## G. Pairwise Matching

Constraint: Time Limit: 1 seconds, Memory: 256MB



## **Problem description**

You are given a set of n (n is always a power of 2) elements containing all integers 0,1, 2,...,n-1 exactly once.

Find n/2 pairs of elements such that:

- Each element in the set is in exactly one pair.
- The sum over all pairs of the <u>bitwise AND</u> of its elements must be exactly equal to k. Formally, if  $a_i$  and  $b_i$  are the elements of the i-th pair, then the following must hold:

$$\sum_{i=1}^{n/2} a_i \& b_i = k$$

where & denotes the bitwise AND operation.

If there are many solutions, print any of them, if there is no solution, print -1 instead.

INPUT	OUTPUT
The input consists of multiple test cases. The first line contains a single integer $t$ ( $1 \le t \le 400$ )	For each test case, if there is no solution, print a single line with the integer $-1$ .
— the number of test cases. Description of the	Otherwise, print n/2 lines, the $i$ -th of them must
test cases follows.	contain $a_i$ and $b_i$ , the elements in the $i$ -th pair.
Each test case consists of a single line with two integers $n$ and $k$ ( $4 \le n \le 2^16$ , $n$ is a power	If there are many solutions, print any of them.  Print the pairs and the elements in the pairs in
of 2, $0 \le k \le n-1$ ).	any order.
The sum of <i>n</i> over all test cases does not	
exceed 2^16. All test cases in each individual	
input will be pairwise different.	

Example 1:

INPUT	OUTPUT
4	0 3
4 0	1 2
4 1	0 2
4 2	1 3
4 3	0 1
	2 3
	-1

## Explaination:

In the first test, (0&3)+(1&2)=0.

In the second test, (0&2)+(1&3)=1.

In the third test, (0&1)+(2&3)=2.

In the fourth test, there is no solution.

<sup>i</sup> In <u>computer programming</u>, a **bitwise operation** operates on a <u>bit string</u>, a <u>bit array</u> or a <u>binary numeral</u> (considered as a bit string) at the level of its individual <u>bits</u>. It is a fast and simple action, basic to the higher-level arithmetic operations and directly supported by the <u>processor</u>. Most bitwise operations are presented as two-operand instructions where the result replaces one of the input operands.

On simple low-cost processors, typically, bitwise operations are substantially faster than division, several times faster than multiplication, and sometimes significantly faster than addition. While modern processors usually perform addition and multiplication just as fast as bitwise operations due to their longer <u>instruction pipelines</u> and other <u>architectural</u> design choices, bitwise operations do commonly use less power because of the reduced use of resources.<sup>1</sup>