

Further down the rabbit hole.



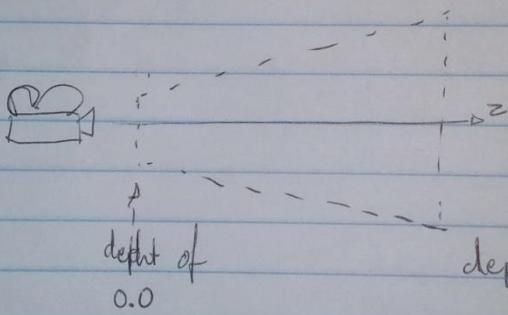
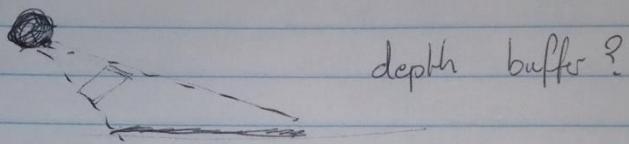
- Render cameras.

Tinae gave piece of advice
→ look at shadows.

- Using code instead.

◦ Render cameras \Rightarrow coding shaders were my largest gaps in knowledge.

- Unity uses a camera to determine shadows.



Depth is non-linear as closer objects need more detail → ask Tim.

It struggles when triangles are on top of each other.
↳ make sure tris not together
↳ increase res. of depth buffer

Note Unity uses Vulkan, not OpenGL

Z-buffer is an image space approach.
→ implemented in screen co-ordination system.

The basic idea is that to find closest z-depth surface.
Cross through every pixel,
frame buffer.

↳ stores the intensity
value of color (x, y)

depth buffer

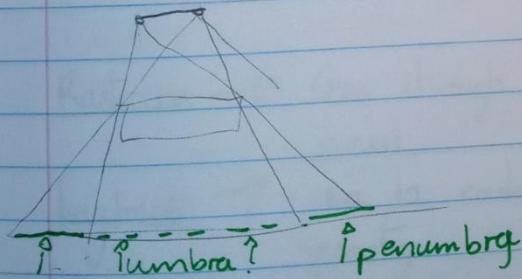
↳ values for (x, y)
 $(0 \leq \text{depth} \leq 1)$.

These processes happen for each polygon each of its pixels
then for each pixel.

→ is this each pixel of camera / screen. How does this translate for shadow rendering?

Fun fact: Couldn't do it before (IMB was big) but now we have terabytes of memory.

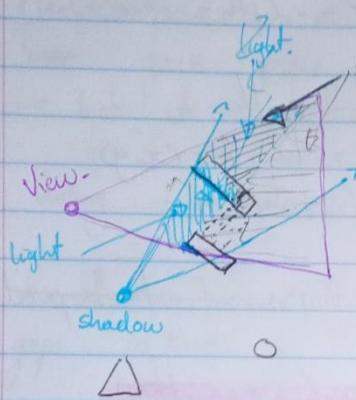
Softness in shadows



Depth buffer

Gl

Depth buffer + view camera.



- In each pixel we find if it is in shade **OR** not, change color accordingly.

How do view & shadow transfer/talk to each other
I am struggling with storage and use of shadow map information.

Using math magic the depth from the source is converted to position in view space.

HSL GLSL → These are what we use in Unity

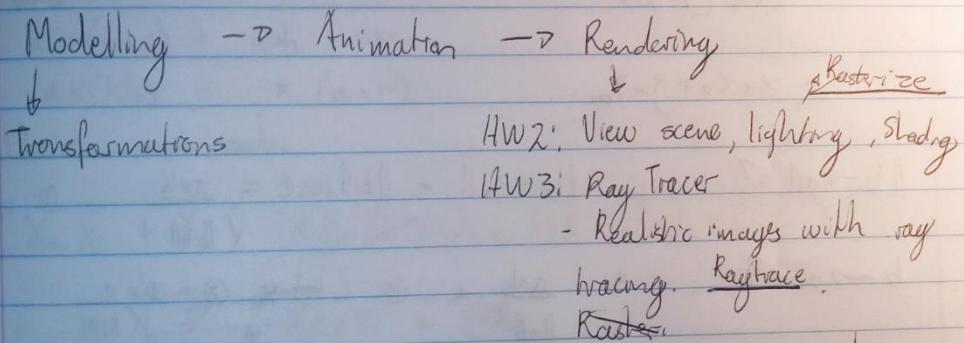
Rendering Engine T

EDX Course 2022/03/31
Computer Graphics

Using Open GL GLSL.
He developed spherical Harmonic lighting.
This course covers basics of computer graphics.

