

```
Epoch 456: f=
                414.111, eps=0.000000305
Epoch 457: f=
                414.111, eps=0.000000321
Epoch 458: f=
                414.111, eps=0.000000337
                414.111, eps=0.000000353
Epoch 459: f=
Epoch 460: f=
                414.111, eps=0.000000371
Epoch 461: f=
                414.111, eps=0.000000390
Epoch 462: f=
                414.111, eps=0.000000195
Epoch 463: f=
                414.111, eps=0.000000097
Epoch 464: f=
                414.111, eps=0.000000102
Epoch 465: f=
                414.111, eps=0.000000107
                414.111, eps=0.000000113
Epoch 466: f=
Epoch 467: f=
                414.111, eps=0.000000118
                414.111, eps=0.000000124
Epoch 468: f=
Epoch 469: f=
                414.111, eps=0.000000062
Epoch 470: f=
                414.111, eps=0.000000031
Epoch 471: f=
                414.111, eps=0.000000033
Epoch 472: f=
                414.111, eps=0.000000034
Epoch 473: f=
                414.111, eps=0.000000036
                414.111, eps=0.000000038
Epoch 474: f=
                414.111, eps=0.000000019
Epoch 475: f=
Epoch 476: f=
                414.111, eps=0.000000020
Epoch 477: f=
                414.111, eps=0.000000021
Epoch 478: f=
                414.111, eps=0.000000010
Epoch 479: f=
                414.111, eps=0.000000011
                414.111, eps=0.000000011
Epoch 480: f=
                414.111, eps=0.000000012
Epoch 481: f=
Epoch 482: f=
                414.111, eps=0.000000013
Epoch 483: f=
                414.111, eps=0.000000006
Epoch 484: f=
                414.111, eps=0.000000007
Epoch 485: f=
                414.111, eps=0.000000007
                414.111, eps=0.000000007
Epoch 486: f=
Epoch 487: f=
                414.111, eps=0.000000008
Epoch 488: f=
                414.111, eps=0.000000008
                414.111, eps=0.000000008
Epoch 489: f=
Epoch 490: f=
                414.111, eps=0.000000009
Epoch 491: f=
                414.111, eps=0.000000009
Epoch 492: f=
                414.111, eps=0.000000010
                414.111, eps=0.000000010
Epoch 493: f=
Epoch 494: f=
                414.111, eps=0.000000011
Epoch 495: f=
                414.111, eps=0.000000011
Epoch 496: f=
                414.111, eps=0.000000012
Epoch 497: f=
                414.111, eps=0.000000013
                414.111, eps=0.00000013
Epoch 498: f=
Epoch 499: f=
                414.111, eps=0.000000014
Result after 500 epochs: f=414.11111711137437
Epoch
        0: f=
               4074.746, eps=0.010000000
Epoch
               2265.591, eps=0.010500000
        1: f=
        2: f=
               1082.377, eps=0.011025000
Epoch
```

```
Epoch
        3: f=
                716.768, eps=0.011576250
Epoch
        4: f=
                681.485, eps=0.012155063
        5: f=
Epoch
                725.750, eps=0.006077531
                725.786, eps=0.003038766
Epoch
        6: f=
Epoch
        7: f=
                550.766, eps=0.003190704
Epoch
        8: f=
                487.585, eps=0.003350239
Epoch
        9: f=
                468.709, eps=0.003517751
Epoch
      10: f=
                460.748, eps=0.003693639
Epoch
      11: f=
                457.667, eps=0.003878321
Epoch
      12: f=
                455.630, eps=0.004072237
                454.261, eps=0.004275848
Epoch
      13: f=
Epoch
      14: f=
                453.340, eps=0.004489641
Epoch
      15: f=
                452.926, eps=0.004714123
Epoch
      16: f=
                452.779, eps=0.004949829
Epoch 17: f=
                454.323, eps=0.002474914
Epoch 18: f=
                451.622, eps=0.002598660
Epoch
      19: f=
                451.259, eps=0.002728593
Epoch
      20: f=
                451.131, eps=0.002865023
Epoch 21: f=
                451.024, eps=0.003008274
Epoch
      22: f=
                450.933, eps=0.003158688
Epoch
      23: f=
                450.855, eps=0.003316622
Epoch 24: f=
                450.787, eps=0.003482453
Epoch 25: f=
                450.730, eps=0.003656576
Epoch 26: f=
                450.682, eps=0.003839405
                450.643, eps=0.004031375
Epoch
      27: f=
Epoch 28: f=
                450.613, eps=0.004232944
Epoch
      29: f=
                450.594, eps=0.004444591
Epoch
      30: f=
                450.601, eps=0.002222295
Epoch
      31: f=
                450.549, eps=0.002333410
Epoch 32: f=
                450.538, eps=0.002450081
Epoch 33: f=
                450.530, eps=0.002572585
Epoch
      34: f=
                450.524, eps=0.002701214
Epoch 35: f=
                450.517, eps=0.002836275
                450.512, eps=0.002978088
Epoch
      36: f=
Epoch
      37: f=
                450.507, eps=0.003126993
Epoch
      38: f=
                450.503, eps=0.003283342
Epoch
      39: f=
                450.499, eps=0.003447510
Epoch 40: f=
                450.495, eps=0.003619885
Epoch 41: f=
                450.493, eps=0.003800879
Epoch 42: f=
                450.490, eps=0.003990923
Epoch 43: f=
                450.488, eps=0.004190469
Epoch
      44: f=
                450.486, eps=0.004399993
                450.485, eps=0.004619993
Epoch
      45: f=
Epoch
      46: f=
                450.484, eps=0.004850992
Epoch
      47: f=
                450.483, eps=0.005093542
Epoch
      48: f=
                450.483, eps=0.002546771
Epoch
      49: f=
                450.482, eps=0.002674109
                450.481, eps=0.002807815
Epoch 50: f=
```

```
Epoch 51: f=
                450.481, eps=0.002948206
Epoch 52: f=
                450.481, eps=0.003095616
Epoch 53: f=
                450.481, eps=0.003250397
Epoch
      54: f=
                450.480, eps=0.003412917
Epoch
      55: f=
                450.480, eps=0.003583562
Epoch
      56: f=
                450.480, eps=0.003762741
Epoch
      57: f=
                450.480, eps=0.003950878
Epoch 58: f=
                450.480, eps=0.004148421
Epoch 59: f=
                450.480, eps=0.004355843
Epoch
      60: f=
                450.480, eps=0.002177921
                450.480, eps=0.002286817
Epoch
      61: f=
Epoch
      62: f=
                450.480, eps=0.002401158
                450.479, eps=0.002521216
Epoch
      63: f=
Epoch
      64: f=
                450.479, eps=0.002647277
                450.479, eps=0.002779641
Epoch
      65: f=
Epoch 66: f=
                450.479, eps=0.002918623
Epoch 67: f=
                450.479, eps=0.003064554
Epoch
      68: f=
                450.479, eps=0.003217782
Epoch 69: f=
                450.479, eps=0.003378671
Epoch
                450.479, eps=0.003547604
      70: f=
Epoch
      71: f=
                450.479, eps=0.003724984
Epoch
      72: f=
                450.479, eps=0.003911234
Epoch 73: f=
                450.479, eps=0.004106795
Epoch 74: f=
                450.479, eps=0.004312135
                450.479, eps=0.004527742
Epoch 75: f=
Epoch 76: f=
                450.479, eps=0.004754129
Epoch
      77: f=
                450.479, eps=0.004991835
Epoch
      78: f=
                450.479, eps=0.005241427
Epoch
      79: f=
                450.479, eps=0.002620714
Epoch 80: f=
                450.479, eps=0.002751749
Epoch 81: f=
                450.479, eps=0.002889337
Epoch
      82: f=
                450.479, eps=0.003033804
Epoch 83: f=
                450.479, eps=0.003185494
Epoch
      84: f=
                450.479, eps=0.003344768
      85: f=
Epoch
                450.479, eps=0.003512007
Epoch
      86: f=
                450.479, eps=0.003687607
Epoch
      87: f=
                450.479, eps=0.003871988
Epoch
                450.479, eps=0.004065587
      88: f=
Epoch
      89: f=
                450.479, eps=0.004268866
Epoch 90: f=
                450.479, eps=0.002134433
Epoch 91: f=
                450.479, eps=0.002241155
Epoch
      92: f=
                450.479, eps=0.002353213
Epoch
                450.479, eps=0.002470873
      93: f=
Epoch
      94: f=
                450.479, eps=0.002594417
Epoch
      95: f=
                450.479, eps=0.002724138
Epoch
      96: f=
                450.479, eps=0.002860345
Epoch 97: f=
                450.479, eps=0.003003362
                450.479, eps=0.003153530
Epoch 98: f=
```

```
Epoch 99: f=
                450.479, eps=0.003311206
Epoch 100: f=
                450.479, eps=0.003476767
Epoch 101: f=
                450.479, eps=0.003650605
Epoch 102: f=
                450.479, eps=0.003833135
Epoch 103: f=
                450.479, eps=0.004024792
Epoch 104: f=
                450.479, eps=0.004226032
Epoch 105: f=
                450.479, eps=0.004437333
Epoch 106: f=
                450.479, eps=0.004659200
Epoch 107: f=
                450.479, eps=0.004892160
Epoch 108: f=
                450.479, eps=0.005136768
Epoch 109: f=
                450.479, eps=0.005393606
Epoch 110: f=
                450.479, eps=0.002696803
Epoch 111: f=
                450.479, eps=0.002831643
Epoch 112: f=
                450.479, eps=0.002973225
Epoch 113: f=
                450.479, eps=0.003121887
Epoch 114: f=
                450.479, eps=0.003277981
Epoch 115: f=
                450.479, eps=0.003441880
Epoch 116: f=
                450.479, eps=0.003613974
Epoch 117: f=
                450.479, eps=0.003794673
Epoch 118: f=
                450.479, eps=0.003984406
Epoch 119: f=
                450.479, eps=0.004183627
Epoch 120: f=
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                450.479, eps=0.000000000
```

```
Epoch 483: f=
                450.479, eps=0.000000000
Epoch 484: f=
                450.479, eps=0.000000000
Epoch 485: f=
                450.479, eps=0.000000000
                450.479, eps=0.000000000
Epoch 486: f=
Epoch 487: f=
                450.479, eps=0.000000000
Epoch 488: f=
                450.479, eps=0.000000000
Epoch 489: f=
                450.479, eps=0.000000000
                450.479, eps=0.000000000
Epoch 490: f=
Epoch 491: f=
                450.479, eps=0.000000000
Epoch 492: f=
                450.479, eps=0.000000000
                450.479, eps=0.000000000
Epoch 493: f=
Epoch 494: f=
                450.479, eps=0.000000000
                450.479, eps=0.000000000
Epoch 495: f=
Epoch 496: f=
                450.479, eps=0.000000000
Epoch 497: f=
                450.479, eps=0.000000000
Epoch 498: f=
                450.479, eps=0.000000000
Epoch 499: f=
                450.479, eps=0.000000000
Result after 500 epochs: f=450.4792408532154
        0: f=
               6759.666, eps=0.010000000
Epoch
Epoch
               6725.770, eps=0.010500000
        1: f=
Epoch
               5125.642, eps=0.011025000
Epoch
        3: f= 28027.453, eps=0.005512500
Epoch
        4: f=
               5292.550, eps=0.005788125
Epoch
        5: f=
                965.989, eps=0.006077531
Epoch
        6: f=
                685.912, eps=0.006381408
        7: f=
                999.714, eps=0.003190704
Epoch
Epoch
        8: f=
                628.348, eps=0.003350239
Epoch
        9: f=
                579.496, eps=0.003517751
Epoch
      10: f=
                578.458, eps=0.003693639
      11: f=
                579.127, eps=0.001846819
Epoch
Epoch
      12: f=
                576.088, eps=0.001939160
Epoch
      13: f=
                575.942, eps=0.002036118
Epoch
      14: f=
                575.935, eps=0.002137924
Epoch
       15: f=
                575.934, eps=0.002244820
       16: f=
Epoch
                575.934, eps=0.002357061
Epoch
       17: f=
                575.934, eps=0.002474914
Epoch
       18: f=
                575.933, eps=0.002598660
Epoch
                575.933, eps=0.002728593
      19: f=
Epoch
      20: f=
                575.933, eps=0.002865023
Epoch 21: f=
                575.933, eps=0.003008274
Epoch 22: f=
                575.933, eps=0.003158688
Epoch 23: f=
                575.933, eps=0.003316622
      24: f=
Epoch
                575.933, eps=0.003482453
Epoch
      25: f=
                575.933, eps=0.003656576
Epoch
      26: f=
                575.933, eps=0.001828288
Epoch
       27: f=
                575.933, eps=0.001919702
Epoch
      28: f=
                575.933, eps=0.002015687
      29: f=
                575.933, eps=0.002116472
Epoch
```

```
Epoch 30: f=
                575.933, eps=0.002222295
Epoch
      31: f=
                575.933, eps=0.002333410
Epoch
      32: f=
                575.933, eps=0.002450081
Epoch
      33: f=
                575.933, eps=0.002572585
Epoch
      34: f=
                575.933, eps=0.002701214
Epoch
      35: f=
                575.933, eps=0.002836275
Epoch
      36: f=
                575.933, eps=0.002978088
Epoch 37: f=
                575.933, eps=0.003126993
Epoch 38: f=
                575.933, eps=0.003283342
Epoch 39: f=
                575.933, eps=0.003447510
                575.933, eps=0.003619885
Epoch
      40: f=
Epoch 41: f=
                575.933, eps=0.003800879
Epoch
      42: f=
                575.933, eps=0.003990923
Epoch
      43: f=
                575.933, eps=0.004190469
Epoch 44: f=
                575.933, eps=0.004399993
Epoch 45: f=
                575.933, eps=0.002199996
Epoch 46: f=
                575.933, eps=0.002309996
Epoch 47: f=
                575.933, eps=0.002425496
Epoch 48: f=
                575.933, eps=0.002546771
Epoch
                575.933, eps=0.001273385
      49: f=
Epoch
      50: f=
                575.933, eps=0.001337055
Epoch 51: f=
                575.933, eps=0.001403907
Epoch 52: f=
                575.933, eps=0.001474103
Epoch 53: f=
                575.933, eps=0.000737051
Epoch 54: f=
                575.933, eps=0.000773904
Epoch 55: f=
                575.933, eps=0.000812599
Epoch 56: f=
                575.933, eps=0.000853229
Epoch 57: f=
                575.933, eps=0.000895891
Epoch 58: f=
                575.933, eps=0.000940685
Epoch 59: f=
                575.933, eps=0.000987719
Epoch 60: f=
                575.933, eps=0.001037105
Epoch
      61: f=
                575.933, eps=0.000518553
Epoch 62: f=
                575.933, eps=0.000544480
Epoch 63: f=
                575.933, eps=0.000571704
      64: f=
Epoch
                575.933, eps=0.000600290
Epoch
      65: f=
                575.933, eps=0.000630304
Epoch
      66: f=
                575.933, eps=0.000661819
Epoch
                575.933, eps=0.000694910
      67: f=
Epoch
      68: f=
                575.933, eps=0.000729656
Epoch 69: f=
                575.933, eps=0.000766138
Epoch 70: f=
                575.933, eps=0.000804445
      71: f=
Epoch
                575.933, eps=0.000844668
      72: f=
                575.933, eps=0.000886901
Epoch
Epoch
      73: f=
                575.933, eps=0.000931246
Epoch 74: f=
                575.933, eps=0.000977808
Epoch
      75: f=
                575.933, eps=0.001026699
Epoch
      76: f=
                575.933, eps=0.001078034
      77: f=
                575.933, eps=0.001131935
Epoch
```

```
Epoch
      78: f=
                575.933, eps=0.001188532
Epoch
      79: f=
                575.933, eps=0.001247959
Epoch
      80: f=
                575.933, eps=0.001310357
Epoch
      81: f=
                575.933, eps=0.001375875
Epoch
      82: f=
                575.933, eps=0.000687937
Epoch
      83: f=
                575.933, eps=0.000722334
Epoch
      84: f=
                575.933, eps=0.000758451
Epoch 85: f=
                575.933, eps=0.000796373
Epoch 86: f=
                575.933, eps=0.000836192
Epoch 87: f=
                575.933, eps=0.000878002
                575.933, eps=0.000921902
Epoch
      88: f=
Epoch 89: f=
                575.933, eps=0.000967997
Epoch
      90: f=
                575.933, eps=0.001016397
Epoch
      91: f=
                575.933, eps=0.001067217
Epoch 92: f=
                575.933, eps=0.001120577
Epoch 93: f=
                575.933, eps=0.001176606
Epoch 94: f=
                575.933, eps=0.000588303
Epoch 95: f=
                575.933, eps=0.000617718
Epoch 96: f=
                575.933, eps=0.000648604
Epoch
                575.933, eps=0.000681034
      97: f=
Epoch
      98: f=
                575.933, eps=0.000715086
Epoch 99: f=
                575.933, eps=0.000750840
Epoch 100: f=
                575.933, eps=0.000788382
Epoch 101: f=
                575.933, eps=0.000827802
Epoch 102: f=
                575.933, eps=0.000869192
Epoch 103: f=
                575.933, eps=0.000912651
Epoch 104: f=
                575.933, eps=0.000958284
Epoch 105: f=
                575.933, eps=0.001006198
Epoch 106: f=
                575.933, eps=0.001056508
Epoch 107: f=
                575.933, eps=0.001109333
Epoch 108: f=
                575.933, eps=0.001164800
Epoch 109: f=
                575.933, eps=0.001223040
Epoch 110: f=
                575.933, eps=0.001284192
Epoch 111: f=
                575.933, eps=0.001348402
Epoch 112: f=
                575.933, eps=0.001415822
Epoch 113: f=
                575.933, eps=0.001486613
Epoch 114: f=
                575.933, eps=0.001560943
Epoch 115: f=
                575.933, eps=0.001638991
Epoch 116: f=
                575.933, eps=0.001720940
Epoch 117: f=
                575.933, eps=0.001806987
Epoch 118: f=
                575.933, eps=0.001897336
