

## Homework #4 Time Complexity Analysis

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## Problem 1: checkIfValidUsername

( ? points)

```

static boolean checkIfValidUsername(String username) {
    // checks string validation and lenght
a.    if (username == null || username.length() == 0) {
        System.out.println("the username is invalid , it should be at least 1 character");
        return false;
    }
    // checks first char is letter or not
b.    if (isLetter(username.charAt(0))) {
        // if last letter valid string is valid
        if (username.length() == 1)
            return true;
        // checks other letters
        return checkIfValidUsername(username.substring(1));
    }
    System.out.println("the username is invalid , it shouldcontains only letters");
    return false;
}

```

(a) {This part have basic compression and println, there is no loop all parts have  $O(1)$  time complexity }

(b) {There is no loop in this part isLetter( $O(1)$ ), charat( $O(1)$ ) .lenght()( $O(1)$ ) and a recursive call with substring function that  $O(N)$ .)}

(**Conc.**) { This method recursively checks the rest of the characters with creating substrings and have  $O(N)$  per step. The recursion continues until either the end of the string is reached that's why this make the method  $O(N^2)$ timecomplexity}

(Solution)

*checkIfValidUsername have  $O(N^2)$ timecomplexity(lenghtoftheusername)*

**Problem 2: isBalancedPassword**

(? points)

```

static boolean isBalancedPassword(String password1) {
a.    Stack<Character> stack = new Stack<>();
        boolean isAnyBracket = false, isAnyLetter = false;

b.    for (char c : password1.toCharArray()) {
            if (c == '(' || c == '{' || c == '[') {
                stack.push(c);
                isAnyBracket = true;
            } else if (c == ')' || c == '}' || c == ']') {
                if (stack.isEmpty()) {
                    System.out.println("the password1 is inv
                    return false;
                }
                char top = stack.pop();
                if ((c == ')') && top != '(') || (c == '}' &&
                    System.out.println("the password1 is inv
                    return false;
            }
            } else if(isLetter(c)) {
                isAnyLetter = true;
            } else {
                System.out.println("the password1 is invalid
                return false;
            }
        }

c.    if (!isAnyBracket)
        System.out.println("the password1 is invalid, it
    if (!isAnyLetter)
        System.out.println("the password1 is invalid, it
    if(!stack.isEmpty())
        System.out.println("the password1 is invalid, it

    return (stack.isEmpty() && isAnyBracket && isAnyLett
}

```

(a) {Initialization of Stack and boolean variables has a time complexity of  $O(1)$ .  
}

(b) { for loop iterates over each character of the password1.toCharArray(), so

*the time complexity of the loop is  $O(N)$ , where  $N$  is the length of the password.  
and toCharArray method have  $O(N)$  time complexity that calls once }*

*(b.inloop) {In the loop there are push, pop, isLetter, isEmpty and println  
methods all of these methods have  $O(1)$  time complexity in worst case }*

*(c) {There is only compressions and println function that have  $O(1)$  time  
complexity }*

*(Conc.) { Therefore, the time complexity of the isBalancedPassword function is  
 $O(N)$ , where  $N$  is the length of the password. )}*

**(Solution)**

*isBalancedPassword function is  $O(N)$ (length of the password.)*

**Problem 3: containsUserNameSpirit**

( ? points)

```

static boolean containsUserNameSpirit(String username, String password1) {
a.    Stack<Character> stack = new Stack<Character>();

        if (password1.length() < 8) {
            System.out.println("the password1 is invalid , it is too short");
        }

        // Push each character of the password onto the stack
b.    for (char c : password1.toCharArray()) {
        stack.push(lowerCase(c));
    }

c.    for(char c : username.toCharArray()) {
        if (stack.contains(lowerCase(c)))
            return true;
    }

d.    System.out.println("the password1 is invalid , it is too long");
    return false;
}

```

(a) { Initialization of stack, compression in if and println have a time complexity of  $O(1)$ . }

(b) { for loop iterates over each character of the password1.toCharArray() and pushes to stack, so the time complexity of the loop is  $O(N)$ . toCharArray method have  $O(N)$  time complexity that calls once, and push function have  $O(1)$ . At the end for loop has  $O(N)$  time complexity, where  $N$  is the length of password1. }

(c) { for loop iterates over each character of the password1.toCharArray() and checks stacks for it's lowercase version, so the time complexity of the loop is  $O(N*M)$ . toCharArray method have  $O(M)$  time complexity that calls once, lowercase function have  $O(1)$ , and contains method has  $O(N)$ . At the end for loop has  $O(N*M)$  time complexity, where  $N$  is the length of password1 and  $M$  is length of username. }

