

TONBRIDGE
SCHOOL

NEA PROJECT

Gomoku and Renju

A software made for Mr Shafer

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Chapter 1

Analysis

1.1 Introduction

1.1.1 The Client

Mr John Shafer is an English teacher in Tonbridge School. He is familiar with some Asian board games, and Gomoku is one of them. He likes the game Gomoku, but sometimes he is unable to find a board and an opponent to play with. Therefore, he asked if I could build a software for him, so he could play Gomoku on his computer.

1.1.2 Gomoku

Gomoku, or Five in a Row, is a strategy board game. The game is played on a 15×15 board, with black and white stones. The player with the black stones moves first. Players take turns to put stones of their color on the board, and the first player to put five stones of their color consecutively in a straight line wins. The line can be horizontal, vertical, or diagonal. Although this game has simple rules, the complexity of the strategies involved is rather high.

1.1.3 Renju

Gomoku begins with black, so black will have a slight advantage. Renju is designed to make it fair for both players. In Renju, there are extra move restrictions for black, namely the moves "3x3 fork", "4x4 fork", and "overline". The detailed rules are stated in the [Renju website¹](#).

1.2 Interview

The following is a manuscript of an interview with the client, Mr John Shafer.

Question: Why do you want this software?

Mr Shafer: Gomoku is a fun game because of its simplicity. I want to bring it around so I can play with my friends, but the game is not portable because it must be played on a large 15×15 board with many black and white stones. I would also like the software version to have more additional functionalities to improve my skills.

Question: You mentioned about the simplicity of this game. Can you explain how do you play this game?

Mr Shafer: You take turns to play black or white stones on the board. The first to get five stones in a row along a vertical, horizontal, or diagonal line wins. These are the rules of Gomoku, but I also like the "Renju" variation of this game, which poses some restrictions to the black player. This makes the game fairer because Black as the first player always has some advantage. It would be great if you can also add the Renju variant in the software.

Question: Why is any of the existing software not suitable for you? How should this software to be the same or different from them?

Mr Shafer: I have used several online Gomoku websites with very strong AI players. However, I cannot learn anything from them because their moves are too complicated for me to understand. I would like to play with a AI players of similar skill level as me. On the other hand, these websites provided a simple interface for me to carry out post-game analysis. The mobile application, Gomoku Online, has a provided a variety of

¹<https://www.renju.net/rules/>

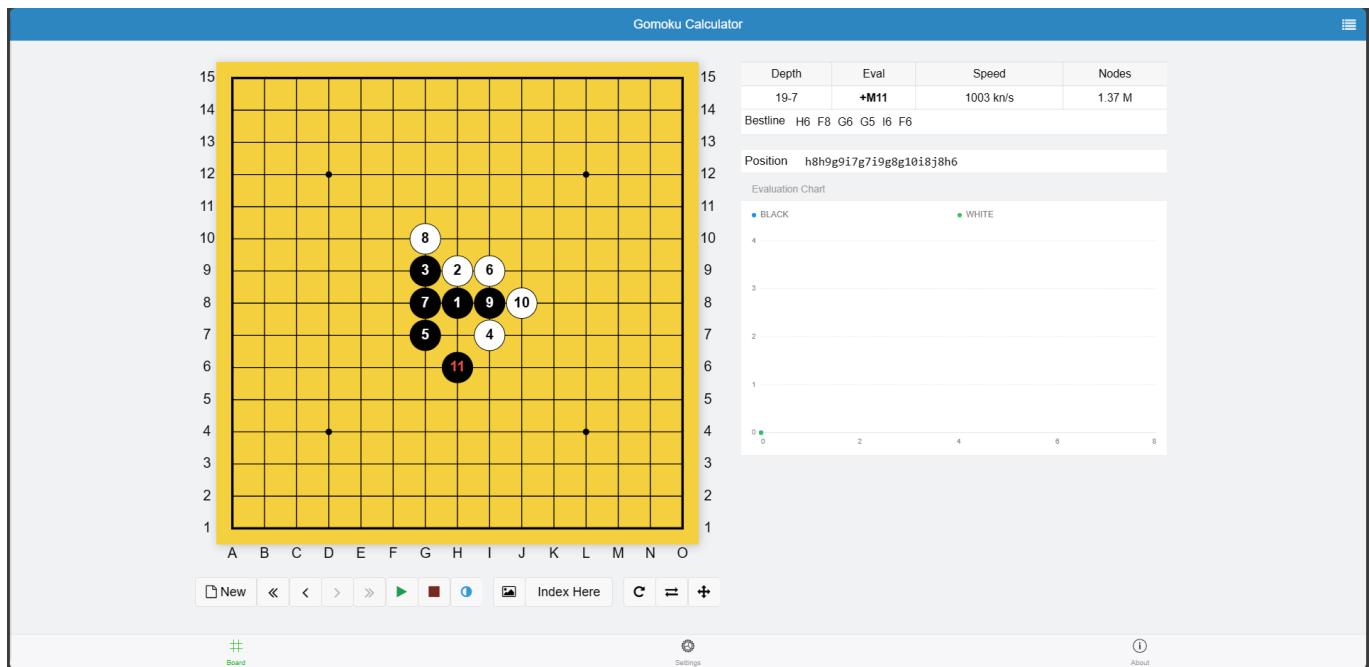


Figure 1.1: The website Gomocalc.

difficulties of AI players, but it is hard to tell whether I have improved. I would like this software to have the best of both worlds. It should provide me with many AI players and my relative skill level comparing to them, while also providing a simple interface for post-game analysis.

Question: What features do you want for post-game analysis in the software?

Mr Shafer: I would like it to tell me that if either black or white is advantageous in some board. This would be very beneficial for me to determine whether a move is good or bad. I would also like it to provide me with a possible continuation of the game. It allows me to see what would happen if I made a different move. This is essential for me to learn from my mistakes.

Question: Is there any other features which you would like to have in the software?

Mr Shafer: I would also like to save a game and load it later, so I can review games again and again.

1.3 Problem

The client wants an electronic version of the board game Gomoku. He would also like to have the Renju variant of the game implemented. He wants features that can improve his strength, with computer players of a variety of strength, a ranking system, and post-game analysis.

1.4 Past solutions

1.4.1 Websites

Multiple apps or websites which allow the users to play Gomoku with a computer player. For example, in the websites <https://gomoku-ai.azurewebsites.net/> and <https://gomocalc.com/#/>, users can play against a powerful Gomoku computer player. Both websites have a user interface that is easy to understand and use. Gomocalc provides additional customisation settings, which the user can configure the game to play with different rulesets, including Renju.

My client, Mr Shafer, said the computer players have deep computation that can calculate forced winning sequences of more than 12 moves long. Although they were great, they were too powerful for him, and he would like to play with players that are of similar level as him. He also mentioned the lack of analysis functions. He wants to setup the board into any position, including artificial ones. He added that he liked the feature showing a possible continuation of the game. In addition, he enjoyed playing Renju, a Gomoku variant, in the website Gomocalc.

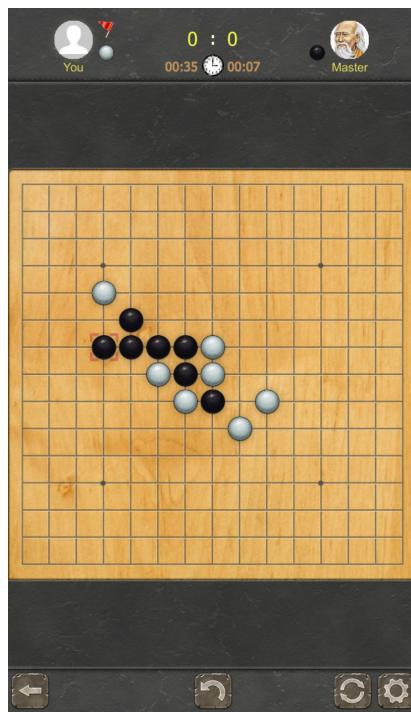


Figure 1.2: The mobile application, Gomoku Online.

1.4.2 Mobile applications

There are many implementations of this game on the mobile platform as well. A notable example is the application called Gomoku Online. It provides a variety of difficulties of computer players to the user, unlike the websites that only provide one. It also allows the user to play with other players online if they have internet access.

My client stated that he liked to play against computers of different skill levels. However, he said it would be better if the application could estimate his skill level comparing to the players, so he could understand whether he had improved and he could decide which player to challenge. He once again emphasised the importance of post-game analysis. He would like to know which side is winning, and the best continuation of some game board.

1.4.3 Conclusion

My client found the above solutions unsatisfactory. In particular, the lack of analysis functions displeased him. In addition, he thinks that multiple computer players of varying difficulties is necessary. Moreover, he would like a feature that estimates his skill level comparing to the computer players.

My client added that he enjoyed using the above solutions because of its simple user interface. He is also fascinated by the long sequence of forced winning moves that the computer is able to calculate in the Gomocalc website. Moreover, he liked the customisation features that Gomocalc provides, he wanted to play Renju. He requested the software that I will build should include all the features he desired.

1.5 Other end users

Other parties might want to add more computer players to the software, to either increase the difficulty or the variety of game strategies. They might need to edit my code and then implement a new computer player. They might implement the players in a compiled language such as C++ to improve the efficiency so as to calculate deeper moves. Therefore, I need to make sure my code can be easily understood and maintained.

1.6 Objectives

After considering the requirements from the client and potential other third parties, the following are the objectives of the software.

1. The software should have a GUI that allows easy navigation to different parts of the software.
 - 1.1. There is a title screen that contains buttons which navigates to the play, analysis, and rankings screen.

- 1.2. There are exit buttons in the play screen, analysis screen, and rankings screen to return to the title screen.
- 1.3. There is a sidebar with buttons to navigate to the moves of a game.
2. The player should be able to play Gomoku and Renju.
 - 2.1. There is a 15x15 game board with black and white stones.
 - 2.2. In Gomoku rules, the player should be able to place stones in any empty cell.
 - 2.3. In Renju rules, the player should be able to place stones in any empty cell that the rules permit.
 - 2.4. Able to claim victory when they placed five stones in a row.
 - 2.5. Transparent pieces floating on the board when the user is hovering over a cell.
 - 2.6. Highlighting the most recent move with the colour red.
3. The player should be able to customise the settings for each game.
 - 3.1. There is a configuration screen before each game is played.
 - 3.2. The user should be able to choose the ruleset of the game.
 - 3.3. The user should be able to choose what player is playing with what colour.
 - 3.4. The user should be able to spectate a computer vs computer game.
4. The player should be able to save a game after it is played.
 - 4.1. There is a button to save the game.
 - 4.2. The user should be able to name the players of the game.
 - 4.3. The game should be saved in a file.
5. The player should be able to analyse a game after it is played.
 - 5.1. The user should be able to load a saved game with a button.
 - 5.2. There are buttons that after pressing, each move places black or white pieces on the board.
 - 5.3. There is a button that after pressing, each move alternates the colour of the pieces on the board.
 - 5.4. The user should be able to see which side is winning, analysed by a computer player of the user's choice.
 - 5.5. The user should be able to see the best continuation of some game state, analysed by a computer player of the user's choice.
6. There should be a variety of computer players.
 - 6.1. There should be at least 10 computer players of different skill levels.
 - 6.2. The player should be able to play with any computer player.
 - 6.3. The computer players should be able to play with each other and themselves.
7. The software should have a ranking system.
 - 7.1. There should be a rankings screen that shows the rank of each player.
 - 7.2. The user should also be able to see the skill level of each player.
 - 7.3. The skill levels of players should be updated after each game.

1.7 Research

1.7.1 Threat-space search

The threat-space search (TSS) algorithm searches for threats and tries to find a threat sequence to win the game [1]. A threat is a move that must be responded by the opponent or else they will lose the game. TSS ignores defensive moves and focus on offensive moves entirely. The Victoria program in [1] plays moves from its database, and when it is out of its database, it uses the TSS algorithm. It won the 1992 Computer Olympiad for Gomoku.

1.7.2 Minimax with alpha-beta pruning

The minimax algorithm with alpha-beta pruning was used for a bot to play Gomoku [2]. In their paper, they used the evaluation function:

$$\begin{aligned} Eval = & w_1 \times \#five-in-row + w_2 \times \#straight-four \\ & + w_3 \times \#four-in-row + w_4 \times \#three-in-row \\ & + w_5 \times \#broken-three + w_6 \times \#two-in-row + w_7 \times \#\text{single marks} \end{aligned} \quad (1.1)$$

They also used the following optimisation methods to reduce search space:

- Eliminate actions of no real value
- Sorted successor list
- Local beam search

These methods are used improve the efficiency of minimax.

1.8 Proposed Solution

1.8.1 Language

I am fluent in C++, Python and Rust. To choose between them, I considered the pros and cons of both languages, and how can the features benefit the development of this project.

C++	
Pros	Cons
Lower execution time due to compilation Has object-oriented programming features Gives low-level control	Hard to use online libraries Longer debug times Unsafe due to lack of garbage collection

Python	
Pros	Cons
Easy memory management due to garbage collection Has many public packages and a package manager High readability	Low efficiency since it is interpreted High memory usage

Rust	
Pros	Cons
High security since memory safety is provided High performance since it is compiled	Longer development times due to complex syntax and concepts Does not strictly support object-oriented Rust is still new, it has fewer packages and libraries

In terms of development time, I think it is important to minimise the development time. Knowing what the client wants is crucial to this project, and usually these meetings are time-consuming. Moreover, the client would like many features, so time must be carefully used to implement all the required features.

In terms of custom libraries, using them will allow me to write a lot less code, hence improving the development time. A convenient GUI library is essential for my project, since the client demands a simple GUI.

In terms of time and memory usage, they are not as important to me since computational heavy calculations are rarely used in this project, it will only be used when the computer player is finding the best move.

In terms of object-oriented programming, I would like to use a language with such feature because it will be beneficial to organise my code in objects in this large project.

Considering these four aspects, I chose Python as my main programming language since it has short development times due to its high readability, the abundance of public packages, and the features of object-oriented programming.

1.8.2 IDE

The three most popular Python IDEs are IDLE, Pycharm, and Visual Studio Code (VS Code). The pros and cons of these IDEs are considered in the following tables.

IDLE	
Pros	Cons
Easy to get started Free	Not suitable for large-scaled projects Fewer customisation functions
Pycharm	
Pros	Cons
Specialises in Python and the development of large-scale projects Reliable debugger	The premium version requires a subscription Less customisable
VS Code	
Pros	Cons
Free and lightweight High customisability including Git integration Has powerful features like IntelliSense code completion and code refactoring	Hard to setup

In terms of the cost, I would prefer to minimise the cost as the project is done without any budget. Therefore, IDLE and VS Code would be more preferable.

In terms of customisability, it will be very useful if it can drastically reduce the development time with powerful functions like code completion, or the use of keyboard shortcuts. VS Code is the only IDE that provides such features.

In terms of debugging, a powerful debugger can reduce development time as well. Instead of manually tracing variables, I can instead rely on the debuggers. VS Code can be customised to provide a debugger, and the debugger provided by Pycharm is also preferred.

In terms of the time used for setting up an IDE, it is not a major concern in my opinion since the time used will be negligible comparing to the long development time.

In conclusion, considering these four aspects, I chose to use VS Code due to its cost, customisability, and the Python debugger. Moreover, I am familiar to VS Code so I am more inclined towards it.

1.8.3 Modelling

A game of Gomoku/Renju consists of moves and game states. These features resemble a graph, in which nodes are game states and edges are moves. In fact, the graph is a rooted tree as each game state only have one previous move, i.e., only one parent. Game states consists of the board, and the current player to make a move. Refer to Figure 1.3 for a diagram.

1.8.4 Programming Paradigms

Object-Oriented Programming

Object-Oriented Programming (OOP) is beneficial to code organisation for objects (classes) in large projects. It is usually regarded as good programming principles and it gives many benefits such as modularity, polymorphism, and code reusability. Most importantly, it can greatly reduce development time.

Observer Pattern

By using the observer pattern, objects in my code can notify its dependents (observers) if there are any changes in their state, by calling the methods of its observers. In particular, it can address one-to-many relationships in my objects and is generally regarded as great for notifications among the GUI elements.

1.9 Software Development Plan

Since only 12 weeks of development time are available for me, proper planning is needed to ensure that the project can be finished on time. Therefore, I have created a Gantt chart to plan the schedule of the project, as shown in Figure 1.4.

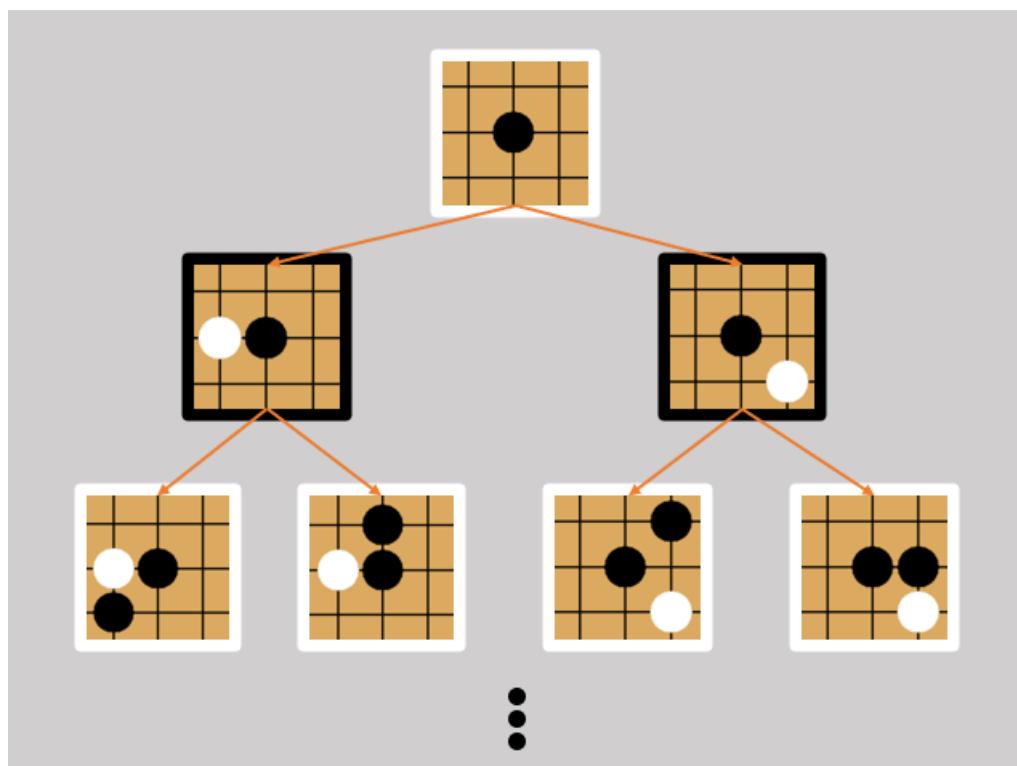


Figure 1.3: The game tree. The color of the outline of the boards represent the current player.

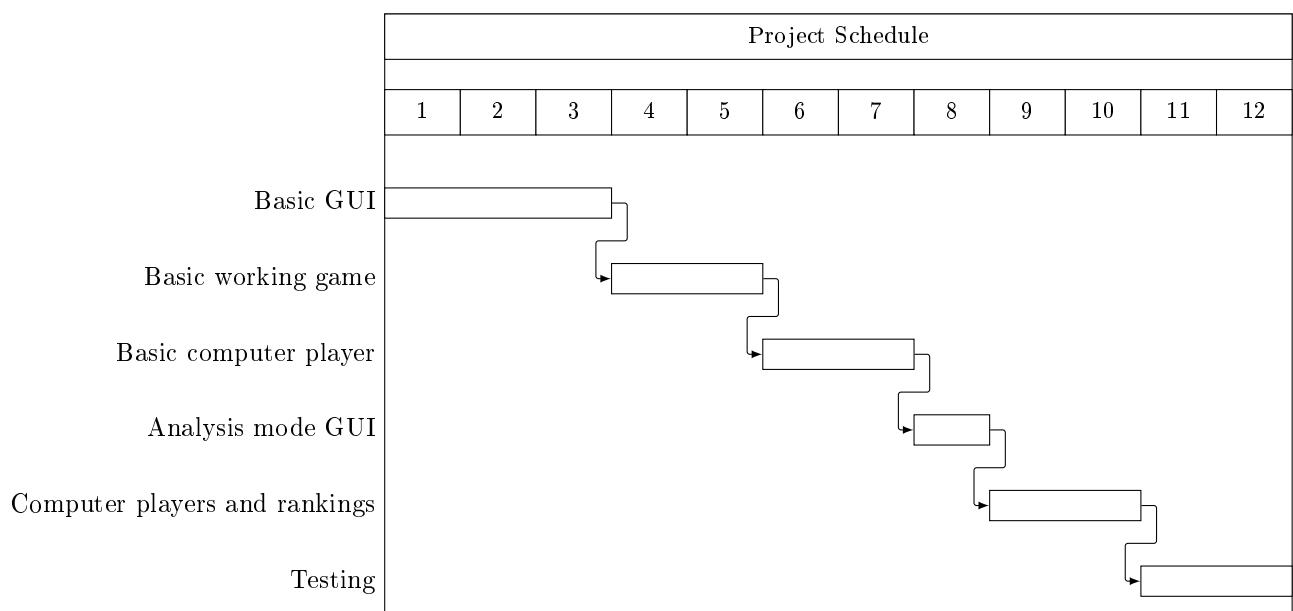


Figure 1.4: Gantt chart for the project schedule.

Chapter 2

Design

2.1 Overview

2.1.1 Top-level

In this subsection, I will describe the top-level overview of how the system works in my program. By abstracting the objects in the system, it allows me to hide all the complexity of the details of the objects and instead focus on the relevant information, such as, the relationships between the objects. Figure 2.1 shows the relationships of the windows in the software.

2.1.2 Title Screen

According to Objective 1.1, the title screen should have buttons that allows the user to navigate to various areas of the software. They include:

- **Play:** This button first asks the user for configuration settings of the game. Then, it navigates the user to the play screen.
- **Analysis:** This button navigates the user to the analysis screen.
- **Rankings:** This button navigates the user to the rankings screen.

A design of the GUI is shown in Figure 2.2.

When the **Play** button is pressed, the software should first ask the user to configure the game, according to the requirements of objective 3. They should be able to:

- Choose to play either Gomoku or Renju.
- Choose who the black player is.
- Choose who the white player is.
- If both players are computer players, the user should be able to choose how many times the game should be played, and the software should then play the game that many times and update the rankings accordingly.

A design of the GUI is shown in Figure 2.3.

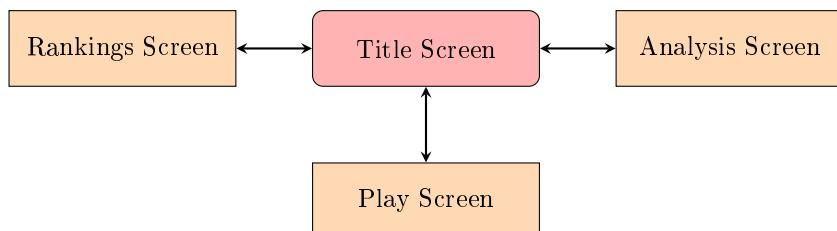


Figure 2.1: Top-level Overview

Gomoku and Renju



Figure 2.2: The GUI of title screen.

Configure the game

Select game type

Gomoku

Select black player

Minimax 3

Select white player

Human Player

Repeat 3 times

Should only appear
if both players are
computer players

Figure 2.3: The GUI of configuration screen.