Epoch 119: f=
                575.933, eps=0.001992203
Epoch 120: f=
                575.933, eps=0.002091813
Epoch 121: f=
                575.933, eps=0.002196404
Epoch 122: f=
                575.933, eps=0.002306224
Epoch 123: f=
                575.933, eps=0.002421535
Epoch 124: f=
                575.933, eps=0.002542612
Epoch 125: f=
                575.933, eps=0.002669743
```

```
Epoch 126: f=
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Epoch 127: f=
                575.933, eps=0.002943392
Epoch 128: f=
                575.933, eps=0.003090561
Epoch 129: f=
                575.933, eps=0.001545281
Epoch 130: f=
                575.933, eps=0.001622545
Epoch 131: f=
                575.933, eps=0.001703672
Epoch 132: f=
                575.933, eps=0.001788855
Epoch 133: f=
                575.933, eps=0.001878298
Epoch 134: f=
                575.933, eps=0.001972213
Epoch 135: f=
                575.933, eps=0.002070824
Epoch 136: f=
                575.933, eps=0.002174365
Epoch 137: f=
                575.933, eps=0.002283083
Epoch 138: f=
                575.933, eps=0.002397237
Epoch 139: f=
                575.933, eps=0.002517099
Epoch 140: f=
                575.933, eps=0.002642954
Epoch 141: f=
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Epoch 142: f=
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Epoch 143: f=
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Epoch 144: f=
                575.933, eps=0.003212527
Epoch 145: f=
                575.933, eps=0.003373154
Epoch 146: f=
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Epoch 147: f=
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Epoch 148: f=
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Epoch 149: f=
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Epoch 150: f=
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Epoch 151: f=
                575.933, eps=0.004520348
Epoch 152: f=
                575.933, eps=0.002260174
Epoch 153: f=
                575.933, eps=0.002373183
Epoch 154: f=
                575.933, eps=0.002491842
Epoch 155: f=
                575.933, eps=0.002616434
Epoch 156: f=
                575.933, eps=0.002747256
Epoch 157: f=
                575.933, eps=0.002884619
Epoch 158: f=
                575.933, eps=0.003028850
Epoch 159: f=
                575.933, eps=0.003180292
Epoch 160: f=
                575.933, eps=0.003339307
Epoch 161: f=
                575.933, eps=0.003506272
Epoch 162: f=
                575.933, eps=0.003681586
Epoch 163: f=
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Epoch 164: f=
                575.933, eps=0.004058948
Epoch 165: f=
                575.933, eps=0.004261896
Epoch 166: f=
                575.933, eps=0.004474990
Epoch 167: f=
                575.933, eps=0.004698740
Epoch 168: f=
                575.933, eps=0.004933677
Epoch 169: f=
                575.933, eps=0.005180361
Epoch 170: f=
                575.933, eps=0.005439379
Epoch 171: f=
                575.933, eps=0.005711348
Epoch 172: f=
                575.933, eps=0.005996915
Epoch 173: f=
                575.933, eps=0.006296761
```

```
Epoch 174: f=
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Epoch 175: f=
                575.933, eps=0.006942179
Epoch 176: f=
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Epoch 177: f=
                575.933, eps=0.007653752
Epoch 178: f=
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Epoch 179: f=
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Epoch 180: f=
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Epoch 181: f=
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Epoch 182: f=
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Epoch 183: f=
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Epoch 184: f=
                575.933, eps=0.002442086
Epoch 185: f=
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Epoch 186: f=
                575.933, eps=0.002692399
Epoch 187: f=
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Epoch 188: f=
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Epoch 189: f=
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Epoch 190: f=
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Epoch 191: f=
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Epoch 192: f=
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Epoch 193: f=
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Epoch 194: f=
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Epoch 195: f=
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Epoch 196: f=
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Epoch 197: f=
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Epoch 198: f=
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Epoch 199: f=
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Epoch 200: f=
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Epoch 201: f=
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Epoch 202: f=
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Epoch 203: f=
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Epoch 204: f=
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Epoch 205: f=
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Epoch 206: f=
                575.933, eps=0.001619895
Epoch 207: f=
                575.933, eps=0.001700890
Epoch 208: f=
                575.933, eps=0.001785934
Epoch 209: f=
                575.933, eps=0.001875231
Epoch 210: f=
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Epoch 211: f=
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Epoch 212: f=
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Epoch 213: f=
                575.933, eps=0.002279355
Epoch 214: f=
                575.933, eps=0.002393323
Epoch 215: f=
                575.933, eps=0.002512989
Epoch 216: f=
                575.933, eps=0.002638638
Epoch 217: f=
                575.933, eps=0.002770570
Epoch 218: f=
                575.933, eps=0.002909099
Epoch 219: f=
                575.933, eps=0.003054554
Epoch 220: f=
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Epoch 221: f=
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```

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Epoch 222: f=
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Epoch 223: f=
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Epoch 224: f=
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Epoch 225: f=
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Epoch 226: f=
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Epoch 227: f=
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Epoch 228: f=
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Epoch 229: f=
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Epoch 230: f=
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Epoch 231: f=
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Epoch 232: f=
                575.933, eps=0.002742770
Epoch 233: f=
                575.933, eps=0.002879908
Epoch 234: f=
                575.933, eps=0.003023904
Epoch 235: f=
                575.933, eps=0.003175099
Epoch 236: f=
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Epoch 237: f=
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Epoch 238: f=
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Epoch 239: f=
                575.933, eps=0.003859353
Epoch 240: f=
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Epoch 241: f=
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Epoch 242: f=
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Epoch 243: f=
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Epoch 244: f=
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Epoch 246: f=
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Epoch 248: f=
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Epoch 249: f=
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Epoch 251: f=
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Epoch 252: f=
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Epoch 253: f=
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Epoch 254: f=
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Epoch 255: f=
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Epoch 256: f=
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Epoch 257: f=
                575.933, eps=0.004422854
Epoch 258: f=
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Epoch 260: f=
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                575.933, eps=0.005376006
Epoch 262: f=
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Epoch 265: f=
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Epoch 266: f=
                575.933, eps=0.003267285
Epoch 267: f=
                575.933, eps=0.003430649
Epoch 268: f=
                575.933, eps=0.001715324
Epoch 269: f=
                575.933, eps=0.001801091
```

```
Epoch 270: f=
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Epoch 271: f=
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Epoch 272: f=
                575.933, eps=0.002084987
Epoch 273: f=
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Epoch 274: f=
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Epoch 275: f=
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Epoch 276: f=
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Epoch 277: f=
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Epoch 278: f=
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Epoch 279: f=
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Epoch 280: f=
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Epoch 281: f=
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Epoch 282: f=
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Epoch 283: f=
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Epoch 284: f=
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Epoch 286: f=
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Epoch 287: f=
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Epoch 288: f=
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Epoch 289: f=
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Epoch 290: f=
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Epoch 291: f=
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Epoch 292: f=
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Epoch 293: f=
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Epoch 294: f=
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Epoch 296: f=
                575.933, eps=0.001524783
Epoch 297: f=
                575.933, eps=0.001601022
Epoch 298: f=
                575.933, eps=0.001681073
Epoch 299: f=
                575.933, eps=0.001765127
Epoch 300: f=
                575.933, eps=0.001853383
Epoch 301: f=
                575.933, eps=0.001946052
Epoch 302: f=
                575.933, eps=0.002043355
Epoch 303: f=
                575.933, eps=0.002145523
Epoch 304: f=
                575.933, eps=0.002252799
Epoch 305: f=
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Epoch 306: f=
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Epoch 307: f=
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Epoch 308: f=
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Epoch 310: f=
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Epoch 311: f=
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Epoch 312: f=
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Epoch 313: f=
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Epoch 314: f=
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Epoch 315: f=
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Epoch 316: f=
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Epoch 317: f=
                575.933, eps=0.004247988
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Epoch 319: f=
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Epoch 320: f=
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Epoch 321: f=
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Epoch 322: f=
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Epoch 323: f=
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Epoch 324: f=
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Epoch 325: f=
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Epoch 326: f=
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Epoch 327: f=
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Epoch 328: f=
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Epoch 329: f=
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Epoch 330: f=
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Epoch 331: f=
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Epoch 332: f=
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Epoch 333: f=
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Epoch 334: f=
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Epoch 335: f=
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Epoch 336: f=
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Epoch 337: f=
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Epoch 338: f=
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Epoch 339: f=
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Epoch 348: f=
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Epoch 349: f=
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Epoch 350: f=
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Epoch 351: f=
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Epoch 352: f=
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Epoch 353: f=
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Epoch 354: f=
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Epoch 355: f=
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Epoch 356: f=
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Epoch 358: f=
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Epoch 359: f=
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Epoch 360: f=
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Epoch 361: f=
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Epoch 362: f=
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Epoch 363: f=
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Epoch 364: f=
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Epoch 365: f=
                575.933, eps=0.002271917
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Epoch 367: f=
                575.933, eps=0.002504789
Epoch 368: f=
                575.933, eps=0.002630028
Epoch 369: f=
                575.933, eps=0.002761530
Epoch 370: f=
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Epoch 371: f=
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Epoch 372: f=
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Epoch 373: f=
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Epoch 374: f=
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Epoch 375: f=
                575.933, eps=0.003700714
Epoch 376: f=
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Epoch 377: f=
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Epoch 378: f=
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Epoch 379: f=
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Epoch 380: f=
                575.933, eps=0.002249120
Epoch 381: f=
                575.933, eps=0.002361576
Epoch 382: f=
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Epoch 383: f=
                575.933, eps=0.002603638
Epoch 384: f=
                575.933, eps=0.002733820
Epoch 385: f=
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Epoch 386: f=
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Epoch 387: f=
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Epoch 388: f=
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Epoch 389: f=
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Epoch 390: f=
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Epoch 391: f=
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Epoch 392: f=
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Epoch 393: f=
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Epoch 394: f=
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Epoch 395: f=
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Epoch 396: f=
                575.933, eps=0.002337880
Epoch 397: f=
                575.933, eps=0.002454774
Epoch 398: f=
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Epoch 399: f=
                575.933, eps=0.002706388
Epoch 400: f=
                575.933, eps=0.002841708
Epoch 401: f=
                575.933, eps=0.002983793
Epoch 402: f=
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Epoch 403: f=
                575.933, eps=0.003289632
Epoch 404: f=
                575.933, eps=0.003454113
Epoch 405: f=
                575.933, eps=0.003626819
Epoch 406: f=
                575.933, eps=0.003808160
Epoch 407: f=
                575.933, eps=0.003998568
Epoch 408: f=
                575.933, eps=0.004198496
Epoch 409: f=
                575.933, eps=0.002099248
Epoch 410: f=
                575.933, eps=0.002204211
Epoch 411: f=
                575.933, eps=0.002314421
Epoch 412: f=
                575.933, eps=0.002430142
                575.933, eps=0.002551649
Epoch 413: f=
```

