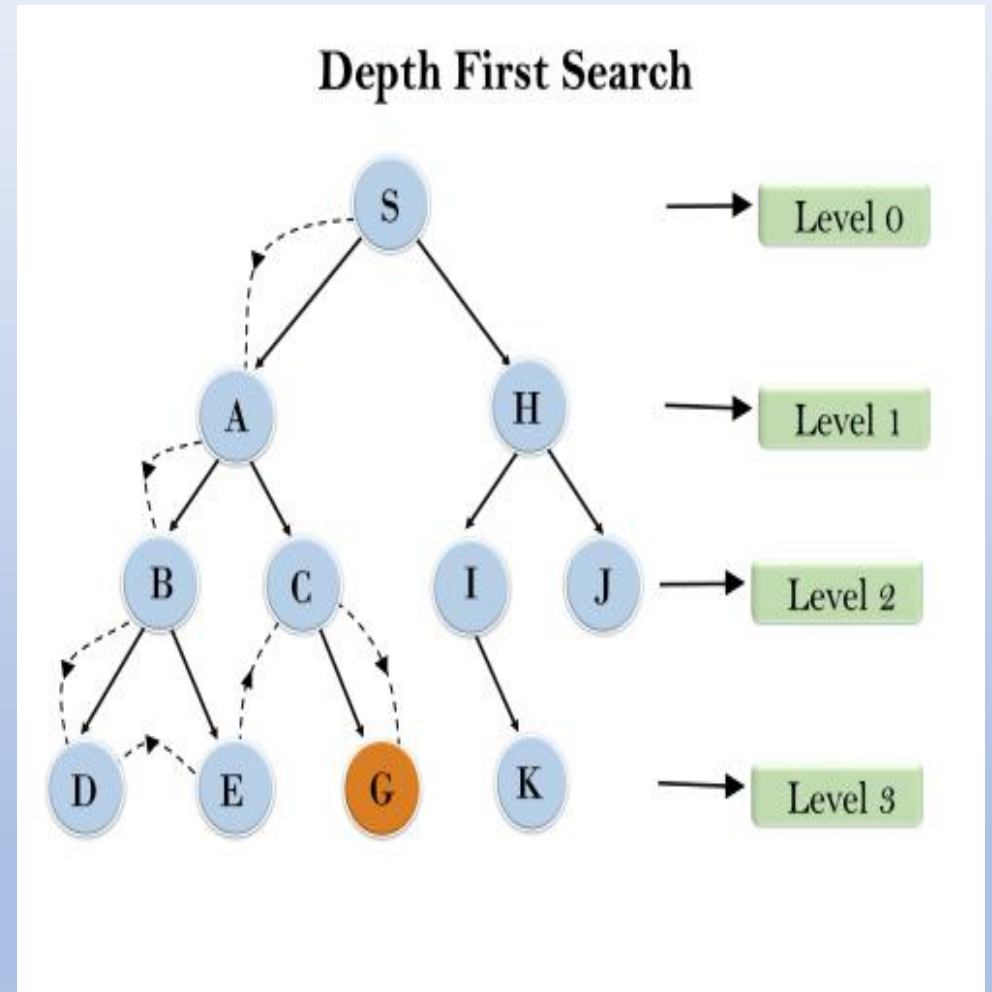


# Uninformed Search

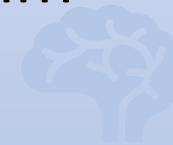
## Unit 2: Uninformed Search Strategy





# Table of Content

- Implicit and Explicit Search
- General Search tree algorithm
- Performance measuring criterion of an algorithm
- Uninformed Search tree
- Breadth first Search(BFS)
- Depth First Search(DFS)



# Search



Searching through a state space involves the following:

- A set of states
- Operators and their cost
- Start state
- A test to check for goal state



# Explicit and Implicit Search Tree



- Explicit Search tree:
  - Explicit representation of node set and edges
  - Store in memory
- Implicit Search tree:
  - Graph is too large to generate and store in memory
  - Nodes are generated as they are explored.