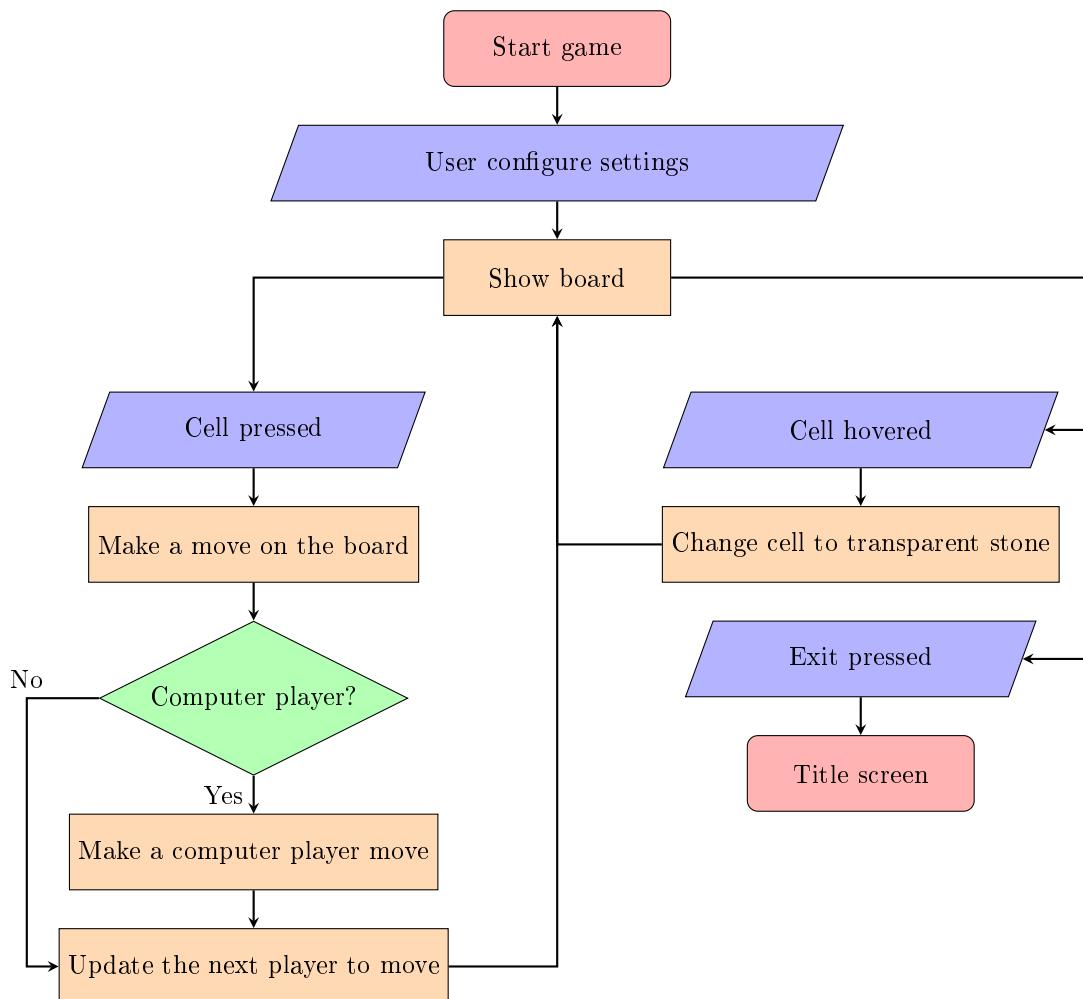


Figure 2.4: Play screen

2.1.3 Play Screen

In the play screen, we wish to achieve objective 2. When the play screen appears (by pressing the **Play** button in the configuration screen), it should show the game board to the player. After that, it should respond to user inputs, including when a cell is hovered, pressed, or when the exit button is pressed. Objective 2.5 is satisfied by showing transparent pieces on the board when a cell is being hovered. A logic flowchart is shown in Figure 2.4.

The GUI is shown in Figure 2.5

2.1.4 Analysis screen

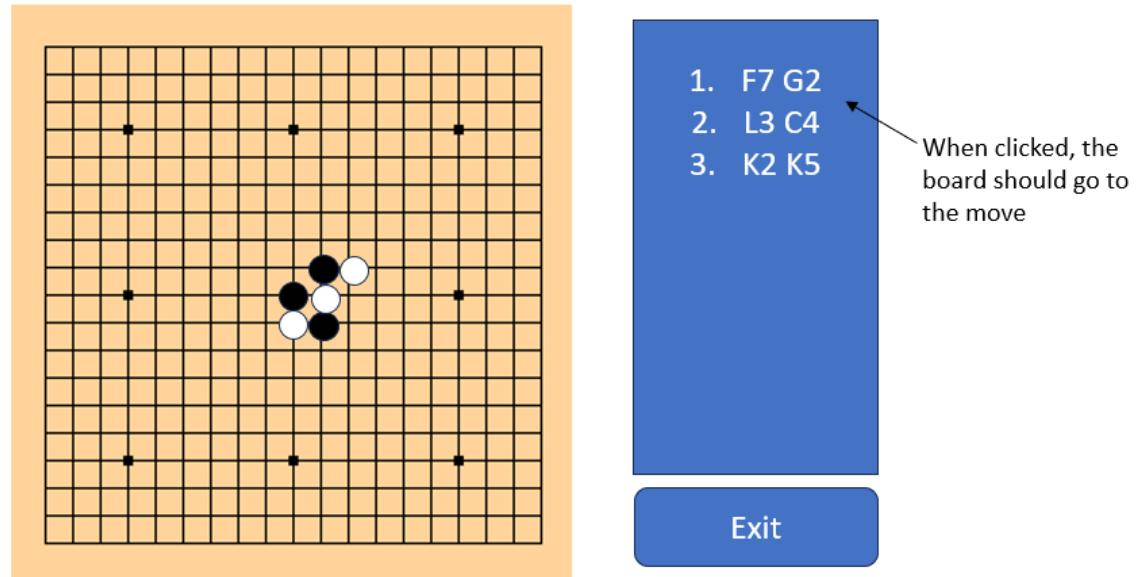
In the analysis screen, the functions in the play screen should be present, with the additional functions of import game, export game, getting the evaluation of the board, and getting the best move of the board.

It should also include three additional buttons to assist setting up the board, according to objective 5.2-3. These three buttons are named as the black, white, and black/white buttons. After the black button is pressed, every cell pressed by the user will be changed to a black stone. The same happens for after the white button is pressed. After the black/white button is pressed, the user now places black and white stones alternatively. Its function is also described in Figure 2.6.

The GUI is shown in Figure 2.7.

2.1.5 Sidebar

The sidebar is present in both the play screen and the analysis screen. It allows the user to navigate to all the moves of the game. Its GUI can be seen in both Figure 2.5 and Figure 2.7. The logic of the buttons in the sidebar is shown in Figure 2.8.



It's now the black player's turn!

A space for showing messages

Figure 2.5: The GUI of play screen.

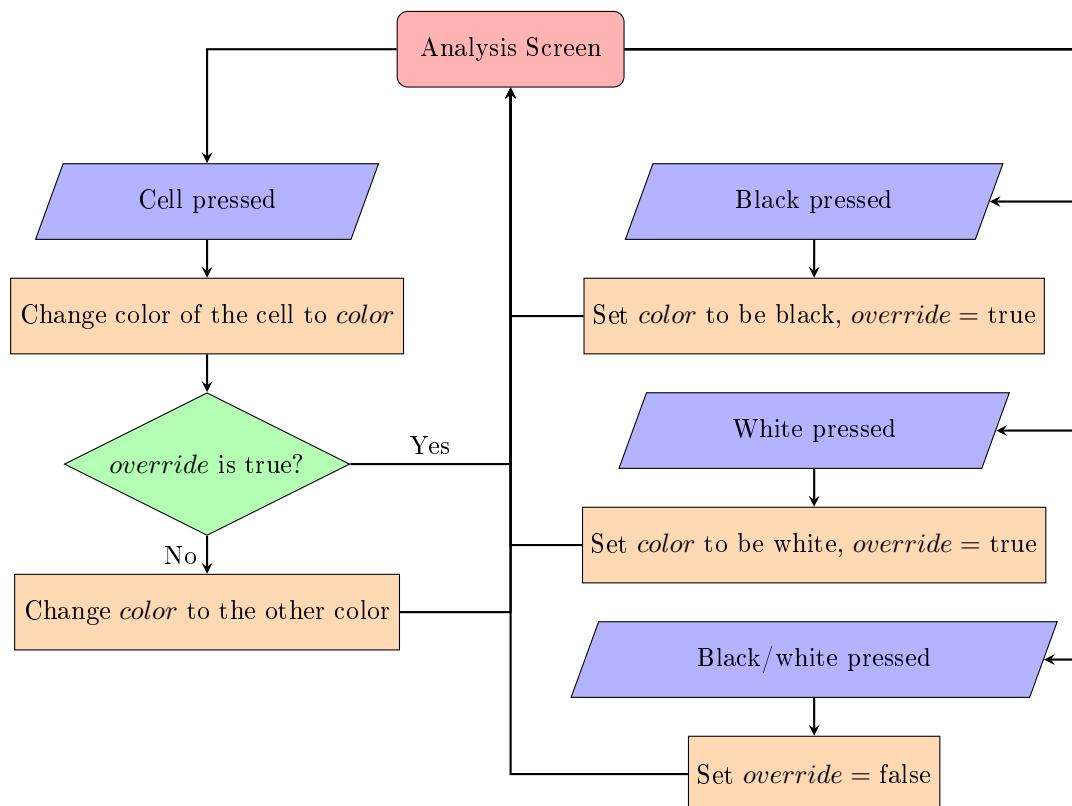
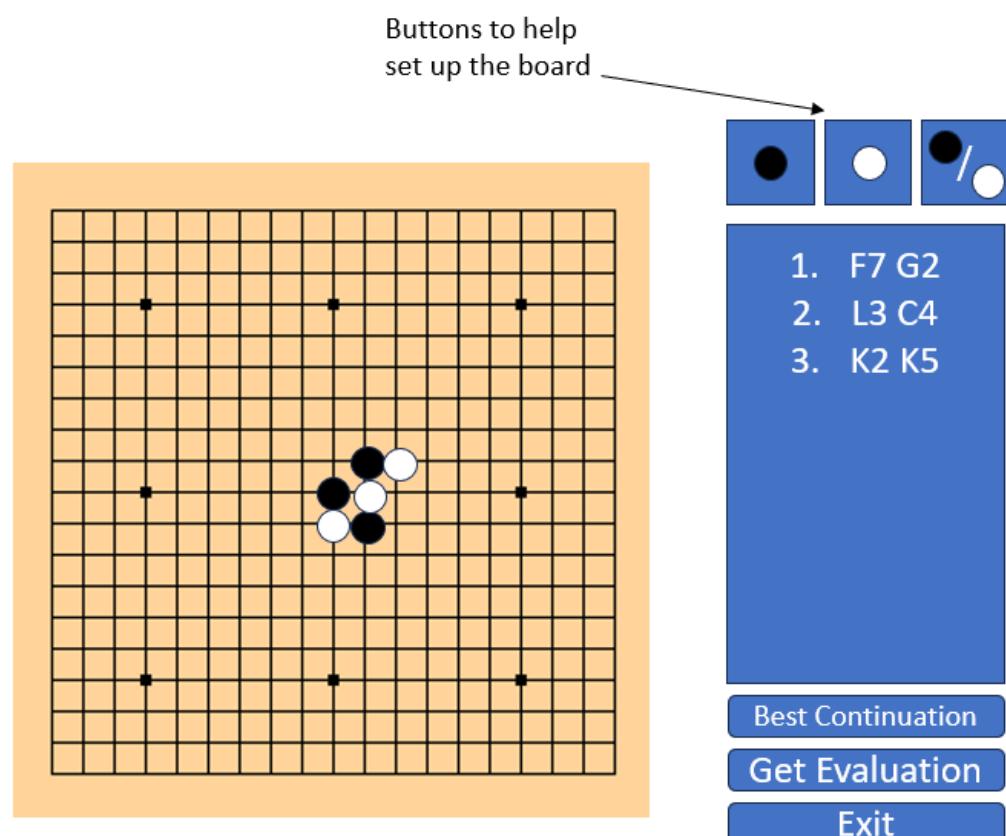


Figure 2.6: The three buttons in analysis screen.



Evaluation: White winning (-503)

Figure 2.7: The GUI of analysis screen.

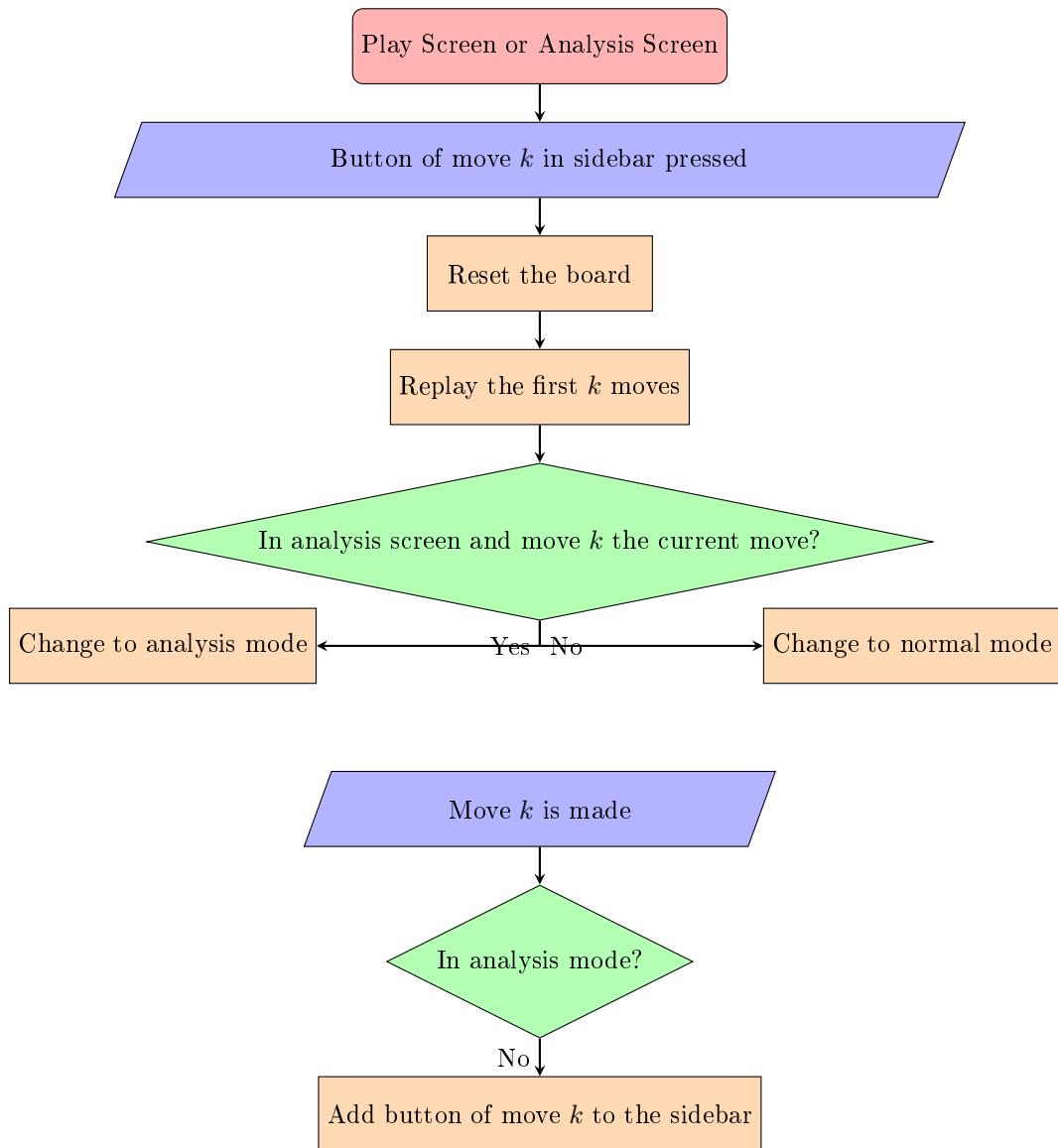


Figure 2.8: Logic of the buttons in the sidebar.

Rank	Name	Elo Rating
1	Minimax 3	1601
2	Human Player	1555
3	Aggressive 2	1539
4	Defensive 4	1438
5	Prioritise Threats 2	1429
6	Random Moves	1328



Exit

Figure 2.9: The GUI of rankings screen.

2.1.6 Rankings screen

In the ranking screen, objective 7 should be met. There should be a table of the rankings of the human player and computer players, and it should be shown sorted by their rating in descending order. The GUI is shown in Figure 2.9. The flowchart for showing the rankings is shown in Figure 2.10.

2.2 Algorithms

2.2.1 Board pattern recognition

According to objective 2, the rules of Gomoku and Renju should be implemented. Therefore, the whole board needs to be checked at every move to disallow illegal moves and to check for winning patterns.

For example, we would like to check for five-in-a-rows, straight fours, and threes. According to the official Renju rules, a straight four is a row with four stones to which you can add one more stone to attain five in a row, and a three is a row with three stones to which you, without at the same time a five in a row is made, can add one more stone to attain a straight four. As these patterns are frequently checked to apply the Renju rules and also by my board evaluation function (in Minimax), these patterns must be checked swiftly. In particular, the questions of "How many given patterns of pieces of a given colour are there? What about the patterns that must involve a given cell?" will be frequently asked. We start with a brute-force approach.

Brute-force search

Here we use a Cartesian grid system to store the state of the board as it is convenient. We can do a brute force search to find fives on the board by Algorithm 1.

In the algorithm I assumed the function `get_color()`, which gets the color in the specified *position* from the board. If the board size is 15×15 , this algorithm will call `get_color` at most $15 \times 15 \times 5 \times 4 = 4500$ times.

This method contains some inefficiencies as there are some repeated calls to `get_color()` with the same arguments, especially in the for loop of *k* from 0 to 4.

Partial sum

Partial sum is a common technique used to optimise the counting of elements in an array. It can count the number of elements in any interval in an array in constant time. It first constructs an array *P*, where *P*[*i*] is the number of elements before *i*. It can then calculate the number of elements within an interval $[l, r)$ using $P[r] - P[l]$, in constant time.

In the for loop of *k* from 0 to 4, we aim to count the number of cells of color *color* starting *position* going in the specified *direction*. Here we can use partial sum to optimise the counting.

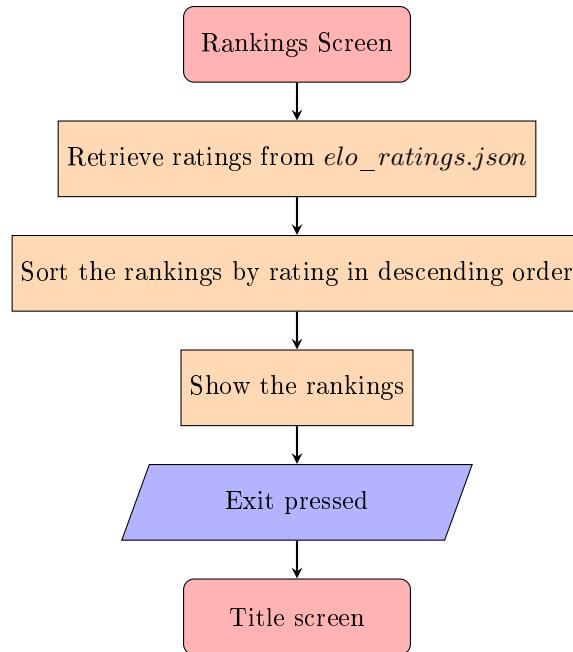
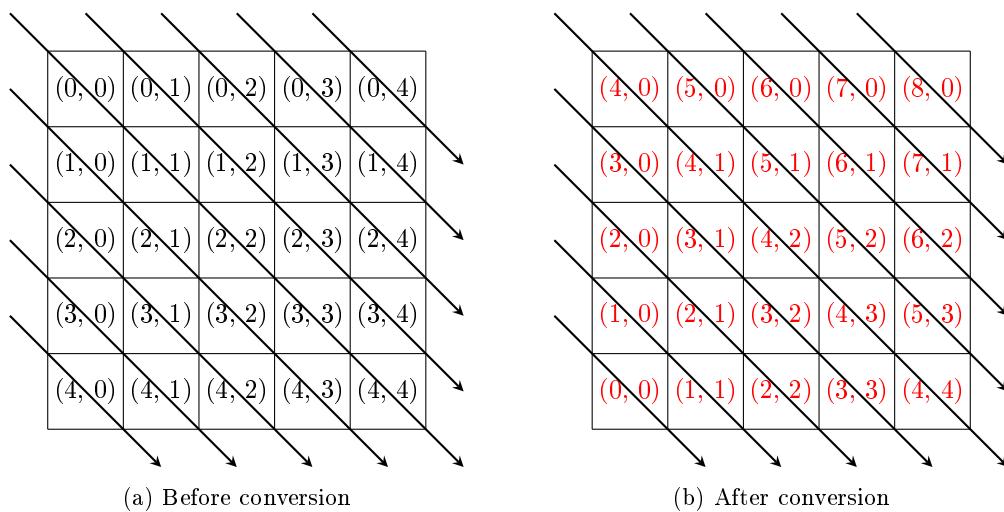
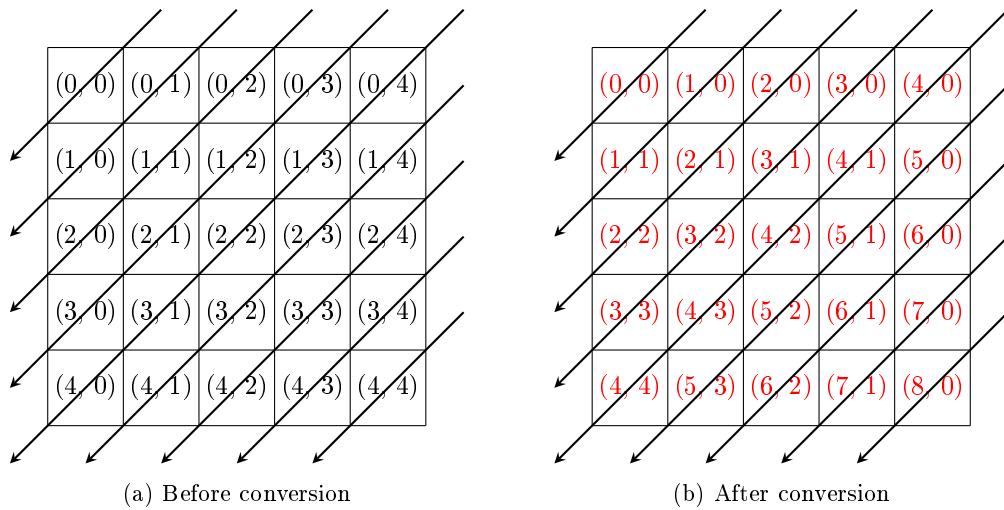


Figure 2.10: Rankings screen

Algorithm 1: Brute-force search

```

function find_five(board, row, col, color):
    # Define the directions: vertical, horizontal, and the two diagonals
    directions  $\leftarrow \{(0, 1), (1, 0), (-1, 1), (1, 1)\}$ 
    foreach direction in directions do
        forall position do                                # for all positions (x, y) on the board
            count  $\leftarrow 0$ 
            for k  $\leftarrow 0$  to 4 do
                new_position  $\leftarrow \text{position} + k \times \text{direction}
                if new_position is out of bounds then
                    break
                end
                if get_color(new_position) is color then
                    count  $\leftarrow \text{count} + 1
                end
            end
            if count = 5 then
                return True
            end
        end
    end
    return False
end$$ 
```

Figure 2.11: $\text{direction} = 2$ Figure 2.12: $\text{direction} = 3$

To use this optimisation, the cells must be in an array. For orthogonal lines, it can be easily implemented, since the cells are ordered in a Cartesian plane system. However, for diagonal lines, it may be hard to implement. We can overcome this problem by using new coordinate systems.

Coordinate conversion

We can use the Cartesian system for orthogonal directions. We can define $\text{direction} = 0$ corresponds to horizontal lines and $\text{direction} = 1$ corresponds to vertical lines. Let (a, b) be the coordinates in the new system. In this system, when traversing a line, a should remain constant and b should be incremented when the next cell on the line is reached. Therefore we can set a to be *row* and b to be *col* for $\text{direction} = 0$ and vice versa for $\text{direction} = 1$.

Let $\text{direction} = 2$ corresponds to southeastwards and $\text{direction} = 3$ corresponds to southwestwards. Notice that on a line of $\text{direction} = 2$, the quantity $\text{col} - \text{row}$ is invariant, so can set a based on this value. Same for the quantity $\text{col} + \text{row}$ for $\text{direction} = 3$. We can then set b according to the requirements with some careful handling. An example for a conversion for both directions in a 5 by 5 grid is shown in Figures 2.11 and 2.12.

Partial sum with converted coordinates

Using this coordinate system (called the *line* system hereinafter), we can apply the partial sum technique. We define the 4-dimensional array *partial_count*, such that *partial_count*[*dir*][*color*][*a*][*b*] is the number of cells with color *color* on a line of direction *dir* that is before the cell (a, b) . After constructing the array, we can query for the number of cells with color *color* on a line of direction *dir* starting from (a, b) with a length of a given *length* using the function *range_query*. Its pseudo-code is shown in Algorithm 2.

Now *find_five* takes a maximum of $15 \times 15 \times 4 = 900$ calls to *range_query* which is an improvement.

Algorithm 2: Partial count

```

 $n \leftarrow 15$  #  $n$  is the size of the board
function line_to_cartesian( $dir, a, b$ ):
    if  $dir = 0$  then
        return  $(a, b)$ 
    else if  $dir = 1$  then
        return  $(b, a)$ 
    else if  $dir = 2$  then
         $d \leftarrow \max(n - 1 - a, 0)$ 
        return  $(b + d, b - d)$ 
    else
         $d \leftarrow \max(a - (n - 1), 0)$ 
        return  $(b + d, a - b - d)$ 
    end
end
# Compute partial_count
partial_count  $\leftarrow$  4-D array with sizes  $[4][3][2n - 1][n + 1]$  initialised with 0
for  $dir \leftarrow 0$  to 3 do
    forall  $(a, b)$  of direction =  $dir$  do
         $(row, col) = \text{line\_to\_cartesian}(dir, a, b)$ 
        foreach color in {black, white, blank} do # We can encode the color with 0, 1, 2
             $\text{partial\_count}[dir][color][a][b + 1] \leftarrow \text{partial\_count}[dir][color][a][b] + (1 \text{ if } \text{get\_color}(row, col) \text{ is } color \text{ else } 0)$ 
        end
    end
end
function range_query( $dir, a, b, color, length$ ):
    # Assuming ( $dir, a, b$ ) is in bounds
    return  $\text{partial\_count}[dir][color][a][b + length] - \text{partial\_count}[dir][color][a][b]$ 
end
# Now we can compute find_five using range_query()
function find_five( $board, row, col, color$ ):
    for  $dir \leftarrow 0$  to 3 do
        forall  $(a, b)$  of direction =  $dir$  do
            # Handle the out of bounds cases
            if range_query( $dir, a, b, color, 5$ ) = 5 then
                return True
            end
        end
    end
    return False
end

```

2.2.2 Computer player: Minimax

Minimax

Both Gomoku and Renju is a zero-sum game, meaning that an advantage for one side is equivalent to a disadvantage for the other side. Minimax is an algorithm that is commonly used in these games, and the key idea is to maximise the minimum gain (or minimise the maximum loss) of every move, hence the name.