(d) { There is only println function that have  $O(1)$  time complexity }

(Conc.) { In the worst case, if both the length of password1 and the length of the username are equal to the maximum possible length, then the time complexity

*will be  $O(N^2)$ , where  $N$  is the maximum length. Otherwise  $O(N * M)$  time complexity, where  $N$  is the length of password and  $M$  is the length of username.*

***(Solution)***

*containsUserNameSpirit function is  $O(N * M)$  (length of the password and username)*

**Problem 4: isPalindromePossible**

(? points)

```

a.    static boolean isPalindromePossible(String password1) {
        StringBuilder output = new StringBuilder();
        String noBPass;

        for (char c : password1.toCharArray()) {
            if (c != '(' && c != ')') && c != '[' && c != ']'
                output.append(c);
        }

b.    Boolean[] table = new Boolean[output.length() + 1]
        for(int i = 0; i < output.length(); ++i) {
            table[i] = false;
        }

        table[output.length()] = (output.length() % 2 == 0)

        noBPass = output.toString();

c.    if(!recursivePolindrome(noBPass, table, 0)) {
        System.out.println("the password1 is invalid, it
            return false;
        }
        return true;
    }

d.    private static boolean recursivePolindrome(String passwo
        if(index == password1.length())
            return true;
        if(table[index] == true)
            return recursivePolindrome(password1, table, ind

        char c = password1.charAt(index);

e.    for(int i = index + 1; i < password1.length(); ++i
        if (c == password1.charAt(i) && !table[i]) {
            table[i] = true;
            return recursivePolindrome(password1, table,
        }
    }

```

```

f.      if ( table [ password1 . length ( ) ] ) {
          table [ password1 . length ( ) ] = false ;
          return recursivePolindrome ( password1 , table , ind
        }

      return false ;
    }

```

**(a)** {string builder initialization have  $O(N)$ }

**(b)** { As we analyze in previous questions password1.toCharArray() have  $O(N)$  call one, Array initialization has  $O(N)$ (default value assignment) or  $O(1)$  depend on JVM, for have  $O(N)$ , inside of for there is only assignment that is  $O(1)$ . }

**(c)** { A recursive call that we will be analyze in the down, and println that have  $O(1)$ }

**(d)** {compression  $O(1)$  and continue recursion call }

**(e)** {have a loop iterates until find same character and do one more recursion call that call have  $O(N^2)$  in worst case time complexity, and  $O(N)$  best case time complexity, where  $N$  is length of password }

**(f)** { It is possible to work on one time for each check and continue the recursive call if work }

**(Conc.)** { In the worst case, have  $O(N^2)$  time complexity, where  $N$  is the length of password1 and in best case have  $O(N)$  time complexity }

**(Solution)**

isPalindromePossible function is  $O(N^2)$  worst case,  $O(N)$  best case (length of the password)

**Problem 5: isExactDivision**

(? points)

```

    static boolean isExactDivision(int password2, int
[] denominations) {
    // Check if password between 10 and 10000
    a.    if(password2 < 10 || password2 > 10000) {
        System.out.println("the password2 is invalid , it
        return false;
    }

    // Checks if password2 obtainable by summing denomin
    b.    if (!isExactDivisionRecursive(password2, denominat
        System.out.println("the password1 is invalid , it
        return false;
    }

    return true;
}

private static boolean isExactDivisionRecursive(int
password2, int [] denominations, int currentsum, int inde
c.    if(index != -1)
        currentsum += denominations[index];
    if (currentsum == password2)
        return true;
    if (currentsum > password2)
        return false;

d.    for (int i = 0; i < denominations.length; ++i) {
        if(isExactDivisionRecursive(password2, denominat
            return true;
    }
    return false;
}

```

(a) {Basic compression and print have  $O(1)$ }(b) { A recursive call that we will be analyze in the down below, and println that have  $O(1)$ }(c) { Basic compressions sum and assigment all of them have  $O(1)$ }

(d) {Each re-



*cursive call results in another loop that also executes  $n$  times, leading to a total of  $n^n$  iterations. This is because each recursive call iterates through the entire denominations array.*

**(Conc.)** { *In the worst case, have  $O(N^N)$  time complexity, where  $N$  is the length of denominations and in best case have  $O(1)$  time complexity.*

**(Solution)**

*isPalindromePossible function is  $O(N^N)$  worst case,  $O(1)$  best case (length of the denominations)*