



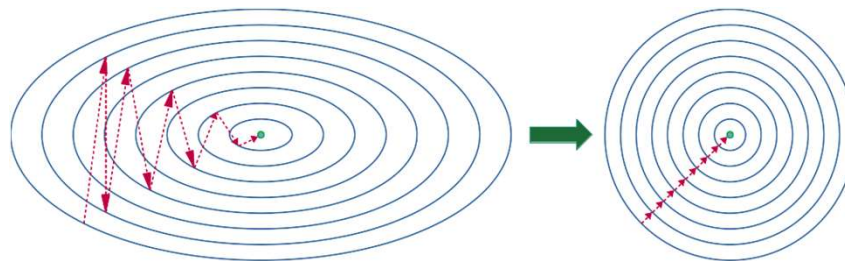
BATCH NORMALIZATION

Deep Neural Networks
Session 13
Pramod Sharma
pramod.sharma@prasami.com

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Batch Normalization

- ❑ It definitely helps to normalize input data
- ❑ Gradient converges faster

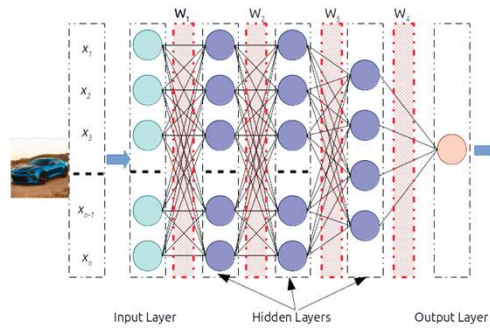


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Batch Normalization

- ❑ What about hidden layer?
- ❑ After all activations from previous layer are inputs for current layer...



- ❑ Will it help if we normalize the hidden layers too?

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Batch Normalization

- ❑ Batch normalization (also known as batch norm) [by Sergey Ioffe and Christian Szegedy in 2015]
 - ❖ Make artificial neural networks faster
 - ❖ More stable through normalization of the input layer by re-centering and re-scaling
 - ❖ Wider choices of hyper- parameter...
- ❑ In theory, its normalizing activation values of the respective layers
- ❑ In practice, it works better if we normalize 'z'
 - ❖ Look at the documentation for details

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Batch Normalization

- In General, any Z^i can be normalized

$$\text{mean } \mu = \frac{\sum Z^i}{m}$$

$$\text{std } \sigma^2 = \frac{1}{m} \sum (Z^i - \mu)^2$$

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Batch Normalization

- In General, any Z^i can be normalized

$$\text{mean } \mu = \frac{\sum Z^i}{m}$$

$$\text{std } \sigma^2 = \frac{1}{m} \sum (Z^i - \mu)^2$$

$$z^i_{\text{Norm}} = \frac{z^i - \mu}{\sqrt{\sigma^2}}$$

$$\hat{z} = \gamma \cdot z^i_{\text{Norm}} + \beta$$

- where γ and β are parameters, we can **Train**

Instead of using z^i_{Norm} , researchers realized that its better to derive \hat{z} with two trainable parameters.

Intuition is that by normalizing z , we are introducing bias in the system. Hence it makes sense to train these parameters

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$$\text{std } \sigma^2 = \frac{1}{m} \sum (Z^i - \mu)^2$$

$$z^i_{\text{Norm}} = \frac{z^i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

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- where γ and β are parameters, we can train

- if $\gamma = \frac{1}{\sqrt{\sigma^2 + \epsilon}}$ and $\beta = -\frac{\mu}{\sqrt{\sigma^2 + \epsilon}}$; $z^i_{\text{Norm}} = \hat{z}^i$

Lets add a small ϵ to prevent zero divide error...