This algorithm requires a measure of value in a board state, and we say the value is positive if it is advantageous to black, and vice versa. This algorithm assumes that both players play their best move, which means they play the move that maximises their minimum gain, according to the evaluation of the board state. To determine the best move for black, the algorithm maximises the value of every board state which the current board state can lead to, assuming white plays the best move.

To find the white's best move we can use the same method, but this time we minimise the values of the subsequent board states, and again we assume optimal play from black. Therefore, we can implement this algorithm recursively, finding the best move for both players, until the depth is reached. The pseudo code of this algorithm is shown in Algorithm 3.

Minimax is a algorithm that **traverses** the game tree (refer to 1.8.3). It uses **post-order traversal**. It processes the children of a node before the node itself. It is a **recursive** algorithm, and the base case is when the depth is 0, or when the board is won. In this case, the value of the board is returned. Otherwise, the algorithm will return the maximum or minimum value of the children depending on the colour of the player.

Algorithm 3: Minimax

```

function minimax(board, depth, color):
    if depth = 0 or board is won then
        return eval(board)
    end
    if color is black then
        value ← −∞
        foreach candidate in board.candidates do
            candidate_value ← minimax(candidate, depth - 1, white)
            value ← max(value, candidate_value)
        end
        return value
    end
    else
        value ← ∞
        foreach candidate in board.candidates do
            candidate_value ← minimax(candidate, depth - 1, black)
            value ← min(value, candidate_value)
        end
        return value
    end
end
# Initial call
d ← 4 # depth
minimax(board, d, color)
```

This algorithm has time complexity $O(n^d)$, where n is the maximum number of candidate boards which will be explained in the next subsection, and d is the depth specified in the parameter of the initial call to minimax.

Candidate boards

In minimax, we would consider all possible moves for both players, i.e., they all become candidate moves. The boards created when these moves are played are called candidate boards. In Gomoku, there are at most $15^2 = 225$ candidate boards. Since the time complexity of minimax is exponential in the number of candidate boards, we want to limit the number of candidate boards.

In practice, most candidate moves are obviously bad and is never considered (e.g. a move at a corner of the board). We can take advantage of this, and only consider moves that are at most r distance from any currently existing piece (*Eliminating actions of no real value* in [2]). We can get all such candidate boards (called the *search space* in this report) by the flowchart in Figure 2.13.

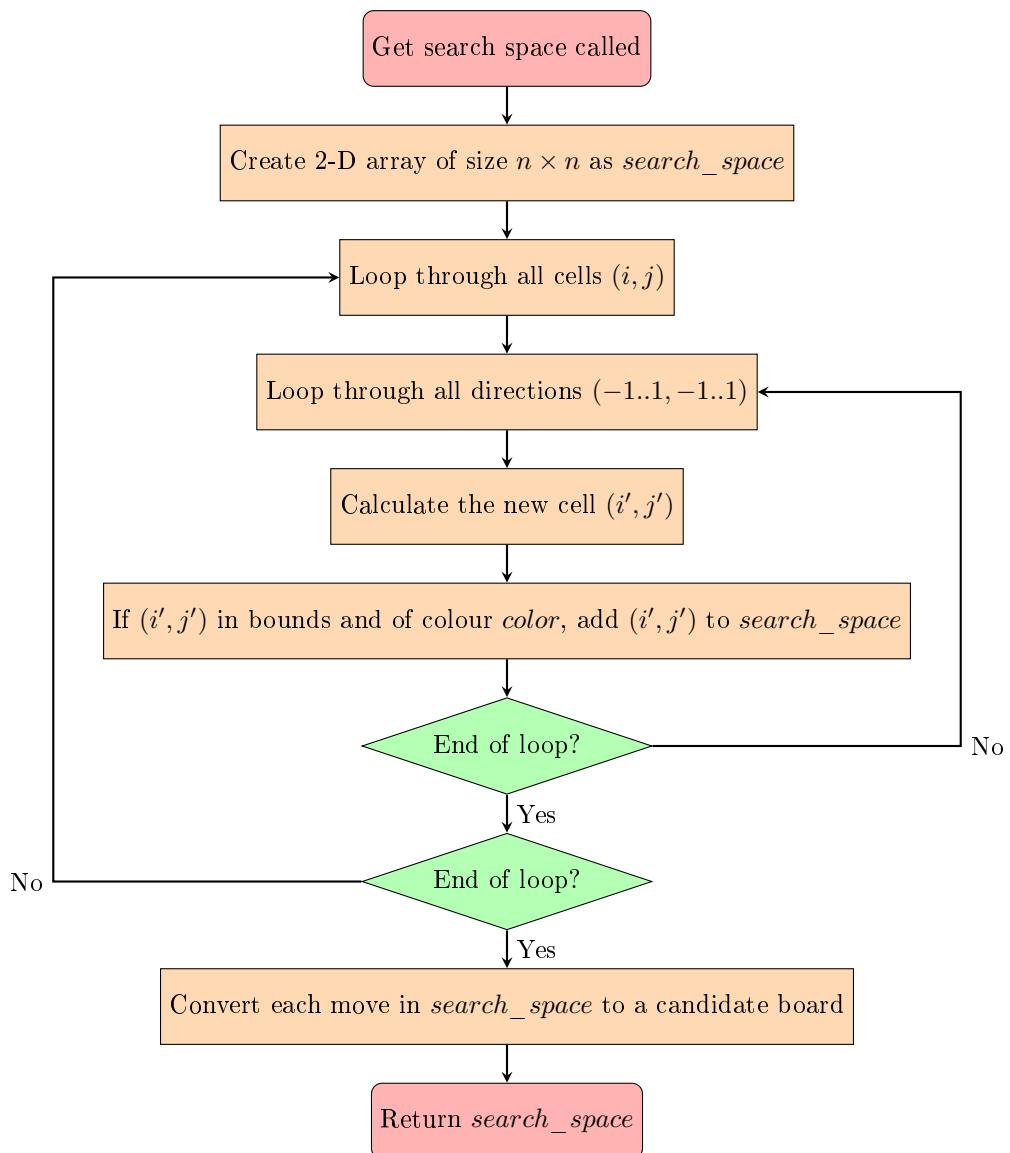


Figure 2.13: Search space

Minimax with local evaluation

As the time complexity of minimax is exponential in n , we want to keep it as low as possible. Therefore, we should limit the number of candidates of each node, which is the *branching factor*.

Instead of considering all possible moves from a board state, we want to limit it down to a chosen value b . We can achieve this by doing local evaluations. We only search the top b best moves according to their current evaluation.

In this way, we reduce the time complexity to $O(b^d)$.

Minimax with alpha-beta pruning

Intuitively, we can see that minimax has some inefficiencies when it searches for moves that is obviously bad for a player. To solve this problem, we can use this optimisation called alpha-beta pruning.

Alpha-beta pruning can reduce the number of nodes in the search tree. It stops evaluating a node when the result of it does not affect the final result of the computation.

This algorithm works by maintaining two variables α and β . They represent the minimum value of the maximising player (black) and the maximum value of the minimising player (white) respectively during the tree search. If at any stage $\alpha \geq \beta$, we can stop searching, since for both players the move will not be advantageous. For black, we do not need to search of any moves that has value less than α , since it is guaranteed that black can get at least a value of α in one of the branches. The same argument can be made with white. It can also be shown that with this pruning, the algorithm gives the same output as the original version of minimax.

To fully utilise this method we want to maximise α and minimise β , or in other words, we want to search the best moves for both players first. This can be done with a sorted candidate list, and can be combined with local evaluation. Algorithm 4 shows the pseudo code with both local evaluation and alpha-beta pruning.

Algorithm 4: Minimax with optimisations

```

 $b \leftarrow 5$  # The limit of the branching factor
function minimax(board, depth, color,  $\alpha$ ,  $\beta$ ):
    if depth = 0 or board is won then
        return eval(board)
    end
    candidates  $\leftarrow$  board.candidates
    sort candidates by eval descending
    candidates  $\leftarrow$  candidates[0 : b] # Take only the first b candidates
    if color is black then
        value  $\leftarrow$   $-\infty$ 
        foreach candidate in candidates do
            candidate_value  $\leftarrow$  minimax(candidate, depth - 1, white,  $\alpha$ ,  $\beta$ )
             $\alpha \leftarrow \max(\alpha, \text{candidate\_value})$ 
            if  $\alpha \geq \beta$  then
                break
            end
            value  $\leftarrow \max(\text{value}, \text{candidate\_value})$ 
        end
        return value
    end
    else # color is white
        value  $\leftarrow \infty$ 
        foreach candidate in candidates do
            candidate_value  $\leftarrow$  minimax(candidate, depth - 1, black,  $\alpha$ ,  $\beta$ )
             $\beta \leftarrow \min(\beta, \text{candidate\_value})$ 
            if  $\alpha \geq \beta$  then
                break
            end
            value  $\leftarrow \min(\text{value}, \text{candidate\_value})$ 
        end
        return value
    end
end
# Initial call
d  $\leftarrow$  4 # depth
minimax(board, d, color,  $-\infty$ ,  $\infty$ )

```

This algorithm gives the new best-case performance of $O(\sqrt{b^d})$, if all unnecessary nodes are optimally pruned. With a good evaluation function, we can expect a significant improvement over the original minimax algorithm.

Evaluation function

To correctly use the minimax algorithm, we need a good evaluation function. The evaluation function should be able to evaluate the board state and give a value that represents the advantage (or disadvantage) of black. It should also be able to evaluate the board state quickly.

In light of the evaluation function used in [2], we can use a similar evaluation function. We use the following:

$$\begin{aligned} \text{eval(board)} &= w_0 \text{ if board is won} \\ \text{eval(board)} &= w_1 \times (\#\text{straight four}) + w_2 \times (\#\text{open three}) + \\ &\quad w_3 \times (\#\text{four}) + w_4 \times (\#\text{three}) + \\ &\quad w_5 \times (\#\text{two}) + w_6 \times (\#\text{single marks}) \text{ otherwise} \end{aligned} \tag{2.1}$$

where $w_0, w_1, w_2, w_3, w_4, w_5, w_6$ are weights that can be adjusted. The weights can be adjusted to reflect the importance of each pattern. For example, if we want to prioritise straight fours, we can set w_1 to be a large value. The values I have used can be seen in `constants.py`.

With partial sum and converted coordinates, we can calculate the counts of board patterns quickly. We can then use these counts to evaluate the board state.

Multi-threading

Even with optimisations, the minimax algorithm still requires a lot of time to run. During this time, the GUI will be unresponsive. To tackle this problem, we can use multi-threading to run the minimax algorithm in the background, keeping the GUI responsive.

2.2.3 Computer player: Prioritise Threats

In this subsection, we will use the heuristic "Threat-space Search" developed by [1]. In their paper, they mentioned the idea of threats, which are compelling moves that must be responded by the opponent. Similar to their work, we define the following shapes of pieces as threats with decreasing power (also see Figure 2.14):

- *five*: a line of five squares, of which the attacker has occupied all five. This is a winning move.
- *straight four*: a line of six squares, of which the attacker has occupied the four center squares, while the two outer squares are empty. This is a winning threat.
- *four*: a line of five squares, of which the attacker has occupied any four, with the fifth square empty.
- *open three*: a shape such that the attacker can create a *straight four* in his next move
- *three*: a shape such that the attacker can create a *four* in his next move
- *open two*: a shape such that the attacker can create an *open three* in his next move

Since threats must be responded, we can use this to our advantage. Instead of searching the whole board for moves, we can search for our threats and the opponent's threats, then play or respond to them. Since the number of such moves is usually small compared to the *search space*, the search will be done very quickly. Therefore, instead of decreasing depth by one step, we can decrease it a fraction of a step. In practice, we could first multiply the maximum depth by some number, so we do not need to deal with fractions. Algorithm 5 shows the move-finding algorithm that prioritises threats.

Of course, we will combine this algorithm with alpha-beta pruning and local evaluation to further improve the performance.

2.2.4 Measurement of skill level

Just like many other quantities in real life, the skill level of a player can only be measured relatively to other players. In this case, it can be measured according to the wins and losses of a player. We would like a rating system that can find the probability of winning of a player given the ratings from both players.

With inspiration from the Elo rating system [3], we can use a logarithmic scale. Let $Q_A = 10^{R_A/400}$ and $Q_B = 10^{R_B/400}$, where R_A and R_B are the ratings of player A and B respectively. Now we can calculate the expected win rates for both players, E_A and E_B , by

$$E_A = \frac{Q_A}{Q_A + Q_B}, E_B = \frac{Q_B}{Q_A + Q_B}$$

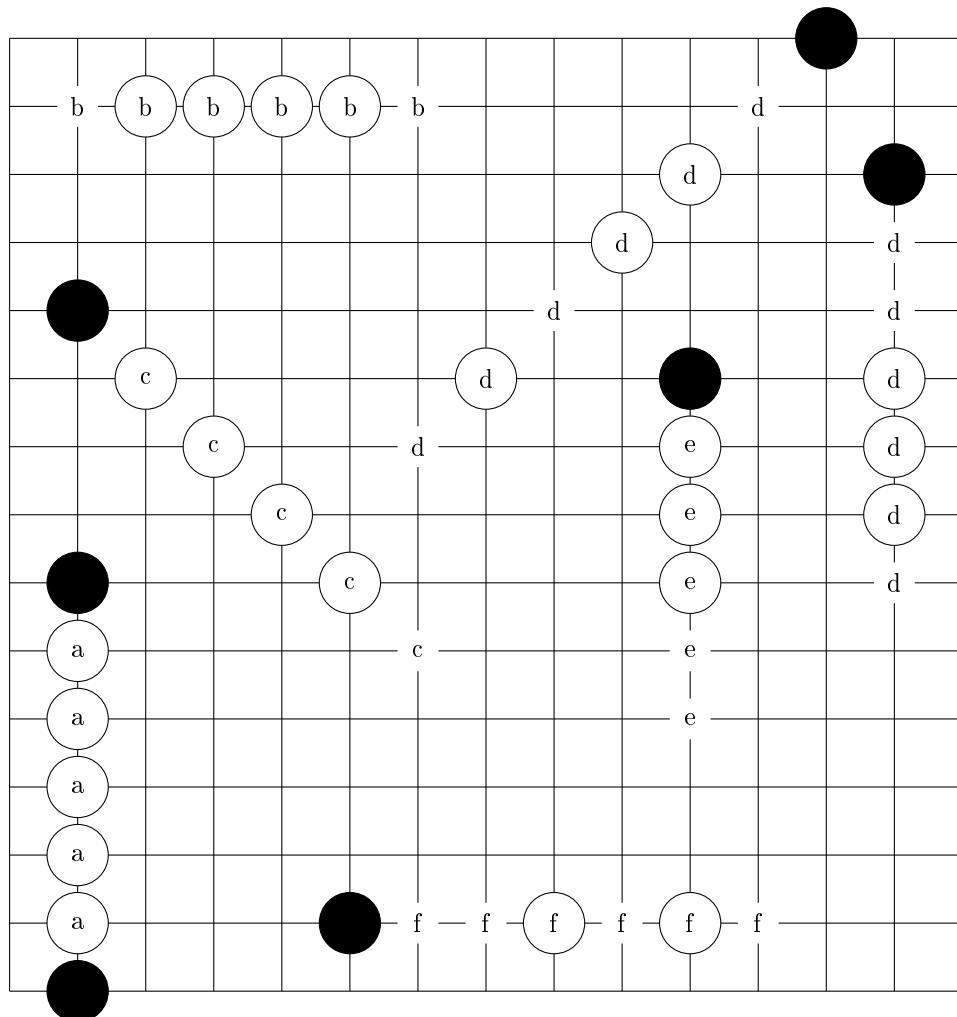


Figure 2.14: The shapes of threats. (a): five, (b): straight four, (c): four, (d): open three, (e): three, (f): open two.

Algorithm 5: Prioritise threats

```

function search(board, depth, color):
    if depth ≤ 0 or find_five(board, color) or find_five(board, opp_color) then
        return eval(board)
    end
    # Play a four if possible
    fours ← find_four(board, color)
    if fours then
        return search(fours[0], depth - 1, opp_color)
    end
    # Block a four if needed
    fours_opp ← find_four(board, opp_color)
    if fours_opp then
        return search(fours_opp[0], depth - 1, opp_color)
    end
    # Play an open three if possible
    open_threes ← find_open_three(board, color)
    if open_threes then
        return search(open_threes[0], depth - 1, opp_color)
    end
    # Refute a open three if needed
    open_threes_opp ← find_open_three(board, opp_color)
    if open_threes_opp then
        # Refute by creating a four
        threes ← find_three(board, color)
        candidate_boards ← open_threes_opp + threes
        return minimax(candidate_boards, depth - 2, opp_color)
    end
    # No more immediate threats, use minimax on remaining threats and non-threats
    threes ← find_three(board, color)
    open_twos ← find_open_two(board, color)
    candidate_boards ← threes + open_twos + get_search_space(board)
    return minimax(candidate_boards, depth - 4, color)
end
# Initial call
d ← 4 * MAX_DEPTH # multiply max depth by 4
search(board, d, color)

```

To update one's ratings, we should first define the sensitivity of the system with a constant called the K-factor K . In this project, I used $K = 32$. Say player A and player B played a game. We define the score of A $S_A = 1$ if player A won, $S_A = 0.5$ if the game has drawn, and $S_A = 0$ if player A lost. We define the same for S_B . We update both players' ratings by the formulae

$$R'_A = R_A + K \times (S_A - E_A)$$

$$R'_B = R_B + K \times (S_B - E_B)$$

According the US Chess Federation (USCF) convention, an average player should have a rating of 1500. We can follow this convention and assign a rating of 1500 to the user and every computer player in the beginning.

2.2.5 Sorting

In minimax, sorting is essential for the use of local evaluation. We need to use sorting to find the best candidate moves for both players, then use alpha-beta allowing pruning of nonoptimal moves. We also need to use sorting when we want to arrange the ratings of computer players in descending order. Therefore, we need a efficient sorting algorithm.

For minimax, I used bubble sort to sort the list of candidate boards. This is because we do not need to sort the whole list, we only need to find the best b boards, where b is the branching factor (which is at most 10). Bubble sort is simple and easy to implement, and it is efficient since it does not have recursion overheads when compared to quicksort or merge sort. The time complexity of bubble sort in this case is $O(nb)$, but since b is a small constant, we can treat it as $O(n)$.

For sorting the ratings of computer players, I used merge sort. Merge sort is a famous sorting algorithm that uses the divide-and-conquer strategy. It has a time complexity of $O(n \log n)$. It is a recursive algorithm, the base case is when the list has only 1 element. In this case, the list is already sorted. Otherwise, it divides the list into two halves, sorts them, and then merges them. It has the the optimal worst-case time complexity among all comparison-based¹ sorting algorithms.

2.2.6 Legality of Renju moves

According to Section 9 of the official Renju rules², a move on an empty intersection is considered illegal if:

- It creates an *overline* (a line of six or more stones).
- Without creating a *five* (directly winning), it creates two *open threes* in two different directions simultaneously, (also called a *3x3 fork*).
- Without creating a *five* (directly winning), it creates two *fours* in two different directions simultaneously, (also called a *4x4 fork*).

Recall that an *open three* is a shape such that the attacker can make a **legal** move and create a *straight four*, and a *four* is a shape such that the attacker can make a **legal** move and create a *five*.

Therefore, the problem of determining the legality of a move is self-referential. We can solve this problem by using a **recursive** algorithm. We can first make the move, then check if the move creates any threes. If it does, we need to play more moves to determine if the three is an open three, and we are solving the same problem when determining whether those new moves are legal. A similar procedure should be done to determine if the move creates a 4x4 fork. The **base case** is when a move does not create two potential threes or fours, and the move is considered legal if it does not create an overline (which does not need to be checked recursively). It is also worth noting that the algorithm **must terminate**, since in each recursive call, we place a new move on the board, and the board is finite.

2.3 Classes

2.3.1 Class relation diagram

Using object-oriented programming, we can organise the code into objects. This makes the code more modular and easier to understand. I would like to use the following classes to organise my code:

- **MainScreen**: The main screen of the game.
- **TitleWindow**: The window where the title is shown.
- **PlayWindow**: The window where the game is played.

¹Comparison-based sorting algorithms are algorithms that only uses a single function for comparison of two elements. An example of a non-comparison based algorithm is counting sort.

²<https://www.renju.net/rifrules/>

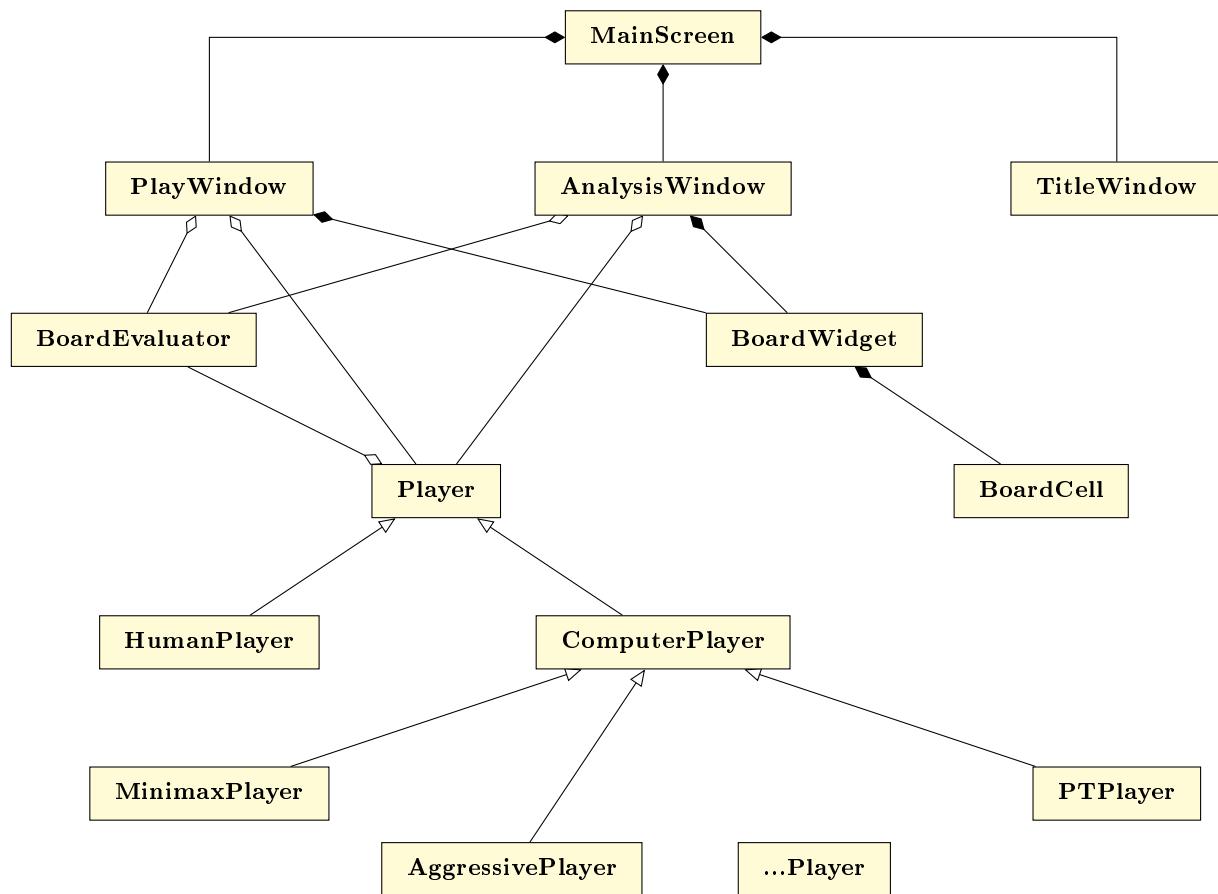


Figure 2.15: The class relation diagram of the system.

- **AnalysisWindow**: The window where the game is analysed.
- **BoardEvaluator**: The class that provides many methods to evaluate the board state.
- **BoardWidget**: The class that manages the GUI of the board.
- **BoardCell**: The class that represents a cell in the board.
- **Player**: The abstract class for a player.
- **HumanPlayer**: The class for a human player.
- **ComputerPlayer**: The abstract class for a computer player.
- **...Player** (e.g. **MinimaxPlayer**): A computer player that uses a certain strategy.

