```
In [220]: from abc import ABC, abstractmethod
          from collections import defaultdict
          import math
          import networkx as nx
          import numpy as np
          import os
          import random
          from matplotlib import pyplot as plt
          class MCTS:
              "Monte Carlo tree searcher. First rollout the tree then choose a mov
              def __init__(self, exploration_weight=1):
                  self.Q = defaultdict(int) # total reward of each node
                  self.N = defaultdict(int) # total visit count for each node
                  self.children = dict() # children of each node
                  self.exploration_weight = exploration_weight
              def choose(self, node):
                   "Choose the best successor of node. (Choose a move in the game)"
                  if node.is_terminal():
                      raise RuntimeError(f"choose called on terminal node {node}")
                  if node not in self.children:
                      return node.find random child()
                  def score(n):
                      if self.N[n] == 0:
                          return float("-inf") # avoid unseen moves
                      return self.Q[n] / self.N[n] # average reward
                  return max(self.children[node], key=score)
              def do rollout(self, node):
                   "Make the tree one layer better. (Train for one iteration.)"
                  path = self. select(node)
                  leaf = path[-1]
                  self. expand(leaf)
                  reward = self. simulate(leaf)
                  self. backpropagate(path, reward)
              def select(self, node):
                  "Find an unexplored descendent of `node`"
                  path = []
                  while True:
                      path.append(node)
                      if node not in self.children or not self.children[node]:
                           # node is either unexplored or terminal
                          return path
                      unexplored = self.children[node] - self.children.keys()
                      if unexplored:
                          n = unexplored.pop()
                          path.append(n)
                          return path
```

```
node = self._uct_select(node) # descend a layer deeper
    def expand(self, node):
        "Update the `children` dict with the children of `node`"
        if node in self.children:
            return # already expanded
        self.children[node] = node.find children()
    def simulate(self, node):
        "Returns the reward for a random simulation (to completion) of `
node`"
        #invert reward = True
        reward = 0
        while True:
            #print(node.to pretty string())
            if node.is_terminal():
                return reward
            node = node.find_random_child()
            reward = node.get_reward()
    def backpropagate(self, path, reward):
        "Send the reward back up to the ancestors of the leaf"
        for node in reversed(path):
            self.N[node] += 1
            self.Q[node] += reward
            reward = 1 - reward # 1 for me is 0 for my enemy, and vice
 versa
    def uct select(self, node):
        "Select a child of node, balancing exploration & exploitation"
        # All children of node should already be expanded:
        assert all(n in self.children for n in self.children[node])
        log N vertex = math.log(self.N[node])
        def uct(n):
            "Upper confidence bound for trees"
            return self.Q[n] / self.N[n] + self.exploration weight * mat
h.sqrt(
                log N vertex / self.N[n]
            )
        return max(self.children[node], key=uct)
```

```
In [221]: class Node(ABC):
               H H H
              A representation of a single board state.
              MCTS works by constructing a tree of these Nodes.
              Could be e.g. a chess or checkers board state.
              @abstractmethod
              def find children(self):
                   "All possible successors of this board state"
                   return set()
              @abstractmethod
              def find random child(self):
                   "Random successor of this board state (for more efficient simula
          tion)"
                   return None
              @abstractmethod
              def is terminal(self):
                   "Returns True if the node has no children"
                   return True
                 @abstractmethod
                def reward(self):
          #
                     "Assumes `self` is terminal node. 1=win, 0=loss, .5=tie, etc"
          #
                     return 0
          #
                 @abstractmethod
                def hash (self):
                     "Nodes must be hashable"
          #
                     return 123456789
                 @abstractmethod
          #
          #
                def __eq_ (node1, node2):
                     "Nodes must be comparable"
          #
          #
                     return True
```