# General Search tree algorithm

Function `tree_search(problem, strategy)` return a solution or failure

Initialize the search tree using the initial state

Loop do

- If there are no candidates for expansion then return failure

- Choose a leaf node for expansion according to strategy

- If node contains a goal state then return the corresponding solution

- Else expand the node and add the resulting nodes to the search tree

# Measuring Problem Solving Performance

- Completeness: algorithm guaranteed find a solution when there is one.
- Optimality: does the strategy find optimal solution
- Time Complexity: how long does it takes to find solution
- Space Complexity: how much memory is needed to perform a search

# Uninformed Search or Blind Search

- No clue whether one non goal state is better than any other
- Don't know if your current exploration is likely to be fruitful.
- Search is blind
- Example:
  - Breadth First Search
  - Depth First Search
  - Iterative Deepening Search
  - Bi-directional Search

# Search Tree Terminology

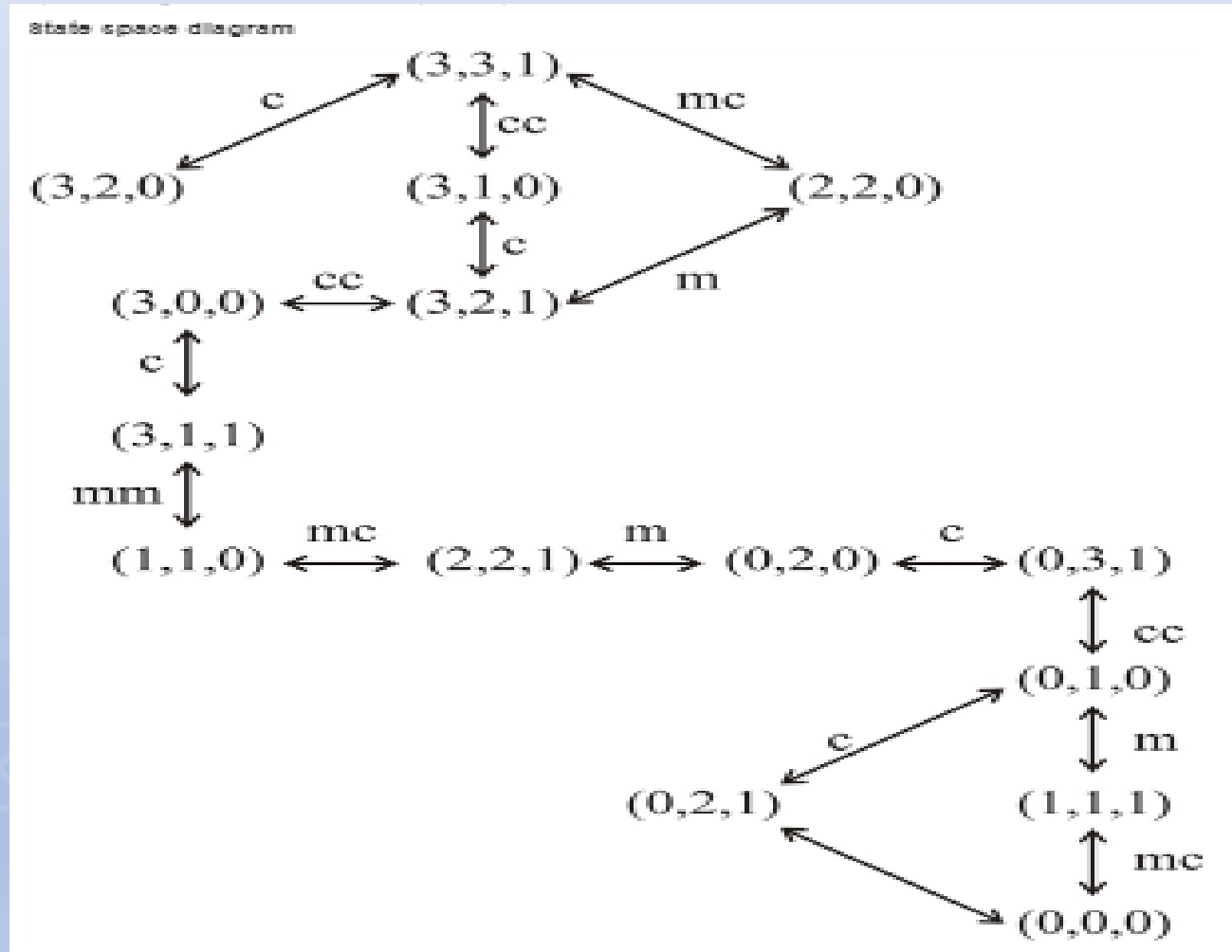


- The search start with initial state or root node
- The OPEN set contains the generated nodes.
- The algorithm picks one node from OPEN, expand it and keep it in CLOSED
- A solution to the search problem is a sequence of operators.
- Search tree may be infinite because of loops even the number of states is small