Figure 2.15 shows the relationship between the classes.

2.3.2 Class details

MainScreen

This class is the main screen of the game. It contains title window, the play window, and the analysis window. It also gives public methods to switch between these windows. Its attributes and methods are shown in Figure 2.16.

PlayWindow

This class represents the play window. It contains the board widget. It contains the code to ensure the game is played correctly. It also aggregates the board evaluator and the player (and its subclasses). The board evaluator class is used to determine the legality of a move, and whether the game has ended. The player class is used to represent the two players of the game. If a player is a computer player, its methods are used to make a move. Otherwise, it will wait for the user to make a move. Its attributes and methods are shown in Figure 2.17.

MainScreen
windows : List[QWidget] # current_window : int
+ add_play_window + add_analysis_window + add_title_window

Figure 2.16: The attributes and methods of MainScreen.

PlayWindow
board_widget : BoardWidget # accepting_input : bool # color : int # ended : bool # players : Tuple[bool, bool] # moves : List[Tuple[int, int]] # renju : bool # repeat : int # selected_move_number : int
+ cell_hovered + cell_pressed # next_turn # make_move # update_sidebar # goto_move # end_game # save_game

Figure 2.17: The attributes and methods of PlayWindow.

AnalysisWindow

This class represents the analysis window. Similar to PlayWindow, it also contains the board widget. It contains the code for post-game analysis. It aggregates the board evaluator for the same reason as PlayWindow. The methods of Player will be called when the user asks for a computer player to analyse the board or to give continuation moves. Its attributes and methods are shown in Figure 2.18.

BoardCell

This class represents a cell in the board. It can only be instantiated within BoardWidget. It contains the code to display the cell and to handle the user's input (hover or click). Using the observer pattern, it will notify its parent (BoardWidget) when the user clicks on it. Its parent will then notify the PlayWindow or AnalysisWindow that a cell has been hovered or pressed. Its attributes and methods are shown in Figure 2.19.

ComputerPlayer

This class is the abstract class for a computer player. It is a subclass of Player. It gives an interface for all computer players to implement. For example, computer players need to implement how to make a move. Its attributes and methods are shown in Figure 2.20.

Other classes

The other classes will not be explained in detail, as the usage of these classes are straightforward. The details of these classes can be found in the source code.

- **TitleWindow:** Can only be instantiated by MainScreen.
- **BoardEvaluator:** A utility class that is aggregated by PlayWindow, AnalysisWindow, and Player (in particular, ComputerPlayer).
- **BoardWidget:** Composed of BoardCell, and is a part of PlayWindow and AnalysisWindow.

AnalysisWindow	
# board_widget : BoardWidget	
# computer_player : ComputerPlayer	
# accepting_input : bool	
# override : bool	
# color : int	
# ended : bool	
# selected_move_number : int	
# moves : List[Tuple[int, int]]	
# renju : bool	
# analysing : bool	
+ cell_hovered	
+ cell_pressed	
# next_turn	
# make_move	
# return_to_game	
# update_sidebar	
# get_continuation	
# show_evaluation	
# goto_move	
# end_game	
# save_game	
# load_game	

Figure 2.18: The attributes and methods of AnalysisWindow.

BoardCell	
# row : int	
# col : int	
# pixmaps : List[QPixmap]	
+ state : int	
+ changePixmap	
+ set_selected	
+ set_deselected	

Figure 2.19: The attributes and methods of BoardCell.

ComputerPlayer	
# name : str	
+ get_move	
+ get_continuation	
+ get_evaluation	

Figure 2.20: The attributes and methods of ComputerPlayer.

- **Player:** An abstract class that is inherited by HumanPlayer and ComputerPlayer. All players must have the attribute `name`.

Chapter 3

Technical Solution

3.1 Summary of Complexity

- Bubble sort. `utils.py` line 24.
- Merging and merge sort. `utils.py` lines 45, 70.
- Coordinate conversion and partial sum technique. `board_evaluator.py` lines 72 - 202.
- Checking for legality of moves recursively. `board_evaluator.py` lines 206 - 359.
- Minimax algorithm. `computer_players/minimax_player.py` line 58,
`computer_players/aggressive_player.py` line 66,
`computer_players/defensive_player.py` line 66,
`computer_players/prioritise_threats_player.py` line 133.
- Recursively searching threats. `computer_players/prioritise_threats_player.py` line 56.
- File handling and JSON parsing. `analysis_window.py` line 363, `elo_ratings.py` line 14.

3.2 Constants

```
constants.py
1 DEBUG = False
2 BOARD_SIZE = 15
3
4 # Evaluation function
5 WIN = 10000
6 STRAIGHT_FOUR = 2000
7 OPEN_THREE = 750
8 FOUR = 250
9 THREE = 80
10 TWO = 20
11 ONE = 10
12 AGGRESSIVE_FACTOR = 1.5
13 DEFENSIVE_FACTOR = 1.5
14
15 # Threshold evaluation points for showing messages
16 CLOSE_TO_WINNING_THRES = 2000
17 GREAT_ADVANTAGE_THRES = 1000
18 ADVANTAGE_THRES = 500
19 SMALL_ADVANTAGE_THRES = 200
20
21 # ELO rating
22 K_FACTOR = 32
23 DEFAULT_ELO = 1500
```

3.3 Utilities

This file contains some utility functions that will be used in my code.

`utils.py`

```

1 from typing import List, Tuple, TypeVar, Callable, Iterator
2 from itertools import islice
3
4 from constants import *
5
6 def previous_of(evaluation: int) -> int:
7     """Modifies the evaluation if either player has a forced winning sequence.
8     For example, if black has a forced winning sequence of 5 moves, then the evaluation is 9995.
9     If white has a forced winning sequence of 3 moves, then the evaluation is -9997.
10
11     Args:
12         evaluation (int): The evaluation to be modified.
13
14     Returns:
15         int: The modified evaluation.
16     """
17     if evaluation >= WIN - 100:
18         return evaluation - 1
19     if evaluation <= -WIN + 100:
20         return evaluation + 1
21     return evaluation
22
23 T = TypeVar('T')
24 def bubble_sort_k(l: List[T], k: int, key: Callable[[T], int] = id, reverse: bool = False) -> List[T]:
25     """Sorts the list in increasing order using bubble sort. Time complexity: O(nk).
26
27     Args:
28         l (List[T]): The list to be sorted.
29         key (Callable[[T], int]): The function to extract the key from the elements.
30         k (int): The number of elements to return.
31         reverse (bool): Whether to sort in reverse.
32
33     Returns:
34         List[T]: The first k elements of the sorted list.
35     """
36     n = len(l)
37     keys = [key(board) for board in l]
38     for i in range(min(k, n)):
39         for j in range(n-1, i, -1):
40             if (keys[j-1] > keys[j]) ^ reverse: # XOR
41                 l[j], l[j-1] = l[j-1], l[j]
42                 keys[j], keys[j-1] = keys[j-1], keys[j]
43     return l[:k]
44
45 def merge(l1: List[T], l2: List[T], key: Callable[[T], int], reverse: bool) -> List[T]:
46     """Merges two sorted lists.
47
48     Args:
49         l1 (List[T]): The first sorted list.
50         l2 (List[T]): The second sorted list.
51         key (Callable[[T], int]): The function to extract the key from the elements.
52         reverse (bool): Whether to sort in reverse.
53
54     Returns:
55         List[T]: The merged sorted list.
56     """
57     result = []
58     i = j = 0
59     while i < len(l1) and j < len(l2):
60         if (key(l1[i]) < key(l2[j])) ^ reverse:
61             result.append(l1[i])
62             i += 1
63         else:
64             result.append(l2[j])
65             j += 1
66     result.extend(l1[i:])
67     result.extend(l2[j:])
68     return result
69
70 def merge_sort(l : List[T], key: Callable[[T], int] = id, reverse: bool = False) -> List[T]:

```

```

71     """Sorts the list in increasing order using merge sort.
72
73     Args:
74         l (List[T]): The list to be sorted.
75         key (Callable[[T], int]): The function to extract the key from the elements.
76         reverse (bool, optional): Whether to sort in reverse. Defaults to False.
77
78     Returns:
79         List[T]: The sorted list.
80     """
81     if len(l) <= 1:
82         return l
83     mid = len(l) // 2
84     left = merge_sort(l[:mid], key, reverse)
85     right = merge_sort(l[mid:], key, reverse)
86     return merge(left, right, key, reverse)
87
88 def generate_evaluation_message(evaluation: int) -> str:
89     """Generates a message based on the evaluation.
90
91     Args:
92         evaluation (int): The evaluation of the board.
93
94     Returns:
95         str: The message.
96     """
97     str_color = 'Black' if evaluation > 0 else 'White'
98     evaluation = abs(evaluation)
99     if evaluation >= WIN - 100:
100         return f'{str_color} forced win in {WIN - evaluation} moves ({evaluation})'
101     if evaluation >= CLOSE_TO_WINNING_THRES:
102         return f'{str_color} close to winning ({evaluation})'
103     if evaluation >= GREAT_ADVANTAGE_THRES:
104         return f'{str_color} has a great advantage ({evaluation})',
105     if evaluation >= ADVANTAGE_THRES:
106         return f'{str_color} has an advantage ({evaluation})'
107     if evaluation >= SMALL_ADVANTAGE_THRES:
108         return f'{str_color} has a small advantage ({evaluation})',
109     return f'Game even ({evaluation})'
110
111 def next_k(iterator: Iterator, k: int) -> None:
112     """Advances the iterator by k steps.
113
114     Args:
115         iterator (Iterator): The iterator to be advanced.
116         k (int): The number of steps to advance.
117     """
118     next(islice(iterator, k, k), None)
119
120 if __name__ == '__main__':
121     # Unit tests
122     l = [5, 3, 8, 6, 2, 7, 1, 4]
123     print(bubble_sort_k(l, 5)) # [1, 2, 3, 4, 5]
124     print(bubble_sort_k(l, 5, reverse=True)) # [8, 7, 6, 5, 4]
125     print(merge_sort(l)) # [1, 2, 3, 4, 5, 6, 7, 8]
126     print(merge_sort(l, reverse=True)) # [8, 7, 6, 5, 4, 3, 2, 1]

```

3.4 Main

This file is the file that will be ran.

`main.py`

```

1 import sys
2 from typing import List, Tuple
3
4 from PyQt6.QtWidgets import QApplication, QStackedWidget
5 from PyQt6 import QtCore
6
7 from title_window import TitleWindow
8 from play_window import PlayWindow
9 from analysis_window import AnalysisWindow
10 from rankings_window import RankingsWindow
11 from players import Player, HumanPlayer
12 from constants import DEBUG

```

```

13
14 class MainScreen(QStackedWidget):
15     """The top-level object that contains all other windows.
16
17     Attributes:
18         _windows (List[QWidget]): A list of all the windows in the program.
19
20     Methods:
21         add_play_window: Add a play window to the stack.
22         add_analysis_window: Add an analysis window to the stack.
23         add_rankings_window: Add a rankings window to the stack.
24
25     Overridden Methods:
26         keyPressEvent: Handle key presses.
27     """
28
29     def __init__(self) -> None:
30         super().__init__()
31         self.setWindowTitle("Gomoku and Renju")
32         self.setStyleSheet(open("./stylesheet.css").read())
33
34         self.addWidget>TitleWindow(self))
35
36         self.setCurrentIndex(0)
37
38         self.showMaximized()
39
40     def add_play_window(self, renju: bool, players: List[Player], repeat: int = 1):
41         """Add a play window to the stack. Called by the title window.
42
43         Args:
44             renju (bool): Whether renju rules are enabled.
45             players (List[Player]): The players in the game.
46             repeat (int): The number of games to play.
47     """
48
49         if self.count() != 1: return
50         if all([type(player) is not HumanPlayer for player in players]):
51             print(f'{repeat} match(es) remaining.')
52         self.setWindowTitle(f"Play - {'Renju' if renju else 'Gomoku'}")
53         self.addWidget(PlayWindow(self, renju, players, repeat))
54         self.setCurrentIndex(1)
55
56     def add_analysis_window(self):
57         if self.count() != 1: return
58         self.setWindowTitle("Analysis")
59         self.addWidget(AnalysisWindow(self))
60         self.setCurrentIndex(1)
61
62     def add_rankings_window(self):
63         if self.count() != 1: return
64         self.setWindowTitle("Rankings")
65         self.addWidget(RankingsWindow(self))
66         self.setCurrentIndex(1)
67
68     def remove_window(self):
69         if self.count() != 2: return
70         self.removeWidget(self.currentWidget())
71         self.setCurrentIndex(0)
72         self.setWindowTitle("Gomoku and Renju")
73
74     def keyPressEvent(self, e):
75         if DEBUG and e.key() == QtCore.Qt.Key.Key_Escape:
76             self.close() # closes the current window
77         if e.key() == QtCore.Qt.Key.Key_F11:
78             if self.isMaximized():
79                 self.showNormal()
80             else:
81                 self.showMaximized()
82
83     if __name__ == '__main__':
84         app = QApplication(sys.argv)
85
86         screen = MainScreen()
87         screen.show()
88
89         app.exec_()

```

3.5 TitleWindow

```

title_window.py

1 from __future__ import annotations
2 from copy import deepcopy
3 from typing import TYPE_CHECKING
4 if TYPE_CHECKING:
5     from main import MainScreen
6
7 from PyQt6.QtWidgets import QMainWindow, QDialog
8 from PyQt6 import uic
9
10 from players import HumanPlayer
11 from computer_players.random_player import RandomPlayer, COMPUTER_PLAYERS
12
13 class TitleWindow(QMainWindow):
14     """The window that shows the title screen.
15
16     UI Elements:
17         play_button (QPushButton): The button that opens the configuration menu, then shows the
18             board.
19         analysis_button (QPushButton): The button that opens the analysis window.
20         rankings_button (QPushButton): The button that opens the rankings window.
21     """
22     def __init__(self, parent: MainScreen):
23         """Initialises the TitleWindow.
24
25         Args:
26             parent (MainScreen): The parent MainScreen widget.
27
28         super().__init__()
29         # Some UI files are stored in the ui folder.
30         # They are XML files that describes the properties of the UI elements.
31         # They are created using the application Qt Designer.
32         # Qt Designer is a powerful tool that uses the WYSIWYG (What You See Is What You Get)
33         # approach to create UIs.
34         # It allows me to create the UIs by dragging and dropping UI elements, drastically lowering
35         # the development time.
36
37         # The uic module loads the UI file and creates the UI elements.
38         # For example, here it creates the buttons of the title window, and
39         # allows me to reference the buttons with self.play_button, self.analysis_button, and self.
40         # rankings_button.
41         # In some other classes, their UI files are loaded in the same way,
42         # so you may see me referencing UI elements without defining them.
43         uic.loadUi('ui/title_window.ui', self)
44
45         # Define the behaviour when the buttons are pressed
46         def play_button_pressed():
47             """Called when the play button is pressed. It opens the configuration menu, then shows
48             the board."""
49             configuration_dialog = QDialog(self)
50             uic.loadUi('ui/configuration.ui', configuration_dialog)
51             configuration_dialog.setWindowTitle("Configuration")
52             configuration_dialog.setModal(True)
53
54             # add the players' names to the combo boxes
55             all_players = {player.name: player for player in ([HumanPlayer()] + COMPUTER_PLAYERS)}
56             all_players['Random'] = RandomPlayer()
57             configuration_dialog.black_combo_box.addItems(all_players.keys())
58             configuration_dialog.white_combo_box.addItems(all_players.keys())
59
60             # when both players are computer players, the repeat option is shown
61             def combo_box_changed():
62                 if configuration_dialog.black_combo_box.currentText() == 'Human Player' or \
63                     configuration_dialog.white_combo_box.currentText() == 'Human Player':
64                     configuration_dialog.repeat_option.hide()
65                 else:
66                     configuration_dialog.repeat_option.show()
67             configuration_dialog.black_combo_box.currentIndexChanged.connect(combo_box_changed)
68             configuration_dialog.white_combo_box.currentIndexChanged.connect(combo_box_changed)
69             configuration_dialog.repeat_option.hide()
70
71             def configuration_play_button_pressed():
72                 renju = bool(configuration_dialog.game_combo_box.currentIndex())
73                 # RandomPlayer has a state (the instance), so players must be deepcopied

```

```

69             black_player = deepcopy(all_players[configuration_dialog.black_combo_box.currentText
70         ()])
71             white_player = deepcopy(all_players[configuration_dialog.white_combo_box.currentText
72         ()])
73             repeat = configuration_dialog.repeat_spin_box.value()
74             if type(black_player) == HumanPlayer or type(white_player) == HumanPlayer:
75                 parent.add_play_window(renju, (black_player, white_player))
76             else:
77                 parent.add_play_window(renju, (black_player, white_player), repeat)
78             configuration_dialog.close()
79             configuration_dialog.play_button.pressed.connect(configuration_play_button_pressed)
80
81             configuration_dialog.show()
82             self.play_button.pressed.connect(play_button_pressed)
83
84     def analysis_button_pressed():
85         parent.add_analysis_window()
86         self.analysis_button.pressed.connect(analysis_button_pressed)
87
88     def rankings_button_pressed():
89         parent.add_rankings_window()
90         self.rankings_button.pressed.connect(rankings_button_pressed)

```

3.6 PlayWindow

play_window.py

```

1  from __future__ import annotations
2  from typing import TYPE_CHECKING, Tuple, List
3  if TYPE_CHECKING:
4      from main import MainScreen
5  from datetime import datetime
6  import json
7
8  from PyQt6.QtWidgets import QMainWindow, QPushButton, QLabel, QDialog
9  from PyQt6.QtCore import Qt, QThreadPool
10 from PyQt6 import uic
11
12 from players import Player, HumanPlayer
13 from computer_players.random_player import RandomPlayer
14 from board_widget import BoardWidget
15 from board_evaluator import BoardEvaluator
16 from worker import Worker
17 from elo_ratings import EloRatings
18 from constants import DEBUG
19
20 class PlayWindow(QMainWindow):
21     """The window where the game is played.
22
23     UI Elements:
24         board_widget_placeholder (QWidget): The placeholder for the board widget.
25         bottom_text (QLabel): The label that shows the bottom text.
26         status_bar (QStatusBar): The status bar that shows the game status.
27         return_to_game_button (QPushButton): The button that returns to the latest move.
28         exit_button (QPushButton): The button that exits the game.
29         save_action (QAction): The action that saves the game.
30         black_player_name (QLabel): The label that shows the name of the black player.
31         white_player_name (QLabel): The label that shows the name of the white player.
32         sidebar (QWidget): The widget that shows the sidebar.
33
34     Attributes:
35         _board_widget (BoardWidget): The widget that displays the board.
36         _accepting_input (bool): Whether the player can make a move.
37         _color (int): The color of the player whose turn it is. 1 for black, 2 for white.
38         _ended (bool): Whether the game has ended.
39         _players (Tuple[bool, bool]): A tuple of two booleans, indicating whether each player is a
40             player.
41         _moves (List[Tuple[int, int]]): A list of the moves made in the game.
42         _renju (bool): Whether renju rules are enabled.
43         _repeat (int): The number of games to play.
44         _selected_move_number (int): The move number that is currently selected.
45
46     Methods:
47         cell_hovered: Called when a cell of board_widget is hovered over.
48         cell_pressed: Called when a cell of board_widget is pressed.

```

```

48     _show_message: Shows a message in the status bar.
49     _make_move: Makes a move on the board.
50     _next_turn: Changes the turn.
51     _update_sidebar: Updates the sidebar with the move that was made.
52     _goto_move: Goes to a move in the game.
53     _end_game: Called when the game ends.
54     _save_game: Saves the game to a file.
55
56     """
57     def __init__(self, parent: MainScreen, renju: bool, players: Tuple[Player, Player], repeat: int
58     = 1):
59         """Initialises the PlayWindow.
60
61         Args:
62             parent (MainScreen): The parent MainScreen widget.
63             renju (bool): Whether renju rules are enabled.
64             players (Tuple[Player, Player]): The players in the game.
65             repeat (int): The number of games to play.
66
67         super().__init__()
68         self.parent = parent
69
70         # Initialise GUI elements
71         uic.loadUi('ui/play_window.ui', self)
72
73         self.board_widget = BoardWidget()
74         self.left_layout.replaceWidget(self.board_widget_placeholder, self.board_widget)
75
76         def return_to_game_pressed():
77             move_number = len(self._moves) - 1
78             if move_number < 0:
79                 return
80             self.sidebar.layout().itemAtPosition(move_number // 2 + 1, move_number % 2 + 1).widget()
81             .setChecked(True)
82             self._goto_move(move_number)
83             self.return_to_game_button.pressed.connect(return_to_game_pressed)
84
85             self.exit_button.pressed.connect(parent.remove_window)
86
87             self.save_action.triggered.connect(self._save_game)
88
89             for player in players:
90                 if type(player) is RandomPlayer:
91                     player.__init__() # reroll random player
92             self.black_player_name.setText(players[0].name)
93             self.white_player_name.setText(players[1].name)
94
95             # Initialise PlayWindow attributes
96             self._selected_move_number = -1
97             self._threadpool = QThreadPool()
98             self._accepting_input = True
99             self._color = 2
100            self._ended = False
101            self._players = players
102            self._moves = []
103            self._renju = renju
104            self._repeat = repeat
105            self._next_turn()
106
107        def cell_hovered(self, row: int, col: int):
108            """Called when a cell is hovered over. It updates the bottom text.
109
110            Args:
111                row (int): The row of the cell.
112                col (int): The column of the cell.
113
114                text = f'{chr(row + ord('A'))}{col+1}'
115                if DEBUG:
116                    text += f'({row}, {col})'
117                self.bottom_text.setText(text)
118                board_cell = self.board_widget.board_cells[row][col]
119                if not self._ended and self._accepting_input and board_cell.state == 0:
120                    board_cell.change_pixmap(self._color + 2)
121
122        def cell_pressed(self, row: int, col: int):
123            """Called when a cell is pressed. It makes a move if it is legal.