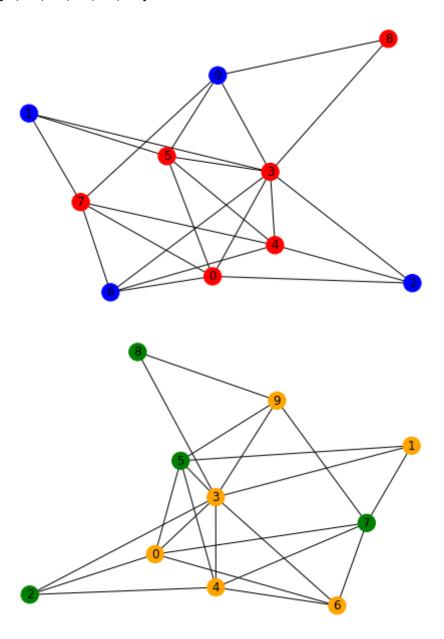
```
In [243]: class VertexCoverInstance(Node):
              def init (self, graph, cover = [], reward = 0):
                  self.graph = graph
                  self.cover = cover
                  self.reward = reward
              def find children(self):
                  possiblemoves = []
                  if self.is_terminal(): # If the game is finished then no moves
           can be made
                      return set(possiblemoves)
                  for i in list(self.graph.nodes):
                      H = self.graph.copy()
                      neigh = H.neighbors(i)
                      step reward = -1
                      H.remove_node(i)
                      possiblemoves.append(VertexCoverInstance(H, self.cover+[i],
          self.reward+step reward))
                  return set(possiblemoves)
              def find random child(self):
                  if self.is_terminal():
                      return None # If the game is finished then no moves can be
           made
                  temp = self.find children()
                  return random.sample(temp,1)[0]
                def reward(board):
          #
                    if not board.terminal:
                        raise RuntimeError(f"reward called on nonterminal board {b
          oard}")
                    return self.reward #reward comes upon reaching terminal state
              def is terminal(self):
                  return nx.classes.function.is_empty(self.graph)
              def to pretty string(self):
                  return str(list(self.graph.nodes()))
              def get cover(self):
                  return str(self.cover)
              def get reward(self):
                  return self.reward
```

```
In [308]: def play_game(G, display = True):
              tree = MCTS()
              board = VertexCoverInstance(G)
              #print(board.to pretty string())
              moves = 0
              while True:
                   if board.is_terminal():
                       break
                   #80 rollouts per turn
                   for _ in range(80):
                       tree.do_rollout(board)
                  board = tree.choose(board)
                  #print(board.to pretty string())
                  moves = moves+1
                   if board.is_terminal():
                       break
              vc = board.get_cover()
              if display:
                  print("\n\nMCTS APPROX\n")
                  print(vc)
                  color_map = []
                   for node in G:
                       if str(node) in vc:
                           color_map.append('red')
                       else:
                           color map.append('blue')
                  plt.figure(1)
                  nx.draw(G, node color=color map, with labels=True)
              return vc, moves
```

```
from networkx.algorithms import approximation as appx
In [309]:
          import itertools
          def show_optimal_vc(G, display=True):
              #opt = list(appx.vertex cover.min weighted vertex cover(G))
              def findsubsets(s):
                  lists =[list(itertools.combinations(s, n)) for n in range(len(s
          ))]
                  return list(itertools.chain.from_iterable(lists))
              powerset = findsubsets(list(G.nodes()))
              for s in powerset:
                  H = G.copy()
                  H.remove nodes from(s)
                  if nx.classes.function.is_empty(H):
                      opt = list(s)
                      break
              if display:
                  print("\n\nOPTIMAL\n")
                  print(opt)
                  color_map = []
                  for node in G:
                       if node in opt:
                           color_map.append('orange')
                       else:
                           color_map.append('green')
                  plt.figure(2)
                  nx.draw(G, node color=color map, with labels=True)
              return opt
```

MCTS APPROX

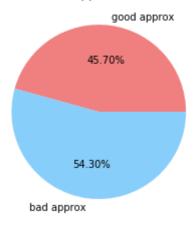
OPTIMAL



```
In [314]: NUM_SIMS = 1000
          def sim_test_approx(simulations):
              count_success = 0
              for x in range(simulations):
                  A = generate_graph(10)
                  vc, moves = play_game(A, display=False)
                  opt = show optimal vc(A, display=False)
                   if moves<=len(opt)*1.1:</pre>
                       count_success=count_success+1
              print(count_success)
              return count_success
          count = sim test approx(NUM SIMS)
          plot_arr = [count,NUM_SIMS-count]
          plt.figure(3)
          plt.pie(plot_arr, colors = ['lightcoral','lightskyblue'], labels = ['goo
          d approx', 'bad approx'],autopct='%1.2f%%')
          plt.title('Percentage of Good MCTS Approximations (Min Vertex Cover)')
          plt.show()
```

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Percentage of Good MCTS Approximations (Min Vertex Cover)



```
In [ ]:
```