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Epoch 414: f=
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Epoch 415: f=
                575.933, eps=0.002813193
Epoch 416: f=
                575.933, eps=0.002953853
Epoch 417: f=
                575.933, eps=0.003101546
Epoch 418: f=
                575.933, eps=0.003256623
Epoch 419: f=
                575.933, eps=0.001628311
Epoch 420: f=
                575.933, eps=0.001709727
Epoch 421: f=
                575.933, eps=0.000854863
Epoch 422: f=
                575.933, eps=0.000897607
Epoch 423: f=
                575.933, eps=0.000942487
Epoch 424: f=
                575.933, eps=0.000989611
Epoch 425: f=
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Epoch 426: f=
                575.933, eps=0.001091047
Epoch 427: f=
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Epoch 428: f=
                575.933, eps=0.001202879
Epoch 429: f=
                575.933, eps=0.001263023
Epoch 430: f=
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Epoch 431: f=
                575.933, eps=0.001392483
Epoch 432: f=
                575.933, eps=0.001462107
Epoch 433: f=
                575.933, eps=0.001535212
Epoch 434: f=
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Epoch 435: f=
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Epoch 436: f=
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Epoch 437: f=
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Epoch 438: f=
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Epoch 439: f=
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Epoch 440: f=
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Epoch 441: f=
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Epoch 442: f=
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Epoch 443: f=
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Epoch 444: f=
                575.933, eps=0.000595404
Epoch 445: f=
                575.933, eps=0.000625175
Epoch 446: f=
                575.933, eps=0.000656433
Epoch 447: f=
                575.933, eps=0.000689255
Epoch 448: f=
                575.933, eps=0.000723718
Epoch 449: f=
                575.933, eps=0.000759904
Epoch 450: f=
                575.933, eps=0.000797899
Epoch 451: f=
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Epoch 452: f=
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Epoch 453: f=
                575.933, eps=0.000923668
Epoch 454: f=
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Epoch 455: f=
                575.933, eps=0.001018344
Epoch 456: f=
                575.933, eps=0.000509172
Epoch 457: f=
                575.933, eps=0.000534630
                575.933, eps=0.000561362
Epoch 458: f=
Epoch 459: f=
                575.933, eps=0.000589430
Epoch 460: f=
                575.933, eps=0.000618902
Epoch 461: f=
                575.933, eps=0.000649847
```