```

```

122
123     Args:
124         row (int): The row of the cell.
125         col (int): The column of the cell.
126     """
127     if self._ended or not self._accepting_input:
128         return
129     self.status_bar.clearMessage()
130     if self.board_widget.board[row][col] != 0:
131         return
132     # place the piece in a board evaluator to check if it is legal
133     board_evaluator = BoardEvaluator(self.board_widget.board, self._color, row, col, self._renju)
134 )
135     legal, open_three, four, five, overline = board_evaluator.is_legal_detailed()
136     if not legal:
137         if overline:
138             self._show_message("Illegal, it is an overline.")
139         elif open_three >= 2:
140             self._show_message("Illegal, it is a 3x3 fork.")
141         elif four >= 2:
142             self._show_message("Illegal, it is a 4x4 fork.")
143         else: # should be unreachable
144             self._show_message("Unknown illegal move.")
145     return
146     self._make_move((row, col))
147
148 def _show_message(self, message: str):
149     """Shows a message in the status bar.
150
151     Args:
152         message (str): The message to be shown.
153     """
154     self.status_bar.showMessage(message)
155     print(message)
156
157 def _make_move(self, pos: Tuple[int, int]):
158     """Makes a move on the board.
159
160     Args:
161         pos (Tuple[int, int]): The position of the move.
162     """
163     self.return_to_game_button.pressed.emit() # The game should be returned to the latest move
before making a new move.
164     row, col = pos
165     self.board_widget.make_move(row, col, self._color)
166     self._moves.append((row, col))
167     self._update_sidebar(row, col)
168     self.return_to_game_button.pressed.emit() # Goes to the newly placed move
169     # place the piece in a board evaluator to check if the game has ended
170     board_evaluator = BoardEvaluator(self.board_widget.board, self._color, renju=self._renju)
171     if board_evaluator.find_five(self._color) or board_evaluator.is_full():
172         self._end_game(draw=board_evaluator.is_full())
173     return
174     self._next_turn()
175
176 def _next_turn(self):
177     """Changes the turn. It tells a computer to make a move if it is its turn."""
178     self._color = 3 - self._color
179     current_player = self._players[self._color - 1]
180     if type(current_player) is HumanPlayer:
181         self._accepting_input = True
182     else: # Current player is a computer player
183         self._accepting_input = False
184     worker = Worker(current_player.get_move,
185                     self.board_widget.board, self._color, self._renju)
186     worker.signals.result.connect(self._make_move)
187     self._threadpool.start(worker)
188
189 def _update_sidebar(self, row: int, col: int):
190     """Updates the sidebar with the move that was made.
191
192     Args:
193         row (int): The row of the move.
194         col (int): The column of the move.
195     """
196     cur_move_number = len(self._moves) - 1

```

```

196     # add a button that when pressed, goes to this move
197     button = QPushButton(f"{chr(row + ord('A'))}{col+1}")
198     button.pressed.connect(lambda: self._goto_move(cur_move_number))
199     button.setCheckable(True)
200     self.sidebar.layout().addWidget(button, cur_move_number // 2 + 1, self._color)
201     if self._color == 1:
202         # add a new row if the move is from black
203         label = QLabel(f"{cur_move_number // 2 + 1}.")
204         self.sidebar.layout().addWidget(label, cur_move_number // 2 + 1, 0)
205
206     def _goto_move(self, move_number: int):
207         """Goes to a move in the game. Called when a move is clicked in the sidebar.
208
209         Args:
210             move_number (int): The move number to go to.
211         """
212         if self._selected_move_number == move_number:
213             return
214         # accept input according to the move pressed
215         if move_number < len(self._moves) - 1 or type(self._players[self._color-1]) is not
216             HumanPlayer:
217                 self._accepting_input = False
218             else:
219                 self._accepting_input = True
220             if self._selected_move_number >= 0:
221                 self.sidebar.layout().itemAtPosition(self._selected_move_number // 2 + 1, self._selected_move_number % 2 + 1).widget().setChecked(False)
222             self._selected_move_number = move_number
223             self.board_widget.reset()
224             # reset the board and make the moves up to the selected move
225             for i in range(move_number + 1):
226                 row, col = self._moves[i]
227                 self.board_widget.make_move(row, col, 1 + i % 2)
228                 if i == move_number:
229                     self.board_widget.board_cells[row][col].set_selected()
230
231     def _end_game(self, draw: bool = False):
232         """Ends the game and updates the rankings. Repeats the game if there are more games to play.
233
234         If DEBUG:
235             for i, move in enumerate(self._moves):
236                 print(move, end=' ' if i % 2 == 0 else '\n')
237             print()
238         self._ended = True
239         if not draw:
240             str_color = "Black" if self._color == 1 else "White"
241             self._show_message(f"{str_color} wins with a five in a row.")
242         else:
243             self._show_message("The game is a draw.")
244
245         EloRatings().update(
246             winner = self._players[self._color - 1].name,
247             loser = self._players[2 - self._color].name,
248             draw = draw
249         )
250         if self._repeat > 1:
251             if DEBUG:
252                 print(f"{self._repeat - 1} matches remaining.")
253                 # remove self and add a new play window, with one less repeat
254                 self.parent.removeWidget(self)
255                 self.parent.add_play_window(self._renju, self._players, self._repeat - 1)
256
257     def _save_game(self):
258         """Saves the game to a file. Called when save game in the menu bar or Ctrl+S is pressed."""
259         save_game_dialog = QDialog(self)
260         uic.loadUi('ui/save_game.ui', save_game_dialog)
261         save_game_dialog.setWindowTitle("Save Game")
262         save_game_dialog.black_player_name.setText(self._players[0].name)
263         save_game_dialog.white_player_name.setText(self._players[1].name)
264         def save_pressed():
265             # retrieve information from the input and save the game to a json file
266             black_player_name = save_game_dialog.black_player_name.text()
267             white_player_name = save_game_dialog.white_player_name.text()
268             current_time = datetime.now().strftime('%Y%m%d')
269             file_name = f'{current_time}_{black_player_name}_vs_{white_player_name}',
```

```

269         file_content = {
270             'black_player_name': black_player_name,
271             'white_player_name': white_player_name,
272             'moves': self._moves,
273             'ended': self._ended,
274             'win': self._color if self._ended else 0,
275         }
276         json.dump(file_content, open(f'games/{file_name}.json', 'w'))
277         save_game_dialog.close()
278         save_game_dialog.save_button.pressed.connect(save_pressed)
279         save_game_dialog.show()

```

3.7 AnalysisWindow

`analysis_window.py`

```

1  from __future__ import annotations
2  from typing import TYPE_CHECKING, Tuple, List
3  if TYPE_CHECKING:
4      from main import MainScreen
5  from datetime import datetime
6  import json
7
8  from PyQt6 import uic
9  from PyQt6.QtWidgets import QMainWindow, QFileDialog, QDialog, QPushButton, QLabel
10 from PyQt6.QtCore import Qt, QThreadPool
11
12 from board_widget import BoardWidget
13 from board_evaluator import BoardEvaluator
14 from worker import Worker
15 from constants import DEBUG
16 from computer_players.random_player import COMPUTER_PLAYERS
17 from utils import generate_evaluation_message
18
19 class AnalysisWindow(QMainWindow):
20     """The window where the game is analysed.
21
22     UI Elements:
23         board_widget_placeholder (QWidget): The placeholder for the board widget.
24         black_button (QPushButton): The button that lets the user override the color of a cell to
25             black.
26         white_button (QPushButton): The button that lets the user override the color of a cell to
27             white.
28         black_white_button (QPushButton): The button that lets the user play normally with black and
29             white alternating.
30         evaluation_button (QPushButton): The button that shows the evaluation of the current board.
31         continuation_button (QPushButton): The button that shows the best continuation of the game.
32         return_to_game_button (QPushButton): The button that returns to the latest move.
33         game_combo_box (QComboBox): The combo box that selects the ruleset of the game.
34         comp_combo_box (QComboBox): The combo box that selects the computer player.
35         exit_button (QPushButton): The button that exits the window.
36         status_bar (QStatusBar): The status bar that shows messages.
37         bottom_text (QLabel): The label that shows the position of the cursor.
38         sidebar (QWidget): The widget that shows the moves made in the game.
39         black_player_name (QLabel): The label that shows the name of the black player.
40         white_player_name (QLabel): The label that shows the name of the white player.
41         analysis_text (QLabel): The label that shows the analysis mode.
42
43     Attributes:
44         _board_widget (BoardWidget): The widget that displays the board.
45         _computer_player (ComputerPlayer): The computer player selected.
46         _accepting_input (bool): Whether the player can make a move.
47         _override (bool): Whether the player can override the color of a cell.
48         _color (int): The color of the player whose turn it is. 1 for black, 2 for white.
49         _ended (bool): Whether the game has ended.
50         _selected_move_number (int): The move number that is currently selected.
51         _moves (List[Tuple[int, int]]): A list of the moves made in the game.
52         _renju (bool): Whether renju rules are enabled.
53         _analysing (bool): Whether the game is being analysed.
54
55     Methods:
56         cell_hovered: Called when a cell of board_widget is hovered over.
57         cell_pressed: Called when a cell of board_widget is pressed.
58         _show_message: Shows a message in the status bar.
59         _return_to_game: Returns to the latest move.

```

```

57     _reset: Resets itself.
58     _make_move: Makes a move on the board.
59     _update_sidebar: Updates the sidebar with the move that was made.
60     _goto_move: Goes to a move in the game.
61     _get_continuation: Gets the best continuation of the game determined by the selected computer
62     player.
63     _show_evaluation: Shows the evaluation of the current board determined by the selected
64     computer player.
65     _end_game: Called when the game ends.
66     _save_game: Saves the game to a file.
67     _load_game: Loads a game from a file.
68     """
69
70     def __init__(self, parent: MainScreen):
71         """Initialises the PlayWindow.
72
73         Args:
74             parent (MainScreen): The parent MainScreen widget.
75         """
76         super().__init__()
77
78         # Initialise GUI elements
79         uic.loadUi('ui/analysis_window.ui', self)
80
81         self.board_widget = BoardWidget()
82         self.left_layout.replaceWidget(self.board_widget_placeholder, self.board_widget)
83
84         self.save_action.triggered.connect(self._save_game)
85         self.load_action.triggered.connect(self._load_game)
86
87         self.exit_button.pressed.connect(parent.remove_window)
88
89         def black_pressed():
90             self._accepting_input = True
91             self._override = True
92             self.analysing = True
93             self._color = 1
94             self.black_button.pressed.connect(black_pressed)
95
96         def white_pressed():
97             self._accepting_input = True
98             self._override = True
99             self.analysing = True
100            self._color = 2
101            self.white_button.pressed.connect(white_pressed)
102
103         def black_white_pressed():
104             self._override = False
105             if self._ended:
106                 self._accepting_input = False
107             else:
108                 self._accepting_input = True
109             self.black_white_button.pressed.connect(black_white_pressed)
110
111             self.evaluation_button.pressed.connect(self._show_evaluation)
112
113             self.continuation_button.pressed.connect(self._get_continuation)
114
115             self._renju = False
116             def game_combo_box_changed(index):
117                 self._renju = index == 1
118                 self.status_bar.clearMessage()
119                 self.game_combo_box.currentIndexChanged.connect(game_combo_box_changed)
120
121                 self.comp_combo_box.addItems([player.name for player in COMPUTER_PLAYERS])
122                 self.comp_combo_box.setCurrentIndex(10)
123                 def change_comp_player(index):
124                     self._computer_player = COMPUTER_PLAYERS[index]
125                     self.comp_combo_box.currentIndexChanged.connect(change_comp_player)
126
127                 # Initialise AnalysisWindow attributes
128                 self._computer_player = COMPUTER_PLAYERS[10]
129                 self._threadpool = QThreadPool()
130                 self._accepting_input = True
131                 self._override = False

```

```

131     self._color = 1
132     self._ended = False
133     self._selected_move_number = -1
134     self._moves = []
135     self._analysing = False
136     self.analysis_text.hide()
137     self._player_names = ("Black", "White")
138
139     @property
140     def analysing(self):
141         return self._analysing
142
143     @analysing.setter
144     def analysing(self, b):
145         if b:
146             self.analysis_text.show()
147         else:
148             self.analysis_text.hide()
149         self._analysing = b
150
151     def cell_hovered(self, row: int, col: int):
152         """Called when a cell is hovered over. It updates the bottom text.
153
154         Args:
155             row (int): The row of the cell.
156             col (int): The column of the cell.
157         """
158         bottom_text = f"{chr(row + ord('A'))}{col+1}"
159         if DEBUG:
160             bottom_text += f"({row}, {col})"
161         self.bottom_text.setText(bottom_text)
162         board_cell = self.board_widget.board_cells[row][col]
163         if self._accepting_input and board_cell.state == 0:
164             board_cell.changePixmap(self._color + 2)
165
166     def cell_pressed(self, row, col):
167         """Called when a cell is pressed. It makes a move if it is legal.
168
169         Args:
170             row (int): The row of the cell.
171             col (int): The column of the cell.
172         """
173         if not self._accepting_input:
174             return
175         self.status_bar.clearMessage()
176         if self._override:
177             # if the cell is already the color of the player, remove it
178             # otherwise, change it to a cell of the selected color
179             if self.board_widget.board[row][col] == self._color:
180                 self.board_widget.make_move(row, col, 0)
181             else:
182                 self.board_widget.make_move(row, col, self._color)
183             return
184         if self.board_widget.board[row][col] != 0:
185             return
186         # place the piece in a board evaluator to check if it is legal
187         board_evaluator = BoardEvaluator(self.board_widget.board, self._color, row, col, self._renju)
188     )
189     legal, open_three, four, five, overline = board_evaluator.is_legal_detailed()
190     if not legal:
191         if overline:
192             self._show_message("Illegal, it is an overline.")
193         elif open_three >= 2:
194             self._show_message("Illegal, it is a 3x3 fork.")
195         elif four >= 2:
196             self._show_message("Illegal, it is a 4x4 fork.")
197         else: # should be unreachable
198             self._show_message("Unknown illegal move.")
199         return
200     self._make_move((row, col))
201
202     def _show_message(self, message: str):
203         """Shows a message in the status bar.
204
205         Args:
206             message (str): The message to be shown.

```

```

206
207     self.status_bar.showMessage(message)
208     print(message)
209
210     def _return_to_game(self):
211         move_number = len(self._moves) - 1
212         if move_number >= 0:
213             self.sidebar.layout().itemAtPosition(move_number // 2 + 1, move_number % 2 + 1).widget()
214             .setChecked(True)
215             self._goto_move(move_number)
216
217     def _reset(self):
218         """Resets the AnalysisWindow."""
219         self._accepting_input = True
220         self._override = False
221         self._color = 1
222         self._ended = False
223         self._selected_move_number = -1
224         self._moves = []
225         self._analysing = False
226         self.analysis_text.hide()
227         self.board_widget.reset()
228         for i in reversed(range(3, self.sidebar.layout().count())):
229             self.sidebar.layout().itemAt(i).widget().deleteLater()
230
231     def _make_move(self, pos: Tuple[int, int]):
232         """Makes a move on the board.
233
234         Args:
235             pos (Tuple[int, int]): The position of the move.
236         """
237         self.status_bar.clearMessage()
238         row, col = pos
239         self.board_widget.make_move(row, col, self._color)
240         if not self.analysing:
241             self._moves.append((row, col))
242             self._update_sidebar(row, col)
243             # check if the game has ended
244             board_evaluator = BoardEvaluator(self.board_widget.board, self._color, renju=self._renju)
245             if (win := board_evaluator.find_five(self._color)) or board_evaluator.is_full():
246                 str_color = "Black" if self._color == 1 else "White"
247                 if not self.analysing: # this block is placed before show message, because this calling
248                     return to game clears message
249                     self._return_to_game() # go to the newly placed move
250                     if win:
251                         self._show_message(f"{str_color} wins with a five in a row.")
252                     else:
253                         self._show_message("The game is a draw.")
254                     if not self.analysing:
255                         self._end_game()
256                     return
257                     # if the game has not ended, change the turn
258                     if not self.analysing:
259                         self._return_to_game() # go to the newly placed move (which changes the turn)
260                     else:
261                         self._color = 3 - self._color
262
263     def _update_sidebar(self, row: int, col: int):
264         """Updates the sidebar with the move that was made.
265
266         Args:
267             row (int): The row of the move.
268             col (int): The column of the move.
269         """
270         cur_move_number = len(self._moves) - 1
271         # add a button that when pressed, goes to this move
272         button = QPushButton(f"chr({row + ord('A')}){col+1}")
273         button.pressed.connect(lambda: self._goto_move(cur_move_number))
274         button.setCheckable(True)
275         self.sidebar.layout().addWidget(button, cur_move_number // 2 + 1, self._color)
276         if self._color == 1:
277             # add a new row if the move is from black
278             label = QLabel(f'{cur_move_number // 2 + 1}.')
279             self.sidebar.layout().addWidget(label, cur_move_number // 2 + 1, 0)
280
281     def _goto_move(self, move_number: int):

```

```

280     """Goes to a move in the game. Called when a move is selected in the sidebar.
281
282     Args:
283         move_number (int): The move number to go to.
284     """
285
286     self.status_bar.clearMessage()
287     self._override = False
288     if self._selected_move_number >= 0:
289         self.sidebar.layout().itemAtPosition(self._selected_move_number // 2 + 1, self.
290     _selected_move_number % 2 + 1).widget().setChecked(False)
291     self._selected_move_number = move_number
292     self._color = (move_number+1) % 2 + 1
293     # turn on analysis mode if the move is not the last move and vice versa
294     if move_number == len(self._moves) - 1:
295         self.analysing = False
296     if self._ended:
297         self._accepting_input = False
298     else:
299         self._accepting_input = True
300         self.analysing = True
301     # reset the board and make the moves up to the selected move
302     self.board_widget.reset()
303     for i in range(move_number + 1):
304         row, col = self._moves[i]
305         self.board_widget.make_move(row, col, 1 + i % 2)
306         if i == move_number:
307             self.board_widget.board_cells[row][col].set_selected()
308
309     def _get_continuation(self):
310         """Gets the best continuation of the game determined by the selected computer player."""
311         self._show_message(f"{self._computer_player.name} is thinking...")
312         worker = Worker(self._computer_player.get_continuation, # use polymorphism to get the
313                         continuation
314                         self.board_widget.board, self._color, self._renju)
315         def show_continuation(moves: List[Tuple[int, int]]):
316             s = ', '.join([f'{chr(move[0] + ord('A'))}{move[1]+1}' for move in moves])
317             self._show_message(f'Continuation: {s}')
318         worker.signals.result.connect(show_continuation) # when worker finishes, show the
319         continuation
320         self._threadpool.start(worker)
321
322     def _show_evaluation(self):
323         """Shows the evaluation of the current board."""
324         self._show_message(f"{self._computer_player.name} is thinking...")
325         worker = Worker(self._computer_player.get_evaluation, # use polymorphism to get the
326                         evaluation
327                         self.board_widget.board, self._color, self._renju)
328         worker.signals.result.connect(
329             lambda x: self._show_message(generate_evaluation_message(x))) # when worker finishes,
330         show the evaluation
331         self._threadpool.start(worker)
332
333     def _end_game(self):
334         """Ends the game."""
335         self._ended = True
336         self._accepting_input = False
337         # for i, move in enumerate(self.moves):
338         #     print(move, end=' ' if i % 2 == 0 else '\n')
339         # print()
340
341     def _save_game(self):
342         save_game_dialog = QDialog(self)
343         uic.loadUi('ui/save_game.ui', save_game_dialog)
344         save_game_dialog.setWindowTitle("Save Game")
345         save_game_dialog.setModal(True)
346         save_game_dialog.black_player_name.setText(self._player_names[0])
347         save_game_dialog.white_player_name.setText(self._player_names[1])
348
349     def save_pressed():
350         # retrieve information from the input and save the game to a json file
351         black_player_name = save_game_dialog.black_player_name.text()
352         white_player_name = save_game_dialog.white_player_name.text()
353         current_time = datetime.now().strftime('%Y%m%d')
354         file_name = f'{current_time}_{black_player_name}_vs_{white_player_name}'
355         file_content = {
356             'black_player_name': black_player_name,

```

```

351         'white_player_name': white_player_name,
352         'moves': self._moves,
353         'ended': self._ended,
354         'win': self._color if self._ended else 0,
355     }
356     with open(f'games/{file_name}.json', 'w') as file:
357         file.write(json.dumps(file_content))
358     save_game_dialog.close()
359     save_game_dialog.save_button.pressed.connect(save_pressed)
360
361     save_game_dialog.show()
362
363 def _load_game(self):
364     # show file dialog and wait for the user to choose a file
365     filename = QFileDialog.getOpenFileName(
366         self,
367         "Load Game",
368         "./games",
369         "JSON Files (*.json)",
370     )[0]
371     if not filename: # load game was cancelled
372         return
373     game_content = json.load(open(filename, 'r'))
374     try:
375         # load in the game content
376         self._player_names = (game_content['black_player_name'], game_content['white_player_name'],
377     ,))
378         self._reset()
379         self.black_player_name.setText(self._player_names[0])
380         self.white_player_name.setText(self._player_names[1])
381         self._ended = game_content['ended']
382         for move in game_content['moves']:
383             self._make_move((move[0], move[1]))
384     except KeyError:
385         # the file is not a valid game file
386         self._show_message("Invalid game file.")
387     return
388 except Exception as e:
389     self._show_message(f"Unexpected error while loading file.")
390     print(e)
391     return

```

3.8 BoardWidget

board_widget.py

```

1 from typing import List
2 from PyQt6.QtWidgets import *
3 from PyQt6.QtCore import *
4
5 from board_cell import BoardCell
6 from constants import BOARD_SIZE
7
8 class BoardWidget(QWidget):
9     """The widget that displays the board.
10
11     Attributes:
12         board_cells (List[List[BoardCell]]): A list of the cells in the board.
13         board (List[List[int]]): A list of the colors of the cells in the board. 0 for empty, 1 for
14         black, 2 for white.
15
16     Methods:
17         make_move: Makes a move on the board.
18         reset: Resets the board.
19
20     """
21     def __init__(self):
22         """Initialises the BoardWidget."""
23         super().__init__()
24
25         self.board_cells: List[List[BoardCell]] = [[None for _ in range(BOARD_SIZE)] for _ in range(
26             BOARD_SIZE)]
27         self.board = [[0 for _ in range(BOARD_SIZE)] for _ in range(BOARD_SIZE)]
28
29         # add corners
30         self.board_cells[0][0] = BoardCell(0, 0, 2, 0)

```

```

28         self.board_cells[0][BOARD_SIZE - 1] = BoardCell(0, BOARD_SIZE - 1, 2, 1)
29         self.board_cells[BOARD_SIZE - 1][BOARD_SIZE - 1] = BoardCell(BOARD_SIZE - 1, BOARD_SIZE - 1,
30         2, 2)
31         self.board_cells[BOARD_SIZE - 1][0] = BoardCell(BOARD_SIZE - 1, 0, 2, 3)
32
33     # add edges
34     for i in range(1, BOARD_SIZE - 1):
35         self.board_cells[0][i] = BoardCell(0, i, 1, 0)
36     for i in range(1, BOARD_SIZE - 1):
37         self.board_cells[i][BOARD_SIZE -
38             1] = BoardCell(i, BOARD_SIZE - 1, 1, 1)
39     for i in range(1, BOARD_SIZE - 1):
40         self.board_cells[BOARD_SIZE -
41             1][i] = BoardCell(BOARD_SIZE - 1, i, 1, 2)
42     for i in range(1, BOARD_SIZE - 1):
43         self.board_cells[i][0] = BoardCell(i, 0, 1, 3)
44
45     # add centres
46     for i in range(1, BOARD_SIZE - 1):
47         for j in range(1, BOARD_SIZE - 1):
48             self.board_cells[i][j] = BoardCell(i, j, 0, 0)
49
50     board_layout = QGridLayout(self)
51     # add the cells in board_cells to layout
52     for i in range(BOARD_SIZE):
53         for j in range(BOARD_SIZE):
54             board_layout.addWidget(self.board_cells[i][j], i+1, j+1)
55
56     board_layout.setSpacing(0)
57     board_layout.setRowStretch(0, 1)
58     board_layout.setRowStretch(BOARD_SIZE + 1, 1)
59     board_layout.setColumnStretch(0, 1)
60     board_layout.setColumnStretch(BOARD_SIZE + 1, 1)
61
62     def make_move(self, row: int, col: int, color: int):
63         """Makes a move on the board.
64
65         Args:
66             row (int): The row of the move.
67             col (int): The column of the move.
68             color (int): The color of the move. 1 for black, 2 for white.
69
70         self.board[row][col] = color
71         self.board_cells[row][col].change_pixmap(color)
72
73     def reset(self):
74         """Resets the board."""
75         for i in range(BOARD_SIZE):
76             for j in range(BOARD_SIZE):
77                 self.board[i][j] = 0
78                 self.board_cells[i][j].change_pixmap(0)

```

3.9 BoardCell

```

board_cell.py

1 from PyQt6.QtWidgets import QLabel
2 from PyQt6.QtGui import QPixmap, QTransform
3 from PyQt6.QtCore import Qt
4
5 class BoardCell(QLabel):
6     """A cell in the board.
7
8     Attributes:
9         _row (int): The row of the cell.
10        _col (int): The column of the cell.
11        _pixmaps (List[QPixmap]): A list of the pixel maps of the cell.
12        state (int): The current index of the pixel map shown.
13
14     Overridden Methods:
15        enterEvent: Called when the mouse enters the cell.
16        leaveEvent: Called when the mouse leaves the cell.
17        mousePressEvent: Called when the cell is pressed.
18
19     Methods:

```

```

20     change_pixmap: Changes the pixmap of the cell.
21     set_selected: Sets the cell as selected.
22     set_deselected: Sets the cell as deselected.
23 """
24 def __init__(self, row: int, col: int, cell_type: int, rotation: int):
25     """Initialises the BoardCell.
26
27     Args:
28         row (int): The row of the cell.
29         col (int): The column of the cell.
30         cell_type (int): The type of the cell. 0 for centre, 1 for edge, 2 for corner.
31         rotation (int): The rotation of the cell. 0 for 0 degrees, 1 for 90 degrees, 2 for 180
32         degrees, 3 for 270 degrees.
33     """
34     super().__init__()
35
36     self._row = row
37     self._col = col
38     self._pixmaps = [None] * 7
39
40     if cell_type == 0:
41         self._pixmaps[0] = QPixmap("assets/centre.png")
42         self._pixmaps[1] = QPixmap("assets/centre_black.png")
43         self._pixmaps[2] = QPixmap("assets/centre_white.png")
44         self._pixmaps[3] = QPixmap("assets/centre_black_alpha.png")
45         self._pixmaps[4] = QPixmap("assets/centre_white_alpha.png")
46         self._pixmaps[5] = QPixmap("assets/centre_black_selected.png")
47         self._pixmaps[6] = QPixmap("assets/centre_white_selected.png")
48     elif cell_type == 1:
49         self._pixmaps[0] = QPixmap("assets/edge.png")
50         self._pixmaps[1] = QPixmap("assets/edge_black.png")
51         self._pixmaps[2] = QPixmap("assets/edge_white.png")
52         self._pixmaps[3] = QPixmap("assets/edge_black_alpha.png")
53         self._pixmaps[4] = QPixmap("assets/edge_white_alpha.png")
54         self._pixmaps[5] = QPixmap("assets/edge_black_selected.png")
55         self._pixmaps[6] = QPixmap("assets/edge_white_selected.png")
56     elif cell_type == 2:
57         self._pixmaps[0] = QPixmap("assets/corner.png")
58         self._pixmaps[1] = QPixmap("assets/corner_black.png")
59         self._pixmaps[2] = QPixmap("assets/corner_white.png")
60         self._pixmaps[3] = QPixmap("assets/corner_black_alpha.png")
61         self._pixmaps[4] = QPixmap("assets/corner_white_alpha.png")
62         self._pixmaps[5] = QPixmap("assets/corner_black_selected.png")
63         self._pixmaps[6] = QPixmap("assets/corner_white_selected.png")
64
65     for i in range(7):
66         self._pixmaps[i] = self._pixmaps[i].transformed(QTransform().rotate(rotation*90))
67         self._pixmaps[i] = self._pixmaps[i].scaled(42, 42, Qt.AspectRatioMode.KeepAspectRatio)
68
69     self.state = 0
70     self.setPixmap(self._pixmaps[self.state])
71
72     def enterEvent(self, ev) -> None:
73         """Called when the mouse enters the cell. It calls the cell_hovered method of the current
74         window."""
75         self.window().currentWidget().cell_hovered(self._row, self._col)
76
77     def leaveEvent(self, ev) -> None:
78         """Called when the mouse leaves the cell. It changes the pixmap from a ghost piece to an
79         empty cell."""
80         if self.state == 3 or self.state == 4:
81             self.change_pixmap(0)
82
83     def mousePressEvent(self, ev) -> None:
84         """Called when the cell is pressed. It calls the cell_pressed method of the current window.
85         """
86         self.window().currentWidget().cell_pressed(self._row, self._col)
87
88     def change_pixmap(self, index: int):
89         """Changes the pixmap of the cell.
90
91         Args:
92             index (int): The index of the pixmap to change to.
93         """
94         self.state = index
95         self.setPixmap(self._pixmaps[index])