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Batch Normalization

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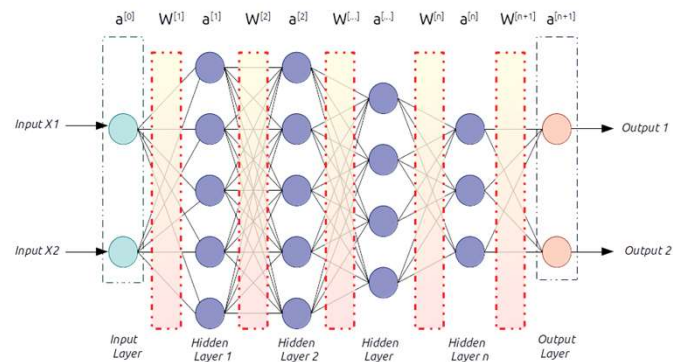
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Batch Normalization

Notes:

- ❖ Batch norm is used along with mini batches
- ❖ Batch norm is applied to the batch under consideration only irrespective of other mini batches

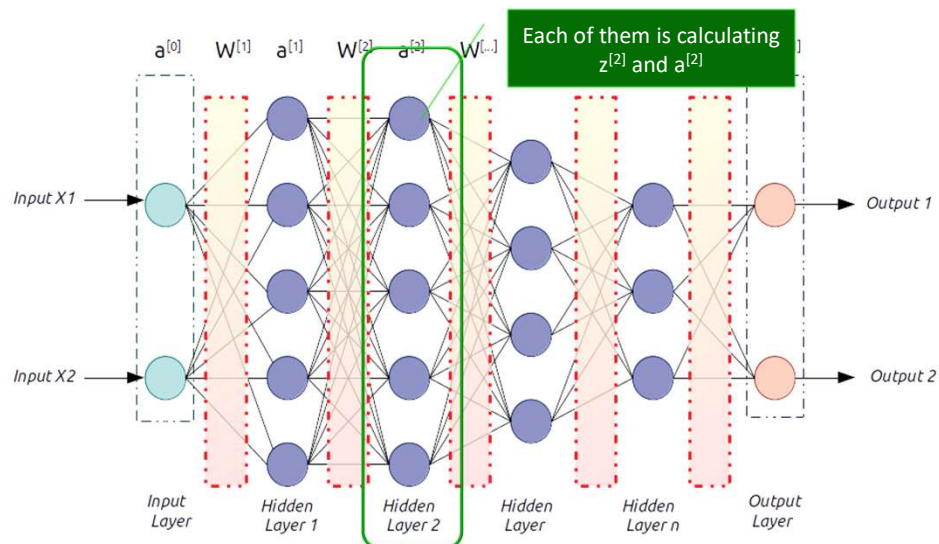
Where does it fit in overall scheme?