```
Epoch 462: f=
                575.933, eps=0.000682339
Epoch 463: f=
                575.933, eps=0.000716456
Epoch 464: f=
                575.933, eps=0.000752279
Epoch 465: f=
                575.933, eps=0.000789893
Epoch 466: f=
                575.933, eps=0.000829387
Epoch 467: f=
                575.933, eps=0.000870857
Epoch 468: f=
                575.933, eps=0.000914399
Epoch 469: f=
                575.933, eps=0.000960119
Epoch 470: f=
                575.933, eps=0.001008125
Epoch 471: f=
                575.933, eps=0.000504063
Epoch 472: f=
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Epoch 473: f=
                575.933, eps=0.000555729
Epoch 474: f=
                575.933, eps=0.000583516
Epoch 475: f=
                575.933, eps=0.000612691
                575.933, eps=0.000643326
Epoch 476: f=
Epoch 477: f=
                575.933, eps=0.000675492
Epoch 478: f=
                575.933, eps=0.000709267
Epoch 479: f=
                575.933, eps=0.000744730
Epoch 480: f=
                575.933, eps=0.000781967
Epoch 481: f=
                575.933, eps=0.000821065
Epoch 482: f=
                575.933, eps=0.000862118
Epoch 483: f=
                575.933, eps=0.000905224
Epoch 484: f=
                575.933, eps=0.000950485
Epoch 485: f=
                575.933, eps=0.000998010
Epoch 486: f=
                575.933, eps=0.000499005
Epoch 487: f=
                575.933, eps=0.000523955
Epoch 488: f=
                575.933, eps=0.000550153
Epoch 489: f=
                575.933, eps=0.000577660
Epoch 490: f=
                575.933, eps=0.000606543
Epoch 491: f=
                575.933, eps=0.000636871
Epoch 492: f=
                575.933, eps=0.000668714
Epoch 493: f=
                575.933, eps=0.000702150
Epoch 494: f=
                575.933, eps=0.000737257
Epoch 495: f=
                575.933, eps=0.000774120
Epoch 496: f=
                575.933, eps=0.000812826
Epoch 497: f=
                575.933, eps=0.000853468
Epoch 498: f=
                575.933, eps=0.000896141
Epoch 499: f=
                575.933, eps=0.000940948
Result after 500 epochs: f=575.9333931856461
        0: f= 10115.815, eps=0.010000000
Epoch
Epoch
        1: f= 26233.982, eps=0.005000000
Epoch
        2: f=
               1807.440, eps=0.005250000
               4190.824, eps=0.002625000
Epoch
        3: f=
Epoch
        4: f=
               1056.775, eps=0.002756250
        5: f=
                666.044, eps=0.002894063
Epoch
Epoch
        6: f=
                657.393, eps=0.003038766
Epoch
        7: f=
                660.438, eps=0.001519383
                648.568, eps=0.001595352
Epoch
        8: f=
```