```

```

92     def set_selected(self):
93         """Sets the cell as selected."""
94         if self.state == 1 or self.state == 3:
95             self.change_pixmap(5)
96         elif self.state == 2 or self.state == 4:
97             self.change_pixmap(6)
98
99     def set_deselected(self):
100        """Sets the cell as deselected."""
101        if self.state == 5:
102            self.change_pixmap(1)
103        elif self.state == 6:
104            self.change_pixmap(2)
105

```

3.10 BoardEvaluator

board_evaluator.py

```

1  from __future__ import annotations
2
3  from copy import deepcopy
4  from typing import List, Tuple, Iterator
5
6  from utils import next_k
7  from constants import BOARD_SIZE
8
9  class BoardEvaluator:
10    """Evaluates a board.
11
12    Attributes:
13      board (List[List[int]]): The board to evaluate.
14      partial_count (List[List[List[List[int]]]]): A list of partial counts of the board.
15      row (int): The row of the current move.
16      col (int): The column of the current move.
17      color (int): The color of the player whose turn it is. 1 for black, 2 for white.
18      renju (bool): Whether renju rules are enabled.
19
20    Methods for partial sum and coordinate conversion: (Refer to Section 2.2.1 of the report for
21    more details)
22      cartesian_to_line: Converts cartesian coordinates to line coordinates.
23      line_to_cartesian: Converts line coordinates to cartesian coordinates.
24      get_max_a: Gets the maximum a coordinate for a given direction.
25      get_max_b: Gets the maximum b coordinate for a given direction and a coordinate.
26      _get_partial_count: Gets the partial count of the board.
27      range_query: Queries how many stones of a color starting from a point given in line
28      coordinates with a given range on a given line.
29      range_query_cartesian: Queries how many stones of a color starting from a point given in
30      cartesian coordinates with a given range on a given line.
31
32    Methods for checking if a move is legal: (Refer to Section 2.2.6 of the report for more details)
33      is_overline: Checks if the current move creates an overline.
34      is_five: Checks if the current move creates a five.
35      count_open_three: Counts the number of open threes created by the current move.
36      count_four: Counts the number of fours created by the current move.
37      count_ends_four: Counts the number of open ends of a four created by the current move.
38      is_legal_detailed: Checks if the current move is legal, and returns the number of threes and
39      fours created by the move.
40      is_legal: Checks if the current move is legal.
41
42    Methods for finding threats and board evaluation: (Refer to Section 2.2.2 and 2.2.3 of the
43    report for more details)
44      find_five: Checks if there is a five of a given color.
45      find_four: Checks if there is a four of a given color.
46      find_open_three: Checks if there is an open three of a given color.
47      find_open_two: Checks if there is an open two of a given color.
48      find_any_three: Checks if there is any three of a given color.
49      count_three: Counts the number of threes of a given color.
50      count_two: Counts the number of twos of a given color.
51      count_one: Counts the number of ones of a given color.
52      get_search_space: Gets the search space of the board.
53      is_empty: Checks if the board is empty.
54      is_full: Checks if the board is full.
55

```

```

51     def __init__(self, board: List[List[int]], color: int, row: int=None, col: int=None, renju: bool
52     =True):
53         """Initialises the BoardEvaluator.
54
55         Args:
56             board (List[List[int]]): The board to evaluate.
57             color (int): The color of the player whose turn it is. 1 for black, 2 for white.
58             row (int, optional): The row of the current move. Defaults to None.
59             col (int, optional): The column of the current move. Defaults to None.
60             renju (bool, optional): Whether renju rules are enabled. Defaults to True.
61
62         self.board = deepcopy(board)
63         self.partial_count = None
64         self.row = row
65         self.col = col
66         self.color = color
67         self.renju = renju
68         if row != None and col != None:
69             self.board[row][col] = color
70
71     """Methods for partial sum and coordinate conversion"""
72
73     def cartesian_to_line(self, direction: int, row: int, col: int) -> Tuple[int, int]:
74         """Converts cartesian coordinates to line coordinates.
75
76         Args:
77             direction (int): The direction of the line.
78             row (int): The row of the cell.
79             col (int): The column of the cell.
80
81         Returns:
82             Tuple[int, int]: The converted line coordinates.
83
84         if direction == 0:
85             a = row
86             b = col
87         elif direction == 1:
88             a = col
89             b = row
90         elif direction == 2:
91             a = col - row + (BOARD_SIZE - 1)
92             b = min(row, col)
93         elif direction == 3:
94             a = row + col
95             b = row - max(a - (BOARD_SIZE - 1), 0)
96         return (a, b)
97
98     def line_to_cartesian(self, direction: int, a: int, b: int) -> Tuple[int, int]:
99         """Converts line coordinates to cartesian coordinates.
100
101        Args:
102            direction (int): The direction of the line.
103            a (int): The a coordinate of the cell.
104            b (int): The b coordinate of the cell.
105
106        Raises:
107            ValueError: If b is out of range.
108
109        Returns:
110            Tuple[int, int]: The converted cartesian coordinates.
111
112        if b >= self.get_max_b(direction, a) or b < 0:
113            raise ValueError
114        if direction == 0:
115            return (a, b)
116        elif direction == 1:
117            return (b, a)
118        elif direction == 2:
119            d = max(a - (BOARD_SIZE - 1), 0)
120            return (BOARD_SIZE - a - 1 + d + b, b + d)
121        elif direction == 3:
122            d = max(a - (BOARD_SIZE - 1), 0)
123            return (d + b, a - b - d)
124
125     def get_max_a(self, direction: int) -> int:
126         """Gets the maximum a coordinate for a given direction.

```

```

126
127     Args:
128         direction (int): The direction of the line.
129
130     Returns:
131         int: The maximum a coordinate.
132         """
133         if direction == 0 or direction == 1:
134             return BOARD_SIZE
135         elif direction == 2 or direction == 3:
136             return 2*BOARD_SIZE - 1
137
138     def get_max_b(self, direction: int, a: int) -> int:
139         """Gets the maximum b coordinate for a given direction and a coordinate.
140
141         Args:
142             direction (int): The direction of the line.
143             a (int): The a coordinate of the cell.
144
145         Returns:
146             int: The maximum b coordinate.
147             """
148         if direction == 0 or direction == 1:
149             return BOARD_SIZE
150         elif direction == 2 or direction == 3:
151             return BOARD_SIZE - abs((BOARD_SIZE-1) - a)
152
153     def _get_partial_count(self):
154         """Computes the partial count of the board."""
155         self.partial_count = [[[0 for _ in range(
156             BOARD_SIZE + 1)] for _ in range(2*BOARD_SIZE - 1)] for _ in range(3)] for _ in range(4)
157
158         for direction in range(4):
159             for a in range(self.get_max_a(direction)):
160                 for b in range(self.get_max_b(direction, a)):
161                     row, col = self.line_to_cartesian(direction, a, b)
162                     for k in range(3):
163                         self.partial_count[direction][k][a][b+1] = self.partial_count[direction][k][
164                             a][b] + \
165                             (1 if self.board[row][col] == k else 0)
166
167     def range_query(self, direction: int, a: int, b: int, color: int, length: int) -> int:
168         """Queries how many stones of a color starting from a point given in line coordinates with a
169         given length on a given line.
170
171         Args:
172             direction (int): The direction of the line.
173             a (int): The a coordinate of the cell.
174             b (int): The b coordinate of the cell.
175             color (int): The color of the stones.
176             length (int): The length of the query.
177
178         Raises:
179             IndexError: If the point (direction, a, b + length) is out of bounds.
180
181         Returns:
182             int: The number of stones of the given color.
183             """
184         if self.partial_count == None:
185             self._get_partial_count()
186         if b + length > self.get_max_b(direction, a):
187             raise IndexError
188         return self.partial_count[direction][color][a][b + length] - self.partial_count[direction][
189             color][a][b]
190
191     def range_query_cartesian(self, direction: int, row: int, col: int, color: int, length: int) ->
192     int:
193         """Queries how many stones of a color starting from a point given in cartesian coordinates
194         with a given length on a given line.
195
196         Args:
197             direction (int): The direction of the line.
198             row (int): The row of the cell.
199             col (int): The column of the cell.
200             color (int): The color of the stones.
201             length (int): The length of the query.

```

```

197
198     Returns:
199         int: The number of stones of the given color.
200     """
201     a, b = self.cartesian_to_line(direction, row, col)
202     return self.range_query(direction, a, b, color, length)
203
204     """Methods for checking if a move is legal:""""
205
206     def is_overline(self) -> bool:
207         """Checks if the current move creates an overline.
208
209         Returns:
210             bool: Whether the current move creates an overline.
211         """
212         overline = False
213         for direction in range(4):
214             a, b = self.cartesian_to_line(direction, self.row, self.col)
215             start_b = max(b-5, 0)
216             end_b = min(b+1, self.get_max_b(direction, a) - 5)
217             for ib in range(start_b, end_b):
218                 if self.range_query(direction, a, ib, self.color, 6) == 6:
219                     overline = True
220
221         return overline
222
223     def is_five(self) -> bool:
224         """Checks if the current move creates a five.
225
226         Returns:
227             bool: Whether the current move creates a five.
228         """
229         five = False
230         for direction in range(4):
231             a, b = self.cartesian_to_line(direction, self.row, self.col)
232             start_b = max(b-4, 0)
233             end_b = min(b+1, self.get_max_b(direction, a) - 4)
234             for ib in range(start_b, end_b):
235                 if self.range_query(direction, a, ib, self.color, 5) == 5:
236                     five = True
237
238         return five
239
240     def count_current_open_three(self) -> int:
241         """Counts the number of open threes created by the current move.
242
243         Returns:
244             int: The number of open threes created by the current move.
245         """
246         num_threes = 0
247         for direction in range(4):
248             a, b = self.cartesian_to_line(direction, self.row, self.col)
249             # iterate through all possible positions of the an open three (of length 6)
250             start_b = max(b-4, 0) # start at 4 spaces before, or 0, whichever is larger
251             end_b = min(b, self.get_max_b(direction, a) - 5) # end at a space before b, or the
252             maximum b, whichever is smaller
253             for ib in (iterator := iter(range(start_b, end_b))):
254                 left_0 = self.range_query(direction, a, ib, 0, 1)
255                 right_0 = self.range_query(direction, a, ib + 5, 0, 1)
256                 middle_color = self.range_query(direction, a, ib + 1, self.color, 4)
257                 middle_0 = self.range_query(direction, a, ib + 1, 0, 4)
258                 if left_0 == 1 and right_0 == 1 and middle_color == 3 and middle_0 == 1:
259                     # found a potential open three
260                     # find b_empty, the b of the cell of the potential straight four that is empty
261                     for b2 in range(ib + 1, ib + 5):
262                         result = self.range_query(direction, a, b2, 0, 1)
263                         if result == 1:
264                             b_empty = b2
265                             break
266                         # place the empty cell and check if it is legal
267                         board_evaluator = BoardEvaluator(
268                             self.board, self.color, *self.line_to_cartesian(direction, a, b_empty), self
269                             .renju)
270                         if not board_evaluator.is_legal():
271                             continue
272                         # a legal move can be placed to create a potential straight four
273                         ends = board_evaluator.count_ends_four(direction, a, ib)
274                         if ends == 2: # new shape is a straight four, so it is an open three

```

```

271             num_threes += 1
272             next_k(iterator, 1) # advance iterator to avoid double counting
273         return num_threes
274
275     def count_current_four(self) -> int:
276         """Counts the number of fours created by the current move.
277
278         Returns:
279             int: The number of fours created by the current move.
280         """
281         num_fours = 0
282         for direction in range(4):
283             a, b = self.cartesian_to_line(direction, self.row, self.col)
284             start_b = max(b-4, 0) # start at 4 spaces before, or 0, whichever is larger
285             end_b = min(b+1, self.get_max_b(direction, a) - 4) # end at b, or the maximum b,
286             whichever is smaller
287             for ib in (iterator := iter(range(start_b, end_b))):
288                 count_color = self.range_query(direction, a, ib, self.color, 5)
289                 count_0 = self.range_query(direction, a, ib, 0, 5)
290                 if count_color == 4 and count_0 == 1:
291                     # find b_empty, the b of the cell of the potential five that is empty
292                     for b2 in range(ib, ib + 5):
293                         result = self.range_query(direction, a, b2, 0, 1)
294                         if result == 1:
295                             b_empty = b2
296                             break
297                         # place the empty cell and check if it is legal
298                         board_evaluator = BoardEvaluator(
299                             self.board, self.color, *self.line_to_cartesian(direction, a, b_empty), self
300                             .renju)
301                         if not board_evaluator.is_legal():
302                             continue
303                         # it is legal, so the shape is a four
304                         num_fours += 1
305                         next_k(iterator, 1) # advance iterator to avoid double counting
306         return num_fours
307
308     def count_ends_four(self, direction: int, a: int, b: int) -> int:
309         """Counts the number of open ends of a four defined by (direction, a, b+1) to (direction, a,
310         b+4).
311
312         Args:
313             direction (int): The direction of the line.
314             a (int): The a coordinate of the cell.
315             b (int): The b coordinate of the cell.
316
317         Returns:
318             int: The number of open ends of the four.
319         """
320         if not self.renju:
321             return 2
322         # It is guaranteed that (direction, a, b) and (direction, a, b+5) is empty
323         board_evaluator1 = BoardEvaluator(
324             self.board, self.color, *self.line_to_cartesian(direction, a, b), self.renju)
325         board_evaluator2 = BoardEvaluator(
326             self.board, self.color, *self.line_to_cartesian(direction, a, b+5), self.renju)
327         count = 0
328         count += 1 if board_evaluator1.is_legal() else 0
329         count += 1 if board_evaluator2.is_legal() else 0
330         return count
331
332     def is_legal_detailed(self) -> Tuple[bool, int, int, bool, bool]:
333         """Checks if the current move is legal, and returns with details.
334
335         Returns:
336             Tuple[bool, int, int, bool, bool]: A tuple containing:
337                 whether the move is legal,
338                 the number of open threes created by this move (if no fives or overlines are created
339             ),
340                 the number of fours created by this move (if no fives or overlines are created),
341                 whether the move creates a five,
342                 and whether the move creates an overline.
343         """
344         overline = self.is_overline()
345         if self.renju and (self.color == 1 and overline): # black creates an overline
346             return (False, 0, 0, False, True)

```

```

343     if self.is_five(): # winning is always legal if no overlines are created
344         return (True, 0, 0, True, overline)
345     open_three = self.count_current_open_three()
346     four = self.count_current_four()
347     if self.renju and self.color == 1 and (open_three >= 2 or four >= 2): # black plays a 3x3 or
348         4x4 fork
349         return (False, open_three, four, False, overline)
350     return (True, open_three, four, False, overline)
351
352 def is_legal(self) -> bool:
353     """Checks if the current move is legal.
354
355     Returns:
356         bool: Whether the current move is legal.
357     """
358     if not self.renju or self.color == 2: # In Gomoku, all moves are legal. In Renju, white
359     moves are always legal.
360     return True
361     return self.is_legal_detailed()[0]
362
363     """Methods for finding threats and board evaluation."""
364
365 def find_five(self, color: int) -> bool:
366     """Checks if there is a five of a given color.
367
368     Args:
369         color (int): The color of the five.
370
371     Returns:
372         bool: Whether there is a five of the given color.
373     """
374     for direction in range(4):
375         for a in range(self.get_max_a(direction)):
376             for b in range(self.get_max_b(direction, a) - 4):
377                 result = self.range_query(direction, a, b, color, 5)
378                 if result == 5:
379                     return True
380     return False
381
382 def count_straight_four(self, color: int) -> bool:
383     """Counts the number of straight fours of a given color.
384
385     Args:
386         color (int): The color of the straight fours.
387
388     Returns:
389         bool: The number of straight fours of the given color.
390     """
391     # Straight fours are a line of 6 cells with 4 consecutive stones of the given color with
392     # empty cells at both ends
393     straight_four = 0
394     for direction in range(4):
395         for a in range(self.get_max_a(direction)):
396             for b in (iterator := iter(range(self.get_max_b(direction, a) - 5))):
397                 count_color = self.range_query(direction, a, b+1, color, 4)
398                 count_0 = self.range_query(direction, a, b, 0, 6)
399                 if count_color == 4 and count_0 == 2:
400                     straight_four += 1
401                     next_k(iterator, 4) # minor optimisation
402     return straight_four
403
404 def find_four(self, color: int) -> List[BoardEvaluator]:
405     """Find fours of a given color.
406
407     Args:
408         color (int): The color of the fours.
409
410     Returns:
411         List[BoardEvaluator]: A list of BoardEvaluators that represent the fours with the
412         remaining empty cell played.
413     """
414     # a line of 5 spaces with 4 stone with the given color and 1 empty space
415     fours = []
416     for direction in range(4):
417         for a in range(self.get_max_a(direction)):
418             for b in range(self.get_max_b(direction, a) - 4):
419

```

```

415     count_color = self.range_query(direction, a, b, color, 5)
416     count_0 = self.range_query(direction, a, b, 0, 5)
417     if count_color == 4 and count_0 == 1:
418         # a four is found
419         # find b_empty, the b of the cell of the potential five that is empty
420         for b2 in range(b, b + 5):
421             result = self.range_query(
422                 direction, a, b2, 0, 1)
423             if result == 1:
424                 b_empty = b2
425                 break
426             # place the empty cell and check if it is legal
427             board_evaluator = BoardEvaluator(
428                 self.board, self.color, *self.line_to_cartesian(direction, a, b_empty),
429                 self.renju)
430             if board_evaluator.is_legal():
431                 fours.append(board_evaluator)
432
433     def find_open_three(self, color: int) -> List[BoardEvaluator]:
434         """Find open threes of a given color. They are a type of threat since placing one more stone
435         would create a straight four.
436
437         Args:
438             color (int): The color of the threes.
439
440         Returns:
441             List[BoardEvaluator]: A list of BoardEvaluators that represent the threes with the
442             remaining empty cell played.
443             """
444             # a line of four spaces with 3 stones of the given color and 1 empty space, surrounded by
445             # empty spaces
446             # e.g. .000.. or ..00.
447             threes = []
448             for direction in range(4):
449                 for a in range(self.get_max_a(direction)):
450                     for b in range(self.get_max_b(direction, a) - 5):
451                         left_0 = self.range_query(direction, a, b, 0, 1)
452                         right_0 = self.range_query(direction, a, b+5, 0, 1)
453                         middle_color = self.range_query(direction, a, b+1, color, 4)
454                         middle_0 = self.range_query(direction, a, b+1, 0, 4)
455                         if left_0 == 1 and right_0 == 1 and middle_color == 3 and middle_0 == 1:
456                             # potential open three found
457                             # find b_empty, the b of the cell of the potential straight four that is
458                             # empty
459                             for b2 in range(b + 1, b + 5):
460                                 result = self.range_query(direction, a, b2, 0, 1)
461                                 if result == 1:
462                                     b_empty = b2
463                                     break
464                                 # place the empty cell and check if it is legal
465                                 board_evaluator = BoardEvaluator(
466                                     self.board, self.color, *self.line_to_cartesian(direction, a, b_empty),
467                                     self.renju)
468
469             if not board_evaluator.is_legal():
470                 continue
471             # check if the four created is a straight four or not
472             ends = board_evaluator.count_ends_four(direction, a, b)
473             if ends == 2:
474                 threes.append(board_evaluator)
475
476     return threes
477
478     def find_open_two(self, color: int) -> List[BoardEvaluator]:
479         """Find open twos of a given color. They are a type of threat since placing one more stone
480         would create an open three.
481
482         Args:
483             color (int): The color of the twos.
484
485         Returns:
486             List[BoardEvaluator]: A list of BoardEvaluators that represent the twos with one of the
487             empty cells played.
488             """
489             # a line of four spaces with 2 stones of the given color and 2 empty spaces, surrounded by
490             # empty spaces
491             open_two_boards = []

```

```

482     for direction in range(4):
483         for a in range(self.get_max_a(direction)):
484             for b in (iterator := iter(range(self.get_max_b(direction, a) - 5))):
485                 left_0 = self.range_query(direction, a, b, 0, 1)
486                 right_0 = self.range_query(direction, a, b+5, 0, 1)
487                 middle_color = self.range_query(direction, a, b+1, color, 4)
488                 middle_0 = self.range_query(direction, a, b+1, 0, 4)
489                 if left_0 == 1 and right_0 == 1 and middle_color == 2 and middle_0 == 2:
490                     # potential open two found
491                     for b2 in range(b + 1, b + 5):
492                         is_0 = self.range_query(direction, a, b2, 0, 1)
493                         if is_0 == 1:
494                             # current cell is empty, place a stone and check if it is legal
495                             board_evaluator = BoardEvaluator(
496                                 self.board, self.color, *self.line_to_cartesian(direction, a, b2
497 ), self.renju)
498                             if not board_evaluator.is_legal():
499                                 continue
500                             open_two_boards.append(board_evaluator)
501             next_k(iterator, 1) # advance iterator to avoid double counting
502         return open_two_boards
503
504     def find_three(self, color: int) -> List[BoardEvaluator]:
505         """Find any threes of a given color.
506
507         Args:
508             color (int): The color of the threes.
509
510         Returns:
511             List[BoardEvaluator]: A list of BoardEvaluators that represent the threes with one of
512             the remaining empty cells played.
513             """
514             # A line of 5 spaces with 3 stones of the given color and 2 empty spaces
515             three_boards = []
516             for direction in range(4):
517                 for a in range(self.get_max_a(direction)):
518                     for b in range(self.get_max_b(direction, a) - 4):
519                         count_color = self.range_query(direction, a, b, color, 5)
520                         count_0 = self.range_query(direction, a, b, 0, 5)
521                         if count_color == 3 and count_0 == 2:
522                             for b2 in range(b, b + 5):
523                                 if self.range_query(direction, a, b2, 0, 1) == 1: # current cell is
524                                     empty
525                                     board_evaluator = BoardEvaluator(
526                                         self.board, self.color, *self.line_to_cartesian(direction, a, b2
527 ), self.renju)
528                                     if board_evaluator.is_legal():
529                                         three_boards.append(board_evaluator)
530
531             return three_boards
532
533     def count_three(self, color: int) -> int:
534         """Counts the number of threes of a given color.
535
536         Args:
537             color (int): The color of the threes.
538
539         Returns:
540             int: The number of threes of the given color.
541             """
542             # A line of 5 spaces with 3 stones of the given color and 2 empty spaces
543             three = 0
544             for direction in range(4):
545                 for a in range(self.get_max_a(direction)):
546                     for b in (iterator := iter(range(self.get_max_b(direction, a) - 4))):
547                         count_color = self.range_query(direction, a, b, color, 5)
548                         count_0 = self.range_query(direction, a, b, 0, 5)
549                         if count_color == 3 and count_0 == 2:
550                             three += 1
551             next_k(iterator, 2) # advance iterator to avoid double counting
552             return three
553
554     def count_two(self, color: int) -> int:
555         """Counts the number of twos of a given color.
556
557         Args:
558             color (int): The color of the twos.

