# Logical Inference for Question Answering

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Stanford University

April 14, 2015



# Natural Logic Inference for **Common Sense Reasoning**

Kittens play with yarn

Kittens play with computers





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April 14, 2015

The city refused the demonstrators a permit because they feared violence.



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a city fears violence

demonstrators fear violence



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I ate the cake with a cherry vs. I ate the cake with a fork cakes come with cherries cakes are eaten using cherries



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I ate the cake with a cherry vs. I ate the cake with a fork cakes come with cherries cakes are eaten using cherries

Put a sarcastic comment in your talk. That's a great idea.

Sarcasm in your talk is a great idea



# Common Sense Reasoning for Vision

Dogs drive cars



People drive cars



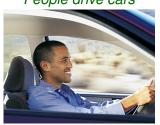


# Common Sense Reasoning for Vision

Dogs drive cars



People drive cars



Baseball is played underwater



Baseball is played on grass





# Prior Work on Common Sense Reasoning

**Old School Al:** Nuanced reasoning; tiny coverage.

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**Information Extraction:** Shallow inference, large data.

- OpenIE (Yates et al., 2007), NELL (Carlson et al., 2010).
- Extraction of facts from a large corpus; fuzzy lookup.

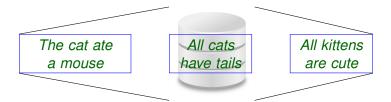


# Start with a large knowledge base



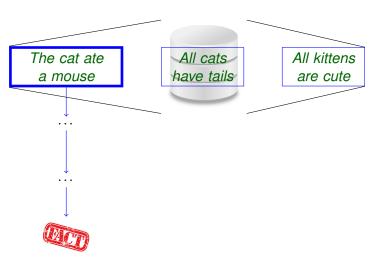


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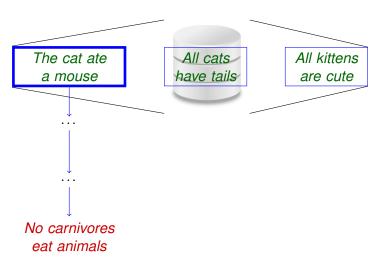




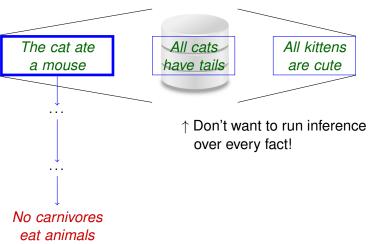
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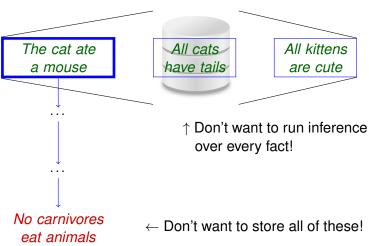






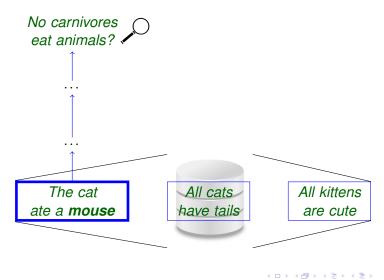






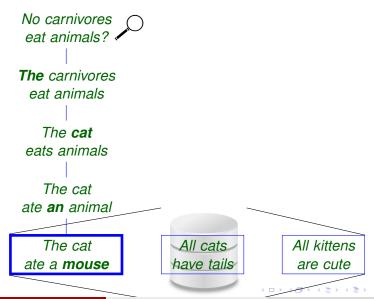


# Infer new facts...on demand from a query...

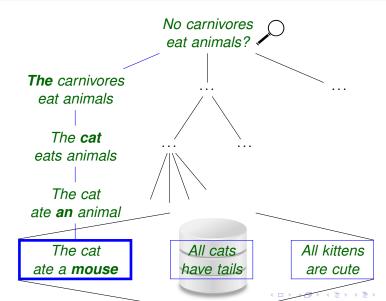




# ...Using text as the meaning representation...



### ...Without aligning to any particular premise.





#### Lookup in 270 million entry KB...

...by lemmas 12% recall

...with NaturalLI 49% recall (91% precision)



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Fast.

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Natural Logic



### s/Natural Logic/Syllogistic Reasoning/g

Some cat ate a mouse (all mice are rodents) Some cat ate a rodent



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#### Facts are text; inference is lexical mutation



Treat hypernymy as a partial order.





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Polarity is the direction a lexical item can move in the ordering.

animal

feline

cat

house cat



Treat hypernymy as a partial order.



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animal
feline

↑ cat
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Treat hypernymy as a partial order.



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living thing

animal





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#### Natural Logic and Polarity

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Quantifiers determines the *polarity* ( $\uparrow$  or  $\downarrow$ ) of words.



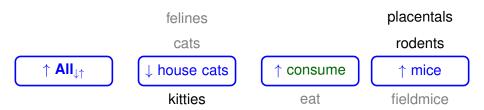


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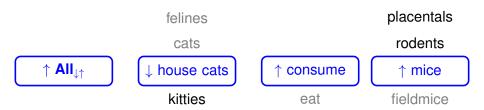




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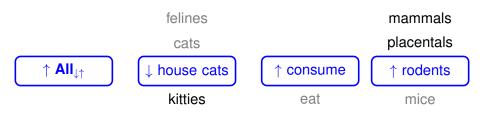




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Mutations must respect polarity.

Inference is reversible.