```
Epoch
        9: f=
                647.174, eps=0.001675120
      10: f=
Epoch
                647.116, eps=0.001758876
                647.109, eps=0.001846819
Epoch
      11: f=
      12: f=
                647.108, eps=0.001939160
Epoch
Epoch
      13: f=
                647.107, eps=0.002036118
                647.107, eps=0.002137924
Epoch
      14: f=
Epoch 15: f=
                647.107, eps=0.002244820
Epoch 16: f=
                647.107, eps=0.002357061
Epoch 17: f=
                647.107, eps=0.002474914
Epoch 18: f=
                647.107, eps=0.002598660
                647.107, eps=0.001299330
Epoch 19: f=
Epoch 20: f=
                647.107, eps=0.001364297
                647.107, eps=0.001432511
Epoch 21: f=
Epoch 22: f=
                647.107, eps=0.001504137
Epoch 23: f=
                647.107, eps=0.001579344
Epoch 24: f=
                647.107, eps=0.001658311
Epoch 25: f=
                647.107, eps=0.001741227
                647.107, eps=0.001828288
Epoch 26: f=
Epoch 27: f=
                647.107, eps=0.001919702
Epoch 28: f=
                647.107, eps=0.002015687
Epoch
      29: f=
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                647.107, eps=0.002222295
Epoch 30: f=
Epoch 31: f=
                647.107, eps=0.002333410
Epoch 32: f=
                647.107, eps=0.002450081
Epoch 33: f=
                647.107, eps=0.001225040
Epoch 34: f=
                647.107, eps=0.001286292
                647.107, eps=0.001350607
Epoch 35: f=
Epoch 36: f=
                647.107, eps=0.001418137
                647.107, eps=0.001489044
Epoch 37: f=
Epoch 38: f=
                647.107, eps=0.001563496
                647.107, eps=0.001641671
Epoch 39: f=
Epoch 40: f=
                647.107, eps=0.000820836
Epoch 41: f=
                647.107, eps=0.000861877
                647.107, eps=0.000904971
Epoch 42: f=
Epoch 43: f=
                647.107, eps=0.000950220
                647.107, eps=0.000997731
Epoch 44: f=
Epoch 45: f=
                647.107, eps=0.001047617
Epoch 46: f=
                647.107, eps=0.001099998
Epoch 47: f=
                647.107, eps=0.001154998
Epoch 48: f=
                647.107, eps=0.001212748
                647.107, eps=0.001273385
Epoch 49: f=
Epoch 50: f=
                647.107, eps=0.001337055
Epoch 51: f=
                647.107, eps=0.001403907
Epoch 52: f=
                647.107, eps=0.001474103
Epoch 53: f=
                647.107, eps=0.001547808
Epoch 54: f=
                647.107, eps=0.001625198
Epoch 55: f=
                647.107, eps=0.000812599
Epoch 56: f=
                647.107, eps=0.000853229
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Epoch 57: f=
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Epoch 58: f=
                647.107, eps=0.000940685
                647.107, eps=0.000987719
Epoch 59: f=
                647.107, eps=0.001037105
Epoch
      60: f=
Epoch 61: f=
                647.107, eps=0.001088961
                647.107, eps=0.001143409
Epoch
      62: f=
Epoch
      63: f=
                647.107, eps=0.001200579
Epoch 64: f=
                647.107, eps=0.001260608
Epoch 65: f=
                647.107, eps=0.000630304
Epoch 66: f=
                647.107, eps=0.000661819
                647.107, eps=0.000694910
Epoch 67: f=
Epoch 68: f=
                647.107, eps=0.000347455
                647.107, eps=0.000364828
Epoch 69: f=
Epoch 70: f=
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Epoch 71: f=
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Epoch 72: f=
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Epoch 73: f=
                647.107, eps=0.000211167
                647.107, eps=0.000221725
Epoch 74: f=
Epoch 75: f=
                647.107, eps=0.000232812
Epoch 76: f=
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Epoch
      77: f=
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Epoch 78: f=
Epoch 79: f=
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Epoch 80: f=
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Epoch 81: f=
                647.107, eps=0.000311990
Epoch 82: f=
                647.107, eps=0.000327589
                647.107, eps=0.000343969
Epoch 83: f=
Epoch 84: f=
                647.107, eps=0.000361167
                647.107, eps=0.000379225
Epoch 85: f=
Epoch 86: f=
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                647.107, eps=0.000418096
Epoch 87: f=
Epoch 88: f=
                647.107, eps=0.000439001
Epoch 89: f=
                647.107, eps=0.000219500
                647.107, eps=0.000109750
Epoch 90: f=
Epoch 91: f=
                647.107, eps=0.000115238
Epoch 92: f=
                647.107, eps=0.000121000
Epoch 93: f=
                647.107, eps=0.000127050
Epoch 94: f=
                647.107, eps=0.000133402
Epoch 95: f=
                647.107, eps=0.000140072
Epoch 96: f=
                647.107, eps=0.000070036
                647.107, eps=0.000073538
Epoch 97: f=
Epoch 98: f=
                647.107, eps=0.000077215
Epoch 99: f=
                647.107, eps=0.000081076
Epoch 100: f=
                647.107, eps=0.000085129
Epoch 101: f=
                647.107, eps=0.000042565
Epoch 102: f=
                647.107, eps=0.000044693
Epoch 103: f=
                647.107, eps=0.000046928
Epoch 104: f=
                647.107, eps=0.000049274
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Epoch 105: f=
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Epoch 106: f=
                647.107, eps=0.000025869
Epoch 107: f=
                647.107, eps=0.000027162
Epoch 108: f=
                647.107, eps=0.000028520
Epoch 109: f=
                647.107, eps=0.000029946
Epoch 110: f=
                647.107, eps=0.000031444
Epoch 111: f=
                647.107, eps=0.000033016
Epoch 112: f=
                647.107, eps=0.000034667
Epoch 113: f=
                647.107, eps=0.000036400
Epoch 114: f=
                647.107, eps=0.000038220
                647.107, eps=0.000040131
Epoch 115: f=
Epoch 116: f=
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                647.107, eps=0.000044244
Epoch 117: f=
Epoch 118: f=
                647.107, eps=0.000046457
Epoch 119: f=
                647.107, eps=0.000048779
Epoch 120: f=
                647.107, eps=0.000051218
Epoch 121: f=
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Epoch 122: f=
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Epoch 123: f=
                647.107, eps=0.000059292
Epoch 124: f=
                647.107, eps=0.000062256
Epoch 125: f=
                647.107, eps=0.000065369
                647.107, eps=0.000068638
Epoch 126: f=
Epoch 127: f=
                647.107, eps=0.000072070
Epoch 128: f=
                647.107, eps=0.000075673
Epoch 129: f=
                647.107, eps=0.000079457
Epoch 130: f=
                647.107, eps=0.000083429
                647.107, eps=0.000087601
Epoch 131: f=
Epoch 132: f=
                647.107, eps=0.000091981
                647.107, eps=0.000096580
Epoch 133: f=
Epoch 134: f=
                647.107, eps=0.000101409
Epoch 135: f=
                647.107, eps=0.000106479
Epoch 136: f=
                647.107, eps=0.000111803
Epoch 137: f=
                647.107, eps=0.000055902
Epoch 138: f=
                647.107, eps=0.000058697
Epoch 139: f=
                647.107, eps=0.000061632
                647.107, eps=0.000030816
Epoch 140: f=
Epoch 141: f=
                647.107, eps=0.000032357
Epoch 142: f=
                647.107, eps=0.000033974
Epoch 143: f=
                647.107, eps=0.000035673
Epoch 144: f=
                647.107, eps=0.000037457
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                647.107, eps=0.001548241
Epoch 494: f=
Epoch 495: f=
                647.107, eps=0.001625653
Epoch 496: f=
                647.107, eps=0.001706935
Epoch 497: f=
                647.107, eps=0.001792282
Epoch 498: f=
                647.107, eps=0.001881896
                647.107, eps=0.001975991
Epoch 499: f=
Result after 500 epochs: f=647.1071050724063
        0: f= 20184.264, eps=0.010000000
Epoch
Epoch
        1: f=368036.938, eps=0.005000000
Epoch
        2: f=889328.801, eps=0.002500000
Epoch
        3: f= 73241.784, eps=0.002625000
       4: f= 13981.321, eps=0.002756250
Epoch
Epoch
        5: f=
               8490.553, eps=0.002894063
               6650.629, eps=0.003038766
Epoch
        6: f=
       7: f= 11704.009, eps=0.001519383
Epoch
Epoch
       8: f=
               1047.754, eps=0.001595352
Epoch
        9: f=
                788.589, eps=0.001675120
Epoch 10: f=
                837.627, eps=0.000837560
Epoch 11: f=
                756.173, eps=0.000879438
                751.407, eps=0.000923410
Epoch 12: f=
                751.226, eps=0.000969580
Epoch 13: f=
Epoch 14: f=
                751.212, eps=0.001018059
Epoch
      15: f=
                751.210, eps=0.001068962
Epoch 16: f=
                751.210, eps=0.001122410
Epoch 17: f=
                751.210, eps=0.001178531
Epoch 18: f=
                751.210, eps=0.001237457
Epoch
      19: f=
                751.210, eps=0.001299330
Epoch 20: f=
                751.210, eps=0.001364297
Epoch
      21: f=
                751.210, eps=0.001432511
      22: f=
Epoch
                751.210, eps=0.001504137
Epoch
      23: f=
                751.210, eps=0.001579344
Epoch 24: f=
                751.210, eps=0.000789672
Epoch 25: f=
                751.210, eps=0.000829156
Epoch 26: f=
                751.210, eps=0.000870613
Epoch 27: f=
                751.210, eps=0.000914144
Epoch 28: f=
                751.210, eps=0.000959851
Epoch 29: f=
                751.210, eps=0.000479926
      30: f=
                751.210, eps=0.000503922
Epoch
Epoch 31: f=
                751.210, eps=0.000529118
Epoch
      32: f=
                751.210, eps=0.000555574
Epoch
      33: f=
                751.210, eps=0.000583353
Epoch
      34: f=
                751.210, eps=0.000612520
                751.210, eps=0.000643146
Epoch
      35: f=
```

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Epoch 36: f=
                751.210, eps=0.000675303
Epoch 37: f=
                751.210, eps=0.000709069
Epoch 38: f=
                751.210, eps=0.000354534
                751.210, eps=0.000372261
Epoch
      39: f=
Epoch 40: f=
                751.210, eps=0.000390874
Epoch 41: f=
                751.210, eps=0.000410418
Epoch 42: f=
                751.210, eps=0.000205209
Epoch 43: f=
                751.210, eps=0.000215469
Epoch 44: f=
                751.210, eps=0.000226243
Epoch 45: f=
                751.210, eps=0.000237555
Epoch 46: f=
                751.210, eps=0.000118777
Epoch 47: f=
                751.210, eps=0.000124716
Epoch 48: f=
                751.210, eps=0.000062358
Epoch
      49: f=
                751.210, eps=0.000065476
Epoch 50: f=
                751.210, eps=0.000068750
Epoch 51: f=
                751.210, eps=0.000072187
Epoch 52: f=
                751.210, eps=0.000075797
Epoch 53: f=
                751.210, eps=0.000037898
Epoch 54: f=
                751.210, eps=0.000039793
Epoch 55: f=
                751.210, eps=0.000041783
Epoch
      56: f=
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Epoch 57: f=
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Epoch 58: f=
                751.210, eps=0.000023033
Epoch 59: f=
                751.210, eps=0.000011516
Epoch 60: f=
                751.210, eps=0.000012092
Epoch 61: f=
                751.210, eps=0.000012697
Epoch 62: f=
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Epoch 63: f=
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Epoch 64: f=
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Epoch 65: f=
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                751.210, eps=0.000007717
Epoch 66: f=
Epoch 67: f=
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Epoch 68: f=
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                751.210, eps=0.000004254
Epoch 69: f=
     70: f=
Epoch
                751.210, eps=0.000004466
Epoch 71: f=
                751.210, eps=0.000002233
Epoch 72: f=
                751.210, eps=0.000002345
Epoch 73: f=
                751.210, eps=0.000002462
Epoch 74: f=
                751.210, eps=0.000002585
Epoch 75: f=
                751.210, eps=0.000001293
Epoch 76: f=
                751.210, eps=0.000001357
Epoch 77: f=
                751.210, eps=0.000001425
Epoch 78: f=
                751.210, eps=0.000000713
Epoch 79: f=
                751.210, eps=0.000000748
Epoch 80: f=
                751.210, eps=0.000000374
      81: f=
Epoch
                751.210, eps=0.000000393
Epoch 82: f=
                751.210, eps=0.000000412
Epoch 83: f=
                751.210, eps=0.000000433
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Epoch 84: f=
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Epoch 85: f=
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Epoch 86: f=
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                751.210, eps=0.000000251
Epoch 87: f=
Epoch 88: f=
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Epoch 89: f=
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Epoch 90: f=
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Epoch 91: f=
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Epoch 92: f=
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Epoch 93: f=
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Epoch 94: f=
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Epoch 95: f=
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Epoch 96: f=
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Epoch 97: f=
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Epoch 98: f=
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Epoch 99: f=
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Epoch 100: f=
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Epoch 101: f=
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Epoch 102: f=
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Epoch 103: f=
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Epoch 104: f=
                751.210, eps=0.000000130
Epoch 105: f=
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Epoch 106: f=
                751.210, eps=0.000000144
Epoch 107: f=
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Epoch 108: f=
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Epoch 109: f=
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                751.210, eps=0.000000175
Epoch 110: f=
Epoch 111: f=
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Epoch 112: f=
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Epoch 113: f=
                751.210, eps=0.000000202
Epoch 114: f=
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Epoch 115: f=
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Epoch 116: f=
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Epoch 117: f=
                751.210, eps=0.000000117
Epoch 118: f=
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Epoch 119: f=
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Epoch 120: f=
                751.210, eps=0.000000135
Epoch 121: f=
                751.210, eps=0.000000142
Epoch 122: f=
                751.210, eps=0.000000149
Epoch 123: f=
                751.210, eps=0.000000157
Epoch 124: f=
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Epoch 125: f=
                751.210, eps=0.000000173
Epoch 126: f=
                751.210, eps=0.000000181
Epoch 127: f=
                751.210, eps=0.000000191
Epoch 128: f=
                751.210, eps=0.000000200
Epoch 129: f=
                751.210, eps=0.000000210
Epoch 130: f=
                751.210, eps=0.000000221
Epoch 131: f=
                751.210, eps=0.000000232
```