- We will write systems
- Theory of algorithms.

3D Graphics pipeline.



Rasterize → Goes through geometry { determines place on screen.

Raytrace → Goes to each point { finds corresponding geometry
Opposites of one another.

Game engines makes uses rasterization

Coding will be in C++ Yay!!!

Vectors $\xrightarrow{3}$ Matrices.

$$a \cdot b = ?$$

$$\|\vec{a}\| \|\vec{b}\| \cos \phi$$

$$\phi = \cos^{-1} \left(\frac{a \cdot b}{\|\vec{a}\| \|\vec{b}\|} \right)$$

$$a \cdot b = \begin{pmatrix} x_a \\ x_b \end{pmatrix} \cdot \begin{pmatrix} x_b \\ y_b \end{pmatrix} = ?$$

$$= x_a x_b (\vec{x} \cdot \vec{x}) + (\vec{x} \cdot \vec{y})$$

$$y_a y_b (\vec{y} \cdot \vec{y})$$

$$\therefore = x_a x_b + y_a y_b$$

$$\|\vec{b} - \vec{a}\| = ?$$

$$\|\vec{b} - \vec{a}\| = \|\vec{b}\| \cos \phi = \frac{a \cdot b}{\|\vec{a}\|} \quad \text{--- (1)}$$

$$\vec{b} - \vec{a} = ?$$

$$= \frac{a \cdot b}{\|\vec{a}\|^2} \vec{a} \quad \text{--- (2)} \quad (\cancel{\text{lost } \times} \quad (2) = (1) \times \frac{\vec{a}}{\|\vec{a}\|})$$

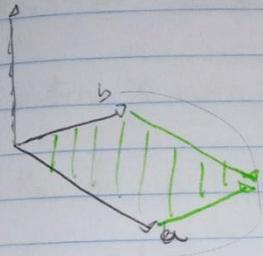
Question! L 291

mag of $i = 1$.

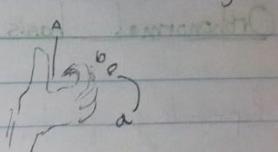
mag of $K = 1$.

Cross product

$a \times b = -b \times a$ = the area of the parallelogram made by $a \# b$.



it has a dir. $a \rightarrow b$ (right-hand)



$$a \times a = 0$$

$$a \times (b+c) = a \times b + a \times c$$

$$a \times (kb) = k(a \times b).$$

Derive cross prod.

$$(X_a \vec{x} + Y_a \vec{y} + Z_a \vec{z}) \times (X_b \vec{x} + Y_b \vec{y} + Z_b \vec{z}).$$

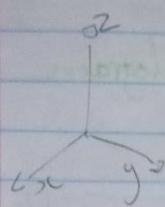
$$= X_a Y_b \vec{z} - Y_a X_b \vec{z} = \ell \vec{a}$$

$$a \times b = \begin{vmatrix} x & y & z \\ x_a & y_a & z_a \\ x_b & y_b & z_b \end{vmatrix} = \begin{bmatrix} y_a z_b - y_b z_a \\ z_a x_b - z_b x_a \\ x_a y_b - x_b y_a \end{bmatrix}$$

$$a \times b = A^* b = \begin{bmatrix} 0 & -z_a & y_a \\ z_a & 0 & -x_a \\ -y_a & x_a & 0 \end{bmatrix} \begin{bmatrix} x_b \\ y_b \\ z_b \end{bmatrix}$$

L2P2

transformations



Orthonormal basis

- Representing points, positions, locations
- There are many co-ord systems e.g. local, world.

Coordinate frame

↳ Any set of 3 vectors so that
 $\|u\| = \|v\| = \|w\| = 1$

$$u \cdot v = v \cdot w = w \cdot u = 0$$

$$u = u \times v$$

$$p = \dots$$

Matrices

- transform, translation, rotation etc.

Area of numbers m-rows, n-columns.