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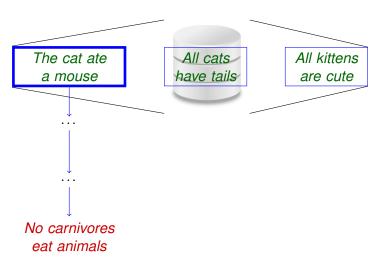


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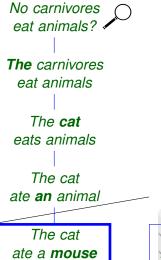


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  - We expect readers to make these inferences instantly.





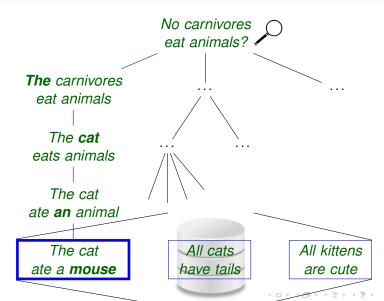




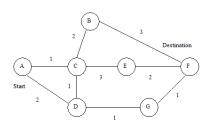
All cats have tails

All kittens are cute



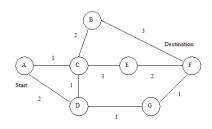






 $\textbf{Nodes} \qquad \quad (\textit{ fact}, \textit{truth maintained} \in \{\textit{true}, \textit{false}\})$ 

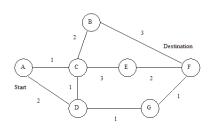




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Start Node ( query fact, true )
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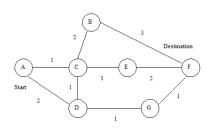


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Nodes ( fact, truth maintained  $\in \{\text{true}, \text{false}\}\)$ 

Start Node ( query fact, true ) **End Nodes** any known fact

**Edges** Mutations of the current fact **Edge Costs** How "wrong" an inference step is (learned)



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#### Search mutates opposite to polarity





Truth maintained:





Truth false





Truth false





Truth false





Truth false





Truth false





Truth false





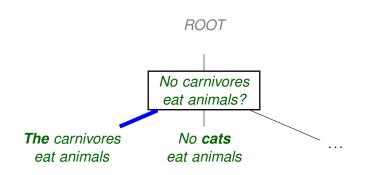
#### Shorthand for a node:



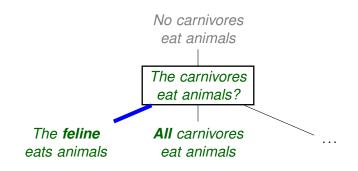


No carnivores eat animals?



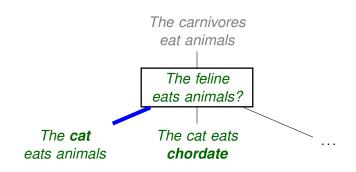




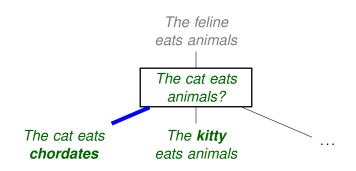






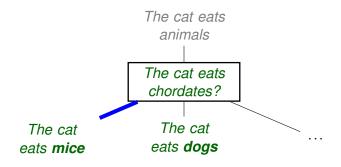




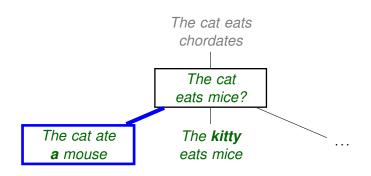






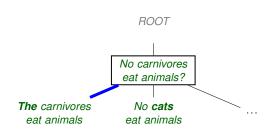








## An Example Search (with edges)

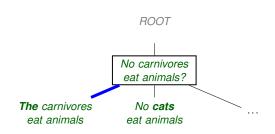


Template Instance Edge

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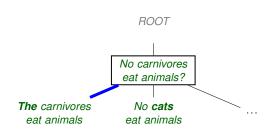


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## An Example Search (with edges)



TemplateInstanceEdgeOperator NegateNo  $\rightarrow$  TheNo carnivores eat animals  $\rightarrow$  The carnivores eat animals



## **Edge Templates**

## **Template** m

Instance

Hypernym Hyponym Antonym Synonym  $animal \rightarrow cat$   $cat \rightarrow animal$   $good \rightarrow bad$   $cat \rightarrow true cat$ 

Add Word Delete Word  $cat \rightarrow \cdot$   $\cdot \rightarrow cat$ 

Operator Weaken
Operator Strengthen
Operator Negate
Operator Synonym

 $some \rightarrow all$   $all \rightarrow some$   $all \rightarrow no$  $all \rightarrow every$ 

Nearest Neighbor

cat o dog



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• nocturnal  $\xrightarrow{1}$  diurnal,  $a \parallel \xrightarrow{\lambda}$  not all

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## **Natural Logic Analog of Transitivity:**

State Fact

Mutation

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## **Natural Logic Analog of Transitivity:**

State Fact Mutation

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 Complex join table can be reduced to tracking a simple binary distinction.





## **Experiments**

#### FraCaS Textual Entailment Suite:

- Used in MacCartney and Manning (2007; 2008).
- RTE-style problems: is the hypothesis entailed from the premise?
  - P: At least three commissioners spend a lot of time at home.
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#### Not a blind test set!

"Can we make deep inferences without knowing the premise a priori?"

### FraCaS Results

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M07: MacCartney and Manning (2007)

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Applicable (1,5,6)		76	90	89



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- A semi-curated collection of common-sense facts.
   not all birds can fly
   noses are used to smell
   nobody wants to die
   music is used for pleasure
- Negatives: ReVerb extractions marked false by Turkers.
- Small (1378 train / 1080 test), but fairly broad coverage.



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270 million lemmatized Ollie extractions.



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4x improvement in recall.



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### **Takeaways**

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## Complexity doesn't grow with knowledge base size.



# Thanks!