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Batch Normalization

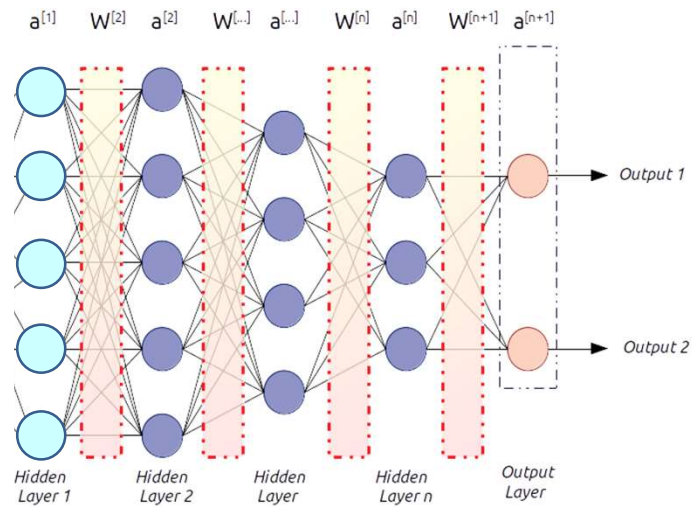


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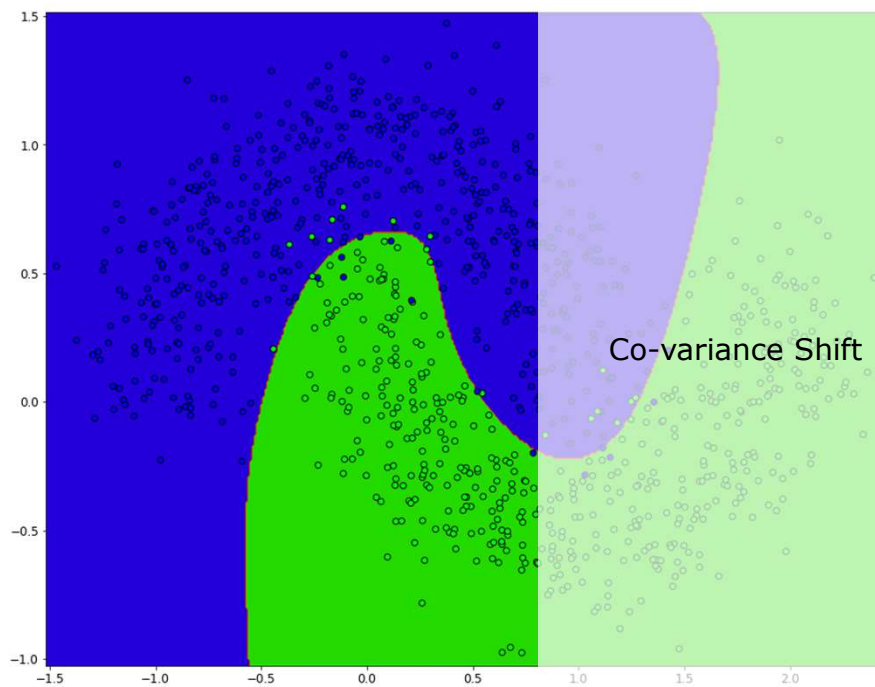
Batch Normalization

For $a^{[2]}$ all $a^{[1]}$ are acting
as input features



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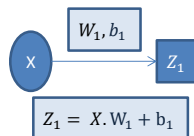


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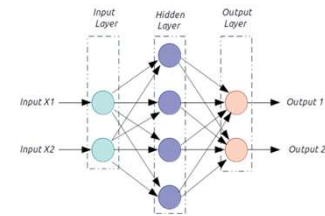
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Batch Normalization

- Forward and back propagation with batch norm:



Our standard equation to calculate z_1 .

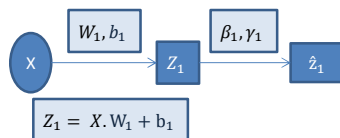


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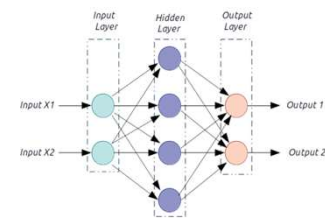
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Batch Normalization

- Forward and back propagation with batch norm:



Calculate \hat{z}_1 , based on β_1, γ_1

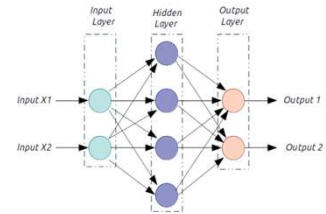
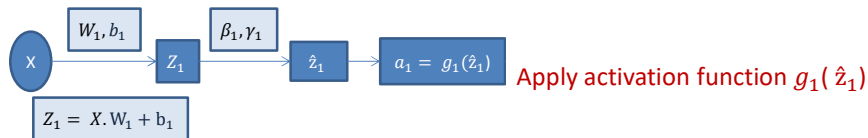


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Batch Normalization

- Forward and back propagation with batch norm:

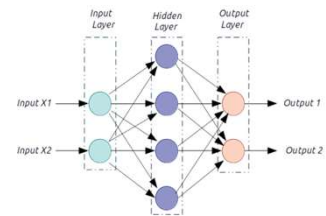
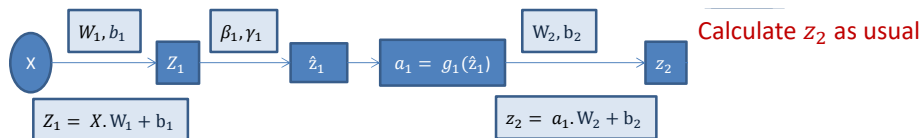


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Batch Normalization

- Forward and back propagation with batch norm:

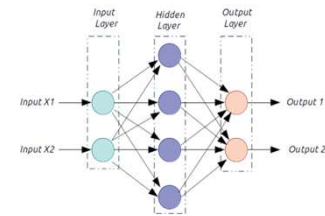
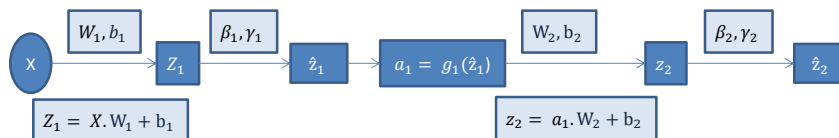


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Batch Normalization

- Forward and back propagation with batch norm:



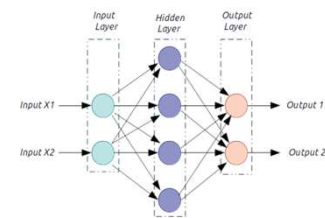
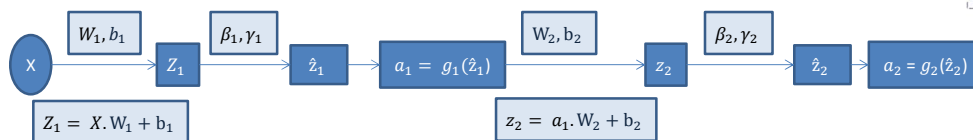
We know how to calculate \hat{z}_2

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Batch Normalization

- Forward and back propagation with batch norm:



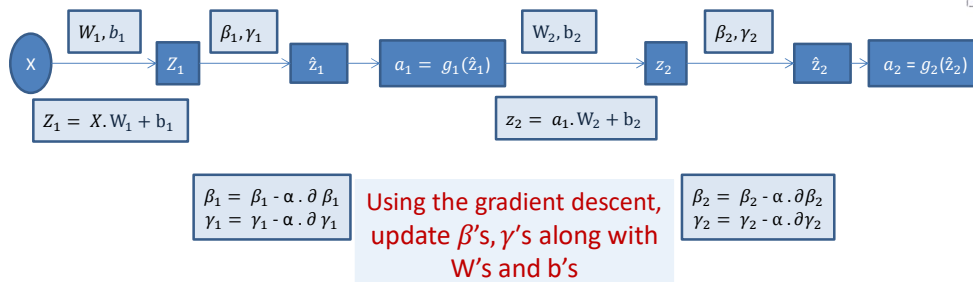
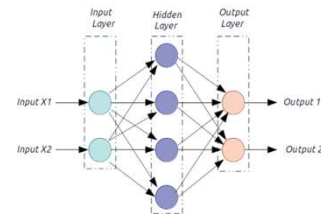
We also know how to calculate a_2

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Batch Normalization

- Forward and back propagation with batch norm:

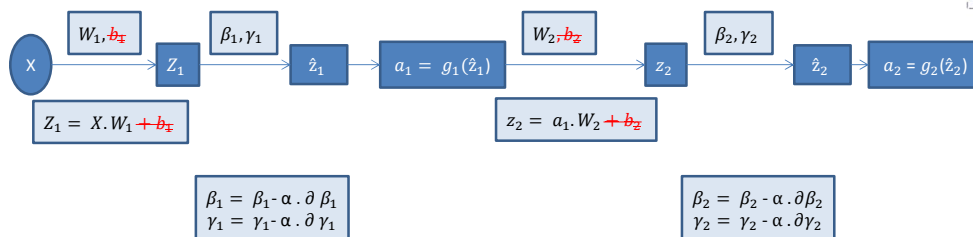
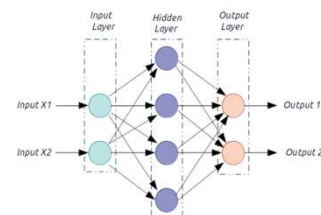


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Batch Normalization

- Forward and back propagation with batch norm:



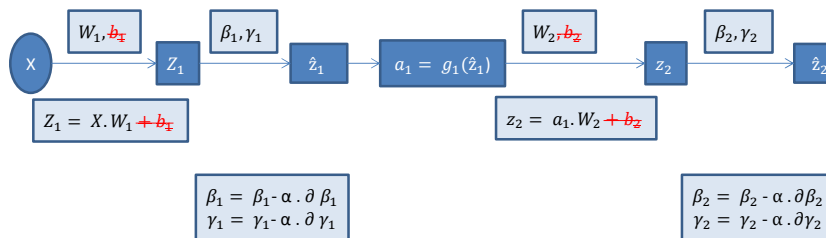
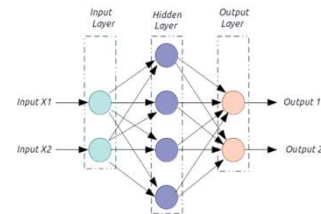
One more thing, since we are normalizing our Z's, keeping b's in the equation does not make any sense now.
Being the constant it will get eliminated!!

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Batch Normalization

- Forward and back propagation with batch norm:



And at test/validation time using a exponentially weighted average!
So while training do not forget to save exponentially weighted values or simply running average!!

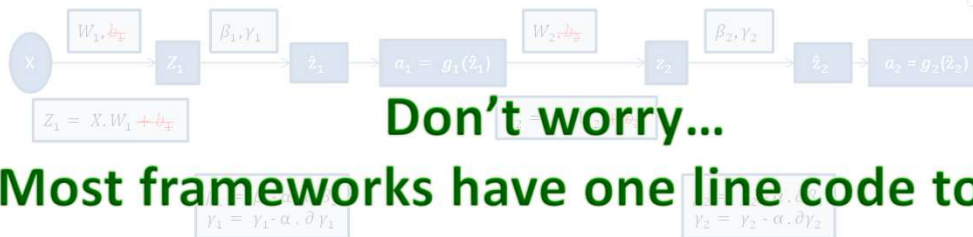
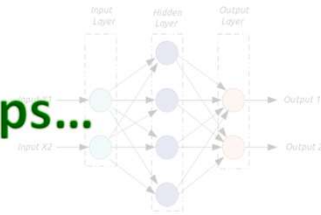
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Batch Normalization

- Forward and back propagation with batch norm:

Too many calculation steps...



Don't worry...

Most frameworks have one line code to do it.

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Batch Normalization – Code Sample

```
model = tf.keras.models.Sequential(
    [
        tf.keras.layers.RNN( keras.layers.LSTMCell(units), input_shape=(None, input_dim) ),
        tf.keras.layers.BatchNormalization(),
        tf.keras.layers.Dense(output_size),
    ]
)
```

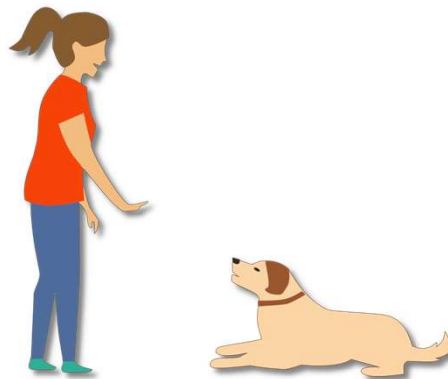
```
class Net(nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        self.dense1 = nn.Linear(in_features=320, out_features=50)
        self.dense1_bn = nn.BatchNorm1d(50)
        self.dense2 = nn.Linear(50, 10)
```

- ❑ And it is applied to **mini batches** only....
- ❑ Batch Norm can be updated using any of the optimization functions...

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Batch Normalization



Remember β, γ are parameters you train!

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