# Search Tree: Missionaries and Cannibals problem



# Breadth First Search (BFS)



Let OPEN/fringe be a list containing the initial state

Loop

if OPEN/fringe is empty return failure

Node  $\leftarrow$  remove-first (fringe)

if Node is a goal

then return the path from initial state to Node

else

generate all successors of Node,

add generated nodes to the back of fringe

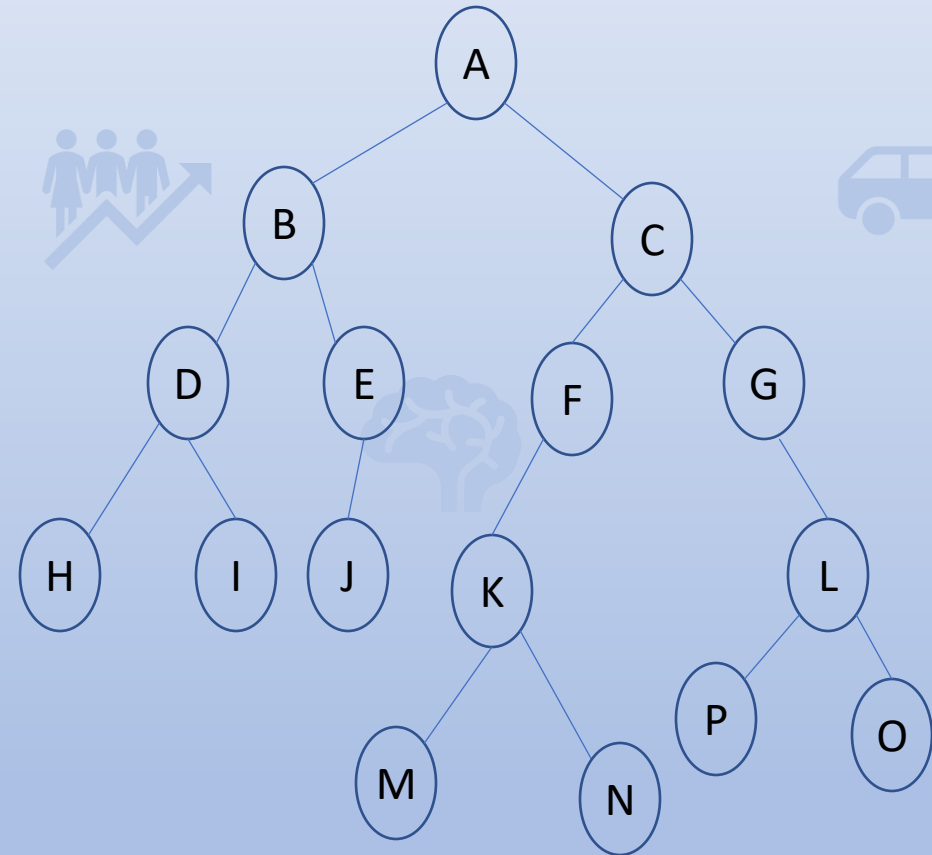
End Loop

# Breadth First Search (BFS)

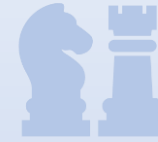
Start State: A

Goal State: G

OPEN	CLOSED
A	
B,C	A
C,D,E	A,B
D,E,F,G	A,B,C
E,F,G,H,I	A,B,C,D
F,G,H,I,J	A,B,C,D,E
G,H,I,J,K	A,B,C,D,E,F
G,H,I,J,K	A,B,C,D,E,F,G