Matrix X matrix. multiplication.

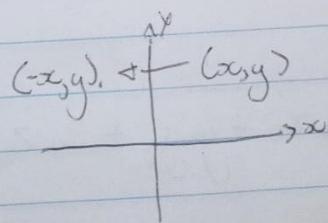
No. of n mat in first = No. m in second. \rightarrow Rule to mult.

$$1 \begin{pmatrix} 1 & 3 \\ 5 & 2 \\ 0 & 6 \end{pmatrix} \times \begin{pmatrix} 1 & 2 & 3 & 4 \\ 3 & 6 & 9 & 4 \\ 2 & 7 & 8 & 3 \end{pmatrix} = \begin{pmatrix} (1,1) & (1,2) & (1,3) & (1,4) \\ (2,1) & (2,2) & (2,3) & (2,4) \\ (3,1) & (3,2) & (3,3) & (3,4) \end{pmatrix}$$

Not commutative.

Matrix mult. is key for transformation.

e.g. Reflection about Y-axis (2-D).



$$= \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -x \\ y \end{bmatrix}$$

Trans

Transpose

Transpose of Matrix

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}^T = \begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{bmatrix}$$

$$(AB)^T = B^T A^T \quad (\text{have to flip order}) *$$

The identity matrix

$$I_{3 \times 3} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$AA^{-1} = A^{-1}A = I$$

$$(AB)^{-1} = B^{-1}A^{-1} \rightarrow (\text{change order}).$$

• Dot product.

$$(x_a, y_a, z_a) \begin{pmatrix} x_b \\ y_b \\ z_b \end{pmatrix} = (x_a x_b + y_a y_b + z_a z_b).$$

$$a \cdot b = a^T b.$$

• Cross product

$$a \times b = A^* b = \begin{bmatrix} 0 & -z_a & y_a \\ z_a & 0 & -x_a \\ -y_a & x_a & 0 \end{bmatrix} \begin{pmatrix} x_b \\ y_b \\ z_b \end{pmatrix}$$

- Wasted time getting VSCode C++ compatible with mingw. VS is already C++ compatible and got HWD to work.

HWD ✓ COMPLETE

L3V1: Transforms 1: Basic 2D Transforms

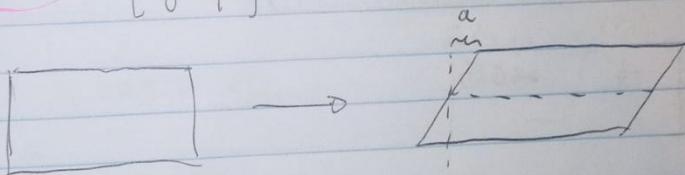
We have many different transf co-ord systems

- World, object, screen space

- To relate them, we transform between

Scale, rotation, translation, shear.

• Shear = $\begin{bmatrix} 1 & a \\ 0 & 1 \end{bmatrix}$

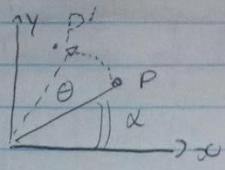


$$\begin{aligned} y' &= y && (y \text{ doesn't change}) \\ x' &= x + a y \end{aligned}$$

• Rotations $R(x+y) = R(x) + R(y)$ 2D.

In 2D they are commutative, in 3D they are not.

Rotations



$$P = r \cos \alpha, r \sin \alpha$$

$$P' = r \cos(\alpha + \theta), r \sin(\alpha + \theta)$$

polar
co-ord.

$$P'_x = \underline{r \cos \alpha \cos \theta} + \underline{r \sin \alpha \sin \theta} \quad \text{Ans: (V.E.) V.E. 1}$$

$$P'_x = x \cos \theta - y \sin \theta$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\text{Ex: } \vec{i}' = \begin{pmatrix} 4, 0 \\ 3, 0 \end{pmatrix}$$

$$Q: \begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{bmatrix} \cos(183) & -\sin(183) \\ \sin(183) & \cos(183) \end{bmatrix} \begin{pmatrix} 4 \\ 3 \end{pmatrix}.$$

$$\vec{j}' = \begin{bmatrix} (1, 1) & (1, 2) \\ -4 & 230.5 \end{bmatrix}$$

$$A: \vec{j}' = \begin{pmatrix} -3.83751 \\ -3.205 \end{pmatrix}$$

Composing Transformations L3V2

e.g. scale it, move it, rotate it.