```

```

554
555     Returns:
556         int: The number of twos of the given color.
557     """
558     # A line of 5 spaces with 2 stones of the given color and 3 empty spaces
559     two = 0
560     for direction in range(4):
561         for a in range(self.get_max_a(direction)):
562             for b in (iterator := iter(range(self.get_max_b(direction, a) - 4))):
563                 count_color = self.range_query(direction, a, b, color, 5)
564                 count_0 = self.range_query(direction, a, b, 0, 5)
565                 if count_color == 2 and count_0 == 3:
566                     two += 1
567                     next_k(iterator, 3) # advance iterator to avoid double counting
568     return two
569
570 def count_one(self, color: int) -> int:
571     """Counts the number of ones of a given color.
572
573     Args:
574         color (int): The color of the ones.
575
576     Returns:
577         int: The number of ones of the given color.
578     """
579     # A line of 5 spaces with 1 stone of the given color and 4 empty spaces
580     one = 0
581     for direction in range(4):
582         for a in range(self.get_max_a(direction)):
583             for b in (iterator := iter(range(self.get_max_b(direction, a) - 4))):
584                 count_color = self.range_query(direction, a, b, color, 5)
585                 count_0 = self.range_query(direction, a, b, 0, 5)
586                 if count_color == 1 and count_0 == 4:
587                     one += 1
588                     next_k(iterator, 4) # advance iterator to avoid double counting
589     return one
590
591 def get_search_space(self, r: int) -> List[BoardEvaluator]:
592     """Gets the search space of the board. Refer to Section 2.2.2 of the report for more details
593
594     Args:
595         r (int): The radius of the search space.
596
597     Returns:
598         List[BoardEvaluator]: A list of BoardEvaluators that represent the boards in the search
599     space.
600     """
601     search_space = [[False for _ in range(
602         BOARD_SIZE)] for _ in range(BOARD_SIZE)]
602     for row in range(BOARD_SIZE):
603         for col in range(BOARD_SIZE):
604             if self.board[row][col] != 0:
605                 for dx in range(-r, r+1):
606                     for dy in range(-r, r+1):
607                         new_row = row + dx
608                         new_col = col + dy
609                         if not (0 <= new_row < BOARD_SIZE and 0 <= new_col < BOARD_SIZE) or self
610                         .board[new_row][new_col] != 0:
611                             continue
612                         search_space[new_row][new_col] = True
613     candidate_boards: List[BoardEvaluator] = []
614     for row in range(BOARD_SIZE):
615         for col in range(BOARD_SIZE):
616             if not search_space[row][col] or self.board[row][col] != 0:
617                 continue
618             new_board = BoardEvaluator(
619                 self.board, self.color, row, col, self.renju)
620             if new_board.is_legal():
621                 candidate_boards.append(new_board)
622     return candidate_boards
623
624 def is_empty(self) -> bool:
625     """Checks if the board is empty.
626
627     Returns:

```

```

627         bool: Whether the board is empty.
628     """
629     return all(all(cell == 0 for cell in row) for row in self.board)
630
631     def is_full(self) -> bool:
632         """Checks if the board is full.
633
634         Returns:
635             bool: Whether the board is full.
636         """
637         return all(0 not in row for row in self.board)
638
639 if __name__ == '__main__':
640     board = [[0 for _ in range(BOARD_SIZE)] for _ in range(BOARD_SIZE)]
641     board[7][8] = board[7][9] = 1
642     board[8][7] = board[9][7] = 1
643     board_evaluator = BoardEvaluator(board, 1, 7, 7, True) # play move (7, 7) for black
644     print(board_evaluator.is_legal_detailed()) # (False, 2, 0, False, False), illegal, 3x3 fork
645     board[7][10] = board[10][7] = 1
646     board_evaluator = BoardEvaluator(board, 1, 7, 7, True)
647     print(board_evaluator.is_legal_detailed()) # (True, 0, 2, False, False), illegal, 4x4 fork
648     board[7][10] = 0
649     board_evaluator = BoardEvaluator(board, 1, 7, 7, True)
650     print(board_evaluator.is_legal_detailed()) # (True, 1, 1, False, False), legal, 3x4 fork
651     board[11][7] = 1
652     board_evaluator = BoardEvaluator(board, 1, 7, 7, True)
653     print(board_evaluator.is_legal_detailed()) # (True, 0, 0, True, False), legal, five
654     board[12][7] = 1
655     board_evaluator = BoardEvaluator(board, 1, 7, 7, True)
656     print(board_evaluator.is_legal_detailed()) # (False, 0, 0, False, True), illegal, overline

```

3.11 Worker

worker.py

```

1 # Modified from https://www.pythonguis.com/tutorials/multithreading-pyqt6-applications-qthreadpool/
2 # This file is used solely for the purpose of multithreading in the application.
3
4 from PyQt6.QtCore import QObject, QRunnable, pyqtSignal, pyqtSlot
5
6 import traceback, sys
7
8 class WorkerSignals(QObject):
9     '''Defines the signals available from a running worker thread.
10
11     Supported signals are:
12         finished: No data
13         error: tuple (excetype, value, traceback.format_exc())
14         result: object data returned from processing, can be anything
15     '''
16     finished = pyqtSignal()
17     error = pyqtSignal(tuple)
18     result = pyqtSignal(object)
19
20 class Worker(QRunnable):
21     '''The worker thread. Inherits from QRunnable to handle worker thread setup, signals and wrap-
22     up.'''
23     def __init__(self, fn, *args, **kwargs):
24         super(Worker, self).__init__()
25
26         # Store constructor arguments (reused for processing)
27         self.fn = fn
28         self.args = args
29         self.kwargs = kwargs
30         self.signals = WorkerSignals()
31
32     @pyqtSlot()
33     def run(self):
34         '''Initialise the runner function with passed args, kwargs.'''
35         try:
36             result = self.fn(*self.args, **self.kwargs)
37         except:
38             traceback.print_exc()
39             excetype, value = sys.exc_info()[:2]
40             self.signals.error.emit((exctype, value, traceback.format_exc()))

```

```

40     else:
41         self.signals.result.emit(result) # Return the result of the processing
42     finally:
43         self.signals.finished.emit() # Done

```

3.12 Players

3.12.1 Player, HumanPlayer, and ComputerPlayer

players.py

```

1  from typing import Tuple, List
2
3  class Player:
4      """The abstract class for all players.
5
6      Attributes:
7          name (str): The name of the player.
8      """
9      def __init__(self) -> None:
10          self.name = 'Player' # Must be changed when subclassed.
11
12  class ComputerPlayer(Player):
13      """The abstract class for all computer players.
14
15      Methods:
16          get_move: Returns the best move to make on the board.
17          get_continuation: Returns the best continuation to make on the board.
18          get_evaluation: Returns the evaluation of the board.
19      """
20      def __init__(self) -> None:
21          self.name = 'Computer Player' # Must be changed when subclassed.
22          pass
23
24      def get_move(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
25          """Returns the best move to make on the board."""
26          pass
27
28      def get_continuation(self, board: List[List[int]], color: int, renju: bool) -> List[Tuple[int, int]]:
29          """Returns the best continuation to make on the board."""
30          pass
31
32      def get_evaluation(self, board: List[List[int]], color: int, renju: bool) -> int:
33          """Returns the evaluation of the board."""
34          pass
35
36  class HumanPlayer(Player):
37      """The human player."""
38      def __init__(self) -> None:
39          self.name = 'Human Player'

```

3.12.2 MinimaxPlayer

computer_players/minimax_player.py

```

1  from typing import List, Tuple
2  from random import randint
3
4  from board_evaluator import BoardEvaluator
5  from constants import *
6  from players import ComputerPlayer
7  from utils import previous_of, bubble_sort_k
8
9  class MinimaxPlayer(ComputerPlayer):
10     """A computer player that uses the minimax algorithm to make moves. Refer to Section 2.2.2 of
11     the report for more details.
12
13     Attributes:
14         name (str): The name of the player.
15         depth (int): The depth of the search tree.
16         max_branches (int): The maximum number of branches to search.

```

```

17     Methods:
18         local_evaluation: Evaluates the board locally.
19         minimax: Applies the minimax algorithm to the board.
20         get_evaluation: Gets the evaluation of the board.
21         get_move: Gets the best move to make on the board.
22         get_continuation: Gets the best continuation to make on the board.
23     """
24     def __init__(self, depth: int, max_branches: int) -> None:
25         """Initialises the MinimaxPlayer.
26
27         Args:
28             depth (int): The depth of the search tree.
29             max_branches (int): The maximum number of branches to search.
30         """
31         self.depth = depth
32         self.max_branches = max_branches
33         self.name = f"Minimax {self.depth}"
34
35     def _local_evaluation(self, board: BoardEvaluator) -> int:
36         if board.find_five(1):
37             return WIN
38         if board.find_five(2):
39             return -WIN
40         evaluation = 0
41         evaluation += board.count_straight_four(1) * STRAIGHT_FOUR
42         evaluation += len(board.find_open_three(1)) * OPEN_THREE
43         evaluation += len(board.find_four(1)) * FOUR
44         evaluation += board.count_three(1) * THREE
45         evaluation += board.count_two(1) * TWO
46         evaluation += board.count_one(1) * ONE
47
48         evaluation += board.count_straight_four(2) * -STRAIGHT_FOUR
49         evaluation += len(board.find_open_three(2)) * -OPEN_THREE
50         evaluation += len(board.find_four(2)) * -FOUR
51         evaluation += board.count_three(2) * -THREE
52         evaluation += board.count_two(2) * -TWO
53         evaluation += board.count_one(2) * -ONE
54
55         evaluation += randint(-ONE//2, ONE//2) # randomize evaluation
56         return evaluation
57
58     def _minimax(self, board: BoardEvaluator, color: int, alpha: int, beta: int, depth: int) ->
59         Tuple[int, List[Tuple[int, int, int]]]:
60         """Applies the minimax algorithm to the board.
61
62         Args:
63             board (BoardEvaluator): The board to be evaluated.
64             color (int): The color of the player whose turn it is. 1 for black, 2 for white.
65             alpha (int): The alpha value.
66             beta (int): The beta value.
67             depth (int): The depth of the search tree.
68             renju (bool): Whether renju rules are enabled.
69
70         Returns:
71             Tuple[int, List[Tuple[int, int, int]]]: A tuple of the evaluation of the board and the
72             moves to make.
73     """
74
75     # apply the minimax alphabeta algorithm with the given candidate boards
76     # black is the maximising player, white is the minimising player
77     if depth == 0 or board.find_five(1) or board.find_five(2):
78         return (self._local_evaluation(board), [])
79     board.color = color
80     candidate_boards = board.get_search_space(1)
81     # sort the candidate boards by their evaluation, descending if black, ascending if white
82     bubble_sort_k(candidate_boards, self.max_branches, self._local_evaluation, color == 1)
83     candidate_boards = candidate_boards[:self.max_branches]
84     if DEBUG and depth == self.depth:
85         for cb in candidate_boards: print((cb.row, cb.col))
86     best_eval = -WIN if color == 1 else WIN
87     best_move = None
88     best_moves = []
89     for candidate_board in candidate_boards:
90         new_eval, moves = self._minimax(candidate_board, 3-color, alpha, beta, depth-1)
91         new_eval = previous_of(new_eval)
92         if color == 1:
93             if new_eval > best_eval:

```

```

91             best_eval = new_eval
92             alpha = new_eval
93             best_move = (candidate_board.row, candidate_board.col, color)
94             best_moves = [best_move] + moves
95         elif color == 2:
96             if new_eval < best_eval:
97                 best_eval = new_eval
98                 beta = new_eval
99                 best_move = (candidate_board.row, candidate_board.col, color)
100                best_moves = [best_move] + moves
101            if alpha >= beta:
102                break
103        return (best_eval, best_moves)
104
105    def get_move(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
106        """Makes a move on the board.
107
108        Args:
109            board (List[List[int]]): The board to be evaluated.
110            color (int): The color of the player whose turn it is. 1 for black, 2 for white.
111            renju (bool): Whether renju rules are enabled.
112
113        Returns:
114            Tuple[int, int]: The move to make.
115        """
116        return self.get_continuation(board, color, renju)[0][:2]
117
118    def get_continuation(self, board: List[List[int]], color: int, renju: bool) -> List[Tuple[int, int]]:
119        board_evaluator = BoardEvaluator(board, color, renju=renju)
120        if board_evaluator.is_empty():
121            return [(BOARD_SIZE // 2, BOARD_SIZE // 2, 1)]
122        evaluation, moves = self._minimax(board_evaluator, color, -WIN, WIN, self.depth)
123        if DEBUG:
124            print(evaluation, moves)
125        return moves
126
127    def get_evaluation(self, board: List[List[int]], color: int, renju: bool) -> int:
128        """Gets the evaluation of the board.
129
130        Args:
131            board (List[List[int]]): The board to be evaluated.
132            color (int): The color of the player whose turn it is. 1 for black, 2 for white.
133            renju (bool): Whether renju rules are enabled.
134
135        Returns:
136            int: The evaluation of the board.
137        """
138        board_evaluator = BoardEvaluator(board, color, renju=renju)
139        if board_evaluator.is_empty():
140            return 0
141        evaluation, _ = self._minimax(board_evaluator, color, -WIN, WIN, self.depth)
142        return evaluation

```

3.12.3 AggressivePlayer

`computer_players/aggressive_player.py`

```

1  from typing import List, Tuple
2  from random import randint
3
4  from board_evaluator import BoardEvaluator
5  from constants import *
6  from players import ComputerPlayer
7  from utils import previous_of, bubble_sort_k
8
9  class AggressivePlayer(ComputerPlayer):
10     """A computer player that uses the minimax algorithm to make moves, with an aggressive
11     evaluation function.
12     The only difference between this and MinimaxPlayer is the evaluation function.
13
14     Attributes:
15         name (str): The name of the player.
16         depth (int): The depth of the search tree.
17         max_branches (int): The maximum number of branches to search.

```

```

18     Methods:
19         local_evaluation: Evaluates the board locally.
20         minimax: Applies the minimax algorithm to the board.
21         get_evaluation: Gets the evaluation of the board.
22         get_move: Gets the best move to make on the board.
23         get_continuation: Gets the best continuation to make on the board.
24     """
25     def __init__(self, depth: int, max_branches: int) -> None:
26         """Initialises the AggressivePlayer.
27
28         Args:
29             depth (int): The depth of the search tree.
30             max_branches (int): The maximum number of branches to search.
31         """
32         self.depth = depth
33         self.max_branches = max_branches
34         self.name = f"Aggressive {self.depth}"
35
36     def _local_evaluation(self, board: BoardEvaluator, color: int) -> int:
37         if board.find_five(1):
38             return WIN
39         if board.find_five(2):
40             return -WIN
41         black_evaluation = 0
42         black_evaluation += board.count_straight_four(1) * STRAIGHT_FOUR
43         black_evaluation += len(board.find_open_three(1)) * OPEN_THREE
44         black_evaluation += len(board.find_four(1)) * FOUR
45         black_evaluation += board.count_three(1) * THREE
46         black_evaluation += board.count_two(1) * TWO
47         black_evaluation += board.count_one(1) * ONE
48         white_evaluation = 0
49         white_evaluation += board.count_straight_four(2) * -STRAIGHT_FOUR
50         white_evaluation += len(board.find_open_three(2)) * -OPEN_THREE
51         white_evaluation += len(board.find_four(2)) * -FOUR
52         white_evaluation += board.count_three(2) * -THREE
53         white_evaluation += board.count_two(2) * -TWO
54         white_evaluation += board.count_one(2) * -ONE
55
56         # multiply the evaluation by the aggressive factor for own color
57         if color == 1:
58             black_evaluation = round(black_evaluation * AGGRESSIVE_FACTOR)
59         else:
60             white_evaluation = round(white_evaluation * AGGRESSIVE_FACTOR)
61         evaluation = black_evaluation + white_evaluation
62
63         evaluation += randint(-ONE//2, ONE//2) # randomize evaluation
64         return evaluation
65
66     def _minimax(self, board: BoardEvaluator, color: int, alpha: int, beta: int, depth: int) ->
67         Tuple[int, List[Tuple[int, int, int]]]:
68         """Applies the minimax algorithm to the board.
69
70         Args:
71             board (BoardEvaluator): The board to be evaluated.
72             color (int): The color of the player whose turn it is. 1 for black, 2 for white.
73             alpha (int): The alpha value.
74             beta (int): The beta value.
75             depth (int): The depth of the search tree.
76             renju (bool): Whether renju rules are enabled.
77
78         Returns:
79             Tuple[int, List[Tuple[int, int, int]]]: A tuple of the evaluation of the board and the
80             moves to make.
81             """
82             # apply the minimax alphabeta algorithm with the given candidate boards
83             # black is the maximising player, white is the minimising player
84             if depth == 0 or board.find_five(1) or board.find_five(2):
85                 return (self._local_evaluation(board, color), [])
86             board.color = color
87             candidate_boards = board.get_search_space(1)
88             # sort the candidate boards by their evaluation, descending if black, ascending if white
89             bubble_sort_k(candidate_boards, self.max_branches, lambda b: self._local_evaluation(b, color))
90             candidate_boards = candidate_boards[:self.max_branches]
91             if DEBUG and depth == self.depth:
92                 for cb in candidate_boards: print((cb.row, cb.col))

```

```

91     best_eval = -WIN if color == 1 else WIN
92     best_move = None
93     best_moves = []
94     for candidate_board in candidate_boards:
95         new_eval, moves = self._minimax(candidate_board, 3-color, alpha, beta, depth-1)
96         new_eval = previous_of(new_eval)
97         if color == 1:
98             if new_eval > best_eval:
99                 best_eval = new_eval
100                alpha = new_eval
101                best_move = (candidate_board.row, candidate_board.col, color)
102                best_moves = [best_move] + moves
103            elif color == 2:
104                if new_eval < best_eval:
105                    best_eval = new_eval
106                    beta = new_eval
107                    best_move = (candidate_board.row, candidate_board.col, color)
108                    best_moves = [best_move] + moves
109                if alpha >= beta:
110                    break
111    return (best_eval, best_moves)
112
113 def get_move(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
114     """Makes a move on the board.
115
116     Args:
117         board (List[List[int]]): The board to be evaluated.
118         color (int): The color of the player whose turn it is. 1 for black, 2 for white.
119         renju (bool): Whether renju rules are enabled.
120
121     Returns:
122         Tuple[int, int]: The move to make.
123     """
124     return self.get_continuation(board, color, renju)[0][:2]
125
126 def get_continuation(self, board: List[List[int]], color: int, renju: bool) -> List[Tuple[int, int]]:
127     board_evaluator = BoardEvaluator(board, color, renju=renju)
128     if board_evaluator.is_empty():
129         return [(BOARD_SIZE // 2, BOARD_SIZE // 2, 1)]
130     evaluation, moves = self._minimax(board_evaluator, color, -WIN, WIN, self.depth)
131     if DEBUG:
132         print(evaluation, moves)
133     return moves
134
135 def get_evaluation(self, board: List[List[int]], color: int, renju: bool) -> int:
136     """Gets the evaluation of the board.
137
138     Args:
139         board (List[List[int]]): The board to be evaluated.
140         color (int): The color of the player whose turn it is. 1 for black, 2 for white.
141         renju (bool): Whether renju rules are enabled.
142
143     Returns:
144         int: The evaluation of the board.
145     """
146     board_evaluator = BoardEvaluator(board, color, renju=renju)
147     if board_evaluator.is_empty():
148         return 0
149     evaluation, _ = self._minimax(board_evaluator, color, -WIN, WIN, self.depth)
150     return evaluation

```

3.12.4 DefensivePlayer

`computer_players/defensive_player.py`

```

1 from typing import List, Tuple
2 from random import randint
3
4 from board_evaluator import BoardEvaluator
5 from constants import *
6 from players import ComputerPlayer
7 from utils import previous_of, bubble_sort_k
8
9 class DefensivePlayer(ComputerPlayer):

```

```

10     """A computer player that uses the minimax algorithm to make moves, with a defensive evaluation
11    function.
12    The only difference between this and MinimaxPlayer is the evaluation function.
13
14    Attributes:
15        name (str): The name of the player.
16        depth (int): The depth of the search tree.
17        max_branches (int): The maximum number of branches to search.
18
19    Methods:
20        local_evaluation: Evaluates the board locally.
21        minimax: Applies the minimax algorithm to the board.
22        get_evaluation: Gets the evaluation of the board.
23        get_move: Gets the best move to make on the board.
24        get_continuation: Gets the best continuation to make on the board.
25
26    def __init__(self, depth: int, max_branches: int) -> None:
27        """Initialises the DefensivePlayer.
28
29        Args:
30            depth (int): The depth of the search tree.
31            max_branches (int): The maximum number of branches to search.
32
33        self.depth = depth
34        self.max_branches = max_branches
35        self.name = f"Defensive {self.depth}"
36
37    def _local_evaluation(self, board: BoardEvaluator, color: int) -> int:
38        if board.find_five(1):
39            return WIN
40        if board.find_five(2):
41            return -WIN
42        black_evaluation = 0
43        black_evaluation += board.count_straight_four(1) * STRAIGHT_FOUR
44        black_evaluation += len(board.find_open_three(1)) * OPEN_THREE
45        black_evaluation += len(board.find_four(1)) * FOUR
46        black_evaluation += board.count_three(1) * THREE
47        black_evaluation += board.count_two(1) * TWO
48        black_evaluation += board.count_one(1) * ONE
49        white_evaluation = 0
50        white_evaluation += board.count_straight_four(2) * -STRAIGHT_FOUR
51        white_evaluation += len(board.find_open_three(2)) * -OPEN_THREE
52        white_evaluation += len(board.find_four(2)) * -FOUR
53        white_evaluation += board.count_three(2) * -THREE
54        white_evaluation += board.count_two(2) * -TWO
55        white_evaluation += board.count_one(2) * -ONE
56
57        # multiply the evaluation by the defensive factor for opponent's color
58        if color == 2:
59            black_evaluation = round(black_evaluation * DEFENSIVE_FACTOR)
60        else:
61            white_evaluation = round(white_evaluation * DEFENSIVE_FACTOR)
62        evaluation = black_evaluation + white_evaluation
63
64        evaluation += randint(-ONE//2, ONE//2) # randomize evaluation
65        return evaluation
66
66    def _minimax(self, board: BoardEvaluator, color: int, alpha: int, beta: int, depth: int) ->
67        Tuple[int, List[Tuple[int, int, int]]]:
68        """Applies the minimax algorithm to the board.
69
70        Args:
71            board (BoardEvaluator): The board to be evaluated.
72            color (int): The color of the player whose turn it is. 1 for black, 2 for white.
73            alpha (int): The alpha value.
74            beta (int): The beta value.
75            depth (int): The depth of the search tree.
76            renju (bool): Whether renju rules are enabled.
77
78        Returns:
79            Tuple[int, List[Tuple[int, int, int]]]: A tuple of the evaluation of the board and the
80            moves to make.
81
82            # apply the minimax alphabeta algorithm with the given candidate boards
83            # black is the maximising player, white is the minimising player
84            if depth == 0 or board.find_five(1) or board.find_five(2):

```

```

83         return (self._local_evaluation(board, color), [])
84     board.color = color
85     candidate_boards = board.get_search_space(1)
86     # sort the candidate boards by their evaluation, descending if black, ascending if white
87     bubble_sort_k(candidate_boards, self.max_branches, lambda b: self._local_evaluation(b, color
88 ), color == 1)
89     candidate_boards = candidate_boards[:self.max_branches]
90     if DEBUG and depth == self.depth:
91         for cb in candidate_boards: print((cb.row, cb.col))
92     best_eval = -WIN if color == 1 else WIN
93     best_move = None
94     best_moves = []
95     for candidate_board in candidate_boards:
96         new_eval, moves = self._minimax(candidate_board, 3-color, alpha, beta, depth-1)
97         new_eval = previous_of(new_eval)
98         if color == 1:
99             if new_eval > best_eval:
100                 best_eval = new_eval
101                 alpha = new_eval
102                 best_move = (candidate_board.row, candidate_board.col, color)
103                 best_moves = [best_move] + moves
104             elif color == 2:
105                 if new_eval < best_eval:
106                     best_eval = new_eval
107                     beta = new_eval
108                     best_move = (candidate_board.row, candidate_board.col, color)
109                     best_moves = [best_move] + moves
110             if alpha >= beta:
111                 break
112     return (best_eval, best_moves)

113 def get_move(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
114     """Makes a move on the board.

115     Args:
116         board (List[List[int]]): The board to be evaluated.
117         color (int): The color of the player whose turn it is. 1 for black, 2 for white.
118         renju (bool): Whether renju rules are enabled.

119     Returns:
120         Tuple[int, int]: The move to make.
121     """
122     return self.get_continuation(board, color, renju)[0][:2]

123 def get_continuation(self, board: List[List[int]], color: int, renju: bool) -> List[Tuple[int,
124 int]]:
125     board_evaluator = BoardEvaluator(board, color, renju=renju)
126     if board_evaluator.is_empty():
127         return [(BOARD_SIZE // 2, BOARD_SIZE // 2, 1)]
128     evaluation, moves = self._minimax(board_evaluator, color, -WIN, WIN, self.depth)
129     if DEBUG:
130         print(evaluation, moves)
131     return moves

132 def get_evaluation(self, board: List[List[int]], color: int, renju: bool) -> int:
133     """Gets the evaluation of the board.

134     Args:
135         board (List[List[int]]): The board to be evaluated.
136         color (int): The color of the player whose turn it is. 1 for black, 2 for white.
137         renju (bool): Whether renju rules are enabled.

138     Returns:
139         int: The evaluation of the board.
140     """
141     board_evaluator = BoardEvaluator(board, color, renju=renju)
142     if board_evaluator.is_empty():
143         return 0
144     evaluation, _ = self._minimax(board_evaluator, color, -WIN, WIN, self.depth)
145     return evaluation

