

Morning AI (A) - Homework

IMPLICIT DERIVATIVE

1. $x^3 + 4y^3 = 1$
2. $x^2 + xy - y^2 = 4$
3. $y \cos x = x^2 + y^2$
4. $x^4(x + y) = y^2(3x - y)$
5. $\tan^{-1}(x^2 \cdot y^2) = x + xy^2$
6. $e^{(x/y)} = x - y$

EQUATION OF THE TANGENT LINE AND NORMAL LINE TO THE CURVE

1. $y \sin 2x = x \cos 2y$ at $(\pi/2, \pi/4)$
2. $x^2 + xy + y^2 = 3$ at $(1, 1)$
3. $x^2 + y^2 = (2x^2 + 2y^2 - x)^2$ at $(0, 1/2)$
4. $2(x^2 + y^2) = 25(x^2 - y^2)$ at $(3, 1)$

ABSOLUTE MAXIMUM AND MINIMUM

1. $f(x) = 2x^3 - 3x^2 - 12x + 1$ Interval: $[-2, 3]$
2. $f(x) = 3x^4 - 4x^3 - 12x^2 + 1$ Interval: $[-2, 3]$
3. $f(x) = x + 1/x$ Interval: $[0.2, 4]$
4. $f(t) = t\sqrt{4 - t^2}$ Interval: $[-1, 2]$
5. $f(t) = 2 \cos t + \sin 2t$ Interval: $[0, \pi/2]$
6. $f(x) = x e^{(-x^2/8)}$ Interval: $[-1, 4]$
7. $f(x) = \ln(x^2 + x + 1)$ Interval: $[-1, 1]$

RELATIVE EXTREMAS

1. $f(x) = 4 + (1/3)x - (1/2)x^2$
2. $f(x) = 2x^3 - 3x^2 - 36x$
3. $g(t) = t^4 + t^3 + t^2 + 1$
4. $g(y) = (y - 1) / (y^2 - 4 + 1)$
5. $h(t) = t^{(3/4)} + 2t^{(1/4)}$
6. $f(x) = x^{(4/5)} (x - 4)^2$
7. $f(\theta) = 2\cos\theta + \sin^2\theta$
8. $f(x) = x^2 e^{(-3x)}$

Mean Value Theorem

1) Roll's Theorem

- i) $f(x) = x^2 - 3x + 2$ on $[1,2]$
- ii) $f(x) = \sin^2 x$ on $[0,x]$
- $f(x) = x^2 - 7x + 12$ on $[3,4]$
- iv) $f(x) = x^2 + 2x - 1$ on $[0,1]$
- v) $f(x) = |x|$, on $[-1,1]$
- vi) $f(x) = x^2 - 2x$, on $[0,2]$
- vii) $f(x) = \cos x$, $[0, 25\pi]$
- (vii) $f(x) = x^3 - 3x$, on $[-\sqrt{3}, \sqrt{3}]$

2) Lagrange's Mean Value Theorem (LMVT)

- $f(x) = x^3 - 3x - 1$, $[-\frac{11}{7}, \frac{13}{7}]$
- $f(x) = 2x^2 - 3x + 1$, $[0,2]$
- $f(x) = x^3 - 3x + 2$, $[-2,2]$
- $f(x) = \ln x$, $[1,4]$
- $f(x) = 1/x$, $[1,3]$

3) Cauchy Mean Value Theorem (CMVT)

- If $f(x) = e^x$ and $g(x) = e^{2x}$ on $[0, \ln 2]$, $C = ?$ by Cauchy theorem?
- $f(x) = x^2$, $g(x) = x^3$ on $[1,2]$ $C = ?$ by Cauchy theorem.

POWER SERIES

Find Maclaurin Series for:

- 1) $f(x) = e^x$
- 2) $f(x) = \ln(1 + x)$
- 3) $f(x) = \ln(1 - x)$
- 4) $f(x) = \cos x$
- 5) $f(x) = \sin x$

Find Taylor Series for:

- 1) $\sin x$ at $x = \pi/2$
- 2) $f(x) = 1/\sqrt{x}$ at $x = 9$