

3. If A then not B else B

$$\lambda bxy(b \times x)(A(\text{not } B)B)$$

$$= A(\text{not } B)B$$

$$\text{xor} = \lambda ab(a(\text{not } b)b)$$

$$\text{xor}(\text{true true})$$

$$= \lambda ab(a(\text{not } b)b)(\text{true true})$$

$$= \text{true}(\text{not true}) \text{true}$$

$$= \underbrace{\text{true}}_{\downarrow} (\underbrace{\text{false true}}_{\text{true}})$$

$$= \text{false} //$$

2. SWAP = $\lambda p(\text{pair}(\text{snd } p)(\text{fst } p))$

$$\text{swap}(\text{pair } a b)$$

$$= \lambda p(\text{pair}([\text{snd } p][\text{fst } p]))(\text{pair } a b)$$

$$= \text{pair}([\underbrace{\text{snd}(\text{pair } a b)}_{b}][\underbrace{\text{fst}(\text{pair } a b)}_{a}])$$

$$= \text{pair}(b a) //$$

3. Map = $\lambda pf(\text{pair}([\text{f}(\text{fst } p)][\text{f}(\text{snd } p)]))$

$$\text{Map}(\text{pair } a b) f'$$

$$= \lambda pf(\text{pair}([\text{f}(\text{fst } p)][\text{f}(\text{snd } p)])) f'$$

$$= \text{pair}([\underbrace{\text{f}'(\text{fst}(\text{pair } a b))}_{a}][\underbrace{\text{f}'(\text{snd}(\text{pair } a b))}_{b}])$$

$$= \text{pair}([\text{f}'a][\text{f}'b]) //$$

4.

→ ADD zero Dois

$$= \lambda nm(n \text{ inc } m)(\text{zero dois})$$

$$= \text{zero inc dois}$$

$$= \lambda fx(x)(\text{inc dois})$$

$$= \text{dois} //$$

→ ADD dois zero

$$= \lambda nm(n \text{ inc } m)(\text{dois zero})$$

$$= \text{dois inc zero}$$

$$= \lambda fx(f(fx))(\text{inc zero})$$

$$= \text{inc } \begin{matrix} 1 \\ 2 \end{matrix} (\text{inc zero})$$

$$= \text{inc } \begin{matrix} 1 \\ 2 \end{matrix} \text{ um}$$

$$= \text{dois} //$$

5. $\text{Fib}_0 = \lambda f_n. (\text{if } (n == 2 \text{ or } n == 1) \text{ then } 1 \\ \text{else } (f(n-1) + f(n-2)))$

$\rightarrow Y \text{Fib}_0 4$

$= \text{fib} (Y \text{fib}) 4$

$= \text{if } (n == 2 \text{ or } n == 1) \text{ then } 1 \text{ else } (Y \text{fib}(3) + Y \text{fib}(2))$

$= (Y \text{fib}(3) + Y \text{fib}(2))$

$\stackrel{?}{=} (Y \text{fib} 2 + Y \text{fib} 3) + 1$

$= 1 + 1 + 1 = 3$