```

3.12.5 RandomMovesPlayer

`computer_players/random_moves_player.py`

```
1 from random import choice
```

```

2 from typing import List, Tuple
3
4 from constants import BOARD_SIZE
5 from board_evaluator import BoardEvaluator
6 from players import ComputerPlayer
7
8 class RandomMovesPlayer(ComputerPlayer):
9     """A computer player that makes random moves.
10
11     Attributes:
12         name (str): The name of the player.
13     """
14     def __init__(self) -> None:
15         self.name = 'Random Moves'
16
17     def get_move(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
18         """Returns a random move."""
19         board_evaluator = BoardEvaluator(board, color, renju=renju)
20         if board_evaluator.is_empty():
21             return (BOARD_SIZE // 2, BOARD_SIZE // 2)
22         candidate_boards = board_evaluator.get_search_space(1)
23         candidate = choice(candidate_boards)
24         return (candidate.row, candidate.col)
25
26     def get_continuation(self, board: List[List[int]], color: int, renju: bool) -> List[Tuple[int, int]]:
27         return [self.get_move(board, color, renju)]
28
29     def get_evaluation(self, board: List[List[int]], color: int, renju: bool) -> int:
30         return 0

```

3.12.6 PTPlayer

`computer_players/prioritise_threats_player.py`

```

1 from random import randint
2 from typing import List, Tuple
3
4 from players import ComputerPlayer
5 from typing import List
6 from board_evaluator import BoardEvaluator
7 from constants import *
8 from utils import previous_of, bubble_sort_k, merge_sort
9
10 class PTPlayer(ComputerPlayer):
11     """A computer player that prioritises to play threats. Refer to Section 2.2.3 of the report for
12     more details.
13
14     Attributes:
15         name (str): The name of the player.
16         depth (int): The depth of the search tree.
17         max_branches (int): The maximum number of branches to search.
18
19     Methods:
20         local_evaluation: Evaluates the board locally.
21         search: Searches for threats to play. If there are none, it will run minimax.
22         minimax: Applies the minimax algorithm to the board.
23         get_evaluation: Gets the evaluation of the board.
24         get_move: Gets the best move to make on the board.
25         get_continuation: Gets the best continuation to make on the board.
26
27     """
28     def __init__(self, depth, max_branches) -> None:
29         self.depth = depth * 4
30         self.max_branches = max_branches
31         self.name = f'Prioritise Threats {depth}'
32
33     def _local_evaluation(self, board: BoardEvaluator) -> int:
34         """Returns the local evaluation of the board."""
35         if board.find_five(1):
36             return WIN
37         if board.find_five(2):
38             return -WIN
39         evaluation = 0
40         evaluation += board.count_straight_four(1) * STRAIGHT_FOUR
41         evaluation += len(board.find_open_three(1)) * OPEN_THREE

```

```

41     evaluation += len(board.find_four(1)) * FOUR
42     evaluation += board.count_three(1) * THREE
43     evaluation += board.count_two(1) * TWO
44     evaluation += board.count_one(1) * ONE
45
46     evaluation += board.count_straight_four(2) * -STRAIGHT_FOUR
47     evaluation += len(board.find_open_three(2)) * -OPEN_THREE
48     evaluation += len(board.find_four(2)) * -FOUR
49     evaluation += board.count_three(2) * -THREE
50     evaluation += board.count_two(2) * -TWO
51     evaluation += board.count_one(2) * -ONE
52
53     evaluation += randint(-ONE//2, ONE//2) # randomize evaluation
54     return evaluation
55
56 def _search(self, board: BoardEvaluator, color, alpha, beta, depth) -> Tuple[int, List[Tuple[int
57 , int, int]]]:
58     """Searches for threats recursively.
59
60     Args:
61         board (BoardEvaluator): The board to be evaluated.
62         color (int): The color of the player whose turn it is. 1 for black, 2 for white.
63         alpha (int): The alpha value.
64         beta (int): The beta value.
65         depth (int): The depth of the search tree.
66
67     Returns:
68         Tuple[int, List[Tuple[int, int, int]]]: The evaluation and the moves to make.
69     """
70     board.color = color
71     opp_color = 3 - color
72     # if depth >= 0:
73     #     print(color,(board.row, board.col), alpha, beta, depth)
74
75     # find fives
76     if depth <= 0 or board.find_five(color) or board.find_five(opp_color):
77         return (self._local_evaluation(board), [])
78
79     # find fours, which are immediate wins or threats
80     four_boards = board.find_four(color)
81     if four_boards:
82         # directly win, do not decrease depth
83         evaluation, moves = self._search(four_boards[0], opp_color, alpha, beta, depth)
84         return (previous_of(evaluation), [(four_boards[0].row, four_boards[0].col, color, 'four'
85 )] + moves)
86     four_boards_opp = board.find_four(opp_color)
87     if four_boards_opp:
88         # forced to block, decrease depth by 1 since this search is short
89         evaluation, moves = self._search(four_boards_opp[0], opp_color, alpha, beta, depth-1)
90         return (previous_of(evaluation), [(four_boards_opp[0].row, four_boards_opp[0].col, color
91 , 'opp four')] + moves)
92
93     # find threes
94     open_three_boards = board.find_open_three(color)
95     if open_three_boards:
96         # win in three moves by creating a straight four, so do not decrease depth
97         evaluation, moves = self._search(open_three_boards[0], opp_color, alpha, beta, depth-1)
98         return (previous_of(evaluation), [(open_three_boards[0].row, open_three_boards[0].col,
99 color, 'open three')] + moves)
100
101     # if opp have a three, it can also be refuted by creating a four
102     three_boards_opp = board.find_open_three(opp_color)
103     if three_boards_opp:
104         candidate_boards: List[BoardEvaluator] = []
105         candidate_boards.extend(three_boards_opp)
106         any_threes = board.find_three(color)
107         candidate_boards.extend(any_threes)
108         bubble_sort_k(candidate_boards, self.max_branches, self._local_evaluation, color == 1)
109         # call minimax on the candidate boards, decreasing depth by 2
110         return self._minimax([(cb, 2) for cb in candidate_boards], color, alpha, beta, depth)
111
112     # consider threats first, then fill up the rest with non-threats, decreasing depth
113     three_boards = board.find_three(color)
114     open_two_boards = board.find_open_two(color)
115     non_threat_boards = board.get_search_space(1)

```

```

113     # sort the candidate boards by their evaluation, descending if black, ascending if white
114     # use library sort for better performance
115     three_boards.sort(key=self._local_evaluation, reverse=color == 1)
116     open_two_boards.sort(key=self._local_evaluation, reverse=color == 1)
117     non_threat_boards.sort(key=self._local_evaluation, reverse=color == 1)
118     # my merge sort
119     # merge_sort(three_boards, key=lambda b: self.local_evaluation(b), reverse=color == 1)
120     # merge_sort(open_two_boards, key=lambda b: self.local_evaluation(b), reverse=color == 1)
121     # merge_sort(non_threat_boards, key=lambda b: self.local_evaluation(b), reverse=color == 1)
122
123     # threes are the most important, then open twos, then non-threats
124     # decrease depth by 2 for threes (since it creates a four - a threat)
125     # 3 for open twos, (since it creates an open three - a less compelling threat)
126     # 4 for non-threats, (does not create a threat)
127     candidate_boards = [(b, 2) for b in three_boards] + \
128         [(b, 3) for b in open_two_boards] + \
129         [(b, 4) for b in non_threat_boards]
130     candidate_boards = candidate_boards[:self.max_branches]
131     return self._minimax(candidate_boards, color, alpha, beta, depth)
132
133 def _minimax(self, candidate_boards: List[Tuple[BoardEvaluator, int]], color, alpha, beta, depth
134 ) -> Tuple[int, List[Tuple[int, int, int]]]:
135     """Applies the minimax alpha-beta algorithm to the board.
136
137     Args:
138         candidate_boards (List[BoardEvaluator]): The boards to be evaluated.
139         color (int): The color of the player whose turn it is. 1 for black, 2 for white.
140         alpha (int): The alpha value.
141         beta (int): The beta value.
142         depth (int): The depth of the search tree.
143
144     Returns:
145         Tuple[int, List[Tuple[int, int, int]]]: The evaluation and the moves to make.
146     """
147     best_eval = -WIN if color == 1 else WIN
148     best_eval = -WIN if color == 1 else WIN
149     best_moves = []
150     for (candidate_board, d) in candidate_boards:
151         new_eval, moves = self._search(candidate_board, 3-color, alpha, beta, depth - d)
152         new_eval = previous_of(new_eval)
153         if color == 1:
154             if new_eval > best_eval:
155                 best_eval = new_eval
156                 alpha = new_eval
157                 best_moves = [(candidate_board.row, candidate_board.col, color)] + moves
158         elif color == 2:
159             if new_eval < best_eval:
160                 best_eval = new_eval
161                 beta = new_eval
162                 best_moves = [(candidate_board.row, candidate_board.col, color)] + moves
163         if alpha >= beta:
164             break
165     return (best_eval, best_moves)
166
167 def get_move(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
168     return self.get_continuation(board, color, renju)[0][:2]
169
170 def get_continuation(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
171     board_evaluator = BoardEvaluator(board, color, renju=renju)
172     if board_evaluator.is_empty():
173         return [(BOARD_SIZE // 2, BOARD_SIZE // 2, 1)]
174     evaluation, moves = self._search(board_evaluator, color, -WIN, WIN, self.depth)
175     if DEBUG:
176         print(evaluation, moves)
177     return moves
178
179 def get_evaluation(self, board, color, renju):
180     board_evaluator = BoardEvaluator(board, color, renju=renju)
181     if board_evaluator.is_empty():
182         return 0
183     evaluation, _ = self._search(board_evaluator, color, -WIN, WIN, self.depth)
184     return evaluation

```

3.12.7 RandomPlayer

`computer_players/random_player.py`

```

1  from random import choice
2  from typing import List, Tuple
3
4  from players import ComputerPlayer
5  from computer_players.minimax_player import MinimaxPlayer
6  from computer_players.prioritise_threats_player import PTPlayer
7  from computer_players.aggressive_player import AggressivePlayer
8  from computer_players.defensive_player import DefensivePlayer
9  from computer_players.random_moves_player import RandomMovesPlayer
10
11 COMPUTER_PLAYERS : List[ComputerPlayer] = [
12     RandomMovesPlayer(),
13     MinimaxPlayer(2, 10),
14     MinimaxPlayer(3, 7),
15     MinimaxPlayer(4, 5),
16     AggressivePlayer(2, 10),
17     AggressivePlayer(3, 7),
18     AggressivePlayer(4, 5),
19     DefensivePlayer(2, 10),
20     DefensivePlayer(3, 7),
21     DefensivePlayer(4, 5),
22     PTPlayer(2, 10),
23     PTPlayer(3, 5),
24 ]
25
26 class RandomPlayer(ComputerPlayer):
27     """A random computer player chosen from the List of computer players.
28
29     Attributes:
30         _instance (ComputerPlayer): The instance of the randomly selected computer player.
31         name (str): The name of the player.
32
33     Methods:
34         get_move: Gets the best move to make on the board.
35         get_evaluation: Gets the evaluation of the board.
36         get_continuation: Gets the best continuation to make on the board.
37     """
38     def __init__(self) -> None:
39         self._instance = choice(COMPUTER_PLAYERS)
40         self.name = self._instance.name
41
42     def get_move(self, board: List[List[int]], color: int, renju: bool) -> Tuple[int, int]:
43         return self._instance.get_move(board, color, renju)
44
45     def get_evaluation(self, board: List[List[int]], color: int, renju: bool) -> int:
46         return self._instance.get_evaluation(board, color, renju)
47
48     def get_continuation(self, board: List[List[int]], color: int, renju: bool) -> List[Tuple[int, int]]:
49         return self._instance.get_continuation(board, color, renju)

```

Chapter 4

Testing

4.1 Unit Tests

4.1.1 EloRankings

Some unit test are carried out during the development process. The following tests are carried out to ensure the correctness of the `EloRankings` class.

- `rankings.update("A", "B")` is ran: `{"A": 1516.0, "B": 1484.0}` is shown in `rankings.json`.
- `rankings.update("A", "B")` is ran again: `{"A": 1530.5..., "B": 1469.5...}` is shown in `rankings.json`.
- `rankings.update("C", "D")` is ran again: `{"C": 1500.0, "D": 1500.0}` is shown in `rankings.json`.

The tests are passed. They can be carried out by directly running `elo_rankings.py`. They can be seen at the end of the file.

4.1.2 BoardEvaluator

The `is_legal_detailed` method of the `BoardEvaluator` class is tested during development to ensure that it can correctly determine the legality of a move. The following tests are carried out:

- Set up a board and play a move such that a 3x3 fork is created in the Renju ruleset.
- Set up a board and play a move such that a 4x4 fork is created in the Renju ruleset.
- Set up a board and play a move such that a 3x4 fork is created in the Renju ruleset.
- Set up a board and play a move such that a five is created.
- Set up a board and play an overline in the Renju ruleset.

The tests are passed. They can be carried out by directly running `board_evaluator.py`. They can be seen at the end of the file.

4.1.3 Other tests

Other classes are tested during development to ensure that they can correctly perform their functions. The tests are evident in the code usually in a `if DEBUG:` block, or commented out. They will not be described in detail here.

4.2 Final Tests

4.2.1 Video

A video is created to demonstrate the tests carried out. The video can be found at the following link:
<https://youtu.be/v4UMOG3nAlo>

4.2.2 Objective 1

The software should have a GUI that allows easy navigation to different parts of the software.

No.	Input	Output	Result
1	Click on the Play button in the title screen	The configuration window appears	Pass
2	Click on the Analysis button in the title screen	The analysis window appears	Pass
3	Click on the Rankings button in the title screen	The rankings window appears	Pass
4	In the play window, press the Exit button	The title window appears	Pass
5	In the analysis window, press the Exit button	The title window appears	Pass
6	In the rankings window, press the Exit button	The title window appears	Pass
7	Go to the play or analysis window	There is a sidebar on the right hand side of the screen	Pass
8	Make a valid move	A new button in the sidebar appears	Pass
9	Click on any button in the sidebar	The game board is replayed to the corresponding move	Pass

4.2.3 Objective 2

The player should be able to play Gomoku and Renju.

No.	Input	Output	Result
10	Press Play in the configuration screen with any settings	The play window appears	Pass
11	With Gomoku ruleset, click on an empty cell on the game board	A piece appears	Pass
12	With Renju ruleset, click on an empty cell that is a valid move	A piece appears	Pass
13	With Renju ruleset, make a move that would then create a 3x3 fork	A message showing the move is a 3x3 fork and is invalid appears	Pass
14	With Renju ruleset, make a move that would then create a 4x4 fork	A message showing the move is a 4x4 fork and invalid appears	Pass
15	With Renju ruleset, make a move that would then create a overline	A message showing the move is an overline and is invalid appears	Pass
16	Place five pieces of the same colour in a row	A message showing who the winning player is appears	Pass
17	Hover on an empty cell on the game board	A transparent piece appears on the cell	Pass
18	Make some moves	The most recent move is always highlighted with the colour red	Pass

4.2.4 Objective 3

The player should be able to customise the settings for each game.

No.	Input	Output	Result
19	Select both the black and white players to be human players and press Play	Both players are controlled by the user	Pass
20	Select the black player to be Minimax 2	Minimax 2 plays as the black player and plays first, the user controls the white player.	Pass
21	Select the white player to be Minimax 2 , then make a move	The user controls the black player and plays first, while Minimax 2 plays as the black player	Pass
22	Select the black player to be Defensive 2 and the white player to be Prioritise Threats 2	Defensive 2 as black plays a game with Prioritise Threats 2 as white	Pass
23	Select the white player to be Random Player and repeat this several times	The white player is a computer player selected at random	Pass
24	Select both players to be Random Player , and set repeat to 5	Five games of pairs of randomly selected computer players are played	Pass

4.2.5 Objective 4

The player should be able to save a game after it is played.

No.	Input	Output	Result
25	In the play screen, press File > Save Game in the menu bar	A save game window appears	Pass
26	In the save game window, enter "Alice" and "Bob" as the white and black player names respectively, then press Save	The game is saved to a file, with the names "Alice" and "Bob" in the file name	Pass

4.2.6 Objective 5

The player should be able to analyse a game after it is played.

No.	Input	Output	Result
27	Click File > Load Game in the menu bar	The system's default file manager appears	Pass
28	In the file manager, click and open a saved game with .json format	The game is loaded in	Pass
29	In the analysis window, click on the Black button and click on cells	The cells are changed to black pieces	Pass
30	Click on the White button and click on cells	The cells are changed to white pieces	Pass
31	Click on the Black / White button and click on cells	Empty cells that are clicked are changed to pieces which the colour alternates in the order they are clicked	Pass
32	Setup the board in a way that black has a large advantage, then press Get Evaluation	A message showing black has a great advantage appears	Pass
33	Setup the board in a way that white has a reasonable advantage, select Minimax 2 as the analysing computer player then press Get Evaluation	A message showing white has a slight advantage appears	Pass
34	Setup the board in a way that black has a forced winning sequence, select Prioritise Threats 3 as the analysing computer player then press Get Evaluation	A message showing black has a forced winning sequence appears	Pass
35	In any board state, press Get Best Continuation	A message showing the continuation moves appears	Pass

4.2.7 Objective 6

There should be a variety of computer players.

No.	Input	Output	Result
36	In the configuration screen, open the select menu for players	11 different computer players are shown	Pass
37	Open the rankings screen	The computer players have a variety of ratings	Pass

4.2.8 Objective 7

The software should have a ranking system.

No.	Input	Output	Result
38	Go to the rankings screen	Rankings of computer players are shown in descending order of rating	Pass
39	Win a game against a computer player, then go to the rankings screen	The rating of the computer player is decreased, and the rating of the human player is increased	Pass
40	Lose a game against a computer player, then go to the rankings screen	The rating of the computer player is increased, and the rating of the human player is decreased	Pass

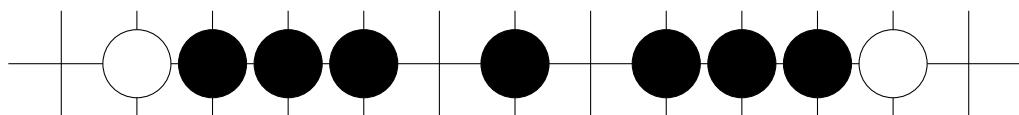


Figure 4.1: Position for 4x4 fork

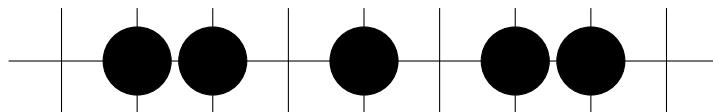


Figure 4.2: A valid move that looks like a 3x3 fork.

4.2.9 Boundary Tests

The following tests are carried out to ensure that the software can handle the edge cases. These situations are very unlikely to occur in a real game, but they are tested to ensure that the software can handle them.

No.	Input	Output	Result
41	In the Renju ruleset, input the position shown in Figure 4.1, placing the central stone last	A message showing the move is a 4x4 fork and is invalid appears	Pass
42	In the Renju ruleset, input the position shown in Figure 4.2, placing the central stone last	The move is placed	Pass
43	Fill in every cell on the board, without winning	A message showing the game is drawn appears	Pass

4.2.10 Erroneous Tests

Most invalid inputs in the software cannot be entered through the GUI. However, in the analysis window, the user may load in an invalid game file, so it must also be tested.

No.	Input	Output	Result
44	Press load game, and choose a JSON file that is not a game file	A message showing the file is invalid appears	Pass

4.3 Summary

All tests, including the boundary and erroneous tests, are passed. The software is able to handle all the inputs and outputs as expected. The tests completely cover the objectives of the software. The software is very robust, and is ready for gathering feedback from the client.

Chapter 5

Evaluation

5.1 Objective 1

The software should have a GUI that allows easy navigation to different parts of the software.

In the title screen, there are three working buttons, leading to the configuration, analysis, and ranking screen respectively. In those screens and the play screen, exit buttons can also be pressed, leading back to the title screen (objectives 1.1-2, tests 1-6). In the play screen and analysis screen, there is a sidebar which allows the user to navigate to any move in the game (objective 1.3, tests 7-9).

The objective is fully met. Every part of the software can be navigated to and from easily, only using the mouse. There is nothing more to be improved in this area when revisiting the software.

5.2 Objective 2

The player should be able to play Gomoku and Renju.

In the play screen and analysis screen, there is a board that allows the user to play Gomoku and Renju (objective 2.1, test 10). In both rulesets, the user can place valid moves but not invalid moves (objectives 2.2-3, tests 11-15). The user can claim a win (objective 2.4, test 16). Transparent pieces appear when a cell is hovered, and the most recent move is highlighted with red (objectives 2.5-6, tests 17-18).

The objective is fully met.

5.3 Objective 3

The player should be able to customise the settings for each game.

When the play button is pressed, a configuration screen appears, allowing the user to change the settings for the game (objective 3.1, test 1). The user can choose the ruleset of the game (objective 3.2, tests 11-15). The user can play against another player or the AI, choosing which colour to play as (objectives 3.3, tests 19-21). The user can also choose to spectate a computer vs computer game (objective 3.4, test 22).

The objective is fully met. Additionally, the user can also specify how many times a computer vs computer game should be played (test 24), if they wish to update the rankings. This is a feature that was not planned, but was added to the software to make it more user-friendly. There is nothing more to be improved in this area when revisiting the software.

5.4 Objective 4

The player should be able to save a game after it is played.

In the play screen, there is a save button that allows the user to save the game (objective 4.1, test 25). The user can also specify the name of both players. The game is saved in a file with the names of both players and the date when the game is played (objectives 4.2-3, test 26).

The objective is fully met. A possible improvement would be to also save all branches of the game while analysing the game. It would also be great if the setup of the board could be saved, so that the user can analyse from a specific position. This is not a priority, but it would be a great feature to have.

5.5 Objective 5

The player should be able to analyse a game after it is played.

In the analysis screen, the user is able to load in a previously saved game (objective 5.1, tests 27-28). The user can set up the board to any positions with the buttons (black, white, black / white) (objectives 5.2-3, test 29-31). The user is also able to see which side is winning (objective 5.4, tests 32-34). The user can also see the best continuation for the current position (objective 5.5, test 35).

The objective is fully met. In addition to objective 5.4, the user can also see whether which side has a forced winning sequence. This helps the user to understand the position better. There is nothing more to be improved in this area when revisiting the software.

5.6 Objective 6

There should be a variety of computer players.

In the configuration, analysis, or rankings screen, it can be seen that there are 11 different computer players with a variety of ratings (objective 6.1, tests 36-37). The user can play against any of these computer players (objective 6.2, tests 20-21). The computer players can play against each other (objective 6.3, test 22).

The objective is fully met. There is nothing more to be improved in this area when revisiting the software.

5.7 Objective 7

The software should have a ranking system.

In the rankings screen, the user can see the ranks and ratings of all computer players and the user (objectives 7.1-2, test 38). The ratings are updated after every game (objective 7.3, tests 39-40).

The objective is fully met. There is nothing more to be improved in this area when revisiting the software.

5.8 Client Feedback

An interview was conducted with the client to gather feedback on the software. The following is the manuscript of the interview.

Question: Did the software meet your expectations?

Mr Shafer: Definitely, it includes everything I wanted and more. The interface is user-friendly, the gameplay is smooth, and most importantly, the analysis tool is very helpful. I am very satisfied with the software.

Question: Are there any sections of the software that exceeded or fall below your expectations?

Mr Shafer: The collection of AI players exceeded my expectations. They have different skill levels and playing styles, which makes playing with them very interesting. There are no areas that fall below my expectations.

Question: Is there anything that could be improved in the software?

Mr Shafer: The software is great as it is, but being able to download Gomoku/Renju files online would enhance my analysis. I could analyse professional games, or play custom positions such as puzzles developed by other people.

Question: Is there anything that you would like to add to the software in the future?

Mr Shafer: An online multiplayer mode would be a great addition. Playing with computer players is fun, but playing with other people is even better. It would also be great if the software could also be used on mobile devices, so that I can play on the go.

5.9 Summary

It was a long 24 weeks of analysing the problem, designing, developing, testing, and evaluating the software. I have met all my objectives and developed a software that the client is satisfied with.

There are many lessons learnt through interacting with the client. I have always created software for myself, but this time, I had to create software for someone else. I learnt to prioritise his requirements, making sure that the software is usable for them. I have also learnt to communicate with the client effectively, making sure that I understand their requirements and they understand my progress.

In terms of development, I have learnt how to use the PyQt library, which is a very powerful library for creating professional-looking GUIs. I have also learnt proper coding conventions, such as using docstrings and comments to make the code more readable. I have also learnt to use version control with Git, which is very important when working on a large project.

5.10 Future Work

The client has suggested that the software could be improved by adding the ability to download Gomoku/Renju files online. This would allow the user to analyse professional games, or play custom positions such as puzzles developed by other people. This is a feature that I could add to the software in the future.

The client has also suggested that an online multiplayer mode would be good to have. This feature might be considered by web developers who are interested in creating a web version of the software.

The client has also suggested that the software could be used on mobile devices. This would require a complete rewrite of the software, which might be time-consuming. Mobile developers may be interested in this project.

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