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Epoch 132: f=
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Epoch 133: f=
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Epoch 134: f=
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                751.210, eps=0.000000282
Epoch 135: f=
Epoch 136: f=
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Epoch 137: f=
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Epoch 138: f=
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Epoch 139: f=
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Epoch 140: f=
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Epoch 141: f=
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Epoch 142: f=
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Epoch 143: f=
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Epoch 144: f=
                751.210, eps=0.000000437
Epoch 145: f=
                751.210, eps=0.000000218
Epoch 146: f=
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Epoch 147: f=
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Epoch 148: f=
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Epoch 149: f=
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Epoch 150: f=
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Epoch 151: f=
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Epoch 152: f=
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Epoch 153: f=
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Epoch 154: f=
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Epoch 155: f=
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Epoch 156: f=
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Epoch 157: f=
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Epoch 158: f=
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Epoch 159: f=
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Epoch 160: f=
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Epoch 161: f=
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Epoch 162: f=
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Epoch 163: f=
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Epoch 164: f=
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Epoch 165: f=
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Epoch 166: f=
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Epoch 167: f=
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Epoch 168: f=
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Epoch 169: f=
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Epoch 170: f=
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Epoch 171: f=
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Epoch 172: f=
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Epoch 173: f=
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                751.210, eps=0.000000097
Epoch 174: f=
Epoch 175: f=
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Epoch 176: f=
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Epoch 177: f=
                751.210, eps=0.000000112
Epoch 178: f=
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Epoch 179: f=
                751.210, eps=0.000000124
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Epoch 180: f=
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Epoch 181: f=
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Epoch 182: f=
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                751.210, eps=0.000000151
Epoch 183: f=
Epoch 184: f=
                751.210, eps=0.000000158
Epoch 185: f=
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Epoch 186: f=
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Epoch 187: f=
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Epoch 188: f=
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Epoch 189: f=
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Epoch 190: f=
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Epoch 191: f=
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                751.210, eps=0.000000234
Epoch 192: f=
Epoch 193: f=
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Epoch 194: f=
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Epoch 195: f=
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Epoch 196: f=
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Epoch 197: f=
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Epoch 199: f=
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Epoch 200: f=
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Epoch 201: f=
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Epoch 202: f=
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Epoch 203: f=
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Epoch 204: f=
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Epoch 205: f=
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Epoch 206: f=
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Epoch 208: f=
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Epoch 209: f=
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Epoch 210: f=
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Epoch 211: f=
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Epoch 212: f=
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Epoch 213: f=
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Epoch 214: f=
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Epoch 215: f=
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Epoch 216: f=
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Epoch 217: f=
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Epoch 218: f=
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Epoch 219: f=
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Epoch 220: f=
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Epoch 221: f=
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Epoch 222: f=
                751.210, eps=0.000000229
Epoch 223: f=
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Epoch 224: f=
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Epoch 225: f=
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Epoch 226: f=
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Epoch 227: f=
                751.210, eps=0.000000292
```

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Epoch 229: f=
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Epoch 230: f=
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Epoch 231: f=
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Epoch 232: f=
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Epoch 233: f=
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Epoch 235: f=
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Epoch 236: f=
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Epoch 239: f=
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Epoch 241: f=
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Epoch 242: f=
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Epoch 243: f=
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Epoch 244: f=
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Epoch 245: f=
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Epoch 246: f=
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Epoch 247: f=
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Epoch 248: f=
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Epoch 249: f=
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Epoch 263: f=
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Epoch 272: f=
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Epoch 273: f=
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Epoch 274: f=
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```

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Epoch 278: f=
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Epoch 283: f=
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Epoch 284: f=
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Epoch 285: f=
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Epoch 286: f=
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Epoch 288: f=
Epoch 289: f=
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Epoch 299: f=
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Epoch 302: f=
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Epoch 317: f=
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Epoch 318: f=
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Epoch 319: f=
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Epoch 320: f=
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Epoch 321: f=
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Epoch 322: f=
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Epoch 323: f=
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Epoch 326: f=
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Epoch 327: f=
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Epoch 328: f=
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Epoch 329: f=
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Epoch 332: f=
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Epoch 333: f=
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Epoch 334: f=
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Epoch 335: f=
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Epoch 336: f=
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Epoch 337: f=
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Epoch 345: f=
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Epoch 349: f=
Epoch 350: f=
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Epoch 499: f=
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Result after 500 epochs: f=751.2097111809543
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lambda 0.01: 320.1482561851763
lambda 0.1: 325.0589707546104
lambda 0.5: 338.1256197756515
lambda 1: 347.85049245754726
lambda 2: 361.1419871051869
lambda 3: 371.1389275935148
lambda 4: 379.44334033241876
lambda 5: 386.6645111344998
lambda 10: 414.11111711137437
lambda 20: 450.4792408532154
lambda 100: 575.9333931856461
lambda 200: 647.1071050724063
lambda 500: 751.2097111809543
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                 1.65495805e-01,
                                 1.51384501e-01,
                 2.94516291e-02, 4.90162267e-03, 3.54578225e-01, 4.02161592e-01,
                 1.69453493e-01, 1.05773365e-01, -9.83190266e-02, 2.51317698e+00,
                 3.21482004e-01, -6.17074426e-02, 1.91659872e+00, 1.80120716e-01,
                -1.91367106e+00, -1.03194548e+00, -2.07505864e+00, 2.84369087e-01,
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7.51209711e+02, 7.51209711e+02, 7.51209711e+02, 7.51209711e+02,
```

```
7.51209711e+02, 7.51209711e+02, 7.51209711e+02, 7.51209711e+02,
```

```
7.51209711e+02, 7.51209711e+02, 7.51209711e+02, 7.51209711e+02,
                7.51209711e+02]),
         'final_objective': np.float64(1.3431465093272068e-07)}}
[325]: test_nll
[325]: {'0': np.float64(319.5707412596371),
        '0.01': np.float64(320.1482561851763),
        '0.1': np.float64(325.0589707546104),
        '0.5': np.float64(338.1256197756515),
        '1': np.float64(347.85049245754726),
        '2': np.float64(361.1419871051869),
        '3': np.float64(371.1389275935148),
        '4': np.float64(379.44334033241876),
        '5': np.float64(386.6645111344998),
        '10': np.float64(414.11111711137437),
        '20': np.float64(450.4792408532154),
        '100': np.float64(575.9333931856461),
        '200': np.float64(647.1071050724063),
        '500': np.float64(751.2097111809543)}
[326]: lambdas = list(test_nll_results.keys())
       # Extracting values for plotting
       test nll values = [test nll[lam] for lam in lambdas]
       # Setting up the scatter plot
       plt.figure(figsize=(10, 6))
       plt.plot(lambdas, test_nll_values)
       # Adding labels and title
       plt.xlabel('Lambda')
       plt.ylabel('Test NLL')
```