# Depth First Search (DFS)



Let OPEN/fringe be a list containing the initial state

Loop

if OPEN/fringe is empty return failure

Node  $\leftarrow$  remove-Last (fringe)

if Node is a goal

then return the path from initial state to Node

else

generate all successors of Node,

add generated nodes to the back of fringe

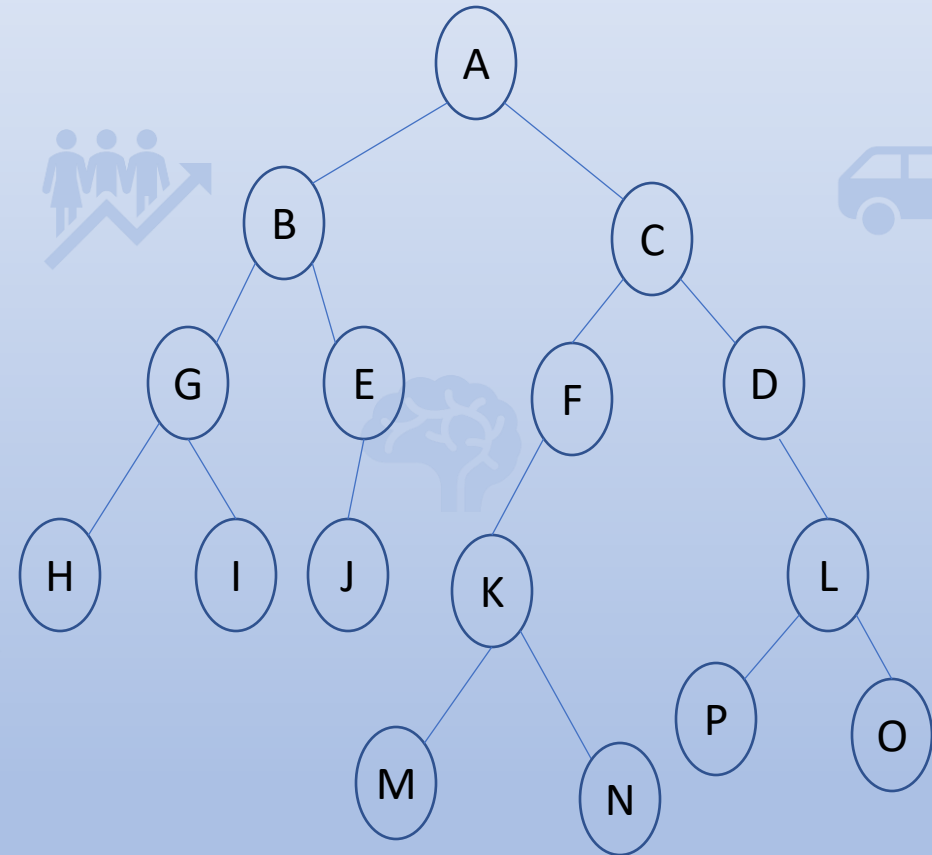
End Loop

# Depth First Search (BFS)

Start State: A

Goal State: G

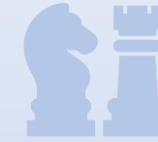
OPEN	CLOSED
A	
B,C	A
B,F,D	A,C
B,F,L	A,C,D
B,F,P,O	A,C,D,L
B,F,P	A,C,D,L,O
B,F	A,C,D,L,O,P
B,K	A,C,D,L,O,P,F





# Time Complexity of BFS

- Progress of the search is a simple complete binary search tree.
- How much memory it will take to execute
- Every state has  $b$  child(say)
- Root of the search tree generate  $b$  nodes at the first level.
- $b^2$  nodes generated at second level.
- Let the solution of the problem has a path length of  $d$
- The maximum numbers of nodes expanded before finding a solution is
- $1+b+b^2+b^3+\dots+b^d$



# Time Complexity of BFS

- The time and space required for BFS is  $O(b^d)$
- The following figure represent the time and space requirement for BFS with branching factor  $b=10$

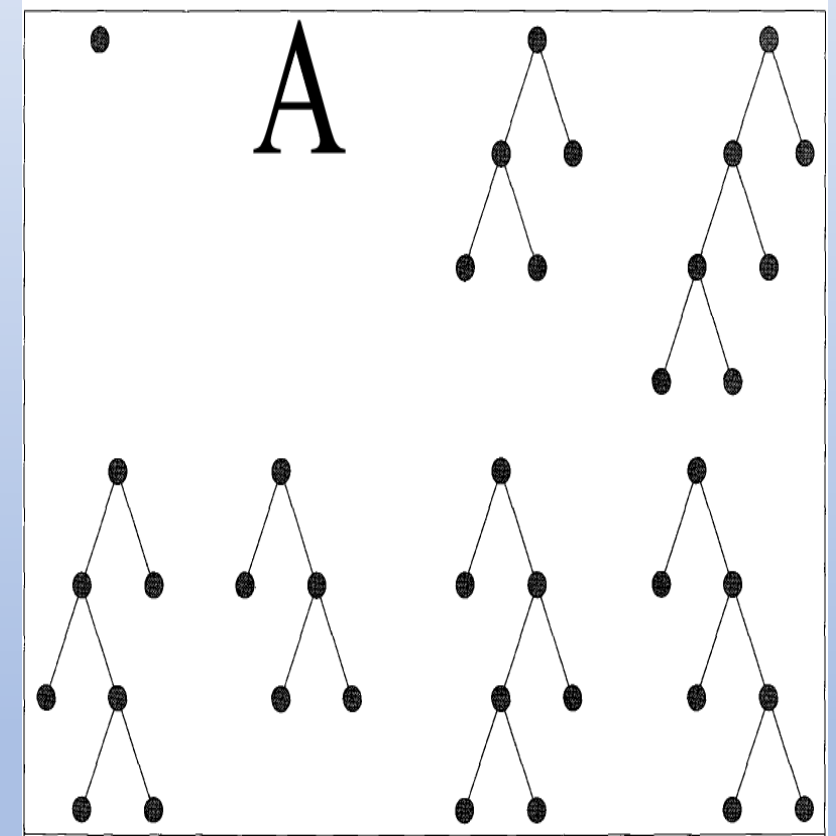
Depth	Nodes	Time	Memory
2	1100	.11 seconds	1 megabyte
4	111,100	11 seconds	106 megabytes
6	$10^7$	19 minutes	10 gigabytes
8	$10^9$	31 hours	1 terabytes
10	$10^{11}$	129 days	101 terabytes
12	$10^{13}$	35 years	10 petabytes
14	$10^{15}$	3,523 years	1 exabyte

**Figure 3.11** Time and memory requirements for breadth-first search. The numbers shown assume branching factor  $b = 10$ ; 10,000 nodes/second; 1000 bytes/node.

Memory requirement is a bigger problem than execution time

# Time and Space Complexity of DFS

- Always expand one of the node at the deepest level of the tree
- The search go back and expand nodes at shallower level when search hits at the dead end.
- Modest memory requirement  $O(bm)$
- Time complexity  $O(b^m)$ ,  $m$  is the maximum depth.







# Advantages of BFS

## Advantages of BFS

- BFS will not get trapped exploring a blind alley.
- It is complete. If there is a solution, then BFS is guaranteed to find it.

## Advantages of DFS

- Requires less memory since only the nodes on the current path are stored.
- Depth first search may find a solution without examining much of the search space at all.

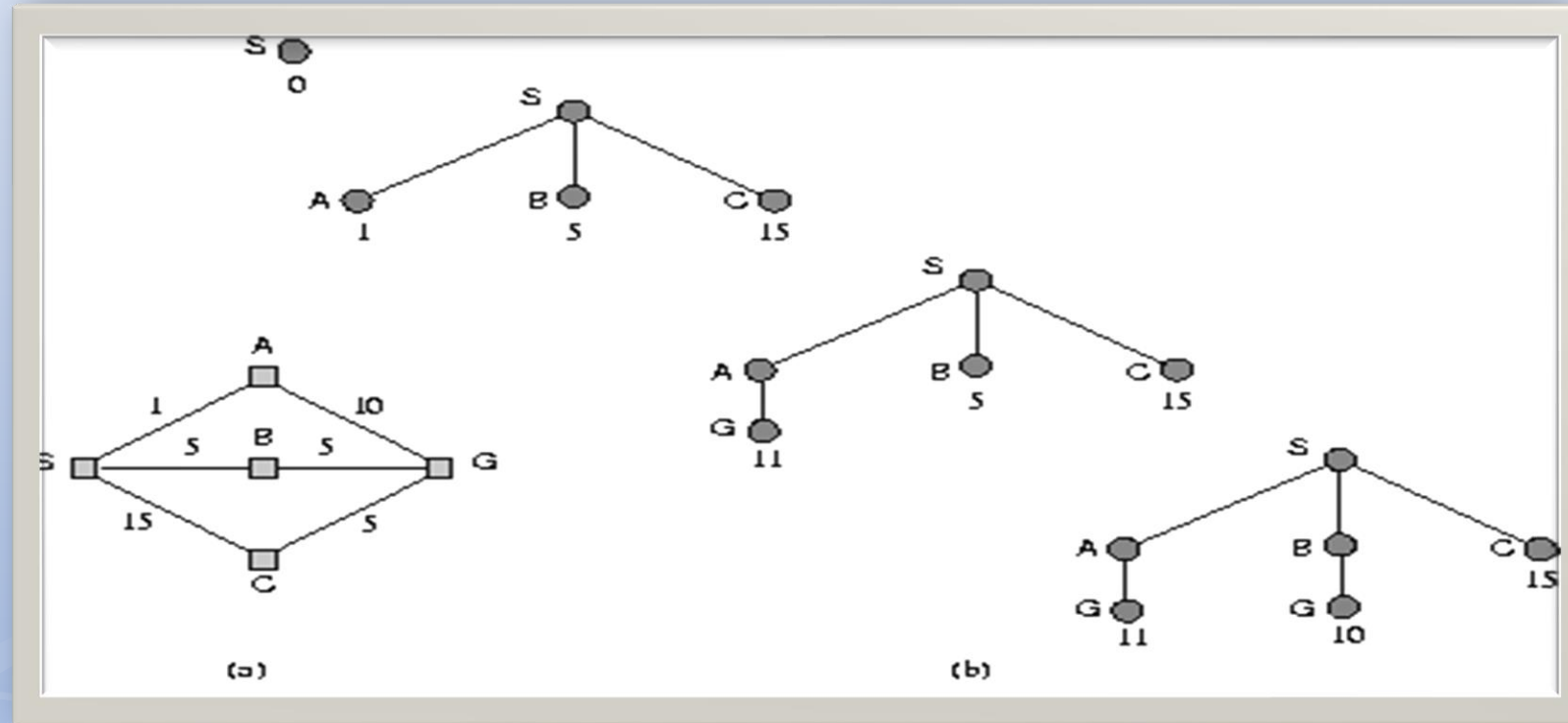
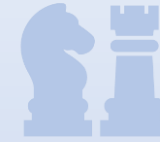
# Uniform Cost Search



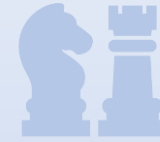
- BFS find the shallowest goal state.
- Goal may not be the least cost solution for a general path cost function.
- Uniform Cost Search is a modified version of BFS, always expand the lowest cost node on the fringe
- Guarantees to find out cheapest solution.
- The path cost should be nondecreasing.



# Uniform Cost Search



# Depth Limited Search



- Depth limited search avoid the pitfalls of DFS by imposing a cut-off on the maximum depth of a path.
- Is complete but not optimal
- If we choose depth limit too small, then is not even complete.
- The time and space complexity is similar to DFS
- Space complexity is  $O(bl)$ , where  $l$  is the depth limit.
- Time complexity is  $O(b^l)$

# Iterative Deepening



- Introduced by Korf , Stickel Tyson 1985
- Utilize the linear memory requirements of depth-first search and ensure to find out goal node at minimal depth.
- Successive depth first searches are conducted.
- Each depth bound increase by 1.
- The number of nodes expanded is not more than DFS.



# Iterative Deepening

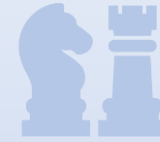
IterativeDeepening(T,S,G)

For  $l=0$  to infinity

DepthlimitedSearch(T,S,G,l)

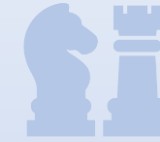
- Overhead expansion is not large
- It search only twice of as long as complete BFS
- Time complexity is still  $O(b^d)$
- Space complexity is  $O(bd)$

# Bidirectional Search



- Simultaneously search from the initial state  $S$  and backward from the goal
- It stops when two search meets at the middle.
- The solution will be found in  $O\left(2 * b^{\frac{d}{2}}\right) = O\left(b^{\frac{d}{2}}\right)$
- Applicable when all operators are reversible.

# Comparing Search Strategies



Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Time	$b^d$	$b^d$	$b^m$	$b^l$	$b^d$	$b^{d/2}$
Space	$b^d$	$b^d$	$bm$	$bl$	$bd$	$b^{d/2}$
Optimal?	Yes	Yes	No	No	Yes	Yes
Complete?	Yes	Yes	No	Yes, if $l > d$	Yes	Yes





# Thank You