polar
co-ords

NB: Not commutative.

$$x_3 = Rx_2 \quad x_2 = Sx_1$$
$$x_3 = R(Sx_1) = (RS)x_1$$

$x_3 \neq SRx_1 \rightarrow$ Cannot change order

Convert Composite matrix

$$M = M_1 M_2 M_3 \quad (M_3 \text{ is the first transformation})$$

$$M^{-1} = M_3^{-1} M_2^{-1} M_1^{-1}$$

$$M^{-1}M = I$$

Ques Cathn $x_n = \frac{1 + 180 \times 180}{2}$

$$16290 \div 360$$

=

3D Rotations L3V3

Rot

Rows of

$$R_p = \begin{bmatrix} x_u & y_u & z_u \\ x_v & y_v & z_v \\ x_w & y_w & z_w \end{bmatrix} \begin{pmatrix} x_p \\ y_p \\ z_p \end{pmatrix}$$
$$= \begin{pmatrix} u \cdot p \\ v \cdot p \\ w \cdot p \end{pmatrix}$$

- Rows of 3 unit vectors
- rotation matrix of 3 ortho normal.

Rotations not commutative (e.g. x axis then y axis).

* [Axis angle $R(a, \theta) = I_{3 \times 3} \cos \theta + aa^T(1 - \cos \theta) + A^* \sin \theta$]

Derivation of Axis angle = hard.

Rodrigues rotation formula.

* Not going to spend time on this - we use Quaternions in Unity.

Q: Using the Rodrigues Rotation form, what effect does negating the axis of rotation have?

L4 VI Trs2 : Homogeneous Co-ords.

(we start HWI after this,

Translation. (moving an object.)

$$\begin{pmatrix} x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ ? & ? & ? \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} x+5 \\ y \\ z \end{pmatrix}$$

To solve we add a 4th homogeneous coord.

in 3D

$$\begin{pmatrix} x' \\ y' \\ z' \\ w' \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ w=1 \end{pmatrix} = \begin{pmatrix} x+5 \\ y \\ z \\ 1 \end{pmatrix}$$

Homogeneous point doesn't matter till end. divide by w to get it.

$w=0 \rightarrow$ This is vector

When we find point to display \rightarrow we do homogenize.
The advantage is division is only done once.

General translation matrix

$$T = \begin{pmatrix} 1 & 0 & 0 & T_x \\ 0 & 1 & 0 & T_y \\ 0 & 0 & 1 & T_z \\ 0 & 0 & 0 & 1 \end{pmatrix} = \begin{bmatrix} I_3 & T \\ 0 & 1 \end{bmatrix}$$

$$P' = TP = P + T \quad (\text{Point} + \text{translation})$$

Translation \nmid Rot. not commutative.

$$P' = (TR)P = MP = RP + T$$

Note: Nice course but
not getting me
less to shake
through.

$$\begin{pmatrix} I_{3 \times 3} & T \\ 0 & 1 \end{pmatrix} \begin{pmatrix} R_{3 \times 3} & 0 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} R_{3 \times 3} & T_{3 \times 1} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} P \\ 1 \end{pmatrix} = \begin{pmatrix} R_{3 \times 3}P + T \\ 1 \end{pmatrix}$$

The conclusion of the lecture is that if
rotate before translate rotate before translate, it will
affect the translation.

Qn). $R^2 i = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$.

$$RF+T. \quad \vec{j} = R(178)T(2, 9, 0)\vec{i}$$

$$\vec{k} = T(2, 9)R(178).$$

A). $\vec{j} = RTP$

$\sim RT + RT \rightarrow$ so we rotate point \nmid translation

$$RF = \begin{bmatrix} \cos(178) & -\sin(178) \\ \sin(178) & \cos(178) \end{bmatrix} \begin{bmatrix} & \\ & \end{bmatrix}$$

$$RP = \begin{bmatrix} \cos(178) & -\sin(178) \\ \sin(178) & \cos(178) \end{bmatrix} \begin{pmatrix} 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$RT = \begin{bmatrix} \cos(178) & -\sin(178) \\ \sin(178) & \cos(178) \end{bmatrix} \begin{pmatrix} 2 \\ 9 \end{pmatrix}$$