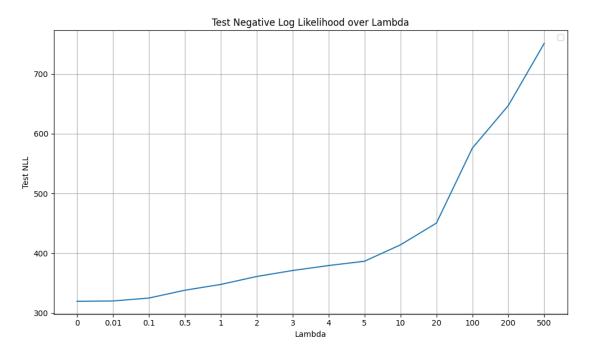
7.51209711e+02, 7.51209711e+02, 7.51209711e+02, 7.51209711e+02,

```
plt.title('Test Negative Log Likelihood over Lambda')
plt.legend()
plt.grid(True)

# Show the plot
plt.tight_layout()
plt.show()
```

/tmp/ipykernel\_32055/2165311344.py:14: UserWarning: No artists with labels found to put in legend. Note that artists whose label start with an underscore are ignored when legend() is called with no argument.

plt.legend()



```
[328]: acc = {}
for la in lam_values:
    yh = predict(Xtestz, results[str(la)]["final_weights"])
    yp = classify(Xtestz, results[str(la)]["final_weights"])
    metrics = sklearn.metrics.classification_report(ytest, yp, output_dict=True)
    acc[la] = metrics['accuracy']
```

[329]: acc

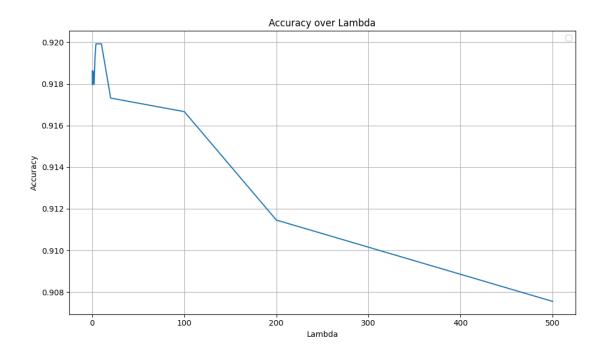
[329]: {0: 0.9186197916666666, 0.01: 0.9186197916666666, 0.1: 0.91796875,

```
1: 0.9186197916666666,
       2: 0.91796875,
       3: 0.9192708333333334,
       4: 0.919921875,
       5: 0.919921875,
       10: 0.919921875,
       20: 0.9173177083333334,
       200: 0.9114583333333334,
       500: 0.9075520833333334}
[330]: lambdas = list(acc.keys())
      # Extracting values for plotting
      accuracies = [acc[lam] for lam in lambdas]
      # Setting up the scatter plot
      plt.figure(figsize=(10, 6))
      plt.plot(lambdas, accuracies)
      # Adding labels and title
      plt.xlabel('Lambda')
      plt.ylabel('Accuracy')
      plt.title('Accuracy over Lambda')
      plt.legend()
      plt.grid(True)
      # Show the plot
      plt.tight_layout()
      plt.show()
```

/tmp/ipykernel\_32055/2620896624.py:14: UserWarning: No artists with labels found to put in legend. Note that artists whose label start with an underscore are ignored when legend() is called with no argument.

plt.legend()

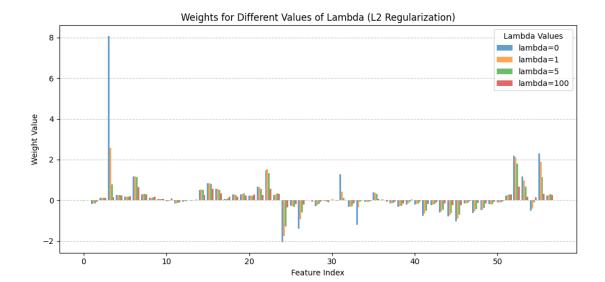
0.5: 0.91796875,



## 8.3 4c Composition of Weight Vector

```
[331]: # YOUR CODE HERE
       nextplot()
       plt.figure(figsize=(10, 5))
       # Plot bars with different offsets to avoid overlap
       bar width = 0.2 # Width of each bar
       plt.bar(np.arange(D), results['0']['final_weights'], width=bar_width,__
        →label='lambda=0', alpha=0.7)
       plt.bar(np.arange(D) + bar_width, results['1']['final_weights'],__
        ⇔width=bar_width, label='lambda=1', alpha=0.7)
       plt.bar(np.arange(D) + 2 * bar_width, results['5']['final_weights'],__
        ⇔width=bar_width, label='lambda=5', alpha=0.7)
       plt.bar(np.arange(D) + 3 * bar_width, results['100']['final_weights'],
        ⇔width=bar_width, label='lambda=100', alpha=0.7)
       # Add labels and title
       plt.xlabel("Feature Index")
       plt.ylabel("Weight Value")
       plt.title("Weights for Different Values of Lambda (L2 Regularization)")
       plt.legend(title="Lambda Values")
       plt.grid(axis="y", linestyle="--", alpha=0.7) # Add grid for easier comparison
       plt.tight_layout()
```

