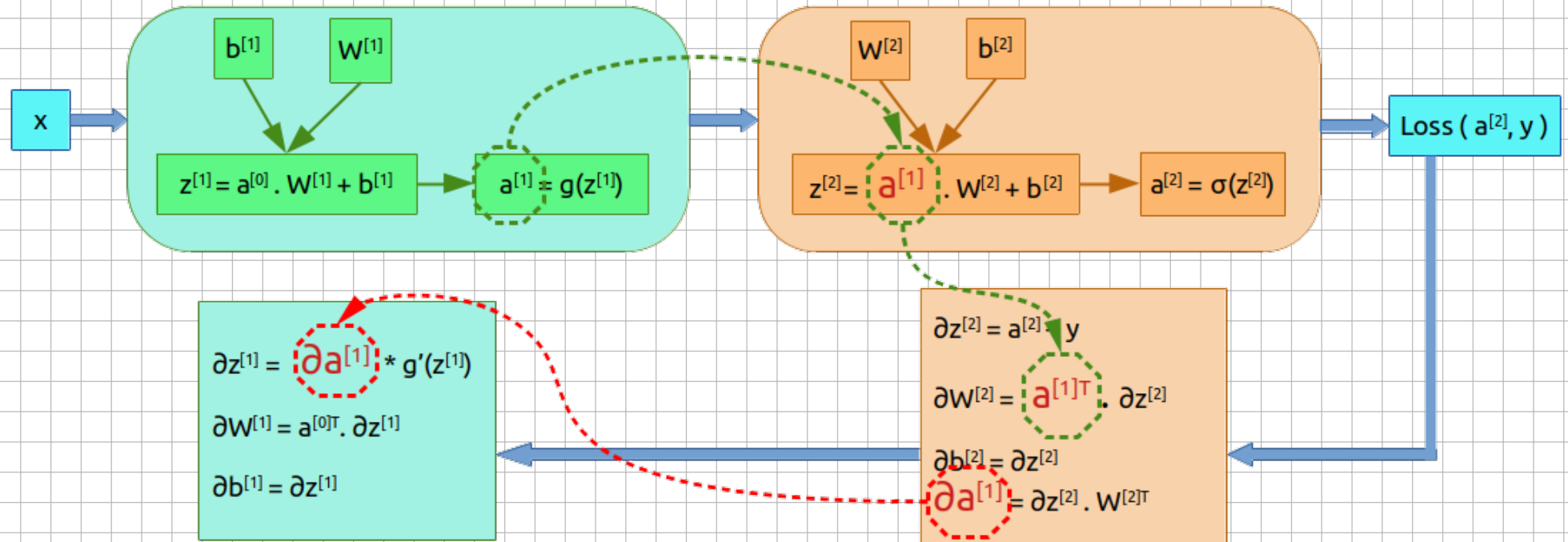


$$\begin{aligned}\frac{\partial \text{Loss}}{\partial z} &= \frac{\partial \text{Loss}}{\partial a} \cdot \frac{\partial a}{\partial z} = (a - y) \\ \frac{\partial \text{Loss}}{\partial W} &= a^T \cdot \frac{\partial \text{Loss}}{\partial z} \\ \frac{\partial \text{Loss}}{\partial b} &= \frac{\partial \text{Loss}}{\partial z}\end{aligned}$$

Forward Propagation



Back Propagation

$$\begin{aligned}\frac{\partial \text{Loss}}{\partial z^{[1]}} &= \frac{\partial \text{Loss}}{\partial z^{[2]}} \cdot \frac{\partial z^{[2]}}{\partial a^{[1]}} \cdot \frac{\partial a^{[1]}}{\partial z^{[1]}} = \frac{\partial \text{Loss}}{\partial a^{[1]}} \cdot g'(z^{[1]}) \\ \frac{\partial \text{Loss}}{\partial W^{[1]}} &= \frac{\partial \text{Loss}}{\partial z^{[1]}} \cdot \frac{\partial z^{[1]}}{\partial W^{[1]}} = a^{[0]T} \cdot \frac{\partial \text{Loss}}{\partial z^{[1]}} \\ \frac{\partial \text{Loss}}{\partial a^{[0]}} &= \frac{\partial \text{Loss}}{\partial z^{[1]}} \cdot \frac{\partial z^{[1]}}{\partial a^{[0]}} = \frac{\partial \text{Loss}}{\partial z^{[1]}} \cdot W^{[1]T} \\ \frac{\partial \text{Loss}}{\partial b^{[1]}} &= \frac{\partial \text{Loss}}{\partial z^{[1]}}\end{aligned}$$

$$\begin{aligned}\frac{\partial \text{Loss}}{\partial z^{[2]}} &= \frac{\partial \text{Loss}}{\partial a^{[2]}} \cdot \frac{\partial a^{[2]}}{\partial z^{[2]}} = (a^{[2]} - y) \\ \frac{\partial \text{Loss}}{\partial W^{[2]}} &= \frac{\partial \text{Loss}}{\partial z^{[2]}} \cdot \frac{\partial z^{[2]}}{\partial W^{[2]}} = a^{[1]T} \cdot \frac{\partial \text{Loss}}{\partial z^{[2]}} \\ \frac{\partial \text{Loss}}{\partial a^{[1]}} &= \frac{\partial \text{Loss}}{\partial z^{[2]}} \cdot \frac{\partial z^{[2]}}{\partial a^{[1]}} = \frac{\partial \text{Loss}}{\partial z^{[2]}} \cdot W^{[2]T} \\ \frac{\partial \text{Loss}}{\partial b^{[2]}} &= \frac{\partial \text{Loss}}{\partial z^{[2]}} \cdot \frac{\partial z^{[2]}}{\partial b^{[2]}} = \frac{\partial \text{Loss}}{\partial z^{[2]}}\end{aligned}$$

Feature			

Target

0  
1  
2  
1  
2  
0  
2

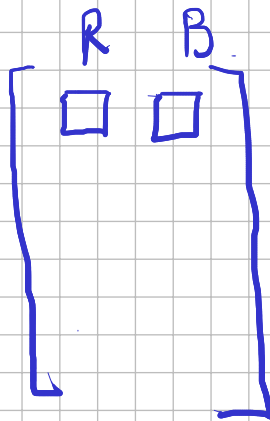
Sparse Rep.

1, 0, 0  
0, 1, 0  
0, 0, 1  
⋮

Dense Rep.

Softmax =

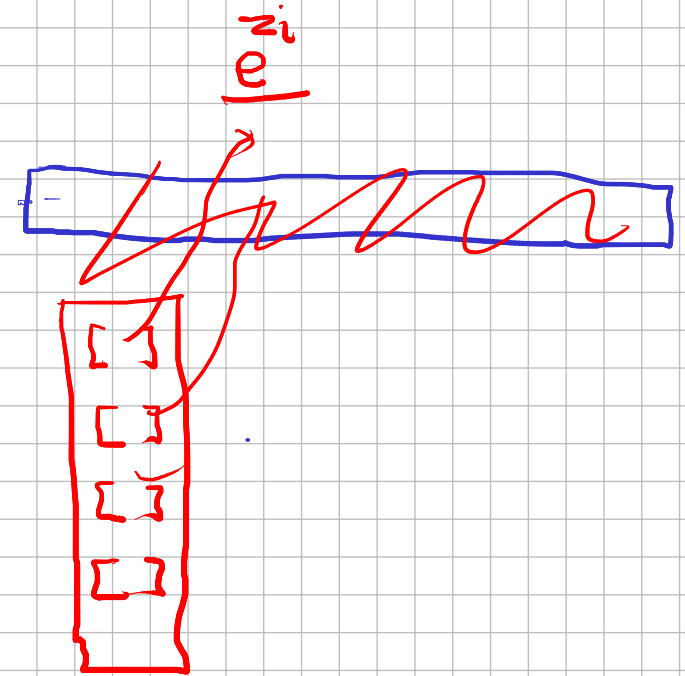
$$\frac{e^{z_i}}{\sum_{i=0}^n e^{z_i}}$$



n Class

m

=



$$\begin{matrix} & 0 & 1 & 2 \\ \begin{matrix} 0 \\ 1 \end{matrix} & \begin{bmatrix} 0.9 & 0.05 & 0.05 \\ 0.2 & 0.6 & 0.2 \end{bmatrix} \end{matrix} \rightarrow \text{A.argmax(axis)}$$