$$\approx \begin{bmatrix} -2.31 \\ -4.92 \end{bmatrix}$$

$$RP + RT = \begin{pmatrix} 0 \\ 0 \end{pmatrix} + \begin{pmatrix} -2.31 \\ -8.91 \end{pmatrix}$$

$$\vec{j} = (-2.31, -8.91).$$

$$\underline{\vec{k}} = (T R) R$$

$$= R(TP),$$

$$\therefore \begin{pmatrix} 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 2 \\ a \end{pmatrix}$$

$$TP = \begin{pmatrix} 2 \\ a \end{pmatrix}$$

$$R(TP) =$$

b) What we did wrong!!!
Appy transforms from right to left.

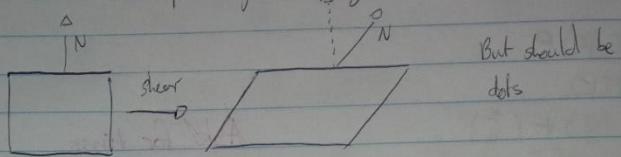
$$\text{So } \vec{j} = P \xrightarrow{\text{translate}} P' \xrightarrow{\text{Rotat}} P''$$

$$\vec{k} = P \xrightarrow{\text{Rotat}} P' \xrightarrow{\text{Translate}} P''$$

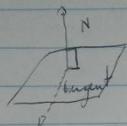
Decision: Going to take a break from maths
↳ code in shaders for a while.

Transforming Normals

This is used for light intensity



But should be dots



$$t \rightarrow Mt$$

$$n \rightarrow Qn$$

$$n^T t = 0$$

M is surface transform

$$Q = ?$$

$n^T t = 0$ (90° is one angle)

$$(Qn)^T = (n^T Q^T) t^T M t = 0$$

$$(n^T Q^T M t) = 0 \Rightarrow Q^T M = I$$

$$Q = (M^{-1})^T$$

$-T$ \hookrightarrow applies to upper

3×3 only

Only affects shear $\begin{cases} \text{Scaling} \\ \text{Rotation} \end{cases}$

not translation

$$[Q = (M^{-1})^T]$$

[Qu: 3D rotation $M = R(\vec{a}, \theta)$ what is normal
transform, Q ?

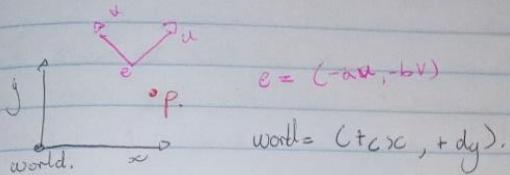
$$= R(\vec{a}, \theta)$$

$M = Q$ Does rotation affect
normals?

4.13 Coord frames

$$\begin{array}{c} P(2,1) \\ \downarrow \\ \text{world.} \end{array} \Rightarrow \begin{array}{c} P'(4) \\ \downarrow \\ \text{world.} \end{array} \equiv \begin{array}{c} P''(3) \\ \vdots \\ \text{world.} \end{array}$$

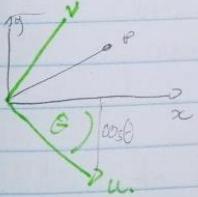
Coord \Rightarrow location?



Remember rotation by angle α produces $\begin{pmatrix} P' \\ \alpha \end{pmatrix}$

$$R = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$$

But we can rotate coord system.



$$R = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix} u$$

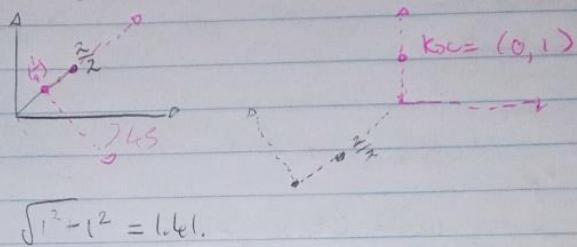
Axis angle Remember

$$R(a, \theta) = I_{3 \times 3} \cos\theta + aa^T(1 - \cos\theta) + A^* \sin\theta$$

$$R(\theta) = \cos\theta \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + (1 - \cos\theta) \begin{bmatrix} x^2 & xy & xz \\ yx & y^2 & yz \\ zx & zy & z^2 \end{bmatrix} + \sin\theta \begin{bmatrix} 0 & -z & y \\ z & 0 & -x \\ -y & x & 0 \end{bmatrix}$$

Ques:

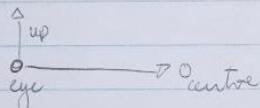
$\vec{i} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$
 $i = \begin{pmatrix} 2 \\ 2 \\ 2 \end{pmatrix}$ What are the coordinates in new coordinate system with origin $\vec{j}(1)$? \vec{j} axis angle 28.45°



$$\sqrt{1^2 + 1^2} = 1.41.$$

L4 V4 Constructing a coordinate frame.

eye x, y, z centre x, y, z up x, y, z



- 1- Create coordinate frame for camera
- 2- Define rotation matrix
- 3- Apply translation for camera

Associate w with $a \& b$.

$$w = \frac{a}{\|a\|}$$

$$u = \frac{b \times w}{\|b \times w\|}$$

$$v = w \times u$$

a is eye

b up vector

What is Orthonormal again?

Orthogonal \equiv $w \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ or v
Unit $\|w\| = 1$ [0]
or $\begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{2} \end{bmatrix}$

- all vectors are unit vectors.
- all vectors are orthogonal to one another
- linearly independent

{

What is linear independence?

if no vectors can be expressed by one another,
they are linearly ind.

$\vec{v}_1, \vec{v}_2, \vec{v}_3, \dots, \vec{v}_n$ in vector space V

for linear independence in the foll. equa. all scalars
must be zero.

$$c_1 \vec{v}_1 + c_2 \vec{v}_2 + \dots + c_n \vec{v}_n = \vec{0}$$

If non-zero scalars exist then it is not linearly
independent

Why do we want linear indep.

for a basis like $x \not\parallel y$ to span cell
of 2D space they must be linearly indep.
if either of them lie parallel / all in some plane
then can't span all of 3D space.

6

Back to lecture.

Rotation matrix.

$$R_{uvw} = \begin{bmatrix} x_u & y_u & z_u \\ x_v & y_v & z_v \\ x_w & y_w & z_w \end{bmatrix} \quad w = x_u X + y_u Y + z_u Z$$

- Cannot apply translation after rotation.
- Translation first.

$$P' = (RT)P = RP + RT$$

$$M = \begin{bmatrix} R_{3 \times 3} & R_{3 \times 3} T_{3 \times 1} \\ 0_{1 \times 3} & 1 \end{bmatrix}$$

$$At = \begin{bmatrix} x_u & y_u & z_u & 0 \\ x_v & y_v & z_v & 0 \\ x_w & y_w & z_w & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -ex \\ 0 & 1 & 0 & -ey \\ 0 & 0 & 1 & -ez \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{array}{l} -u.e \\ -v.e \\ -w.e \end{array}$$

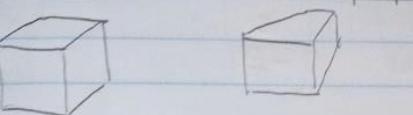
The gluLookAt matrix ~~can be~~ thought of as translating the world so that the camera is at origin. Then rotate new origin ~~despite~~ the direction camera will be looking at. \rightarrow -z in OpenGL
 This would be camera space.

L5V1: Viewing : Orthographic projection

6d 3 hours.

All of our calculations & workings are in 2D but view in 2D.

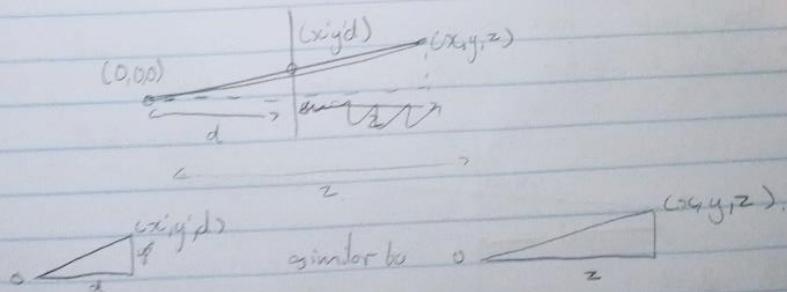
So we must project the 3D world to a 2D space.



To do this we translate to origin then scale

$$g_{\text{ortho}} = \begin{pmatrix} \frac{2}{f-n} & 0 & 0 & -\frac{r+n}{r-n} \\ 0 & \frac{2}{b-n} & 0 & -\frac{b+n}{b-n} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

L5V2: Perspective projection



$$\therefore \frac{d}{x'} = \frac{z}{z} \Rightarrow x' = \frac{d \cdot x}{z}$$

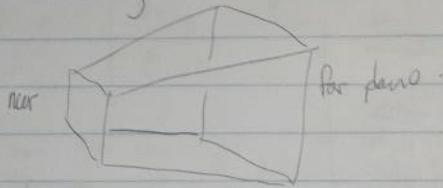
NB.

$$y = \frac{d \cdot y}{z}$$

$$P = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -\frac{1}{d} & 0 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ w=1 \end{pmatrix} = \begin{pmatrix} x \\ y \\ z \\ -\frac{z}{d} \end{pmatrix} \text{ dehomogenize} = \begin{pmatrix} -x \frac{d}{z} \\ -y \frac{d}{z} \\ -\frac{z}{d} \\ 1 \end{pmatrix}$$

Derivation of glu Perspective.

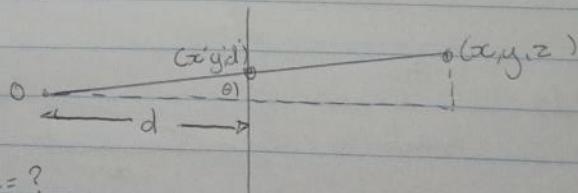
Viewing Frustum.



$$\text{Aspect} = \frac{\text{width}}{\text{height}}$$

glu Perspective (fovY, aspect, zNear > 0, zFar > 0).

- ↳ fovY, aspect form in x^3y
- ↳ $z_{\text{Near}}, z_{\text{far}}$ control viewing frustum



$$\theta = ? \quad d = ?$$

$$\text{fovY} =$$

$$\theta = \frac{\text{fovY}}{2} \quad d = \cot(\theta)$$

In Matrices

Simplest form.

$$P = \begin{bmatrix} \frac{1}{\text{aspect}} & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -\frac{1}{2} & 0 \end{bmatrix} *$$

Multiply by d. ↴ ↵ perspective.

$$Pd = \begin{bmatrix} \frac{d}{\text{aspect}} & 0 & 0 & 0 \\ 0 & d & 0 & 0 \\ 0 & 0 & A & B \\ 0 & 0 & -1 & 0 \end{bmatrix} \xrightarrow{\text{still homogeneous.}} z_w$$

$\Rightarrow A \setminus B$ sends $n \setminus f$ to $-1, +1$.

$$\begin{pmatrix} A & B \\ -1 & 0 \end{pmatrix} \begin{pmatrix} z \\ 1 \end{pmatrix} = ? \approx \begin{pmatrix} Az + B \\ -z \end{pmatrix} = -A - \frac{B}{z}$$

$$z = -n \rightarrow -1 \quad \therefore -A + \frac{B}{n} = -1$$

$$z = -f \rightarrow +1 \quad \therefore -A + \frac{B}{nf} = +1.$$

$$\therefore A = \frac{f+n}{f-n}$$

* Note need to research this more

$$B = \frac{-2fn}{f-n}$$

Depth check

Mapping of z is non-linear.

→ handles large range of depth.

→ Depth res. not uniform.

Do not set near clipping to 0.

HWI = This is my hand in.

Step 1 - fix VS, Took 2 hrs total, no sln.

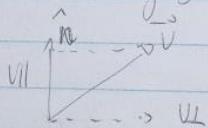
had to download & install VS 2022.

VS 2016 kept making file paths that don't exist.

Let's rotate GL

$$\text{Rotation matrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \cdot \begin{bmatrix} x \\ y \end{bmatrix}$$

Need to use Rodrigues rotation.



$$\begin{aligned}\vec{v}' &= \vec{v}_n + \cos(\theta) \vec{v}_L + \sin(\theta) (\hat{n} \times \vec{v}_L) \\ &= \vec{v}_n + \cos(\theta) (\vec{v} - \vec{v}_n) + \sin(\theta) (\hat{n} \times \vec{v}) \\ &\quad \cancel{\hat{n} \times \vec{v}} = \hat{n} \times (v_L + \vec{v}_n) \\ &= (1 - \cos(\theta)) \vec{v}_n + \cos(\theta) \vec{v} + \sin(\theta) (\hat{n} \times \vec{v})\end{aligned}$$

9-3

6.

$$\vec{U}_n = a\hat{n} \quad a = (\vec{V} \cdot \hat{n})$$

$$\therefore \vec{V}_n = (\vec{V} \cdot \hat{n})\hat{n}$$

$$[\vec{V}' = (1 - \cos(\theta))(\vec{V} \cdot \hat{n})\hat{n} + \cos(\theta)\vec{V} + \sin(\theta)(\hat{n} \times \vec{V})]$$

$$R(a, \theta) = \cos \theta \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + (1 - \cos \theta) \begin{bmatrix} x^2 & xy & xz \\ yx & y^2 & yz \\ zx & zy & z^2 \end{bmatrix} + \sin \theta \begin{bmatrix} 0 & -z & y \\ z & 0 & -x \\ -y & x & 0 \end{bmatrix}$$

Row 3 column
Vectors handled by GotoL

$$(x, y, z) \begin{pmatrix} x \\ y \\ z \end{pmatrix} \begin{array}{c} x^2 & xy & xz \\ yx & y^2 & yz \\ zx & zy & z^2 \end{array}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} (xyz).$$

There is no support to do a $3 \times 1 * 3 \times 3$
so custom matrix.

NOW there is an error mat[3][0] = anything

NO documentation on how to set matrix.

a is given as eye-center
b = up.

$$w = \frac{a}{\|a\|}$$

$$R = \begin{matrix} \text{row} \\ \begin{bmatrix} x_u & y_u & z_u \\ x_v & y_v & z_v \\ x_w & y_w & z_w \end{bmatrix} \end{matrix}$$

$$u = \frac{b \times w}{\|b \times w\|}$$

$$v = w \times u$$

Most of this is struggling
with custom library lib.
Like vec3 doesn't have a
size().

loop through a divide by may = w.

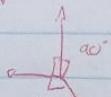
Note: I discovered that the program uses
a custom GLM library, which has made coding
difficult as it is quite different from C++

U. Find cross, loop ? divide.

XD. \rightarrow There is a normalize function in GLM.

Time-wasted

Many cross product to give orthonormal basis



How do I add a row to a matrix!?

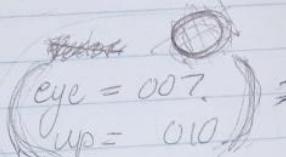
argenthian

Code does not work as expected.

Going to make functions to output
matrix & vectors.

$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$

Create 4 func \rightarrow display vec $\vec{3}$
vec $\vec{4}$
mat $\vec{3}$
mat $\vec{4}$.

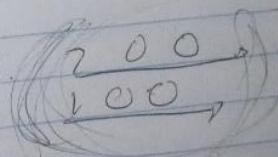
as ~~eye~~  \Rightarrow $w = 0\ 0\ 1$
 $u = 1\ 0\ 0$
 $v = 0\ 1\ 0$.

$$\frac{\textcircled{1} \textcircled{2} \textcircled{3}}{r^2}$$
$$= (0, 0, 143)$$
$$= 0, 0, 1$$

$$0\ 1\ 0 \times 0\ 0\ 1$$
$$cx = aybz - azby = 1 \times 1 - 0 \times 0$$
$$= 1$$

$$cy = azbx - axbz = 0 \times 0 - 0 \times 0$$
$$= 0$$

$$cz = axby - aybx = 0 - 0$$
$$= 0$$





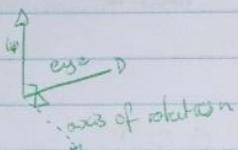
No i: left / Right

Just going to use unchanged Rodrigues formula
don't see why we need to muddle things up with
matrices.

Look Up

Quick 3D.T.Y.

axis of rotation = up \times eye.



Something funky but need to do report.