## plt.show()



## 8.4 5 Exploration (optional)

## 8.4.1 5 Exploration: PyTorch

[332]: !pip install torch

```
Requirement already satisfied: torch in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (2.4.1)
Requirement already satisfied: filelock in /home/tu2/.local/lib/python3.10/site-
packages (from torch) (3.12.2)
Requirement already satisfied: typing-extensions>=4.8.0 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (4.12.2)
Requirement already satisfied: sympy in /home/tu2/.local/lib/python3.10/site-
packages (from torch) (1.12)
Requirement already satisfied: networkx in /home/tu2/.local/lib/python3.10/site-
packages (from torch) (3.1)
Requirement already satisfied: jinja2 in /home/tu2/.local/lib/python3.10/site-
packages (from torch) (3.1.2)
Requirement already satisfied: fsspec in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (2024.9.0)
Requirement already satisfied: nvidia-cuda-nvrtc-cu12==12.1.105 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (12.1.105)
Requirement already satisfied: nvidia-cuda-runtime-cu12==12.1.105 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (12.1.105)
Requirement already satisfied: nvidia-cuda-cupti-cu12==12.1.105 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (12.1.105)
Requirement already satisfied: nvidia-cudnn-cu12==9.1.0.70 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (9.1.0.70)
Requirement already satisfied: nvidia-cublas-cu12==12.1.3.1 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (12.1.3.1)
Requirement already satisfied: nvidia-cufft-cu12==11.0.2.54 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch)
(11.0.2.54)
Requirement already satisfied: nvidia-curand-cu12==10.3.2.106 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch)
(10.3.2.106)
Requirement already satisfied: nvidia-cusolver-cu12==11.4.5.107 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch)
(11.4.5.107)
Requirement already satisfied: nvidia-cusparse-cu12==12.1.0.106 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch)
Requirement already satisfied: nvidia-nccl-cu12==2.20.5 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (2.20.5)
Requirement already satisfied: nvidia-nvtx-cu12==12.1.105 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (12.1.105)
Requirement already satisfied: triton==3.0.0 in
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from torch) (3.0.0)
```

```
/home/tu2/anaconda3/envs/ml/lib/python3.10/site-packages (from nvidia-cusolver-
      cu12==11.4.5.107->torch) (12.6.68)
      Requirement already satisfied: MarkupSafe>=2.0 in
      /home/tu2/.local/lib/python3.10/site-packages (from jinja2->torch) (2.1.3)
      Requirement already satisfied: mpmath>=0.19 in
      /home/tu2/.local/lib/python3.10/site-packages (from sympy->torch) (1.3.0)
[333]: # if you want to experiment, here is an implementation of logistic
       # regression in PyTorch
       import math
       import torch
       import torch.nn as nn
       import torch.utils.data
       import torch.nn.functional as F
       # prepare the data
       Xztorch = torch.FloatTensor(Xz)
       ytorch = torch.LongTensor(y)
       train = torch.utils.data.TensorDataset(Xztorch, ytorch)
       # manual implementation of logistic regression (without bias)
       class LogisticRegression(nn.Module):
           def __init__(self, D, C):
               super(LogisticRegression, self).__init__()
               self.weights = torch.nn.Parameter(
                   torch.randn(D, C) / math.sqrt(D)
               ) # xavier initialization
               self.register_parameter("W", self.weights)
           def forward(self, x):
               out = torch.matmul(x, self.weights)
               out = F.log_softmax(out)
               return out
       # define the objective and update function. here we ignore the learning rates
       # and parameters given to us by optimize (they are stored in the PyTorch model
       # and optimizer, resp., instead)
       def opt_pytorch():
           model = LogisticRegression(D, 2)
           criterion = nn.NLLLoss(reduction="sum")
           # change the next line to try different optimizers
           # optimizer = torch.optim.SGD(model.parameters(), lr=learning rate)
           optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate)
```

Requirement already satisfied: nvidia-nvjitlink-cu12 in

```
def objective(_):
    outputs = model(Xztorch)
    return criterion(outputs, ytorch)

def update(_1, _2):
    for i, (examples, labels) in enumerate(train_loader):
        outputs = model(examples)
        loss = criterion(outputs, labels)
        optimizer.zero_grad()
        loss.backward()
        optimizer.step()

W = model.state_dict()["W"]
    w = W[:, 1] - W[:, 0]
    return w

return (objective, update)
```

```
[334]: # run the optimizer
learning_rate = 0.01
batch_size = 100 # number of data points to sample for gradient estimate
shuffle = True # sample with replacement (false) or without replacement (true)

train_loader = torch.utils.data.DataLoader(train, batch_size, shuffle=True)
wz_t, vz_t, _ = optimize(opt_pytorch(), None, nepochs=100, eps0=None, ___
overbose=True)
```

/tmp/ipykernel\_32055/2194961090.py:26: UserWarning: Implicit dimension choice for log\_softmax has been deprecated. Change the call to include dim=X as an argument.

```
out = F.log_softmax(out)
```

```
Epoch 0: f= 2167.742, eps=
                                   nan
Epoch 1: f=
               858.704, eps=
                                   nan
Epoch 2: f=
               776.136, eps=
                                   nan
Epoch 3: f=
               741.471, eps=
                                   nan
Epoch 4: f=
               723.754, eps=
                                   nan
Epoch 5: f=
               711.613, eps=
                                   nan
Epoch 6: f=
               703.819, eps=
                                   nan
Epoch 7: f=
               697.749, eps=
                                   nan
Epoch 8: f=
               693.980, eps=
                                   nan
Epoch 9: f=
               689.839, eps=
                                   nan
Epoch 10: f=
               686.455, eps=
                                   nan
Epoch 11: f=
               685.140, eps=
                                   nan
Epoch 12: f=
               682.958, eps=
                                   nan
Epoch 13: f=
               681.823, eps=
                                   nan
               681.342, eps=
Epoch 14: f=
                                   nan
Epoch 15: f=
               678.672, eps=
                                   nan
```

Epoch	16: f	= 6	578.164,	eps=	nan
Epoch	17: f	= 6	577.424,	eps=	nan
Epoch	18: f	= 6	576.983,	eps=	nan
Epoch	19: f	= 6	575.968,	eps=	nan
Epoch	20: f	= 6	576.158,	eps=	nan
Epoch	21: f	= 6	575.512,	eps=	nan
Epoch	22: f	= 6	375.020,	eps=	nan
Epoch	23: f	= 6	574.520,	eps=	nan
Epoch	24: f	= 6	574.022,	eps=	nan
Epoch	25: f	= 6	573.802,	eps=	nan
Epoch	26: f	= 6	373.689,	eps=	nan
Epoch	27: f	= 6	373.208,	eps=	nan
Epoch	28: f	= 6	373.288,	eps=	nan
Epoch	29: f	= 6	572.501,	eps=	nan
Epoch	30: f	= 6	572.435,	eps=	nan
Epoch	31: f	= 6	572.252,	eps=	nan
Epoch	32: f	= 6	571.503,	eps=	nan
Epoch	33: f	= 6	571.300,	eps=	nan
Epoch	34: f		571.908,	eps=	nan
Epoch	35: f		671.844 <b>,</b>	eps=	nan
Epoch			371.182,	eps=	nan
Epoch	37: f	= 6	570.691,	eps=	nan
Epoch	38: f		570.405,	eps=	nan
Epoch	39: f		671.025,	eps=	nan
Epoch	40: f		370.754,	eps=	nan
Epoch	41: f		69.944,	eps=	nan
Epoch			669.227,	eps=	nan
Epoch	43: f	= 6	69.309,	eps=	nan
Epoch	44: f	= 6	69.374,	eps=	nan
Epoch	45: f	= 6	68.963,	eps=	nan
Epoch	46: f	= 6	69.855,	eps=	nan
Epoch	47: f	= 6	69.853,	eps=	nan
Epoch	48: f		68.648,	eps=	nan
Epoch	49: f		68.168,	eps=	nan
Epoch			68.196,	eps=	nan
Epoch			68.369,	eps=	nan
Epoch			67.841,	eps=	nan
Epoch			68.308,	eps=	nan
Epoch			67.862,	eps=	nan
Epoch			67.308,	eps=	nan
Epoch			67.335,	eps=	nan
Epoch			66.495,	eps=	nan
Epoch			68.021,	eps=	nan
Epoch			66.829,	eps=	nan
Epoch			66.158,	eps=	nan
Epoch			666.187,	eps=	nan
Epoch			66.081,	eps=	nan
Epoch			65.798,	eps=	nan
_r		•	,	- 1- ~	

```
Epoch
       64: f=
                665.544, eps=
                                      nan
Epoch
       65: f=
                665.496, eps=
                                      nan
Epoch
       66: f=
                666.050, eps=
                                      nan
Epoch
       67: f=
                665.503, eps=
                                      nan
Epoch
       68: f=
                664.774, eps=
                                      nan
Epoch
       69: f=
                665.563, eps=
                                      nan
Epoch
       70: f=
                664.641, eps=
                                      nan
Epoch
       71: f=
                665.250, eps=
                                      nan
Epoch
       72: f=
                664.187, eps=
                                      nan
Epoch
       73: f=
                664.695, eps=
                                      nan
                663.757, eps=
Epoch
       74: f=
                                      nan
Epoch
       75: f=
                664.139, eps=
                                      nan
                664.565, eps=
Epoch
       76: f=
                                      nan
       77: f=
Epoch
                663.946, eps=
                                      nan
Epoch
       78: f=
                663.746, eps=
                                      nan
Epoch
       79: f=
                664.476, eps=
                                      nan
Epoch
       80: f=
                662.315, eps=
                                      nan
Epoch
       81: f=
                663.081, eps=
                                      nan
Epoch
       82: f=
                662.142, eps=
                                      nan
Epoch
       83: f=
                662.654, eps=
                                      nan
Epoch
       84: f=
                663.786, eps=
                                      nan
Epoch
       85: f=
                662.094, eps=
                                      nan
Epoch
       86: f=
                661.566, eps=
                                      nan
Epoch
                661.118, eps=
       87: f=
                                      nan
Epoch
       88: f=
                661.899, eps=
                                      nan
Epoch
       89: f=
                662.141, eps=
                                      nan
Epoch
       90: f=
                661.724, eps=
                                      nan
Epoch
       91: f=
                661.799, eps=
                                      nan
Epoch
       92: f=
                660.493, eps=
                                      nan
Epoch
       93: f=
                660.781, eps=
                                      nan
                660.424, eps=
Epoch
       94: f=
                                      nan
Epoch
       95: f=
                660.235, eps=
                                      nan
Epoch
       96: f=
                659.848, eps=
                                      nan
Epoch
       97: f=
                659.318, eps=
                                      nan
Epoch
       98: f=
                659.318, eps=
                                      nan
Epoch
      99: f=
                658.994, eps=
                                      nan
Result after 100 epochs: f=659.8973388671875
```

[]: